# Next-Generation High-Performance Biobased Naphthalate-Modified PET for Sustainable Food Packaging Applications

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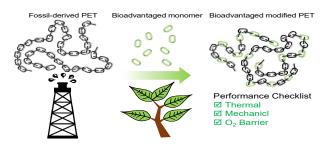
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### Abstract

Here we report a series of novel poly(ethylene terephthalate) (PET) copolymers with improved properties through the incorporation of bioadvantaged dimethyl 2,7naphthalene dicarboxylate (2,7-N) as a comonomer. PET is amongst the most commonly used engineering thermoplastics, ubiquitous in the food packaging industry. However, its application is limited by poor thermal (low  $T_g$ ) and oxygen barrier performance. A series of poly(ethylene terephthalate-stat-2,7-naphthalate) copolymers were synthesized from ethylene glycol (EG), terephthalic acid (TPA), and 2,7-N via a standard two-step melt polycondensation reaction. The 2,7-N significantly improved the thermal, mechanical, and barrier properties. The glass transition temperature  $(T_g >$ 75.4 °C) and thermal stability ( $T_{d,5\%} > 405.1$  °C) of the copolymers increase monotonically with 2,7-N content, exceeding those of PET ( $T_g=69.7$  °C,  $T_{d,5\%}=401.4$ °C). Moreover, the mechanical properties and the crystallization behaviors are tunable through the 2,7-N loading. Composition-optimized copolymers showed an increase of 70% and 200% in elongation at break and tensile strength, respectively. In addition, the oxygen permeability value of the copolymers containing 20% 2,7-N loading fell to  $P_{\rm O_2}$ = 0.0073 barrer, a 30% improvement over that of PET. These results illustrate that the novel substitution patterns offered by biobased chemicals can translate to performance advantages in packaging materials. Finally, the fundamental structure-property relationships connecting the bioadvantaged chemicals as the comonomers to the product performance were constructed as a guide for value-added renewable polymers in the future.

# Introduction

Polyethylene terephthalate (PET) is one of the most-consumed thermoplastics as well as single-use plastics (SUPs) in the world for numerous applications, representing approximately 18% of the global plastic market with an annual production of around 50 million metric tons. It is a part of daily life due to its low cost, durability, and plethora of other desirable

properties.<sup>2</sup> PET has good thermal and mechanical properties, as well as excellent chemical resistance to most solvents compared to other plastics. Owing to its performance, it is reported to have been used to make fibers, sheets, and films, and, more specifically, it is used in food and beverage packaging, electronics and communication devices, automotive parts, lighting products, sports goods, and textiles, healthcare applications, etc.<sup>3,4</sup> Nonetheless, there are some shortcomings: for example, PET cannot withstand hot water cleaning and pasteurization due to its low glass transition temperature  $(T_g)$ , which increases the risk for bacteria and microorganisms growth during reuse. Moreover, while the barrier performance of PET is acceptable for  $H_2O$  and  $CO_2$ , it has poor  $O_2$  barrier making it poorly suited to many oxygen-sensitive products such as most liquors.<sup>5,6</sup>

These limitations have motivated the development of multiple pathways to improve PET performance to meet the requirements for more stringent applications. For instance, the introduction of fillers/fibers can improve the mechanical properties, although not without tradeoffs.<sup>7,8</sup> For example, often the fillers require compatibilizers to improve interfacial adhesion, adding significant complexity and cost.<sup>9–11</sup> Moreover, fillers/fibers are problematic at the end-of-life by acting as a contaminants in recycling stream.

Alternatively, the PET resin itself can be improved upon through the partial or complete substitution of the terephthalate unit with analogous rigid segments. Comonomers like isophthalic acid (IPA), 1,4-cyclohexanedimethanol (CHDM), and diethylene glycol (DEG) are used frequently to optimize the properties for particular applications by depressing the melt temperature (e.g., for ease-of-processing) or by altering the crystallinity (e.g., for optical clarity). <sup>12–14</sup> Given the deterioration in some material properties, like thermal and barrier, and the petrochemical nature of these comonomers that has been questioned due to environmental concerns such as greenhouse gas emission and non-renewable resource consumption, there is an opportunity to discover new biobased comonomers that address these issues.

Amongst the highest-performance known terephthalate alternatives is 2,6-naphthalene dicarboxylate (2,6-N), which has received both academic and industrial attention as PET

copolymers as well as in poly(ethylene 2,6-naphthalate) (26PEN) homopolymers. <sup>15–18</sup> The rigidity and stability of the 2,6-N fused aromatic yields polymers superior to PET in most respects including thermal, mechanical, and barrier properties. The high service temperature and barrier performance are attractive for hot-filling and liquor packaging applications; however, cost, limited availability, and environmental considerations narrow the use of 2,6-N to very high-value, low-volume applications such as high-end packaging, films, and fibers.

Given the dramatic price volatility in crude oil and concerns over the sustainability of chemical manufacturing, there is an earnest search for renewable building blocks that can compete with the petroleum-based comonomers mentioned above. <sup>19–27</sup> Inspired by these concerns and the potential utility of the naphthalate polyesters, we recently reported a family of biomass-derived poly(ethylene naphthalate) homopolymers as sustainable and potentially lower-cost 26PEN alternatives. <sup>28</sup> Amongst these, 2,7-naphthalene dicarboxylate (2,7-N) was found to be especially promising. Derived from malic acid, 2,7-N is structurally analogous to 2,6-N in the same manner as meta-substituted isophthalate to para-substituted terephthalate. We found that like 26PEN, poly(ethylene 2,7-naphthalate) (27PEN) exhibits exceptional thermal and barrier performance; however, these homopolymers were brittle due to their sluggish crystallization kinetics. Thus while 27PEN has many appealing properties, its prospects for use in applications where resilience to even modest mechanical distress appear to be limited without remediation.

The production of 2,6-N originates with the combination of m-xylene and butadiene, and goes through a multistep process including alkylation, cyclization, (de)hydrogenation, oxidation, etc. <sup>29</sup> Butadiene comes from the naphtha feedstock, which has become increasingly scarce as the refining complex has shifted to natural gas processing. It is only manufactured at select locations globally and is subject to massive price fluctuations due to crude oil. Moreover, its life cycle impacts include CO<sub>2</sub> emissions of 2.518 kg per kg and energy consumption of 65 MJ per kg. <sup>30</sup> Conversely, bio-derived 2,7-N is produced primarily from malic acid, which is obtained readily from many fruit extracts, while industrial methods

have focused on metabolically engineering microbial strains to generate sufficient volumes.<sup>31</sup> In addition, malic acid is already commercially available as a food additive for < \$1 per kg in the market, which has both potentially economically and environmentally competitive compared to 2,6-N.

In a study examining the structure-property relationships in a series of nylon-6,6 copolymers, Abdolmohammadi and Gansebom argued that the future of sustainable materials may be more accessible through a more gradual bootstrapping process. <sup>32</sup> These authors posited the view that novel "bioadvantaged" chemicals may find better value as additives that differentiate the properties of legacy materials whose support infrastructure is already in place. With respect to semicrystalline polymers like nylon-6,6, they found that up to 20 mol % of adipic acid could be replaced without severe disruptions in the nylon crystallinity that serves as the foundation for properties in that materials system. The biobased counit (trans-3-hexene dioate) was effectively partitioned to the amorphous phase, whose properties could therefore be tailored somewhat independently of the crystal phase.

In this manuscript, we hypothesized that this concept, in which the biobased counit would not significantly affect the crystallization behaviors up to a certain composition threshold and allows for the performance to be tailored, might be well-applied to realizing the potential of 2,7-N. While the sluggish 27PEN crystallization rate leads to fragile materials, its superior thermal and barrier properties could be exploited through amorphous-phase modification in PET copolymers. Success in this regard could offer a pathway for commercial adoption of 2,7-N, its role as a valorizing PET additive mitigating the costly barrier-to-entry associated with the immature biochemical industry. We therefore present structure-function relationships between comonomer loading and copolymer properties in a series of poly(ethylene terephthalate-stat-2,7-naphthalate) copolymers. These were produced using a classic two-step melt polycondensation reaction (Scheme 1) with molecular weights similar to those of industrial-grade resins. We found that 2,7-N substitution rates near 20 mol % impart optimal improvements in thermal, mechanical, and barrier properties. These copolymers could

be scalable alternatives to 26PEN/PET copolymers, providing a pathway to biochemical adoption through enabling high-value materials for demanding applications while managing product expense.

Scheme 1: Step-growth polycondensation of naphthalate-based copolymers via a two-step polymerization

Table 1: Compositions and characteristics of PET and naphthalate-based copolymers

Sample Code <sup>a</sup>	Temp./Time <sup>b</sup> (°C / hour)	IV ° (dL/g)	Mn <sup>d</sup> (kDa)	Mw <sup>e</sup> (kDa)	$D^{ m f}$	[ET]/[EN] in polymer	$L_{nET}{}^{ m h}$	$L_{nEN}{}^{ m h}$	DR h
PET	240/8	0.73	16.3	27.2	1.67	100/0			
27PEN5	240/6	0.83	19.8	36.3	1.83	95.2/4.8	16.60	1.11	0.96
27PEN10	240/6	0.86	20.6	39.6	1.92	90.2/9.8	9.98	1.15	0.97
27PEN20	240/8	0.75	17.4	31.8	1.83	78.6/21.4	5.20	1.30	0.96
27PEN100 <sup>g</sup>	240/3	0.48	11.9	42.9	3.61	0/100			

aSample code: 27PENX, x = mol% of 2,7-N unit. bThe esterification/transesterification reaction was carried out at 220 °C for 5h and bis-hydroxy ester monomer conversion of each precursor is ≥ 99%, which was determined by gas chromatography—mass spectrometry. Intrinsic viscosity was measured in phenol/1,1,2,2- tetrachloroethane (60/40, v/v) solution by using an Ubbelohde viscometer at 25 °C. dNumber-average molecular weight. Weight-average molecular weight by GPC in 1,1,1,3,3,3-hexafluoro-2-propanol solution with Poly(methyl methacrylate) (PMMA) standards. Poly(ethylene 2,7-naphthalate). Ln is the average number of M1 monomer units that follow each other consecutively in a sequence uninterrupted by M2 units but bounded on each end of the sequence by M2 units. DR is a measure of the adjacency of monomers and their statistical distribution of the polymer sequence.

### Results and discussion

We prepared a series of poly(ethylene terephthalate-stat-2,7-naphthalate) (27PENX) copolymers as summarized in Table 1, where X denotes the molar 2,7-N composition. Additionally, for comparison purposes we also considered an analogous series of poly(ethylene terephthalate-stat-isophthalate) (PEIX) as described in Table S1 with X as the isophthalate fraction. PEIX and 27PENX are similar in that the meta-substituted aryl content is asymmetric with respect to the chain axis in both systems; they differ due to the two fused rings of the naphthalate vs. the single ring of the isophthalate. All polymers were produced using the two stage polymerization method and then were first characterized using gel permeation chromatography (GPC) and intrinsic viscosity (IV) to determine molecular weight distribution. The high D (3.61) of 27PEN100 is likely due to mass transport limitations, which resulted from the high viscosity during polymerization compared to that of PET and 27PEN copolymers, as mentioned in our previous study. The measured IV values of the polymers are consistent with the GPC results, and all polymers were within the range typical for industrially produced PET.

Beyond molecular weight, chain architecture is a critical factor in properties of copolymers. It is well known that comonomers can have dramatically different reactivity ratios leading to heterogeneous monomer sequence distributions (MSDs). To determine the MSD,

<sup>1</sup>H NMR was used to obtain information about the degree of randomness (DR), a useful heuristic in the description of copolymer microstructure. The number-average sequence lengths Ln of the ethylene terephthalate (ET) and ethylene naphthalate (EN), as well as DR, were estimated for each 27PENX copolymer by using the following equations:<sup>33</sup>

$$L_{n ET} = 1 + \frac{2f_{TT}}{f_{NT/TN}}, \quad L_{n EN} = 1 + \frac{2f_{NN}}{f_{NT/TN}}$$
 (1)

$$DR = \frac{1}{L_{n,ET}} + \frac{1}{L_{n,EN}} \tag{2}$$

where the mole fraction of each dyad sequence including  $f_{NN}$ ,  $f_{NT/TN}$ , and  $f_{TT}$  was calculated from the integral intensities of each corresponding peak of, NN, NT/TN, and TT, respectively. DR was calculated from  $L_{n ET}$  and  $L_{n EN}$  values of the ET and EN units.

When the DR value is close to 1, the MSD is random, whereas the DR values of a block copolymer and alternating copolymer are 0 and 2, respectively.  $^{34-36}$   $^{1}$ H NMR spectra of the 27PEN copolymers and peak assignments appear in Figure 1 and S1; the molar composition of corresponding ethylene terephthalate (ET) and ethylene naphthalate (EN) repeating units in 27PEN copolymers were estimated from these data. For the  $^{1}$ H NMR spectrum of 27PEN20, chemical shifts of the peak a ( $\delta$ =8.14 ppm) corresponds to the protons (-CH) of the single aromatic ring, whereas the peak c ( $\delta$ =8.77 ppm), peak d ( $\delta$ =8.16 ppm), and peak e ( $\delta$ =7.94 ppm) represent protons (-CH) of the naphthalene ring. All 27PEN copolymers show the expected peak area which is close to the feed content of TPA and 2,7-N. The multiple peaks at 4.75-4.95 ppm are assigned to the methylene units (-CH<sub>2</sub>-) within the ET and EN repeat units. In particular, three methylene peaks in the 27PEN20 spectrum are attributed to the four possible dyads (NN, NT/TN, TT), which can be used to estimate DR. The calculated DR values of 27PEN copolymers are close to 1, which indicated the ET and EN repeating units were randomly distributed in the copolymers.

The FTIR spectra of PET and naphthalate-based copolymers are shown in Figure 2.

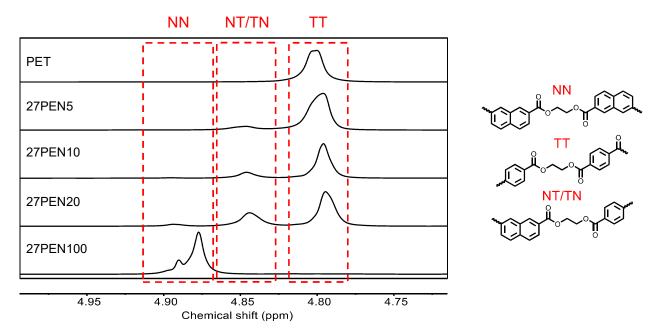


Figure 1: <sup>1</sup>H NMR spectra of the dyad fractions of NN, NT/TN, and TT of PET and naphthalate-based copolymers

The strong peak at 1713 cm<sup>-1</sup> is attributed to the stretching vibration of the carbonyl group (C=O) for both PET and 27PEN. The carbonyl (C-O) stretching vibration of PET appears near 1240 cm<sup>-1</sup>, while that of 27PEN shifts to 1260 cm<sup>-1</sup>. In particular, the peak intensity of the naphthalene ring vibration is observed at 1215 and 1180 cm<sup>-1</sup> for 27PEN and the copolymers. The increase in the peak intensity of these two peaks is in accordance with the increase in the molar content of 27PEN, and there is no significant peak showing in this region for PET.

Having established the quantitative and uniform distribution of 2,7-N units in the copolymers, we next examine the thermomechanical properties as a function of composition. As a first consideration, thermal stability has to be understood (see Figure 3 and Table 4). The TGA results indicate that the thermal stability of 27PEN copolymers rise gradually with increasing 2,7-N loading in the materials, which produce slightly more char residue and show slightly higher  $T_{d,max}$  and  $T_{d,5\%}$  values. In contrast, the thermal stability of PEI copolymers showed an opposite trend of  $T_{d,max}$  and  $T_{d,5\%}$  (see Figure S3) indicating that the thermal stability of the meta-substitution polymer (PEI) was lower than that of para-substitution

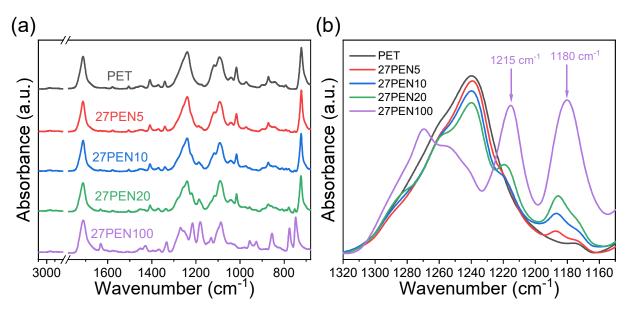


Figure 2: (a) ATR-FTIR spectra of PET and naphthalate-based copolymers, and (b) the superimposed magnified spectra with the wavenumber of  $1000-1400 \text{ cm}^{-1}$ 

polymer (PET). Therefore, the enhancement of the thermal stability was attributed to the fused aromatic rings instead of the meta-substitution orientation. Unsurprisingly, the higher % mass fraction of aromatic content in the polymer chains, the more stable the polymer will be and the higher the char residue will produce.

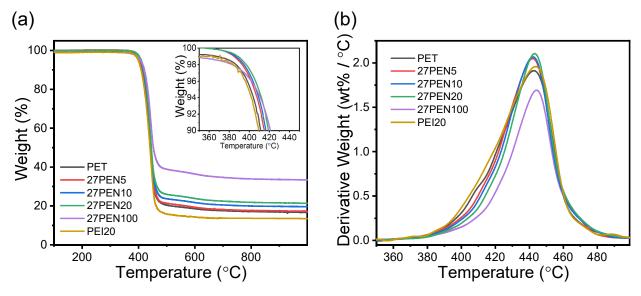


Figure 3: (a) TGA thermograms and (b) DTG curve of PET and naphthalate-based copolymers with heating rate of 10 °C min<sup>-1</sup>.

Since the thermal and mechanical properties are significantly dependent on the level of

crystallinity and crystallization rate, DSC and WAXS were used to evaluate the effects of 2,7-N loading on the crystallization behaviors. <sup>37-40</sup> The WAXS/SAXS patterns of 27PEN copolymers are illustrated in Figure 4 and information regarding crystallinity is summarized in Table 2. The samples before annealing are highly amorphous, showing no WAXS diffraction peaks except 27PEN100, which has been discussed in our previous study. <sup>28</sup> After annealing, the 27PENX diffraction peaks match those of PET homopolymer, indicating that 27PENX crystals are comprised solely of PET sequences. At modest substitution rates, sequences containing 2,7-N units are too irregular to crystallize and are relegated to the amorphous phase. Furthermore, the degree of crystallinity of the copolymers decreases gradually as the content of 2,7-N increases. In the case of 27PEN copolymers, 2,7-N acts as an impurity from the viewpoint of crystallization, which disrupts the orderly fold pattern of the crystal. A similar trend is observed in PEI copolymer (see Figure S4). The rising content of IPA in the polymer chains clarifies the detrimental effect of crystallization behavior by the comonomer units.

Moreover, to study the effect of 2,7-N in PET chains on the lamellar periodicity of the copolymers, SAXS was carried out (see Figure 4) and the results are shown in Table 2. The SAXS patterns exhibit a clear peak due to the periodic lamellar stacks, and the lamellar thickness correlates with peak position. The peak position varies monotonically as a function of 2,7-N content, as it tends to decrease as the content of fused aromatic rings rises. This implies that the long period (L, Table 2) increases along with 2,7-N loading.  $^{41,42}$  The amorphous lamellar thickness ( $l_a$ ) (Equation 8) also increases along with 2,7-N loading, which leads to the reduction of overall crystallinity in 27PEN copolymers and is in line with the WAXS results. However, the crystal lamellar thickness ( $l_c$ ) (Equation 8) shows an increasing trend along with 2,7-N loading as well, which contradicts the comonomer unit exclusion hypothesis. Hence, an alternative explanation is required. Based on the model proposed by previous studies, a one-dimensional correlation function, including long period (L) as well as the crystal/amorphous lamellar thickness, can be obtained by using the inverse-cosine-

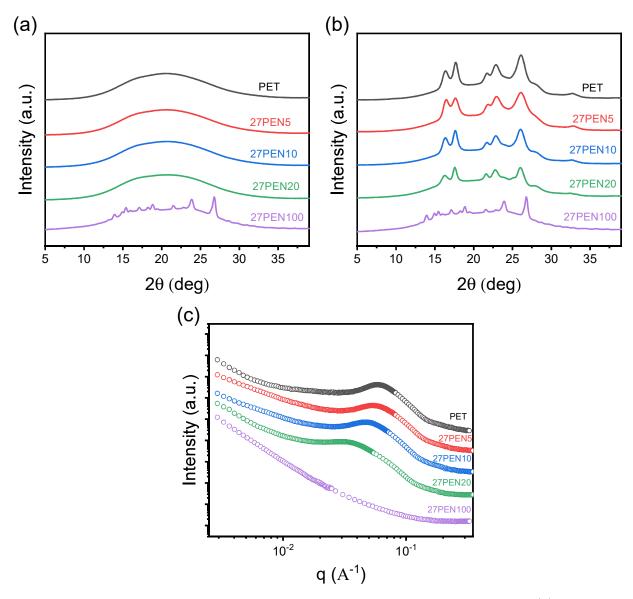


Figure 4: WAXS patterns of PET and naphthalate-based copolymers: (a) tensile bar quenched from 270 °C; (b) after annealing at 175 °C for 6 h; (c) SAXS spectra of the samples after annealing at 175 °C for 6 h

Fourier-transform of the SAXS profile.  $^{43,44}$  The results imply that the crystal/amorphous lamellar thickness needs to be estimated correctly with the relative volume fraction of lamellae rather than with the bulk volume crystallinity. The results in these studies show that  $l_c$  decreases as the comonomer loading increases, in accord with the comonomer exclusion hypothesis.

The impact of 2,7-N on crystallization dynamics was also investigated through a series of

Table 2: Crystallinity values of PET and naphthalate-based copolymers after annealing at 175 °C for 6 h

Sample Code a			WAXS & SAXS		
Sample Code <sup>a</sup>	X <sub>c</sub> (%) <sup>b</sup>	q <sub>max</sub> (Å)	L (Å) c	$l_c$ (Å) <sup>d</sup>	$l_a$ (Å) $^e$
PET	56.5	0.058	108.3	61.2	47.1
27PEN5	52.5	0.053	118.6	62.3	56.3
27PEN10	47.5	0.047	133.7	63.5	70.2
27PEN20	35.0	0.029	216.7	75.8	140.9
27PEN100	18.3				

<sup>a</sup>Sample Code: 27PENX, x = mol% of 2,7-N unit. <sup>b</sup>Degree of crystallinity calculated from the WAXS pattern. <sup>c</sup>Lamellar thickness. <sup>d</sup>Crystal lamellar thickness. <sup>e</sup>Amorphous lamellar thickness.

isothermal DSC experiments as illustrated in Figure S5 and S6. Following Avrami kinetics, the crystallized fraction versus time follows a sigmoidal curve. The crystallization rate constant (k) increases with temperature and decreases with 2,7-N loading. The increase with temperature is due to accelerated chain mobility. The downward trend is due to the crystal disruption by 2,7-N and the higher energy requirement for chain rearrangement, which is in accordance with the WAXS results. The reciprocal crystallization half-time  $(t_{1/2}^{-1})$  versus temperature is more intuitive to describe the dependence of overall crystallization rate vs. temperature (Figure S7). The  $t_{1/2}^{-1}$  values of 27PEN copolymers except 27PEN20 increase with temperature (faster crystallization), whereas 27PEN20 shows a downward trend. This observation can be understood through consideration of two competing factors: first, crystal nuclei are easier to form as the crystallization temperature decreases, which leads to crystallization rate acceleration. Second, the polymer chain diffusion slows down as T approaches  $T_g$ . Therefore, the crystallization rate increases as temperature is reduced when near  $T_m$ due to the increased thermodynamic driving force, but passes through a maximum rate due to attenuation of the chain mobility.  $^{45}$  The temperature conditions of PET and 27PEN copolymers except 27PEN20 are dominated by the second term, whereas that of 27PEN20 is dominated by the first term.

The mechanism of nucleation and the morphology of crystal growth is suggested by the Avrami exponent n, which varies from 0.5 to 4 for most semicrystalline polymers. 46 As

Table 3: Parameters of isothermal crystallization calculated by Avrami equation

Sample Code	T <sub>c</sub> <sup>a</sup> (°C)	n <sup>a</sup>	k <sup>a</sup>	<i>t</i> <sub>1/2</sub> <sup>a</sup> (s)
	110	2.67	5.236*10-6	82.9
PET	113	2.51	1.988*10-5	64.5
1 L1	118	2.42	1.522*10-4	32.5
	120	2.40	2.850*10-4	25.8
	125	2.23	8.994*10-6	155.4
27PEN5	128	2.14	2.219*10-5	126.0
ZIPENS	130	2.21	3.800*10-5	84.7
	135	2.1	1.844*10-4	50.4
	130	2.21	6.777*10-6	184.9
27PEN10	133	2.19	1.944*10-5	119.8
Z/FENIU	138	2.09	7.124*10-5	80.9
	140	2.08	1.091*10-4	67.4
	165	2.16	6.680*10-7	609.8
27PEN20	170	2.24	3.404*10-7	655.3
Z/FENZU	173	2.23	2.689*10-7	749.9
	175	2.28	1.584*10-7	817.9

 $<sup>{}^{</sup>a}T_{c}$ : the isothermal crystallization temperature, k: the crystallization rate constant, n: the Avrami exponent,  $t_{1/2}$ : the crystallization half-time

shown in Table 3, an average value of n=2.5 for PET is obtained. Since PET is a pure homopolymer without any nucleating agent, the nucleation mechanism is a homogeneous nucleation followed by three-dimensional spherulite growth, in accordance with Avrami exponent value. In contrast, the values for the copolymers are close to 2.1. This implies that 2,7-N units might act as nucleating agents, since nucleation is often very sensitive to "impurities" in the system. Therefore, the crystal geometry growth of 27PEN copolymers shifts to two-dimensional axialites. As 2,7-N loading in the copolymers increases further, the development of three-dimensional order becomes more difficult and will be replaced by two-dimension axialite. Nonetheless, since there are many other factors that would affect the nucleation of the polymer such as the free energy changes on crystallization, the lamellar thickness, and the interfacial energy, etc, further study is required to understand the nucleation mechanism of 27PEN copolymers in future works.

The melting point  $T_m$  (see Figure 5 and Table 4) passes through a maximum in 27PEN5 and decreases thereafter, illustrating the interplay of competing enthalpic and entropic ef-

fects. At sparing 2,7-N composition, the extent of crystallinity is not yet significantly impacted; from the perspective of a crystalline PET sequence, the enthalpic penalty for melting is increased due to the thermodynamically incompatible 2,7-N units in the amorphous phase. However, at a higher 2,7-N fraction, the lamellar thickness is suppressed due to shorter PET sequences. This increases the crystallite surface area (and surface energy), depressing the melting point as anticipated by the Thompson-Gibbs equation.<sup>46</sup>

Likewise, the melt recrystallization temperature  $T_c$  also passes through a maximum with respect to 2,7-N loading. Based on the Avrami analysis above, the comonomer unit (2,7-N) might act as a nucleation site. This tends to increase  $T_c$  as observed in 27PEN5. As the 2,7-N composition increases, however, its disruption to the regularity of crystallizable PET sequences overwhelms the nucleation effect and depresses  $T_c$ . In the case of cold crystallization, the  $T_{cc}$  trend increases along with 2,7-N loading. This could be attributed to the energy barriers for the chain motion increase with the increasing amount of fused aromatic rings, requiring greater thermal energy for chain rearrangement. A similar trend is observed in thermal behaviors of PEI copolymers (see Figure S8 and Table S2), which further demonstrates that both the comonomer units (2,7-N and IPA) can cause the disruption effect on PET crystallization ability.

In summary, the dramatic difference in the thermal properties shown between 27PEN20 and other composition copolymers can be attributed to the disruption effect of the comonomer on PET crystallization ability. When 2,7-N loading is below 10%, the crystallization ability is not yet significantly affected. However, the crystallization ability of 27PEN20 is close to the boundary that crystal formation will become critically hindered and cause the polymer to be completely amorphous. This observation is in agreement with a study exploring custom property enhancements for polyamides by bioenabled platform monomers. <sup>47</sup>

Turning to the amorphous phase, where the vast majority of the 2,7-N content evidently resides, all 27PEN copolymers show one unique  $T_g$  value via DSC, indicating a homogeneous amorphous phase.  $T_g$  increases with 2,7-N content. 27PEN20 shows a  $T_g$  value more than

20 °C higher compared to PET, reaching  $T_g = 120$  °C for 27PEN100. Comparison with PEI analogs show this effect is attributed to the increased chain stiffness from the fused aromatic rings and not the meta-substitution pattern. PEI20 has a  $T_g$  about 10 °C lower than PET, dropping to 51.3 °C for PEI100 homopolymer (Figure S8, Table S2). In conclusion, the thermal and crystallization behaviors of 27PEN copolymers can be tuned by adjusting 2,7-N content to meet the desired performance for specific application.

In addition, to reach the target of saving cost and time as well as to predict the performance of the materials, using a model before doing experiment would be cost-effective and time-saving. The trend of  $T_g$  versus 27PEN loading shows a monotonic dependency, which can be fitted to semiempirical equation, Gordon-Taylor equation (equation 3), as shown in Figure S13. The higher 2,7-N loading copolymer can be estimated by using the following equation:

$$T_{g, 27PENcopolymer} = \frac{k_{GT}w_1T_{g,1} + (1 - w_1)T_{g,2}}{k_{GT}w_1 + (1 - w_1)}$$
(3)

where  $T_{g,1}$  and  $T_{g,2}$  are the glass transition temperature of 27PEN and PET homopolymer, respectively.  $w_1$  corresponds to the weight fraction of the 27PEN units in the copolymer; and  $k_{GT}$  is the Gordon-Taylor parameter, which is an adjustable fitting parameter. A highly correlated fit was obtained with  $k_{GT} = 2$ , indicating a behavior that is typical of random copolymers.

Table 4: Thermal transition properties of PET and naphthalate-based copolymers

	DSC				WAXS		TGA		
Sample Code <sup>a</sup>	T <sub>g</sub> <sup>b</sup>	T <sub>cc</sub> <sup>b</sup>	T <sub>c</sub> <sup>b</sup>	T <sub>m</sub> <sup>b</sup>	$X_{\rm c} (\%)^{\rm b}$	$X_{\rm c} \left(\%\right)^{\rm c}$	T <sub>d,5%</sub> d	T <sub>d,max</sub> d	Residue (wt%) d
PET	69.7	124.3	179.7	237.8	33.0	56.5	401.4	442.7	16.7
27PEN5	75.4	138.7	193.3	243.2	25.3	55.6	405.1	443.1	17.4
27PEN10	82.3	146.6	181.3	228.2	21.6	47.5	406.8	443.2	19.6
27PEN20	90.1	163.1	139.3	207.1	3.2	35.0	409.4	443.5	21.3
27PEN100	120.1	N.D.	N.D. <sup>e</sup>	341.0	N.A. <sup>f</sup>	18.3	407.3	444.3	33.4

aSample code: 27PENX, x = mol% of 2,7-N repeat unit. bGlass transition  $(T_g)$ , crystallization  $(T_c)$ , cold crystallization  $(T_{cc})$  and melting  $(T_m)$  temperatures, degree of crystallinity  $(X_c)$  during heating cycle. bGegree of crystallinity  $(X_c)$  after annealing at 175 °C for 6 h.  $^4T_{d,5\%}$ : decomposition temperatures at which the weight loss reached 5% of its initial weight.  $T_{d,max}$ : the temperature at the maximum rate of decomposition. The residual mass at 1000 °C. Not detected by DSC. Not available.

Measuring and understanding the mechanical properties is critical for processing control

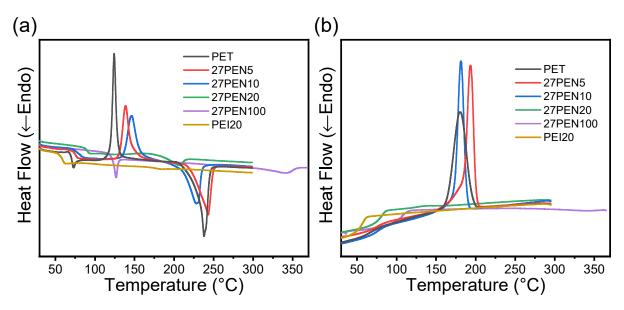


Figure 5: DSC thermograms of quenched PET and naphthalate-based copolymers at scan rate of 10 °C min<sup>-1</sup>: (a) heating and (b) cooling

as well as product development. 48 Therefore, tensile testing was used to assess the effect of 2,7-N loading in the mechanical aspect of the copolymer, as illustrated in Figure S10. It should be mentioned that the mechanical properties, especially elongation at break, can be affected by the extent of crystallinity inside PET. A small amount of crystal embedded inside the sample might result in the fracture before reaching maximum elongation at break. In order to measure the true flexibility of the materials, completely amorphous tensile samples of PET and 27PEN copolymers were prepared via injection molding at 270 °C into a 40 °C mold, which was confirmed by WAXS. As shown in Table 5, 27PEN100 shows brittle performance compared to PET, which has been discussed in our previous study. 28 However, the copolymers show ductile deformation with similar yield, plastic deformation and necking behaviors as compared to PET. Notably, PET fractures after necking with only slight strain hardening, whereas 27PEN copolymers display obvious strain hardening before breaking. Strain hardening is observed as a strengthening of a material during large strain deformation, which is attributed to the fact that the polymer chains tend to orient and align in the direction of the load and results in the crystallization of lamellar crystals perpendicular to the strain axis. The tensile strength of strain hardening shows an increase of almost 200% from 40

MPa to 80 MPa as 2,7-N loading increases to 10%, and is followed by a decrease to 70 MPa with 20% loading thereafter. This observation can be attributed to two effects: first, the increase in the rigidity of the polymer chains due to the fused aromatic rings segment, which enables the materials to withstand higher load without being damaged. Second, the suppression effect of 2,7-N will disrupt the strain-induced crystallization, which is affirmed by the WAXS, SAXS and DSC results. At low loading (<10%) of 2,7-N, the first term is predominant while the crystallization ability is still sufficiently high. As 2,7-N loading keeps increasing, the crystallization ability of the copolymer is dramatically affected and overwhelms the first term eventually. Based on the same effects mentioned above, a similar trend is also shown in elongation at break. The elongation at break shows an increase of 70% more than that of PET as 2,7-N loading increases to 10%; however, as 2,7-N loading keeps rising up to 20%, it only shows an improvement of 40% increase compared to that of PET. All the observations are in agreement with the results of PEI copolymer reported in a previous study as well as the experimental results in this work. <sup>13</sup>

Table 5: Mechanical and barrier properties of the homo- and copolymers

Sample Code <sup>a</sup>	Young's modulus (Mpa)	Yield Strength (Mpa)	Elongation at break (%)	Impact Strength (J/m)	O2 permeability (Barrer) <sup>b</sup>
PET	$1026.8 \pm 23.9$	$73.0 \pm 2.4$	$359.4 \pm 20.1$	$12.6 \pm 1.8$	0.0108
27PEN5	$1028 \pm 45.5$	$76.1 \pm 2.4$	$503.9 \pm 46.2$	$13.7\pm0.6$	0.0099
27PEN10	$991.1 \pm 20.5$	$82.9 \pm 5.6$	$611.9 \pm 74.1$	$14.1\pm1.8$	0.0095
27PEN20	$987.3 \pm 19.0$	$77.1 \pm 1.5$	$494.7 \pm 27.8$	$13.1\pm0.6$	0.0073
27PEN100	$756.7 \pm 76.9$	$44.9\pm13.0$	$6.5\pm1.8$	$12.5\pm1.2$	0.0022
PEI10	$1049.7 \pm 12.2$	$78.2 \pm 2.2$	$98.7 \pm 18.9$	$12.4 \pm 0.4$	N.A. <sup>c</sup>
PEI20	$1162.3 \pm 95.2$	$78.0 \pm 3.8$	$9.1\pm2.0$	$11.9 \pm 0.7$	N.A.
PEI100	$144.8 \pm 30.7$	$12.3\pm0.4$	$14.3 \pm 2.7$	$9.1\pm0.3$	N.A.

<sup>a</sup>Sample code: 27PENX/PELX, x = mol% of 2.7-N/IPA repeat unit. <sup>b</sup>1 Barrer =  $3.348*10^{-16}$  mol m m<sup>-2</sup> s<sup>-1</sup> Pa<sup>-1</sup>. <sup>c</sup>Not available.

SEM images of fractured polymer were further analyzed with the aim of providing a direct observation on the material appearance and elucidating the differences in mechanical properties, as presented in Figure S11. PET and 27PENX copolymers exhibited a massive network of cracks across the specimen surface, indicating the ability of these materials to dissipate energy throughout the sample. In contrast, 27PEN100 shows a smooth surface with tiny crystals, which has been discussed in the previous study.<sup>28</sup> Analysis of surface

appearance confirmed that 27PENX copolymers possess similar energy dissipating ability to that of PET.

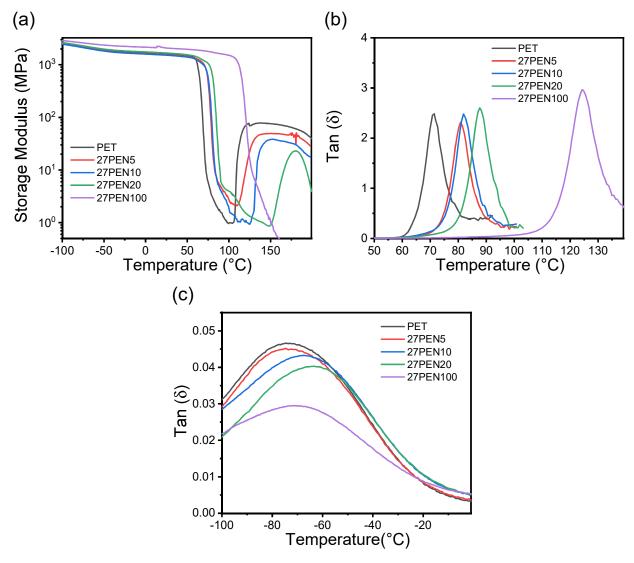


Figure 6: DMA spectra of PET and naphthalate-based copolymers: (a) storage modulus; (b) tan  $(\delta)$   $\alpha$ -relaxation transition; and (c) tan  $(\delta)$   $\gamma$ -relaxation transition

In addition to thermal, crystallization, and mechanical aspects, barrier performance is also critical for making useful single-use packaging equipment. To that end, the effect of PET modification by 2,7-N on the barrier properties must be studied to meet Food and Drug Administration requirements for food packaging. Herein, the  $\gamma$ -relaxation could be expressed by a change in activation energy for either diffusion or permeation which relates to barrier properties; thus, DMA was performed to investigate low-temperature molecular

motions of 27PEN copolymers (see Figure 6c).  $^{49-52}$  As 2,7-N loading in the polymer chain increased,  $T_{\gamma}$  transition increased from -74.2 to -63.4 °C, indicating more energy needed for the copolymer to carry out localized chain motion. Furthermore, it appears that the observed reduction in  $\gamma$ -relaxation peak areas is entirely the result of modifying PET polymer chain with an meta-substitution fused aromatic rings, which restricted sub  $T_g$  molecular motions. The observation for this change can be separated into two effects: first, the incorporation of the restricted mobility naphthalene ring in the polymer chains, which is in accordance with the trend reported in the literature. Second, the meta-substitution structure decreases the chain mobility compared to the para-substitution structure. A similar trend shown in PEI copolymers (see Figure S12) further illustrated that the meta-structure repeating unit could suppress the ring flip motion of the para-structure polymer.

In addition to the  $\gamma$ -transition, the  $\alpha$ -transition and crystallization behaviors of 27PEN copolymers were studied. The peak of  $\alpha$ -transition (denoted as  $T_{\alpha}$  in Figure 6) increases with the increasing amount of 2,7-N. This is attributed to the inhibition of the free movement of the polymer chain in amorphous phase from the embedded fused aromatic rings segment. The  $T_{\alpha}$  value is comparable to the  $T_g$  determined by DSC, which indicates that the copolymer with higher 2,7-N loading possesses higher service temperature. The subsequent increase in storage modulus (related to the elasticity of the material) after  $\alpha$ -transition that reached the rubbery plateau was attributed to cold crystallization, which was associated with the density modulation caused by the formation of a crystalline phase. <sup>54</sup> The starting temperature of cold crystallization increases along with 2,7-N loading in the copolymers, which further proves the interference effect of 2,7-N on crystallization, consistent with the cold crystallization results detected by DSC. It should be noted that the value of storage modulus decreases progressively with 2,7-N loading. It is probable that the reduced crystal packing efficiency afforded by comonomer loading largely depresses the crystal lamellar thickness and causes the elasticity to drop. This phenomenon becomes more pronounced with increased 2,7-N loading, and the rubbery plateau related to cold crystallization will vanish when the crystallization ability is completely destroyed.

These cooperative relaxation phenomena are implicitly related to the gas permeability. The oxygen barrier performance is very important to many performance packaging applications. As shown in Table 5, the oxygen permeability of 27PEN copolymers decreases monotonically with 2,7-N loading. The oxygen barrier performance of 27PEN20 (0.0073 barrer) shows a 30% improvement over PET (0.0108 barrer) with only 20% 2,7-N embedded in PET chains, indicating the barrier capability of meta-substitution fused aromatic rings is 2 times better than that of commercial used para-substitution fused aromatic rings (26NDA) reported in the previous study. <sup>55</sup> This is mainly attributable to restricted ring-flip associated with the nonlinear axis of meta-naphthalene structure, which would suppress the chain rotation and mobility related directly to gas diffusivity.

In summary, 27PEN copolymers showed improved performance compared to PET with respect to thermal, mechanical, and barrier properties, which strongly suggests that these copolymers with value-added property improvement using biosourced 2,7-N are promising candidate materials for broader packaging applications. Nonetheless, more analyses, including techno-economic assessment, life-cycle assessment, and toxicological evaluations of 2,7-N would be would be necessary before being commercialized in large-scale for food packaging.

# Conclusions

In this work, PET incorporated with bio-derived naphthalate-based monomers were successfully synthesized by a two-step melt polycondensation reaction. <sup>1</sup>H NMR analysis revealed that the synthesized copolymers were statistically random copolymers and the molar ratio of 2,7-N in the copolymers was consistent with that of the input reactants. Comonomer units were found to partition into the amorphous phase while leaving the crystal lattice units unaltered. 2,7-N acted as an impurity from the viewpoint of crystallization, which significantly affected the nucleation mechanism and crystallization ability of the materials.

The observed results were the change in crystal geometry from 3D spherulite growth to 2D axialite growth, as well as the increasing suppression effect on crystal lamellar thickness with increasing 2,7-N loading. The effect that 2,7-N imposed on crystallization behaviors was the key to the improvement of thermal and mechanical properties. By analysis using various methods, it was confirmed that 2,7-N has a positive effect on the drawbacks of PET, where 27PEN10 in particular showed a dramatic increase in all the properties while retaining most of the crystallization behaviors of PET. The  $T_g$  of 27PEN10 is 15 °C higher than that of PET, which is due to the increased energy barrier of the chain motion for the polymer chains in amorphous domain, whereas the increased rigidity of the polymer chain caused by fused aromatic rings resulted in the improvement in strain hardening and elongation at break. Moreover, the restricted ring-flip associated with the nonlinear axis of meta-naphthalene structure effectively suppressed the oxygen permeability of the materials. These results suggest that bioadvantaged comonomers like 2,7-N are capable of being used for modifying polymer properties, both in sustainability and performance compared with those of traditional PET. The strategy in this work would not only allow PET to have widespread applications requiring higher service temperature, and better barrier/mechanical properties, but also constructed the fundamental structure-property relationships connecting the bioadvantaged chemicals as hard-segment inside polymers to its performance. Compared to the petroleum-derived chemicals (IPA, CHDM, DEG) which are widely available and under commercial development including technoeconomic model development, 2,7-N is a potential bio-derived chemical, which could be used in PET property enhancements, and further studies like techno-economic and life-cycle assessment would be needed to be developed. In general, by utilizing bioadvantaged monomers, the economic incentive for adoption and industry growth of biochemicals can be provided and capital requirements for product startup can be simultaneously minimized.

# **Experimental Section**

### Materials

Terephthalic acid (TPA, 99+%, Acros Organics), isophthalic acid (IPA, 99+%, TCI America), and ethylene glycol (EG, anhydrous, 99.8%, Sigma-Aldrich) were purchased as the precursors for polymer synthesis. Dimethyl naphthalene-2,7-dicarboxylate (2,7-N) were synthesized based on the reaction procedures reported in our previous study. <sup>28</sup> Zinc acetate (Zn(CH<sub>3</sub>COO)<sub>2</sub>), anhydrous, 99.8%, Alfa Aesar) and antimony(III) oxide (Sb<sub>2</sub>O<sub>3</sub>, 99%, Sigma-Aldrich) were used as catalysts in transesterification and polycondensation reaction, respectively. Triphenyl phosphate (TPP, >99%, Sigma-Aldrich) was used as a thermal stabilizer in polycondensation reaction. 1,1,1,3,3,3-Hexafluoro-2-propanol (HFIP), dichloroacetic acid (DCAA), phenol, 1,1,2,2-tetrachloroethane, trifluoroacetic acid-d (TFA-d), and chloroform-d (CDCl3) were purchased from Fisher Scientific and were used as received for solvent and sample preparation.

### Synthesis

The homo- and copolymers were synthesized using a 300ml stainless steel reactor (type 4560, Parr Instrument Company) equipped with mechanical stirrers, reactor controller (Model 4848, Parr Instrument Company), liquid nitrogen cold traps, and vacuum pump (DUO 10, Pfeiffer Vacuum). Poly(ethylene terephthalate-stat-2,7-naphthalate) (27PENX) and poly(ethylene terephthalate-stat-isophthalate) (PEIX) were synthesized by a two-step polycondensation reaction (see Schemes 1 and S1). The first step was esterification as well as transesterification of TPA/2,7-N or TPA/IPA with EG, respectively, using Zn(CH<sub>3</sub>COO)<sub>2</sub> (0.15 mol % to diester) as the transesterification catalyst. For TPA/IPA esterification, no catalyst is needed since diacid served as both reagent and catalyst. The molar ratio of overall diacid/diester to EG were 1 to 10. The purpose of this molar ratio is to prepare completely bis-hydroxy ester end group monomers and ensure both end groups have the

same reactivity toward other monomers. This will make the growth of polymer chain more consistent and lower the dispersity compared to the different end group monomers. The reaction mixture was purged with argon for 0.5 h and the reaction temperature was heated to 220 °C. The stirring speed was set at 250 rpm for 5 h with the pressure at 110 psi and an argon sweep to remove water and methanol. After the first step reaction, the mixture was transferred to a round bottom flasks to distill the excess amount of EG by using an oil bath set to 110 °C under vacuum for 12 h. Then the monomer was returned to the autoclave reactor with antimony(III) oxide (0.02 mol % to the diacid/diester) and triphenyl phosphate (0.1 mol % to the diacid/diester) acting as catalyst and thermal stabilizer, respectively. The second step of polycondensation was carried out at 240 °C under high vacuum with the stirring speed at 600 rpm. At the end of the reaction, the reactor was purged by argon to ambient pressure to prevent thermal oxidation of the material while removing the polymer from the reactor.

### Characterization

The composition and the chemical structures were determined by <sup>1</sup>H NMR (600 MHz, Bruker Avance III) in CDCl<sub>3</sub>/TFA-d (75/25) solvent mixture at 10 mg/mL.

The molar composition of the copolymers was calculated based on the integral intensities of peak a from PET units and peak c from 27PEN units by using the following equation:

$$ET = \frac{\frac{I_a}{4}}{\frac{I_a}{4} + \frac{I_c}{2}}, \quad EN = \frac{\frac{I_c}{2}}{\frac{I_a}{4} + \frac{I_c}{2}}$$
 (4)

where the contents of ET and EN unit were their molar ratio in the polymer chain and  $I_a$  and  $I_c$  corresponded to the protons on the aromatic ring of ET and EN, respectively.

Intrinsic viscosity [ $\eta$ ] measurement was performed in phenol/1,1,2,2-tetrachloroethane (60/40, v/v) solvent mixture at 25 °C water bath using an Ubbelohde viscometer (Xylem, type 537 13).

Gel permeation chromatography (GPC) measurements were running at at a flow rate of 0.3 mL/min in a Tosoh Ecosec GPC (Tosoh Ecosec HLC-8320GPC) equipped with UV and RI detector. The concentration of samples was 6 mg/mL in HFIP/DCAA (50/50, v/v) solvent mixture, and HFIP was used as an eluent. Poly(methyl methacrylate) (PMMA) standards were used to determine the molecular weights.

FTIR (iD7 ATR Accessory for the Nicolet<sup>TM</sup> iS<sup>TM</sup> 5 Spectrometer, ThermoFisher) was used to analyze functionality. Spectra were obtained from 4000 to 400 cm<sup>-1</sup> from 32 scans at a resolution of 4 cm<sup>-1</sup>.

The crystal structure morphology and the extent of crystallinity were characterized by a Xenocs Xeuss 2.0 S/WAXS system equipped with Cu  $K_{\alpha}$  x-ray source. The data was collected by Dectris Pilatus3 R 1M detector and was calibrated by silver behenate standard. The specimens were attached directly onto the sample stage and the measurement was carried out under vacuum. Data acquisitions for WAXS and SAXS analysis were 600 s and 7200 s, respectively. The background signal of each samples was taken at the same condition. All data post-processing was using Foxtrot 3.3.4 (SOLEIL Synchrotron, France) for 2D raw data reduction and absolute intensity correction, and Irena package (Advanced Photon Source, Argonne National Lab, USA) for profile combination.<sup>57</sup> The crystal structure information was calculated by using scattering vector equation 5 and equation 6.

$$q = \frac{4\pi}{\lambda} sin\theta \tag{5}$$

$$L = \frac{2\pi}{q_{max}} \tag{6}$$

$$X_c = \frac{A_c}{A_a + A_c} * 100\% (7)$$

Where  $\lambda$  is the X-ray wavelength for Cu  $K_{\alpha}$  radiation ( $\lambda$ =1.542 Å),  $\theta$  is Bragg's angle, and  $q_{max}$  is peak position in the q range. The degree of crystallinity ( $X_c$ ) was measured by

equation 7 based on the ratio of the crystalline fraction  $(A_c)$  to the total area  $(A_a + A_c)$  under the WAXS curve.

The crystalline lamellar thickness ( $l_c$ ) and amorphous lamellar thickness ( $l_a$ ) in the lamellar stacks can be estimated from the WAXS and SAXS results using equation 8, where the amorphous region is assumed to be located only within the lamellar stacks.

$$l_c = LX_c, \qquad l_a = LX_a \tag{8}$$

Thermal characterizations were conducted by using differential scanning calorimetry (DSC, TA instruments Q2500) under nitrogen. The specimens from injection molding were conducted from 25 to 300 °C (27PEN100 to 370 °C) at a rate of 10 °C min<sup>-1</sup>, and were held for 5 min before being cooled back to 25 °C at a rate of 10 °C min<sup>-1</sup>. The isothermal crystallization kinetics were carried out on completely amorphous tensile bar samples in the temperature range from 110 to 175 °C. Samples were placed in DSC at 25 °C and heated to the desired temperature at 160 °C min<sup>-1</sup>. They were kept at the crystallization temperature for a sufficient period until the completion of crystallization. Thermal stability was evaluated by a simultaneous thermal analyzer (STA 449 F1 Jupiter, NETZSCH) in the temperature range from 40 to 1000 °C at a rate of 10 °C min<sup>-1</sup> under nitrogen.

Tensile tests were performed by an Instron 3369 at room temperature with a 1 kN load cell and the speed of 10 mm-min<sup>-1</sup> following the standards of ISO 527-2. The dimension of the tensile bar is type 1BB with 2 mm (thickness)  $\times$  10 mm (guage length). The impact strength of the samples were conducted by an impact tester (IT504, Tinius Olsen) according to the standards of ASTM D256 with the sample dimension of 63.5 mm (length)  $\times$  12.7 mm (width)  $\times$  3 mm (thickness).

The cryofractured surface were photographed by a scanning electron microscope (S4800 FE-SEM, Hitachi) at 10 kV SEM acceleration voltage. The samples from injection molding were freezed in liquid nitrogen for 5 min before being fractured.

The dynamic mechanical measurements were performed on a rheometer (ARES-G2, TA

Instruments) using the torsion fixture at a constant frequency of 1 Hz and a strain of 0.1%. The testing was conducted from -120 to 200 °C at a heating rate of 5 °C min<sup>-1</sup>.

The gas barrier property was measured by an oxygen permeation testing analyzer (MO-CON's OX-TRAN Model 2/21) under carrier gas mixture of 98% nitrogen and 2% hydrogen, and test gas of 99.9% oxygen. The analysis procedure is based on ASTM D3985 standards. The specimens with 0.5 mm thickness were prepared via injection molding (HAAKE Minijet, ThermoFisher) at 270 °C into a 120 °C mold and quenched in cold water bath. The permeability of the films was measured via oxygen transmission at 23 °C under 1% relative humidity and 1 atm. <sup>58,59</sup>

# Supporting Information Available

The Supporting information is available free of charge at. Additional experimental details, including isothermal crystallization kinetics study, isophthalate-based copolymer synthesis pathway and its characterization, GPC analysis, SEM images, and Mechanical tensile testing.

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# Next-Generation High-Performance Biobased Naphthalate-Modified PET for Sustainable Food Packaging Applications

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# Supplementary Information

• Number of pages (including cover): 13

• Number of figures: 14

• Number of table: 2

## Index

- Crystallization kinetics study of naphthalate-based copolymers
- Isophthalate-based copolymer synthesis pathway
- <sup>1</sup>H NMR spectra of naphthalate- and isophthalate-based copolymers
- Compositions and characteristics of isophthalate-based copolymers
- TGA results of isophthalate-based copolymers
- WAXS results of isophthalate-based copolymers
- Isothermal crystallization dynamics results
- DSC results of isophthalate-based copolymers
- Thermal transition properties of isophthalate-based copolymers
- GPC results of naphthalate- and isophthalate-based copolymers
- Mechanical tensile testing of naphthalate- and isophthalate-based copolymers
- SEM images
- DMA results of isophthalate-based copolymers

The crystallization kinetics study was carried out in completely amorphous samples prepared by injection molding. The crystallization kinetics of PET and the copolymers under isothermal conditions for various modes of nucleation and growth can be well approximated based on the known Avrami equation. The general form of Equation 1 was:

$$X_t = 1 - exp(-kt^n) \tag{1}$$

where  $X_t$  was the relative crystallinity at time t, k was crystallization rate constant related to nucleation, and n was the Avrami exponent based on the mechanism of nucleation and the form of crystal growth. The  $X_t$  can be calculated according to Equation 2:

$$X_t = \frac{Q_t}{Q_\infty} = \frac{\int_0^t \frac{dH}{dt} dt}{\int_0^\infty \frac{dH}{dt} dt}$$
 (2)

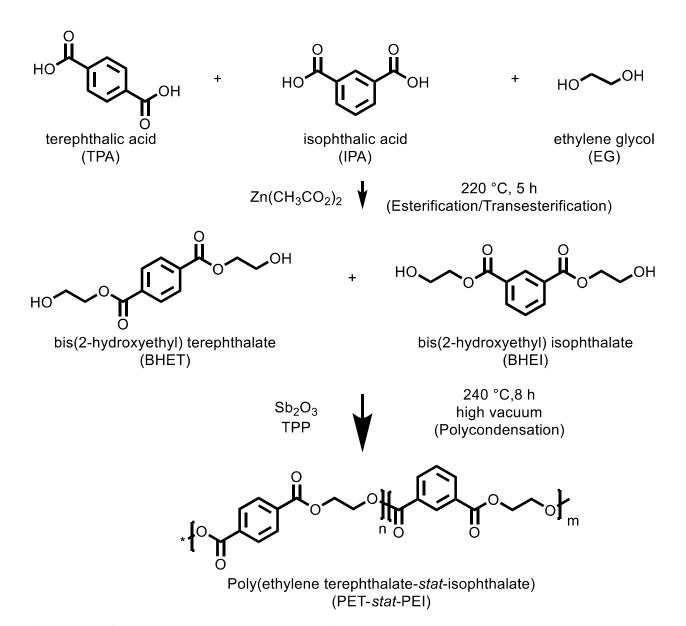
where  $Q_t$  and  $Q_{\infty}$  were the amounts of enthalpy generated at time t and infinite time  $t_{\infty}$ , respectively, and dH/dt was the enthalpy evolution rate. For convenience, Equation 1 could be written in a double logarithmic form as follows Equation 3:

$$ln[-ln(1-X_t)] = nlnt + lnk$$
(3)

According to Equation 2, a graphic representation of  $ln[-ln(1-X_t)]$  versus lnt was developed, and n and lnk were the slope and the intercept of the straight line, respectively.

The crystallization half time  $(t_{1/2})$  was defined as the time at which the relative crystallinity reached 50% and it can be determined according to the measured kinetic parameters by Equation 4:

$$t_{1/2} = (\frac{\ln 2}{k})^{\frac{1}{n}} \tag{4}$$



Scheme 1: Step-growth polycondensation of isophthalate-based copolymers via a two-step polymerization

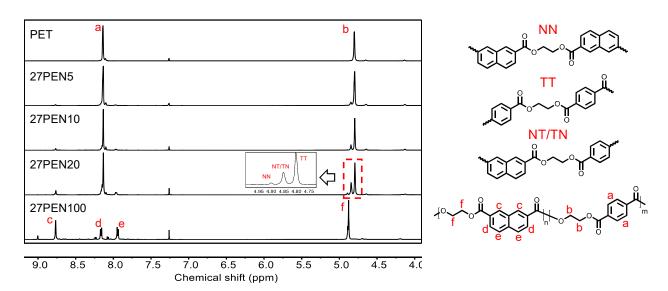


Figure S1:  $^{1}\mathrm{H}$  NMR spectra of PET and naphthalate-based copolymers

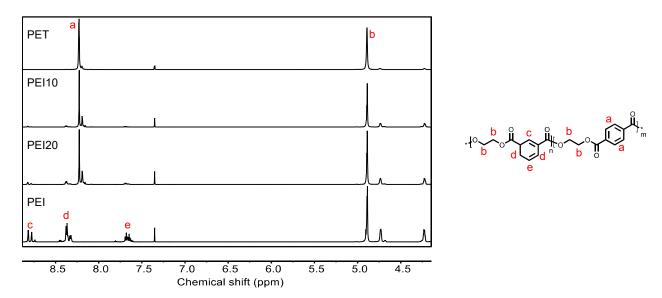


Figure S2: <sup>1</sup>H NMR spectra of PET and isohthalate-based copolymers

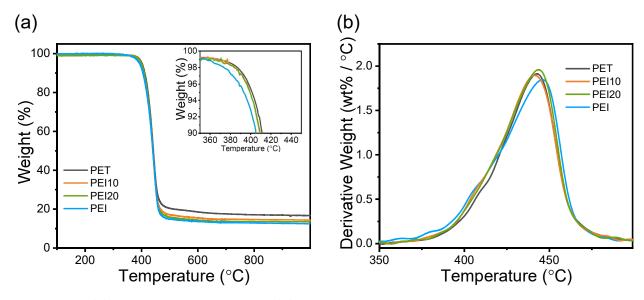


Figure S3: (a) TGA thermograms and (b) DTG curve of PET and isophthalate-based copolymers with heating rate of 10 °C min<sup>-1</sup>.

Table S1: Compositions and characteristics of isophthalate-based copolymers

Sample Code <sup>a</sup>	Temp./Time (°C / hour)	IV <sup>b</sup> (dL/g)	Mn <sup>c</sup> (kDa)	Mw <sup>d</sup> (kDa)	Đ <sup>e</sup>
PEI10	240/8	0.65	13.3	23.4	1.76
PEI20	240/8	0.75	17.2	30.2	1.76
PEI100 <sup>f</sup>	240/8	0.55	23.4	37.3	1.59

<sup>&</sup>lt;sup>a</sup> Sample code: PEIX, x = mol% of IPA unit. <sup>b</sup> Intrinsic viscosity was measured in phenol/1,1,2,2-tetrachloroethane (60/40, v/v) solution by using an Ubbelohde viscometer at 25 °C. <sup>c</sup> Number-average molecular weight. <sup>d</sup> Weight-average molecular weight. <sup>e</sup> Dispersity calculated by Mw/Mn. The molecular weights were determined by GPC in 1,1,1,3,3,3-hexafluoro-2-propanol solution with Poly(methyl methacrylate) (PMMA) standards. <sup>f</sup> Poly(ethylene isophthalate).

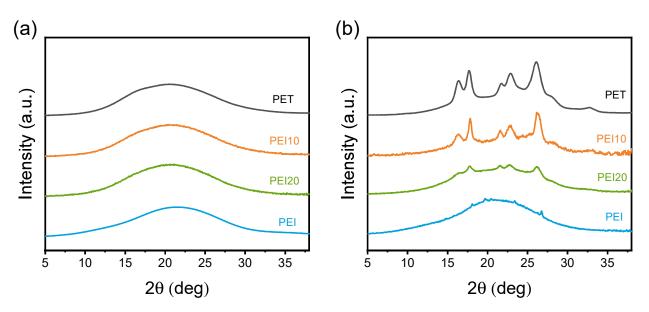


Figure S4: WAXS patterns of PET and isophthalate-based copolymers: (a) tensile bar quenched from 270 °C; (b) after annealing at 175 °C for 6 h

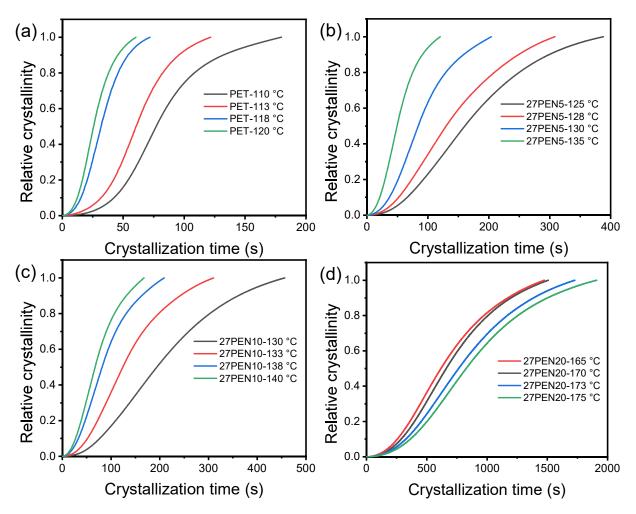


Figure S5: Relative crystallinity with time for isothermal crystallization of PET and naphthalate-based copolymers at different temperatures

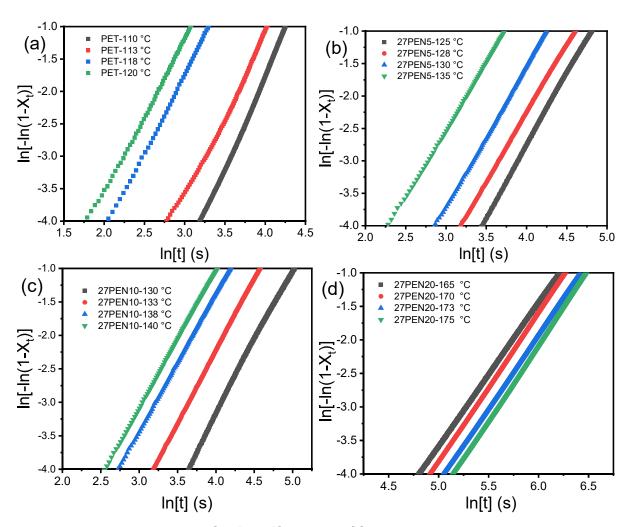


Figure S6: Avrami plots of  $\ln[-\ln(1-X_t)]$  versus  $\ln[t]$  for isothermal crystallization of PET and naphthalate-based copolymers at different temperatures

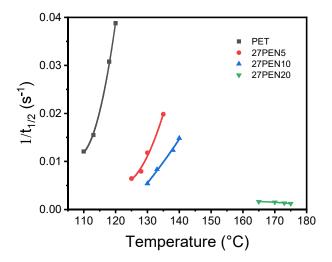


Figure S7: Dependence of  $1/t_{1/2}$  on isothermal crystallization temperature  $(T_c)$  of PET and naphthalate-based copolymers

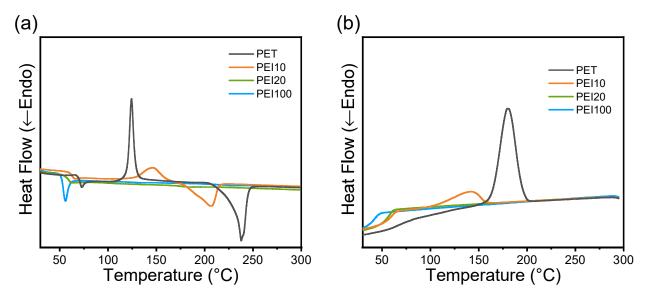


Figure S8: DSC thermograms of quenched PET and isophthalate-based copolymers at scan rate of  $10~^{\circ}\text{C min}^{-1}$ : (a) heating and (b) cooling

Table S2: Thermal transition properties of PET and isophthalate-based copolymers

~	DSC					TGA		
Sample Code <sup>a</sup>	T <sub>g</sub> <sup>b</sup>	T <sub>cc</sub> <sup>b</sup>	$T_c^{\ b}$	$T_m^{\ b}$	$X_{\rm c} (\%)^{\rm b}$	T <sub>d,5%</sub> c	$T_{d,max}^{c}$	Residue (wt%) c
PET	69.7	124.3	179.7	237.8	33.0	401.4	442.7	16.7
PEI10	62.2	147.0	141.6	207.1	18.9	399.5	441.3	14.4
PEI20	58.0	157.0	N.D. <sup>d</sup>	182.9	0.6	399.3	443.6	13.5
PEI100	51.3	N.D.	N.D.	N.D.	N.D.	393.3	445.9	12.5

<sup>a</sup>Sample code: PEIX, x = mol% of IPA repeat unit. <sup>b</sup>Glass transition ( $T_g$ ), crystallization ( $T_c$ ), cold crystallization ( $T_c$ ) and melting ( $T_m$ ) temperatures, degree of crystallinity ( $X_c$ ) during heating cycle. <sup>c</sup> $T_{d,5\%}$ : decomposition temperatures at which the weight loss reached 5% of its initial weight.  $T_{d,max}$ : the temperature at the maximum rate of decomposition. The residual mass at 1000 °C. <sup>d</sup>Not detected by DSC.

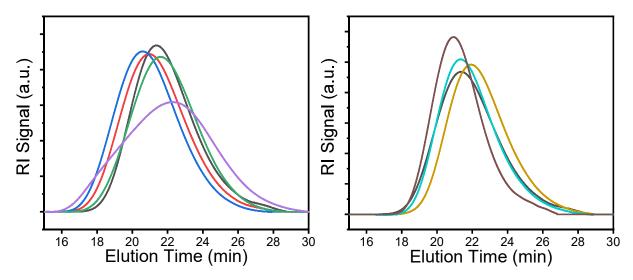


Figure S9: GPC analysis of naphthalate- and isophthalate-based copolymers produced in this study: PET (black); 27PEN5 (red); 27PEN10 (blue); 27PEN20 (green); and 27PEN100 (purple); PEI10 (goldenrod); PEI20 (cyan); PEI100 (brown)

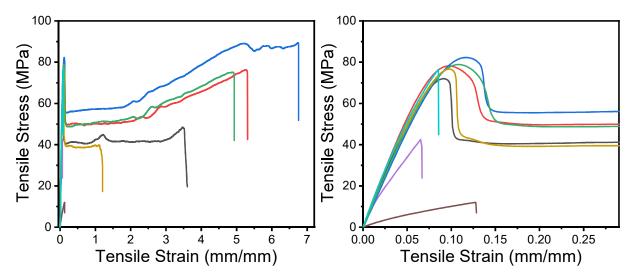


Figure S10: Representative stress-strain curves of naphthalate- and isophthalate-based copolymers with the speed of 10 mm-min<sup>-1</sup> at room temperature: PET (black); 27PEN5 (red); 27PEN10 (blue); 27PEN20 (green); and 27PEN100 (purple); PEI10 (goldenrod); PEI20 (cyan); PEI100 (brown)

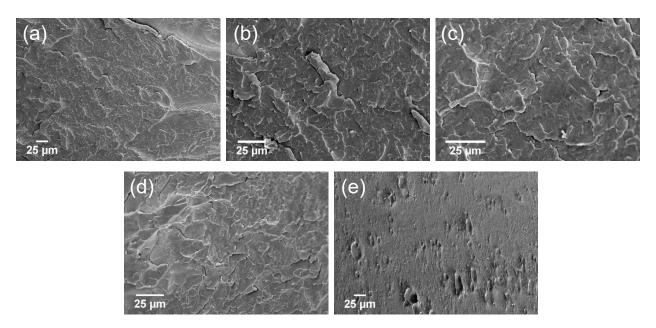


Figure S11: Fractured surfaces of PET and naphthalate-based copolymers: (a) PET; (b) 27PEN5; (c) 27PEN10; (d) 27PEN20; and (e) 27PEN100

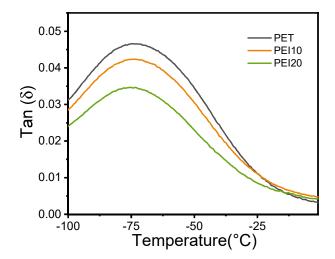


Figure S12: DMA spectra of PET and isophthalate-based copolymers: tan ( $\delta$ )  $\gamma$  relaxation transition

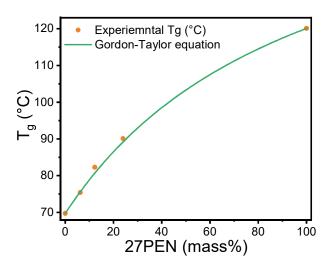


Figure S13:  $T_g$  values of 27PEN copolymers as a function of 27PEN loading and their fitting with the Gordon-Taylor equation