

# Multiwavelength optical and NIR variability analysis of the Blazar PKS 0027-426

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## ABSTRACT

We present multiwavelength spectral and temporal variability analysis of PKS 0027-426 using optical *griz* observations from Dark Energy Survey between 2013 and 2018 and VEILS Optical Light curves of Extragalactic Transient Events (VOILETTE) between 2018 and 2019 and near-infrared (NIR) *JKs* observations from Visible and Infrared Survey Telescope for Astronomy Extragalactic Infrared Legacy Survey (VEILS) between 2017 and 2019. Multiple methods of cross-correlation of each combination of light curve provides measurements of possible lags between optical–optical, optical–NIR, and NIR–NIR emission, for each observation season and for the entire observational period. Inter-band time lag measurements consistently suggest either simultaneous emission or delays between emission regions on time-scales smaller than the cadences of observations. The colour–magnitude relation between each combination of filters was also studied to determine the spectral behaviour of PKS 0027-426. Our results demonstrate complex colour behaviour that changes between bluer when brighter, stable when brighter, and redder when brighter trends over different time-scales and using different combinations of optical filters. Additional analysis of the optical spectra is performed to provide further understanding of this complex spectral behaviour.

**Key words:** galaxies: active – quasars: individual: PKS 0027-426 – galaxies: jets.

## 1 INTRODUCTION

Blazars are the most variable subclass of active galactic nuclei (AGN), whose radiation is considered to be dominated by a bright, relativistic jet less than  $10^\circ$  from the line of sight (e.g. Urry & Padovani 1995). They can be divided into two subclasses based on their spectra; Flat Spectrum Radio Quasars (FSRQs) and BL Lacertae objects (BL Lacs), as the spectra of FSRQs contain strong, broad emission lines, whilst BL Lacs are characterized by a relatively featureless optical continuum.

The emission from blazars is strongly variable over the entire electromagnetic spectrum, and is composed of both thermal and non-thermal contributions which originate in different components of the AGN. Their spectral energy distributions (SEDs) contain two characteristic bumps; one at low energies which covers the range

from radio to UV and a higher energy bump which is located in the X-rays to gamma-rays (e.g. Fossati et al. 1998). The dominating emission processes corresponding to these bumps are considered to be synchrotron radiation from the relativistic electrons in the jet at lower energies (e.g. Urry & Mushotzky 1982) and at higher energies can be described by either leptonic models where the bump is due to inverse Compton scattering of the low-energy emission (e.g. Böttcher 2007), or hadronic models in which the bump is due to emission from relativistic protons (e.g. Mücke & Protheroe 2001). In the optical and near-infrared (NIR), additional contributions are expected from thermal emission from the accretion disc and torus.

Multiwavelength variability studies of blazars provide further information on these emission processes; for example, analysis of temporal variability can be used to infer their location within the AGN using correlations between the radiation from the wavelength ranges corresponding to these processes. Additionally, spectral variability studies give insight into how the contributions from the thermal and

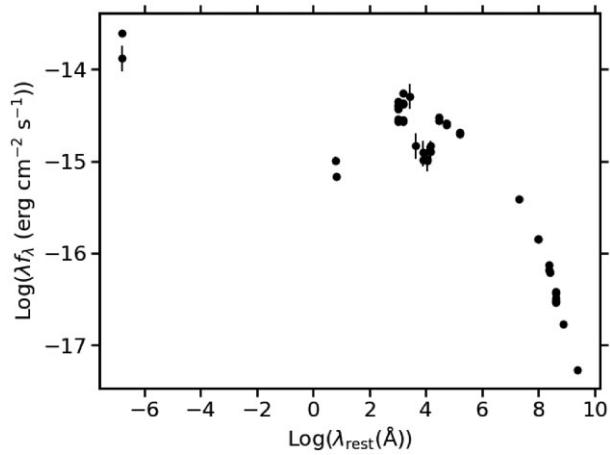
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non-thermal emission vary with respect to each other, as the ratio of thermal and non-thermal emission changes with the variations in the flux, and can result in changes to the spectral shape and colour of the blazar (e.g. Gu & Ai 2011).

Several studies of the correlations between the flux variations from different wavelength ranges of blazars commonly show that they are strongly correlated with short lags between the light curves on time-scales  $< 1$  d or with no significant lag determined on the order of days (e.g. D’Ammando et al. 2013; Zhang et al. 2013; Kaur & Baliyan 2018). This implies that the dominant source of the emission in the different wavelength ranges is co-temporal in the blazar, and possibly co-spatial. However, some studies have also reported lags on the order of 10–100 d between optical and NIR light curves in blazars (e.g. Li et al. 2018; Safna et al. 2020), which could imply that the sources of the emission are located with a distance between them, or Li et al. (2018) suggest that if the emission is produced by shocks in the jet, the higher energy emission could emerge closer to the front of the shock than the lower energy emission, resulting in a delay.

Studies of the spectral variation of blazars have shown three main colour behaviours; bluer when brighter (BWB), redder when brighter (RWB), or achromatic/stable when brighter (SWB). These colour trends are often explained as a result of variations between the different emission processes that contribute to the overall emission, for example, a RWB trend could indicate that a red component, such as synchrotron emission from the relativistic jet, is more quickly varying than the bluer component, such as the thermal emission from the accretion disc, and vice versa for a BWB trend (e.g. Fiorucci, Ciprini & Tosti 2004; Bonning et al. 2012; Agarwal et al. 2019). Alternatively, BWB trends have also been explained by processes associated with the relativistic jet only; for example, Fiorucci et al. (2004) describe a one component synchrotron model in which the more intense the energy release, the higher the particle’s energy. A shock-in-jet model has also been used to describe the BWB trend as accelerated electrons at the front of the shock lose energy while propagating away, and because of synchrotron cooling the higher frequency electrons lose energy faster, thus making the high frequency bands more variable (e.g. Kirk, Rieger & Mastichiadis 1998; Agarwal et al. 2019). The RWB trend is most frequently observed with FSRQs, and similarly the BWB trend is most commonly observed in BL Lacs (e.g. Gu et al. 2006; Bonning et al. 2012; Meng et al. 2018); however, this is not always the case, as some studies find the reverse or find SWB trends (e.g. Gu & Ai 2011; Zhang et al. 2015; Mao & Zhang 2016). Furthermore, while many studies find these simple colour behaviours, some find that the colour trends can be complex; for example, Isler et al. (2017) showed that the B-J colour behaviour of the FSRQ 3C 279 varied on different time-scales, and over different periods during the 7 yr of observation. Specifically, the average colour trend of the entire 7 yr is BWB; however, the colour variability is shown to deviate for individual observation seasons, such as from achromatic or a SWB trend between May and August 2008, RWB between September 2009 and April 2010, and BWB between February and August 2011. Furthermore, the colour trend of some blazars has been shown to change at a certain magnitude; for example, Zhang et al. (2015) found that several sources showed RWB trends in the low flux state and then kept a SWB trend or a BWB trend in the high flux states.

PKS 0027-426<sup>1</sup> is classified as a FSRQ with  $z = 0.495$  (Hook et al. 2003). It has been observed in the optical *griz* bands with Dark Energy



**Figure 1.** The spectral energy distribution of PKS 0027-426 using data from NED.

Survey (DES) from 2013–2018 and VEILS OptIcal Light curves of Extragalactic TransienT Events (VOILETTE) from 2018 onwards, with concurrent observations in the NIR *J* and *K<sub>s</sub>* bands with Visible and Infrared Survey Telescope for Astronomy (VISTA) Extragalactic Infrared Legacy Survey (VEILS) from 2017 onward. PKS 0027-426 was found to be the most variable AGN detected in the VEILS fields thus far. The SED of PKS 0027-426 is displayed in Fig. 1 and is made using data from NASA/IPAC Extragalactic Database (NED). The lower energy peak can be seen in the wavelength range corresponding to  $\log(\lambda_{\text{rest}}(\text{\AA})) \sim 0\text{--}10$ , and a dip is present at  $\sim 4$  which corresponds to the optical–NIR wavelength range.

In this paper, we analyse the temporal and spectral variability of PKS 0027-426 using optical *griz* observations from DES and VOILETTE between 2013–2019 and NIR *JK<sub>s</sub>* observations from VEILS between 2017–2019. The structure is as follows: in Section 2 we describe the observations and data reduction. In Sections 3 and 4 we present the temporal and spectral variability analysis of PKS 0027-426, respectively. In Section 5 we discuss the results and provide further analysis of the spectra to explain the colour behaviour observed. Finally, in Section 6 we present a summary of the conclusions.

## 2 OBSERVATIONS AND DATA REDUCTION

### 2.1 Overview of optical and NIR Surveys

#### 2.1.1 DES-SN

DES was a 5-yr survey that observed using DECam on the 4-m Blanco telescope at the Cerro Tololo Inter-American Observatory (CTIO) in the *grizY* bands between 2013–2018 (Flaugher et al. 2015). It consisted of two programmes; a wide-area survey that covered 5000 square degrees, in which each region was observed 10 times in each of the filters over the course of the survey, and a time-domain survey (DES-SN; Kessler et al. 2015) that covered a smaller region of 27 square degrees, but was observed repeatedly and regularly. The observed 27 square degrees of the DES-SN programme was divided between four fields; the Chandra Deep Field South (CDFS), Elias South (ES), Sloan Digital Sky Survey (SDSS) Stripe 82 field, and the XMM deep field, each of which were observed with  $\sim 6$  month observation seasons per year, with  $\sim 6$ -d cadences.

<sup>1</sup>RA = 00h30m17.584s, DEC = -42d24m46.02s (J2000)

### 2.1.2 VEILS

VEILS is a current ESO Public Survey which repeatedly targets nine square degrees of sky in the  $JKs$  bands starting in 2017 using VIRCAM on the VISTA telescope at the Paranal Observatory (Emerson, McPherson & Sutherland 2006). It was designed to observe regions that are covered by DES (three square degrees in each of the CDFS, ES, and XMM fields), also with  $\sim 6$  month observation seasons and cadences of 10–14 d, to provide concurrent optical and NIR observations which will allow for multiwavelength time domain studies of AGN. For example, one of the primary science goals of VEILS is to measure the time lags between the accretion disc variability and the response from the hot dust in the surrounding torus in a process referred to as dust reverberation mapping.

### 2.1.3 VOILETTE

From 2018 onwards, the optical  $griz$  band observations continued with VOILETTE, which uses OmegaCAM on the 2.6-m *VLT Survey Telescope* (VST) at the Paranal Observatory (Kuijken et al. 2002). VOILETTE was designed as the optical counterpart to VEILS, and as such covered approximately the same region of sky with planned cadences of  $\sim 6$ –10 d.

## 2.2 Data reduction and calibration

The reduction of the data from DES included correcting for cross-talk and non-linear pixel response, as well as subtraction of bias and sky frames, bad pixel masking, and flat fielding as explained by Morganson et al. (2018). The raw data from VOILETTE and VEILS were similarly reduced by bad pixel masking, flat fielding and subtraction of bias, dark current, and sky frames. Aperture photometry was then performed using fixed aperture sizes in each survey on PKS 0027-426, and also on nearby objects in the same detector that were variable by less than 0.5 dex over the entire observation period. These non-varying objects (listed in Appendix A1), whose magnitudes were calibrated using the DES photometric catalogue (Abbott et al. 2018) for the optical observations and the 2MASS catalogue (Skrutskie et al. 2006) for the NIR observations, were used to correct the observed counts of PKS 0027-426 for the nightly effects such as the seeing or change in atmospheric conditions. The corrected counts for PKS 0027-426 in each filter were converted into apparent AB magnitudes, creating the light curves displayed in Fig. 2.

## 2.3 Light curves of PKS 0027-426

The top four panels of Fig. 2 show the optical light curves of PKS 0027-426 over 6 yr in the  $griz$  bands, with each season separated by the dotted lines and with overall magnitude variations (brightest–dimmest magnitude) of  $|\Delta g| = 1.56 \pm 0.06$  mags,  $|\Delta r| = 1.95 \pm 0.07$  mags,  $|\Delta i| = 1.79 \pm 0.06$  mags, and  $|\Delta z| = 1.52 \pm 0.06$  mags. The cadences of the observations in the  $griz$  bands are  $6.3 \pm 4.9$  nights,  $6.5 \pm 5.3$  nights,  $6.6 \pm 4.7$  nights, and  $6.2 \pm 4.8$  nights, respectively, over the entire observational period, and Appendix A3 displays the average cadence for each observation season. The variability in the optical bands is relatively low in the seasons starting 2013–2015, but increases in the seasons starting in 2016–2018. The 2017 season displays the largest variability in each optical filter, and contains its peak magnitude in the first of two flares that are separated by approximately 75 d. The 2018 season contains only three observations in the  $g$  and  $z$  filters, however, displays a

decreasing brightness in all optical filters. The lower two panels of Fig. 2 show the NIR light curves with 2 yr of observations in the  $J$  and  $Ks$  bands, respectively, with magnitude variations of  $|\Delta J| = 1.32 \pm 0.01$  mags and  $|\Delta Ks| = 1.24 \pm 0.02$  mags and cadences of  $11.3 \pm 5.9$  nights and  $11.2 \pm 8.1$  nights. Similarly to the optical, the 2017 season displays the largest variability in both NIR filters; however, it also contains a gap in the observations between  $\sim 58\,000$  and  $58\,050$  MJD, which corresponds to the epochs containing the first and brightest peak in the optical. The brightness of the 2018 season is also shown to decrease in the NIR.

### 2.3.1 Light curve variability with the amplitude variability parameter

To characterize the variability of PKS 0027-426 in each filter and in each season, the amplitude variability parameter,  $A$ , was calculated using equation (1) (Heidt & Wagner 1996),

$$A = \sqrt{(A_{\max} - A_{\min})^2 - 2\sigma^2}, \quad (1)$$

Where  $A_{\max}$  and  $A_{\min}$  are the maximum and minimum apparent magnitudes, and  $\sigma$  is the average measurement error.

Table 1 shows the amplitude variation of each filter in each year. The variation in the  $griz$  light curves is relatively small in the seasons starting in 2013–2015 with amplitude variability parameters of  $\sim 0.25$ –0.5, but in the 2016 and 2017 seasons they increase to  $\sim 0.6$ –0.9 and  $> 1$ , respectively, and in the 2018 season decreases back to  $\sim 0.6$ –0.7. The  $J$  and  $Ks$  bands in both the 2017 and 2018 seasons are shown to vary similarly to the optical.

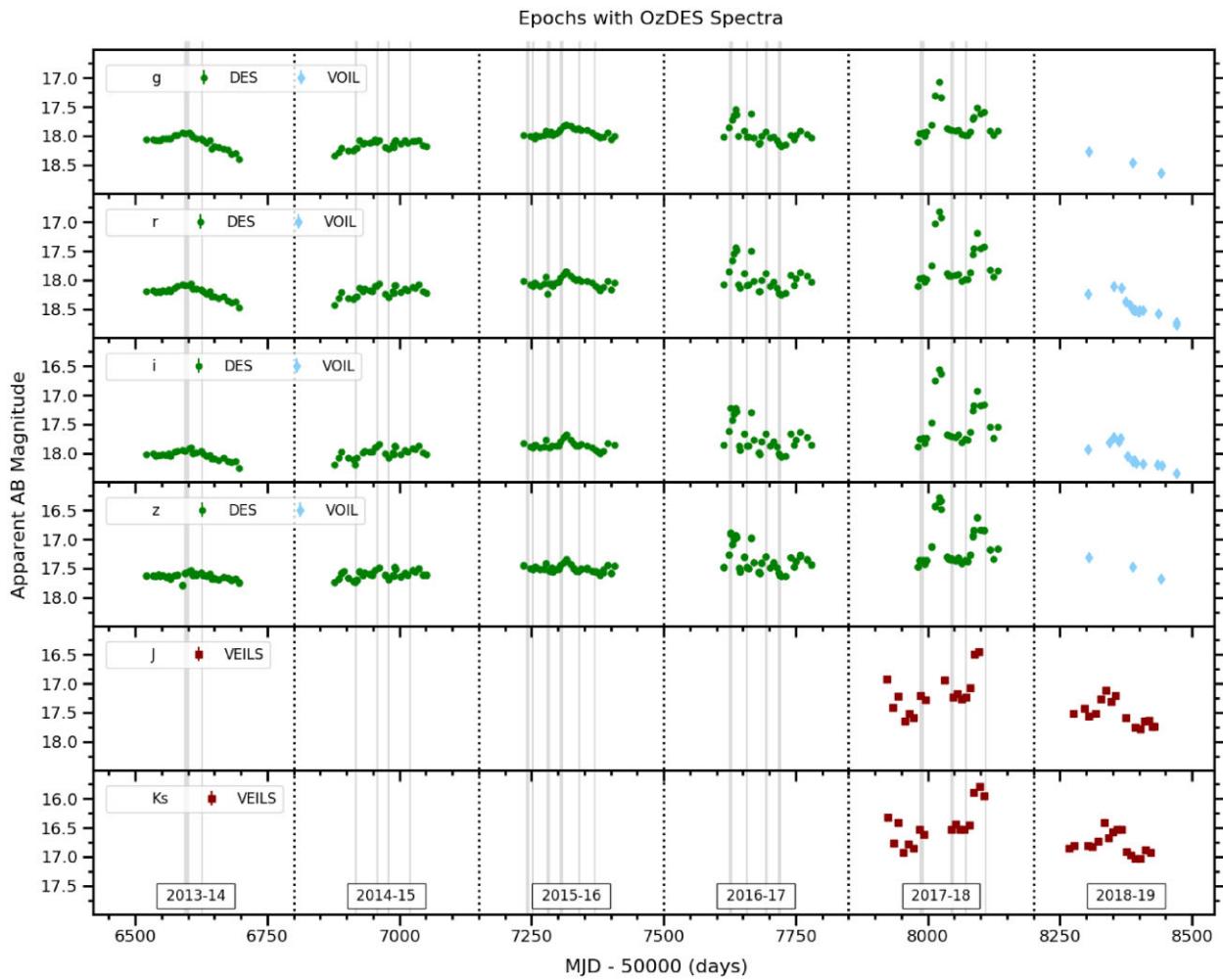
### 2.3.2 DES light curve variability with flux–flux plots

As PKS 0027-426 was often observed on the same night with each DES filter, the flux variations in each optical filter relative to another could be further analysed using flux–flux plots for the seasons starting 2013–2017, for example, Fig. 3 displays the  $r$ ,  $i$ , and  $z$  band fluxes compared to the  $g$  band fluxes. The flux in each filter is shown to increase as the  $g$  band flux increases, and though the relationships are not necessarily linear overall, Fig. A1(b) in Appendix A2 shows that the relationship in the individual seasons of the  $g$ – $z$  flux–flux plots are approximately linear. Furthermore, Fig. A1(a) displays the flux–flux plots of the 2017 season including VEILS observations, but as PKS 0027-426 was not observed simultaneously in the NIR, the light curves were interpolated.

## 2.4 Spectroscopy

Optical spectra of PKS 0027-426 were obtained on 37 epochs between 2013 and 2018 by OzDES (Australian spectroscopic Dark Energy Survey), the spectroscopic follow up survey for DES. OzDES uses the 3.9-m Anglo-Australian Telescope (AAT; Smith et al. 2004) at Siding Spring Observatory in Australia, along with the AAOmega spectrograph with the Two Degree Field (2dF) 400 multi-object fibre positioning system (Lewis et al. 2002), which covers the wavelength range of 3700–8800 Å with a spectral resolution of 1400–1700 (Lidman et al. 2020).

The spectra were flux calibrated using the photometry from DES, as described by Hoermann et al. (2019), to remove any differences from each epoch due to factors including the image quality, airmass, transparency, and accuracy of the fibre placement. Fig. 4 displays the mean and smoothed RMS spectra of PKS 0027-426, for the entire



**Figure 2.** Light curves of PKS 0027-426 in the optical *griz* bands and NIR *JKs* bands. The optical light curves contain a combination of DES (green circles) in the seasons starting in 2013–2017 and VOILETTE (blue diamonds) in the season starting in 2018 and the NIR observations are from VEILS (red squares) in seasons starting in 2017–2018. Each observation season is separated by the dotted lines and the epochs corresponding to OzDES observations are shown with the grey lines.

**Table 1.** The amplitude variation of the light curves in different filters in each observation season, calculated using equation (1). The 2013–2016 seasons contain only data from the *griz* bands from DES, the 2017 season also contains the *JKs* bands from VEILS, and the 2018 season only has the *r* and *i* bands from VOILETTE and the *J* and *Ks* bands from VEILS due to limited *g* and *z* data.

| Year starting | <i>g</i> (mag) | <i>r</i> (mag) | <i>i</i> (mag) | <i>z</i> (mag) | <i>J</i> (mag) | <i>Ks</i> (mag) |
|---------------|----------------|----------------|----------------|----------------|----------------|-----------------|
| 2013          | 0.46           | 0.41           | 0.35           | 0.26           | –              | –               |
| 2014          | 0.28           | 0.36           | 0.36           | 0.27           | –              | –               |
| 2015          | 0.26           | 0.39           | 0.32           | 0.27           | –              | –               |
| 2016          | 0.63           | 0.81           | 0.85           | 0.76           | –              | –               |
| 2017          | 1.03           | 1.29           | 1.33           | 1.20           | 1.13           | 1.19            |
| 2018          | –              | 0.66           | 0.61           | –              | 0.62           | 0.66            |

observational period and the individual observations seasons, with most relevant emission lines labelled.

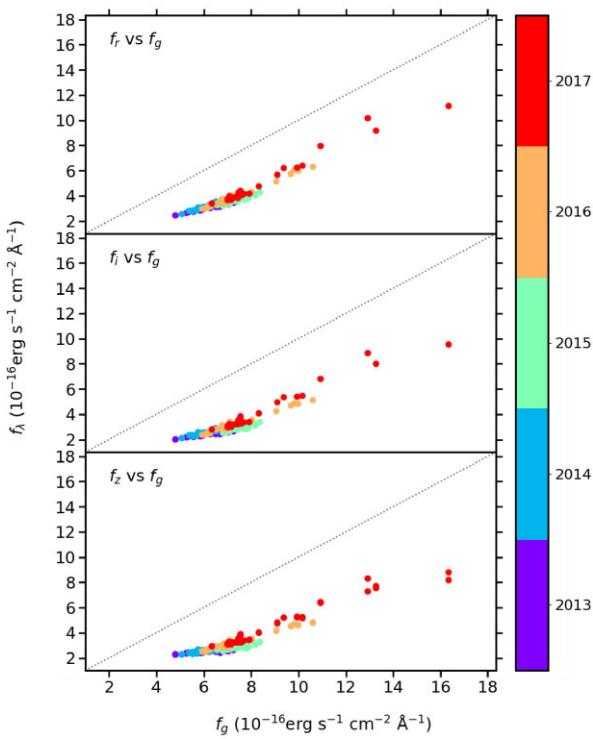
An excess in the red wing can be seen in some of the broad emission lines (BELs) in Fig. 4, which is a phenomenon observed in many radio loud quasars. Punzly et al. (2020) studied the red asymmetry in the BELs of radio loud quasars and found that the blazars with the most redward asymmetric BELs had a low Eddington rate, a strong

jet relative to the accretion flow bolometric luminosity and a polar line of sight.

The Mg II and H  $\beta$  lines in the spectra were used to obtain an estimate for the virial mass of the SMBH of PKS 0027-426,  $M_{\text{BH}}$ , using equation (2),

$$\log\left(\frac{M_{\text{BH}}}{M_{\odot}}\right) = a + b \log\left(\frac{\lambda L_{\lambda}}{10^{44} \text{ erg s}^{-1}}\right) + 2 \log\left(\frac{\text{FWHM}}{\text{km s}^{-1}}\right), \quad (2)$$

where the coefficients  $a$  and  $b$  for the Mg II line are 0.74 and 0.62, respectively (Shen et al. 2011), and for the H  $\beta$  line are 0.91 and 0.50, respectively (Vestergaard & Peterson 2006),  $\lambda L_{\lambda}$  is the monochromatic luminosity at 3000 Å and 5100 Å for the Mg II and H  $\beta$  lines, respectively, which are calculated from the *gri* magnitudes as described by Kozłowski (2015), and the FWHM is the full width half maximum of the emission line. This was calculated for each OzDES spectra, and the mean of  $\log(M_{\text{BH}})$  was found to be  $8.16 \pm 0.08 M_{\odot}$  for the Mg II line and  $8.06 \pm 0.28 M_{\odot}$  for the H  $\beta$  line, which are consistent within their  $1\sigma$  uncertainties.



**Figure 3.** Flux variations in each DES  $r$ ,  $i$ ,  $z$  filter compared to the DES  $g$  band, where the data points are coloured according to observation season.

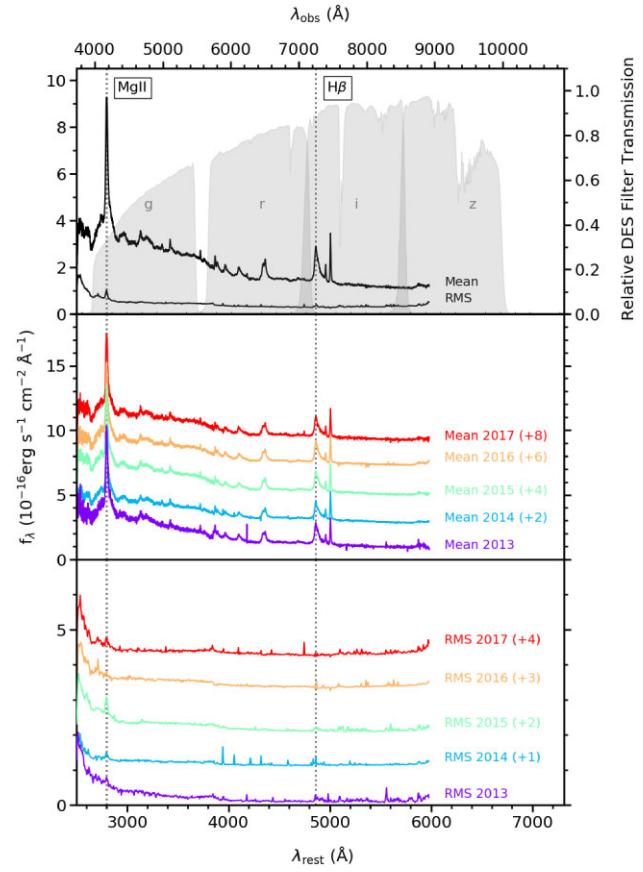
### 3 TEMPORAL VARIABILITY

Temporal variability studies of blazars typically report lags between the optical and NIR emission on time-scales  $< 1$  d (e.g. D’Ammando et al. 2013; Zhang et al. 2013; Kaur & Balaian 2018), which implies that the dominant emission regions are co-spatial and could be expected to be due to the synchrotron emission from the relativistic jet. This expected lag is smaller than can be detected with the cadences of observations from DES, VOILETTE, and VEILS, as these surveys were designed to detect dust reverberation lags in AGN. However, temporal variability analysis is used here to explore whether any larger lags, possibly one corresponding to a delay between the thermal emission in the optical and NIR, could be detected as well, as other studies have reported significant lags between the optical and NIR in blazars on the order of 10–100 d (e.g. Li et al. 2018; Safna et al. 2020).

In order to quantitatively study the temporal variability between the optical and NIR light curves from DES, VOILETTE and VEILS, the cross-correlation function (CCF) was computed (e.g. Peterson 1993). The CCF requires continuous light curves, therefore they were interpolated using the structure function (SF), which is a measure of the fractional change in flux for observations that are separated by a given time interval,  $\tau$ , (e.g. Suganuma et al. 2006; Emmanoulopoulos, McHardy & Uttley 2010), to simulate data points where there were no observations. The first order structure function,  $SF(\tau)$ , is defined in equation (3) (Suganuma et al. 2006),

$$SF(\tau) = \frac{1}{N(\tau)} \sum_{i < j} [f(t_i) - f(t_j)]^2, \quad (3)$$

where  $f(t)$  is the flux at time  $t$  and the sum is over all pairs for which  $t_j - t_i = \tau$  and  $N(\tau)$  is the number of pairs.



**Figure 4.** *Top panel:* Overall mean spectra of PKS 0027-426 using 92 observations from OzDES over 37 epochs between 2013 and 2018, with some of the relevant emission lines labelled. The filter transmission curves for DES are overlaid to demonstrate which filter each emission line lies in. *Middle panel:* The mean spectra for each individual observation season, labelled with the starting year of observations. *Lower panel:* The smoothed RMS spectra for each individual observation season, labelled with the starting year of observations.

Interpolating the light curves introduces uncertainties, however, as it creates large portions of simulated data in the  $\sim 6$  month gaps between the observation seasons. Therefore, to reduce the effect of the simulated data in the observation gaps, two methods of interpolated cross-correlation function (ICCF) were compared. The first method is the standard ICCF (S-ICCF), which utilizes as much of the observed data as possible by cross correlating both light curves which were interpolated with 1-d cadences. This method was computationally inexpensive, and generally worked well when cross correlating individual observation seasons; however, it treated the interpolated data between the observing seasons of the entire light curve equally with the data which could decrease its reliability.

The second method was used to limit the impact of the simulated data between the observations, by only interpolating one light curve and extracting the epochs that matched the other filter’s observations plus the range of possible lags being tested to get simultaneous light curves. This method is more reliable when using light curves that contain multiple observing seasons as it includes less of the interpolation in the gaps between observations. However, it did not utilize the entirety of the observations available as only the epochs of one of the light curves were used at a time. This method was used

twice, alternatively interpolating each filter, which will be referred to as the modified ICCF (M-ICCF) and reverse modified ICCF (RM-ICCF), respectively.

### 3.1 Cross-correlation results

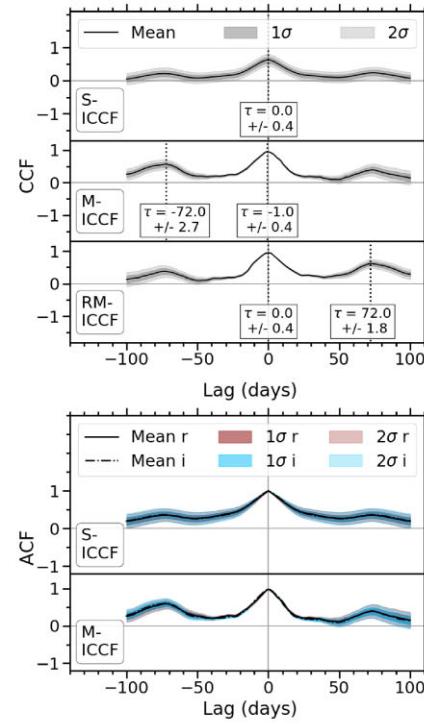
The entire light curves of each combination of filters in both the optical and NIR were interpolated 10 000 times and cross correlated using the methods described above, as well as the light curves from individual years. Each season was tested with possible observed lags between  $\pm 100$  d due to the length of the individual season light curves. The CCFs were also compared with the autocorrelation functions (ACFs) of each light curve to determine whether the peaks in the CCFs were a result of a lag between the light curves, or an effect of quasi-periodicity within the individual light curve. Potential lags that were measured from peaks on the mean CCFs were considered positive detections if the CCF values were greater than 0.5. This was chosen as the limit as most non-zero peaks in the ACFs had values smaller than this, with the exception of ACFs where the optical 2017 or 2018 season light curves were included. The possible lags that were classified as positive detections are labelled on the plots, with the uncertainties calculated as the standard deviations of the peak of the CCF for each interpolation around the peak of the mean CCF.

In this section, the cross-correlations of the  $r$  and  $i$ ,  $r$  and  $K_s$  and  $J$  and  $K_s$  band light curves are discussed to represent the emission between the optical filters, the optical with NIR filters, and the NIR filters with each other, as these were the light curves with the most observations.

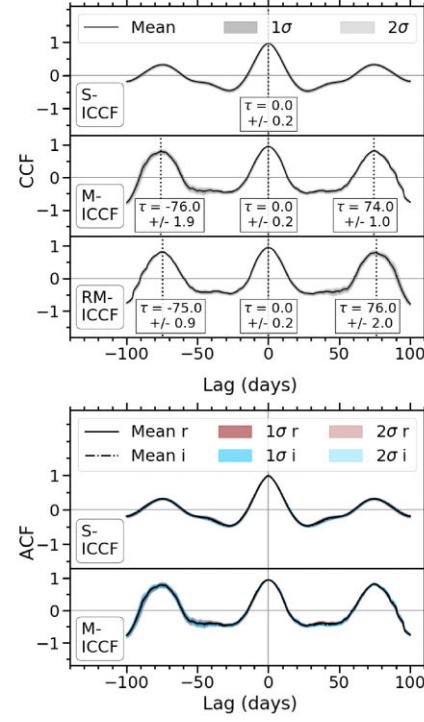
#### 3.1.1 Cross-correlations of $r$ and $i$ bands

The cross-correlation between the  $r$  and  $i$  band light curves and their ACFs are displayed in Fig. 5, for the entire observational period and the individual season starting 2017. The CCFs of the other individual observation seasons are displayed in Fig. B3 in Appendix B1. Possible lags are measured from the CCFs of the entire  $r$  and  $i$  band light curves in Fig. 5(a) with values of  $0.0 \pm 0.4$ ,  $-1.0 \pm 0.4$ , and  $0.0 \pm 0.4$  d with the S-ICCF, M-ICCF and RM-ICCF methods respectively, and at  $-72.0 \pm 2.7$  and  $72.0 \pm 1.8$  d with the M-ICCF and RM-ICCF methods, respectively. To further investigate these lags, the CCFs of the individual observation seasons of the  $r$  and  $i$  band light curves were analysed to determine whether the lag between light curves remained constant over every year, and to reduce the impact of the interpolations between observation seasons.

The strong correlation at  $\sim 0$  d is consistently present in the CCFs of each year, except the season starting in 2016 as discussed in Appendix B1, with an overall mean value of  $-0.1 \pm 0.2$  d. This implies that the emission in both filters is co-temporal, or any delay between the emission regions is on time-scales smaller than the cadences of observations. The  $\sim \pm 75$ -d lags are also observed in all of the 2017 CCFs which are displayed in Fig. 5(b), and in 2018 M-ICCF and RM-ICCF in Fig. B3(c); however, this is assumed to be due to the shape of the light curves, as in the 2017 light curves there are two peaks separated by  $\sim 75$  d, and in the 2018 season the light curves follow a decline that tapers off for a short period before declining again. This is also seen in the corresponding ACFs of each light curve in the 2017 and 2018 seasons therefore implying that it is not a delay between emission regions but a consequence of aliasing.



(a) CCFs and ACFs of the entire  $r$  and  $i$  light curves.



(b) CCFs and ACFs of the 2017  $r$  and  $i$  light curves.

**Figure 5.** Top panels: Mean CCFs of the  $r$  and  $i$  light curves in the season starting 2017 and in the entire observation period between 2013 and 2019. Lower panels: The corresponding ACFs. Here, the M-ICCF method refers to the interpolated  $r$  band, and the RM-ICCF method refers to the interpolated  $i$  band.

### 3.1.2 Cross-correlations of $J$ and $Ks$ bands

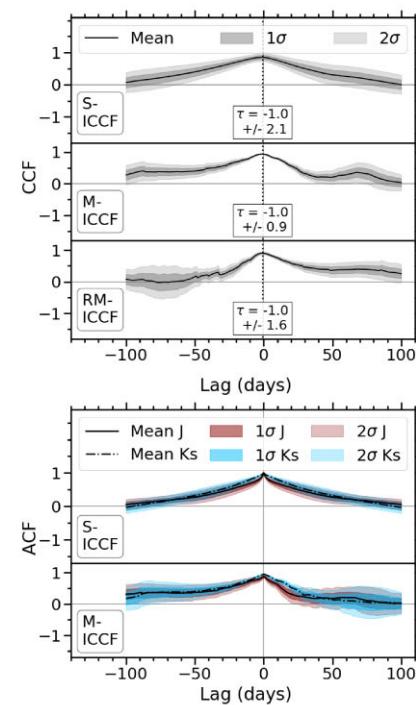
The cross-correlation between the  $J$  and  $Ks$  band light curves for the individual season starting in 2017 and the entire light curves are displayed in Fig. 6, along with their ACFs, and the individual 2018 season is displayed in Fig. B4. These CCFs show the presence of a strong correlation at  $\sim 0$  d in all seasons with a mean value of  $-0.8 \pm 1.0$  d, as well as possible lags at  $\sim 55$  d in the 2017 season, and at  $\sim 85$  d in the 2018 season. The  $\sim 0$ -d correlation is seen consistently in the M-ICCF and RM-ICCF methods over all seasons, however, is not observed in the 2017 S-ICCF method, which is assumed to be due to large gaps in the light curves and the interpolations between these observations diluting the overall correlation. The  $55.0 \pm 4.5$ -d lag in the 2017 season is only recorded in the RM-ICCF method. Furthermore, the 2017 CCFs in Fig. 6(b) are relatively flat, especially in the S-ICCF method which indicates that the lags found are not very distinctive. The  $\sim 85$ -d lag in the M-ICCF and RM-ICCF methods of the 2018 season, shown in Fig. B4, are also present in the ACFs of the  $J$  and  $Ks$  light curves, which implies that the lag is not between the different filters but is due to aliasing, for example, the dip at  $\sim$  MJD 58300 d and the dips at  $\sim$  MJD 58400 d follow similar shapes and therefore correlate with each other. It therefore follows that this peak is more pronounced in the M-ICCF and RM-ICCF methods as the interpolations between observations could dilute the correlation found here. As this lag is only present in this scenario and not in the 2017 season or overall light curve, it can be assumed that it is not a delay between the  $J$  and  $Ks$  band light curves.

### 3.1.3 Cross-correlations of $r$ and $Ks$ bands

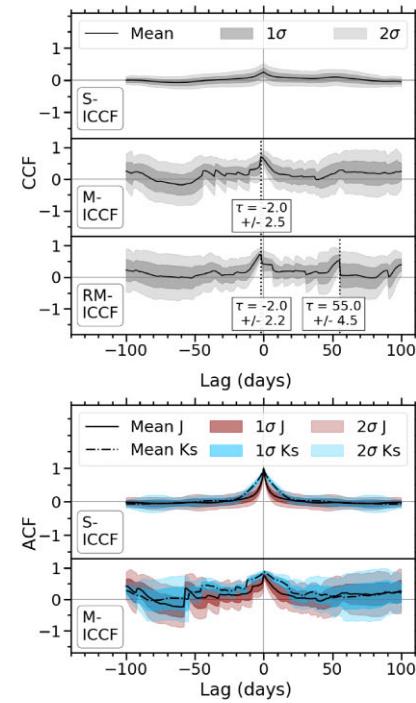
The results of the cross-correlations between the  $r$  and  $Ks$  band light curves are displayed in Fig. 7 along with their ACFs for the 2017 season and the entire overlapping observational period. The CCFs and ACFs of the 2018 season are displayed in Fig. B5. The  $r$  and  $Ks$  band CCFs show the presence of strong correlations at  $\sim 0$  d, with a mean of  $0.0 \pm 1.2$  d, and at  $\sim \pm 75$  d, however, these measured lags are not consistent over all methods and all seasons of the  $r$  and  $Ks$  band light curves therefore further analysis of these lags was performed.

In the S-ICCF methods, the light curves are not as well correlated at 0 d, which could be due to the interpolated epochs equally impacting the CCFs, and therefore reducing the overall correlation. Furthermore, there is a lower correlation at 0 d for RM-ICCF method when the 2017 season is used, but this is suspected to be due to the lack of observations in the NIR when the optical light curve displays the first of two peaks. As the NIR light curve is interpolated and epochs extracted matching the observed optical epochs, the interpolations during the unobserved month will reduce the overall correlation.

The  $\sim \pm 75$ -d lags only appear when the 2017  $r$  band observation season, which contains two peaks separated by  $\sim 75$  d, is included in the CCF. This can be seen in the ACFs, as the ACF of the  $r$  band in the 2017 season from both S-ICCF and M-ICCF methods also contains peaks at  $\sim \pm 75$  d, as does the ACF of the entire  $r$  band light curve, although the correlations are not as strong. The  $Ks$  band ACFs do not include the  $\sim \pm 75$ -d lags however, which is likely due to a lack of observations in the NIR band during the month that corresponded to the first peak in the  $r$  band. The presence of the  $\sim \pm 75$ -d lags was further investigated in Appendix B2 using the SF of the  $r$  and  $Ks$  bands from observations between 2017 and 2019. By simulating light curves using the method described by Timmer & Koenig (1995) with a range of power spectra with varied properties

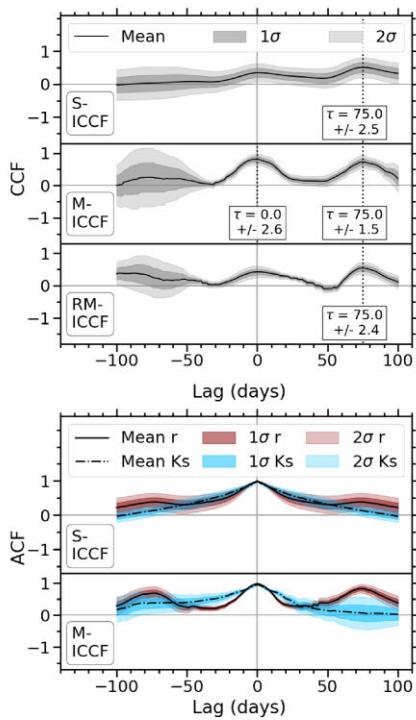


(a) CCFs and ACFs of the entire  $J$  and  $Ks$  light curves.

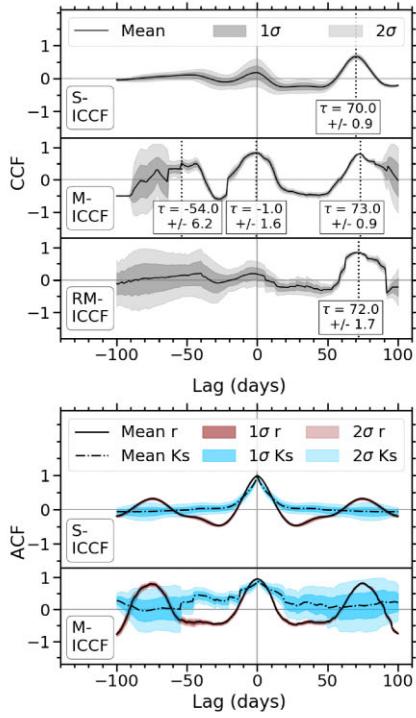


(b) CCFs and ACFs of the 2017  $J$  and  $Ks$  light curves.

**Figure 6.** Top panels: Mean CCFs of  $J$  and  $Ks$  light curves in the season starting 2017 and in the entire observation period between 2017 and 2019. Lower panels: The corresponding ACFs. Here, the M-ICCF method refers to the interpolated  $J$  band and the RM-ICCF method refers to the interpolated  $Ks$  band.



(a) CCFs and ACFs of the combined 2017 and 2018  $r$  and  $Ks$  light curves.



(b) CCFs and ACFs of the 2017  $r$  and  $Ks$  light curves.

**Figure 7.** Top panels: Mean CCFs of  $r$  and  $Ks$  light curves in the season starting 2017 and in the entire observation period between 2017 and 2019. Lower panels: The corresponding ACFs. Here, the M-ICCF method refers to the interpolated  $r$  band and the RM-ICCF method refers to the interpolated  $Ks$  band.

including break frequencies, slopes, and white noise amplitudes, it is found that the  $\sim 75$ -d time-scale does not depend on specific properties of the light curve of PKS 0027-426, but occurred for a random  $\sim 12$  and 14 per cent of the 10 000 simulated light curves in the  $r$  and  $Ks$  bands, respectively.

## 4 SPECTRAL VARIABILITY

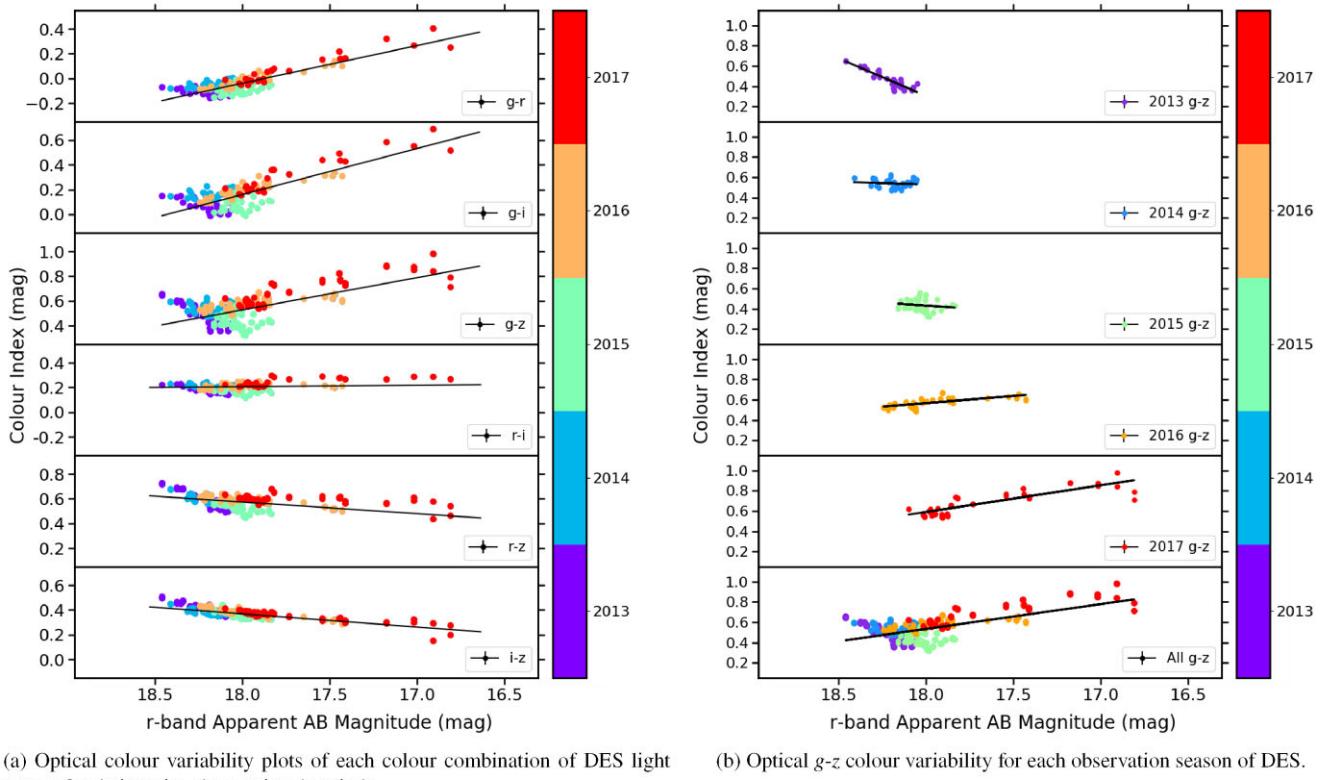
### 4.1 Optical colour variability from DES

The optical colour behaviour of PKS 0027-426 was studied by measuring the colour indices of each combination of the observed  $griz$  bands, starting with DES data. Each colour index from DES was calculated using quasi-simultaneous observations from the same instrument that were first corrected for galactic extinction using the measurements from Schlafly & Finkbeiner (2011), and had an average time difference of  $\sim 12$  min between observations in the different bands, and a maximum time difference of  $\sim 18.5$  min.

The optical colour indices ( $g-r$ ,  $g-i$ ,  $g-z$ ,  $r-i$ ,  $r-z$ , and  $i-z$ ) were plotted against the  $r$  magnitude in Fig. 8(a), and the colour behaviour was quantified using the slope of the plot, the Spearman rank correlation coefficient ( $\rho$ -values), and the probability of no correlation ( $p$ -values). The slope here is calculated as described by Kelly (2007) using a Bayesian method of linear regression, excluding outliers as explained in Appendix C1. The Spearman rank correlation coefficient is a non-parametric measure of the strength and direction of the relationship between variables, which returns a value between  $\pm 1$ , where values of 0 corresponds to no correlation, and correlations of  $\pm 1$  is an exact monotonic relationship. A large  $p$ -value indicates a high probability of no correlation and a small  $p$ -value indicates a low probability that the correlation is due to random noise. Positive slopes and Spearman rank correlation coefficients imply the colour increases with decreasing brightness (increasing magnitude), which corresponds to a BWB trend, while negative slopes and Spearman rank correlation coefficients imply RWB trends. These possible colour trends were deemed significant if the linear slopes were consistent within  $3\sigma$ . The plots with colour trends that were not significantly BWB or RWB within  $3\sigma$  have corresponding  $p$ -values that were relatively large ( $p > 0.01$ ) and  $\rho$ -values that were relatively small ( $|\rho| < 0.4$ ) compared to those with significant colour trends, which therefore imply a SWB trend. The data points in Fig. 8(a) were coloured according to observation season. Table 2(a) contains the slope of each colour-magnitude plot, the Spearman rank correlation coefficient, the probability that no correlation is present between the colour and  $r$  magnitude, and the colour trend.

The overall  $g-r$ ,  $g-i$ , and  $g-z$  colours are shown to be RWB by the strong anticorrelations present, with slopes of  $-0.30 \pm 0.02$ ,  $-0.36 \pm 0.02$ , and  $-0.25 \pm 0.02$ , respectively, and  $\rho$ -values of  $-0.60$ ,  $-0.52$ , and  $-0.33$ , respectively. The  $r-i$  colour has a slope of  $-0.06 \pm 0.01$  and  $\rho = -0.26$  which indicates a slight RWB trend, but also has a relatively high probability of no correlation with a  $p$ -value of  $1.73 \times 10^{-3}$ , which implies this RWB trend is not as significant as in the  $g-r$ ,  $g-i$ , and  $g-z$ . Finally, the  $r-z$  and  $i-z$  colours show positive correlations which implies the source becomes BWB with slopes of  $0.06 \pm 0.01$  and  $0.12 \pm 0.01$  and  $\rho$ -values of 0.31 and 0.73, respectively.

The colour behaviours of each season are also shown to vary; for example, Fig. 8(b) displays plots of the colour behaviour of  $g-z$  in the different observations seasons of DES. Table 2(b) contains the slope, the Spearman rank correlation coefficient, the probability of no correlation for each season of  $g-z$ , and the colour trend. The 2013 season shows a strong BWB trend, with slope and  $\rho$ -



(a) Optical colour variability plots of each colour combination of DES light curves for their entire observational periods.

(b) Optical  $g-z$  colour variability for each observation season of DES.

**Figure 8.** Optical colour variability plots of PKS 0027-426 in DES. The colours of the data points correspond to each observation season.

**Table 2.** The slopes, Spearman rank coefficients, probability of no correlation, and colour trend of the DES filters in the colour versus  $r$  magnitudes plots in Fig. 8.

(a) The slopes, Spearman rank coefficients, probability of no correlation, and colour trend for each combination of DES filters in the colour versus  $r$  magnitudes plots in Fig. 8(a).

| Colour | Slope of colour versus $r$ mag | $\rho$ -value | $p$ -value             | Colour trend |
|--------|--------------------------------|---------------|------------------------|--------------|
| $g-r$  | $-0.30 \pm 0.02$               | $-0.60$       | $2.45 \times 10^{-15}$ | RWB          |
| $g-i$  | $-0.36 \pm 0.02$               | $-0.52$       | $5.50 \times 10^{-11}$ | RWB          |
| $g-z$  | $-0.25 \pm 0.02$               | $-0.33$       | $1.67 \times 10^{-8}$  | RWB          |
| $r-i$  | $-0.06 \pm 0.01$               | $-0.26$       | $1.73 \times 10^{-3}$  | RWB          |
| $r-z$  | $0.06 \pm 0.01$                | $0.31$        | $1.25 \times 10^{-7}$  | BWB          |
| $i-z$  | $0.12 \pm 0.01$                | $0.73$        | $5.06 \times 10^{-48}$ | BWB          |

(b) The slopes, Spearman rank coefficients, probability of no correlation, and colour trend for each season of DES in the  $g-z$  colour versus  $r$  magnitude plots in Fig. 8(b).

| Season | Slope of $g-z$ versus $r$ mag | $\rho$ -value | $p$ -value             | Colour trend |
|--------|-------------------------------|---------------|------------------------|--------------|
| 2013   | $0.74 \pm 0.06$               | 0.8           | $5.77 \times 10^{-13}$ | BWB          |
| 2014   | $0.06 \pm 0.06$               | 0.09          | 0.52                   | SWB          |
| 2015   | $0.12 \pm 0.09$               | 0.17          | 0.18                   | SWB          |
| 2016   | $-0.14 \pm 0.02$              | $-0.77$       | $3.58 \times 10^{-12}$ | RWB          |
| 2017   | $-0.26 \pm 0.02$              | $-0.78$       | $3.68 \times 10^{-11}$ | RWB          |

values of  $0.74 \pm 0.06$  and 0.8, respectively. The 2014 and 2015 seasons both display a small positive correlation with slopes of  $0.06 \pm 0.06$  and  $0.12 \pm 0.09$ , respectively, and  $\rho$ -values of 0.09 and

**Table 3.** Colour behaviour of each combination of optical  $griz$  filters in each season.

| Colour | 2013 | 2014 | 2015 | 2016 | 2017 |
|--------|------|------|------|------|------|
| $g-r$  | BWB  | RWB  | SWB  | RWB  | RWB  |
| $g-i$  | BWB  | SWB  | SWB  | RWB  | RWB  |
| $g-z$  | BWB  | SWB  | SWB  | RWB  | RWB  |
| $r-i$  | BWB  | SWB  | SWB  | SWB  | RWB  |
| $r-z$  | BWB  | BWB  | BWB  | BWB  | BWB  |
| $i-z$  | BWB  | BWB  | BWB  | BWB  | BWB  |

0.17, respectively; however the positive slopes are not significant within  $3\sigma$  uncertainties, and they also have a large probability of no correlation with  $p$ -values of 0.52 and 0.18, respectively, which indicates the colour behaviour follows a SWB trend. The seasons starting in 2016 and 2017 demonstrate RWB trends, with slopes of  $-0.14 \pm 0.02$  and  $-0.26 \pm 0.02$ , and  $\rho$ -values given as  $-0.77$  and  $-0.78$ , respectively. The  $g-z$  colour behaviour over the entire observational period is shown to follow a RWB trend due to the 2016 and 2017 seasons which are the brightest, most variable seasons and therefore dominate the correlation. The colour–magnitude plots and tables containing slopes of each season of the remaining combination of optical DES  $griz$  filters are given in Appendix C1, and a summary of the colour trends of each combination of filters in each observation season is given in Table 3.

#### 4.2 Optical colour–magnitude plots from interpolation

The colour indices of PKS 0027-426 were also studied for each combination of observations in the optical and the NIR; however, the optical and NIR were not observed simultaneously or even quasi-

simultaneously as is necessary for studying the colour behaviour of highly variable objects such as blazars. Therefore, one of the light curves was interpolated so that quasi-simultaneous observations could be used.

To test the reliability of obtaining the colour behaviour from interpolated light curves, the optical colour variability from interpolated DES light curves were studied first, by removing half of the observations (randomly selected) from one light curve, and interpolating the remaining light curve using the structure function method to produce a light curve with a cadence of 1 d, as explained in Section 3. The dates matching the observations from the second filter were then used to recreate the colour–magnitude plots.

This method was repeated 10 000 times for each light curve. The distribution of slopes given from the colour–magnitude plots from interpolated DES light curves are shown in Fig. 9(a) and the results of these were then compared to the values obtained from Fig. 8(a) in Table 4. The results from each of the interpolated light curves are shown to be consistent with each other and within  $1\sigma$  uncertainties of the results from Fig. 8(a). It is shown in Fig. 9(a) that distributions from interpolating filter 1 return a smaller slope of the filter 1–filter 2 colour index versus  $r$  band magnitude than the distributions from interpolating filter 2, and often the result from interpolating filter 1 and filter 2 return a smaller and larger slope than the actual measured slope from Fig. 8(a), respectively. This could be due to the interpolations underestimating some of the larger variability in the light curves, which therefore means that when filter 1 is interpolated it could be less variable than filter 2 during these regions of large variability and therefore the filter 1–filter 2 colour is smaller, and vice versa for filter 2. Furthermore, some of the histograms in Fig. 9(a) also display a secondary smaller peak, which corresponds to a slope less than the slope of the main peak when filter 1 is interpolated and a slope greater than the slope of the main peak when filter 2 is interpolated. Analysis of this peak has shown that it occurs when the brightest points in the light curve are removed before interpolation, specifically the dates between MJD 58014 and 58025. This results in a smaller peak to the left when filter 1 is interpolated as the interpolated light curve is then shown to vary less than filter 2, hence the slope becomes steeper, and the smaller peak to the right when filter 2 is interpolated as in this case the slope becomes shallower as the subtracted filter varies less.

To further investigate this method, it was then replicated for each colour combination in each individual season of DES, for example, Fig. 9(b) shows the distribution of the slope of  $g-z$  in each season of DES. It was found that 82 percent of the mean slopes from interpolations of individual years for all combination of filters were consistent with the slopes from individual years within  $1\sigma$  and all were consistent within  $1.5\sigma$ . Comparisons between the slope obtained using all observations and using the interpolation method are displayed in Appendix C2, for each season in each colour combination.

#### 4.3 Optical–NIR colour–magnitude plots from interpolation

The interpolation method was shown to be consistent for the DES colour indices, so it was therefore used to measure each combination of optical and NIR in the 2017 and the 2018 seasons. The results of the 2017 season slope of optical–NIR colour against  $r$  band are displayed in Fig. 10. VEILS did not observe in the 2017 season between MJD 57993 and 58044, during which time a peak was present in the optical, so therefore the light curves were restricted to MJD greater than 58044 to prevent large portions of interpolations impacting the results as explained in Appendix C3. Fig. 10 was plotted against the  $r$  band to show comparable colour trends with

the optical colours in Fig. 8(a); however, this required additional interpolation of the  $r$  band when the dates matching the NIR light curves were extracted. The other interpolated optical and  $r$  band light curves in this situation therefore did not necessarily follow the same variations during the interpolations which could have an effect on the slope of the interpolated optical–NIR colour versus  $r$  band magnitude plot. The results in Fig. 10 show that 50 per cent of the interpolated slopes of the colour versus  $r$  magnitude plot are consistent within  $1\sigma$  of each other, and all are consistent within  $1.8\sigma$ . Furthermore, it was found that the plots of  $g-J$  and  $g-Ks$  versus  $r$  have negative slopes within  $5\sigma$  and  $4\sigma$  uncertainties, respectively, and the plots of  $z-J$  and  $z-Ks$  versus  $r$  have negative slopes within  $1.7\sigma$  and  $1\sigma$  uncertainties, respectively, which implies RWB trends. The plots of  $r-J$ ,  $r-Ks$ ,  $i-J$ , and  $i-Ks$  do not show a conclusive trend. All slopes of the 2018 season, which are displayed in Appendix C4, show inconclusive colour behaviours.

## 5 DISCUSSION

In the previous sections, the multiwavelength variability of PKS 0027-426, a FSRQ at  $z = 0.495$ , was studied using observations in the optical and NIR to attempt to further understand the inner regions of AGN that cannot be spatially resolved.

### 5.1 Temporal variability

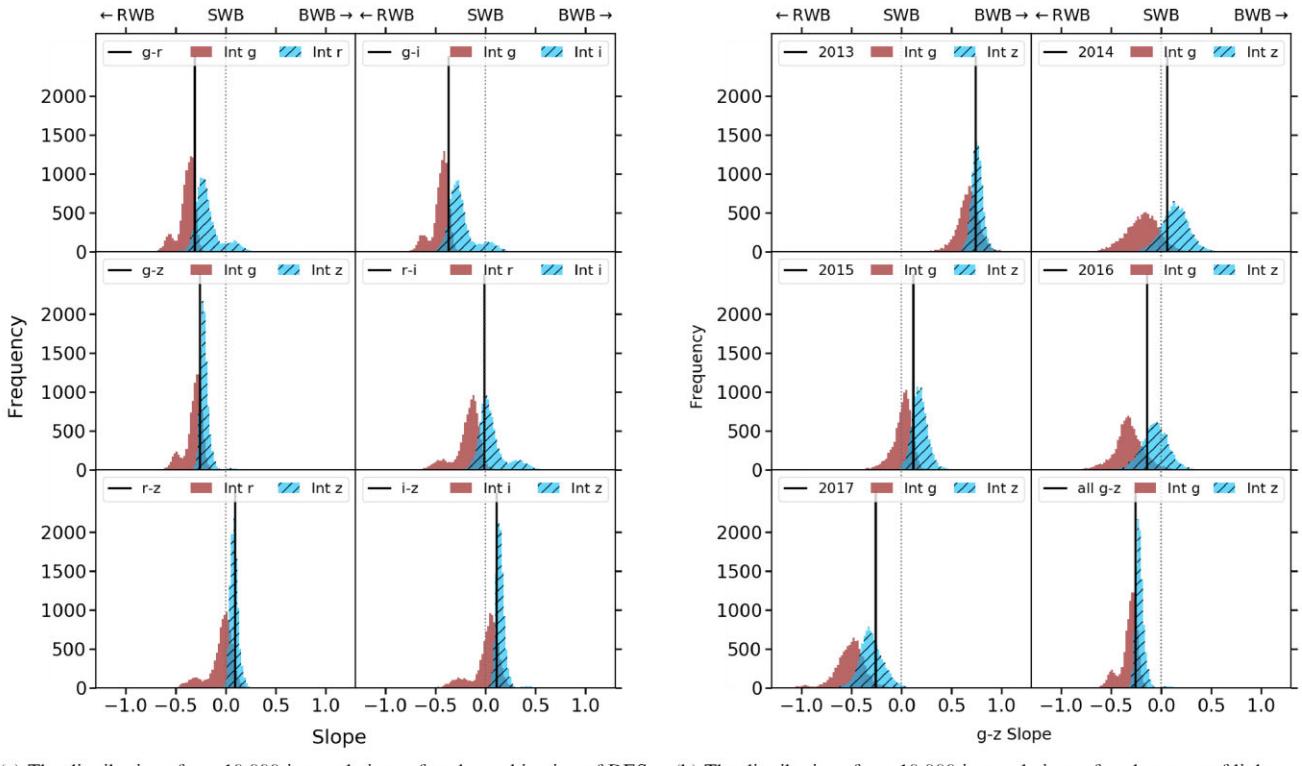
The optical and NIR light curves of PKS 0027-426 were cross correlated amongst themselves and with each other to determine possible lags between the light curves emission. In this paper, the  $r$  and  $i$ ,  $r$  and  $Ks$ , and  $J$  and  $Ks$  CCFs were discussed as representations of optical–optical, optical–NIR, and NIR–NIR correlations as they had the most observations.

Over each combination of filters, the most consistent correlation present was at  $\sim 0$  d, which implies that the emission is simultaneous or any time delay between the light curves is on time-scales less than the cadence of the surveys used (which have mean values of  $\sim 6$  d in the optical and  $\sim 11$  d in the NIR). Many studies of other blazars have also shown strong correlations between the optical and NIR light curves with time lags shorter than 1 d which implies that the source of the emission processes are co-spatial (e.g. Bonning et al. 2012; D’Ammando et al. 2013; Gupta et al. 2017; Kushwaha et al. 2017). This could be due to the synchrotron radiation in the inner jet originating in similar regions for the optical and NIR. As this possible detected lag is smaller than the cadences of observations, multiple intra-day observations would be necessary to further constrain it.

Longer lags have also been found between the optical and NIR light curves in other blazars, for example, Safna et al. (2020) found significant time delays for three FSRQs on the order of 10–100 d. Similarly, Li et al. (2018) found that the NIR light curves variations lagged the optical by a few weeks in PKS 0537-441. Additional non-zero lags were also measured for PKS 0027-426 inconsistently across the light curves, for example, in the 2017 season, when optical light curves were included in the cross-correlation, an observed lag of  $\sim \pm 75$  d (which corresponds to a rest frame lag of  $\sim \pm 50$  d) was often recorded. However, further analysis of these lags shows that they are unlikely to be a delay between the emission regions and instead are caused by aliasing in the light curves.

### 5.2 Spectral variability

The spectral variability of PKS 0027-426 was studied for each combination of optical and NIR light curves by calculating the slopes



(a) The distributions from 10,000 interpolations of each combination of DES light curves for their entire observational periods.

(b) The distributions from 10,000 interpolations of each season of light curve of  $g-z$ .

**Figure 9.** The distributions of the slopes returned from the colour–magnitude plots created from 10 000 interpolations of each light curve compared to the slopes measured from Fig. 8(a).

**Table 4.** Comparison between the slopes of the colour–magnitude plots and those made from 10 000 interpolated light curves. The uncertainties of the interpolated slopes are the  $1\sigma$  uncertainties.

| Colour Index | Actual slope     | Mean slope from Filter 1 | Mean slope from Filter 2 |
|--------------|------------------|--------------------------|--------------------------|
| $g-r$        | $-0.30 \pm 0.02$ | $-0.39 \pm 0.09$         | $-0.18 \pm 0.13$         |
| $g-i$        | $-0.36 \pm 0.02$ | $-0.45 \pm 0.09$         | $-0.24 \pm 0.14$         |
| $g-z$        | $-0.25 \pm 0.02$ | $-0.32 \pm 0.09$         | $-0.21 \pm 0.05$         |
| $r-i$        | $-0.06 \pm 0.01$ | $-0.18 \pm 0.13$         | $0.06 \pm 0.13$          |
| $r-z$        | $0.06 \pm 0.01$  | $-0.05 \pm 0.13$         | $0.09 \pm 0.05$          |
| $i-z$        | $0.12 \pm 0.01$  | $0.01 \pm 0.14$          | $0.15 \pm 0.05$          |

of colour versus magnitude plots, and was found to demonstrate a complex colour behaviour.

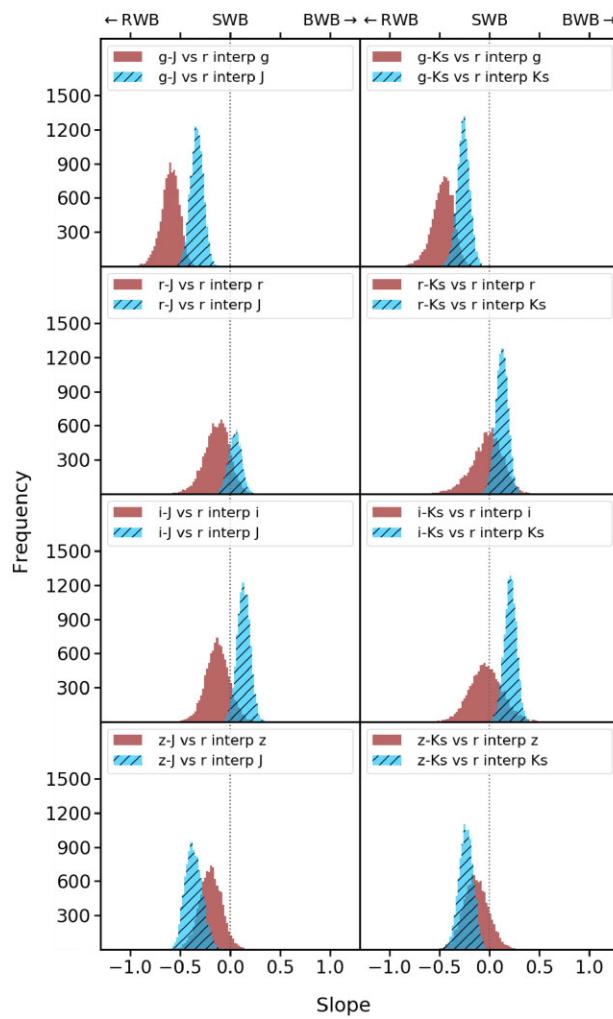
The colour trend for each combination of the DES  $griz$  filters, which could be studied directly due to the quasi-simultaneous observations, were shown to change both over time and depending on the colours used. For example, in the plot of  $g-z$  versus  $r$  band magnitude in Fig. 8(b), it changes from BWB in the 2013 season to SWB in the 2014 and 2015 seasons, and RWB in the 2016 and 2017 seasons. Furthermore, RWB, SWB, and BWB trends were observed simultaneously depending on the combination of filters used to calculate the colour, as shown in Fig. 8(a), for example, the overall colour behaviour of the  $g-r$ ,  $g-i$ ,  $g-z$ , and  $r-i$  demonstrates RWB trends, while the  $r-z$  and  $i-z$  follow a BWB trend.

The spectral behaviour of the observations from VEILS and VOILETTE could not be directly measured from their light curves as they were not observed even quasi-simultaneously. Instead, one of the light curves was interpolated so that epochs matching the

other light curve could be extracted. This method was first tested by comparing the mean colour versus  $r$  magnitude slopes measured by removing 50 per cent of the data and interpolating one of the DES light curves with the original slope measured for that colour, and was shown to be consistent for all DES colours across all seasons within  $1.5\sigma$  uncertainties. It was therefore used to obtain measurements of the optical–NIR spectral behaviour using VEILS and VOILETTE. It was found that the  $g-J$ ,  $g-Ks$ ,  $z-J$ , and  $z-Ks$  slopes for the 2017 season were negative withing  $5\sigma$ ,  $4\sigma$ ,  $1.7\sigma$ , and  $1\sigma$ , respectively, which indicates RWB behaviour. The remaining colours showed inconclusive trends within their uncertainties.

The possible colour trends observed in blazars have previously been explained independently. For example, a RWB colour behaviour could be explained in terms of the contribution of thermal emission from the accretion disc, which is more slowly varying than the variable jet emission (e.g. Bonning et al. 2012). Similarly, the BWB trend can be explained in terms of a faster varying blue component with a slower varying red component (e.g. Fiorucci et al. 2004). Alternatively, the BWB colour behaviour has been explained by a one component synchrotron model by Fiorucci et al. (2004), who suggest that the more intense the energy release, the higher the particle’s energy. Additionally, the BWB trend has been explained in terms of the shock-in-jet model, which suggests that accelerated electrons at the front of the shock lose energy while propagating away, and the higher frequency electrons lose energy faster due to synchrotron cooling therefore making the higher frequency bands more variable (e.g. Kirk et al. 1998; Agarwal et al. 2019).

The change in colour behaviour over different periods of time shown in Fig. 8(b) has similarly been seen by Bonning et al. (2012), who found that individual flares in other blazars can behave differ-



**Figure 10.** The distributions of the slope of the 2017–18 optical–NIR colour versus  $r$  magnitude plots returned from 10 000 interpolations of each light curve.

ently to the overall colour behaviours, which suggests that different jet components become important at different times. Furthermore, Raiteri et al. (2008) find that 3C 454.3 shows a RWB trend until the blazar reaches a saturation magnitude and turns into a BWB trend in bright states. In the  $g$ – $z$  colour–magnitude plots of PKS 0027-426, the 2016 and 2017 seasons are brighter than the earlier seasons and do demonstrate a different colour trend, but the 2013 season also follows a different colour behaviour while covering a similar magnitude range to the 2014 and 2015 seasons, which means a saturation magnitude is not likely to be the entire explanation in this scenario. Furthermore, while the 2016 and 2017 seasons demonstrate flares, the 2014 and 2015 seasons do not show any dramatic change in magnitude and yet still follow a SWB trend instead of the BWB trend in the 2013 seasons, thus implying individual flares are not solely responsible for the change in colour behaviour over time.

The varying colour behaviour in different combination of filters has also been observed in 3C 345 by Wu et al. (2011), who explained this phenomenon in terms of the emission features from the accretion disc or BLR, such as the Mg II line, which vary less than the non-thermal continuum and dominate the flux at the shorter wavelength (i.e.  $g$  band). This theory was investigated for PKS 0027-426 using

the spectra from OzDES that were observed over the same periods as DES.

### 5.2.1 Possible contamination of spectral variability from emission lines

Concurrent spectra of PKS 0027-426 were observed on 37 epochs with OzDES along side the photometric DES observations, so therefore the theory presented by Wu et al. (2011) could be examined. If emission features from the accretion disc varied less and dominated the flux, then it would be expected that synthesized light curves created from the emission lines in the  $g$  band would be shown to be less variable than both synthesized light curves from different sections of the continuum and the photometric light curves from DES.

To create synthesized light curves from emission lines within the spectra, they were first continuum subtracted. For example, the Mg II line is displayed in the upper panels of Fig. 11(a), and exists within a region of the spectra known as the small blue bump, in which the Fe II emission lines contribute substantially to the underlying continuum. The continuum was approximately subtracted from the Mg II line by fitting a line between points on either side of the emission line, depicted by the blue and red shaded regions, and subtracting this approximate continuum, depicted by the green line, from the spectra. The amplitude variability of the synthesized light curves were compared for emission lines in different filters and with synthesized light curves created from the continuum to then test whether the emission lines are less variable than the continuum emission. The fraction of the total flux in each synthesized DES band light curve that comes from the individual emission lines was also calculated to test whether the emission lines dominated in the filters.

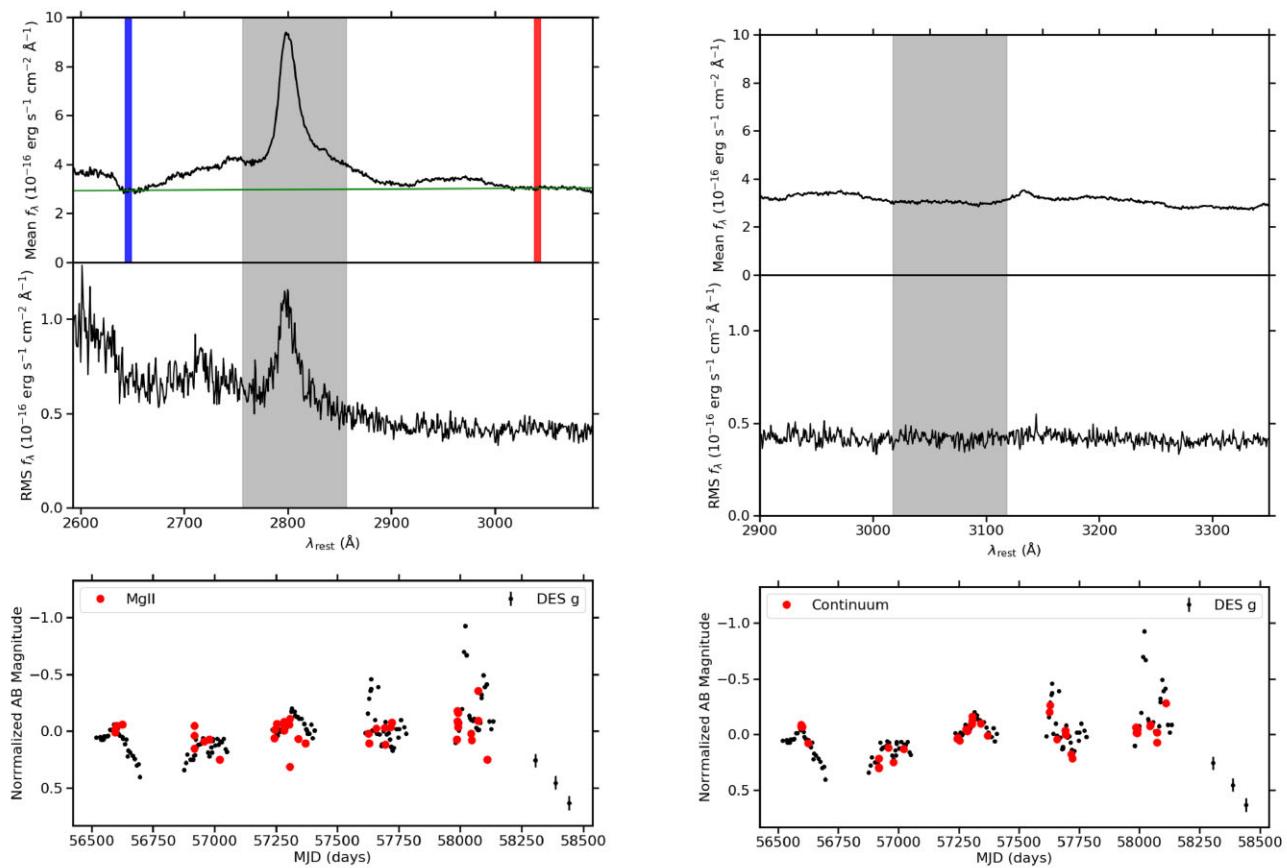
The lower panels of Figs 11(a) and (b) display the normalized light curves created for the Mg II line and a section of the continuum in the  $g$  band, respectively. It can be seen that the synthesized light curve from a section of the continuum follows similar variability to the photometric DES  $g$  band light curve, which is to be expected; however, the synthesized light curve from the continuum subtracted Mg II line varies differently to the photometric  $g$  band light curve. Furthermore, Table 5 contains the amplitude variations for the Mg II and blue continuum synthesized light curves, as well as from synthesized  $H\beta$  light curves. The light curves from the emission lines are shown to vary similarly to the continuum region and to the synthesized DES light curves. Furthermore, the Mg II line is more variable than the  $H\beta$  line, and the synthesized light curve from the blue continuum region, which disagrees with the theory presented by Wu et al. (2011) as they suggest that the Mg II line should be the least variable and should dominate in the  $g$  band. Table 5 also contains the percentage of the flux in each synthesized light curve that contributes to the overall flux of the synthesized DES light curves, and shows that the Mg II and  $H\beta$  emission lines contribute to 5 per cent of the overall flux.

### 5.2.2 Multiple contributing components to the overall emission

The differences in colour behaviour that occur simultaneously with different combination of optical  $griz$  filters could be explained by the multiple components that contribute to the overall optical emission.

#### 5.2.2.1 Decomposing the spectra into red and blue components

The change in spectral behaviour between different filter light curves could be explained by the presence of multiple different coloured components that contribute to the overall optical emission. The



(a) Mean and RMS Mg II spectra and synthesised light curve compared to the DES  $g$  band.

(b) Mean and RMS continuum spectra and synthesised light curve compared to the DES  $g$  band.

**Figure 11.** *Top panel:* The regions of OzDES spectra used to create the synthesized light curves (grey shaded regions). The Mg II line is continuum subtracted by fitting a line for the approximate continuum (green line) between points on either side of the emission line region (the blue and red shaded regions). *Middle panel:* RMS Spectra. *Lower panel:* Synthesized light curves created from spectra compared to the DES photometric light curves.

**Table 5.** The amplitude variations of the synthesized light curves created from OzDES spectra.

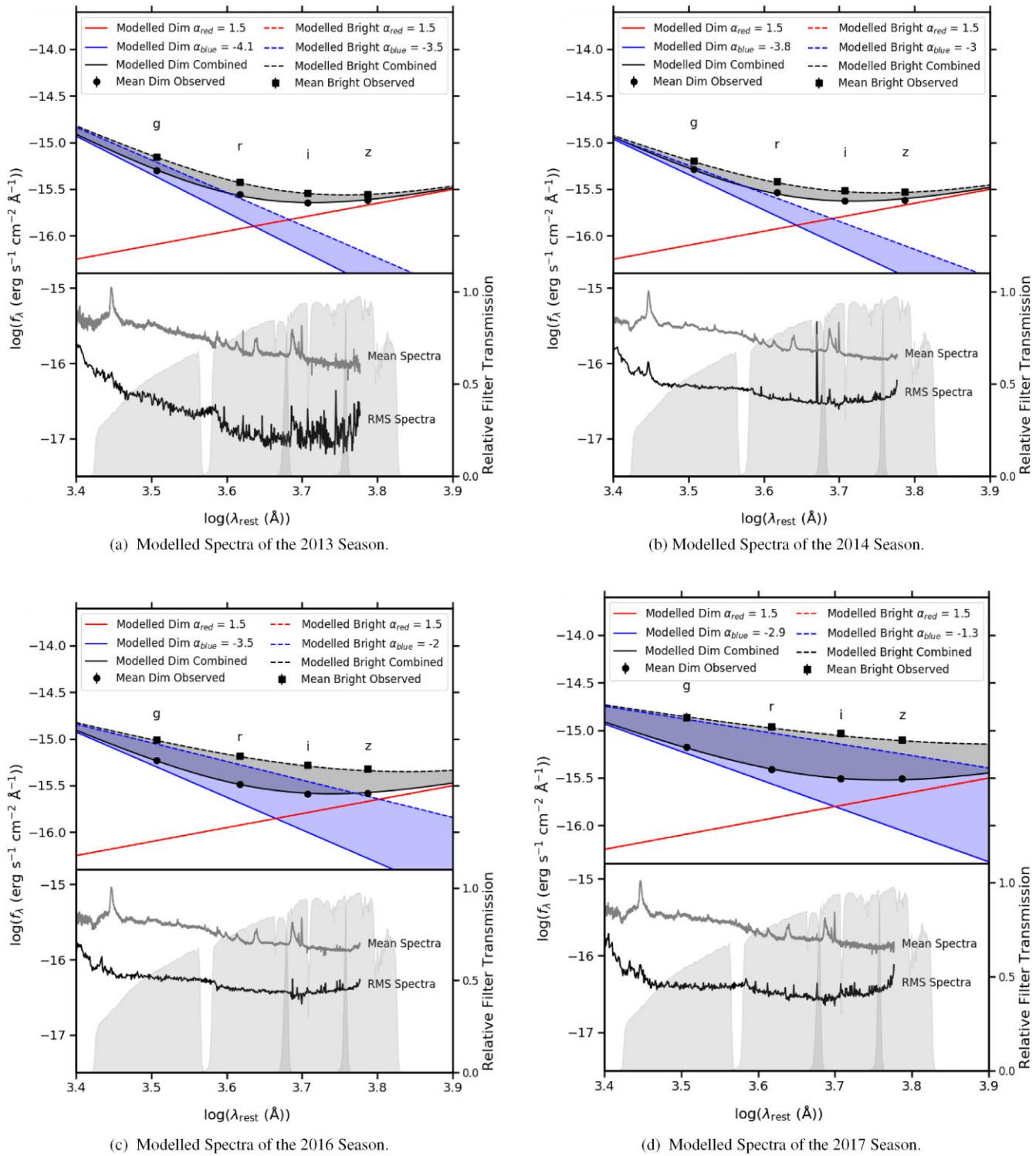
| Emission line or region of the spectra | Rest frame wavelength range (Å) | Amplitude variation (mag) | Percentage of total flux (per cent) |
|--|---------------------------------|---------------------------|-------------------------------------|
| Synthesized $g$ band                   | 2500–3780                       | 0.54                      | 100                                 |
| Synthesized $r$ band                   | 3620–4930                       | 0.79                      | 100                                 |
| Synthesized $i$ band                   | 4530–5830                       | 0.93                      | 100                                 |
| Mg II                                  | 2760–2860                       | 0.67                      | 5                                   |
| Blue continuum                         | 3020–3120                       | 0.59                      | 9                                   |
| $H\beta$                               | 4830–4930                       | 0.51                      | 5                                   |

different wavelength ranges could be dominated by a different coloured component which would mean when one component varies differently to the other, the colour behaviour will not follow the same trend for each combination of filters.

This was investigated using the optical broad-band spectra which were made using the optical DES light curves. The overall emission is assumed to follow a power law of  $f_\lambda \propto \lambda^{\alpha_\lambda}$ , where  $f_\lambda$  is the flux density at wavelength  $\lambda$  and  $\alpha_\lambda$  is the spectral index. The total flux here is assumed to be a combination of the flux from a red component and a blue component, which each follow their own power laws and have spectral indices of  $\alpha_{\text{red}}$  and  $\alpha_{\text{blue}}$ , respectively. The broad-band

spectra of the red and blue emission for each season were modelled and summed to match the shape of the average spectra of the three dimmest epochs that were observed within their  $1\sigma$  uncertainties. The spectral index of one of the components was then varied so that the new total spectra matched the shape of the average spectra of the brightest three epochs that were observed within their  $1\sigma$  uncertainties.

Fig. 12 displays the mean brightest and mean dimmest spectra of the  $griz$  bands in the seasons starting 2013, 2014, 2016, and 2017, along with examples of the modelled red and blue emission that are combined to fit the observed spectral shape. The 2015 season and the model over the entire DES observational period are displayed in Fig. C8. In these figures, the red emission was kept constant with the equation  $\log(f_\lambda) = 1.5 \log(\lambda_{\text{rest}}) - 21.35$ , where  $\alpha_{\text{red}} = 1.5$ , and the blue emission was varied to match the mean brightest spectra. The value of  $\alpha_{\text{red}}$  was chosen somewhat arbitrarily here to demonstrate how the change in the blue slope can effect the shape of the overall spectra; however, the value is not unique to the broad-band spectra as shown in Appendix C7, which explores alternative values including plots in which the blue slope is fixed and the red component is varied to match the change in spectra with brightness. The mean and RMS OzDES spectra of each season are plotted below for comparison. Table 6 gives the equations of the lines that are modelled for the blue and red components in each season to match the mean brightest and dimmest spectra. The change in the blue slope is shown to increase



**Figure 12.** *Upper panel:* Modelled broad-band spectra of the red and blue emission that combine to match the average brightest and dimmest epochs in each observation season compared to the observed broad-band spectra. The solid lines correspond to the modelled spectra of the dimmest epochs, and the dashed lines correspond to the modelled spectra of the brightest epochs. *Lower panel:* Mean and smoothed RMS OzDES spectra for each season plotted over the DES filter transmissions.

towards the later seasons where the object has previously been shown to be more variable in Table 1.

These simple models in Fig. 12 demonstrate that if one component is varying when the source gets brighter, the overall variability

observed between filters can be different due to the dominating emission process in each filter. For example, when the blue emission varies, the overall variation observed in the filters that are more strongly impacted by the red emission is diluted due to the strong

**Table 6.** The slopes (spectral indices,  $\alpha$ ) and intercepts (int) of the red and blue components that are modelled in Fig. 12 to match the mean observed brightest and dimmest broad-band spectra in each season.

| Season | $\alpha$ red | int red | $\alpha$ blue, dim | int blue, dim | $\alpha$ blue, bright | int blue, bright |
|--------|--------------|---------|--------------------|---------------|-----------------------|------------------|
| 2013   | 1.5          | -21.35  | -4.1               | -0.99         | -3.5                  | -2.94            |
| 2014   | 1.5          | -21.35  | -3.8               | -2.04         | -3                    | -4.75            |
| 2015   | 1.5          | -21.35  | -3.6               | -2.62         | -2.9                  | -4.98            |
| 2016   | 1.5          | -21.35  | -3.5               | -3.03         | -2                    | -8.04            |
| 2017   | 1.5          | -21.35  | -2.9               | -5.07         | -1.3                  | -10.33           |
| All    | 1.5          | -21.35  | -3.9               | -1.70         | -1.3                  | -10.33           |

constant red emission, whereas in the filters where the blue component dominates, the overall variability will better reflect the blue emission's variability, which could therefore explain why the colour behaviour has been shown to change between different combinations of optical filters.

The blue and red components used here could correspond to physical processes such as the thermal emission from the accretion disc and the synchrotron emission from the jet, respectively, as Wills et al. (1992) suggest that the thermal emission generally dominates in the optical-UV region; however, in FSRQs, when bright, the spectrum could be dominated by the synchrotron component towards the longer optical wavelengths and the IR. The spectral indices of the accretion disc and synchrotron emission from the jet have previously been predicted to be  $\alpha_{\lambda, \text{AD}} \approx -7/3$  (Kishimoto et al. 2008) and  $\alpha_{\lambda, \text{Sync}} \approx -0.5$  (Wills et al. 1992), which are not consistent with the steep slopes used in this analysis; however, Appendix C7 demonstrates that the values used for the red and blue slopes here are not unique. This analysis assumes the presence of only one variable component which may be oversimplifying it, so therefore, an alternative approach is applied in the following section.

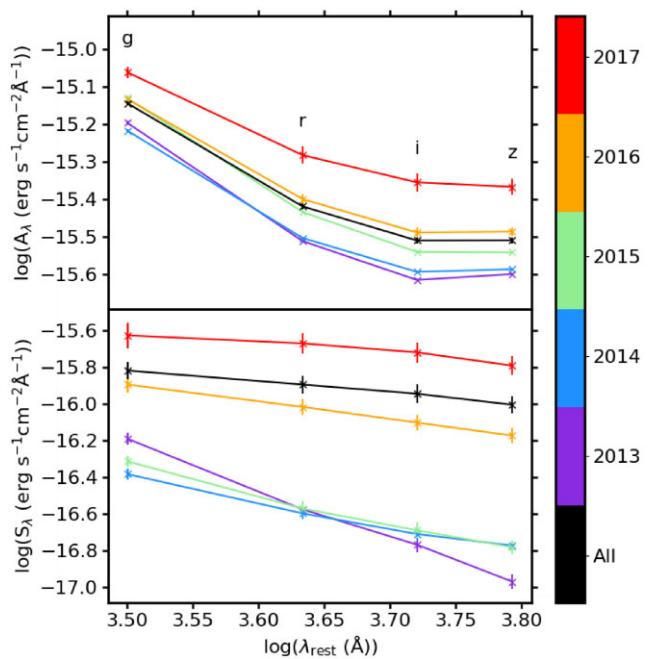
**5.2.2.2 Decomposing the spectra into the variable and non-variable components** The previous section assumes the presence of two different coloured components that contribute to the overall optical emission; however, it is simplified and only implies that one component varies while the other remains constant. To explore this further, the light curves in each wavelength range,  $f_{\lambda}(t)$ , are instead decomposed into the variable and non-variable components using the separable model given in equation (4).

$$f_{\lambda}(t) = A_{\lambda} + S_{\lambda} X(t), \quad (4)$$

where  $A_{\lambda}$  is the spectra of the mean light (i.e. the non-variable component),  $S_{\lambda}$  is the spectra of the variable component, and  $X(t)$  is the light curve that has been normalized such that  $\langle X(t) \rangle = 0$  and  $\langle X^2(t) \rangle = 1$ .

Fig. 13 displays the  $A_{\lambda}$  and  $S_{\lambda}$  spectra covering the DES *griz* filters in each observation season in DES and for the overall observation period, and Table 7 gives the slopes between each filter for the  $A_{\lambda}$  and  $S_{\lambda}$  spectra, where the slopes and uncertainties correspond to the mean slope and the standard deviation obtained from bootstrapping the light curves. Appendix C5 contains similar analysis for the OzDES spectra in each season.

The constant component,  $A_{\lambda}$ , is shown to follow roughly the same shape for each observations season, where the slope of  $\log(A_{\lambda})$  versus  $\log(\lambda)$  is steepest between the *g* and *r* bands and flattest between the *i* and *z* bands. This implies that there are multiple different coloured components that contribute to the non-variable emission, as there is a strong blue component effecting the *g* and *r* region of the spectra



**Figure 13.** Decomposition of the spectra into the variable ( $S_{\lambda}$ ) and non-variable ( $A_{\lambda}$ ) components for each season of DES and for the entire observational period.

**Table 7.** Slope of  $\log(A_{\lambda})$  and  $\log(S_{\lambda})$  versus  $\log(\lambda)$  from Fig. 13 between the *g-r*, *r-i*, and *i-z* filters for each season of DES and for the entire observational period.

| Season  | <i>g-r</i>       | <i>r-i</i>       | <i>i-z</i>       |
|---|------------------|------------------|------------------|
| (a) Slope of $\log(A_{\lambda})$ versus $\log(\lambda)$ from Fig. 13. |                  |                  |                  |
| 2013  | $-2.37 \pm 0.01$ | $-1.19 \pm 0.01$ | $0.22 \pm 0.01$  |
| 2014  | $-2.15 \pm 0.01$ | $-1.04 \pm 0.01$ | $0.09 \pm 0.01$  |
| 2015  | $-2.28 \pm 0.01$ | $-1.23 \pm 0.01$ | $-0.02 \pm 0.01$ |
| 2016  | $-2.00 \pm 0.02$ | $-1.03 \pm 0.02$ | $0.03 \pm 0.02$  |
| 2017  | $-1.66 \pm 0.03$ | $-0.84 \pm 0.03$ | $-0.17 \pm 0.03$ |
| All   | $-2.06 \pm 0.01$ | $-1.05 \pm 0.01$ | $0.01 \pm 0.01$  |
| (b) Slope of $\log(S_{\lambda})$ versus $\log(\lambda)$ from Fig. 13. |                  |                  |                  |
| 2013  | $-2.90 \pm 0.05$ | $-2.22 \pm 0.05$ | $-2.77 \pm 0.06$ |
| 2014  | $-1.61 \pm 0.05$ | $-1.29 \pm 0.05$ | $-0.83 \pm 0.05$ |
| 2015  | $-1.92 \pm 0.05$ | $-1.37 \pm 0.06$ | $-1.29 \pm 0.06$ |
| 2016  | $-0.92 \pm 0.06$ | $-0.99 \pm 0.06$ | $-0.98 \pm 0.06$ |
| 2017  | $-0.34 \pm 0.09$ | $-0.57 \pm 0.08$ | $-1.00 \pm 0.08$ |
| All   | $-0.57 \pm 0.07$ | $-0.58 \pm 0.07$ | $-0.83 \pm 0.07$ |

and a redder component that is flattening the spectra between the *r* and *i* and the *i* and *z* bands.

The slope of the variable component,  $S_{\lambda}$ , is also shown to change between seasons, with the 2013 season having the steepest slope between all filters and the 2017 season the flattest. The shape of the spectra here also indicates the presence of more than one spectral component, including a steep blue component but also a red component that contributes to the change of slope of the variable spectra with increasing wavelength in the later seasons.

This method of decomposing into the spectra into variable and non-variable components therefore supports the assumption in the previous section that both a blue and red spectral component contribute to the overall optical emission, but it also demonstrates

that both coloured components are likely to contribute to the overall variable and non-variable emission. The contribution of multiple different coloured components could therefore explain the change in colour behaviour that is observed simultaneously with different combinations of optical DES filters.

## 6 SUMMARY

We studied the multiwavelength temporal and spectral variability of the FSRQ PKS 0027-426, using optical observations from DES (2013–2018) and VOILETTE (2018–2019) in the *griz* bands, and NIR observations from VEILS (2017–2019) in the *JKs* bands. The results are summarized below:

(i) The temporal variability was studied using cross-correlation analysis of the optical and NIR light curves, and the most consistent correlation over all combination of light curves was found at  $\sim 0$  d, which implies that the emission is simultaneous or any delay between light curves occurs on time-scales smaller than the cadence of observations.

(ii) The spectral variability was studied for each combination of optical DES *griz* light curves using the slopes of the colour versus r magnitude plots. The overall colour trends are shown to vary when different combinations of filters are used, from RWB trends in the *g-r*, *g-i*, *g-z*, and *r-i* to BWB in the *r-z* and *i-z*.

(iii) The spectral variability was also shown to vary over each observation season; for example, in the *g-z*, the colour behaviour follows a BWB trend in the 2013 season, a SWB trend in the 2014 and 2015 seasons, and a RWB trend in the 2016 and 2017 seasons.

(iv) Using OzDES spectra from 2013–2018, we investigated the possible explanation for the changing colour behaviour with different combinations of filters provided by Wu et al. (2011) for 3C 345, in which emission features from the accretion disc or BLR dominate the flux at shorter wavelengths and vary less than the non-thermal continuum, and found that our results disagreed as the emission lines were not less variable than the continuum.

(v) The variations in colour behaviour across different combinations of filters was instead explained as a result of each filter containing a different ratio of the multiple different coloured components that combine to give the overall optical emission. These red and blue components are thought to vary differently, which could therefore cause the emission between filters to vary.

(vi) The optical and NIR spectral variability was also studied; however, as the observations were not simultaneous, one of the light curves was interpolated to extract matching epochs. This method was shown to be reliable for the DES data after half of the observations were removed, with consistent results given within  $1.5\sigma$  uncertainties.

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## DATA AVAILABILITY

The data underlying this article are available in the article and in its online supplementary material.

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## APPENDIX A: LIGHT CURVES

### A1 Calibrating the light curves of PKS 0027-426 with nearby non-varying objects

Nearby non-varying sources were used to calibrate the observations of PKS 0027-426 to create the light curves shown in Fig. 2. Table A1 contains the list of objects within the same detector that were used to correct the light curves of PKS 0027-426, including their position in RA and Dec (J2000), mean magnitude over the entire observational period in each filter, and standard deviation of the magnitudes in each night from the mean. The object had to be detected in every epoch observed for PKS 0027-426 for it to be included, which is why some objects were only used as reference stars in some of the filters. As the NIR observations contained inconsistencies across the detector, the non-varying objects used to correct the NIR light curves were further restricted to within  $\sim 200$  pixels of PKS 0027-426.

### A2 Light curve variability with VEILS flux–flux plots

Fig. A1(a) demonstrates a comparison between the flux in all DES  $r$ ,  $i$  and  $z$  bands and VEILS  $J$  and  $K_s$  bands with the DES  $g$  band flux in the season starting 2017. Each flux is shown to increase with increasing  $g$  band flux. The NIR light curves were not observed on the same epochs as the optical light curves therefore to create this plot, the NIR light curves were interpolated. To prevent the interpolations from impacting the results too much, the light curves were limited to the epochs greater than MJD 58044 as there is an  $\sim$  month long gap between observations in the NIR light curve during which a flare is present in the optical.

Fig. A1(b) displays the comparison between the DES  $g$  and  $z$  bands for each individual observation season. Although the relation over the entire observational season is not exactly linear, the individual seasons do look approximately linear. The slope is shown to get steeper over time, which supports the analysis of the spectral variability in Section 4 as in the later seasons of the  $g$ - $z$  plots, the redder filter ( $z$ ) becomes more variable as it gets brighter.

### A3 Mean cadences of each observation season

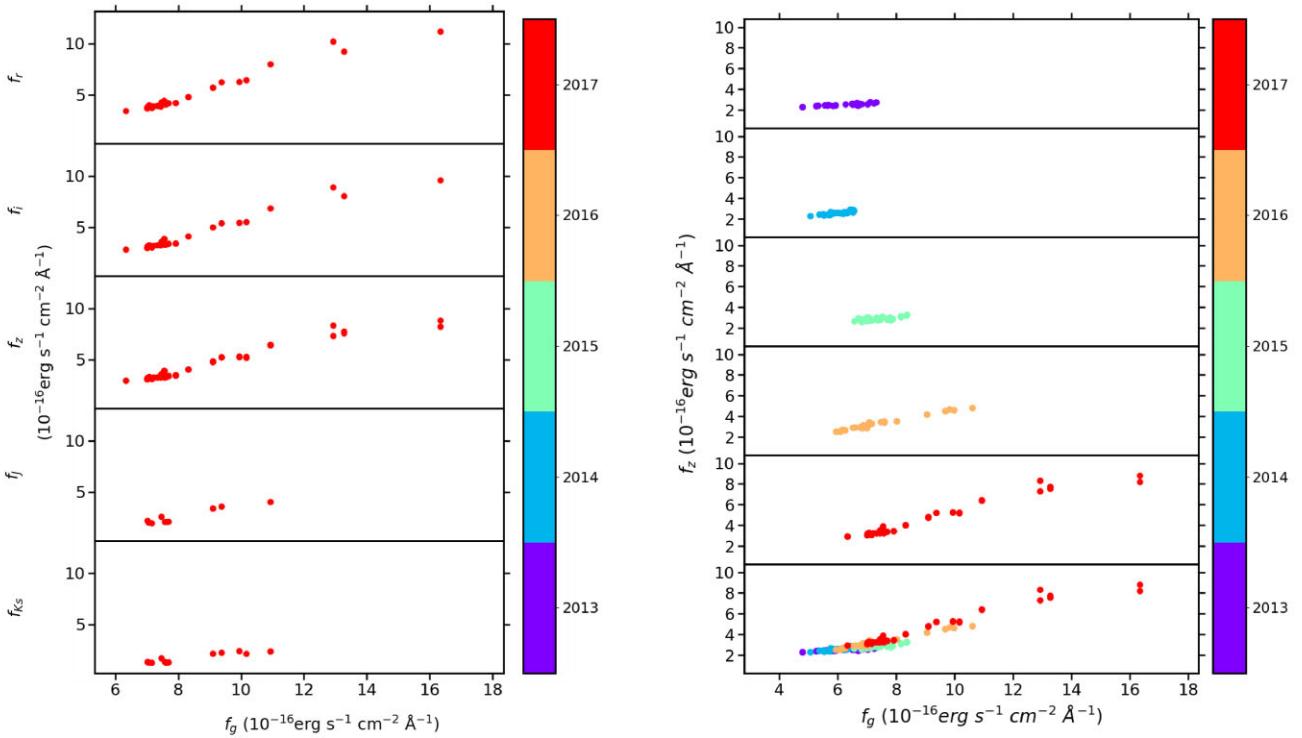
The mean cadence of each observation season in each filter is presented in Table A2. PKS 0027-426 was only observed three times in the  $g$  and  $z$  bands in the 2018 season, hence it has a much larger mean cadence.

**Table A1.** List of non-varying objects used to calibrate the light curves of PKS 0027-426.

| RA<br>(deg) | Dec<br>(deg) | Mean <i>g</i><br>mag | 1 $\sigma$<br>( <i>g</i> mag) | Mean <i>r</i><br>mag | 1 $\sigma$<br>( <i>r</i> mag) | Mean <i>i</i><br>mag | 1 $\sigma$<br>( <i>i</i> mag) | Mean <i>z</i><br>mag | 1 $\sigma$<br>( <i>z</i> mag) | Mean <i>J</i><br>mag | 1 $\sigma$<br>( <i>J</i> mag) | Mean <i>Ks</i><br>mag | 1 $\sigma$<br>( <i>Ks</i> mag) |
|-------------|--------------|----------------------|-------------------------------|----------------------|-------------------------------|----------------------|-------------------------------|----------------------|-------------------------------|----------------------|-------------------------------|-----------------------|--------------------------------|
| 7.50        | -42.41       | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | 18.91                | 0.02                          | -                     | -                              |
| 7.51        | -42.43       | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | 19.06                | 0.02                          | -                     | -                              |
| 7.51        | -42.44       | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | 19.61                | 0.03                          | -                     | -                              |
| 7.51        | -42.37       | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | 19.58                | 0.02                          | -                     | -                              |
| 7.53        | -42.41       | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | 17.10                 | 0.03                           |
| 7.53        | -42.44       | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | 18.86                | 0.02                          | 19.08                 | 0.04                           |
| 7.54        | -42.38       | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | 20.20                | 0.03                          | -                     | -                              |
| 7.54        | -42.35       | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | 18.58                | 0.02                          | -                     | -                              |
| 7.54        | -42.42       | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | 18.33                | 0.02                          | 18.52                 | 0.04                           |
| 7.55        | -42.43       | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | 16.74                 | 0.03                           |
| 7.55        | -42.38       | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | 19.52                | 0.02                          | 19.85                 | 0.13                           |
| 7.56        | -42.50       | -                    | -                             | 18.48                | 0.09                          | 18.19                | 0.09                          | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.56        | -42.40       | 20.75                | 0.03                          | 20.32                | 0.07                          | -                    | -                             | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.56        | -42.51       | -                    | -                             | 18.38                | 0.07                          | 17.84                | 0.08                          | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.57        | -42.58       | -                    | -                             | 20.59                | 0.09                          | 19.78                | 0.11                          | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.57        | -42.49       | -                    | -                             | -                    | -                             | 20.28                | 0.10                          | 20.17                | 0.04                          | -                    | -                             | -                     | -                              |
| 7.57        | -42.41       | 20.67                | 0.05                          | 20.06                | 0.07                          | 19.80                | 0.08                          | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.57        | -42.44       | -                    | -                             | -                    | -                             | -                    | -                             | 20.51                | 0.04                          | -                    | -                             | -                     | -                              |
| 7.57        | -42.53       | 19.90                | 0.06                          | 19.77                | 0.05                          | 19.66                | 0.05                          | 19.50                | 0.04                          | -                    | -                             | -                     | -                              |
| 7.57        | -42.39       | -                    | -                             | 18.00                | 0.06                          | 17.70                | 0.05                          | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.57        | -42.55       | 17.91                | 0.03                          | 18.88                | 0.06                          | 17.56                | 0.06                          | 17.02                | 0.02                          | -                    | -                             | -                     | -                              |
| 7.57        | -42.34       | -                    | -                             | 17.31                | 0.05                          | 17.04                | 0.05                          | 18.64                | 0.05                          | -                    | -                             | -                     | -                              |
| 7.58        | -42.52       | 18.48                | 0.01                          | 20.77                | 0.13                          | 20.22                | 0.10                          | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.58        | -42.61       | 19.88                | 0.09                          | 18.02                | 0.05                          | -                    | -                             | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.58        | -42.56       | -                    | -                             | 18.22                | 0.10                          | 17.79                | 0.03                          | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.58        | -42.34       | -                    | -                             | 19.78                | 0.05                          | 17.10                | 0.13                          | 18.93                | 0.04                          | 18.41                | 0.02                          | -                     | -                              |
| 7.58        | -42.60       | -                    | -                             | -                    | -                             | 19.13                | 0.05                          | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.59        | -42.53       | -                    | -                             | 20.70                | 0.12                          | 19.47                | 0.04                          | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.59        | -42.46       | -                    | -                             | 20.79                | 0.04                          | 20.31                | 0.18                          | 20.48                | 0.11                          | -                    | -                             | -                     | -                              |
| 7.59        | -42.55       | -                    | -                             | -                    | -                             | -                    | -                             | 19.32                | 0.02                          | -                    | -                             | -                     | -                              |
| 7.59        | -42.59       | -                    | -                             | -                    | -                             | -                    | -                             | 17.63                | 0.01                          | -                    | -                             | -                     | -                              |
| 7.59        | -42.34       | -                    | -                             | 19.51                | 0.07                          | 19.76                | 0.04                          | 20.37                | 0.07                          | -                    | -                             | -                     | -                              |
| 7.59        | -42.54       | 20.61                | 0.03                          | 20.59                | 0.06                          | 18.24                | 0.07                          | 20.19                | 0.06                          | -                    | -                             | -                     | -                              |
| 7.60        | -42.34       | -                    | -                             | -                    | -                             | -                    | -                             | 19.95                | 0.03                          | -                    | -                             | -                     | -                              |
| 7.60        | -42.44       | 20.06                | 0.01                          | 20.88                | 0.06                          | 20.27                | 0.06                          | 18.51                | 0.02                          | -                    | -                             | -                     | -                              |
| 7.60        | -42.59       | -                    | -                             | 19.28                | 0.06                          | 18.73                | 0.06                          | 19.25                | 0.03                          | -                    | -                             | -                     | -                              |
| 7.60        | -42.60       | -                    | -                             | -                    | -                             | -                    | -                             | 17.21                | 0.00                          | -                    | -                             | -                     | -                              |
| 7.61        | -42.50       | 20.77                | 0.01                          | 18.51                | 0.02                          | -                    | -                             | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.61        | -42.45       | -                    | -                             | 20.09                | 0.07                          | 19.05                | 0.09                          | 18.92                | 0.09                          | -                    | -                             | -                     | -                              |
| 7.61        | -42.62       | 20.54                | 0.01                          | 20.74                | 0.27                          | 19.52                | 0.14                          | 18.67                | 0.01                          | -                    | -                             | -                     | -                              |
| 7.61        | -42.34       | 20.21                | 0.02                          | 19.46                | 0.03                          | 18.91                | 0.02                          | 19.01                | 0.01                          | -                    | -                             | -                     | -                              |
| 7.61        | -42.43       | -                    | -                             | 19.99                | 0.03                          | 19.32                | 0.02                          | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.61        | -42.35       | 17.73                | 0.01                          | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.61        | -42.32       | -                    | -                             | 19.41                | 0.06                          | -                    | -                             | 19.99                | 0.08                          | -                    | -                             | -                     | -                              |
| 7.61        | -42.42       | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.62        | -42.51       | -                    | -                             | 20.98                | 0.05                          | -                    | -                             | 19.82                | 0.03                          | -                    | -                             | -                     | -                              |
| 7.62        | -42.45       | 18.56                | 0.02                          | 17.27                | 0.05                          | 20.44                | 0.12                          | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.62        | -42.59       | -                    | -                             | -                    | -                             | 19.47                | 0.02                          | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.62        | -42.32       | 19.37                | 0.04                          | 20.77                | 0.04                          | 18.34                | 0.02                          | 18.03                | 0.02                          | -                    | -                             | -                     | -                              |
| 7.62        | -42.55       | 19.57                | 0.02                          | 18.68                | 0.04                          | 18.01                | 0.02                          | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.63        | -42.38       | 20.42                | 0.04                          | 18.19                | 0.02                          | 18.68                | 0.10                          | 18.42                | 0.02                          | -                    | -                             | -                     | -                              |
| 7.63        | -42.33       | -                    | -                             | 18.95                | 0.10                          | -                    | -                             | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.63        | -42.47       | -                    | -                             | -                    | -                             | 18.13                | 0.04                          | 16.74                | 0.03                          | -                    | -                             | -                     | -                              |
| 7.63        | -42.58       | 17.49                | 0.02                          | 18.57                | 0.05                          | 17.39                | 0.03                          | 20.08                | 0.06                          | -                    | -                             | -                     | -                              |
| 7.63        | -42.51       | 18.52                | 0.02                          | 18.79                | 0.04                          | -                    | -                             | 20.40                | 0.10                          | -                    | -                             | -                     | -                              |
| 7.63        | -42.28       | 18.38                | 0.05                          | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.64        | -42.34       | -                    | -                             | -                    | -                             | 16.42                | 0.07                          | 17.65                | 0.02                          | -                    | -                             | -                     | -                              |
| 7.64        | -42.31       | -                    | -                             | 16.72                | 0.08                          | 17.69                | 0.01                          | 16.60                | 0.04                          | -                    | -                             | -                     | -                              |
| 7.65        | -42.57       | -                    | -                             | 17.94                | 0.02                          | -                    | -                             | 17.99                | 0.01                          | -                    | -                             | -                     | -                              |
| 7.65        | -42.35       | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.65        | -42.36       | -                    | -                             | -                    | -                             | 19.50                | 0.06                          | -                    | -                             | -                    | -                             | -                     | -                              |
| 7.66        | -42.59       | 19.09                | 0.03                          | -                    | -                             | 20.19                | 0.09                          | 16.92                | 0.02                          | -                    | -                             | -                     | -                              |
| 7.66        | -42.41       | -                    | -                             | -                    | -                             | 16.96                | 0.04                          | -                    | -                             | -                    | -                             | -                     | -                              |

Table A1 – continued

| RA<br>(deg) | Dec<br>(deg) | Mean <i>g</i><br>mag | 1 $\sigma$<br>( <i>g</i> mag) | Mean <i>r</i><br>mag | 1 $\sigma$<br>( <i>r</i> mag) | Mean <i>i</i><br>mag | 1 $\sigma$<br>( <i>i</i> mag) | Mean <i>z</i><br>mag | 1 $\sigma$<br>( <i>z</i> mag) | Mean <i>J</i><br>mag | 1 $\sigma$<br>( <i>J</i> mag) | Mean <i>Ks</i><br>mag | 1 $\sigma$<br>( <i>Ks</i> mag) |
|-------------|--------------|----------------------|-------------------------------|----------------------|-------------------------------|----------------------|-------------------------------|----------------------|-------------------------------|----------------------|-------------------------------|-----------------------|--------------------------------|
| 7.66        | –42.36       | 19.10                | 0.01                          | 17.23                | 0.05                          | 18.47                | 0.03                          | –                    | –                             | –                    | –                             | –                     | –                              |
| 7.66        | –42.31       | –                    | –                             | 18.86                | 0.04                          | 17.21                | 0.08                          | 19.36                | 0.01                          | –                    | –                             | –                     | –                              |
| 7.66        | –42.40       | 19.86                | 0.03                          | 17.77                | 0.07                          | 20.10                | 0.03                          | –                    | –                             | –                    | –                             | –                     | –                              |
| 7.66        | –42.44       | –                    | –                             | –                    | –                             | 16.82                | 0.03                          | –                    | –                             | –                    | –                             | –                     | –                              |
| 7.66        | –42.51       | 19.53                | 0.02                          | 17.61                | 0.04                          | 16.69                | 0.06                          | 19.09                | 0.00                          | –                    | –                             | –                     | –                              |
| 7.67        | –42.43       | 20.61                | 0.05                          | –                    | –                             | 19.10                | 0.01                          | –                    | –                             | –                    | –                             | –                     | –                              |
| 7.67        | –42.51       | –                    | –                             | 19.36                | 0.02                          | 19.59                | 0.03                          | 16.40                | 0.02                          | –                    | –                             | –                     | –                              |
| 7.68        | –42.46       | 21.06                | 0.06                          | 20.75                | 0.02                          | 16.87                | 0.02                          | 16.36                | 0.01                          | –                    | –                             | –                     | –                              |
| 7.68        | –42.28       | –                    | –                             | 17.90                | 0.04                          | 16.37                | 0.01                          | –                    | –                             | –                    | –                             | –                     | –                              |
| 7.69        | –42.55       | 21.17                | 0.06                          | 16.59                | 0.03                          | 18.12                | 0.02                          | 19.05                | 0.01                          | –                    | –                             | –                     | –                              |
| 7.69        | –42.50       | –                    | –                             | 19.09                | 0.02                          | 19.33                | 0.03                          | 18.31                | 0.01                          | –                    | –                             | –                     | –                              |
| 7.69        | –42.32       | 18.17                | 0.03                          | 19.96                | 0.03                          | 18.71                | 0.02                          | 19.42                | 0.04                          | –                    | –                             | –                     | –                              |
| 7.70        | –42.50       | 18.85                | 0.01                          | 19.58                | 0.02                          | –                    | –                             | –                    | –                             | –                    | –                             | –                     | –                              |
| 7.70        | –42.41       | 17.75                | 0.00                          | –                    | –                             | –                    | –                             | 19.18                | 0.02                          | –                    | –                             | –                     | –                              |
| 7.70        | –42.37       | –                    | –                             | 20.87                | 0.06                          | 19.35                | 0.02                          | 17.93                | 0.02                          | –                    | –                             | –                     | –                              |
| 7.70        | –42.43       | –                    | –                             | 19.77                | 0.02                          | 19.40                | 0.05                          | 16.83                | 0.01                          | –                    | –                             | –                     | –                              |
| 7.70        | –42.44       | 20.83                | 0.04                          | –                    | –                             | 17.87                | 0.06                          | –                    | –                             | –                    | –                             | –                     | –                              |
| 7.70        | –42.40       | –                    | –                             | 17.55                | 0.03                          | 17.04                | 0.02                          | 19.16                | 0.03                          | –                    | –                             | –                     | –                              |
| 7.71        | –42.49       | 18.93                | 0.00                          | 17.22                | 0.02                          | 16.96                | 0.02                          | 19.26                | 0.05                          | –                    | –                             | –                     | –                              |
| 7.71        | –42.39       | –                    | –                             | –                    | –                             | 19.99                | 0.05                          | 20.46                | 0.07                          | –                    | –                             | –                     | –                              |
| 7.71        | –42.30       | –                    | –                             | 20.49                | 0.04                          | –                    | –                             | –                    | –                             | –                    | –                             | –                     | –                              |
| 7.71        | –42.32       | –                    | –                             | 20.58                | 0.04                          | –                    | –                             | –                    | –                             | –                    | –                             | –                     | –                              |
| 7.72        | –42.31       | –                    | –                             | 20.75                | 0.05                          | 20.16                | 0.05                          | 18.38                | 0.03                          | –                    | –                             | –                     | –                              |
| 7.72        | –42.33       | 17.31                | 0.02                          | 17.50                | 0.03                          | 16.76                | 0.03                          | –                    | –                             | –                    | –                             | –                     | –                              |
| 7.74        | –42.50       | –                    | –                             | 18.65                | 0.04                          | 18.41                | 0.03                          | –                    | –                             | –                    | –                             | –                     | –                              |
| 7.74        | –42.42       | –                    | –                             | –                    | –                             | 19.77                | 0.15                          | 18.18                | 0.01                          | –                    | –                             | –                     | –                              |



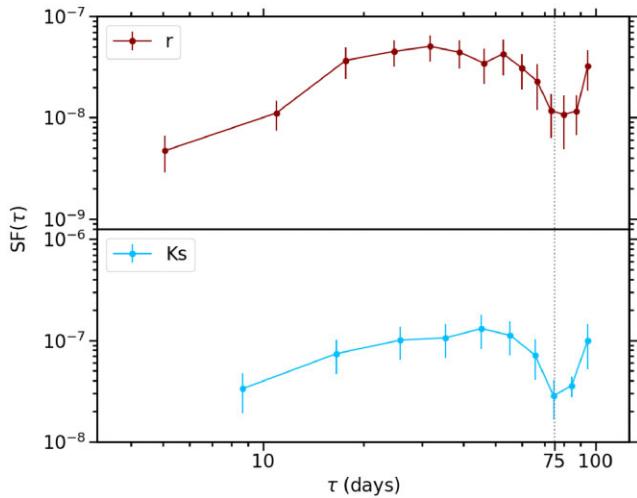
(a) Flux variations in each DES and VEILS filter compared to the DES *g* band for the 2017 season. The NIR light curves were interpolated to extract simultaneous data to the DES *g* band observations.

(b) Flux variations in the DES *z* band compared to the DES *g* band for each season season.

Figure A1. Flux variations in the different filters compared to the DES *g* band.

**Table A2.** The mean cadences of observations of PKS 0027-426 each season for each filter, where the uncertainty is the standard deviation.

| Year starting | <i>g</i> (nights) | <i>r</i> (nights) | <i>i</i> (nights) | <i>z</i> (nights) | <i>J</i> (nights) | <i>Ks</i> (nights) |
|---------------|-------------------|-------------------|-------------------|-------------------|-------------------|--------------------|
| 2013          | $6.5 \pm 3.0$     | $6.5 \pm 3.0$     | $6.5 \pm 3.0$     | $5.5 \pm 3.0$     | –                 | –                  |
| 2014          | $6.2 \pm 2.9$     | $6.2 \pm 2.9$     | $6.4 \pm 3.0$     | $6.2 \pm 2.6$     | –                 | –                  |
| 2015          | $5.7 \pm 2.7$     | $5.5 \pm 2.9$     | $5.9 \pm 3.2$     | $5.5 \pm 2.9$     | –                 | –                  |
| 2016          | $5.7 \pm 3.0$     | $5.7 \pm 2.7$     | $5.3 \pm 2.9$     | $5.3 \pm 2.9$     | –                 | –                  |
| 2017          | $6.1 \pm 2.2$     | $6.1 \pm 2.2$     | $6.1 \pm 2.2$     | $6.1 \pm 2.2$     | $12.2 \pm 10.5$   | $11.7 \pm 6.6$     |
| 2018          | $68.9 \pm 14.9$   | $12.9 \pm 14.4$   | $12.8 \pm 11.3$   | $68.8 \pm 14.9$   | $10.3 \pm 4.3$    | $10.9 \pm 5.0$     |



**Figure B1.** Structure functions of PKS 0027-426 from the *r* and *Ks* band combined 2017 and 2018 light curves.

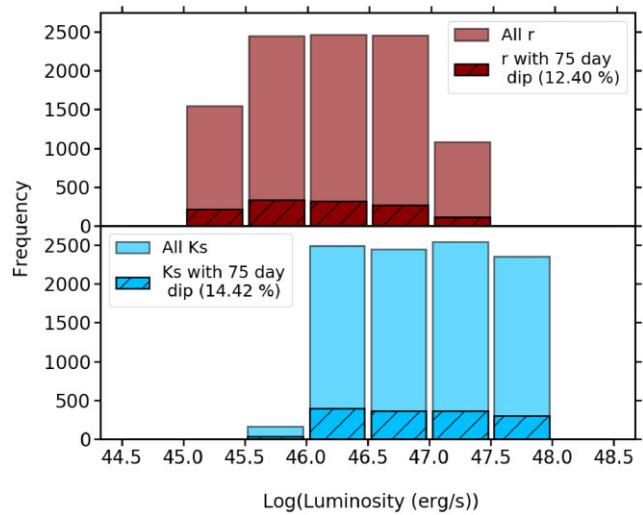
## APPENDIX B: TEMPORAL VARIABILITY

### B1 More CCFs of the individual observation seasons

The *r* and *i* band CCFs of the individual seasons starting 2013–2016 and 2018 are displayed in Fig. B3 for each CCF method, along with their corresponding ACFs. Each CCF detects a correlation at  $\sim 0$  d, except the 2016 season which instead contains a small peak at  $\sim 0$  d with a value of less than 0.5 in the S-ICCF and M-ICCF methods, and was therefore not counted. The CCFs from 2016 are relatively level, especially in the S-ICCF method, implying that there is no distinctive lag observed in this season, which could be due to the shape of the 2016 light curves, which contain multiple peaks and troughs that would all correlate with each other. The 2018 season CCFs of the *J* and *Ks* band light curves and the *r* and *Ks* band light curves are displayed in Figs B4 and B5, respectively.

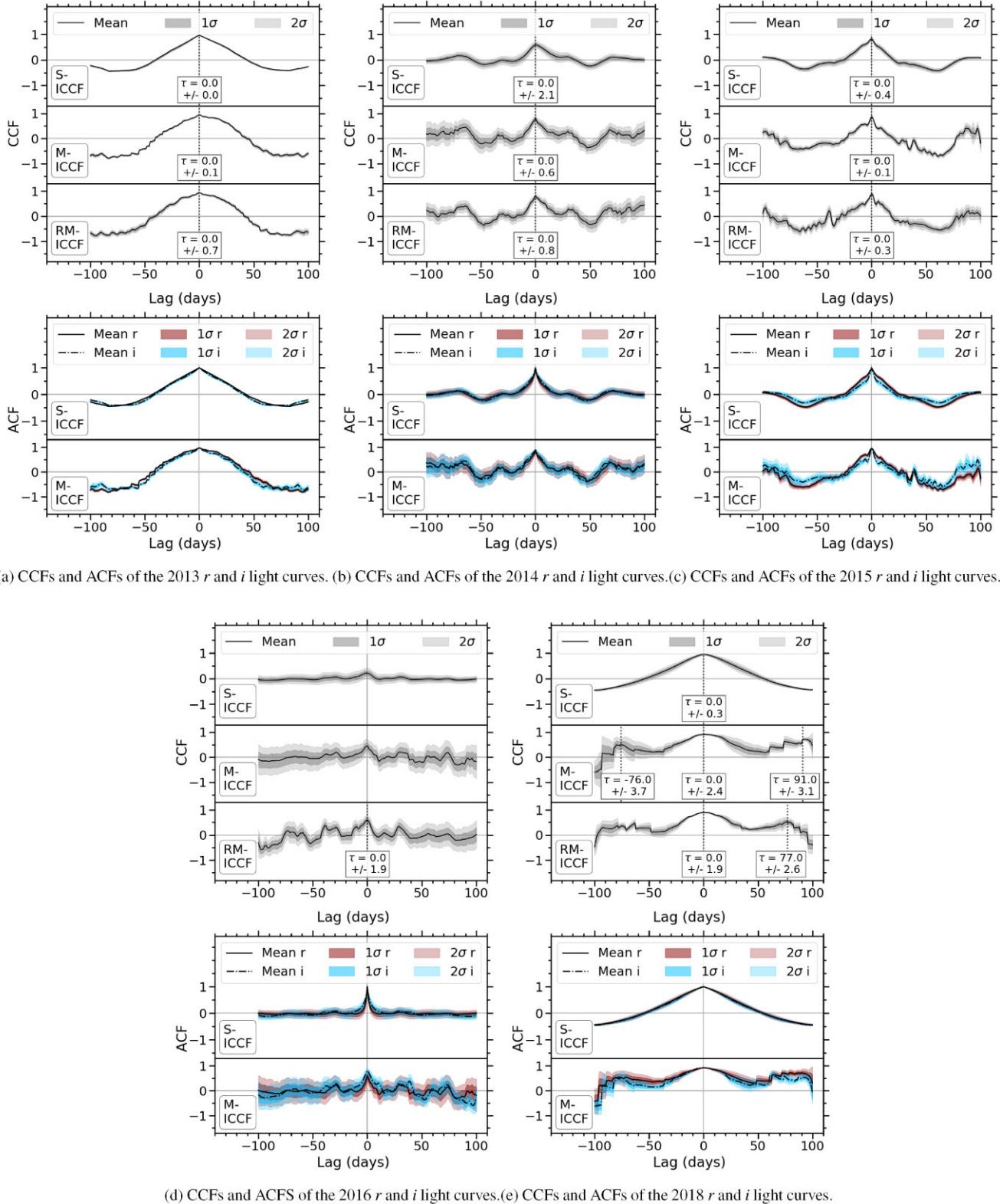
### B2 Investigating the possible 75-d lag between light curves

In multiple CCFs a possible lag is detected at  $\sim \pm 75$  d which appears to be due to aliasing. This lag was further investigated by analysing the *r* and *Ks* band SFs from observations between 2017–2019, which

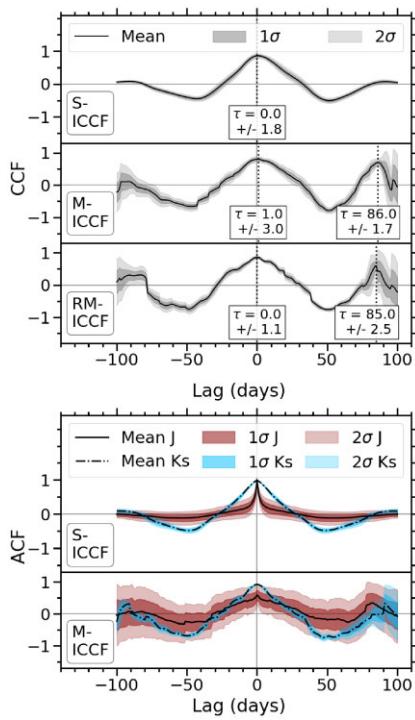


**Figure B2.** Comparisons between the distributions of the luminosity corresponding to the structure functions from the simulated light curves that demonstrate a dip at  $\sim 75$  d with all simulated light curves in *r* and *Ks* bands.

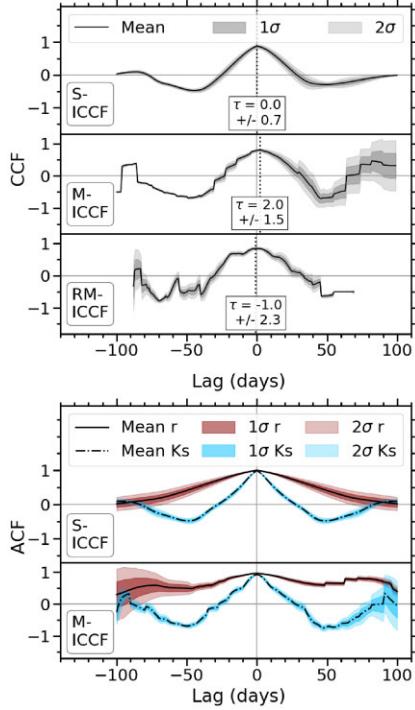
are displayed in Fig. B1, in which an obvious dip is seen at  $\sim 75$  d in both filters. To test whether or not this dip in the SFs was intrinsic to PKS 0027-426, light curves were simulated using the method described by Timmer & Koenig (1995), in which a power spectrum is created from the data and is used to produce light curves with similar variability and noise as the data. 10 000 light curves were created using this method for a range of power spectra with varied break frequencies, slopes, and white noise amplitudes, created by varying properties of PKS 0027-426 including the luminosity and Eddington luminosity (Kelly, Sobolewska & Siemiginowska 2011). The percentage of the SFs from these light curves that also displayed a dip at  $\sim 75$  d were found to be  $\sim 12$  per cent and  $\sim 14$  per cent in *r* and *Ks* bands, respectively. Furthermore, the distributions of the SFs with varied inputs that returned the dip at  $\sim 75$  d were plotted and compared to the distribution of SFs from all simulated light curves. The shape was shown to be similar for each value of luminosity in Fig. B2, which therefore implied that the  $\sim 75$ -d dip did not depend on specific properties of the light curve of PKS 0027-426, but occurred for a random  $\sim 12$  per cent.



**Figure B3.** *Top panels:* Mean CCFs of the  $r$  and  $i$  light curves of the individual years of PKS 0027-426 between 2013–2016 and 2018, made using each method of CCF. *Lower panels:* The corresponding ACFs. In these CCFs, the M-ICCF method refers to the interpolated  $r$  band, and the RM-ICCF method refers to the interpolated  $i$  band. Potential lags corresponding to peak in the mean CCF are labelled, with the uncertainties calculated as the standard deviation of the peak in each CCF around the peak of the mean CCF.



**Figure B4.** Top panels: Mean CCFs of the  $J$  and  $Ks$  light curves of the 2018 season, made using each method of CCF. Lower panels: The corresponding ACFs. In these CCFs, the M-ICCF method refers to the interpolated  $J$  band, and the RM-ICCF method refers to the interpolated  $Ks$  band.



**Figure B5.** Top panels: Mean CCFs of the  $r$  and  $Ks$  light curves of the 2018 season, made using each method of CCF. Lower panels: The corresponding ACFs. In these CCFs, the M-ICCF method refers to the interpolated  $r$  band, and the RM-ICCF method refers to the interpolated  $Ks$  band.

## APPENDIX C: SPECTRAL VARIABILITY

### C1 DES colour–magnitude plots for individual observation seasons

The optical colour–magnitude plots for each season of each combination of DES  $griz$  filters,  $g-r$ ,  $g-i$ ,  $r-z$ , and  $i-z$  are plotted in Fig. C1, and the corresponding tables containing the slopes, Spearman rank correlation coefficients, and probability of no correlation are given in Table C1, to demonstrate how the spectral behaviour changes over time. These colour–magnitude plots are made excluding the outliers that are displayed in Fig. C2 for the 2013–2016 seasons of DES, and the corresponding differences in slope between when the outliers are included and excluded is given in Table C2.

### C2 Colour–magnitude plots from interpolating DES light curves

Fig. C3 further demonstrates the consistency between calculating the slope of the colour versus  $r$  magnitude plots from DES using quasi-simultaneous observations,  $S_{\text{Act}}$ , and calculating the slope of each interpolated light curve which have had 50 per cent of the data points removed,  $S_{\text{Interp}}$ , using  $\Delta S$ :

$$\Delta S = S_{\text{Act}} - S_{\text{Interp}} \quad (\text{C1})$$

### C3 Optical–NIR colour–magnitude plots from 2017–18, with gap in observations

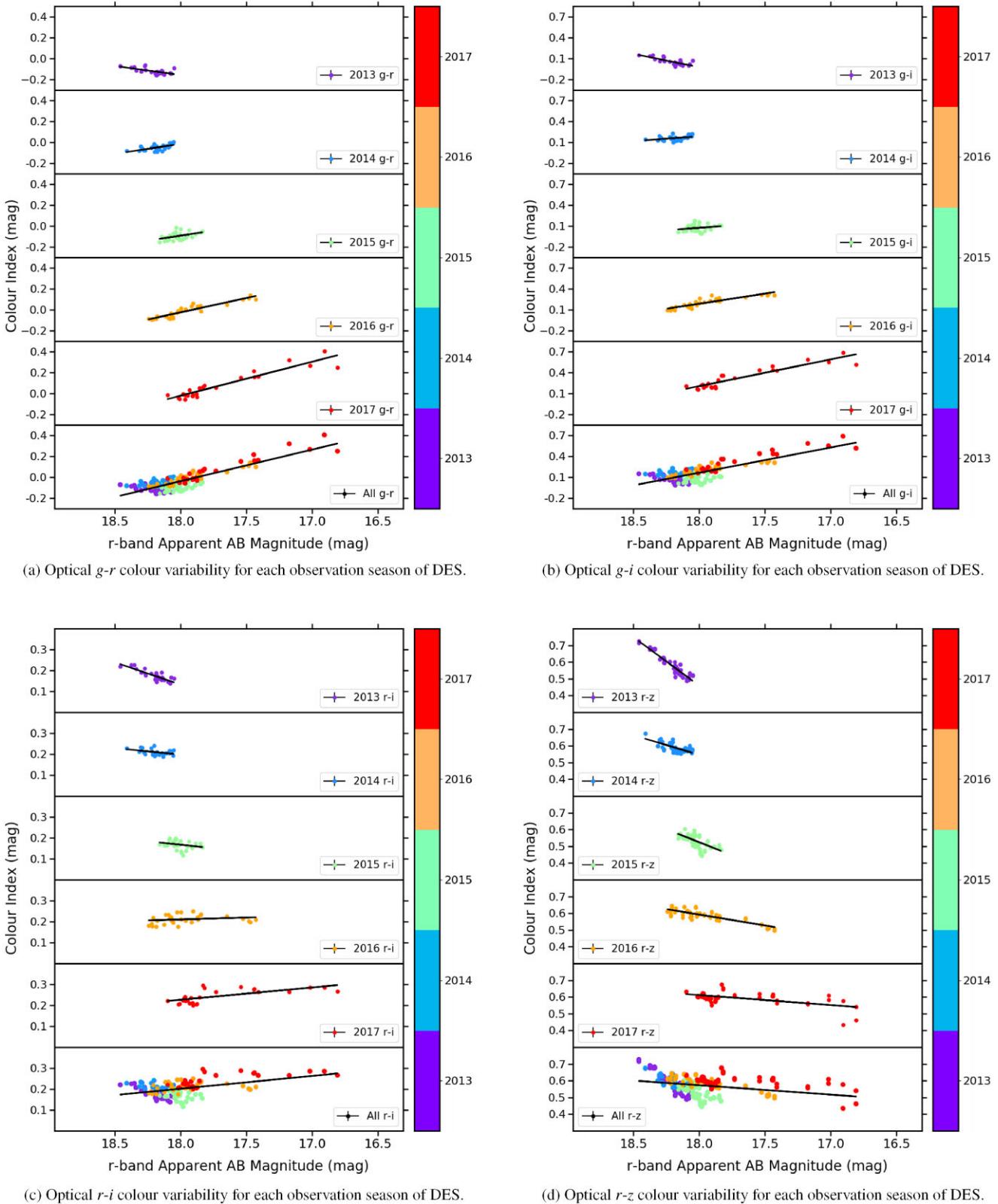
Fig. C4 display histograms of the measured slopes of the 2017–2018 optical–NIR colour versus  $r$  magnitude plots, from each interpolated light curve, with the  $\sim$  month long break in observations between MJD 57993 and 58044. The measured slope from each light curve are no longer consistent with each other in this scenario, which is assumed to be due to the peak that occurs in the optical light curve within this period. When the optical light curve is interpolated, the results are similar to Fig. 10; however, when the NIR light curve is interpolated, the results are shown to be more positive as the interpolations in the NIR light curve in this gap will not be as drastically variable as the optical light curve within this period. This means that the overall slope will be shifted to be positive as the optical light curve will be a lot more variable in this period.

### C4 Optical–NIR colour magnitude plots from 2018–19

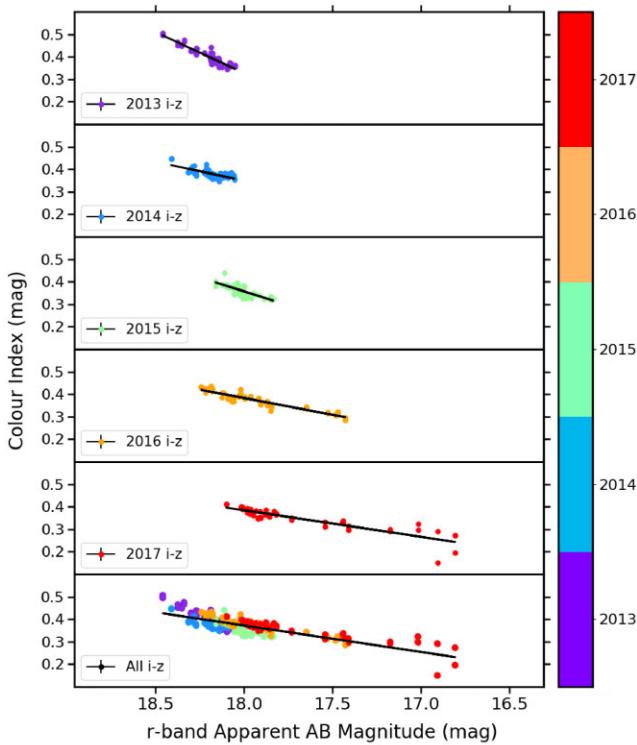
In the 2018 season, only the optical  $r$  and  $i$  bands could be used in the colour–magnitude plots as there were very few epochs observed in the  $g$  and  $z$  bands with VOILETTE during this time. Fig. C5 displays the histograms of the slope from each colour combination of optical,  $r$  and  $i$ , and NIR,  $J$  and  $Ks$  bands, plotted against the  $r$  band. It was found that 75 per cent of the colour versus  $r$  band slopes for each interpolated filter are consistent with each other within  $1\sigma$  and all are consistent within  $1.1\sigma$ . The slopes for the 2018 season show inconclusive colour behaviours.

### C5 Decomposition of the ozdes spectra into variable and non-variable components

In Fig. C6, the OzDES spectra are decomposed into their variable and non-variable components using equation (4). The behaviour of the OzDES components is similar to the behaviour seen in Fig. 13 for the broad-band DES spectra, although it is worth noting that the 2017 OzDES spectra were not observed during the brightest epochs



**Figure C1.** Optical colour variability for each combination of filters in each observation season of DES, where the colour of the data points corresponds to the observation season.

(e) Optical  $i$ - $z$  colour variability for each observation season of DES.**Figure C1.** – *continued*

of the DES observations. The shape of the  $A_\lambda$  component remains similar over all seasons, and is steeper towards the bluer wavelengths, flattening towards the redder wavelengths. The  $S_\lambda$  component also behaves similarly to Fig. 13; however, the lack of spectra during the brightest, most variable flare of the DES observations is reflected in the 2017 season. There is a noticeable bump in the  $\log(S_\lambda)$  versus  $\log(\lambda_{\text{rest}})$  plots especially at  $\log(\lambda_{\text{rest}}) \sim 3.58$  which corresponds to the split between the red and blue arms of the spectrograph as explained in Hoormann et al. (2019).

## C6 Broad-band spectra from DES for each observation season

In Section 5.2.2.1, only the mean brightest and dimmest broad-band spectra are shown. Fig. C7 displays the broad-band spectra for each DES epoch in each observation season, coloured according to the observation epoch, to demonstrate how it changes between the brightest and dimmest states.

## C7 Additional models of the broad-band spectra of DES

Fig. C8 displays the modelled broad-band spectra for the 2015 season and for the entire DES observational period.

In Section 5.2.2.1, the broad-band spectra are fit using models of blue and red components; however, the models displayed are not unique, and the overall broad-band spectra can be fit using a variety of spectral indices for the blue and red emission. In Fig. C9, more examples of the change in spectral slope are displayed for the 2014 season of DES, including models in which the blue component is fixed and the red emission varied.

**Table C1.** The slopes, Spearman rank coefficients, probability of no correlation and colour trend for each season of DES in each combination of filters plotted in Fig. C1(a).

| Season | Slope of $g$ - $r$ versus $r$ mag | $\rho$ -value | $p$ -value             | Trend |
|--------|-----------------------------------|---------------|------------------------|-------|
| 2013   | $0.16 \pm 0.05$                   | 0.54          | $3.86 \times 10^{-3}$  | BWB   |
| 2014   | $-0.19 \pm 0.05$                  | -0.56         | $2.02 \times 10^{-3}$  | RWB   |
| 2015   | $-0.19 \pm 0.07$                  | -0.4          | 0.03                   | SWB   |
| 2016   | $-0.27 \pm 0.02$                  | -0.93         | $1.26 \times 10^{-13}$ | RWB   |
| 2017   | $-0.32 \pm 0.02$                  | -0.87         | $1.09 \times 10^{-8}$  | RWB   |

| Season | Slope of $g$ - $i$ versus $r$ mag | $\rho$ -value | $p$ -value             | Trend |
|--------|-----------------------------------|---------------|------------------------|-------|
| 2013   | $0.38 \pm 0.07$                   | 0.63          | $4.73 \times 10^{-4}$  | BWB   |
| 2014   | $-0.14 \pm 0.07$                  | -0.33         | 0.09                   | SWB   |
| 2015   | $-0.14 \pm 0.12$                  | -0.11         | 0.57                   | SWB   |
| 2016   | $-0.29 \pm 0.03$                  | -0.92         | $1.30 \times 10^{-12}$ | RWB   |
| 2017   | $-0.38 \pm 0.03$                  | -0.84         | $1.67 \times 10^{-7}$  | RWB   |

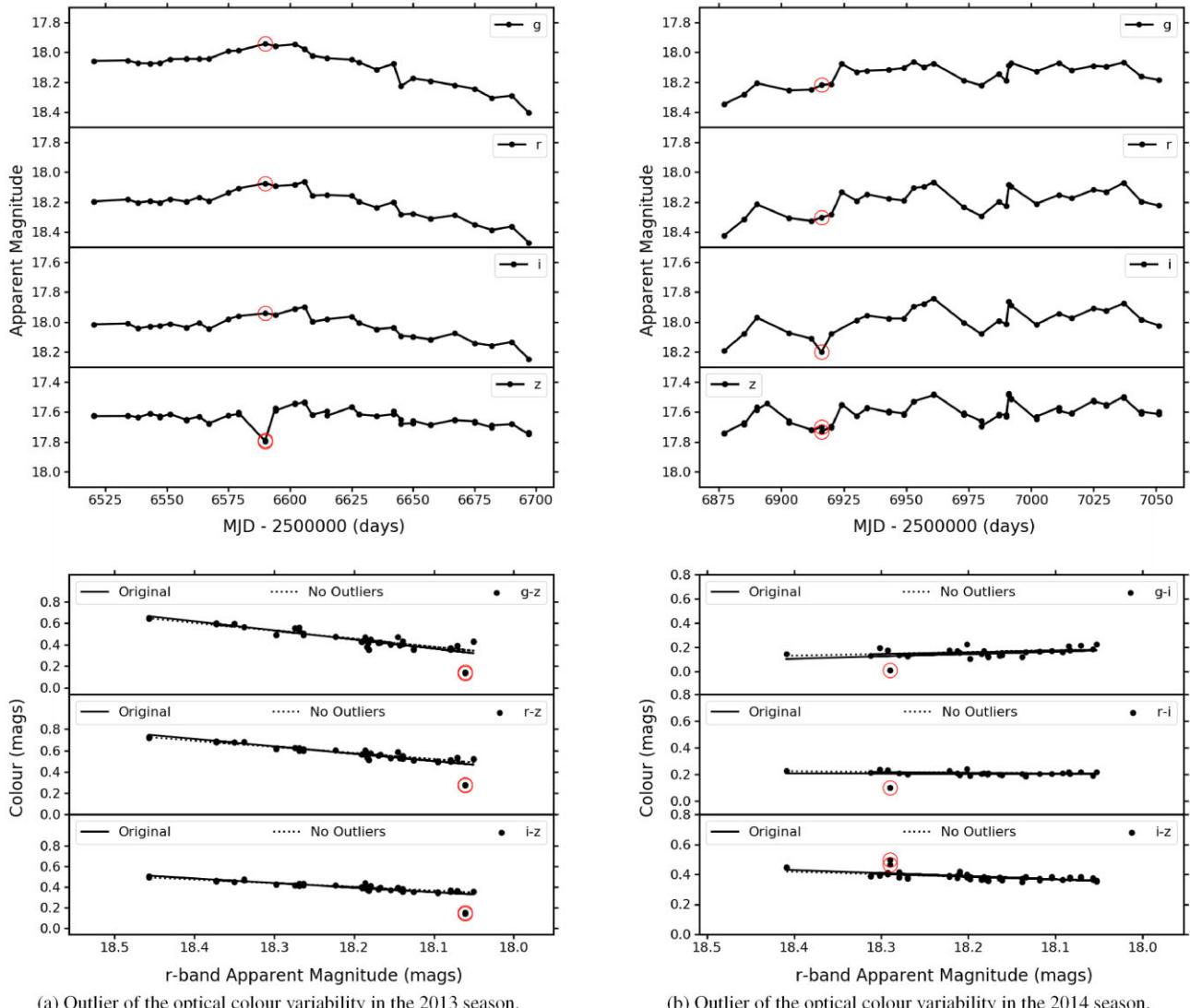
| Season | Slope of $r$ - $i$ versus $r$ mag | $\rho$ -value | $p$ -value            | Trend |
|--------|-----------------------------------|---------------|-----------------------|-------|
| 2013   | $0.21 \pm 0.03$                   | 0.7           | $3.11 \times 10^{-5}$ | BWB   |
| 2014   | $0.06 \pm 0.03$                   | 0.34          | 0.09                  | SWB   |
| 2015   | $0.07 \pm 0.05$                   | 0.35          | 0.06                  | SWB   |
| 2016   | $0.01 \pm 0.02$                   | -0.33         | 0.08                  | SWB   |
| 2017   | $-0.06 \pm 0.01$                  | -0.71         | $5.45 \times 10^{-5}$ | RWB   |

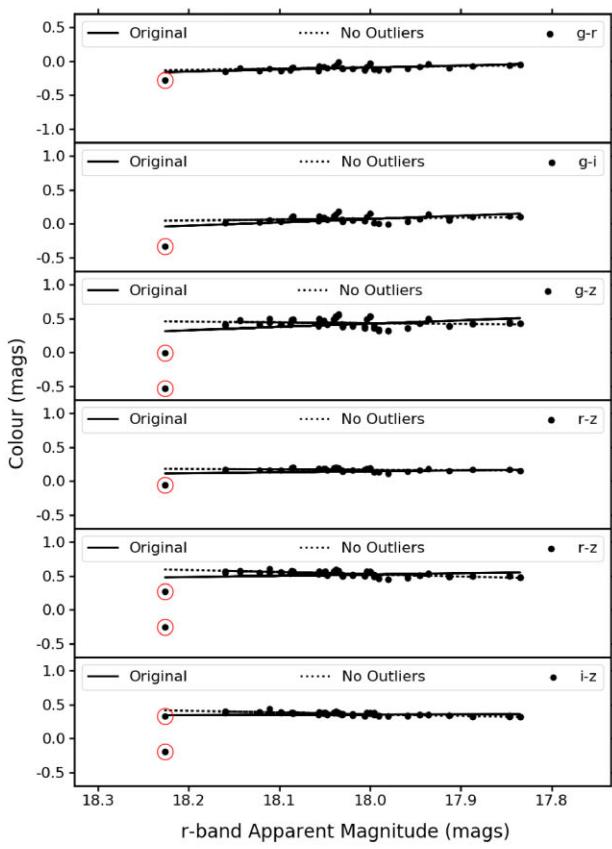
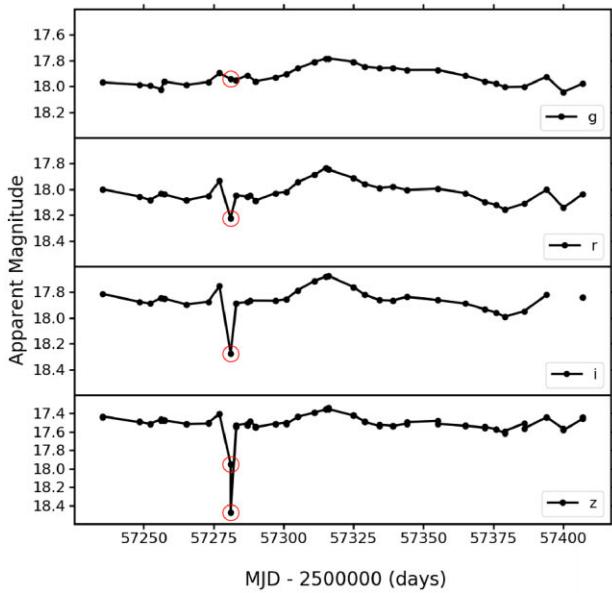
| Season | Slope of $r$ - $z$ versus $r$ mag | $\rho$ -value | $p$ -value             | Trend |
|--------|-----------------------------------|---------------|------------------------|-------|
| 2013   | $0.58 \pm 0.03$                   | 0.88          | $1.56 \times 10^{-19}$ | BWB   |
| 2014   | $0.23 \pm 0.03$                   | 0.58          | $3.81 \times 10^{-6}$  | BWB   |
| 2015   | $0.31 \pm 0.05$                   | 0.67          | $1.03 \times 10^{-9}$  | BWB   |
| 2016   | $0.13 \pm 0.01$                   | 0.75          | $1.02 \times 10^{-11}$ | BWB   |
| 2017   | $0.06 \pm 0.01$                   | 0.36          | $9.58 \times 10^{-3}$  | BWB   |

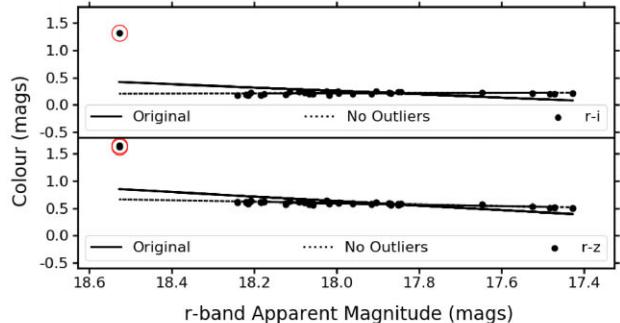
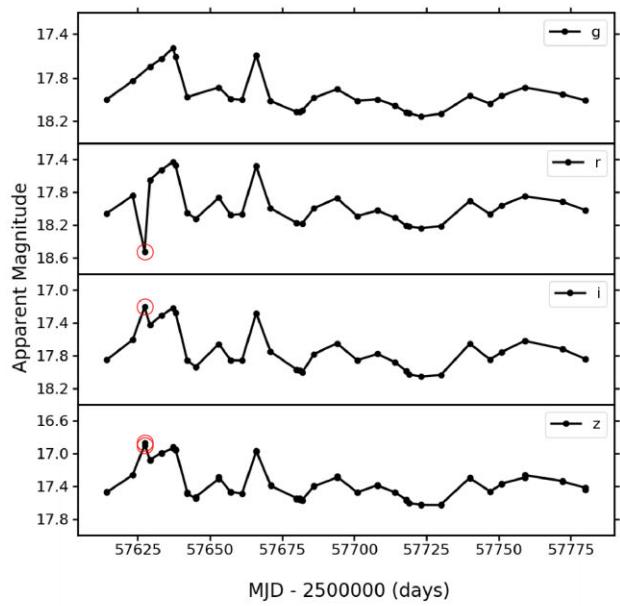
| Season | Slope of $i$ - $z$ versus $r$ mag | $\rho$ -value | $p$ -value             | Trend |
|--------|-----------------------------------|---------------|------------------------|-------|
| 2013   | $0.37 \pm 0.02$                   | 0.9           | $1.03 \times 10^{-20}$ | BWB   |
| 2014   | $0.17 \pm 0.02$                   | 0.65          | $1.73 \times 10^{-7}$  | BWB   |
| 2015   | $0.25 \pm 0.03$                   | 0.77          | $3.68 \times 10^{-13}$ | BWB   |
| 2016   | $0.15 \pm 0.01$                   | 0.9           | $3.07 \times 10^{-22}$ | BWB   |
| 2017   | $0.12 \pm 0.01$                   | 0.89          | $9.82 \times 10^{-19}$ | BWB   |



**Figure C2.** Outliers in the DES light curves of PKS 0027-426 and the optical colour variability.



(c) Outlier of the optical colour variability in the 2015 season.



(d) Outlier of the optical colour variability in the 2016 season.

Figure C2. – *continued*

**Table C2.** The change in slope after the outliers are excluded.

| (a) The 2013 season after the outliers on MJD 56590 are excluded. |                       |                       |
|---|-----------------------|-----------------------|
| Colour  | Slope with all epochs | Slope without outlier |
| $g-r$   | $0.15 \pm 0.05$       | $0.16 \pm 0.05$       |
| $g-i$   | $0.39 \pm 0.07$       | $0.38 \pm 0.07$       |
| $g-z$   | $0.85 \pm 0.07$       | $0.74 \pm 0.05$       |
| $r-i$   | $0.22 \pm 0.03$       | $0.22 \pm 0.03$       |
| $r-z$   | $0.69 \pm 0.06$       | $0.58 \pm 0.03$       |
| $i-z$   | $0.45 \pm 0.05$       | $0.36 \pm 0.02$       |

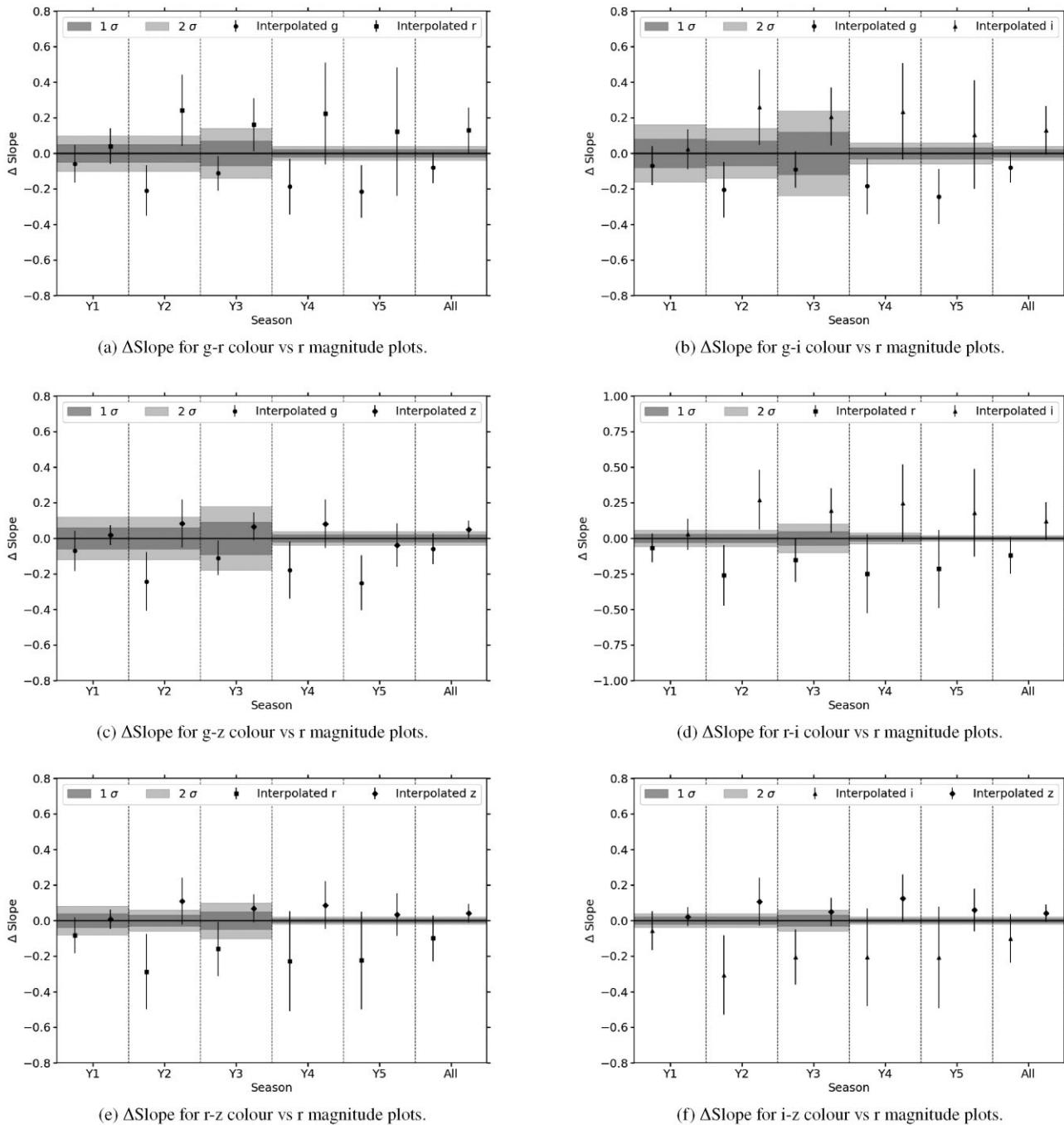
| (b) The 2014 season after the outliers on MJD 56916 are excluded. |                       |                       |
|---|-----------------------|-----------------------|
| Colour  | Slope with all epochs | Slope without outlier |
| $g-r$   | $-0.2 \pm 0.05$       | $-0.19 \pm 0.05$      |
| $g-i$   | $-0.2 \pm 0.09$       | $-0.14 \pm 0.08$      |
| $g-z$   | $0.03 \pm 0.06$       | $0.06 \pm 0.06$       |
| $r-i$   | $0.01 \pm 0.06$       | $0.06 \pm 0.03$       |
| $r-z$   | $0.22 \pm 0.03$       | $0.23 \pm 0.03$       |
| $i-z$   | $0.21 \pm 0.03$       | $0.17 \pm 0.02$       |

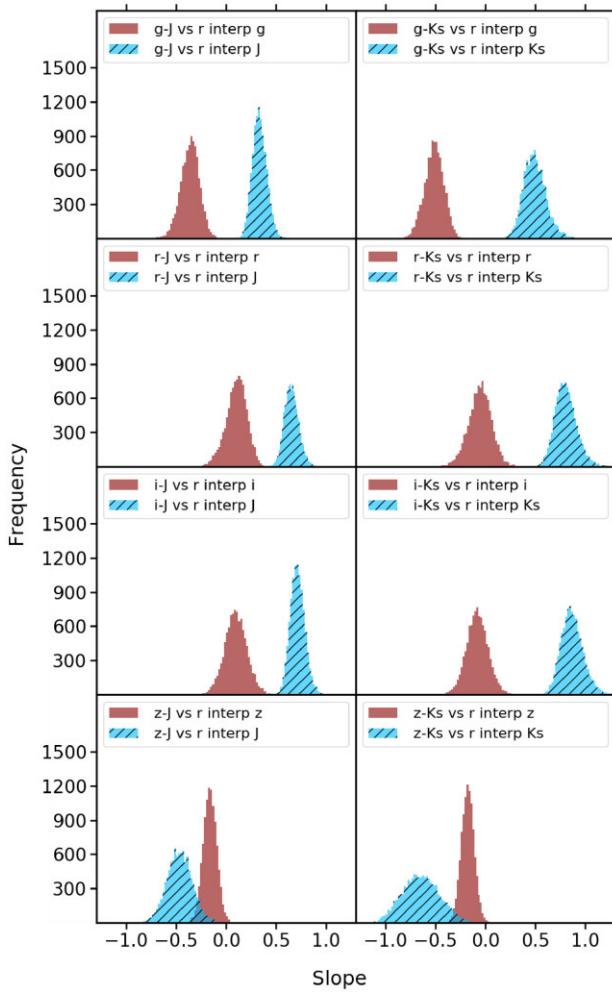
| (c) The 2015 season after the outliers on MJD 57281 are excluded. |                       |                        |
|---|-----------------------|------------------------|
| Colour  | Slope with all epochs | Slope without outliers |
| $g-r$   | $-0.31 \pm 0.09$      | $-0.19 \pm 0.08$       |
| $g-i$   | $-0.48 \pm 0.18$      | $-0.14 \pm 0.13$       |
| $g-z$   | $-0.49 \pm 0.20$      | $0.12 \pm 0.09$        |
| $r-i$   | $-0.14 \pm 0.10$      | $0.07 \pm 0.05$        |
| $r-z$   | $-0.18 \pm 0.16$      | $0.31 \pm 0.05$        |
| $i-z$   | $-0.04 \pm 0.11$      | $0.24 \pm 0.03$        |

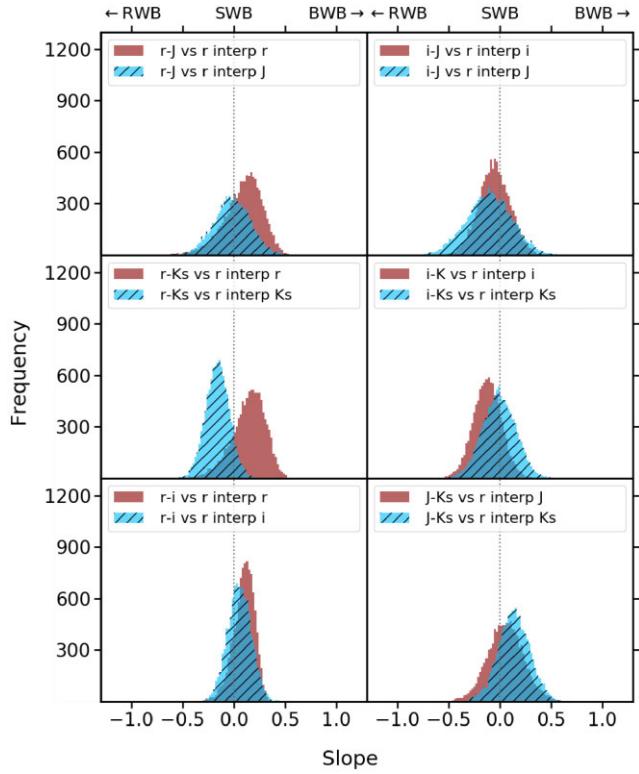
| (d) The 2016 season after the outliers on MJD 57627 are excluded. |                       |                        |
|---|-----------------------|------------------------|
| Colour  | Slope with all epochs | Slope without outliers |
| $g-r$   | $-0.27 \pm 0.02$      | $-0.27 \pm 0.02$       |
| $g-i$   | $-0.29 \pm 0.03$      | $-0.29 \pm 0.03$       |
| $g-z$   | $-0.14 \pm 0.02$      | $-0.14 \pm 0.02$       |
| $r-i$   | $0.31 \pm 0.15$       | $-0.02 \pm 0.02$       |
| $r-z$   | $0.42 \pm 0.09$       | $0.13 \pm 0.01$        |
| $i-z$   | $0.11 \pm 0.01$       | $0.15 \pm 0.01$        |



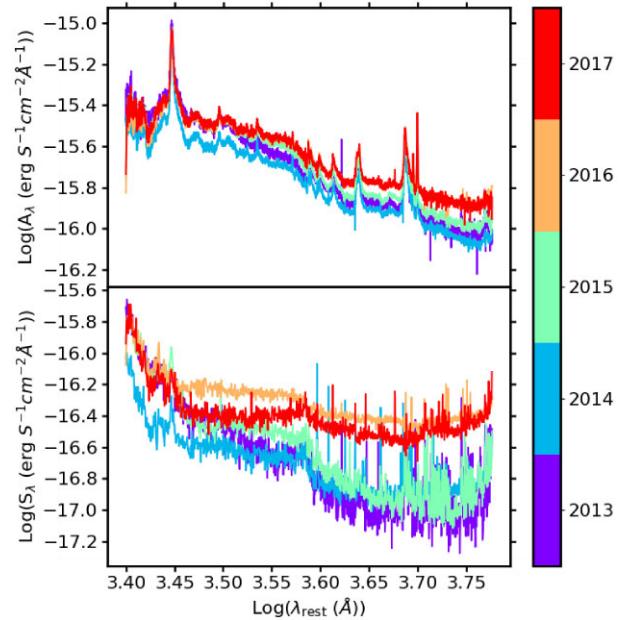
**Figure C3.**  $\Delta$ Slope for the DES colour versus r magnitude plots, comparing the slope obtained from the data with the slope obtain from interpolating one of the light curves after removing 50 per cent of the observations. The shaded regions demonstrate the  $1\sigma$  and  $2\sigma$  uncertainties of the slopes obtained from the data.



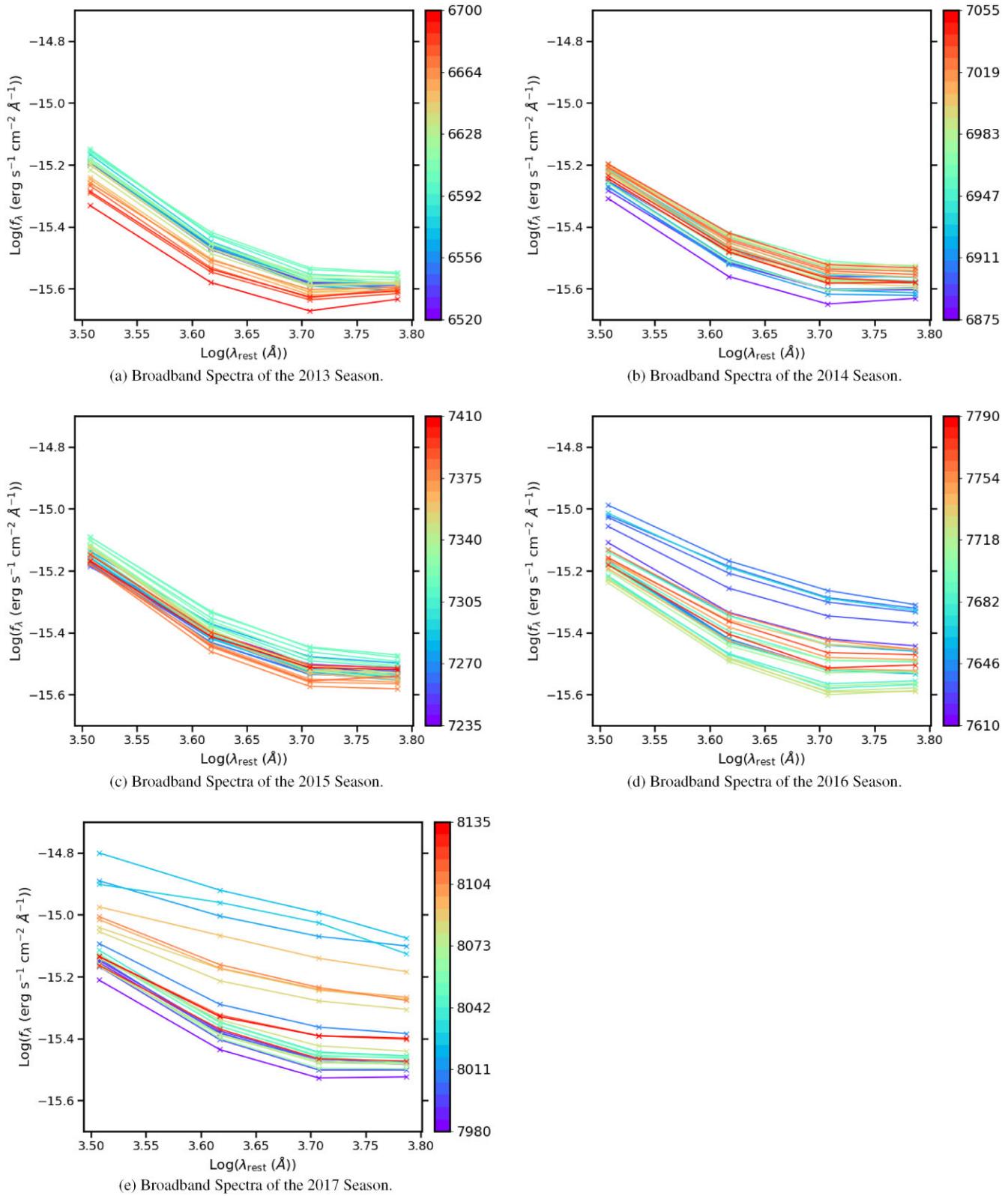
**Figure C4.** The slopes measured for each combination of the optical–NIR colour versus  $r$  magnitude plots in the 2017 season, for the entire light curve, which includes a  $\sim$  month long gap in the NIR light curve between MJD 57993 and 58044.



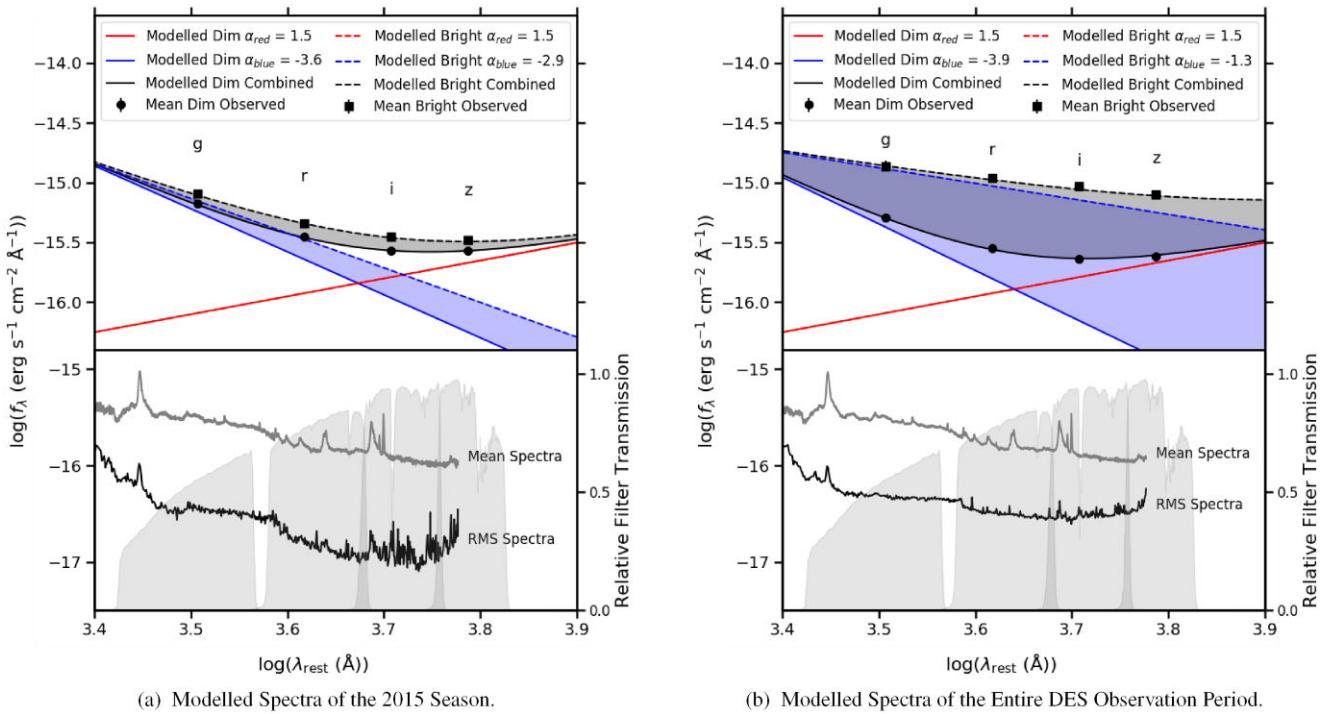
**Figure C5.** The distributions of the slope of the 2018–19 optical and NIR colours versus  $r$  magnitude plots returned from 10 000 interpolations of each light curve.



**Figure C6.** Decomposition of the OzDES spectra into the variable ( $S_\lambda$ ) and non-variable ( $A_\lambda$ ) components for each season of DES. The  $S_\lambda$  spectra are smoothed in this plot so that they are easier to see.



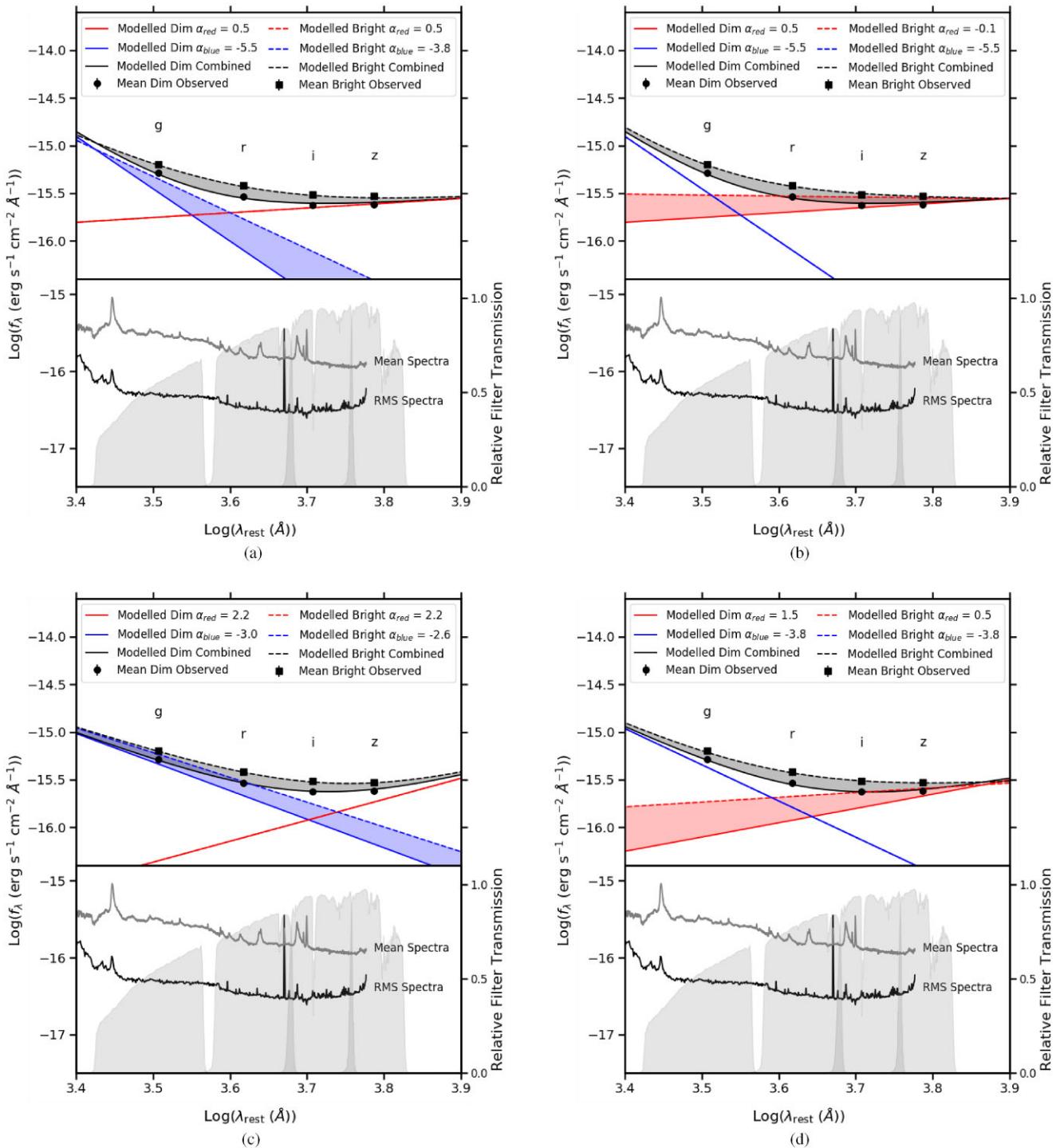
**Figure C7.** All broad-band spectra in each observation season of DES, coloured according to observation epoch.



(a) Modelled Spectra of the 2015 Season.

(b) Modelled Spectra of the Entire DES Observation Period.

**Figure C8.** *Upper panel:* Modelled broad-band spectra of the red and blue emission that combine to match the average brightest and dimmest epochs in the 2015 observation season and the entire observational period compared to the observed broad-band spectra. The solid lines correspond to the modelled spectra of the dimmest epochs, and the dashed lines correspond to the modelled spectra of the brightest epochs. *Lower panel:* Mean and smoothed RMS OzDES spectra for each season plotted over the DES filter transmissions.



**Figure C9.** *Upper panel:* Alternative examples of the modelled broad-band spectra of the blue and red emission to match the average observed brightest and dimmest epochs in the 2014 season. The solid lines correspond to the modelled spectra of the dimmest epochs, and the dashed lines correspond to the modelled spectra of the brightest epochs. *Lower panel:* Mean and smoothed RMS OzDES spectra for each season plotted over the DES filter transmissions.

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