

State-specific solvation for restricted active space spin-flip (RAS-SF) wave functions based on the polarizable continuum formalism

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Bushra Alam,¹ Hanjie Jiang,²  Paul M. Zimmerman,²  and John M. Herbert^{1,a)} 

AFFILIATIONS

¹ Department of Chemistry and Biochemistry, The Ohio State University, Columbus, Ohio 43210, USA

² Department of Chemistry, University of Michigan, Ann Arbor, Michigan 48109, USA

^a Author to whom correspondence should be addressed: herbert@chemistry.ohio-state.edu

ABSTRACT

The restricted active space spin-flip (RAS-SF) formalism is a particular form of single-reference configuration interaction that can describe some forms of strong correlation at a relatively low cost and which has recently been formulated for the description of charge-transfer excited states. Here, we introduce both equilibrium and nonequilibrium versions of a state-specific solvation correction for vertical transition energies computed using RAS-SF wave functions, based on the framework of a polarizable continuum model (PCM). Ground-state polarization is described using the solvent's static dielectric constant and in the nonequilibrium solvation approach that polarization is modified upon vertical excitation using the solvent's optical dielectric constant. Benchmark calculations are reported for well-studied models of photo-induced charge transfer, including naphthalene dimer, $C_2H_4 \cdots C_2F_4$, pentacene dimer, and perylene diimide (PDI) dimer, several of which are important in organic photovoltaic applications. For the PDI dimer, we demonstrate that the charge-transfer character of the excited states is enhanced in the presence of a low-dielectric medium (static dielectric constant $\epsilon_0 = 3$) as compared to a gas-phase calculation ($\epsilon_0 = 1$). This stabilizes mechanistic traps for singlet fission and helps to explain experimental singlet fission rates. We also examine the effects of nonequilibrium solvation on charge-separated states in an intramolecular singlet fission chromophore, where we demonstrate that the energetic ordering of the states changes as a function of solvent polarity. The RAS-SF + PCM methodology that is reported here provides a framework to study charge-separated states in solution and in photovoltaic materials.

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I. INTRODUCTION

Multireference wave function methods^{1–3} are important tools in the quantum chemist's arsenal, for the description of static correlation in systems with stretched bonds or other types of (near-) degeneracies, as well as open-shell systems including radicals and excited states.² However, the exponential scaling of computational cost with respect to active space size, for methods such as the complete active-space self-consistent field (CASSCF) theory, limits the size and scope of problems that can be addressed in this way. To reduce the cost of multireference approaches, alternative *Ansätze* have been developed, notably spin-flip (SF) methods.^{4–9} Among the SF family of approaches, one of the most important variants is the restricted active space (RAS-)SF method. Configuration interaction (CI) wave functions within the RAS

family include all possible configurations within an active space and (at a minimum) single excitations into and out of the active space.¹⁰ As such, RAS-SF provides a low-cost, balanced treatment of ground and excited states with multi-radical character.^{5,6} Unlike CASSCF, the RAS-SF technique does not require orbital optimization, which significantly reduces both complexity and cost.^{5–7}

A recently developed variant of RAS-SF allows analysis of charge-transfer (CT) states,¹¹ which were previously inaccessible to the theory. The new method can compute not just CT states but also electronic couplings, using a diabatic framework that may facilitate a more in-depth understanding of photophysical processes such as artificial or biological light-harvesting. The position of CT states in the excitation manifold is often sensitive to polarization effects,^{12–15} even in low-dielectric environments such as organic photovoltaic

materials.¹⁵ Therefore, some treatment of the surrounding medium is likely necessary in order to make contact with experiments.

In the present work, we augment the RAS-SF methodology to include solvent polarization based on dielectric continuum theory,¹⁶ within the framework of the polarizable continuum model (PCM).^{16–18} Specifically, we introduce both equilibrium (state-relaxed) and nonequilibrium versions of the RAS-SF + PCM formalism, in order to account for differential polarization upon electronic excitation of the solute. The nonequilibrium continuum approach^{16,19–24} separates the medium's polarization response into fast (electronic) and slow (vibrational and orientational) components, then uses the solvent's optical dielectric constant (ϵ_∞) to describe the fast processes while the static dielectric constant (ϵ_0) describes the total polarization response, including both nuclear and electronic contributions. In this way, nonequilibrium PCMs describe the change in electronic polarization following a sudden change in the charge distribution of the solute, corresponding to vertical electronic excitation^{20–22} or vertical ionization.^{21,23,24} In contrast, the state-relaxed algorithm is targeted at equilibrium solvation where all polarization mechanisms are fully relaxed in the excited state, as appropriate for the description of emission.

II. THEORY

The method introduced in this work builds upon the RAS-SF approach for CT states,¹¹ introducing a PCM framework for solvation effects. The RAS-SF formalism is briefly reviewed in Sec. II A, following which we introduce the state-specific equilibrium and nonequilibrium solvation theories in Secs. II B and II C, respectively. The nonequilibrium version is built upon a perturbative framework introduced previously.^{20–24} Section II D describes how the PCM theory is integrated with the RAS-SF approach to computing the wave function.

A. RAS-SF wave function

A RAS-SF calculation starts from high-spin, restricted open-shell Hartree-Fock (ROHF) reference orbitals, from which target states of interest are computed via SF excitations. The RAS scheme divides the orbitals into three subspaces labeled RAS1, RAS2, and RAS3 and the wave function *Ansatz* for RAS-SF is

$$|\Psi\rangle = \sum_{m \in \text{RAS2}} c_m |\phi_m\rangle + \sum_{\substack{h \in \text{RAS1} \\ m \in \text{RAS2}}} c_m^h |\phi_m^h\rangle + \sum_{\substack{p \in \text{RAS3} \\ m \in \text{RAS2}}} c_m^p |\phi_m^p\rangle. \quad (1)$$

The RAS2 space is the active space and should include the most important orbitals needed to describe the electronic states of interest; $m \in \text{RAS2}$ in Eq. (1) includes all configurations within the active space, meaning that RAS-SF resembles a CAS-CI method within the RAS2 space. The RAS1 space contains all doubly occupied orbitals and RAS3 contains virtual orbitals, and we allow single excitations between these two subspaces and RAS2, corresponding to holes $h \in \text{RAS1}$ and particles $p \in \text{RAS3}$. This particular *Ansatz* has been called RAS(h,p)-SF.^{10,11}

To describe CT states,¹¹ the high-spin reference orbitals are first localized onto molecular fragments, where they are then categorized

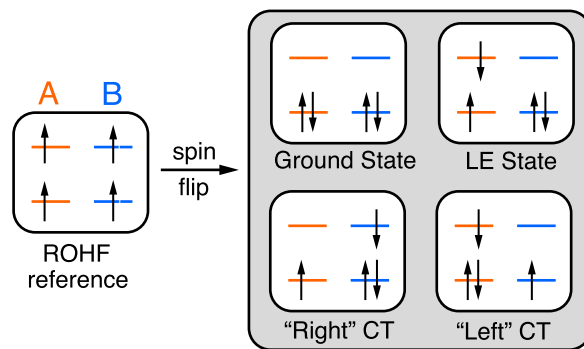


FIG. 1. Schematic representation of the states that emerge in RAS-SF from a high-spin quintet reference configuration. Note that each state (including the ground state) emerges from the diagonalization of a CI Hamiltonian, indicated by the gray box.

by subspace (RAS1, RAS2, or RAS3) and fragment. The RAS Hamiltonian is then partitioned into CT and non-CT blocks, where the latter will also be called the “locally excited” (LE) block. Diagonalization of these blocks provides either the LE states or the CT states, and the latter are further grouped into left–right vs right–left character, or equivalently $A \rightarrow B$ vs $B \rightarrow A$ (Fig. 1).

B. Equilibrium state-specific solvation

Electrostatic interactions between the electronic ground state of the solute and the continuum solvent are described by a reaction-field operator, \hat{R}_0 . The total electronic energy in the ground state is

$$E_0 = \langle \Psi_0 | \hat{H}_{\text{vac}} + \hat{R}_0 | \Psi_0 \rangle, \quad (2)$$

in which \hat{H}_{vac} is the vacuum (gas-phase) Hamiltonian. The subscript “0” in \hat{R}_0 indicates that the ground-state wave function is used to polarize the medium. In a ground-state self-consistent reaction-field (SCRf) calculation, the energy that is variationally minimized is not actually E_0 but rather the *free* energy $G_0 = E_0 - W_0$, where

$$W_0 = \frac{1}{2} \langle \Psi_0 | \hat{R}_0 | \Psi_0 \rangle \quad (3)$$

is the work required to polarize the continuum. A ground-state SCRf calculation therefore corresponds to minimization of a functional $G_0[\Psi]$ that is given by^{16,25}

$$G_0 = \left\langle \Psi_0 \left| \hat{H}_{\text{vac}} + \frac{1}{2} \hat{R}_0 \right| \Psi_0 \right\rangle. \quad (4)$$

We will now extend this idea to state-specific solvation of an excited-state wave function $|\Psi_k\rangle$, starting with an equilibrium approach in which the polarization of the medium is fully relaxed with respect to the excited-state charge distribution, using the solvent's static dielectric constant (ϵ_0) to represent all possible polarization mechanisms for the medium. This approach should be valid in the long-time limit after excitation, whereas the case of a sudden

(vertical) excitation requires a nonequilibrium approach, as developed in Sec. II C. For equilibrium solvation on excited state k , one must solve the state-specific Schrödinger equation

$$(\hat{H}_{\text{vac}} + \hat{R}_k)|\Psi_k\rangle = E_k|\Psi_k\rangle. \quad (5)$$

(Our notation for excited-state PCM calculations follows that used in a recent review.¹⁶) The quantity \hat{R}_k is the reaction-field operator for state k , meaning that the charge distribution corresponding to wave function $|\Psi_k\rangle$ is used to polarize the medium. Since \hat{R}_k depends on $|\Psi_k\rangle$, Eq. (5) must be solved iteratively and this constitutes the excited-state SCRF problem.

In analogy to Eq. (2), the electronic energy for state k in this fully relaxed approach is

$$E_k^{\text{eq}} = \langle \Psi_k | \hat{H}_{\text{vac}} + \hat{R}_k | \Psi_k \rangle, \quad (6)$$

using a superscript “eq” to indicate equilibrium solvation. The corresponding free energy is

$$G_k^{\text{eq}} = E_k^{\text{eq}} - W_k, \quad (7)$$

where

$$W_k = \frac{1}{2} \langle \Psi_k | \hat{R}_k | \Psi_k \rangle \quad (8)$$

represents the work required to polarize the continuum using \hat{R}_k . The fully relaxed (equilibrium) excitation energy is

$$G_k^{\text{eq}} - G_0 = \Delta E_k^{\text{eq}} - W_k + W_0, \quad (9)$$

where

$$\Delta E_k^{\text{eq}} = E_k^{\text{eq}} - E_0 \quad (10)$$

is the state-specific eigenvalue difference. The quantity $W_k - W_0$ in Eq. (9) represents the differential polarization work between the excited state and the ground state.

The iterative procedure required to solve the state-specific eigenvalue problem in Eq. (5) is relatively straightforward if there are no quasi-degeneracies, although this equation must be solved separately for each electronic state of interest. However, the presence of near-degeneracies may lead to convergence problems associated with root-flipping, and properties other than the energy (including oscillator strengths) are not entirely well-defined because the excited states are not eigenfunctions of a common Hamiltonian and are therefore not orthogonal to one another.²⁶ To circumvent these difficulties, we next describe a perturbative approach to state-specific solvation,^{20–22} which furthermore allows for all of the solvent-corrected excitation energies to be obtained from a single calculation, including nonequilibrium corrections.

C. Perturbative state-specific solvation

We next describe a *nonequilibrium* approach to state-specific solvation that is appropriate for modeling vertical excitation energies.¹⁶ The nonequilibrium formalism recognizes that nuclear (vibrational and orientational) degrees of freedom within the (implicit) solvent do not respond quickly enough to remain in equilibrium with a vertical electronic transition, and indeed this is the

sense in which the excitation is “vertical.” There is also an electronic component to the solvent’s polarization response, however, and it ought to remain in equilibrium with the solute. The total polarization in the ground state is thus partitioned into “slow” (nuclear) and “fast” (electronic) components,

$$\hat{R}_0 = \hat{R}_0^s + \hat{R}_0^f. \quad (11)$$

Operationally this means that the ground-state polarization charge σ_0 (generated by \hat{R}_0) is partitioned as $\sigma_0 = \sigma_0^s + \sigma_0^f$, where¹⁶

$$\sigma_0^s = \left(\frac{\epsilon_0 - \epsilon_\infty}{\epsilon_0 - 1} \right) \sigma_0, \quad (12a)$$

$$\sigma_0^f = \left(\frac{\epsilon_\infty - 1}{\epsilon_0 - 1} \right) \sigma_0. \quad (12b)$$

The solvent’s optical dielectric constant (ϵ_∞), which has been called the “dielectric constant for induced polarization,”²⁷ is used to describe electronic polarization.

Considering the equilibrium expression for E_k in Eq. (6), where $\hat{R}_k = \hat{R}_k^s + \hat{R}_k^f$, a corresponding nonequilibrium expression is obtained by instead using $\hat{R}_0^s + \hat{R}_k^f$ as the reaction-field operator for excited state k , corresponding to a state-specific polarization charge density $\sigma_k = \sigma_0^s + \sigma_k^f$. This substitution affords

$$E_k^{\text{noneq}} = \langle \Psi_k | \hat{H}_k^{\text{noneq}} | \Psi_k \rangle, \quad (13)$$

where

$$\hat{H}_k^{\text{noneq}} = \hat{H}_{\text{vac}} + \hat{R}_0^s + \hat{R}_k^f \quad (14)$$

is a state-specific Hamiltonian for nonequilibrium solvation.

As discussed in the context of the equilibrium case, the state-specific nature of the Hamiltonian may lead to convergence problems and other formal complexities arising from the nonorthogonality of the excited-state wave functions.^{16,26} As a result of root-flipping problems, it is probably only realistic to imagine a fully self-consistent solution to the state-specific Schrödinger equation in cases where the state k of interest is spectrally isolated, unless specialized convergence algorithms are employed.²⁶ (One such algorithm is described in Ref. 26.) Even if convergence is not problematic, a separate calculation is required for each excited state. For reasons of simplicity, we desire an approach that can generate the entire spectrum in a single calculation. A perturbative approach to incorporating the solvation correction solves both of these problems.

To obtain such an approach, we start from the unperturbed Hamiltonian

$$\hat{H}_0 = \hat{H}_{\text{vac}} + \hat{R}_0^s + \hat{R}_0^f \quad (15)$$

that is simply a rewriting of the ground-state Hamiltonian in Eq. (2), but in a form that suggests a partition of the state-specific Hamiltonian in Eq. (14), namely,

$$\hat{H}_k^{\text{noneq}} = \hat{H}_0 + \hat{R}_k^f - \hat{R}_0^f. \quad (16)$$

Introducing a perturbation parameter λ , this partition can be used to develop a perturbation theory expression for the energy of state k , including nonequilibrium corrections:

$$E_k^{\text{noneq}} = \langle \Psi_k | \hat{H}_0 + \lambda(\hat{R}_k^f - \hat{R}_0^f) | \Psi_k \rangle. \quad (17)$$

This has been called the perturbation theory state-specific (ptSS) approach.^{20–22} Unperturbed states $|\Psi_k^{(0)}\rangle$ are eigenfunctions of \hat{H}_0 , and the zeroth-order energy for state k is

$$E_k^{\text{ptSS}(0)} = \langle \Psi_k^{(0)} | \hat{H}_{\text{vac}} + \hat{R}_0 | \Psi_k^{(0)} \rangle \quad (18)$$

within the nonequilibrium formalism. The corresponding free energy expression is¹⁶

$$G_k^{\text{ptSS}(0)} = E_k^{\text{ptSS}(0)} - W_0^s - W_0^f, \quad (19)$$

where W_0^s and W_0^f are defined analogously to W_0 in Eq. (3) but with \hat{R}_0^s or \hat{R}_0^f replacing \hat{R}_0 .

Equation (18) for E_k is a natural generalization of Eq. (2) for E_0 and corresponds to solving the Schrödinger equation in the fixed reaction field of the equilibrated ground state. A nonequilibrium correction arises in first-order perturbation theory and is given by

$$E_k^{\text{ptSS}(1)} = \langle \Psi_k^{(0)} | \hat{R}_{k(0)}^f - \hat{R}_0^f | \Psi_k^{(0)} \rangle, \quad (20)$$

where the notation $\hat{R}_{k(0)}^f$ indicates that this reaction-field operator is constructed using the charge density corresponding to wave function $|\Psi_k^{(0)}\rangle$. The corresponding free energy correction is

$$G_k^{\text{ptSS}(1)} = E_k^{\text{ptSS}(1)} - W_{k(0)}^f + W_0^f + W_{0,k(0)}, \quad (21)$$

where

$$W_{k(0)}^f = \frac{1}{2} \langle \Psi_k^{(0)} | \hat{R}_{k(0)}^f | \Psi_k^{(0)} \rangle \quad (22)$$

in analogy to Eq. (8). The quantity $W_{0,k(0)}$ in Eq. (21) is a charge-separation penalty arising from the Coulomb interaction of the initial- and final-state surface charges,^{16,21}

$$W_{0,k(0)} = \frac{1}{2} \int [\sigma_{k(0)}^f(\mathbf{r}) - \sigma_0^f(\mathbf{r})] \varphi^{\sigma_0^s}(\mathbf{r}) d\mathbf{r}. \quad (23)$$

Here, $\varphi^{\sigma_0^s}(\mathbf{r})$ is the electrostatic potential generated by the ground-state polarization charge, $\sigma_0^s(\mathbf{r})$. As discussed in Refs. 16 and 21, the $W_{0,k(0)}$ term has sometimes been omitted from nonequilibrium polarization treatments, but is necessary when the “Marcus partition” into fast and slow components is used, corresponding to Eq. (12).

Taking the free energy for state k to be the zeroth-order result plus the first-order correction,

$$G_k = G_k^{\text{ptSS}(0)} + G_k^{\text{ptSS}(1)}, \quad (24)$$

the ptSS approximation to the excitation energy is

$$\begin{aligned} \Delta G_k^{\text{ptSS}(1)} &= G_k - G_0 \\ &= \Delta E_k^{\text{ptSS}(1)} - W_{k(0)}^f + W_0^f + W_{0,k(0)}, \end{aligned} \quad (25)$$

where

$$\Delta E_k^{\text{ptSS}(1)} = E_k^{\text{ptSS}(0)} + E_k^{\text{ptSS}(1)} - E_0. \quad (26)$$

The formula in Eq. (25) has a straightforward interpretation.¹⁶ The leading term, which is given by Eq. (26), is the difference between eigenvalues E_k and E_0 of the state-specific Schrödinger equation, where E_k is correct through first order in perturbation theory. This eigenvalue difference becomes a free energy upon subtracting $W_{k(0)}^f - W_0^f$, which is the difference between the work required to polarize the fast charge on the excited state relative to that required on the ground state. Finally, $W_{0,k(0)}$ is the aforementioned charge-separation penalty.

For future reference, we define

$$\Delta E_k^{\text{ptSS}(0)} = E_k^{\text{ptSS}(0)} - E_0, \quad (27)$$

which is the zeroth-order approximation to $E_k - E_0$. Equivalently, this is the excitation energy obtained by solving the Schrödinger equation in the fixed reaction field of the ground state, and therefore this approximation does not contain nonequilibrium effects. Equation (25) can then be rewritten as

$$\Delta G_k^{\text{ptSS}(1)} = \Delta E_k^{\text{ptSS}(0)} + G_k^{\text{ptSS}(1)}. \quad (28)$$

The ptSS approximation for the free energy of excitation ($\Delta G_k^{\text{ptSS}(1)}$) is thus obtained by adding the zeroth-order eigenvalue difference ($\Delta E_k^{\text{ptSS}(0)}$) to the first-order free energy correction ($G_k^{\text{ptSS}(1)}$), with all nonequilibrium effects contained in the latter.

D. Implementation

A flow chart for the RAS-SF + PCM algorithm is illustrated in Fig. 2, including both the nonequilibrium ptSS and the state-relaxed equilibrium procedure. The algorithm begins by computing the RAS-SF ground state wave function in the gas phase. Next, one-electron integrals are modified to incorporate \hat{R}_0 and the ground-state total energy is iterated to convergence, as in any SCRf calculation except that the lowest eigenstate of a CI Hamiltonian must be computed at each SCRf iteration. A damping scheme was implemented for the PCM surface charges,²⁴ such that the charges at each iteration are a convex linear combination of the charges obtained from the current reaction field operator and the previous one. However, the use of this algorithm proves to be unnecessary. Convergence of the ground-state SCRf problem is typically accomplished in 3–4 iterations if the convergence criterion is set to 10^{-8} hartree on the change in G_0 . This completes step 1 in Fig. 2.

Once the ground-state eigenfunction has been equilibrated with respect to the medium, excited states (including LE and/or CT states, as desired) are obtained by computing additional eigenstates in the presence of a fixed reaction-field operator \hat{R}_0 . These are the zeroth-order states $|\Psi_k^{(0)}\rangle$, with energies $E_k^{\text{ptSS}(0)}$ [Eq. (18)]. From there, the corrected free energies for each state can be computed using Eq. (19) or excitation free energies using Eq. (25). Note that ptSS corrections can be computed for all excited states at once, without any additional SCRf iterations in step 2 of Fig. 2.

The equilibrium state-relaxed procedure starts from a gas-phase RAS-SF calculation to obtain an initial wave function $|\Psi_k\rangle$ for the excited state of interest, from which \hat{R}_k can be constructed. This procedure bypasses the ground-state SCRf procedure (although the ground-state SCRf problem needs to be solved in advance, to obtain E_0), instead proceeding directly to the state-specific

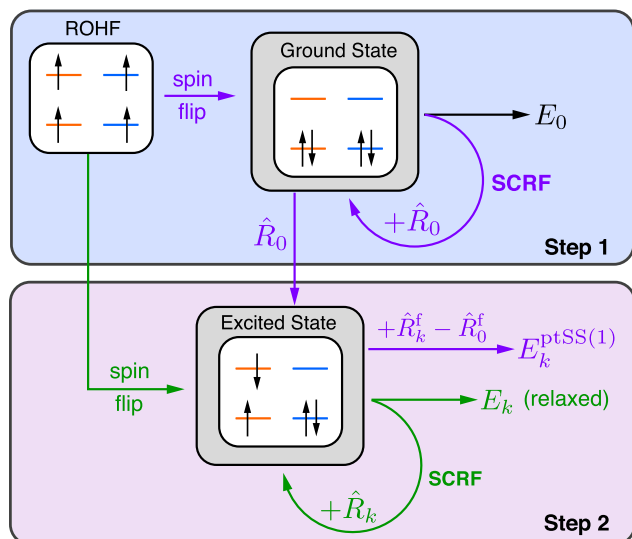


FIG. 2. Flowchart for the RAS-SF + PCM procedure, illustrating the ptSS procedure (purple arrows) vs the equilibrium state-relaxed procedure (green arrows). Step 1 of the ptSS approach involves an SCRF calculation using the ground-state eigenvector of the CI Hamiltonian (illustrated with a gray box, as in Fig. 1). In step 2, excited-state eigenvectors are computed from the CI Hamiltonian using a frozen reaction field for the ground state (\hat{R}_0), then corrected using the perturbation $\hat{R}_k^f - \hat{R}_0^f$. In this approach, all of the CI eigenvectors can be corrected at once and only a single CI calculation is required in step 2. Alternatively, the fully relaxed equilibrium procedure corresponds to a SCRF calculation in the presence of reaction-field \hat{R}_k , solving the state-specific Schrödinger equation [Eq. (5)] one state at a time to obtain fully relaxed energies E_k .

eigenvalue problem for E_k [Eq. (5)]. The solution of this equation requires SCRF iterations in the excited state because each time the RAS-SF Hamiltonian is diagonalized to obtain $|\Psi_k\rangle$, the operator \hat{R}_k must be modified to reflect how the new excited-state charge density polarizes the medium. This process is iterated to convergence, which typically requires 7–10 iterations with a convergence criterion of 10^{-6} hartree. Upon convergence, E_k^{eq} is obtained from Eq. (6). The proper state energy, however, is G_k^{eq} [Eq. (7)], and the excitation energy for state k is given in Eq. (9). The SCRF procedure must be repeated for every state of interest.

The equilibrium state-relaxed approach has some similarities to the state-specific implementation of time-dependent density functional theory (TD-DFT) with PCM,^{28,29} especially if TD-DFT is viewed as a CI method with single excitations (CIS), where excited states are obtained iteratively as roots of an eigenvalue problem. Our procedure also bears some similarities to the most complete version of the SCRF approach for correlated wave functions, which is usually called “perturbation to energy and density,”^{16,22,30–33} meaning that all correlation effects are included in the charge density that is used to equilibrate the reaction field. Some differences exist with respect to the present procedure, as RAS-SF is not a post-Hartree–Fock procedure where correlation is added to a single-determinant reference, but rather it is a method in which the ground-state wave function emerges as the lowest eigenfunction of a CI Hamiltonian.

The ptSS-PCM procedure described in Sec. II C has previously been implemented for CIS and TD-DFT wave functions,^{20,21} which is technically simpler because in that case the reference state is the physical ground state. The TD-DFT + ptSS-PCM method^{20,21} is very similar to the “corrected linear response theory” of Caricato *et al.*³⁴

III. RESULTS AND DISCUSSION

The RAS-SF + PCM procedure has been implemented in a locally modified version of Q-Chem 5.3.³⁵

A. Computational details

All RAS calculations use a (4,4) active space and the hole-particle (h,p) algorithm that was outlined in Sec. II A, starting from a quintet ROHF reference state. In order to use the CT version of RAS-SF, the ROHF orbitals were localized using the Pipek–Mezey procedure.³⁶ Core orbitals are not correlated (i.e., frozen core approximation). The basis set is 6-31G*, cc-pVDZ, or cc-pVTZ, as indicated in the discussion that follows. Q-Chem’s RAS algorithm uses a resolution-of-identity (RI) approximation for the integrals.⁵ For the auxiliary (density fitting) basis set, we use either the ones designed for use with cc-pVXZ³⁷ or else those designed for use with the Ahlrichs SVP basis set.³⁸ In Q-Chem, these two basis sets are called RIMP2-cc-pVDZ and RIMP2-VDZ, respectively.

For the solvent model, we use the “conductor-like” (C-)PCM.^{16,39} The alternative “integral equation formalism” (IEF)-PCM^{40–43} is a formally more complete treatment of dielectric boundary conditions,¹⁶ and therefore in principle might be a better model for low-dielectric environments since C-PCM introduces errors of $\mathcal{O}(1/\epsilon)$ in the dielectric boundary conditions.^{18,44} In practice, however, this difference is usually numerically unimportant and the two models afford similar solvation energies even in non-polar solvents.^{16,43,45,46} The more important consideration is that both models contain an implicit correction for outlying charge,⁴⁷ i.e., for penetration of the wave function beyond the cavity. From a technical standpoint, IEF-PCM is somewhat more challenging to work with, and in particular its integral operators are more sensitive to discretization as compared to the surface potential operator in C-PCM.^{16,48} For these reasons, we have opted for the simpler C-PCM approach.

A van der Waals cavity is used to define the interface with the continuum.^{16,49} That cavity is constructed using Bondi’s atomic radii (as modified in Ref. 50), scaled by a factor of 1.2. Atomic spheres were discretized using 194 Lebedev grid points per sphere. The switching/Gaussian (SwiG) method is used for the cavity surface discretization.^{25,51}

For intermolecular CT states, we report some test calculations using constrained density functional theory (cDFT)⁵² to move an electron from one monomer to the other using a ground-state formalism. In these calculations, which were performed at the B3LYP/cc-pVTZ level, the charge constraint is implemented using Becke populations with atomic size corrections.^{53,54}

B. State-relaxed equilibrium procedure

All calculations in this section use the state-specific equilibrium procedure that is described in Sec. II B. The convergence criterion for the ground-state SCRF iterations (used to determine \hat{R}_0) is set

to 10^{-8} hartree and that for the excited-state SCRF iterations (to determine \hat{R}_k) is set to 10^{-6} hartree.

1. Distance dependence for CT excitation

To test the equilibrium version of the theory for a CT excitation, we consider intermolecular CT in the well studied model system,^{21,55–57} $\text{C}_2\text{H}_4 \cdots \text{C}_2\text{F}_4$, and in the somewhat larger (naphthalene)₂, whose CT states have also received attention.^{58–61} Both dimers are arranged in a parallel face-to-face orientation. Solvation corrections for singlet CT from C_2H_4 to C_2F_4 , and from one naphthalene monomer to the other, are shown in Fig. 3 as a function of reciprocal intermolecular separation, $1/R$. The quantity plotted is the difference between excitation energies computed using $\epsilon_0 = 78.4$ vs $\epsilon_0 = 1.0$, i.e., the solvent shift in water. RAS-SF calculations on $\text{C}_2\text{H}_4 \cdots \text{C}_2\text{F}_4$ use the cc-pVTZ basis set and RIMP2-cc-pVTZ auxiliary basis set while those on (naphthalene)₂ use the 6-31G* basis set and RIMP2-cc-pVDZ basis set.

For a point of comparison, we also computed the CT energies using a ΔSCF approach in conjunction with cDFT, a comparison that was also used in Ref. 11 to test the gas-phase RAS-SF CT procedure. With cDFT, both of the energies required for the ΔSCF calculation can be computed as ground-state DFT + PCM calculations, and comparison to an equilibrium model of the solvent response is therefore appropriate.

For both systems, the behavior of the solvent shift is very similar in both the RAS-SF and the cDFT calculations, despite significant differences in methodology: RAS is a correlated wave function approach that uses excited-state SCRF iterations to compute the state-specific solvation energy, while the cDFT-based ΔSCF procedure uses two ground-state calculations, one of them with a charge constraint that forces the monomers to integrate to ± 1 charge. Despite these differences, the solvent shift is found to be a linear function of $1/R$, in accordance with the Born model of two well-separated charges in a dielectric medium.¹⁶ For $\text{C}_2\text{H}_4 \cdots \text{C}_2\text{F}_4$, the shift varies by about 0.6 eV (14 kcal/mol) over a 1.5 Å change in R ,

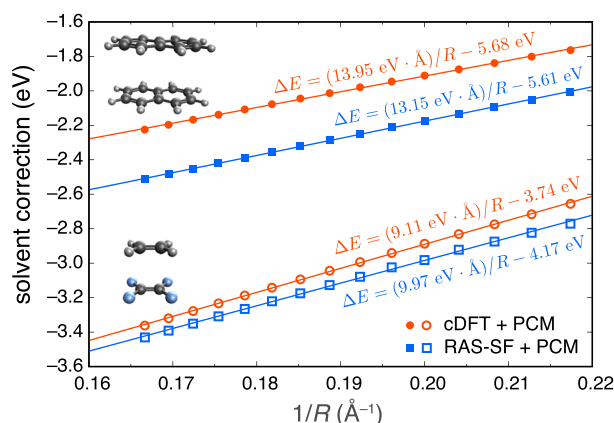


FIG. 3. Equilibrium PCM corrections ΔE , equal to the difference between aqueous ($\epsilon_0 = 78$) and vacuum ($\epsilon_0 = 1$) values for the excitation energy, for naphthalene dimer (filled symbols) and $\text{C}_2\text{H}_4 \cdots \text{C}_2\text{F}_4$ (open symbols). Calculations are reported using either RAS(h,p)-SF or ground-state cDFT, with C-PCM solvation in either case. Lines represent linear fits to the data with correlation coefficients $R^2 > 0.999$.

at both levels of electronic structure theory, despite the fact that the absolute shifts are offset by about 0.1 eV. The slope (solvent shift vs $1/R$) that is obtained from RAS-SF + PCM is within 10% of that obtained using cDFT + PCM for both dimers. These tests suggest that the combination of a PCM with the RAS-SF *Ansatz* for CT states provides a meaningful description of solvation for a photo-excited ion pair.

2. Perylene diimide dimer

Perylene diimide (PDI) and its derivatives have often been used as chromophores for singlet fission.^{62–65} The overall kinetics of the singlet fission process are solvent-dependent,^{65–67} and while CT states in PDI materials appear rapidly in polar solvents, high-yield singlet fission occurs equally rapidly in nonpolar solvents.^{65,68,69} Here, we use RAS-SF + PCM to explore the impact of solvent polarity on the singlet fission process.

Previous work has suggested that CT contributions are mixed into the key multi-exciton (ME) state of interest in singlet fission.^{70,71} The ME state is nominally a singlet-coupled pair of triplet excitations,^{15,72,73}

$$|^1\text{ME}\rangle = \frac{1}{\sqrt{3}}(|^3\text{A}_{+1}{}^3\text{B}_{-1}\rangle + |^3\text{A}_{-1}{}^3\text{B}_{+1}\rangle - |^3\text{A}_0{}^3\text{B}_0\rangle). \quad (29)$$

However, it may also contain small contributions from charge-separated determinants $|^+\text{A}^- \text{B}^-\rangle$ and $|^-\text{A}^+ \text{B}^+\rangle$. These sometimes appear in the form of charge-resonance (CR) states,^{15,59}

$$|\text{CR}\rangle = c_1|^+\text{A}^- \text{B}^-\rangle + c_2|^-\text{A}^+ \text{B}^+\rangle. \quad (30)$$

Despite its charge-separated character, the CR state may have a small or vanishing dipole moment if $c_1 \approx -c_2$, which is often the case for high-symmetry (or even near-symmetry) dimers.¹⁵ Gas-phase calculations suggest that the charge-separated states in (PDI)₂ are indeed of CR form.⁷¹

Here, we consider two geometries of (PDI)₂ that are taken from Ref. 70 and which afford the fastest and slowest singlet fission rates of the eight (PDI)₂ geometries that were examined in Ref. 71. The geometries of these two dimer models are illustrated on the left side of Fig. 4, and their frontier molecular orbitals are illustrated in the middle part of Fig. 4. The two dimers have somewhat different offset-stacking arrangements for the cofacial PDI monomers and also different face-to-face distances. We will examine the S_1 ($^1\pi\pi^*$) state of these dimers and also two different ME states that will be designated ^1ME (lower state) and $^1\text{ME}'$ (upper state), following Ref. 71.

Figure 5 reports the percentage of CT character for these three states, as quantified using the RAS-SF CT method,¹¹ as a function of solvent polarity. We consider the values $\epsilon_0 = 1$ (corresponding to vacuum boundary conditions), $\epsilon_0 = 3$ [characteristic of typical thin films, such as poly(methyl methacrylate), PMMA], and $\epsilon_0 = 37.5$ (representing acetonitrile). For model 1 of the dimer, the CT character varies only slightly as a function of these very significant changes in ϵ_0 , but for model 2 we observe significant changes in CT character in polar vs nonpolar environments. In particular, the S_1 state of model 2 exceeds 50% CT character in acetonitrile as compared to 30% CT character in the gas phase.

The molecular orbitals that are primarily responsible for the CT character are illustrated in the middle part of Fig. 4, with arrows

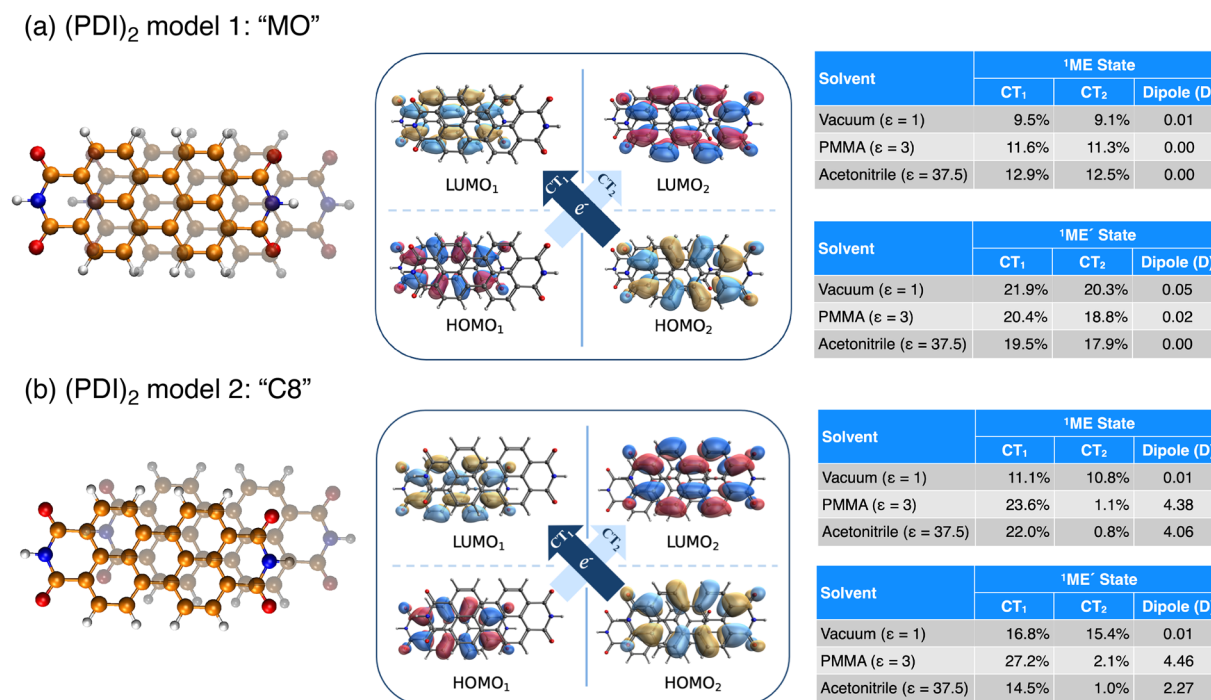


FIG. 4. RAS-SF/cc-pVDZ + PCM results for two geometries of (PDI)₂ that have been called (a) "MO" and (b) "C8."^{70,71} Structures are shown on the left and correspond to slightly different offsets in the lateral plane as well as different stacking distances, 3.46 Å for model 1 and 3.28 Å for model 2.⁷¹ Both models give rise to a pair of ¹ME states, and the middle panel illustrates the orbitals involved in the two largest CT configurations for both states. The tables on the right quantify the percentage CT character in each of these two configurations, along with the corresponding dipole moment, as a function of the solvent's dielectric constant. The state labeled ¹ME' is the higher-energy state.

that represent the two dominant configurations in the wave function. The right side of Fig. 4 quantifies the CT contribution in these two configurations, as a function of ϵ_0 . In the gas phase, the two CT configurations appear in essentially equal percentages, in both

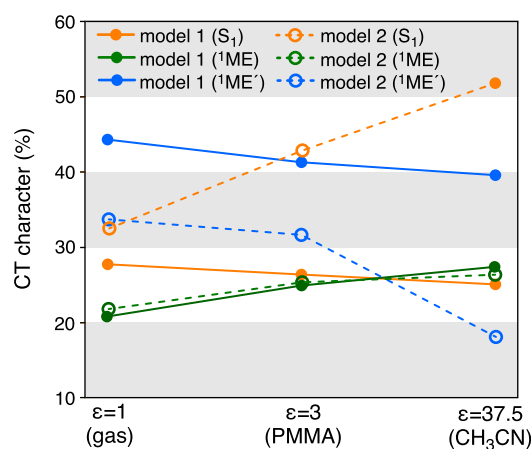


FIG. 5. Percentage CT character for the S_1 , ¹ME, and ¹ME' states in two different geometries of (PDI)₂, called models 1 and 2 (or "MO" and "C8") in Fig. 4. The ¹ME' state is defined to be a higher-energy state of pair of ME states that emerge from the calculation.

structures of (PDI)₂, leading in both cases to a CR state with a vanishing dipole moment. For model 2, however, a dielectric constant of $\epsilon_0 = 3$ is sufficient to break the symmetry, resulting in a net dipole moment. In contrast, symmetry-breaking is not observed in model 1 even in acetonitrile. This observation has potential ramifications for singlet fission. The CR character in model 2 facilitates the overall singlet fission process by increasing the electronic coupling between the S_1 and ¹ME states.^{71,73–75} Model 2, which transfers electrons in only one direction when $\epsilon_0 \geq 3$, might act as an energetic trap in a dielectric medium. This trap (an excimer state) would then compete with singlet fission and would lower the yield of the latter process. This suggests that one possible route to improving the efficiency of singlet fission in PDI dimers is to exploit geometries in which single-directional CT is inhibited. This difference highlights the fact that calculations carried out using vacuum boundary conditions are ill-positioned to address whether CT character plays a role in the singlet fission mechanism.

C. State-specific perturbation theory

In this section, we consider the ptSS approach for vertical excitation energies. We first examine the model systems $C_2H_4 \cdots C_2F_4$ and (naphthalene)₂ that were considered above, but we also investigate some pentacene dimers of interest in organic photovoltaic applications. These include a model system extracted from an intramolecular singlet fission chromophore,⁷⁵ and we note that

the role of CT states in the singlet fission mechanism has been much debated.^{15,62,72,73,76–78} For these calculations, the convergence criterion on the SCRF iterations was set to 10^{-10} hartree, with convergence achieved in 12–16 cycles.

1. Distance and solvent dependence of CT energies

We first consider the distance dependence of CT excitation energies in $\text{C}_2\text{H}_4 \cdots \text{C}_2\text{F}_4$ and in (naphthalene)₂, similar to the tests reported in Sec. III B 1 using the equilibrium solvation approach. Comparison to cDFT calculations is not appropriate in the present case, however, because we use a nonequilibrium formulation of the solvation correction in order to describe vertical excitation energies, and there is no analogous ΔSCF calculation. RAS-SF excitation energies *in vacuo* and in water are shown in Fig. 6 as a function of $1/R$. These calculations use the 6-31G* basis set and RIMP2-VDZ auxiliary basis set.

As expected, the excitation energies vary linearly with $1/R$ and the solvent shifts are quite large, e.g., $\Delta E = -1.33$ eV for $\text{C}_2\text{H}_4 \cdots \text{C}_2\text{F}_4$ at $R = 5$ Å (RAS-SF/cc-pVDZ level). This is comparable to the shift of $\Delta E = -1.15$ eV that was reported previously for this system using TD-DFT + ptSS-PCM.²¹

Table I lists the lowest CT excitation energy that is obtained for $\text{C}_2\text{H}_4 \cdots \text{C}_2\text{F}_4$ in six different solvents including cyclohexane (cHex), toluene, tetrahydrofuran (THF), chlorobenzene (ClBz), benzonitrile (BzCN), and water. Because we consider only the electrostatic part of the solvation energy, each solvent is fully characterized by the pair of values ϵ_0 and ϵ_∞ . Although nonelectrostatic solvation models are reasonably well established for ground-state solvation¹⁶ (e.g., using the SMx models),⁷⁹ there has been much less work on nonelectrostatic effects for excited states and we do not consider that topic here. (For a brief overview of this topic, see Ref. 16.) Changes

TABLE I. Lowest CT excitation energies and solvent corrections (both in eV) for $\text{C}_2\text{H}_4 \cdots \text{C}_2\text{F}_4$ at $R = 4.5$ Å in various solvents using the RAS-SF/6-31G* + ptSS-PCM approach.

Solvent	ϵ_0	ϵ_∞	Exc. energy		
			ptSS(0) ^a	ptSS(1) ^b	$G_k^{\text{ptSS}(1)}$ ^c
cHex	2.02	2.03	13.233	11.873	−1.360
Toluene	2.38	2.23	13.232	11.754	−1.478
THF	5.66	1.98	13.210	11.882	−1.327
ClBz	5.69	2.32	13.209	11.684	−1.525
BzCN	25.9	2.34	13.199	11.664	−1.535
Water	78.4	1.78	13.197	12.024	−1.173

^a $\Delta E_k^{\text{ptSS}(0)}$ [Eq. (27)].

^b $\Delta G_k^{\text{ptSS}(1)}$ [Eq. (25)].

^c Equation (21).

in nonelectrostatic interactions upon electronic excitation, including dispersion and Pauli repulsion, are expected to be much smaller than changes in the electrostatic solvation energy.

Listed in Table I is the first-order solvation correction to the excitation energy, $G_k^{\text{ptSS}(1)}$ [Eq. (21)], along with the zeroth-order approximation to the excitation energy itself, $\Delta E_k^{\text{ptSS}(0)}$ [Eq. (27)], and the first-order approximation to the same excitation energy, $\Delta G_k^{\text{ptSS}(1)}$ [Eq. (25)]. These three quantities are related according to Eq. (28). The zeroth-order quantity $\Delta E_k^{\text{ptSS}(0)}$ is the excitation energy computed in the frozen reaction field of the ground state and does not contain nonequilibrium corrections, i.e., it depends on ϵ_0 but not ϵ_∞ .

We note that the nonequilibrium correction $G_k^{\text{ptSS}(1)}$ exceeds 1 eV for the CT state that is considered in Table I, even in nonpolar solvents. Perhaps counterintuitively, this correction is smaller in water than it is in less polar solvents. This is ultimately a consequence of the partition between “slow” and “fast” (or “inertial” and “noninertial”) contributions to the solvent response,^{16,80} with the consequence that for a solvent like water where $\epsilon_0 \gg \epsilon_\infty$, a much greater proportion of the solvent response is frozen upon vertical excitation. This can be understood in terms of the “Pekar factor,” $\epsilon_\infty^{-1} - \epsilon_0^{-1}$, which replaces the familiar factor of $1 - \epsilon_0^{-1}$ in the Born (or generalized Born) solvation energy expression, in cases where vertical excitation energies are involved.⁸⁰ For example, $\epsilon_\infty^{-1} - \epsilon_0^{-1}$ appears in the Marcus theory expression for the outer-sphere reorganization energy, which is the earliest version of a nonequilibrium dielectric continuum theory.¹⁶

2. Pentacene dimer models

In thinking about CT states that might be relevant in organic photovoltaic applications,^{15,72} it is interesting to note that even nonpolar solvents (with $\epsilon_0 \lesssim 5$) afford a large nonequilibrium correction to a CT excitation energy. This can be seen for $\text{C}_2\text{H}_4 \cdots \text{C}_2\text{F}_4$ in Table I, for example. The nonequilibrium correction comes from the optical dielectric constant, which is related to the electronic polarizability of the solvent molecules and has values $\epsilon_\infty = 1.7$ –2.3 for most common solvents,¹⁶ even while the static dielectric constant varies from $\epsilon_0 = 2$ –4 for nonpolar hydrocarbons up to $\epsilon_0 = 78$ for water.

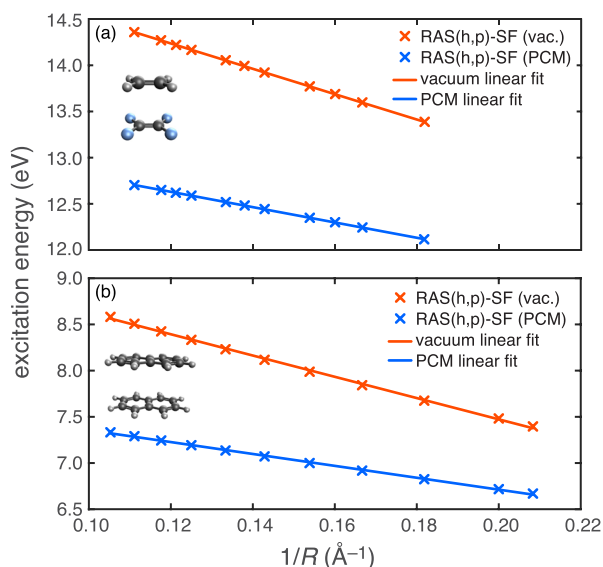


FIG. 6. Excitation energies in vacuum and in aqueous solution ($\epsilon_0 = 78.4$ and $\epsilon_\infty = 1.78$), as a function of inverse monomer separation, for (a) $\text{C}_2\text{H}_4 \cdots \text{C}_2\text{F}_4$ and (b) naphthalene dimer. Excitation energies were computed at the RAS-SF/6-31G* level with the ptSS-PCM approach to correct the excitation energies for solvent effects.

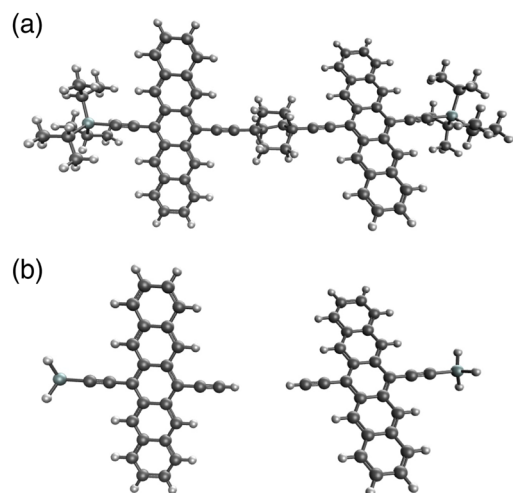


FIG. 7. Structural models for an intramolecular singlet fission chromophore based on pentacene dimer: (a) the original chromophore from Ref. 75, which includes a 1,4-diethynylbicyclo[2.2.2]octane spacer and tri-isobutyl silyl side chains, vs (b) a truncated and unlinked dimer model, in which the side chains are replaced by SiH_3 and the spacer has been replaced by ethynyl side chains. Positions of the atoms that constitute the pentacene dimer core are the same in both systems.

With this in mind, we next consider an example relevant to organic photovoltaics, namely, a pentacene dimer model of a chromophore that undergoes intramolecular singlet fission,⁷⁵ which is depicted in Fig. 7(a). Calculations are reported here using the unlinked dimer model that is shown in Fig. 7(b). We have

confirmed, via CIS calculations, that the model system and the full chromophore afford excitation energies within about 0.3 eV of one another, which is sufficient for our purposes. The same is true for two other truncated models (not shown) in which the side chains or the spacer group were removed, but not both, indicating that the tri-isobutyl silyl side chains in the full chromophore [Fig. 7(a)] function mainly for solubility while the spacer moiety functions mostly to position the pentacene chromophores relative to one another. The singlet fission dynamics can be quite sensitive to the relative position and orientation of the pentacene moieties,⁸¹ so the atomic positions of the pentacene dimer core are the same in the model system as they are in the full chromophore. Calculations on the model are reported below in six different solvents, and in each case we compute six RAS-SF states: the ground state, the first LE state (which is T_1), two left CT states (LCT1 and LCT2), and two right CT states (RCT1 and RCT2). These calculations use the 6-31G* basis set and RIMP2-VDZ auxiliary basis set. Selected results are shown in Table II, focusing on the LCT1 state but also including LE1 for comparison.

We observe that stabilization of the ground state increases with solvent polarity, and at the level of the zeroth-order eigenvalues $E_k^{(0)}$, which are computed in the reaction field of the ground state, approximately the same stabilization is obtained for the LCT1 state as for the ground state itself, to within a few millihartree. The first-order corrected excitation energies show a different trend, however. Here, both the static and optical dielectric constants are in play, and the value of the first-order correction $G_k^{\text{ptSS}(1)}$ is smaller in water than it is in nonpolar solvents. As explained in Sec. III C 1, this behavior results from the fact that water has a much larger fraction of its total polarization response frozen upon vertical excitation since

TABLE II. RAS-SF/6-31G* + ptSS-PCM energies for the pentacene dimer model in Fig. 7(b), computed in various solvents. Values in parenthesis are shifts relative to the corresponding calculation in vacuum.

Solvent	ϵ_0	ϵ_∞	$E_k^{(0)}$ (hartree)		LCT1 exc. energy (eV)		$\Delta G_k^{\text{ptSS}(1)}$ (eV) ^a	
			E_0	LCT1	$\Delta E_k^{\text{ptSS}(0)}$ ^b	$G_k^{\text{ptSS}(1)}$ ^c	LCT1 ^d	LE1(T_1)
Vacuum	1.00	1.00	−2564.965	−2564.778	5.074	1.136
cHex	2.02	2.03	−2564.993 (−0.028)	−2564.807 (−0.029)	5.069	−1.166	3.904 (−1.171)	1.131 (−0.005)
Toluene	2.38	2.23	−2564.998 (−0.033)	−2564.812 (−0.034)	5.068	−1.267	3.801 (−1.273)	1.130 (−0.006)
THF	5.66	1.98	−2565.015 (−0.050)	−2564.829 (−0.050)	5.064	−1.137	3.928 (−1.147)	1.128 (−0.008)
ClBz	5.69	2.32	−2565.015 (−0.050)	−2564.829 (−0.050)	5.064	−1.307	3.758 (−1.317)	1.128 (−0.008)
BzCN	25.9	2.34	−2565.025 (−0.060)	−2564.839 (−0.061)	5.061	−1.315	3.746 (−1.328)	1.126 (−0.010)
Water	78.4	1.78	−2565.027 (−0.070)	−2564.841 (−0.063)	5.061	−1.005	4.056 (−1.018)	1.126 (−0.010)

^aCorrected nonequilibrium excitation energy [Eq. (25)].

^bZeroth-order excitation energy [Eq. (27)].

^cFirst-order nonequilibrium correction [Eq. (21)].

^dNote that $\Delta G_k^{\text{ptSS}(1)} = \Delta E_k^{\text{ptSS}(0)} + G_k^{\text{ptSS}(1)}$ [Eq. (28)].

$\epsilon_0 \gg \epsilon_\infty$. This is a feature of the Marcus partition of the polarization into fast and slow components.^{16,21,80} In nonpolar or weakly polar solvents, where ϵ_0 is much closer to ϵ_∞ , the nonequilibrium correction amounts to a greater fraction of the total solvation energy of the excited state, and the trend in first-order corrections $G_k^{\text{ptSS}(1)}$ is governed primarily by the value of ϵ_∞ . As noted elsewhere,^{16,21,82} the partition between inertial and noninertial solvent response need not be done in this way, and the total solvation correction is essentially the same in Pekar's alternative partition scheme but is apportioned differently into zeroth-order and corrective terms.^{16,82} For the LE1 state, we also observe a reduction in the excitation energy as solvent polarity increases, but the effect is smaller as compared to the LCT1 state because LE1 does not involve significant charge separation.

We next compare RAS-SF + ptSS-PCM results to the corresponding calculation at the CIS level, which will illustrate the ease of reaching target states with the RAS-SF procedure. Table III shows results for the pentacene dimer model in Fig. 7(b), in two different solvents. In cyclohexane, we observe a correspondence between the RAS-SF states LCT1 (triplet) and LCT2 (singlet) and the 37th and 38th excited states obtained from the CIS calculation. Comparing excitation energies, the RAS-SF and the CIS results agree within 0.04 eV and the dipole moments agree within 0.5 D. A similar correspondence is observed between the RAS-SF states RCT1 and RCT2, and the 39th and 40th excited states obtained from the CIS calculation. The principle pair of natural transition orbitals (NTOs) for states 37 and 39 are plotted in Fig. 8, from the CIS calculation, which confirms the CT character of the states in question. (The RAS-SF states have CT character by construction.) While the excitation energies are similar, indicative of the lack of significant dynamical correlation in the RAS-SF wave function,⁷ the CIS approach

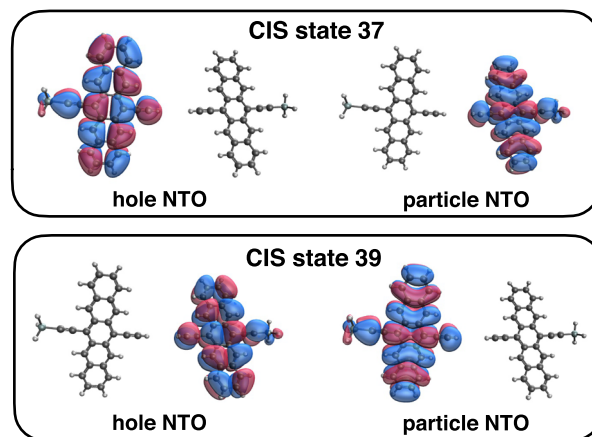


FIG. 8. Principle NTO pair for each of CIS states 37 and 39, depicting a CT excitation between pentacene fragments.

necessitates the calculation of a large number of excited states, which must then be analyzed in terms of orbitals and amplitudes in order to deduce which states possess CT character. With RAS-SF, on the other hand, one may target the CT states directly (essentially by fiat), so that these emerge as the lowest eigenvalues of the CT block of the Hamiltonian.¹¹

Steady state absorption measurements performed on the intramolecular singlet fission chromophore in Fig. 7(a) indicate a red shift in the absorption maxima as solvent polarity increases, which was taken as evidence that the excited state is more polar than the ground state.⁷⁵ We observe a similar pattern for the unlinked dimer

TABLE III. RAS-SF/ and CIS/6-31G* excitation energies and excited-state dipole moments for the pentacene dimer model in Fig. 7(b), computed in various solvents using the nonequilibrium ptSS-PCM approach.

State	Multip.	Solvent	Exc. energy (eV)		Dipole mom. (D) ^a
			ptSS(0)	ptSS(1)	
CIS state 37	Triplet	Cyclohexane	5.038	3.863	65.47
CIS state 38	Singlet	Cyclohexane	5.038	3.863	65.47
RAS LCT 1	Triplet	Cyclohexane	5.069	3.904	64.99
RAS LCT 2	Singlet	Cyclohexane	5.069	3.904	64.99
CIS state 39	Triplet	Cyclohexane	5.038	3.864	65.47
CIS state 40	Singlet	Cyclohexane	5.038	3.864	65.47
RAS RCT 1	Triplet	Cyclohexane	5.070	3.906	64.83
RAS RCT 2	Singlet	Cyclohexane	5.070	3.906	64.83
CIS state 37	Triplet	Benzonitrile	5.030	3.705	65.46
CIS state 38	Singlet	Benzonitrile	5.030	3.705	65.46
RAS LCT 1	Triplet	Benzonitrile	5.061	3.746	64.99
RAS LCT 2	Singlet	Benzonitrile	5.061	3.746	64.99
CIS state 39	Triplet	Benzonitrile	5.031	3.706	65.46
CIS state 40	Singlet	Benzonitrile	5.031	3.706	65.46
RAS RCT 1	Triplet	Benzonitrile	5.062	3.748	64.83
RAS RCT 2	Singlet	Benzonitrile	5.062	3.748	64.83

^a CIS excited-state dipole moments are unrelaxed.

TABLE IV. Excitation energies (ΔE) and excited-state dipole moments (μ) for the full chromophore in Fig. 7(a) vs the unlinked dimer model in Fig. 7(b). All calculations are performed in vacuum.

System	State	ΔE (eV)	μ (D)
Full ^a	S ₀	0.00	0.22
Full ^a	T ₁	0.89	0.38
Full ^a	T ₈	3.39	63.40
Full ^a	S ₆	3.40	64.46
Full ^a	T ₉	3.41	64.78
Full ^a	S ₇	3.42	64.68
Model ^b	S ₀	0.000	0.03
Model ^b	LE1 (triplet)	1.136	0.04
Model ^b	LCT1 (triplet)	5.074	64.99
Model ^b	LCT2 (singlet)	5.074	64.99
Model ^b	RCT1 (triplet)	5.076	64.82
Model ^b	RCT2 (singlet)	5.076	64.82

^aSA15-XMCQDPT(8,8)/DZV level, from Ref. 75.^bRAS-SF/6-31*G level.

model, as discussed above, with a decrease in the excitation energy as a function of increasing solvent polarity, although such a shift is observed in both the LE and the CT states.

Table IV compares RAS-SF results for the unlinked dimer model to multireference perturbation theory calculations on the full chromophore, from Ref. 75. The latter calculations were performed *in vacuo* so the same is true for the RAS-SF calculations in Table IV. Both sets of calculations reveal four closely spaced excited states of alternating multiplicity (singlet and triplet), with significant CT character as indicated by excited-state dipole moments $\mu \approx 65$ D. This comparison suggests at least a qualitative correspondence between the two levels of theory, even if the gas-phase excitation energies are rather different.

TABLE V. Excitation energies (ΔE) and excited-state dipole moments (μ), computed in benzonitrile solution, for the full chromophore in Fig. 7(a) vs the unlinked dimer model in Fig. 7(b).

System	State	Exc. energy (eV)		μ (D)
		ΔE	Shift ^a	
Full ^b	T ₁	0.61	−0.01	0.04
Full ^b	S ₅	2.63	−1.73	62.06
Full ^b	T ₁₁	2.62	−1.73	61.57
Full ^b	S ₆	2.92	−1.43	56.46
Full ^b	T ₁₈	2.97	−1.39	55.03
Model ^c	LE1	1.13	−0.01	0.06
Model ^c	LCT1	3.75	−1.33	64.99
Model ^c	LCT2	3.75	−1.33	64.99
Model ^c	RCT1	3.75	−1.33	64.83
Model ^c	RCT2	3.75	−1.33	64.83

^aSolvent shift relative to vacuum value.^bCISD calculations using the AM1 Hamiltonian and a SCRF solvation model, from Ref. 75.^cRAS-SF/6-31*G with ptSS-PCM solvation.

In Ref. 75, the effects of solvent polarity were investigated by comparing excitation energies in vacuum to those computed in benzonitrile, using a SCRF model in conjunction with a semi-empirical Hamiltonian. These results are reproduced in Table V alongside the corresponding RAS-SF + ptSS-PCM results. Semi-empirical calculations in Ref. 75 afford four closely spaced singlet excited states (in vacuum), in the range $\Delta E = 2.63$ – 2.97 eV, with dipole moments ranging from $\mu = 55.0$ – 62.1 D and which are stabilized by 1.4–1.7 eV in benzonitrile whereas other nonpolar states are stabilized by ≤ 0.01 eV. With RAS-SF and nonequilibrium ptSS-PCM solvation, we obtain four closely spaced states ranging from $\Delta E = 3.75$ – 3.91 eV with dipole moments $\mu = 64.8$ – 65.0 D, which are stabilized by 1.33 eV in benzonitrile. By contrast, the LE1 (T₁) state hardly shifts at all in benzonitrile solvent, consistent with T₁ results from Ref. 75. The present calculations therefore corroborate the results in Ref. 75, indicating that “polar” states (meaning those with CT character) are considerably shifted whereas “nonpolar” (LE) states are not. Note that the nonpolar S₁ bright state should have essentially the same charge density as T₁ and thus will not be significantly shifted by the solvent model.

IV. CONCLUSIONS

We have formulated, implemented, and tested a state-specific approach to solvation for RAS-SF wave functions. Both equilibrium (self-consistent and fully relaxed) and nonequilibrium (vertical excitation) versions are reported, the latter within a perturbative “ptSS” approximation introduced in earlier work.^{20,21} This new methodology opens the possibility to describe dielectric continuum effects on CT states within a cost-effective and easy-to-use wave function model for strong correlation, which can describe multi-exciton states and other types of excitations that are beyond the reach of (or poorly described by) single-excitation methods such as CIS and TD-DFT. Benchmark tests indicate good agreement with other methods for well-separated CT excitations (ion-pair states), in systems such as C₂H₄ ··· C₂F₄ and (naphthalene)₂. The ptSS approach to vertical excitation energies agrees with literature results for stabilization of CT states vs LE states, in a model of a covalently linked pentacene dimer that undergoes intramolecular singlet fission.

Calculations on (PDI)₂ in two different geometries provide a rationale to understand the very different singlet fission rates that have previously been calculated for these systems. These calculations suggest that dielectric stabilization creates excitonic trap states in one geometry but not the other, by breaking symmetry and localizing charge. This observation has potentially important implications for the design of materials with good singlet fission rates, as the excitation spectra of model chromophores can now be easily tested as a function of solvent polarity. It also suggests that gas-phase calculations, even with highly correlated wave function models, may not offer a realistic description of singlet fission in solution, where polarization-induced charge localization is observed in solvents with dielectric constants as small as $\epsilon_0 = 3$, but not in vacuum ($\epsilon_0 = 1$).

SUPPLEMENTARY MATERIAL

See the [supplementary material](#) for coordinates for all structures considered.

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AUTHOR DECLARATIONS

Conflict of Interest

J.M.H. serves on the board of directors of Q-Chem, Inc.

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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