

# Beyond “Mega”: Origin of the “Giga” Stokes Shift for Triazolopyridiniums

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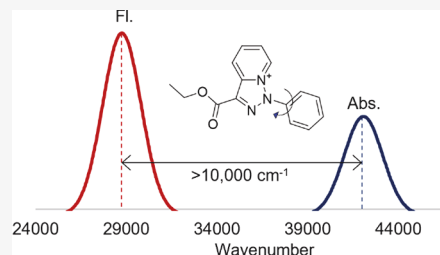


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**ABSTRACT:** Over the past decade, fluorophores that exhibit “mega” Stokes shifts, defined to be Stokes shifts of greater than 100 nm, have gained considerable attention due to their potential technological applications. A subset of these fluorophores have Stokes shifts of at least  $10,000\text{ cm}^{-1}$ , for whom we suggest the moniker “giga” Stokes shift. The majority of “giga” Stokes shifts reported in the literature arise from the twisted intramolecular charge transfer mechanism, but this mechanism does not fit empirical characterization of triazolopyridinium (TOP). This observation inspired a density functional theory (DFT) and time-dependent DFT study of TOP, and several related fluorophores, to elucidate the novel photophysical origin for the “giga” Stokes shift of TOP. The resulting computational models revealed that photoexcitation of TOP yields a zwitterionic excited state that undergoes significant structural relaxation prior to emission. Most notably, TOP has two orthogonal moieties in the ground state that adopt a coplanar geometry in the excited state. According to Hückel’s rule, both the heterocycle and phenyl moieties of TOP should be aromatic in an orthogonal ground state. However, according to Baird’s rule, these individual moieties should be anti-aromatic in the excited state. By relaxing to a coplanar conformation in the excited state, TOP likely forms a single aromatic system consisting of both the heterocycle and phenyl moieties.



## INTRODUCTION

The development of organic fluorophores with large Stokes shifts is a growing area of scientific research with tremendous technological potential. The moniker “mega” Stokes shift was first used in 2010 to describe fluorophores with Stokes shifts of greater than 100 nm,<sup>1</sup> and the set of molecules that fit this criterion has recently been reviewed.<sup>2</sup> However, this definition of a large Stokes shift is somewhat misleading. In general, the large energy difference between the absorption and emission bands of “mega” Stokes shift fluorophores minimizes self-absorption and favors technological applications. Thus, a major motivation for identifying new “mega” Stokes shift fluorophores is to minimize the overlap between the excitation and emission bands. The overlap of the excitation and emission bands depends upon both the Stokes shift and the bandwidths, so the role of bandwidths also needs to be considered. In solution, the main contribution to emission and excitation bandwidths is an unresolved vibronic structure. As a result, bandwidths are relatively consistent for aromatic molecules when quantified in an energy unit such as wavenumbers. However, when bandwidths are reported in wavelength, near-infrared (nIR) bands are significantly broader than ultraviolet (UV) bands due to the nonlinear dependence of energy on wavelength in the Planck–Einstein relation. Consequently, it can be difficult to distinguish fluorophores with minimal overlap between their excitation and emission bands from fluorophores with moderate overlap that emit in the nIR when quantifying the Stokes shift in wavelength. This issue can be

avoided by reporting Stokes shifts in energy units, such as wavenumbers.

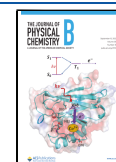
Compared to “mega” Stokes shift fluorophores,<sup>1,2</sup> a much smaller set of molecules have Stokes shifts greater than  $10,000\text{ cm}^{-1}$ ,<sup>3–7</sup> for whom we suggest the designation “giga” Stokes shift. In the past, “mega” Stokes shift fluorophores have been utilized for imaging,<sup>1,8–13</sup> thermometry,<sup>4,14</sup> sensing,<sup>15–17</sup> and organic light-emitting diode (OLED)<sup>18</sup> applications. Several of these applications rely upon the minimal self-absorption of “mega” Stokes shift fluorophores, which is expected to be further minimized for “giga” Stokes shift fluorophores. Thus, the preparation of novel organic fluorophores that exhibit “giga” Stokes shifts is expected to be of considerable technological utility.

To date, “giga” Stokes shifts have been attributed to the twisted intramolecular charge transfer (TICT) mechanism. TICT is a phenomenon whereby two coplanar moieties adopt a perpendicular orientation in the electronic excited state to decouple the cationic and anionic radicals generated by charge transfer.<sup>19</sup> The photophysics of a number of “giga” Stokes shift fluorophores have been attributed to the TICT mechanism

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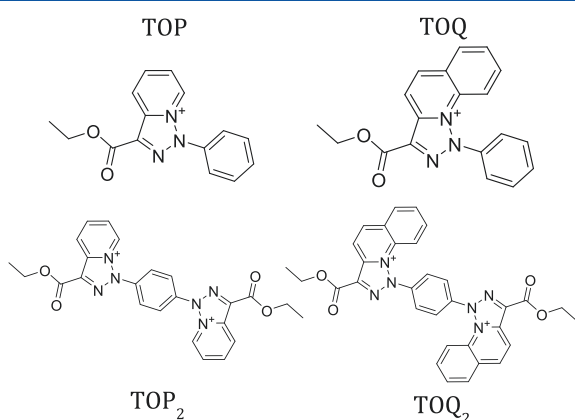
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based upon time-dependent density functional theory (TDDFT) calculations.<sup>4–6</sup> One major contribution to the Stokes shift of TICT fluorophores is excited structural relaxation. The zwitterionic excited state is stabilized by a twisted geometry, whereas the neutral ground state is destabilized by a twisted geometry, resulting in a smaller energy gap and red-shifted emission compared to the excitation wavelength. A second major contribution to the Stokes shift of TICT fluorophores is the influence of the zwitterionic excited state on the solvent structure. The zwitterionic excited state will induce a significant reorganization of the solvent structure, particularly for a polar solvent. Again, this will stabilize the excited state, destabilize the ground state, and red-shift the emission transition relative to the excitation transition.

The noteworthy exception to the emerging paradigm that “giga” Stokes shifts arise from TICT is triazolopyridinium (TOP). Efficient syntheses of TOP and the TOP dimer (TOP<sub>2</sub>) using a Cu(II) oxidant were first reported in 2013 (Figure 1).<sup>3</sup> TOP exhibited a “giga” Stokes shift of 11,790



**Figure 1.** Fluorophores whose photophysical mechanisms were modeled in this article. These include monomeric and dimeric triazolopyridiniums (TOP and TOP<sub>2</sub>), plus monomeric and dimeric triazoloquinoliniums (TOQ and TOQ<sub>2</sub>).

cm<sup>−1</sup> in water, and the excitation transition was assigned to intramolecular charge transfer based upon TDDFT calculations. Later, in 2017, efficient syntheses of the triazoloquinolinium monomer (TOQ) and triazoloquinolinium dimer (TOQ<sub>2</sub>) were reported, along with more extensive characterization of the photophysics for this family of dyes.<sup>7</sup> Importantly, X-ray crystallographic characterization of TOP, and computational modeling of TOQ, has indicated that these molecules adopt twisted ground-state geometries. Thus, the “giga” Stokes shifts of TOP cannot arise from TICT because it is already twisted prior to photoexcitation. This observation motivated us to launch a detailed investigation of the photophysical mechanisms for TOP and TOQ dyes to gain insight into an alternative strategy for preparing “giga” Stokes shift fluorophores.

In this work, spectroscopically validated density functional theory models for triazolopyridinium and triazoloquinolinium salts were developed to gain insight into the novel photophysics of the “giga” Stokes shift fluorophores. Ground-state (S<sub>0</sub>) geometries for TOP, TOP<sub>2</sub>, TOQ, and TOQ<sub>2</sub> were predicted using six different density functionals. The DFT-predicted S<sub>0</sub> geometries for TOP were compared to the X-ray

crystal structure of this molecule to assess the accuracies of ground-state structures predicted by each functional.<sup>3</sup> Next, the excitation spectra for all four dyes were modeled by TDDFT calculations using the same six functionals. The accuracies of these predictions were gauged by comparing the experimental and TDDFT-predicted UV/Vis absorption (Abs) spectra.<sup>3,7</sup> Finally, TDDFT was employed to predict the excited-state (S<sub>1</sub>) geometries and emission spectra for TOP, TOP<sub>2</sub>, TOQ, and TOQ<sub>2</sub>. The experimental and predicted Stokes shifts were compared to judge the accuracy of these calculations. Ultimately, these models revealed that the “giga” Stokes shift of TOP arises from a photophysical mechanism that can be rationalized with Hückel and Baird’s rules.<sup>20–23</sup>

## METHODS

**Ground-State Electronic Structure Calculations.** The minimum energy ground-state geometries of all four dyes were obtained via complete geometry optimization calculations using DFT. The initial structural model of TOP was based upon the X-ray crystal structure of this molecule.<sup>3</sup> Initial structural models for TOP<sub>2</sub>, TOQ, and TOQ<sub>2</sub> were prepared by modifying the TOP starting structure using the Argus Lab software program (Planaria software). All electronic structure calculations reported in this article utilized the ORCA 4.0.0.2 software program as installed on the Vermont Advanced Computing Core.<sup>24</sup> Geometry optimizations were conducted using the BLYP,<sup>25,26</sup> PBE,<sup>27</sup> B3LYP,<sup>28</sup> PBE0,<sup>29</sup> ωB97,<sup>30</sup> and ωB97X<sup>30</sup> density functionals. All geometry optimizations utilized a def2-TZVP basis set,<sup>31</sup> a def2/J auxiliary basis set,<sup>32</sup> and the TightSCF convergence algorithm. For the hybrid density functionals, the RIJCOSX method was used to speed up calculation of the Coulomb and exchange terms.<sup>33</sup> Cartesian coordinates for all fully optimized gas phase structures are available in the [Supporting Information](#).

Following complete geometry optimization in the gas phase, the electronic structures of each dye were calculated in solution. Single-point calculations were completed using the same density functionals and basis sets noted above with the addition of a conductor-like polarizable continuum model (CPCM) for solvent.<sup>34</sup> For TOP and TOP<sub>2</sub>, the CPCM parameters were set to model solvation by water. For TOQ and TOQ<sub>2</sub>, the CPCM parameters were set to model solvation by methanol and acetonitrile, respectively. To aid in the analysis of the DFT data, valence molecular orbitals (MOs) were plotted in gOpenMol with isodensity values of 0.001 a.u.<sup>35,36</sup>

**Excited-State Electronic Structure Calculations.** The UV/Vis Abs spectra of the four dyes were predicted using TDDFT calculations. All UV/Vis Abs spectral prediction calculations utilized the fully optimized, gas phase geometries. These calculations employed the same density functionals, basis sets, and solvation models as the ground-state calculations. To predict the UV/Vis Abs spectra, the 20 lowest energy excited states were predicted using TDDFT with an expansion space of 120 vectors. The predicted UV/Vis Abs spectra shown in this article were generated by convoluting Gaussian-shaped bands with full-width, half-maximum bandwidths of 2500 cm<sup>−1</sup>.

The Stokes shifts for each dye were predicted using excited-state geometry optimizations. The starting structures for these calculations were the fully optimized, ground-state structures. Excited-state geometry optimization calculations employed the same density functionals and basis sets noted above but did not

include an implicit solvent model. TDDFT, using the same parameters as for the UV/Vis Abs spectral predictions, was used to calculate the minimum energy structure for the  $S_1$  excited state of each dye. Cartesian coordinates for all  $S_1$  excited-state structures are available in the [Supporting Information](#).

Finally, the fluorescence spectra for all four solvated dyes were predicted using CPCM and TDDFT. All fluorescence spectral predictions employed the  $S_1$  excited-state geometries. The fluorescence spectral predictions employed the same density functionals, basis sets, and solvation models described above. The TDDFT calculations used the same parameters as for the UV/Vis Abs spectral predictions. Again, to aid in the analysis of the DFT data, valence MOs were plotted in gOpenMol with isodensity values of 0.001 a.u.<sup>35,36</sup> Finally, the fluorescence spectra were generated by convoluting Gaussian-shaped bands with full-width, half-maximum bandwidths of 2500  $\text{cm}^{-1}$ .

## RESULTS

**$S_0$  Ground-State Geometries.** The  $S_0$  ground-state geometry of TOP was predicted using a variety of density functionals and compared to published X-ray crystal structure data. Structural models were prepared based upon generalized gradient approximation (GGA) functionals (BLYP and PBE),<sup>25–27</sup> hybrid functionals (B3LYP and PBE0),<sup>28,29</sup> and range-separated functionals ( $\omega$ B97 and  $\omega$ B97X).<sup>30</sup> All structural models utilized a def2-TZVP triple- $\zeta$  basis set.<sup>31</sup> Generally, all six density functionals provided good models for the TOP structure, with RMSD values between the computational and crystallographic structures ranging from 0.253 to 0.354 Å for the nonhydrogen atoms (Figure 2 and Figures S1–

with experiment (Table 1 and Tables S1–S5). Thus, although the B3LYP density functional yielded the most accurate

**Table 1.** B3LYP  $S_0$  Geometries of TOP Dyes

	1 (Å) <sup>a</sup>	2 (Å) <sup>a</sup>	3 (Å) <sup>a</sup>	$\alpha$ (°) <sup>a</sup>
TOP(exp) <sup>b</sup>	1.439	1.364	1.323	59.7
TOP(DFT)	1.436	1.368	1.311	66.7
TOP <sub>2</sub> (DFT) <sup>c</sup>	1.426	1.370	1.320	55.6
TOQ(DFT)	1.442	1.375	1.311	51.0
TOQ <sub>2</sub> (DFT) <sup>c</sup>	1.445	1.383	1.324	58.0

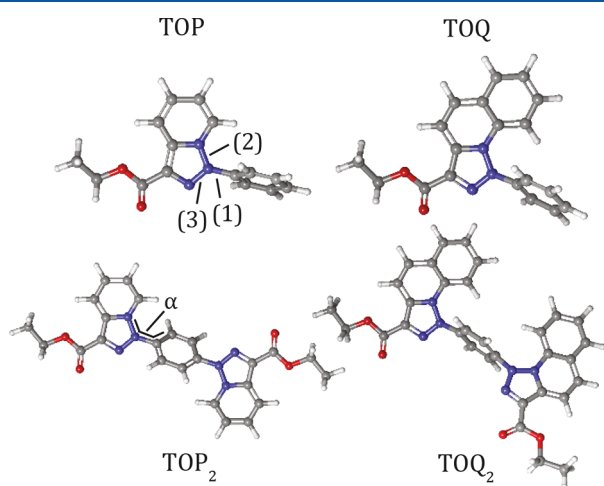
<sup>a</sup>See Figure 2. <sup>b</sup>Ref 3. <sup>c</sup>Data reported for TOP<sub>2</sub> and TOQ<sub>2</sub> are the average for both heterocycle moieties.

structural model for TOP, all six density functionals predicted  $S_0$  geometries in good agreement with experiment.

Next, the B3LYP density functional was used to predict the ground-state structures of TOP<sub>2</sub>, TOQ, and TOQ<sub>2</sub>. The lengths of three key bonds for the triazole moiety are relatively unperturbed by the substituent changes (Table 1). For all four dyes, the average C–N linker bond length is 1.44 Å, with a standard deviation of <0.01 Å, and all four dyes exhibit asymmetric bonding within the triazole moiety (average bond lengths of 1.37 and 1.32 Å, with standard deviations of <0.01 Å). All four dyes also exhibit rotation about the heterocycle–phenyl linker. The average rotation about the C–N linker bond is 60°, with a standard deviation of <10°, which should be sufficient to break the conjugation between the heterocycle and phenyl moieties. This bond rotation can be readily understood in terms of Hückel's rule, which states that conjugated  $\pi$  systems with  $4n + 2$  electrons are aromatic, whereas conjugated  $\pi$  systems with  $4n$  electrons are anti-aromatic.<sup>20–22</sup> The triazolopyridinium heterocycle contains 10  $\pi$  electrons, the triazoloquinolinium heterocycle contains 14  $\pi$  electrons, and the phenyl ring has six  $\pi$  electrons. Thus, each of these ring systems is expected to be aromatic, but the coplanarity of the heterocycle and phenyl rings would be expected to create an anti-aromatic system. In summary, the twisted  $S_0$  ground-state geometries of TOP, TOP<sub>2</sub>, TOQ, and TOQ<sub>2</sub> can all be rationalized on the basis of Hückel's rule.

**UV/Vis Abs Spectra.** The UV/Vis Abs spectra of all four TOP and TOQ dyes were predicted using TDDFT. Briefly, the electronic structures of solvated dyes were predicted using the optimized  $S_0$  ground-state geometries described above, the same six density functionals described above, and the CPCM implicit solvation model.<sup>34</sup> TDDFT was employed to model the excited-state electronic structures and UV/Vis Abs spectra of these dyes (Figure 3 and Figures S6–S10). The GGA functionals consistently underestimated the electronic transition energies measured by UV/Vis Abs spectroscopy, whereas the hybrid and range-separated functionals consistently overestimated the electronic transition energies (Table 2). Overall, the B3LYP/def2-TZVP model yielded the most accurate transition energies with an average absolute error of 600  $\text{cm}^{-1}$  between this model and experiment.

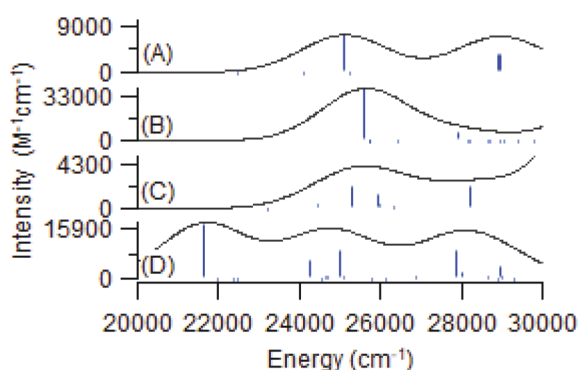
However, the TDDFT-predicted UV/Vis Abs intensities are a better gauge for the accuracy of these calculations than the TDDFT-predicted UV/Vis Abs energies. The trend observed above where the transition energies increase with increasing amounts of Hartree–Fock exchange had been observed previously for a set of 29 functionals and 500 molecules.<sup>37</sup> So, the accurate prediction of the transition energies by the B3LYP functional may simply arise from a cancellation of



**Figure 2.**  $S_0$  ground-state geometries of TOP (top left), TOP<sub>2</sub> (bottom left), TOQ (top right), and TOQ<sub>2</sub> (bottom right). The ground-state structures were optimized using the B3LYP density functional and the def2-TZVP basis set. The RMSD between B3LYP/def2-TZVP and the crystallographic structure of TOP is 0.253 Å for the nonhydrogen atoms.

S5).<sup>3</sup> The B3LYP model had the smallest RMSD of all six, so this model was used for all further ground-state structural analysis. It is important to note that, in addition to a good overall RMSD, all DFT-predicted N–N bond lengths within the triazole moiety, and the C–N bond length between the heterocycle and phenyl moieties, were in excellent agreement





**Figure 3.** TDDFT-predicted UV/Vis Abs spectra for the TOP monomer in water (A), TOP dimer in water (B), TOQ monomer in methanol (C), and TOQ dimer in acetonitrile (D). The electronic structures were modeled using the BLYP density functional and the def2-TZVP basis set. The solvent was modeled using the CPCM implicit solvation model.

**Table 2.**  $S_0 \rightarrow S_1$  Abs Energies ( $\text{cm}^{-1}$ ) of TOP Dyes

	TOP	TOP <sub>2</sub>	TOQ	TOQ <sub>2</sub>	error
(exp)	33,100 <sup>a</sup>	32,200 <sup>a</sup>	29,300 <sup>b</sup>	28,800 <sup>b</sup>	
BLYP	25,100	25,700	25,600	21,700	6300
PBE	26,000	25,800	26,200	22,000	5900
B3LYP	33,600	31,800	30,200	29,400	600
PBE0	35,700	32,800	31,600	31,100	2000
$\omega$ B97	42,100	38,100	36,200	34,000	6800
$\omega$ B97X	41,800	38,500	35,800	35,400	7000

<sup>a</sup>Ref 3. <sup>b</sup>Ref 7.

errors derived from the overall biases of these functionals. Alternatively, the TDDFT-predicted UV/Vis Abs intensities depend upon the overlap between the donor and acceptor states. As a result, the TDDFT-predicted UV/Vis Abs intensities are excellent indicators for the accuracy of the valence orbital shapes predicted by DFT.

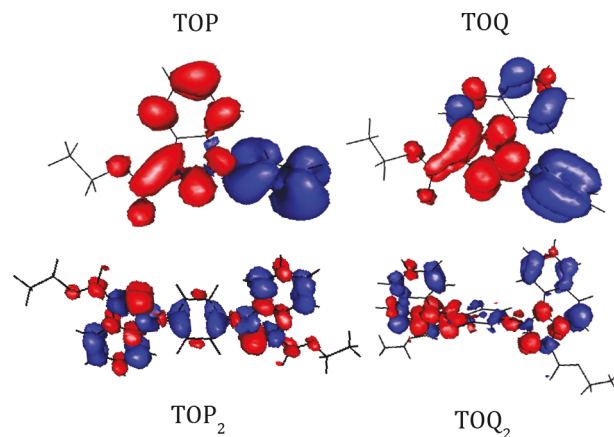
Based upon the observed and predicted UV/Vis intensities, the BLYP model provides the most accurate model for the valence electronic structures of TOP and TOQ dyes. The UV/Vis Abs intensities predicted by the GGA functionals are an order of magnitude more accurate than the intensities predicted by the hybrid and range-separated functionals (Table 3). Overall, the UV/Vis Abs intensities predicted by the BLYP functional are the most accurate with an average absolute error of  $6500 \text{ M}^{-1} \text{ cm}^{-1}$ . Consequently, the BLYP functional is considered to provide the most accurate models for the excitation transitions and excitation band assignments made in this article will exclusively rely upon the BLYP model.

**Table 3.**  $S_0 \rightarrow S_1$  Abs Intensities ( $\text{M}^{-1} \text{ cm}^{-1}$ ) of TOP Dyes

	TOP	TOP <sub>2</sub>	TOQ	TOQ <sub>2</sub>	error
(exp)	11,100 <sup>a</sup>	22,100 <sup>a</sup>	8100 <sup>b</sup>	16,400 <sup>b</sup>	
BLYP	7200	38,800	4100	17,800	6500
PBE	8900	46,100	6700	24,500	8900
B3LYP	20,600	70,600	17,100	25,000	18,900
PBE0	26,200	80,300	19,100	27,800	23,900
$\omega$ B97	17,400	84,100	23,000	56,300	30,800
$\omega$ B97X	17,200	74,100	23,500	41,500	24,700

<sup>a</sup>Ref 3. <sup>b</sup>Ref 7.

**Excitation Transitions.** The BLYP/def2-TZVP models for TOP and TOP<sub>2</sub> suggest charge transfer and  $\pi \rightarrow \pi^*$  assignments, respectively. The electron density difference map (EDDM) for TOP, predicted using the BLYP density functional, illustrates that the excitation transition for this molecule partially transfers an electron from the phenyl moiety to the triazolopyridinium heterocycle (Figure 4). Some

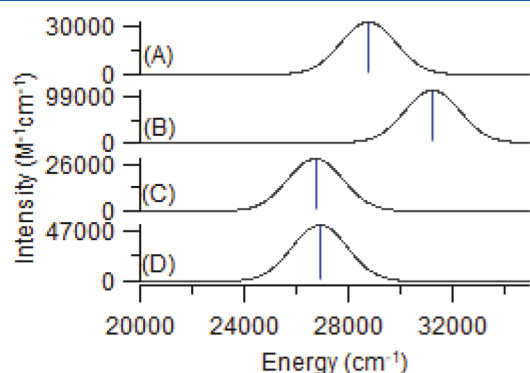


**Figure 4.** TDDFT-predicted UV/Vis Abs transitions for TOP in water (A), TOP<sub>2</sub> in water (B), TOQ in methanol (C), and TOQ<sub>2</sub> in acetonitrile (D). Blue indicates loss of electron density, and red indicates gain of electron density. The electronic structures were modeled using the BLYP density functional and the def2-TZVP basis set. The solvent was modeled using the CPCM implicit solvation model.

alternative band assignments are suggested by the other density functionals (Figures S11–S15), which emphasize the importance of using spectroscopically validated models for band assignments. Thus, the best assignment for the TOP excitation transition is phenyl  $\rightarrow$  heterocycle charge transfer. In contrast, the EDDM for TOP<sub>2</sub> suggests that the electron donation and acceptance for the excitation transition are delocalized throughout the entire molecule. The best description for this electronic transition is a  $\pi \rightarrow \pi^*$  transition. These spectral assignments are fully consistent with those made in an earlier work based upon a PBE model.<sup>3</sup> Also as noted previously, the addition of a second heterocyclic moiety to TOP fundamentally changes the nature of the excitation transition.

The TOQ and TOQ<sub>2</sub> excitations are also assigned to charge transfer and  $\pi \rightarrow \pi^*$  transitions, respectively. Compared to TOP, there is additional electron donation from the heterocycle moiety in the TOQ excitation transition (Figure 4). However, this transition is still best described as a phenyl  $\rightarrow$  heterocycle charge transfer since the phenyl moiety is primarily an electron donor. The excitation spectra of TOQ were previously modeled using semi-empirical calculations.<sup>7</sup> The band assignments made here based upon TDDFT are generally in agreement with this previous report. In addition, the TOP<sub>2</sub> and TOQ<sub>2</sub> transitions are quite similar. Both involve electron donation and electron acceptance throughout the entire molecule and are assigned to  $\pi \rightarrow \pi^*$  transitions. Thus, the excitation transitions of TOP and TOQ can best be described as phenyl  $\rightarrow$  heterocycle charge transfer transitions, whereas the excitation transitions of TOP<sub>2</sub> and TOQ<sub>2</sub> are better described as  $\pi \rightarrow \pi^*$  transitions.

**Stokes Shifts.** A critical component of TOP and TOQ photophysics that had not been modeled prior to this work is the Stokes shift. The Stokes shift is the energy difference between the absorption and emission transitions observed using UV/Vis Abs and fluorescence spectroscopy, respectively. A Stokes shift is observed when the energy difference between the ground and excited electronic states differs for the ground- and excited-state geometries. One component of this energy change is intramolecular; electron excitation changes the bonding throughout a molecule, which alters the minimum energy structure. A second component of the Stokes shift is intermolecular; solvent molecules will rearrange to stabilize the altered charge distribution in the electronic excited state, which is particularly significant for charge transfer transitions. In this work, the intramolecular component has been modeled with excited-state geometry optimizations using TDDFT. The intermolecular component has been modeled by predicting the electronic transition energies for both the ground- and excited-state geometries following the addition of a CPCM implicit solvation model (Figure 5 and Figures S16–S20).<sup>34</sup>



**Figure 5.** TDDFT-predicted fluorescence emission spectra for TOP in water (A), TOP<sub>2</sub> in water (B), TOQ in methanol (C), and TOQ<sub>2</sub> in acetonitrile (D). The electronic structures were modeled using the  $\omega$ B97 density functional and the def2-TZVP basis set. The solvent was modeled using the CPCM implicit solvation model.

These considerations mean that the accuracy of the computed Stokes shift offers an assessment for the accuracies of the excited-state geometry optimization, the excitation transition, and the emission transition.

Overall, the range-separated hybrid functionals offer the best models for the Stokes shift of TOP and TOQ dyes. Although the GGA functionals do yield the most accurate model for the excitation transition of these molecules, the Stokes shifts predicted by these molecules have poor agreement with experiment (Table 4). Furthermore, the GGA functionals

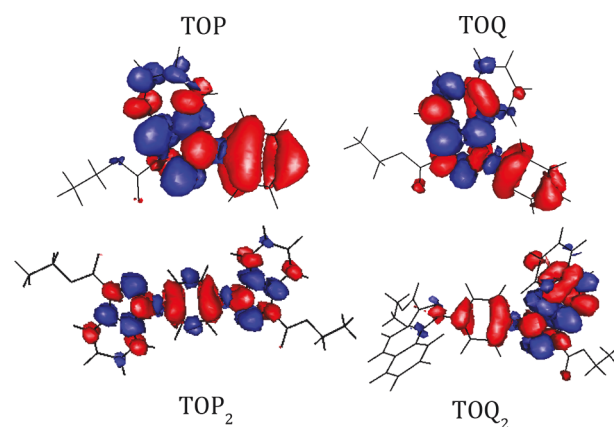
**Table 4.** Stokes Shifts (cm<sup>-1</sup>) for TOP Dyes

	TOP	TOP <sub>2</sub>	TOQ	TOQ <sub>2</sub>	error
(exp)	11,200 <sup>a</sup>	7800 <sup>a</sup>	9200 <sup>b</sup>	7000 <sup>b</sup>	
BLYP	10,200 <sup>c</sup>	22,500 <sup>c</sup>	13,100 <sup>c</sup>	19,900 <sup>c</sup>	8100
PBE	9400 <sup>c</sup>	19,900 <sup>c</sup>	13,600 <sup>c</sup>	19,700 <sup>c</sup>	7800
B3LYP	17,900	6600 <sup>c</sup>	15,300	12,700	4900
PBE0	18,100	6100	14,800	11,700	4700
$\omega$ B97	13,300	6900	9500	7100	900
$\omega$ B97X	14,900	7900	9900	9000	1600

<sup>a</sup>Ref 3. <sup>b</sup>Ref 7. <sup>c</sup>Quenched.

predict one or more dark states at energies lower than the emissive states noted in Table 4, suggesting that these dyes are quenched,<sup>38</sup> which is inconsistent with experimental data. The hybrid functionals do offer a moderate improvement over the GGA functionals with regard to the Stokes shift. B3LYP- and PBE0-predicted Stokes shifts have average absolute errors of 4900 and 4700 cm<sup>-1</sup>, respectively, and there is only one instance where a dye is predicted to be quenched. However, the range-separated functionals clearly offer the most accurate models for the Stokes shift of TOP and TOQ dyes. The Stokes shifts predicted by the  $\omega$ B97 and  $\omega$ B97X functionals have average absolute errors of merely 900 and 1600 cm<sup>-1</sup>, respectively, and all TOP and TOQ dyes are predicted to be emissive. It should be noted that the emission energies predicted by the  $\omega$ B97 and  $\omega$ B97X functionals are not particularly accurate due to the sizable errors in the excitation energy predictions (Table 2). However, the systematic overestimation of S<sub>1</sub> excited-state energies by these functionals cancels out when the differences between the excitation and emission energies are taken to calculate the Stokes shifts. Overall, the  $\omega$ B97 functional offers the most balanced treatment for all the components of the Stokes shift.

**Emission Transitions.** In general, the  $\omega$ B97/def2-TZVP models predict that the emission transitions for TOP and TOQ are the inverse of the excitation transitions. The EDDM for the TOP emission transition, predicted using the  $\omega$ B97 density functional, illustrates that the fluorescence of this molecule arises from heterocycle → phenyl charge transfer (Figure 6). The charge transfer transition relieves the



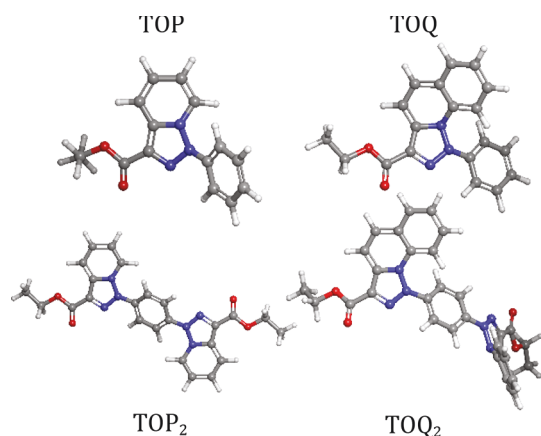
**Figure 6.** TDDFT-predicted fluorescence emission transitions for TOP in water (A), TOP<sub>2</sub> in water (B), TOQ in methanol (C), and TOQ<sub>2</sub> in acetonitrile (D). Blue indicates loss of electron density, and red indicates gain of electron density. The electronic structures were modeled using the  $\omega$ B97 density functional and the def2-TZVP basis set. The solvent was modeled using the CPCM implicit solvation model.

zwitterionic character of the excited state, resulting in a structurally perturbed version of the S<sub>0</sub> ground state. As is the case for the excitation transitions, there are differences between the emission transitions predicted by various density functionals (Figures S21–S25). However, the  $\omega$ B97 data are presented here based upon the agreement between the experimental and computed Stokes shifts (Table 4). The EDDM for TOQ also suggests a heterocycle → phenyl charge transfer to relieve the zwitterionic character of the excited state. In both cases, the emission transitions are roughly the inverse

of the excitation transitions (Figure 4). The small differences between the excitation and emission transitions can be attributed to vibronic relaxation in the  $S_1$  excited state following excitation and prior to emission. Thus, for TOP and TOQ, structural relaxation in the electronic excited state does not fundamentally alter the electronic transition.

The photophysics of TOP<sub>2</sub> and TOQ<sub>2</sub> are more complicated than those of TOP and TOQ. The TOP<sub>2</sub> emission transition can be assigned to a  $\pi^* \rightarrow \pi$  transition based upon the EDDM (Figure 6). Similar to the cases for TOP and TOQ, this is roughly the inverse of the excitation transition for this compound (Figure 4). On the other hand, the TOQ<sub>2</sub> emission transition is best described as a charge transfer from one of the heterocycle moieties to the phenyl linker. This transition is fundamentally different from the  $\pi \rightarrow \pi^*$  excitation transition for this molecule and implies significant electronic reorganization during structural relaxation of the  $S_1$  excited state for TOQ<sub>2</sub>. The fundamental differences between the TOP<sub>2</sub> and TOQ<sub>2</sub> emission transitions predicted by TDDFT are supported by previously published quantum yield data.<sup>7</sup> The quantum yield of TOP<sub>2</sub> (0.22) is double that of TOQ<sub>2</sub> (0.11), which correlates with the larger TDDFT-predicted oscillator strength for the TOP<sub>2</sub> emission (1.29) compared to the TOQ<sub>2</sub> emission (0.60). The quantum yield of TOP<sub>2</sub> is significantly larger than the other three molecules in this study because it maintains a  $\pi \rightarrow \pi^*$  excited state that has excellent overlap with the ground state following excited-state relaxation.

**$S_1$  Excited-State Geometries.** With spectroscopically validated models for the  $S_0$  and  $S_1$  structures available, it was possible to make comparisons to reveal the excited-state distortions. TOP and TOQ exhibit dramatic ring rotations in the  $S_1$  excited states predicted by the  $\omega$ B97 density functional (Figure 7). The dihedral angles between the heterocycle and



**Figure 7.**  $S_1$  excited-state geometries of TOP (top left), TOP<sub>2</sub> (bottom left), TOQ (top right), and TOQ<sub>2</sub> (bottom right). The excited-state structures were optimized using the  $\omega$ B97 density functional and the def2-TZVP basis set. Excitation to the  $S_1$  excited state induces significant rotation about the heterocycle–phenyl bond.

phenyl moieties decrease to 6.4° and 3.0°, respectively, which are nearly coplanar (Table 5). Ring rotations are also observed in TOP<sub>2</sub> and TOQ<sub>2</sub>, albeit to a lesser extent. The average heterocycle–phenyl dihedrals in TOP<sub>2</sub> and TOQ<sub>2</sub> are 25.9° and 18.1°, respectively. It is important to note that these excited-state geometries are simply the lowest energy conformations of the molecules, and the TOP and TOQ dyes are likely to rotate about the heterocycle–phenyl linker in

**Table 5.**  $\omega$ B97  $S_1$  Geometries of TOP Dyes

	1 (Å) <sup>a</sup>	2 (Å) <sup>a</sup>	3 (Å) <sup>a</sup>	$\alpha$ (°) <sup>a</sup>
TOP(DFT)	1.365	1.399	1.371	6.4
TOP <sub>2</sub> (DFT) <sup>b</sup>	1.375	1.372	1.327	25.9
TOQ(DFT)	1.374	1.393	1.343	3.0
TOQ <sub>2</sub> (DFT) <sup>b</sup>	1.402	1.372	1.326	18.1

<sup>a</sup>See Figure 2. <sup>b</sup>Data reported for TOP<sub>2</sub> and TOQ<sub>2</sub> are the average for both heterocycle moieties.

solution. Fortunately, ring rotation does not appear to significantly alter the nature of the electronic transitions (Figures 4 and 6), which suggests that the primary impact of the ring rotation is expected to be a diminished Stokes shift at elevated temperatures and decreased viscosities.

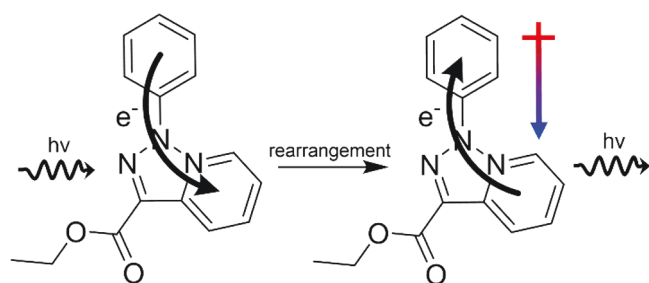
In all cases, the length of the heterocycle–phenyl bond decreases in the  $S_1$  excited state. This can be understood in terms of the zwitterionic character of the  $S_1$  excited state; the opposite charges on the heterocycle and phenyl moieties strengthen the linker bond. Other spectroscopically invalidated functionals yield alternative  $S_1$  excited-state geometries (Figures S26–S30 and Tables S6–S10). Overall, the  $\omega$ B97 functional predicts that these four triazole dyes undergo significant excited-state structural relaxation, which is consistent with their “mega” Stokes shifts.

Just as the relative orientation of the conjugated rings could be rationalized using Hückel’s rule, the relative orientations of these rings in the excited state are consistent with Baird’s rule. Baird’s rule is perhaps less appreciated than Hückel’s rule, and it states that conjugated  $\pi$  systems with  $4n$  electrons are aromatic in their first excited state, whereas conjugated  $\pi$  systems with  $4n + 2$  electrons are anti-aromatic.<sup>23</sup> This is the opposite of Hückel’s rule. The triazolopyridinium heterocycle, the triazoloquinolinium heterocycle, and the phenyl ring all have  $4n + 2$   $\pi$  electrons. This suggests that each of these moieties is aromatic in the  $S_0$  ground state and anti-aromatic in the  $S_1$  excited state. However, by rotating the phenyl ring into a coplanar arrangement with either the triazolopyridinium or triazoloquinolinium heterocycle,  $4n$   $\pi$  electron systems can be formed. These structural arrangements are likely aromatic, and hence favorable, in the  $S_1$  excited state. Thus, the relative orientations of the heterocycle and phenyl moieties in TOP and TOQ dyes can be rationalized using Baird and Hückel’s rules.

## DISCUSSION

**TOP and TOQ Photophysics.** The computational data presented in this article provide detailed insight into the excitation transitions for TOP and TOQ dyes, which are generally consistent with previous reports. To make excitation transition band assignments for TOP and TOQ dyes, the TDDFT-predicted UV/Vis Abs spectra were generated using six different density functionals. The accuracies of the computational models were assessed by comparing experimental and computed Abs intensities, not transition energies, because UV/Vis Abs intensities depend upon the overlap of the donor and acceptor states. The TOP and TOP<sub>2</sub> excitation transitions had previously been assigned to charge transfer and  $\pi \rightarrow \pi^*$  transitions, respectively,<sup>3</sup> based upon PBE density functional models,<sup>27</sup> and the BLYP models presented here are consistent with those assignments (Figure 8).<sup>25,26</sup> Similarly, the TOQ excitation transition had been previously assigned to a charge transfer transition based upon semi-empirical





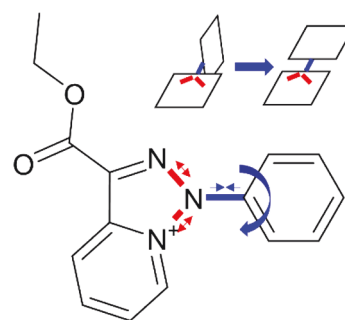
**Figure 8.** Proposed fluorescence mechanism for TOP. Light absorption by TOP induces intramolecular electron transfer from the phenyl ring to the heterocyclic ring, resulting in an excited state with zwitterionic character. Following excited-state structural relaxation, electron transfer back to the phenyl ring quenches the zwitterionic character and triggers the release of a photon.

calculations,<sup>7</sup> and that assignment is also supported by the BLYP model presented here. To our knowledge, the TOQ<sub>2</sub> excitation spectrum had not been modeled prior to this work. The spectroscopically validated BLYP model suggests a  $\pi \rightarrow \pi^*$  assignment similar to TOP<sub>2</sub>. Thus, this work corroborates prior assignments for the excitation transitions of TOP, TOP<sub>2</sub>, and TOQ and provides the first validated band assignment for TOQ<sub>2</sub>.

The computational data presented in this article yield the first validated band assignments for the fluorescence transitions of TOP and TOQ dyes. The  $S_1$  excited-state structure and fluorescence spectrum for all four TOP and TOQ dyes were modeled using six different density functionals; a comparison of the predicted Stokes shifts to the experimental Stokes shifts revealed that the  $\omega$ B97 range-separated functional provides the most accurate descriptions of the  $S_1$  excited states (Table 4). The conclusion that two different density functionals, BLYP and  $\omega$ B97, yield the most accurate descriptions of two different electronic states,  $S_0$  and  $S_1$ , is not necessarily surprising. The magnitude of charge separation in the  $S_1$  excited state is significantly greater than in the  $S_0$  ground state, and the range-separated functionals were designed to provide improved treatment of long-range electron exchange, resulting in better descriptions for charge transfer excited states.<sup>30</sup> Based upon the spectroscopically validated  $S_1$  excited-state models (Figure 8), the fluorescence transition for three of the four dyes studied here (TOP, TOQ, and TOP<sub>2</sub>) is essentially the inverse of the excitation transition with minor perturbations due to excited-state structural relaxation. However, the excitation and emission transitions for TOQ<sub>2</sub> are fundamentally different from one another. Following excitation,  $S_1$  excited-state relaxation of TOQ<sub>2</sub> results in charge separation to form a zwitterionic excited state. Consequently, only TOP<sub>2</sub> maintains a delocalized excited state following excited-state relaxation.

**Origin of the Stokes Shift.** The computational data presented here provide the first detailed insight into the origin of the “giga” Stokes shift in TOP. At room temperature, the  $S_1$  excited states of TOP and TOQ dyes are fluorescent with lifetimes of  $\sim 1$  ns,<sup>7</sup> which precludes structural characterization. Thus, TDDFT excited-state optimizations were employed to generate excited-state structural models whose accuracies were evaluated on the basis of the predicted Stokes shifts (Table 4). The most readily apparent structural change in the  $S_1$  excited state is a rotation along the heterocycle–phenyl bond from a ground-state conformation that is best described as twisted to an excited-state conformation that is best described as coplanar

(Figure 9), the reverse of TICT!<sup>19</sup> It is noteworthy that TOP and TOQ have both the largest ring rotations ( $60.3^\circ$  and



**Figure 9.** Prominent structural changes observed following photoexcitation of TOP. In accordance with Baird’s rule, the phenyl and heterocycle rings adopt a coplanar orientation with a compressed C–N bond following excited-state relaxation (blue). In addition, the N–N bonds of the triazole moiety expand in the excited state due to the charge transfer nature of the excitation transition (red).

$48.0^\circ$ , respectively, Tables 1 and 5) and the largest Stokes shifts ( $11,200$  and  $9200$   $\text{cm}^{-1}$ , respectively). As noted above, these structural changes can be rationalized within the frameworks of Hückel and Baird’s rules.<sup>20–23</sup> A twisted conformation may be favored in the  $S_0$  ground state to yield two separate aromatic systems, and a coplanar conformation may be favored in the  $S_1$  excited state to produce a single, delocalized aromatic system. It is interesting to note that a similar excited-state relaxation was recently proposed for other donor–acceptor fluorophores,<sup>39–41</sup> albeit for chromophores that do not exhibit a “giga” Stokes shift. These observations suggest that construction of a chromophore with two aromatic moieties separated by a single, rotatable bond may be a viable strategy for the development of novel fluorophores with “giga” Stokes shifts.

What are less apparent from inspection of the excited-state structures, but likely more significant with regard to the Stokes shift, are the structural changes within the triazole moiety upon photoexcitation. For all four TOP and TOQ dyes modeled here, the C–N bond between the heterocycle and phenyl groups shortens by nearly  $0.1$  Å (Figure 9). This bond shortening makes sense within the context of Baird’s rule;<sup>23</sup> conjugation between the heterocycle and phenyl groups in the excited state will increase the double bond character of this bond. For TOP and TOQ, photoexcitation also lengthens the N–N bonds within the triazole by nearly  $0.05$  Å. This can be ascribed to the charge transfer transition populating a  $\pi^*$  orbital of this moiety. Although these bond length changes may seem small compared to the ring rotation upon photoexcitation, they are likely the major contributor to the Stokes shift. This is because bond stretches for aromatic systems are on the order of  $2000$ – $3000$   $\text{cm}^{-1}$  and, as a result, small structural changes have large energetic consequences. The N–N bond length changes are derived from the charge transfer nature of the photoexcitation, which suggests that the design of a “giga” Stokes shift chromophore from rotatable aromatic moieties could be further optimized by maximizing the charge transfer nature of the photoexcitation.

**Photophysical Origins for “Giga” Stokes Shifts.** This article has identified a second photophysical mechanism that yields “giga” Stokes shift fluorophores. As noted earlier, the majority of “giga” Stokes shift fluorophores reported to date

arise from TICT.<sup>4–6</sup> There are two aspects of TICT that are primarily responsible for the “giga” Stokes shift of these fluorophores: excited-state structural relaxation from a planar conformation to a twisted conformation and solvent reorganization to accommodate a zwitterionic excited state.<sup>19</sup> To our knowledge, the TOP dyes are currently the sole examples of “giga” Stokes shift fluorophores that do not follow a TICT mechanism.<sup>3,7</sup> As such, these compounds represent a new lead for the development of novel “giga” Stokes shift fluorophores. It should be noted that the excited-state aromaticity reversal observed for TOP dyes has also been invoked in the past for excited-state proton transfer reactions.<sup>42–44</sup> In addition, aromaticity reversal in an electronic excited state has also been invoked to explain aggregation-induced emission and the fluorescence of macromolecular structures.<sup>45,46</sup> Clearly, the influence of Baird’s rule on the photophysics of conjugated fluorophores is a topic that merits further study.

## CONCLUSIONS

In summary, spectroscopically validated computational models for TOP and TOQ photophysics have been developed. These models reveal that the excitation transitions of TOP and TOQ are best described as charge transfer, whereas the excitation transitions of TOP<sub>2</sub> and TOQ<sub>2</sub> are better described as  $\pi \rightarrow \pi^*$ . The emission transitions of TOP, TOP<sub>2</sub>, and TOQ are essentially the inverse of their excitation transitions, with minor perturbations due to structural relaxation in the excited state. However, charge localization in the excited state of TOQ<sub>2</sub> results in an emission transition that is best described as charge transfer. This approach has yielded the first detailed models for the excited-state structures of TOP and TOQ. Inspection of these structures reveals that the “giga” Stokes shift of TOP arises from ring rotation and triazole bond weakening in the excited state. These observations suggest that novel “giga” Stokes shift fluorophores could be designed by focusing on two features: a pair of conjugated moieties that have different relative orientations according to Hückel and Baird’s rules and maximizing charge transfer between these two moieties upon photoexcitation.

## ASSOCIATED CONTENT

### Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.jpcb.2c04397>.

S<sub>0</sub> and S<sub>1</sub> geometries, TDDFT-predicted UV/Vis Abs and fluorescence spectra, and Cartesian coordinates for all computational models (PDF)

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