1 **A site for deep ice coring at West Hercules Dome: results from**

2 **ground-based geophysics and modeling**

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15 **ABSTRACT**

16 Hercules Dome, Antarctica, has long been identified as a prospective deep ice core site due to

17 the undisturbed internal layering, climatic setting, and potential to obtain proxy records from the

18 last interglacial period when the West Antarctic Ice Sheet may have collapsed. We performed a

19 geophysical survey using multiple ice-penetrating radar systems to identify potential locations

20 for a deep ice core at Hercules Dome. The surface topography, as revealed with recent satellite

21 observations, is more complex than previously recognized. The most prominent dome, which

22 we term "West Dome", is the most promising region for a deep ice core for the following

23 reasons: (1) bed-conformal radar reflections indicate minimal layer disturbance and extend to

24 within tens of meters of the ice bottom; (2) the bed is likely frozen, as evidenced by both the

25 shape of the measured vertical ice velocity profiles beneath the divide and modeled ice

26 temperature using three remotely-sensed estimates of geothermal flux; and (3) models of layer

27 thinning have 132 ka old ice at 45 to 90 m above the bed with an annual layer thickness of ~1

28 mm, satisfying the resolution and preservation needed for detailed analysis of the last

29 interglacial period.

30

31 **1. INTRODUCTION**

32   The West Antarctic Ice Sheet (WAIS) is vulnerable to rapid retreat because it is

33 grounded below sea level (e.g. Mercer, 1968; Bamber and others, 2009), and has collapsed at

34   least once in the Pleistocene (Scherer and others, 1998). During the last interglacial (LIG, 116-

35   132 ka), global eustatic sea level was higher than today, though the timing and magnitude of the

36   sea level highstand remain uncertain. Estimates of the upper limit of sea level during the LIG

37   range from 4 m (Dyer and others, 2021) to 9 m higher than today (Dutton and others, 2015). A

38   collapse of the WAIS would help explain the LIG sea level, but there is no unequivocal evidence

39   this occurred.

40   Ice core records provide one possible means to obtain information about past changes

41   in the WAIS. Existing ice core records from West Antarctica either do not contain ice dating to

42   the LIG (e.g. WAIS Divide, Buizert and others, 2015) or, if they do, the ice is very near the bed

43   and is difficult to interpret (e.g. Siple Dome, Brook and others, 2005; Roosevelt Island, Lee and

44   others, 2020; Skytrain Ice Rise, Mulvaney and others, 2020). An ice core site from a location

45   that would be sensitive to the climatic changes induced by WAIS collapse, but where the ice

46   flow would not be directly affected, has the potential to elucidate the size and rate of change of

47   the WAIS during the LIG.

48   Hercules Dome (86°S, 105°W) is located in East Antarctica approximately 400 km from

49   the South Pole towards the Horlick and Thiel ranges in the Transantarctic Mountains. The

50   primary moisture source region for snowfall at Hercules Dome is the Pacific sector, such that

51   the moisture pathway passes over the WAIS; in contrast, the moisture pathways for existing

52   East Antarctic ice cores that preserve LIG records do not pass over the WAIS (Sodeman and

53   Stall, 2009; Nicolas and Bromwich, 2011). Hercules Dome is not likely to have changed

54   elevation significantly in elevation from the LIG to present even in scenarios of WAIS collapse

55   (Sutter et al., 2016), with changes of less than 75 meters in models (e.g. Pollard and DeConto,

56   2016; Garbe et al., 2020). On the other hand, the composition of snowfall at Hercules Dome

57   should be sensitive to changes in the elevation of the WAIS (Steig and others, 2015).

58   Simulations with multiple atmospheric models show that a lowered WAIS topography would

59   cause a cyclonic anomaly which changes regional atmospheric circulation, bringing a greater

60   flow of warm, moist air across the WAIS toward the South Pole (Steig and others, 2015;

61   Holloway and others, 2016). Based on these simulations, an ice core from Hercules Dome

62   would provide a climate record that is influenced by the size and extent of the WAIS.
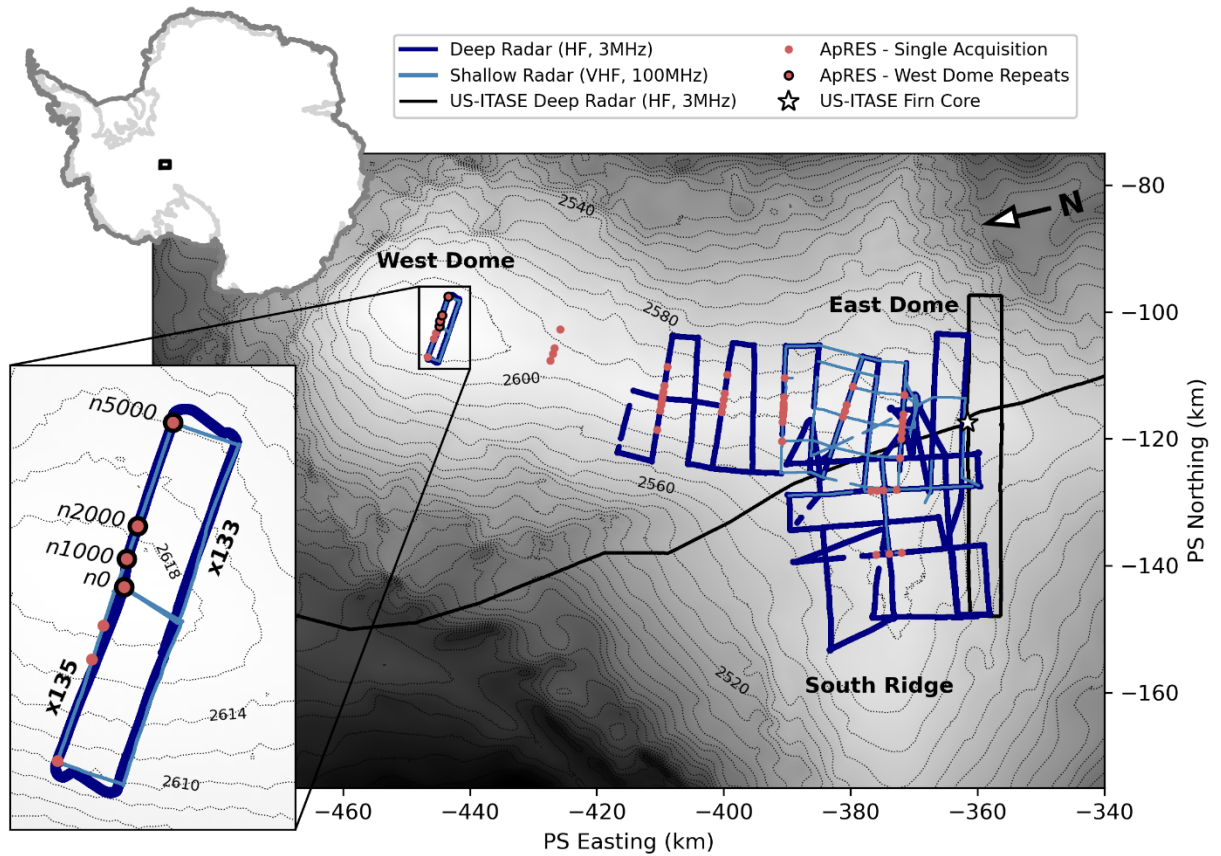
Fig. 1: *Overview map of the Hercules Dome geophysical survey in polar stereographic (PS) coordinates. The directions in the PS projection are used in the remainder of the paper. Arrow indicates direction of geographic North. Inset shows the two radar lines, x135 and x133, at West Dome. Surface elevation contours from the Reference Elevation Model of Antarctica (REMA, Howat et al., 2019) are shown at 10-m spacing for the overview and 2-m spacing for the inset.*

Climate records from a deep ice core at Hercules Dome could be used in conjuction with other paleoclimate records to constrain the size and rate of change of the WAIS during the LIG. Indicators of past ice-sheet extent, such as subglacial bedrock exposure (e.g. Hein et al, 2015; Spector and others, 2018), lack information on the rate of change which is likely preserved in ice core records. A record from Hercules Dome would complement other ice core records both directly affected by WAIS topography changes, such as Skytrain Ice Rise (Mulvaney et al., 2020), and indirectly affected, such at Mt. Moulton (Korotkihk and others, 2012). Indeed, Steig and others (2015) showed if the WAIS collapsed, surface temperatures at Mt. Moulton would have warmed less, and Hercules Dome would have warmed more, than sites farther inland on

79   the East Antarctic plateau. Therefore, existing ice core records from the East Antarctic plateau

80   provide independent information against which the Hercules Dome record could be compared.

81   Hercules Dome was first identified as a promising location for a deep ice core during the

82   2001-2002 US-ITASE traverse from West Antarctica to South Pole (Jacobel and others, 2005).

83   Ice-penetrating radar was collected along the main traverse route as well as two perpendicular

84   50-km-long tracks. The radar revealed clear internal layering with ice thicknesses that ranged

85   from approximately 1500 m to 2800 m. A 72-m firn core was also recovered. Analyses of the firn

86   core show that annual layering and volcanic signals are well preserved and the 400-year

87   average accumulation rate was 0.12 m a^{-1} ice equivalent (Dixon and others, 2013).

88   We conducted a geophysical survey across the Hercules Dome region during the

89   2018/2019 and 2019/2020 austral summers. Recent satellite observations (Cryosat-2, ICESat2,

90   and Maxar Imagery) revealed a complex surface topography (Fig. 1). There are three local

91   surface divides, which we refer to here by their relative positions in polar-stereographic space

92   with respect to grid north (Fig. 1). "West Dome" (85.8°S, 102.9°W) lies furthest to the true north,

93   and is connected to "East Dome" by a ~70 km ridge. A secondary ridge extends approximately

94   grid south from East Dome that we term "South Ridge". East Dome, where the US-ITASE

95   traverse visited, has large variations in bedrock topography and lacks a clear dome summit;

96   East Dome is the current source region for South Ridge. We therefore focus on West Dome

97   where our geophysical data suggest a simple flow regime and small bedrock topography

98   variations (Fig. 2), and assess the suitability of West Dome as a site for recovering a deep ice

99   core that preserves LIG ice. We focus on a 10-km long radar line (named x135 within our grid)

100   which nearly transects the dome summit, and describe the results of ice-flow modeling

101   constrained by near-surface, deep-profiling, and phase-sensitive radar.

102

103   **2. GEOPHYSICAL DATA AND MODEL SETUP**

104   The three radar systems used at Hercules Dome in the 2018/2019 and 2019/2020 field seasons

105   as well as the kinematic model setup used to help interpret the observations are described in

106   this section; Section 3 will present the results. The extent of each survey is indicated by Fig. 1.

107   We use stereographic grid directions, following the orientation of Fig. 1, in the remainder of the

108   paper. This paper focuses on the radar data collected near the West Dome summit. Two 10-km

109   long lines across the divide were collected (Fig. 1 inset); x135 is closest to the dome summit

110   and x133 is 2 km to the east.

111

112   **2.1 Deep (HF) Radio-Echo Sounding Surveys**

113   Radio-echo sounding (RES) has been used to map ice thickness and bed elevation, and

114   ice-sheet internal stratigraphy along two 10-km lines at West Dome (x135 shown in Fig. 2). We

115   used a custom high-frequency (HF, 3 MHz) monopulse radar system (Welch and others, 2003,

116   2009; Christianson and others, 2012; 2016). The RES data were processed using standard

117   techniques, including horizontal stacking, bandpass filtering, correction for antenna separation,

118   geolocation from contemporaneous kinematic Global Navigation Satellite System (GNSS) data,

119   interpolation to standard trace spacing, and time-wavenumber migration using the open-source

120   radar-processing and interpretation toolbox ImpDAR (Lilien and others, 2020). Englacial

121   reflections were picked through the semi-automated digitization routine in ImpDAR. The two-

122   way travel times (TWTT) were then converted to depth using a spatially uniform firn-density

123   profile (ITASE 02-4, Dixon and others, 2013) and a Looyenga and others (1965) mixing model

124   (Fig. 2D). There is a ~100m data gap at 4.9 km on x135. The noise on the picked layers in Fig.

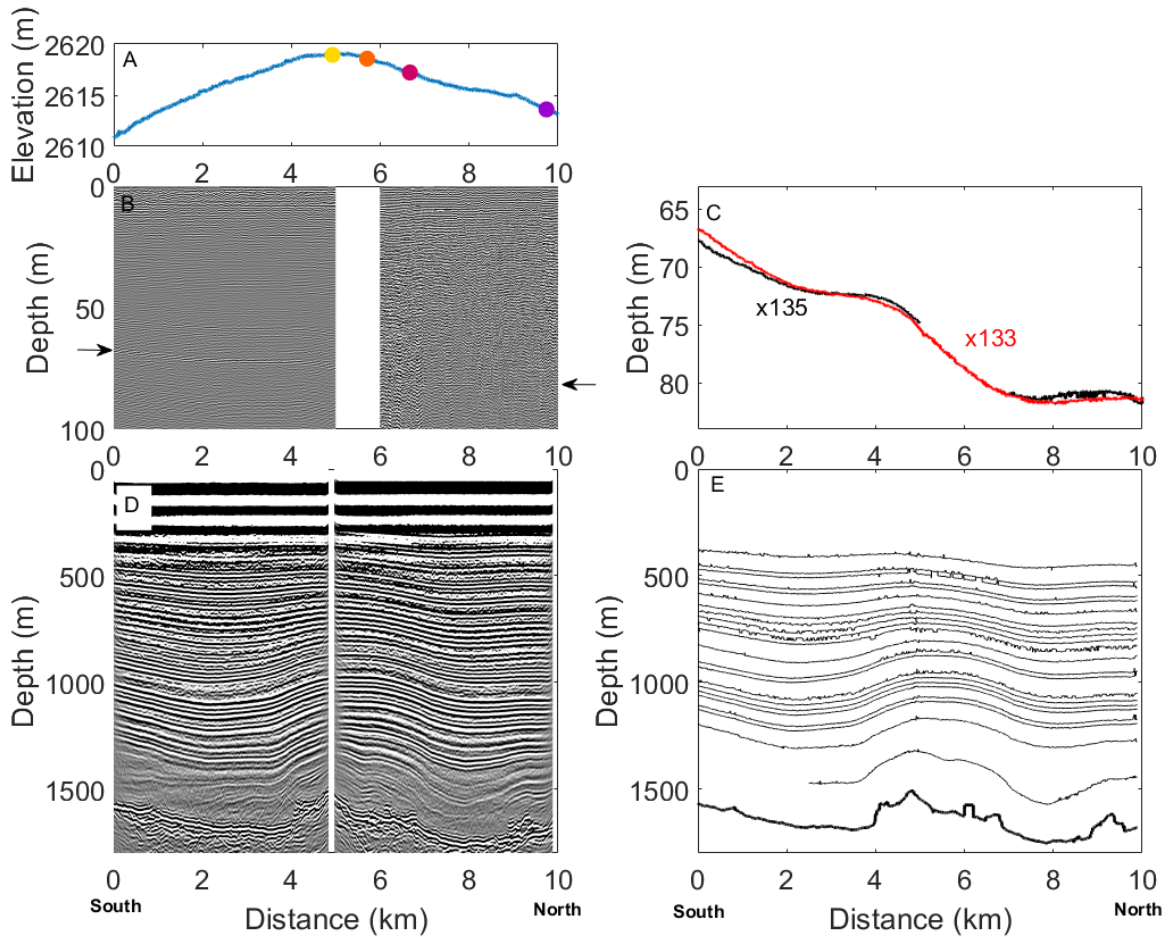125   2E is due to sample resolution and the picking algorithm in ImpDAR.

126

127

128 ***Fig. 2****: A) GNSS derived surface elevation along x135 with ApRES sites shown by colored dots:*

129 *n0 (yellow), n1000 (orange), n2000 (pink), n5000 (purple). B) VHF radar of line x135 with*

130 *arrows pointing to bright layer identifiable throughout survey. Data quality is lower to the north.*

131 *C) The depth of the bright layer on x135 agrees well with x133, which does not have the data*

132 *gap or quality issues. VHF data along x133 is used for the accumulation forcing in the kinematic*

133 *model. D) HF radar of x135 showing internal layer and bed reflections. E) Traced internal layers*

134 *of x135 radargram shown in D). <Note that panel B is difficult to render properly at low*

135 *resolution which we will work on in a final figure>*

136

137 **2.2 Shallow (VHF) Radio-Echo Sounding Surveys**

138   To image the upper 20-200 m of the ice sheet, we used a Pulse-EKKO Pro radar system

139 with very high frequency (VHF, 100 MHz) antennas. Our VHF data-processing flow is similar to

140 that described for the HF radar and includes bandpass filtering, correction for antenna

141 separation, geolocation from contemporaneous kinematic GNSS data, interpolation to standard

142 trace spacing, and exponential range gain to increase the relative amplitude of deeper

143 reflections. Englacial reflectors were traced using the semi-automated reflection digitization

144 routine in ImpDAR. A distinct high-amplitude reflector at ~75 m depth (Fig. 2b), observed in all

145 the shallow RES profiles, is used to infer the spatial pattern of accumulation at West Dome.

146   We convert the TWTT to depth with a depth-density profile based on the firn core density

147 measurements; we fit a Herron and Langway (1980) model to the firn core measurements to

148 produce a smooth depth-density profile. The bright layer is at 73.5 m depth at the closest

149 intersection (within 1 km) of our VHF profiles and the US-ITASE 02-4 core (Dixon and others,

150 2013; Fig. 1). The core extends to 72-m depth and was collected 17 years prior to our VHF

151 survey. The age at 73.5 m depth is 1600 CE, or 420 years before the VHF radar data was

152 collected, where we have assumed a steady-state firn column and determined the additional

153 age in the bottom 1.5 m from the same model fit used for the TWTT conversion.

154   For the x133 and x135 radar lines, the conversion of TWTT for the bright layer to depth

155 (Fig. 2C) and the inference of accumulation rate from the layer depth both depend on the

156 density profile. Because there is no firn core at West Dome, we use a Herron and Langway

157 (1980) firn model to estimate the depth-density profile. We use fixed inputs of 370 kg m^{-3} for the

158 surface density and -40°C for the surface temperature; we start with an initial value of 0.13 m a^{-1}

159 for the accumulation rate (all accumulation rates are given in ice equivalent and can be

160 converted to kg m^{-2} yr^{-2} using a density of 917 kg m^{-3}), which is greater than the value inferred

161 from the ITASE core because the average bright layer depth at West Dome is deeper than at

162   the ITASE core site. We then infer the accumulation rate from the layer depth and the modeled

163   density profile. To find a self-consistent solution, we iterate by calculating a new density profile

164   along the radar line with the inferred accumulation rate at each trace, convert TWTT to depth,

165   and infer the updated accumulation rate with the new density profile. The solution becomes self-

166   consistent within three iterations.

167

168   **2.3 Automated phase-sensitive radio echo sounding (ApRES)**

169   Acquisitions of autonomous phase-sensitive radio-echo sounding (ApRES; Nicholls and

170   others, 2015) were performed at four locations along the x135 line in the 2018-2019 season,

171   and repeated in 2019-2020. ApRES measurements are used to determine the relative phase

172   offset of englacial reflectors between the two acquisitions. ApRES processing is implemented in

173   ImpDAR (Lilien and others, 2020) and follows the processing flow described by Brennan and

174   others (2014). The wave speed is not corrected for the density variations of the firn and we do

175   not interpret the data in the upper 150 m. The phase offset is converted to a relative range offset

176   which determines a depth-velocity averaged over the period between the two measurements.

177   Since phase is relative, the phase offset profile is unwrapped against a point of known velocity

178   such as the bed or surface which then can shift the velocity profile by a constant.

179

180   **2.4 Kinematic model setup**

181   We employ a kinematic model to help interpret the internal structure of West Dome. In

182   this section we describe the model setup and the application of the model follows in Section 4.

183   The kinematic model uses inputs of the accumulation rate, bed topography, and prescribed

184   shape functions for the horizontal and vertical velocities (Nereson and others, 2002;

185   Waddington and others, 2007; Koutnik and others, 2012). These model inputs are based on the

186   geophysical observations described in Section 3. The ability to fit the measured layers provides

187   information about the stability of the current flow regime near the divide and about the

188   appropriate forcing for depth-age modeling.

189   We choose a kinematic model for two primary reasons. First, the existing radar coverage

190   is limited. The primary radar line is 10 km in length, which results in a distance of only ~3 ice

191   thicknesses between the divide and downstream boundary. Using dynamic models requires

192   extending the lower boundary to approximately 10 ice thicknesses from the divide, so that the

193   area of interest is not affected by the edge boundary (Martín and others, 2006). Second,

194   dynamic models have difficulty reproducing divide flow, particularly in areas with variations in

195   bed topography (Goel and others, 2018). Therefore, we use a kinematic model where we can

196   specify the shape of the englacial velocity profiles and the position of the divide.

197   The horizontal velocities, u, are calculated as:

198 $$u(x, \hat{z}, t) = \bar{u}(x, t)\emptyset(x, \hat{z}, t) \quad (1)$$

199   where $\bar{u}$ is the depth-average velocity, x is the distance along the flow line, $\hat{z}$ is the relative

200   height above the bed, t is time, and Φ is the horizontal velocity shape function. We use the

201   Lliboutry (1979) approximation:

202

203 $$\phi(\hat{z}) = \frac{p+2}{p+1}(1 - (1 - \hat{z})^{p+1}) \quad (2)$$

204   where p is the shape factor. The corresponding vertical velocity shape function is:

205 $$\psi(\hat{z}) = \left(1 - \frac{p+2}{p+1}(1 - \hat{z}) + \frac{1}{p+1}(1 - \hat{z})^{p+2}\right). \quad (3)$$

206

207   The depth-averaged horizontal velocity is calculated from the ice flux from upstream, based on

208   the accumulation rate and ice thickness. We assume no divergence in the ice flow (i.e., the

209   flowband width is constant) based on comparisons with the measured surface velocities along

210   x135 (Fig. S1). The vertical velocity is calculated as

211 $$w = (\dot{b} - \dot{S})\psi - \bar{u}\phi\left(\frac{\partial B}{\partial x} + \hat{z}\frac{\partial H}{\partial x}\right) - \bar{u}H \int_0^{\hat{z}} \frac{\partial \phi}{\partial x} \partial \hat{\zeta} \quad (4)$$

212   where

213   w, ψ, ϕ vary in $x, \hat{z}$, and t

214                         $\dot{b}, \dot{S}, \bar{u}$ vary in x and t;

215   B and H vary in x

216   and $\dot{b}$ is the accumulation rate, $\dot{S}$ is the change in surface elevation, B is the bed elevation, and

217   H is the ice thickness.

218   An example of the modeled velocity field is shown in Fig. 3. The details of our model

219   results are presented in section 4, but we present the individual velocity components, the three

220   terms on the right-hand side of Eq. 4, to aid in visualizing the model construction. By

221   representing the velocity field with these three terms, we can separate the influence of the bed

222   from dynamics within the ice column to better understand the cause of variability in ice-flow

223   along profile.

224   We refer to the first term on the right-hand side of Eq. 4 as the one-dimensional term,

225   which is governed by the surface vertical velocity. The surface vertical velocity (w_s) is given by

226 the difference between the accumulation rate ($\dot{b}$) and the change in the surface elevation ($\dot{S}$):

227 $w_s = \dot{b} - \dot{S}$. We do not consider basal melt (see sections 3.4 and 4.4).

228 We refer to the second term on the right-hand side of Eq. 4 as the two-dimensional term

229 since it ensures bed and surface parallel flow.

230 The third term on the right in Eq. 4 accounts for variations in the shape of the horizontal

231 vertical velocity, which in our case is the transition from divide to flank flow.

232 The bed elevation and ice thickness (section 3.2) as well as the accumulation rate

233 (section 3.3) used in the kinematic model are derived from the radar data. The prescribed shape

234 functions are based on vertical velocity profiles fit to the ApRES data (see section 3.4). The

235 ApRES measurements are at only four locations and we must define the vertical velocity

236 continuously along the flowline. To do so, we define one shape function for the divide and one

237 for the flank, and prescribe a smooth transition between them. We follow Nereson and

238 Waddington (2002) and assume the width of divide flow influence can be approximated as:

239
$$\beta(x) = exp\left(-\frac{x^2}{2\sigma^2}\right) \text{ (5)}$$

240 where σ is the half-width of the divide zone for the vertical velocity and the transition for the

241 horizontal velocity is then:

242
$$\alpha(x) = \frac{\sqrt{2\pi}\sigma}{2x} erf\left(\frac{x}{\sqrt{2}\sigma}\right) \text{ (6)}$$

243 The transition in the vertical velocity occurs in one to two ice thicknesses from the divide, based

244 on modeling studies (Raymond, 1983) and observations of the width of Raymond arches (e.g.,

245 Matsuoka and others, 2015). The transition in horizontal velocity occurs over a longer distance.

246 The value of p for the shape functions (Eq. 3) are 0.3 for the divide and 7 for the flank. The

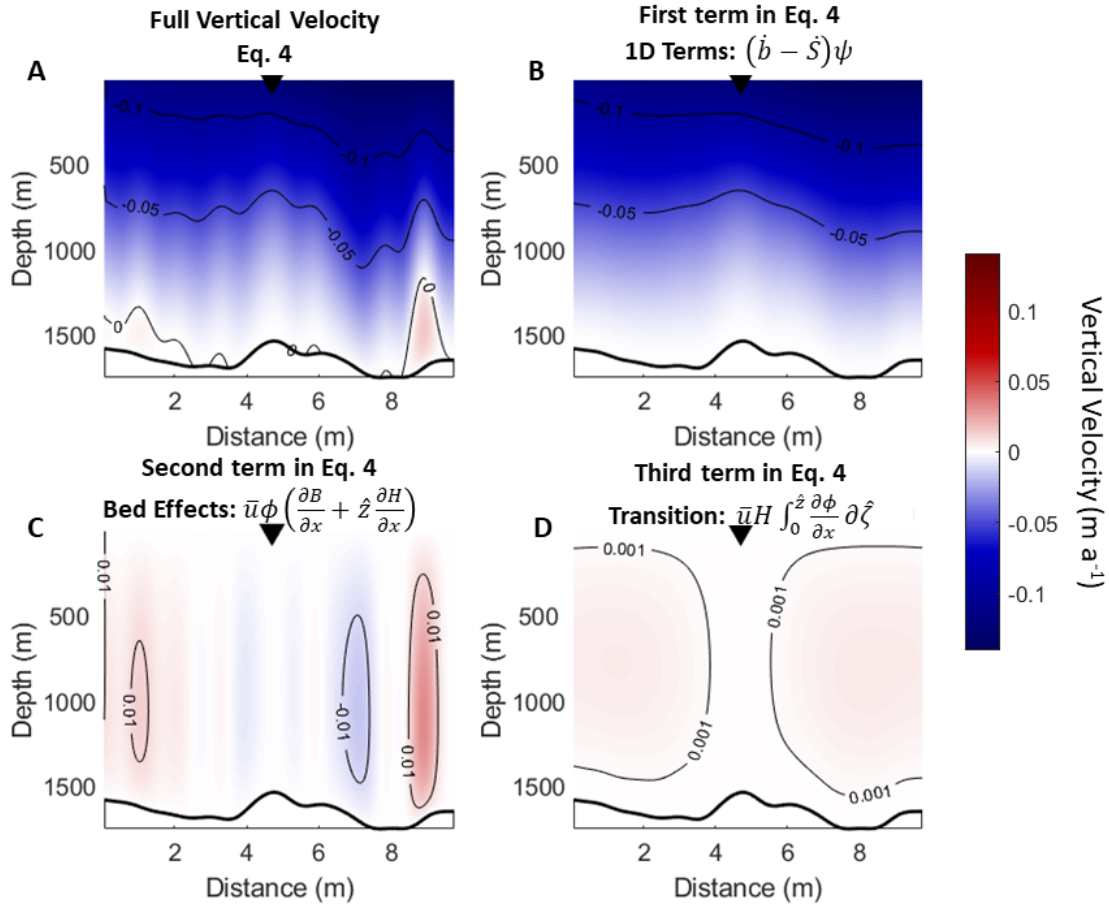247 divide-zone half-width is 2800 m, approximately 1.5 ice thicknesses.

248

Fig. 3: *A) Modeled vertical velocity field using Eq. 4 with the divide at 4.7 km (black triangle). B) First term of Eq. 4, which has the one-dimensional effects and is set by the accumulation rate and shape function. C) second term of Eq. 4, which expresses the vertical velocity for bed-parallel horizontal flow. D) third term of Eq. 4, which expresses the impact of the varying horizontal shape function. All figures use the same color scale to show the relative importance of the terms but have contours of different values to emphasize the magnitude of the terms.*

3. GEOPHYSICAL OBSERVATIONS

The geophysical observations reveal the internal structure and bed of West Dome and provide inputs and constraints for the kinematic model. We first determine the internal stratigraphy from the HF radar reflections. Second, we use the HF radar to determine the bed elevation and assess ambiguities in the bed picks using the kinematic model and measured internal layers. Third, we find the accumulation rate across the dome using a bright layer in the VHF radar which can be dated to 420 years before 2020, when the data were collected, near

264   the US-ITASE shallow core. Finally, we assess the englacial vertical velocity profiles and

265   identify a change in shape with distance from the present ice divide.

266

267   **3.1 Internal Layer Geometry**

268   We traced 22 internal layers from approximately 400 m below the surface to 200 m

269   above the bed (Fig. 2d,e). Layers are consistent and traceable along the full profile to within 400

270   m of the bed. Below 400 m, there is a difference in the character of the layers on the north and

271   south sides of the divide. To the north, there is a bed-conformal and traceable layer between

272   100 and 200 m above the bed that extends to the northern end of the profile. Between that layer

273   and the ice bottom, there appears to be coherent layering just north of the divide, but that signal

274   is lost as the ice thickens along the profile. The lack of continuous layering in this interval is not

275   surprising given the challenges of resolving deep layers (e.g., Drews and others, 2009): returns

276   from the deep layers are weaker due to greater attenuation; the layers vary more in depth as

277   they drape the irregular bedrock; and the relatively long wavelength (~55 m) of the HF system

278   integrates a larger number of small-scale electrical contrasts which can cause more complex

279   reflections. To the south, there is a package of layers that diverge from the traced layer at 400

280   m, indicating a local thickening of the layer package that sits between 200 and 400 m above the

281   bed at the divide as you move south along the profile. These layers lose coherence as they

282   approach the ice bottom.

283   The internal layers cannot be dated with existing information from ice cores because

284   there are no continuous radar profiles between the two West Dome radar profiles and the

285   ITASE ground-based or airborne radar data sets. The only layer that can be dated is the bright

286   reflector in the VHF data (section 2.2, Fig. 2b) because it can be unambiguously matched by

287   correlation to a radar line within 1 km of the dated ITASE core despite the lack of a continuous

288   link. The internal reflectors of the HF radar profiles at West Dome are not distinct enough to be

289   matched to the East Dome and South Ridge HF radar profiles.

290

291   **3.2 Bed Topography**

292   We imaged the bed of West Dome along the x135 and x133 radar lines using the HF

293   radar. The current surface divide is located above a bedrock high (Fig. 2). The ice thickness

294   along x135 ranges from 1510 m below the divide summit to 1750 m at approximately 8 km

295   along the radar line. The bed topography is smoother than at East Dome (Jacobel and others,

296   2005). The bed reflection is visible along the full profile (Fig. 4), although there are two locations

297   where the bed reflection is ambiguous. The most important of these is at 6 km along the radar

298 line. The brightest reflection is at 1640 m depth; however, there is also a weaker return from

299 1580 m depth. This smaller amplitude reflection is likely an off-nadir return and may indicate a

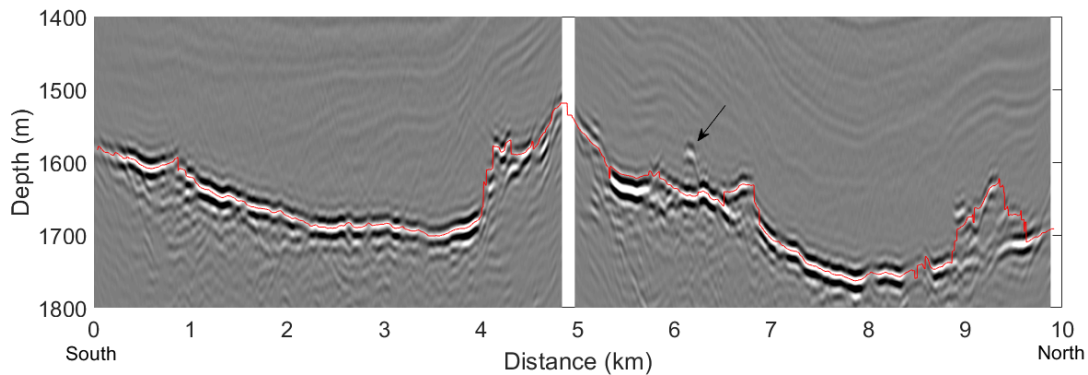300 decameter-scale bump at the bed close to the profile.

301

302

Fig. 4: *The interpreted bed location is shown (red). There is an ambiguity in the bed reflection at*

304 *6 km (arrow).*

305

306   To evaluate the significance of such a feature on the internal layering, we run the

307 kinematic model with bed topographies based on both the original pick and by picking the

308 decameter-scale bump at ~6 km. We also use two different low-pass filters of 500 m and 1000

309 m, resulting in four different potential boundary conditions. The observed layers (and the

310 associated model-predicted layers) deeper than 1000 m are shown in Fig. 5 because they are

311 the most affected by the bed boundary condition. The age of the internal layers is unknown so

312 we cannot compare the modeled and measured layers based on age; instead, we compare the

313 observed layers to a modeled layer with the same average depth. The modeled layers produced

314 using the 500-m filtered beds show greater variability than the observed layers while the 1000-m

315 filtering produces internal layering with smoothness comparable to the measured layers. Using

316 the bed with 1000-m filtering and the decameter-scale bump, the model is able to reproduce the

317 slight dip in the deepest layer at 5.5 km along the radar line. Therefore, we use the 1000-m

318 filtered bed with the bump in all of the model runs used to help interpret the internal layering
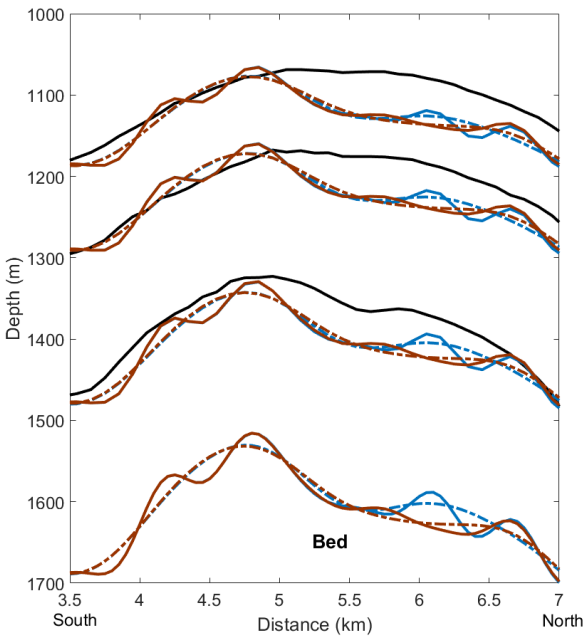
319 (section 4).

320

Fig. 5. *Black lines are observed internal layers. The bottom layers are the four different beds used in the kinematic model. The two brown lines have no bump at 6km; the two blue lines have the bump added. Low pass filtering of 500 m is shown as solid lines and 1000 m is shown as dash dot. The modeled internal layers have line color and type that match the bed.*

325

3.3 Accumulation Rate

The accumulation rates inferred from the VHF radar profiles along x135 and x133 are shown in Fig. 6. There is a ~2 km gap in the x135 line because of poor radar quality. The inferred accumulation rates are similar between the two lines. The highest accumulation rates of 0.14 m a^{-1} are in the north and are relatively constant from 7 km to 10 km along the radar lines. The accumulation rates decrease by about 25% to less than 0.115 m a^{-1} at the south end of the radar line. Because the data from x133 is of higher quality and agrees well with the high-quality portions of x135, we use the accumulation rate inferred from x133 as the forcing for the model runs used to help interpret the internal layering (section 4).
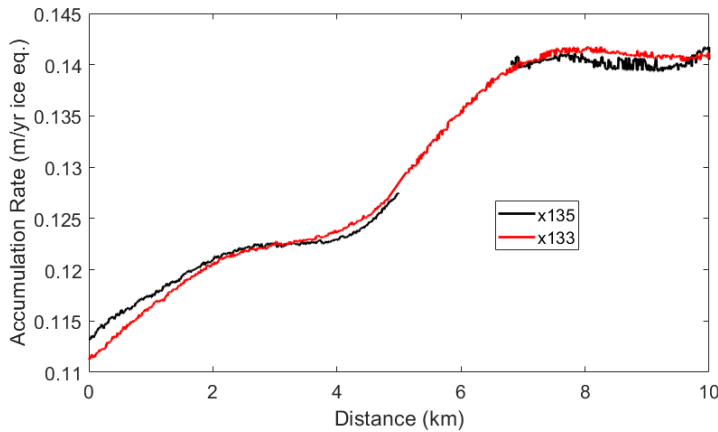
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Fig. 6: *Accumulation rate inference from the bright layer dated to an age of 420 years (1600*
CE). Profile x135 has poor data quality in the center so x133 is used for model forcing given the
close agreement between the two. Note that the x133 profile is slightly offset at 5km (Fig. 1,
inset) such that we interpolate linearly from 4.8 to 5.1 km.

3.4 Englacial Vertical Velocities

Divides with frozen beds have vertical strain rates which are greater near the surface
and smaller near the bed compared with locations of larger surface slopes and shear strain
rates. We refer to this characteristic shape of the vertical velocity near divides as divide-flow,
and the more linear vertical velocity away from divides as flank-flow. The difference in the
vertical velocity patterns yields Raymond arches (Raymond, 1983) when the divide position is
stable. Englacial vertical velocities were derived using ApRES acquisitions in the 2018/19 and
2019/20 field seasons at four sites shown in Fig. 2A with the goal to 1) identify whether the
shape of the vertical velocity is characteristic of those with a frozen bed, and 2) provide
constraints for kinematic modeling of internal layers.

The vertical velocity profiles are plotted by relative height above the bed in Fig. 7A
(where 0 represents the bed and 1 the ice surface) and by absolute height above the bed in Fig.
7B. A useful way to visualize whether divide flow is occurring is to perform a linear fit of the
upper portion of the vertical velocities and to compare the extension of the linear fit to the bed
with the measured vertical velocities (Fig. 7A). The fit is calculated by linear regression between
a relative height of 0.5 to 0.9. The near-surface portion is excluded because of the influence of
firn compaction on the velocity profile above 0.9. For n5000, approximately 5 km north of the
divide, the linear fit matches well for all velocities except for those below 0.05. This near-linear
increase of vertical velocity with height above bed is typical of ice away from a divide (Kingslake

14

362 and others, 2014). At sites n0 and n1000, there is a noticeable divergence from the linear fit, as

363 the vertical velocities show little change below 0.3.

364   The four sites were revisited in the 2021/22 field season. Sites n0, n1000, and n5000

365 showed nearly identical vertical velocities for the 19/20-21/22 period as the 18/19-19/20 period;

366 however, n2000 did not (Fig. S2-5). Therefore, we focus our discussion on the differences

367 between n0 and n1000 near the present divide and n5000, which is outside the divide region. A

368 discussion of the vertical velocities using the 2021/22 field data are in given in the

369 Supplementary Information.

370   To quantitatively describe the vertical velocity profiles, we fit the vertical velocities using

371 two simplified versions of Eq. 4. First, we follow Kingslake and others (2014) and fit with the

372 following one-dimensional term,

373 $$w(\hat{z}) = w_s \psi \quad (7)$$

374 The value of p in the calculation of ψ (Eq. 4) is a useful measure of the shape of the vertical

375 velocity and can be used to characterize the influence of the divide. Small values of p indicate

376 divide-like flow, with increased vertical strain near the surface and reduced vertical strain near

377 the bed. Higher p values indicate more uniform vertical strain with depth.

378   Since the ApRES measures phase, we can only infer a relative velocity, and we must

379 specify one absolute velocity. We assume no motion at the bed and set the average of the

380 velocities within 100 m of the bed to zero. This allows an estimate of the surface vertical

381 velocity, excluding firn compaction, which should be similar to the ice-equivalent accumulation

382 rate. The best-fit values of p and w_s are given in Table 1; the velocities within 100 m of the bed

383 and within 150 m of the surface are not used in the fit. The inferred surface vertical velocity

384 exceeds the inferred 420-year average accumulation rates from the VHF radar data, except at

385 n2000. The inferred surface vertical velocity at n5000 is 0.17 m a^{-1}, nearly 0.04 m a^{-1} (30%)

386 greater than the 420-year average accumulation rate of 0.13 m a^{-1}. We suspect that this is

387 because n5000 has the greatest horizontal velocity (~0.5 m a^{-1}) and is expected to have the

388 largest component of the vertical velocity due to horizontal flow over the bedrock.

389   To account for ice flow over an irregular bed, we also fit the vertical velocities with

390 $$w(\hat{z}) = w_s \psi + \bar{u}\phi \frac{\partial B}{\partial x} \quad (8)$$

391 We neglect the component of the vertical velocity due to lateral variation in the shape of the

392 horizontal velocity profile because it is the smallest term (Fig. 3). We estimate the depth-

393 averaged horizontal velocity from the balance velocity. The bed slopes are calculated on a 200
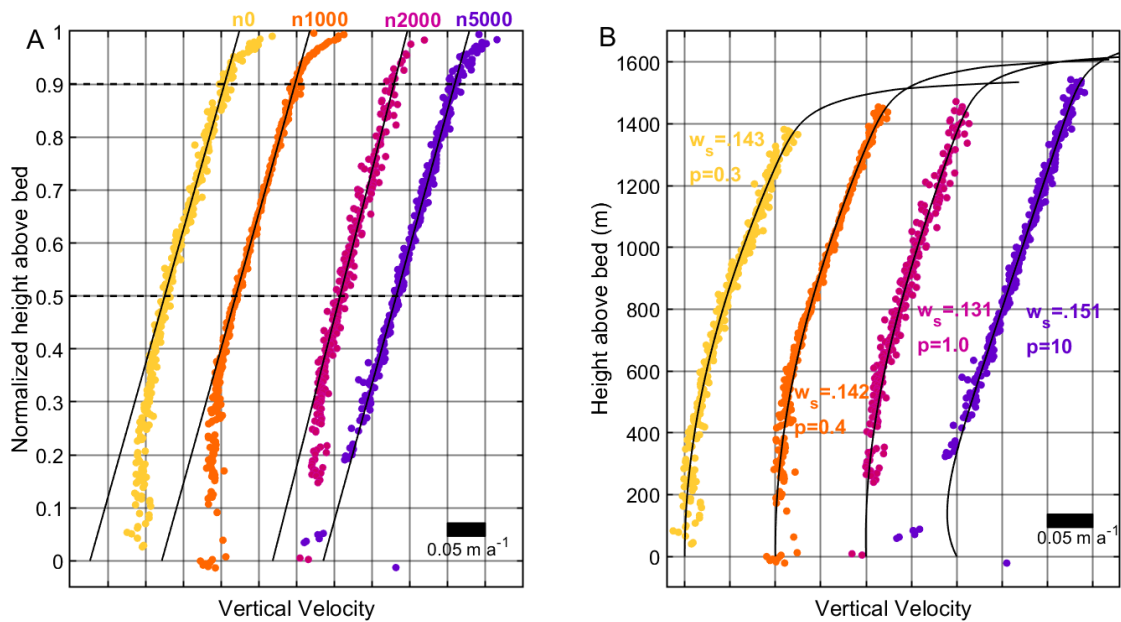
394 m length scale using the unfiltered bed (Fig. S6).

395   In the fit using Eq. 8, the surface vertical velocity is constrained to within 0.02 m a^{-1} of

396   the measured accumulation rate. In addition, the fit finds a uniform shift of the vertical velocity

397   profile since the velocities are relative; this relaxes the constraint we applied when using Eq. 7,

398   where the average velocity in the bottom 100 m was set to 0, and allows us to determine if the

399   vertical velocities are consistent with the glaciological setting. The fit values are also shown in

400   Table 1.

401   The largest difference in the fit parameters between Eq. 7 and Eq. 8 is at n5000, where

402   a reasonable fit with a surface vertical velocity of 0.151 m a^{-1} is possible because of the

403   negative (upward) vertical velocities near the bed caused by flow up the bedrock slope (e.g.

404   Hills and others, 2022). The two measurements closest to the divide, n0 and n1000 are similar

405   to each other with the value of p being indicative of divide-flow; n5000 has a large p value

406   indicative of flank-flow. Because of the uncertainty in the measurements at n2000 and the lack

407   of measurements in between n2000 and n5000, it is difficult to determine the width of the divide

408   zone.

409

410

411 *Table 1: Fits to ApRES vertical velocities*

	Accumulation rate	Fit 1D only			Fit 1D and 2D			Horizontal balance velocity ($\bar{u}$)	bed slope
		w_s	p	rms	w_s	p	rms		
	m a^{-1}	m a^{-1}		10^{-3} m a^{-1}	m a^{-1}		10^{-3} m a^{-1}	m a^{-1}	
n0	0.123	**0.145**	**-0.2**	8.2	**0.143**	**0.3**	4.4	0	-0.21
n1000	0.127	**0.145**	**-0.2**	7.7	**0.141**	**0.4**	3.5	0.056	0.04
n2000	0.131	**0.135**	**2.0**	9.5	**0.131**	**1.0**	9.0	0.127	0.04
n5000	0.131	**0.170**	**4.5**	7.3	**0.151**	**10**	8.6	0.350	0.07

412

413

414 **Fig. 7**: Modeled and measured vertical velocity profiles for the four ApRES locations labeled by

415 their approximate distance in meters from the divide. The horizontal spacing of the vertical lines

416 in both panels is 0.05 m a^{-1}. The positions are shown in Fig. 1 and 2, with n0 in yellow, n1000 in

417 orange, n2000 in pink, and n5000 in purple. A) ApRES vertical velocities; black lines are a linear

418 fit to the interval of 0.5H to 0.9H. B) shows Lliboutry fits to the vertical velocities where the

17

419   surface vertical velocity (excluding firn compaction) is required to be within 0.02 m a^{-1} of the

420   420-year average accumulation rate, the vertical component of ice flow over uneven bedrock is

421   included, and a constant shift for the vertical velocity profile is a free parameter. The transition

422   from divide-flow with low p values to flank-flow with high p values occurs with increasing

423   distance from the divide (see section 2.4).

424

425

4. KINEMATIC MODEL RESULTS

Our kinematic model and data comparison focuses on five objectives: 1) fit the shallowest layer using the kinematic model to determine how well the modern observations reflect late Holocene dynamics and forcing; 2) assess differences in layer depths in the divide region to evaluate the presence of a Raymond arch; 3) fit all layers across the full radar profile to evaluate the likelihood of divide migration within our domain; 4) determine the likelihood of basal melt; and 5) use our best fit model to produce a depth-age scale that captures the annual-layer thickness near the bed.

4.1 Fit to shallowest layer

Before examining the model fit for all of the internal layers, we focus on the shallowest HF radar layer which has a depth of ~430 m and a modeled age of ~4 ka. We assess whether the modern observations of accumulation and vertical velocity are likely to have been constant for the past ~4 ka. The accumulation rate pattern is a 420-year average while the measured vertical velocities are a snapshot over one year.

Using the modern patterns of accumulation and vertical velocity for the past 4 ka produces a layer which is too shallow beneath the divide and too deep north of the divide (Fig. 8). This suggests that the modern accumulation and vertical velocity patterns have not been constant for the past 4 ka, which may indicate that the divide has not been stable at its current position. To evaluate this possibility, we test scenarios of divide onset occurring in 1 ka increments. Prior to the divide onset, we assume spatially uniform flank-flow vertical velocities and uniform accumulation. The modeled layers and the misfit is shown in Figure (8). The modeled layers fit the measured layer best with a 2 ka onset of modern conditions although there is still a significant discrepancy on the south edge of the profile.

For these tests, we have assumed that the divide in the surface topography causes both the vertical velocity pattern and the accumulation pattern. The vertical velocity pattern is primarily caused by the low deviatoric stress beneath the divide although the development of ice fabric may also play a role (Pettit and others, 2007; Martin and others, 2009); however, it is less clear how closely the surface topography of the divide and the accumulation pattern are coupled. More complicated temporal and spatial variations in the accumulation pattern and divide position can improve the fit; however, without evidence to guide *a priori* expectations for how the patterns should develop in time, the improvements would not necessarily be meaningful. An improved fit with more complicated variations in the forcings would reinforce the primary conclusion that the modern conditions are unlikely to have been stable for the past ~4

460   ka. In the following sections, we explore the fit to all of the internal layers to extend our

461   understanding of the divide position and accumulation pattern to older ages.
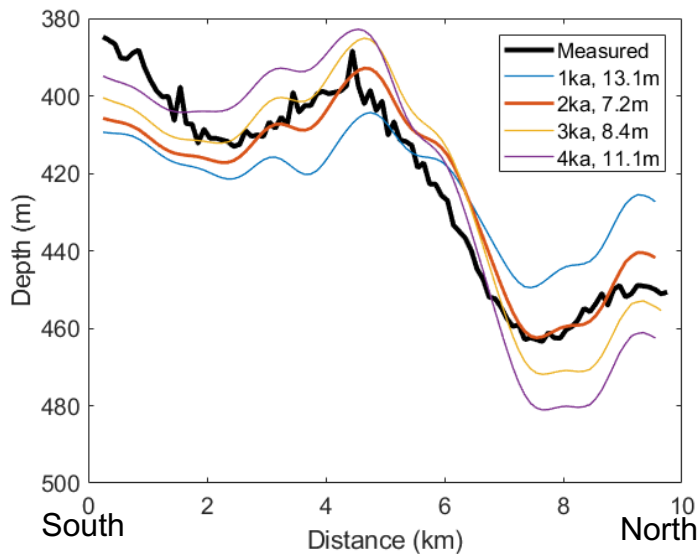
462

463

464

465   **Fig. 8**: *Model fit to the shallowest HF (deep) radar layer. The legend gives the spatially*

466   *averaged misfit to the measured layer (in m) and the age at which the modern vertical velocity*

467   *and accumulation rate patterns are applied (in ka). The divide zone has a width of 1.5H. The*

468   *modeled age of the layer is about 4 ka.*

469

470   **4.2 Evaluating the presence of a Raymond Arch**

471   Although the ApRES vertical velocities indicate that divide-flow is occurring, there is not

472   an obvious Raymond Arch beneath the divide. However the measured internal layers are

473   shallower in the ice column at ~6 km than might be expected based on the bed topography (Fig.

474   2D). In areas of flat bedrock, the amplitude of a Raymond arch can be determined by comparing

475   the depth of an internal layer beneath the divide to the depth on the flank outside of the divide

476   region (e.g. Roosevelt Island, Conway and others, 1999), but the identification of Raymond

477   arches is challenging in areas with greater ice thickness, lower accumulation rates, and without

478   smooth bedrock (e.g. Goel and others, 2018). Since the irregular bedrock at our site does not

479   allow a simple comparison between the depth of a layer beneath the divide and on the flank, we

480   use the kinematic model.

481   We compare the height of the measured layer to one from the kinematic model forced

482   with a spatially constant vertical-velocity shape function (p=4, Fig. 9). The difference between

483   the measured and modeled layers at 5.5 km along the radar line has both similarities and

484   differences to the Raymond arch amplitude at Roosevelt Island (Fig. 9b). The Raymond arch at

485   Roosevelt Island began forming about 3 ka (Conway et al., 1999; Martin et al., 2006). The onset

486   of a layer mismatch begins deeper in the ice column, at a normalized height of about 0.7 at

487   West Dome compared to 0.9 at Roosevelt Island. There are also large misfits in the layer

488   depths outside of the divide zone at West Dome, particularly to the south (Fig. 9A). Thus, the

489   existence of a Raymond arch is uncertain. In the following section (4.3), we model the full set of

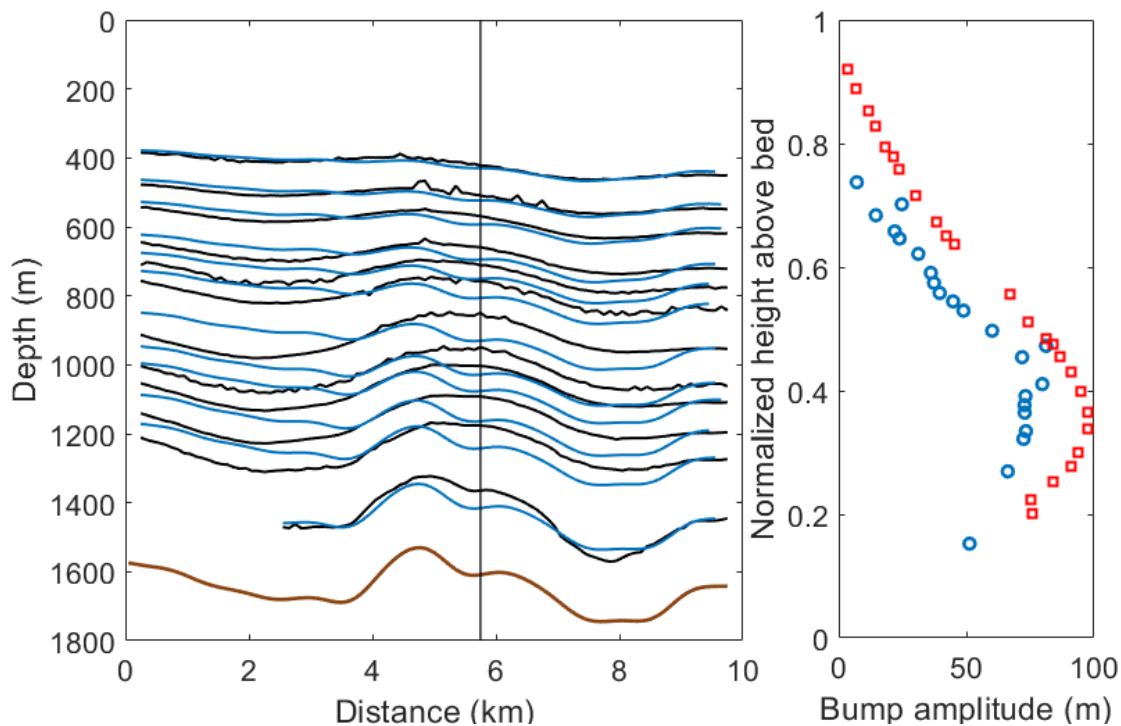490   internal layers to better understand the observed layering.

491

493   **Fig. 9**: *A) Modeled internal layers (blue) assuming uniform flank flow (p=4) compared to*

494   *measured layers (black). The bed is shown in brown. B) The difference between modeled and*

495   *measured layers (blue circles) at 5.75 km (black vertical line) compared to the Raymond arch*

496   *amplitude of Roosevelt Island (red squares) (Conway and others, 1999).*

497

498   **4.3 Model fit to all layers**

499   The kinematic model fit to the shallowest layer (section 4.1) suggested that the modern

500   divide and accumulation pattern have not been stable for more than a couple of thousands of

501   years while the possibility of a Raymond arch exists (Section 4.2) offset to north from the

502   present divide. Here we evaluate the fit to all the layers for test scenarios of divide migration and
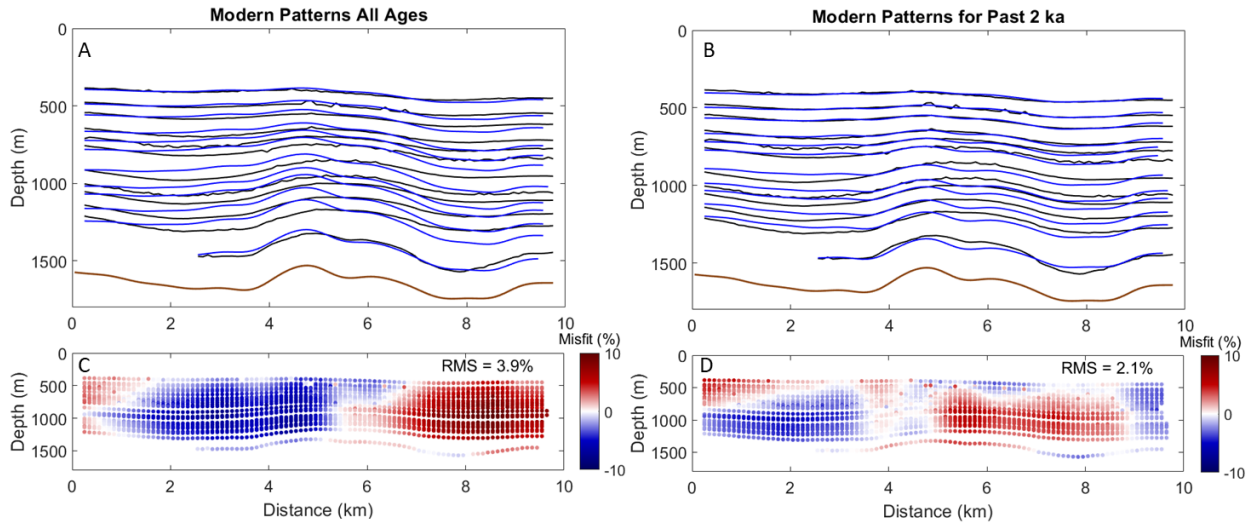
503   variations in the accumulation pattern. The primary goals are to evaluate the likelihood of divide

504   migration within our domain and identify the appropriate forcings for the thermal and depth-age

505   modeling.

506   The kinematic model fit to the full depth of measured layers is shown in Fig. 10 for two

507   scenarios: A) using the measured accumulation and vertical velocity forcings for all ages and B)

508   using the measured forcings for only the past 2 ka (i.e. divide onset at 2 ka, see section 4.1) and

509   spatially uniform patterns of accumulation and vertical velocity for ages older than 2 ka. The root

510   mean square error, calculated as fraction of layer depth offset, is improved by about a factor of

511   2 when the modern patterns are used for only the past the 2 ka. The resulting misfit shows a

512   pattern of the modeled layers being too deep to the north of the divide, and too shallow to south.

513   There are two primary changes in the model forcing that will yield deeper layers to the

514   south, shallower layers to the north, and thereby improve the fit: 1) Move the region of divide

515   flow to the north; and 2) reverse the accumulation gradient such that there is more accumulation

516   to the south and less to the north.

517   We performed model runs with the divide shifted north to 6 km along the flowline for

518   different ages prior to 2 ka. The divide then migrates from 6 km to 4.7 km (the modern divide

519   position) between 2.5 and 2 ka. The best fit occurs with a divide onset at 6 km at 6 ka. In Fig.

520   11, we show the misfit for divide onset at 6 ka as well as for 9 ka; the misfit for the base

521   scenario (Fig. 10B) of divide onset at 2 ka at 4.7 km along the flowline is also shown. In the

522   scenarios with divide onset prior to 2 ka, the modeled layers are shallower to the north because

523   of the increased layer thinning in the upper portion of the ice sheet. The modeled layers are also

524   deeper to the south, better matching the measured layers, because the average depth of the

525   modeled layer is constrained to match the average depth of the measured layer. Divide onset at

526   6 ka results in better fits from 5 to 7 km and from 0 to 4 km along the flowline throughout most

527   the depth; however, the misfit increases from 4 to 5 km, the modern divide region. The scenario

528   with divide onset at 9 ka further increases the misfit beneath the modern divide, which drives an

529   overall increase in the misfit for the full flowline. The timing of the divide onset should be

530   interpreted with caution because the layers are not dated and the improvement in fit is modest.

531   These tests with the kinematic model indicate that the divide is unlikely to have been

532   established prior to the mid-Holocene.

533

534   **Fig. 10**: *A and B) Bed (brown), measured internal layers (black) and modeled internal layering*
535   *(blue) using the modern spatial patterns of vertical velocity and accumulation rate for all ages*
536   *(A) and only the past 2 ka (B, uniform vertical velocity and accumulation rate before 2 ka). C,D)*
537   *Relative misfit (measured depth – modeled depth)/measured depth. Panels A) and B) show only*
538   *13 of the 22 measured layers for clarity while panels C) and D) show all 22 layers.*

539

540   To assess the impact of the spatial pattern of accumulation, we performed two tests to
541   compare with the base scenario in Fig. 10B. In both scenarios, the modern pattern of vertical
542   velocities began at 2 ka with uniform flank-flow for older ages. The first scenario kept the
543   modern accumulation gradient fixed for all ages; the second scenario flipped the modern
544   accumulation gradient for ages older than 2 ka (Fig. S7). Using the modern accumulation
545   gradient for all ages increases the relative misfit from 2.1% to 3.2%, while using a flipped
546   accumulation gradient increases the relative misfit from 2.1% to 2.2%. As indicated above, a
547   reversal in the accumulation gradient results in deeper layers to the south and shallower layers
548   to the north, yielding a similar misfit as the base scenario. Different accumulation gradients
549   and/or timing of changes in the past accumulation gradients can yield better fits. This issue of
550   non-uniqueness is inherent in inferring accumulation rates from deep internal layers near ice
551   divides (e.g. Koutnik et al., 2016), and is more challenging when the layers have not been
552   dated. Scenarios with an onset of the flipped accumulation gradient in the Holocene, and
553   uniform accumulation for older ages, produce a worse fit than when the flipped gradient is
554   applied for all ages. We have no *a priori* expectation that a reversal in the gradient should have
555   occurred during the early-to-mid Holocene when West Antarctic climate was relatively stable.

556   While past changes in the accumulation gradient cannot be well constrained, it is unlikely that

557   the modern pattern has persisted for more than a few thousand years.

558   Overall, the kinematic modeling shows that the divide position was unlikely to be stable

559   before the mid-Holocene and that the pattern of accumulation is difficult to constrain. A key

560   conclusion for the depth-age relationship is that because the divide is unlikely to have been

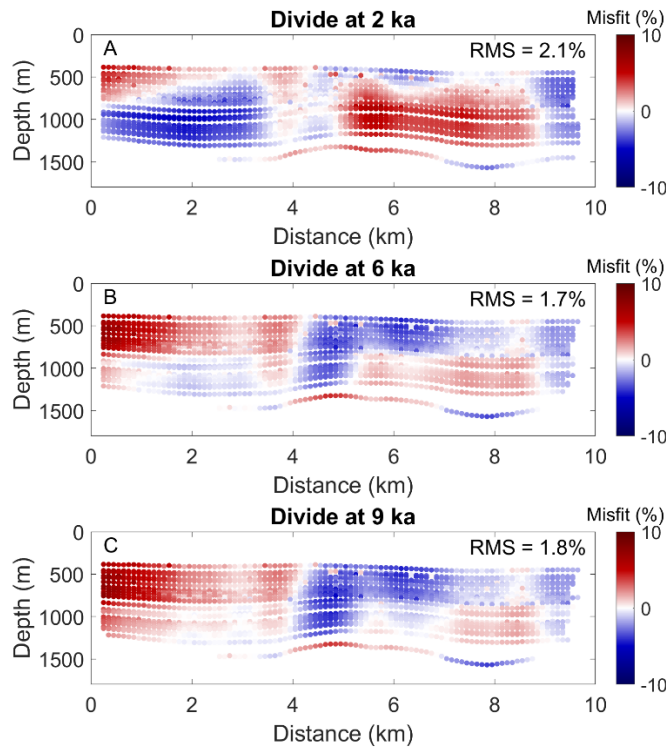561   stable, a flank-flow vertical velocity is most appropriate for modeling the depth of the older ice.

562

563

564   **Fig. 11**: *Relative misfit as calculated in Figure 10E,F for kinematic model scenarios with no*

565   *divide onset prior to 2 ka (A), divide onset at 6 ka at 6 km (B), and divide onset at 9 ka at 6 km*

566   *(C).*

567

568   **4.4 Temperature modeling and basal thermal state**

569   We use a 1-D ice-and-heat flow model to estimate the internal and basal temperature at

570   West Dome. The model is described in Fudge and others (2019) and Buizert and others (2021).

571   We take two approaches. First, we estimate the internal temperature based on the 65 mW m^{-2}

572   average of three recent remotely-sensed estimates of geothermal flux which are tightly

573   clustered: 62±10 mW m^{-2} (Shen and others, 2020), 68±25 mW m^{-2} (Stal and others, 2020), and

574   66±11 mW m^{-2} (Martos and others, 2017). This provides a prior estimate for the temperature

575   profile for use in planning ice core drilling and analyses. Second, we find the minimum

576   geothermal flux at which melting begins (e.g. Fudge and others, 2019).

577   The ice-and-heat flow model is forced by time-varying surface temperature,

578   accumulation rate, and vertical velocity shape factor histories. We use an ice thickness of 1600

579   m, which is held constant. The histories are based on the two closest deep ice cores, the WAIS

580   Divide ice core (WDC) and the South Pole ice core (SPICEcore); these histories are extended

581   through the LIG using the EPICA Dome C core (EPICA, 2004; Veres et al., 2013). The

582   temperature histories is found using:

583    $$T(t)_{Model} = T(0)_{Herc} + \left(T(t)_{core} - T(0)_{core}\right) \quad (12)$$

584

585   Where $T(t)_{Model}$ is the surface temperature forcing for the thermo-mechanical model, $T(0)_{Herc}$

586   is the modern temperature at Hercules Dome and is -41°C based on a 10-m firn temperature

587   measurement in 2019, $T(t)_{core}$ is the inferred temperature history from the one of the ice cores,

588    $T(0)_{core}$ is the modern surface temperature of the ice core site, and t is model time. The LGM-

589   modern change is -11°C for WDC (Cuffey and others, 2016) and -6°C for SPICEcore (Kahle and

590   others, 2021). The accumulation rate histories are calculated as

591    $$\dot{b}(t)_{model} = \dot{b}(0)_{Herc} \times \frac{\dot{b}(t)_{core}}{\dot{b}(0)_{core}} \quad (13)$$

592

593   Using the same notation as for the surface temperature in Eq. 12. The modern accumulation

594   rate at Hercules Dome, $\dot{b}(0)_{Herc}$, is 0.13 m a^{-1}. Both WDC (Fudge and others, 2016) and

595   SPICEcore (Kahle and others, 2021) have inferred LGM accumulation rates of about 40% of
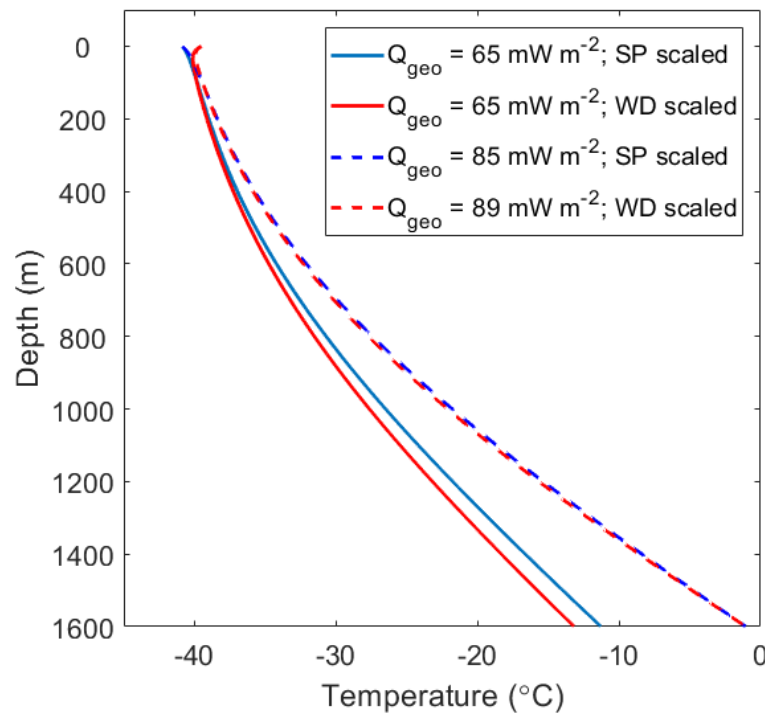
596   modern.

Fig. 12: Temperature profiles for West Dome. Solid lines use the average of the remotely sensed geothermal flux estimates (65 mW m^{-2}); dashed lines assume the bed is at the pressure melting point. The surface temperature and accumulation rate histories are scaled from values at SPICEcore (blue) and WAIS Divide (red) using modern values of -41°C and 0.13 m a^{-1}.

The englacial temperature profiles are shown in Fig. 12. The geothermal flux necessary for melting at present is 85±7 mW m^{-2} using the SPICEcore scaling and 89±7 mW m^{-2} using the WDC scaling. The uncertainty was calculated assuming an end-member modern surface temperature of -39°C (2°C warmer) and modern accumulation rate of 0.11 m a^{-1} (0.02 m a^{-1} lower). The minimum geothermal flux to produce melting is considerably larger than the remotely sensed estimates inferred by three different studies. Our estimated range of the geothermal flux necessary for basal melting overlaps with the uncertainty of only one of these estimates, Stal and others (2020), and only because of its large (25 mW m^{-2}) uncertainty.

4.5 Depth-Age Relationship

Because the measured internal layers cannot be dated, preliminary depth-age relationships must be assessed from modeling. We use the onset of the divide at 2 ka (sections 4.1 and 4.3) and three different choices for the vertical velocity shape factor (4, 7, and 10) for

26

617   ages prior to 2 ka. We use the two accumulation histories described in section 4.4 which are

618   based on WDC and SPICEcore. For the kinematic model forcing, the fractional accumulation is

619   multiplied by the modern spatial accumulation-rate pattern.

620   The resulting depth-age relationships at 5.5 km along the x135 flowline are shown in Fig.

621   13. The choice of vertical-velocity shape factor has a larger influence than the choice of

622   accumulation history. Ice of 132 ka age, the start of the LIG, ranges from 47 m to 87 m above

623   the bed. The average LIG annual-layer thickness is approximately 1 mm.
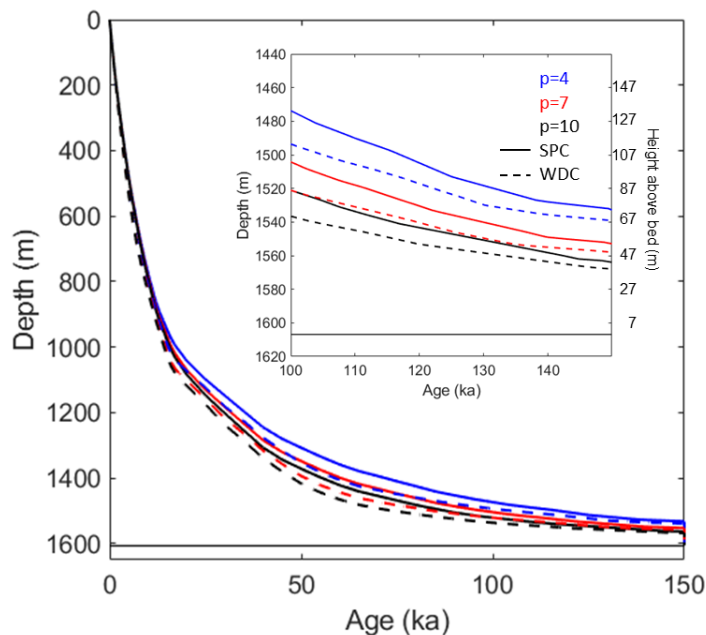
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625

626

627   **Fig. 13**: *Depth-age relationships at 5.5 km along the flow line. Accumulation forcing is scaled to*

628   *SPC (SPICEcore, solid) or WDC (WAIS Divide, dashed). Three different vertical velocity profiles*

629   *for flank flow (p=4, 7, or 10) are shown for each accumulation forcing. The height above the bed*

630   *for ice of 132 ka age ranges from 47 to 87 m.*

631

632   **5. DISCUSSION**

633   **5.1 Potential for a deep ice core**

634   One goal of drilling a deep ice core at Hercules Dome is to recover ice that includes the

635   onst of the LIG (132 ka), and preferable Termination II (the transition into the LIG from the

636   previous glacial maximum) as well. To preserve ice of this age, there must be limited or zero

637   basal melt and no more than minor disturbances to the stratigraphy. The current pattern of

27

638 vertical velocity across the divide at West Dome suggests the ice is frozen to the bed. This is

639 supported by the ice-and-heat flow modeling (section 4.4). With a geothermal flux of 65 mW m^{-2},

640 the ice at the bed is approximately -10°C, which would allow subglacial bedrock drilling after

641 completion of the ice core.

642   The presence of a frozen bed today also implies no significant impact from basal melt at

643 older ages, even if the bed is near the pressure melting point. In the model runs where we found

644 the maximum geothermal flux before basal melt occurred, the bed remains frozen at all ages

645 with the WAIS Divide forcing. For the SPICEcore scenario, there is a ~3000-year period of basal

646 melt that occurs at the end of the last glacial maximum (i.e., from ~25 to 22 ka). The maximum

647 melt rate is 0.04 mm a^{-1}, and the total predicted melt is 80 mm. While these two scenarios do

648 not encompass the full range of possibilities, they indicate that significant basal melt is unlikely

649 to impact the age of the basal ice.

650   The impact of changes in ice thickness are difficult to evaluate because it is not clear if

651 Hercules Dome was thicker or thinner at the Last Glacial Maximum. A thicker ice sheet at the

652 LGM would cause a warmer basal temperature and likely increased basal melt, while a thinner

653 ice sheet would have the opposite effect. The modest amount of basal melt would not remove

654 ice from the LIG. In fact, basal melt rates up to ~0.8 mm a^{-1} would preserve thicker packets of

655 ice from the LIG, although the ice would be closer to the bed. While the evidence for a frozen

656 bed and limited basal melt may not be as definitive as a measured basal temperature, our work

657 suggests that basal melt is unlikely to have removed ice older than 132 ka from the West Dome

658 site.

659   The preservation of stratigraphic order is more difficult to assess. The layering at West

660 Dome is resolvable until just a few tens of meters above the bed, but the deepest layer that is

661 traceable along the full radar profile is ~400 m meters above the bed. Ice from the start of the

662 LIG (132 ka) is likely between 47 m and 87 m above the bed, and thus continuity of the deep

663 stratigraphy is important for recovering ice of this age. The deep internal reflectors are coherent

664 all the way to the ice bottom just north of the divide, with more bed conformal layering on the

665 north side of the divide generally, suggesting the north is the preferable location for a core.

666   The internal layers suggest that the current divide position has not been stable beyond

667 the mid-Holocene; however, the internal layers alone are not enough to constrain the extent of

668 divide migration. Modest variations in the divide position of a few kilometers are enough to

669 prevent the development of a clear Raymond Arch above an irregular bed. The lack of a clear

670 Raymond arch at West Dome is not surprising because the characteristic time of ~13 ka, $(\frac{H}{\dot{b}})$, is

671   substantially larger than for the thinner and higher accumulation coastal domes where Raymond

672   Arches are widely observed (Matsuoka and others, 2015).

673   Our best-fit models indicate that average annual layer thicknesses are about 1 mm

674   during the LIG. With continuous-flow analysis methods that are able to make measurements

675   with ~0.5 cm resolution (e.g., Röthlisberger, 2000; Osterberg and others, 2006; Gkinis and

676   others, 2010; Sigl and others, 2016; Jones and others, 2017), measurements of the chemistry

677   and isotopes during the interglacial will have approximately decadal resolution. For gas

678   sampling with a typical sample length of ~10 cm, this translates to a maximum of centennial

679   resolution. The largest challenge from thin annual layering will not be resolution but the limited

680   ice availability for ice of older ages. One approach to overcome the challenge of a thinner

681   packet of LIG ice is to drill one or multiple replicate cores with a deviation from the main

682   borehole.

683   One limitation of the shallower ice at West Dome is that borehole thermometry (e.g.

684   Cuffey and others, 2016) to constrain the magnitude of the glacial-interglacial temperature

685   change becomes increasingly difficult. However, new techniques such as water isotope diffusion

686   lengths, and firn thickness and gas-age ice-age difference (Δage) constraints, have been

687   pioneered to provide alternate ways of addressing this question (e.g. Gkinis and others, 2014;

688   Holme and others, 2018; Kahle and others, 2021; Buizert and others, 2021).

689   The geophysical survey at Hercules Dome indicates that a continuous climate record

690   through the LIG could likely be obtained at West Dome. West Dome is the highest elevation

691   portion of Hercules Dome, and is the most pronounced dome with the simplest ice-flow setting.

692   The ice thickness varies relatively little at West Dome, with a mean depth of ~1600 m, which

693   minimizes the risk of disrupted layering from complicated ice flow. The ice temperature at the

694   bed is likely below freezing, preserving old ice near the bed.

695

696   **5.2 Future Plans**

697   A full field season focused on the West Dome region is planned for 22/23. Future

698   measurements will include more extensive HF and VHF surveys. Additional ApRES

699   measurements will be made to both more fully characterize the englacial vertical velocities and

700   to constrain ice fabric variations. These future measurements will improve both the spatial

701   resolution and coverage of the data to more precisely define the best ice core site within the

702   West Dome region. Other locations at Hercules Dome are less promising for a deep ice core,

703   and are not prioritized for future work. At East Dome, where the US-ITASE traverse visited

704   (Jacobel and others, 2005), the basal topography and ice flow appears prohibitively complex.

705 South Ridge has moderately thicker ice but the ice flow is from East Dome and over complex
706 bedrock topography.
707

708 **6. CONCLUSIONS**

709   The surface elevation of Hercules Dome is not defined by a single topographic high, but
710 rather three features with local divides. We have focused on West Dome, which is at the highest
711 elevation in the Hercules Dome region and has the simplest ice-flow regime. Coherent internal
712 layers are imaged to within tens of meters of the bed. The ice is of moderate thickness (~1600
713 m) and the bed is likely frozen; a geothermal flux ~20 mW m^{-2} greater than suggested by
714 regional estimates would be required to produce melting. The internal layer pattern cannot be
715 well fit with a kinematic ice-flow model if modern accumulation and vertical velocity patterns are
716 held constant in the past; the lack of fit indicates that the modern divide position has likely been
717 established during the Holocene. As with other inland divides in Greenland and Antarctica,
718 modest variations in divide position would prevent the development of a prominent Raymond
719 arch. Our best-fit modeled depth-age relationship suggests ice from the LIG is between 45 m
720 and 90 m above the bed, and that the average annual layer thickness for that time period is
721 about 1 mm. The modeled depth-age relationship is insensitive to the Holocene flow history
722 because the age of the deep ice depends primarily on the average shape of the vertical velocity
723 profile for the last glacial-interglacial cycle. The lack of modern basal melt implies no significant
724 melt in the past and therefore ice from the LIG should not have been removed. In conclusion,
725 West Dome is a promising location for a deep ice core that will preserve a climate record
726 sensitive to the size of WAIS during the LIG.
727

728 **AUTHOR CONTRIBUTION**
729 TJF, KC, and EJS conceived of the study. AOH, ANH, BH, EJS, GKO, JEC, KC, and
730 NH collected the geophysical data. AOH, ANH, BH, KC, LD, NH, and TJF contributed to the
731 data processing, analysis and interpretation. BH and TJF conducted ApRES interpretation in
732 this manuscript. ANH, LD, and TJF inferred the snow-accumulation record for this manuscript.
733 NH contributed insight to layer and bed interpretations. TJF performed the kinematic and
734 temperature modeling. All authors contributed to the manuscript.
735

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740

741 **DATA AVAILABILITY**: Radar data is available at https://www.usap-
742 dc.org/view/project/p0010359

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