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4	Survival of polymeric microstructures subjected to interrogatory touch
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# 25 Abstract

26 Polymeric arrays of microrelief structures have a range of potential applications. For 27 example, to influence wettability, to act as biologically inspired adhesives, to resist biofouling, 28 and to play a role in the "feel" of an object during tactile interaction. Here, we investigate the 29 damage to micropillar arrays comprising pillars of different modulus, spacing, diameter, and 30 aspect ratio due to the sliding of a silicone cast of a human finger. The goal is to determine the 31 effect of these parameters on the types of damage observed, including adhesive failure and 32 ploughing of material from the finger onto the array. Our experiments point to four principal 33 conclusions. (1) Aspect ratio is the dominant parameter in determining survivability through its 34 effect on the bending stiffness of micropillars. (2) All else equal, micropillars with larger 35 diameter are less susceptible to breakage and collapse. (3) The spacing of pillars in the array 36 largely determines which type of adhesive failure occurs in non-surviving arrays. (4) Elastic 37 modulus plays an important role in survivability. Clear evidence of elastic recovery was seen in 38 the more flexible polymer and this recovery led to more instances of pristine survivability where 39 the stiffer polymer tended to ablate PDMS. We developed a simple model to describe the 40 observed bending of micropillars, based on the quasi-static mechanics of beam-columns, that indicated they experience forces ranging from  $10^{-4} - 10^{-7}$  N to deflect into adhesive contact. 41 42 Taken together, results obtained using our framework should inform design considerations for 43 microstructures intended to be handled by human users.

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# 48 Introduction

### 49 Background

50 High-aspect-ratio organic microstructures (e.g., posts, pillars, tubes, wires, and other 51 shapes) occur naturally in the plant and animal kingdoms (e.g., lotus leaves and gecko feet). 52 Moreover, they are potentially important for myriad technological applications, ranging from 53 anti-fouling surfaces to materials with reconfigurable tactile properties, i.e., for haptic interfaces. 54 In most envisioned applications, such structures will be subject to substantial mechanical insults, 55 like contact by human fingers. Unlike high-aspect-ratio microstructures of biological origin, 56 artificial ones cannot regenerate readily. Thus, it is necessary to develop criteria for the design of 57 structures such that they are likely to survive interrogatory touch by human users. Here, we 58 fabricated a series of high-aspect-ratio micropillars in a photocurable resin which differed in 59 interpillar spacing, height, diameter (and thus aspect ratio), and elastic modulus. We subjected 60 these arrays to a tangential force provided by a silicone replica of a human finger. The downward 61 pressure and lateral contact area was designed to approximate normal interaction of human 62 fingers with real materials and devices—i.e., "interrogatory touch." The goal was to determine 63 the design criteria necessary for micropillar survival in the laboratory using a setup that 64 simulated a realistic scenario.

Since the development of soft lithography in the 1990s(1), high-aspect-ratio polymeric microstructures fabricated by replica molding in silicone templates have been central to a range of proposed applications. In many of these applications, the role of the microstructuring is to modify the interfacial forces.(2–4) Taking inspiration from structures in nature, superhydrophobic and oleophobic surfaces modeled after the lotus leaf have become an

70 important area of research.(5–8) Similar structures are under investigation for their abilities to

71 retard the formation of biofilms (e.g., of bacteria on medical devices or of barnacles on the hulls 72 of ships).(9) While these structures are meant to reduce adhesion, it is also possible to engineer 73 other types of high-aspect-ratio structures for the purposes of promoting it. For example, the 74 long, thin keratinous spatulae of the gecko have inspired the development of a range of 75 bioinspired adhesives based on van der Waals forces. (10–13) The structures on the toes of tree 76 frogs modify hydrodynamic forces that can permit the animal to adhere to surfaces, even under 77 water.(14) In human-engineered applications, high-aspect-ratio relief structures are used for their 78 mechanical behavior. For example, conical structures composed of biodegradable polymers and 79 drugs have been used as microneedle patches for noninvasive drug delivery.(15–17) These 80 structures are designed to puncture the skin and dissolve. In contrast to this application, contact 81 with the skin of micropillars for most other applications is potentially highly damaging to the 82 relief structures, yet almost impossible to avoid in everyday use. One potential application of 83 polymeric microstructures is in haptics, (18,19) where contact with the skin is not just 84 unavoidable but the very reason for these structures to exist.(20) Applications in robotic 85 touch,(21–24) along with haptics-enhanced minimally invasive surgery(25) and virtual 86 reality(26) require contact with human skin at realistic (i.e., significant) contact pressures.(27) 87 Because of the importance of these high-aspect-ratio polymeric structures, along with the 88 necessity to have them exposed to the environment, it would be highly beneficial to develop a 89 framework for avoiding breakage and collapse of the structures when subjected to realistic forces 90 by imperfect, highly non-ideal indenters (i.e., human fingertips exploring surfaces— 91 "interrogatory touch").(28) Our approach is thus different from most other studies on the failure 92 of polymeric microstructures, which use idealized indenters or sliders in highly controlled 93 conditions.(29–31)

94 Degradation in function of an array of polymeric microstructures can occur by breakage 95 of the structures, collapse of the structures, or deposition of material from the comparatively soft 96 indenter (i.e. the finger) onto the array. These modes of degradation originate from intensive and 97 extensive properties of the structures and of the array. Intensive properties deriving from the 98 polymeric material include strength, toughness, modulus, and surface forces, while extensive 99 properties derive from the geometries of the individual microstructures and of the array (e.g., 100 spacing, diameter, and aspect ratio). Breakage occurs when the applied tangential force 101 overcomes the ultimate tensile stress of the polymeric structures. In principle, it is 102 straightforward to mitigate breakage by increasing the strength of the polymer (greater molecular 103 weight, crosslink density, and intermolecular forces). Collapse occurs due to bending and 104 subsequent adhesion to another microstructure (lateral collapse) or to the substrate (ground 105 collapse).(28) As a mode of failure, collapse is more difficult to mitigate than breakage, as all 106 sufficiently thin structures exhibit appreciable bending upon application of a tangential force, 107 regardless of the modulus (i.e., low bending stiffness). There are at least three ways in which 108 structures can collapse (Fig 1). For example, "pairwise collapse," in which two adjacent 109 structures adhere at their tips, "clustering," in which a group of structures adhere at an apex, and 110 "matting," in which groups of structures bend in the same direction.

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- Fig 1. Spectrum of mechanical responses. Digital rendering and example SEM images showing a range
  of deformation outcomes in order of decreasing micropillar bending stiffness.

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### 115 **Theory**

#### 116 Lateral collapse (pairwise and clustering)

117 The tendency toward lateral collapse stems from a competition between the elastic energy 118 stored in bent pillars and the adhesive energy between them.(32,33) In the case of pairwise 119 collapse and clustering, Glassmaker et al. formulated a critical aspect ratio beyond which 120 patterned cylinders made of polydimethylsiloxane (PDMS, Sylgard 184) laterally collapse as a 121 result of the strong adhesion between adjacent pillars once in contact

122 
$$\frac{l}{d} = \left(\frac{0.57E^{\frac{1}{3}}a^{\frac{1}{2}}}{\gamma_s^{\frac{1}{3}}d^{\frac{1}{6}}(1-\nu^2)^{\frac{1}{12}}}\right) \quad (1)$$

where 1/d is the aspect ratio of length over diameter, a is the pitch, *E* is the elastic modulus,  $\gamma_s$  the surface energy, and v is the Poisson ratio of the material system.(32)<sup>(34)</sup>

125

#### 126 Matting

127 In the case of matting, Persson derived a critical aspect ratio beyond which arrays of 128 fibers would condense and form tilted compact layers. By considering the van der Waals 129 interaction between fibers,  $\varepsilon$ , the curvature of the bent fibers,  $\theta$ , and the elastic modulus of the 130 fibers, Persson concluded that elastic fibers would fail by matting when they exceeded the aspect 131 ratio:(33)

132 
$$\frac{l}{d} = \frac{1}{2} \left( \frac{\pi}{24} \frac{E d^2}{\varepsilon} \right)^{\frac{1}{2}} \theta \quad (2)$$

This model is especially interesting because there is a dependence on the curvature of the fibers leading to lateral collapse. Persson's derivation has an indirect dependence on the density of the array because of there is an increase in elastic restoring force with increasing fiber curvature. Tightly packed arrays may prevent failure by matting because the reduced penetration past the plane defined by the tops of the pillars can prevent a large enough angle from being obtained. 138

#### 139 Ground collapse

Ground collapse, a type of degradation especially likely in low-density arrays, has been
predicted with derivations by Roca-Cusachs et al.(35) The authors determined that the critical
aspect ratio is:

143 
$$\frac{l}{d} = \frac{\pi^{\frac{5}{3}}}{2^{\frac{11}{3}}3^{\frac{1}{2}}}(1-\nu^2)^{-\frac{1}{6}} \left(\frac{E}{2\gamma_s}\right)^{\frac{2}{3}} d^{\frac{2}{3}} \quad (3)$$

144 assuming that the pillars and the substrate are formed of identical materials. Each of these 145 models only considers elastic deformation held in place by adhesive forces alone; there are no 146 considerations of external loads on the pillars or plastic deformation which is expected to lower 147 the critical aspect ratio. Furthermore, these models do not consider buckling from gravitational 148 forces as described by Hui et al.(36) However, with increasing surface area to volume ratio for 149 standing structures, the effects of gravitational forces are overcome by adhesive forces for 150 structures with sizes in the micrometer to nanometer range.(28)

151 The deflection of the pillars and, consequently, the extent of degradation of an array will 152 depend to a large degree on the extent of adhesion and tangential force (i.e., friction) needed for 153 the slider (or finger) to traverse the substrate. Amontons-Coulomb friction law state that the 154 frictional force opposing sliding is proportional to the normal load and independent of the 155 apparent area of contact.(37) In their seminal work on friction(38), Fuller and Tabor explained 156 this law through the difference between the apparent versus real area of contact. They posited 157 that the solids in contact are largely supported through the summits of surface irregularities such 158 that intimate contact occurs over an area so small as to be independent of the size of the surfaces. 159 With an increase in normal force, increasing numbers of asperities come into contact in order to

160 accommodate the load and this results in intense local pressure leading to plastic deformation 161 and flow. Fuller and Tabor observed that when one material is harder than the other and 162 sufficient tangential force was applied to initiate sliding, the harder material tended to abrade the 163 softer material in a phenomenon they refer to as "ploughing". Fuller and Tabor were also among 164 the first to experimentally show how the interfacial adhesion between elastic solids decreases 165 with increasing roughness of the substrate.(39) They further showed that adhesive effects due to 166 surface roughness are more significant for interrogatory work pieces (i.e., the indenter, slider, or 167 finger) with higher elastic moduli. Both relationships can be understood as the relationship 168 between surface energy and contact area. Rough surfaces with large asperities reduce the contact 169 area in the interface for high-elastic moduli materials, (40) while softer materials can conform to 170 the rough surfaces and increase the contact area.(41)

Persson et al. were able to apply JKR theory—which describes adhesive force between a ball on a flat surface when one is elastic(41)—to formulate a quantitative model to calculate interfacial adhesion of a smooth rubber ball on a hard and rough surface as a function of surface roughness.(42) This idealized scenario involving a smooth slider surface does not account for surface irregularities on complex surfaces and cannot be directly applied to finger sliders.

Formulating a model to predict the degradation of a micropillar array that accurately describes the effects of the friction and adhesive forces involved when a finger makes dynamic contact with the micropillar surface remains a challenge. An attempt at modeling a similar interaction has been made by Degrandi-Contraires et al.(43) However, in their case the interrogatory material was a smooth elastomer. No attempts have been made to understand this interaction with a realistic model of fingertip, which contains fingerprint ridges and other idiosyncratic asperities of a real finger that might serve to concentrate force on the array at

various "hot spots" on the finger. To produce an accurate model based on empirical observation
would require testing with either human subjects or automated mechanical actuation involving a
mock finger. Human subject testing is inherently time consuming and difficult to control owing
to the variability of human fingers and the difficulty in controlling the level of moisture and the
force applied.(44,45)

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# 189 Materials and methods

### 190 **Replica finger probe**

191 Our approach is thus a hybrid between a tribology experiment which uses a slider with an 192 idealized shape, and one which uses human participants. Namely, we used a silicone rubber cast 193 of a human finger connected to an actuator programmed to deliver and monitor a constant load 194 across an array of micropillars (Fig 2). Designing this realistic finger model was challenging 195 because it required a model with mechanical properties and an epidermal morphology that is 196 similar to an actual finger.(46) One particular challenge arose from the fingerprints. While these 197 ridges may appear to be a loosely periodic train of wavelike crests to the naked eye, the curvature 198 at the top of these ridges varies from ridge to ridge on the same finger and also varies between 199 individuals. Furthermore, examination of fingerprint molds under magnification shows evidence 200 of another order of roughness arising from irregular surface asperities and depressions-i.e., 201 microrelief.(47) These structures fell within the order of 10 µm in all dimensions but were most 202 commonly 5 – 30  $\mu$ m (mean = 12  $\mu$ m,  $\sigma$  = 7.7  $\mu$ m, n = 81) with an apparent exponential 203 distribution, according to image analysis on a SEM image of a representative sample. 204 In order to emulate this behavior with our replica finger probe, we used paraffin wax to

take a mold (negative replica) of our fingerprints and cast the replica using PDMS (Sylgard-184,

206 30:1 base:crosslinker) that has an elastic modulus roughly approximating that of human skin.(48) 207 Collection of participant samples (fingerprints) was done under the supervision of the University 208 of California, San Diego Human Research Protections Program Institutional Review Board under 209 project #191950S. Informed written consent was obtained for collection of participant samples. 210 Upon release of the mold, we subjected the surface of the replica finger to a UV-ozone treatment 211 to make the surface glassy and to reduce the tackiness.(49,50) This material could not however, 212 simulate the extent that lubricated sliding occurs on real fingers due to lubrication from sweat, 213 sebum and other oils, nor does it approximate possible osmotic repulsion due to the electric 214 double layer that forms on the skin in atmosphere.(51) The contribution and variability of these 215 factors in real fingers when compared to a more simplified contact model such as our replica 216 PDMS finger could be an issue to investigate further. Regardless, we assumed that the contact 217 probe we used to simulate interrogatory touch could be modeled as an elliptical region of skin-218 compliant elastomer with roughness imparted by periodic arrays of ridges.

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Fig 2. Summary of the experimental design. (a) Surface of PDMS replica finger with fingerprint ridges molded from human fingers. (b) Overview of geometrical parameters, namely micropillar diameter, aspect ratio and interpillar spacing, that were varied in this experiment. (c) Rendering of replica finger showing the sliding path across substrate carrier. The inset shows example SEM images of the phenomena we refer to as pair-wise, clustering, and matting. A complete schematic drawing of the testing apparatus can be found in the Supplementary Information.

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### 227 **Design of arrays**

228 Our goal was to determine the effects of realistic human touch on the survivability of 229 arrays of polymeric micropillars by varying (1) the geometry of the array and (2) the mechanical 230 properties of the polymer. By subjecting epoxy micropillar arrays of varied elastic modulus, 231 aspect ratio, diameter, and spacing to the shearing movement of a PDMS replica finger, we 232 hypothesized that we could arrive at useful guidelines for survivability across a wide variety of 233 materials. We chose hexagonally arrayed cylindrical micropillars as our representative relief 234 structure due to their analytical utility and equidistant spacing. We chose cylindrical pillars 235 because the corners of, e.g., a square column, might introduce unwanted anisotropy. The 236 simplicity of the circular polar moment allowed for more compact calculations regardless of their 237 orientation with respect to the direction the replica finger traveled across the array. Additionally, 238 there is a wealth of literature involving the mechanics of cylindrical columns due to their use as 239 structural elements throughout history. Hexagonal packing likewise assured that the orientation 240 of the array with respect to the replica finger would have no bearing on its response. A square 241 array, on the other hand, would be expected to have a different frictional response depending on 242 whether the finger moves orthogonally or diagonally across the arrays due to the elements having a distance d vs  $d\sqrt{2}$  separation between them. 243

The arrays were made using standard soft lithographic techniques, with masters made from silicon patterned with SU-8 negative photoresist as the relief structures (S1 Fig of Supplementary Information). From these masters, PDMS molds were made. To fabricate our micropillar arrays, we used Norland Optical Adhesive (NOA), a line of photocurable resins which exhibit a wide range of mechanical properties.(52–54) We selected two products, NOA 73 (E = 11 MPa) and NOA 81 (E = 1379 MPa). We believed that the two orders of magnitude difference in elastic modulus would lead to an appreciable difference in the mechanical response

of the micropillars. For convenience, we will refer to NOA 73 as the E = 10 MPa material and NOA 81 as the E = 1000 MPa material going forward.

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# **Test motion of experimental probe**

255 Our custom-built tribology apparatus (Fig 1 and S2 Fig) used slotted calibration masses to apply 256 a 200 g (1.98 N) constant normal force. A stepper-driven linear actuator (ET-100, Newmark 257 Systems) provided approximately 95 N of axial loading to move our replica finger across the 258 micropillar arrays. A resin-printed replica phalanx ("bone") was suspended in the PDMS mold of 259 the fingertip and provided the means to mount it to a PTFE shaft with a diameter of ca. 10 mm. 260 We initially mounted the replica on an aluminum shaft of similar size but found that metal was 261 too stiff and supported the applied 200 g load so completely that the load failed to push the replica finger into greater contact with the micropillar arrays. A more elastic shaft made of 262 263 PTFE, however, readily deflected under load but was stiff enough to allow the replica finger to 264 be pushed laterally by the stepper motor. Each micropillar array comprised an area of 20 mm 265  $\times$  20 mm, so we decided on a testing surface in which we stamped NOA micropillars upon two 266 adjacent areas to create an array surface that was 20 mm wide by 41 mm long with 1 mm 267 separating the two stamped arrays. This arrangement allowed the mass loading to take place 268 while the replica finger was centered and in contact with the surface of the first die, leaving 269 enough horizontal distance for the replica finger to traverse outside of this initial contact area. 270 The micropillar arrays were stamped onto 2.5 cm  $\times$  7.5 cm glass microscope slides that 271 were mounted in a milled acrylic carrier for testing. This carrier was supported at one end by a 272 tangential force sensor (Futek LSB200 S-beam load cell, 2.5 N capacity) that was mounted to the 273 fixed end of the linear actuator. Micrometer-actuated positioning stages were used to bring both

274 the replica finger as well as the normal force sensor (Honeywell FSG005WNPB, 5 N capacity) 275 into gentle contact with the top and bottom of the test substrate, respectively. After a baselining 276 procedure to ensure that the test surface was level and under approximately the same loading for all samples, the linear actuator drove the replica finger at a velocity of 5 mm s<sup>-1</sup> in the forward 277 278 direction for 17 mm, at which time it would pause for 1 s before moving in the reverse direction 279 for 5 mm. We chose a forward- then backward-traveling test routine because, in the course of 280 experimentally moving our fingers across a mass balance, we observed the spikes in normal 281 force that occur when arresting motion or changing direction (possibly a signal of damage to the 282 micropillar array). These movements seemed natural for human users in the course of handling 283 objects or exploring surfaces.

284

#### 285 **Results and discussion**

## 286 Effect of interrogatory touch on micropillar arrays

287 As intended, our selection of material properties and array geometries allowed us to observe the 288 whole range of predicted behavior: lateral collapse, ground collapse, ploughing of the "finger," 289 and pristine survival. The general trend of survivability vs. deformation that we observed was 290 dominated by the aspect ratio of the micropillars. As shown in Fig 3a, both the 6 µm and the 18 291 μm (Fig 3c-d) micropillars experienced irrecoverable deformation at the 6:1 aspect ratio. The 292 greater compliance of the 6 µm micropillars, however, is clear by their lateral collapse at the 4:1 293 aspect ratio as well. Taken together, these failure modes among the 6 µm and 18 µm 294 micropillars, regardless of elastic modulus, underscore how much the slenderness of relief

structures can modify their stiffness. Our results indicate that this effect is further mediated bythe diameter of these structures.

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**Fig 3. Survivability of tested micropillar arrays.** Panel (a) displays the smallest diameter micropillars (d = 6  $\mu$ m) that were the most prone to deformation and the only diameter to display lateral and ground collapse phenomena at both 4:1 and 6:1 aspect ratios. In contrast, panel (b) shows the outcome for micropillar arrays with the largest diameter (d = 36  $\mu$ m) for both materials. The medium diameter (d = 18  $\mu$ m) micropillars for the more compliant material (E = 10 MPa) are shown in (c) while the medium diameter micropillars composed of the stiffer polymer (E = 10 MPa) are shown in subpanel (d).

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305 We must call attention to the fact that the plots shown in Fig 3 are strictly qualitative; 306 they were constructed by comparing scanning microscope images taken at multiple points along 307 the replica fingers path of travel. These images were taken first at extremely low magnification 308 to determine the extent (or lack) of deformation and then zoomed in to capture clear 309 representations of that behavior for analysis and categorization. Our survivability criterion was 310 based loosely on these microfabricated surfaces remaining functional after this experimental 311 mimic of interrogatory touch and we presumed this should amount to the microcontact interface 312 being preserved. The ploughing condition, therefore, was considered to constitute survival while 313 the instances of lateral collapse and ground collapse failed simply because micropillars thus 314 deformed can lead to a change in contact area, texture, wettability, etc. As far as the occurrence 315 or yield of deformed micropillars required to categorize their survivability, we originally 316 established a criterion that a deformed micropillar was an outlier if there were no similar defects 317 within ten micropillars in any direction. This criterion was seldom used in practice, however,

318 because we observed that deformed micropillars (or evidence of ploughing) tended to be either 319 grouped much closer together or much farther apart. We also wanted our determination of 320 survivability to be robust so we chose to be strict in our assessment of survivability such that 321 failure anywhere in the path of travel was judged as failure for the entire array. Our reasoning for 322 this strict criterion was that we did not want to qualify a given array in an unrealistic fashion 323 such as stipulating that it can survive interrogatory touch provided that it is only touched once 324 without stopping or changing directions. However, the initial contact area was an exception to 325 this criterion due to idiosyncratic manipulations in setting up each sample for testing. That is, the 326 length of time it took to carefully load the 200 g of calibration mass and fine-tune the apparatus 327 to a repeatable baseline led to geometric aging of the contact due to the viscoelastic creep of the 328 PDMS replica finger. Such creep increases the real area of contact of the interface beyond what 329 the remaining travel path experiences, leading to an increased frictional response in that region. 330 The micropillar states shown in the horizontal axis of Fig 3, ranging from ploughing (of 331 the PDMS replica finger) to matting (of micropillars due to lateral and/or ground collapse), 332 encompassed all phenomena we observed and we thought if appropriate to order them left to 333 right by increasing flexibility of the micropillars. Subtle differences in horizontal placement are 334 intended to convey differences in severity and/or extent of deformation and were especially 335 helpful in recognizing trends in the effect of micropillar spacing within the arrays. 336 The effect of spacing is especially evident when comparing micropillar arrays that are too 337 stiff to be deflected by the replica finger, highlighting the importance of how the competition in 338 stiffness between two drastically different material surfaces, in geometry and mechanical 339 properties, leads to a micropillar's survivability or mechanism of failure.. Examining first the 340 higher modulus material with the largest diameter (E = 1000 MPa,  $d = 36 \mu m$ , Fig 3b, shown in

341 blue), we conclude that these parameters both point towards inflexibility of the micropillars 342 regardless of aspect ratio. By comparison, the micropillars composed of the more flexible 343 material generally ploughed less PDMS – a possible indication of deflection and elastic recovery. 344 The stiffer micropillar arrays, however, all appeared to plough PDMS equally except for those 345 with the tightest interpillar spacing ( $s = 1/2d = 18 \,\mu m$ ). This is presumably because these 346 arrays most closely resembled a flat surface and the distance between micropillars was small 347 enough that the fingerprint ridges were afforded less purchase, resulting in the replica finger 348 sliding across the tops of these structures with significantly less mechanical insult.

349 We observed an interesting trend among arrays with the same aspect ratio and material 350 properties but with micropillars half the diameter of those previous ( $d = 18 \mu m$ , Fig 3d). At each 351 of the three shortest aspect ratios, the three different micropillar spacings each exhibited 352 distinguishable behavior but with the same trend in horizontal ordering. As with the case of the 353  $d = 36 \mu m$  micropillars, the arrays with the tightest interpillar spacing were the most pristine. 354 This outcome is possibly the result of a greater top contact area resulting in a lower concentration 355 of stress on any individual micropillar and, overall, less damage to the PDMS "skin." If much of 356 the replica finger was in contact with the micropillar arrays, however, then the arrays with the 357 widest spacing should plough the most PDMS because those micropillars experience the greatest 358 stress locally. This is not the case, however, as Fig 3d shows that the arrays of intermediate 359 spacing alone are capable of severely ploughing the PDMS skin among the arrays with 18 µm 360 diameter micropillars.

361 This apparent discrepancy illustrates how the geometric and material properties combined 362 to determine mechanical response in our experiment. It can be seen in Fig 3b that the more 363 flexible polymer ablated less PDMS in all cases for the 36 µm diameter micropillars, implying

364 that some deflection took place. It is also likely that for all micropillars with the same diameter 365 composed of the stiffer polymer, such deflection occurred only minimally. Except for those 366 arrays with the smallest spacing, the severity of ploughing was indistinguishable. When the 367 diameter was decreased to 18 µm (Fig 3d), however, the degree of ploughing became 368 distinguishable. As the arrays increased in aspect ratio from 2:1 to 3:1, ploughing became 369 markedly more severe (by visual inspection). We suspect that these longer micropillars were able 370 to penetrate deeper into the replica finger; even the most tightly-spaced array abraded the PDMS 371 finger somewhat. When the aspect ratio was increased to 4:1, however, the decrease in bending 372 stiffness was enough that the micropillars were able to deflect slightly and so caused less damage 373 to the replica finger. Among the pillars at these three aspect ratios, greater ploughing could 374 simply be the result of greater micropillar density, until the spacing is tight enough that the 375 replica fingerprint ridges do not penetrate between individual structures. We suspect that stress 376 concentration also plays a role in the extent of ploughing, as the arrays with the least density (s =377 2d) will deflect more and offer less resistance to the replica finger. The spacing of the 378 micropillars thus affects the severity of PDMS ploughing, which we consider to be a state of 379 survival for a microstructured surface and liken it to the way human fingers slough away skin 380 cells when drawn across a rough surface.

Spacing also plays a large role in determining what type of failure occurs when tested arrays do not meet our survivability criteria; namely, the underlying cause of failure is always adhesion, either between pillars (lateral collapse) or between the pillars and substrate (ground collapse). The non-surviving micropillar arrays plotted throughout Fig 3 illustrate how the pairwise variety of lateral collapse generally occurs as simply the predecessor of the more drastic case of lateral collapse, which we called clustering. Pairwise lateral collapse was seen more often

in the tightly-spaced arrays (and more often in the stiffer material) because micropillars that are just slender enough for a slight deflection are able to come into contact with their close neighbors and adhere to them, largely stabilizing both structures from further deflection. In contrast, the matting condition occurred only with the more flexible polymer at higher aspect ratios and the largest interpillar spacing. Such micropillars of comparatively low bending stiffness were then capable of being bent horizontally before coming into contact with their neighbors.

393 The form of lateral collapse known as clustering generally occurred as a more severe case 394 of lateral collapse than the pairwise form, meaning we observed it where greater micropillar 395 deflection could be expected. Unsurprisingly, we found that usually the bidirectional travel of the 396 replica finger facilitated this multidirectional bending behavior. We categorized any clumping-397 together of greater than two micropillars as clustering but often it was seen as a distinct star-398 shaped cluster of seven that results from the hexagonal spacing of the arrays (Fig 4a). This 399 example of a clustering array has the same geometric parameters (6:1 aspect ratio,  $d = 6 \mu m$ , s = 400  $2d = 12 \mu m$ ) as that of the array in Fig 4b showing pairwise lateral collapse. We chose this 401 comparison as a visual example of how, all else equal, the difference in elastic modulus between 402 the two formulations of thiol-ene resin causes a subtle difference in the mechanical response of 403 micropillars but markedly different outcomes as an array.

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Fig 4. Representative SEM images showing the deformation of micropillar arrays. Panel (a) shows an example of "clustering" lateral collapse by the 6  $\mu$ m diameter elements for the compliant (*E* = 10 *MPa*) material. In contrast, panel (b) shows the stiffer material (*E* = 1000 *MPa*) with the same geometry exhibiting pairwise lateral collapse. Both images (a) and (b) were taken in the bidirectional region of the travel path of the replica finger. To illustrate the role that unidirectional versus bidirectional

410 travel can play in the deformation mode of micropillars, images (c) (unidirectional) and (d) (bidirectional)411 are taken from the same sample.

412 In some cases, we observed significant differences in the mechanical response of 413 micropillars at different areas of the same test sample due to the travel path of the replica finger. 414 For instance, Figs 4c and 4d illustrates a micropillar array sample composed of the higher 415 modulus epoxy with 6:1 aspect ratio elements with  $d = 18 \mu m$  and spacing  $s = 2d = 36 \mu m$ . The 416 matting that is shown in Fig 4c occurred in the first array slightly forward from where the replica 417 finger initially makes contact. The pairwise lateral collapse shown in Fig 4d, however, took place 418 at the pivot point in which the replica finger reached the end of its forward travel, paused, and 419 then moved in the reverse direction. This contrast in separate locations of the same test sample is 420 therefore between unidirectional and bidirectional travel, that is, between micropillars that the 421 replica finger has traveled over in one direction vs. those that have been traveled over in both 422 directions. Careful scrutiny of these images, however, reveal pairwise pillars present in Fig 4c 423 and likewise, some pillars we considered matting in Fig 4d. This discrepancy underscores the 424 fact that our categorization of mechanical behavior was subjective. We took great care to 425 determine the dominant failure mode for each micropillar array tested and in most cases the 426 particular type of adhesion was obvious. It was more difficult, however, to sort the relative 427 severity or extent of deformation and such decisions were often a judgment call made after 428 comparing images with those of other test samples exhibiting similar behavior.

Another example of mixed forms of mechanical behavior in the same test sample is evident in Figs 4c and 4d, where micropillars that suffered either lateral or ground collapse were surrounded by pristine micropillars. This phenomenon was extremely common; in nearly all micropillar arrays that we considered non-surviving, pristine micropillars were found throughout

the replica finger's path of travel. These apparently untouched micropillars were the first
indication that, rather than the bulk of our replica fingerprint ridges colliding with these relief
structures, contact between the finger and the micropillar arrays largely occurred between
surface asperities on the surface of the molded fingerprint ridges.

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# 438 **Contact between finger mold and micropillar arrays**

439 Examination of both the paraffin molds, taken from the index fingers of the authors in 440 this study, and the PDMS replica fingers showed an additional length scale of microroughness 441 smaller than that of periodic ridges. We observed these bumps and depressions regardless of the 442 various molding, inking or impression techniques used, and while their distribution appeared to 443 be random, they were noticeably more prevalent as asperities found on ridges (Fig 5). In light of 444 this morphological disorder, we anticipated that our attempt at mimicking real-life interrogatory 445 touch might complicate idealized scenarios where Hertzian or JKR contact mechanics have 446 otherwise been used to good effect. These theories of contact can be used to predict the contact 447 area and indentation of a spherical body into a flat counterbody provided the applied force, 448 radius of indenter and elastic modulus of the bodies are known. In our case, we molded index 449 finger pads that were ellipsoidal and measured ca. 20 mm  $\times$  14 mm for an area of ca. 220 mm<sup>2</sup>. 450 During testing, however, we were only able to obtain a contact area ca. 13 mm  $\times$  8 mm for an 451 apparent contact area of  $\approx 80 \text{ mm}^2$ . This contact area was reached quickly during mass loading 452 and subsequent attempts to increase this area by adding more mass only pushed this existing 453 contact area into the substrate with more force, deflecting the substrate carrier. We noted that the 454 width of our contact area closely matched the width the resin-printed distal phalanx that served 455 as a "replica finger bone" and allowed us to mount the replica finger. While this limitation

underscores the compliance of our testing apparatus, it also reinforces how the presence of a
rigid backing material such as fingernails can greatly affect the apparent contact area.(55)

459 Fig 5. Topology of human finger pads. Panels (a) through (c) are SEM images of a paraffin mold used 460 to cast the PDMS replica finger probes used in this study, shown at sequentially higher magnification. 461 Note that because this mold is a negative image from which the replica finger probe is cast, pits and 462 depressions within the lower regions represent asperities that protrude from the fingerprint ridges of the 463 probe. Panels (d) and (e) are SEM images of a 30:1 PDMS probe at the conclusion of testing. Panel (f) 464 shows profilometry traces of fingerprint molds from two authors to demonstrate the general dimension 465 and variability of human fingerprints where the single ridge rectangular insets are then plotted in (g) with 466 equally scaled axes to convey the true extent of microroughness in contact with the micropillar arrays.

467

468 A similar effect has also been noted by Tomlinson et al., in a study that used real human 469 fingers to measure friction in a variety of materials with milled surfaces.(56) They reported that 470 after applied normal loads of 1 N, the finger seemingly met its limit of compressibility and began 471 to behave as a rigid body. Also of note in that study is that the standard model of Hertzian 472 contact did not fit their experimental data. Among other reasons, the authors speculated that 473 modeling friction in fingers using a sphere in contact with a flat plate does not account for 474 fingerprint ridges – a key feature in our own experiment. As expected, the Hertzian contact 475 model also provided a poor fit to the contact radius and indentation depth that we measured 476 experimentally. Due to the large difference in elastic modulus between 30:1 Sylgard-184 and 477 both of the polymers we studied, we calculated Hertzian contact using reduced elastic modulus, 478 plane-strain modulus, and PDMS modulus alone for a range of 100 kPa - 245 kPa found in the

479 literature.(57,58) The resulting Hertzian contact radius never exceeded less than half of our
480 measured value and indentation depth was even less accurate.

On the other hand, we found agreement between our apparent contact area and the JKR contact model, which takes adhesion into account. Using representative values of surface energy reported elsewhere for UVO-treated PDMS ( $\gamma_{PDMS} = 72 \text{ mJ} m^2$ )(50) and 1% fluorinated thiolene ( $\gamma_{R-SH} = 20.2 \text{ mJ} m^2$ )(59) provided values of JKR contact radius and indention depth within 1 µm of our own averaged values for some geometries. We took this as an encouraging sign that our distribution of normal force in these calculations was acceptable, especially given the assumptions we will elaborate upon shortly.

488 We suspect that contact in our study usually occurred between the micropillar arrays and 489 the curved surfaces at the apex of the fingerprint ridges. These curved ridges are themselves rife 490 with microstructures in the form of asperities that are of similar dimension to micropillars, 491 suggesting asperity-on-asperity contact. Our experimental conditions were then best described as 492 contact between a rough curved surface and a rough flat surface that took place at relatively high 493 force regimes. Fig 5f shows the results of a high-resolution (24 nm per point horizontal travel) 494 stylus profilometry scan over a horizontal range of 1.75 mm in which several consecutive ridges 495 are shown in the approximate center of the replica finger contact area. Although the amplitude of 496 fingerprint ranges varied considerably among co-authors, there was considerable agreement in 497 pitch (ca. 500 µm). Curve-fitting these profilometry scans with equally scaled axes (Fig 5g) 498 allowed us to determine an average radius of curvature for fingerprint ridges of 416 µm. We 499 chose to include micropillars of each diameter and spacing across the x-axis to give a sense of 500 scale between the features of the two contacting surfaces. Note that, although the profilometry 501 traces shown speak to the roughness of fingerprint ridges, the 25 µm stylus tip is of the same

502 order as the asperities evident in the SEM images. This means that even if the profilometry scan 503 were to intersect with one of these random asperities, their profile would be smoothed 504 considerably. We encourage readers who are interested in finger print ridge topology to look at 505 the work of Childs for a 3D profilometry scan that more clearly illustrates the extent of random 506 roughness of human finger pads.(60)

507 In order to measure the contact width of a fingerprint ridge under load, we used 508 fingerprint ink to ink three replica fingers molded from three different subjects and loaded them 509 with the same 200 g mass that we used in the experiment. We made these impressions on both 510 blank glass microscope slides as well as slides containing micropillar arrays and measured the 511 resulting ridge widths with an optical microscope. This allowed us to determine an average 512 fingerprint ridge contact radius,  $r = 107.5 \mu m$  (n = 12,  $\sigma = 30.4 \mu m$ ).

513 To further construct our contact model, we examined several representative replica 514 fingers to determine the best way to model the ridge pattern in order to measure the total length 515 of fingerprint ridges within the apparent contact area. We used computer-aided drafting software 516 to construct a 3D solid model of the simplest representative pattern, featuring a slotted central 517 "whirl" at one end of the contact area with concentric rings radiating outward according to our measured pitch (500  $\mu$ m) and width (2r = 215  $\mu$ m). From this model we summed and averaged 518 519 the inner and outer lengths of these 10 fingerprint ridges, along with the central whirl, to arrive at 520 a total length of 115.5 mm along the central peaks of these ridges. The product of their total 521 length and their width gave us a total area available for contact with the micropillar arrays of 215  $\times 10^{-5}$  m<sup>2</sup> amounting to 26% of the apparent contact area. 522

523 In order to find the number of micropillars, N<sub>m</sub>, in contact with the fingerprint ridges, we 524 first calculated the density, n, of micropillars per unit area according to their diameter and

525 interpillar spacing. We modeled the arrays as hexagonal unit cells with central micropillars so 526 that their density per unit area was simply the inverse of their area, A<sub>hex</sub>:

527 
$$\frac{1}{n} = A_{hex} = \frac{\sqrt{3}}{2} (d+s)^2 m^2$$
(4)

528

where d is the micropillar diameter and s is their spacing (we found it programmatically convenient to reformulate this simple formula in terms of our feature geometry). When we assume top contact, the number of micropillars, N<sub>m</sub>, in contact with the total area of the fingerprint ridges, A<sub>ridges</sub>, is then:

$$N_m = n \times A_{ridges} \tag{5}$$

534

535 For instance, the micropillar arrays shown in Figs 4a and 4b with diameter  $d = 6 \,\mu\text{m}$ 536 and spacing  $s = 2d = 12 \,\mu\text{m}$  have a density n of  $3.56 \times 10^9 \,\text{m}^{-2}$  which gives  $N_m =$ 

537  $8.85 \times 10^5$  microcontacts. On the other hand, an array of micropillars with diameter  $d = 18 \,\mu m$ 

and spacing 
$$s = d = 18 \,\mu m$$
 has a density  $n = 8.9 \times 10^8 \, m^{-2}$  giving  $N_m = 2.21 \times 10^8 \, m^{-2}$ 

539 10<sup>4</sup> microcontacts. We borrowed a straightforward approach that has been applied elsewhere(47)540 and took these contacts as a number of points upon which to distribute the total applied normal541 force in our contact model. The agreement of our contact geometry with that predicted by the542 JKR model thus leads us to believe that this normal force distribution was reasonably accurate.543 Although both approaches are generally applied to stationary contact, the total population of544 asperity junctions is conserved in a multicontact interface under conditions of steady sliding and545 constant normal force.(61)

546 The distribution of tangential force that provided transverse (shear) loading on individual 547 micropillars was a matter of greater difficulty. We assumed that contact with micropillars would 548 occur only with the leading edge of fingerprint ridges and as the replica finger traveled, the 549 contact population would be constantly refreshed as with contacts bearing axial stress. We 550 therefore multiplied the linear length of the modeled fingerprint ridges within our apparent 551 contact area by the linear density of micropillars to arrive at a micropillar population in contact 552 with those ridges. Illustrated details of our contact model geometry can be found in S3 Fig. 553 This manner of modeling a force distribution is a decidedly coarse approach to a matter 554 of considerable complexity, as tangential force and motion in cases such as this generally require 555 examination of friction in a multicontact interface. When such an interface involves a 556 viscoelastic material (such as PDMS or skin), there are additional aspects to be considered such 557 as junction rheology and the dependence of frictional response on velocity of travel and 558 geometric age. While we have attempted to better understand the bending deflection of 559 micropillars in what follows, rubber friction and the contact mechanics of rough on rough 560 surfaces are outside the scope of this study. This is largely because the necessary material 561 properties –e.g. complex modulus,  $E(\omega)$ , of 30:1 PDMS, surface roughness power spectrum, 562 C(q), of the combined elastic half-space– were not available.(62) We, however, wish to 563 encourage interested readers to look at a comprehensive review on the topic of solid friction.(61) 564

#### 565 **Details of contact and deformation**

We were able to measure the total tangential force applied by the linear actuator using a force sensor positioned at the fixed end of the device and opposing the moving stage so that its applied force ( $F_T \approx 95 N$ ) is measured when its forward movement is completely arrested. We likewise have high confidence that the total applied normal force ( $F_N = 2.08 N$ ) was the 200 g of slotted calibration mass in addition to the mass of the replica finger itself ( $\bar{m}_{finger} =$  571 12.4 g, n = 4). The manner in which these total forces were distributed to individual 572 micropillars, however, was uncertain and cannot be assumed purely on a geometric basis due to 573 the randomly rough nature of human finger pads. But due to our inability to observe the interface 574 of replica finger and micropatterned features *in situ*, our quasi-static analysis was based on the 575 simple geometric contact model detailed in the previous section. This quasi-static analysis was, 576 however, explicitly statically indeterminant because we were unable to solve for an equilibrium 577 of moments and forces, i.e., the shape of the elastic line was known but the moments and forces 578 were not(63). Ultimately, our understanding of the mechanics at the scale of individual 579 micropillars was necessarily informed by the deformation observed ex situ through SEM image 580 analysis of micropillar deformation. Because we are able to observe the slope and deflection of 581 micropillars subjected to bending stress, we were able to solve for the inverse problem of likely 582 distributions of normal and tangential force that caused this deformation.

When treating a micropillar as a column with one fixed end and the other end free, it can be modeled as a cantilever beam. When such a beam is subjected to both an axial load and a transverse load simultaneously, it is considered a beam-column(64) and the standard forms of either Timoshenko or the Euler-Bernoulli equations for beam bending do not apply. This is because the axial compression can greatly increase the bending moment at the base of the beam, which in turn affects its slope and deflection. In the case of the beam-column, the deflection, y, of deformed micropillars is given by:(65)(66,67)

591  

$$y = \frac{-W}{kP} \left[ \frac{\sin kl \left[1 - \cos k(l-a)\right] - \cos kl \left[k(l-a) - \sin k(l-a)\right]}{\cos kl} \right] + \frac{W}{kP} \frac{1 - \cos k(l-a)}{\cos kl} \sin kx - \frac{W}{kP} \left[k\langle x - a \rangle - \sin k\langle x - a \rangle\right]$$
(6)

where W is the applied concentrated transverse (tangential) load, P is the applied axial (normal) load, a is the distance from the tip that W is applied, *l* is the length of the beam-column, and  $k = \sqrt{P/EI}$  is a parameter used to factor in the effect of applied normal force and bending stiffness. The expression  $\langle x - a \rangle$  is a unit step function that that is designed such that:

596 
$$\langle x-a\rangle^n = 0 \text{ if } x < a$$

 $\langle x-a\rangle^n = \langle x-a\rangle^n \text{ if } x > a$  (7)

598 
$$(x-a)^n = undefined when x = a$$

599 Although we believe that a distributed load describes more accurately the manner in which 600 tangential force is delivered to the micropillars, the concentrated transverse force equation is 601 more compact. A distributed load can be equivalently expressed as a concentrated load where the 602 integrated area of the distributed force profile is applied at the centroid of the shape of that 603 profile. In choosing to use Equation (6), we were then able to easily experiment with different 604 force profiles by simply varying the *a* parameter. Fig 6a shows a free-body diagram of our beam 605 column model with relevant mechanical parameters and the boundary parameters that are a result 606 of the end constraints.

607

Fig 6. Mechanical analysis of PDMS-micropillar interactions. (a) Free-body diagram with associated moments, reactions, forces and deformation. (b) 3D models of the micropillar cases from Figs 4a and 4b along with deflections and forces to produce those deflections. (c) 3D model showing same for the d = $18 \ \mu m, s = d = 18 \ \mu m, E = 1000 \ MPa$  case. (d-e) SEM images showing the isolated nature of deformation for the case shown in (c).

613

614 We were thus able to conduct analysis of SEM images to determine the deflection, and 615 constructed 3D models of the deformed micropillars so we could view them from various angles 616 (including the 30° tilt angle we used for all SEM images) and refine the accuracy of our

617 observations to account for parallax error. Fig 6b shows 3D models of the micropillars with d =

618 6  $\mu$ m and  $s = 2d = 12 \mu$ m, SEM images of which were shown in Figs 4a and 4b, along with the

619 normal and axial forces that were required to cause the given deflections.

620 In the case of the more compliant polymer system (E = 10 MPa), we found that all of 621 the aspect ratios that we tested experienced a normal force that exceeded the critical force,  $P_{cr}$ , 622 for elastic instability(63,68), namely:

623 
$$P_{cr} = \frac{\pi^2 E I}{4l^2}$$
(8)

624 When such a structure is subjected to an axial load  $P > P_{cr}$ , not only will it fail to return 625 elastically to its original undeformed shape when the external force is removed, but it will be in 626 unstable equilibrium. This means that the equations based on static equilibrium such as (6) are 627 not strictly applicable because equilibrium might be disrupted by an infinitesimal bending of 628 columns subjected to compression from  $P > P_{cr}$ . So not only will such micropillars be prone to 629 large deflection (as already indicated by their much lower elastic modulus), but they will be 630 especially vulnerable to the adhesion phenomena we observed (i.e. clustering, in this particular 631 case).

We therefore posit that our single micropillar mechanical model predicts a much lower force to deflect these lower modulus micropillars simply because their spacing prevents them from bending further. The two micropillar cases shown in Figs 4a and 4b with identical geometric parameters but different elastic moduli were presumed to experience the same magnitude of forces because the images were taken from the same region along the replica finger path of travel. But substituting the forces necessary to deflect the E = 1000 MPa micropillars a distance  $y_a = 9 um$  into (6) at E = 10 MPa yields a non-physical amount of deflection that

we would interpret as ground collapse. But perhaps because they were bent into contact with
their neighboring elements, these more compliant micropillars adhere together into a structural
configuration that was much stronger and therefore proof against further deformation.

642 We ultimately found that micropillars composed of the more compliant polymer were 643 prohibitively sensitive to the manner of combining axial and transverse loading used in (6). We 644 generally used the axial load calculated from our simple contact model because this approach 645 had precedent and agreed well with JKR contact mechanics. When we tried to solve for the 646 transverse loading that would lead to the observed deflection profile, the elastically unstable 647 beam-column would either deflect negligibly or explosively. We suspect this is because the 648 assumption of axial-centric loading in (6) leads to buckling modes without deflection at the free 649 end, reminiscent of classical Euler buckling with maximum deflection at the midpoint of a 650 column.

For the sake of arriving at a solution for combined forces that could have resulted in an endpoint deflection of 13  $\mu m$ , we instead modeled the E = 10 MPa micropillar shown in Fig 6b as if it were obliquely and eccentrically loaded.(69) We chose a resultant force, P, that was directed at an angle  $\alpha = 45^\circ = \pi/4$  from vertical and centered at a point with eccentricity e = $0.5r = 3 \mu m$  radially outward from the centroid of the cross-section. After applying the same boundary conditions as in (6) for a cantilevered beam-column, the deflection has the solution

$$y(x) = [\cot(\alpha) / k] \sin(kx) + [(y_A + e)$$

661 
$$-l \cot(\alpha) ] \cos(kx) + [\cot(\alpha)(l-x) - (y_A + e)]$$
(9)

657

658 where  $y_a$  is the deflection at the free end and *l* is the length of the beam column (as before). In 659 this case, however, the parameter  $k = \sqrt{P \sin \alpha / EI}$  so that only the axial compressive 662 component of the oblique eccentric load is included. This eccentricity adds an additional bending 663 moment while the oblique loading angle combines the axial and transverse loads at the expense 664 of applying the transverse load to the side of the structure. The resulting elastic line, however, 665 showed a smooth bending profile equivalent to what we observed under SEM.

666

## 667 Guidelines for survivability

668 Our experiment was motivated by the hypothesis that there would be a window of 669 diameter, spacing, aspect ratio and elastic modulus that would allow an array of microfabricated 670 structures to survive being touched firmly by people and this window could provide useful 671 guidelines for the rational design of such surfaces. The column plot shown in Fig 7 illustrate the 672 sum of mechanical outcomes for the parameters we tested. We chose to assign the color yellow 673 to the occurrence of ploughing because, although we consider it survival of the micropillar array, 674 it is reasonable to assume there may be applications where the possibility of ploughing is 675 undesirable.

676

Fig 7. Resulting mechanical outcomes for all samples tested. Mechanical outcomes for all E=10 MPa micropillar samples are shown on the left while all E=1000 MPa micropillar results are shown on the right. The legend in the foreground assigns reds of increasing saturation for increasingly severe adhesion/deformation. Green indicates the tested micropillars remained in pristine condition while yellow was chosen for ploughing because micropillars survived despite injurious results for the replica finger.

682

683 The survivability results shown in Fig 7 highlight several trends. The more severe failure
684 modes were seen in the more compliant (E=10 MPa) system while the stiffer (E=1000 MPa)

685 material shows a prevalence of pairwise lateral collapse in pink. The larger population of yellow 686 segments in the stiffer polymer plot illustrates the tendency of those micropillars to resist 687 deformation by ploughing material off of the replica finger while (we suspect) many of the more 688 compliant micropillars of same geometry avoid ploughing owing to elastic deformation and 689 recovery. There is also more variability in the column plot representing micropillars with E=10 690 MPa; this variability reflects the elastic instability of micropillars at the lower modulus. In each plot, 691 the saturation in the red palette increases from top-right to bottom-left showing the trend towards 692 failure as diameter decreases and spacing increases.

693 We intended this study to inform the rational design of micropatterned surfaces that could 694 be handled by human users. Most design decisions involve constraints that recommend a 695 particular attribute in order to grant the best chance of survivability. For example, if an 696 engineering application called for 6:1 micropillars that have a smaller diameter but significant 697 interpillar spacing (e.g.  $d = 6 \ \mu m \ and \ s \le 2d = 12 \ \mu m$ ), a higher modulus polymer with  $E > 12 \ \mu m$ 698 1000MPa would be in order for increased durability and resistance to lateral collapse when 699 handled. If design constraints called for a lower aspect ratio and spacing, but required a larger 700 diameter (e.g.  $d = 18 \,\mu m$ ), then a lower modulus polymer would be the more appropriate choice 701 if the potential for ploughing is to be avoided.

All else equal, lower aspect ratio structures and larger diameters lead to increased survivability. Tighter spacing means a higher micropillars density. Decreased pitch increases the real contact area of the multicontact interface resulting in a decreased local pressure that each micropillar must bear. The tradeoff with tighter spacing is that micropillars then have less room for deflection without coming in contact with, and adhering to, neighboring elements. Because polymers—particularly adhesive resins of relatively high surface energy—were

708 the material of interest in our study, the failure modes were all related to bending deflections

leading to interpillar adhesion. Under a given loading condition, the stiffness, K, of an individualmicropillar,

711 
$$K = \frac{P}{v} = E\frac{A}{l}$$
(10)

712

determines whether that micropillar is capable of bending deflection to a particular distance for interpillar adhesion. This distance is largely dependent on the spacing between the individual elements. In the event that this distance is greater than the length of the micropillar, under a sufficiently high load, that micropillar will continue bending until adhering to the substrate by ground collapse. In any case, with this simple dependency of polymer micropillar failure upon stiffness and spacing, s, optimization should be possible, for example by minimizing the elastic modulus subject to the constraint that the bending deflection,

720

$$y < y_{critical} = s \tag{11}$$

721 This relation is admittedly a first-order approximation, and depends on a reasonably 722 accurate distribution of forces in the system. A more sophisticated formulation was developed by 723 Glassmaker et al. by balancing energies of elastic deformation and adhesion.(32) Glassmaker 724 also offered insight into predicting the transition from doublet to clump formation (which we 725 refer to as pairwise and clustering lateral collapse, respectively) and even successfully predicted 726 the characteristic clump size for their array and element geometry. We must note that their 727 experimental validation consisted of spherical indentation with a smooth glass probe (r =4 mm) at speeds of both 1 and 10  $\mu$ m s<sup>-1</sup> so it did not feature lateral movement or human-scale 728 729 speeds. This type of testing, however, allowed them to make appropriate use of JKR contact 730 mechanics in their model and avoid many complications inherent in the sliding of rough on 731 rough surfaces. We therefore believe that the JKR contact model has limited applicability in our

own experiment for reasons which we have already detailed as well as the observation that
deformation we observed was not particularly confined to the center of the contact radius (where
JKR dictates pressure is maximum) as it was in their scenario.

735

# 736 **Conclusions**

737 Experiments in contact mechanics generally take place in idealized conditions using 738 lower than human-scale forces that are often necessary to reveal subtle adhesion phenomena. 739 Studies in friction largely take place at lower than human-scale velocities to avoid temperature 740 effects. Both disciplines tend to constrain their experiments in this way to increase precision and 741 limit sources of error. Our experiment illustrates that a motion as simple as sliding a finger 742 across an engineered textured surface can be complicated to understand quantitatively, especially 743 if it cannot be observed in situ and with fully characterized materials and an expensive 744 sophisticated test apparatus. Our intent was to mimic interrogatory touch in sliding forward, 745 pausing and sliding backways across a micropattened surface in a manner that is inconvenient for 746 isolating physical phenomena but represents a realistic occurrence if such surfaces engage the 747 curiosity of primates.

We have determined that for the two polymers we chose study, failure occurred entirely due to adhesion via lateral collapse or ground collapse. For two of the diameters we tested,  $d = 6 \mu m$  and  $d = 18 \mu m$ , this failure took place at an aspect ratio of 6:1 due to the gradual decrease in bending stiffness as length increases. At equal aspect ratios, a larger cross-sectional area grants an increased chance of survivability. In light of this fact, we therefore suspect that survivability at the 6:1 aspect ratio may begin at or around  $d = 36 \mu m$  due to the absence of

deformation for those diameter arrays at 4:1. Unfortunately, we were unable to realizefabrication of those arrays so this prediction cannot be confirmed.

Because the failure mechanisms are driven by competition between elastic restoring force and adhesion/surface energy, the question of whether adhesion can be mitigated would be an enriching topic of future work. In haptics, the potential to make adhesion and thus, changes in texture arising from lateral/ground collapse, reversible would open up a wide range of applications and commercial potential.

761 When the replica finger we used in this study was stationary, as during loading prior to 762 movement and during the one second pause between sliding forward and in reverse, 763 understanding was largely a problem of viscoelastic contact mechanics between rough on rough 764 surfaces. While the finger was in motion, the scenario was one of rubber friction in a system that 765 was likely overdamped by finite device stiffness. We have posited a model employing the 766 mechanics of cantilevered beam-columns in order to predict the mechanical response of 767 micropillars being deflected towards failure by adhesion. Future work is needed to quantitatively 768 understand the interaction of human fingers with micropatterned surfaces, and great care should 769 be taken to select materials that are highly characterized, especially the viscoelastic material 770 chosen to mimic skin. Human fingertip mechanical properties are also highly influenced by skin 771 hydration(70) and while this would require further environmental controls, it would be insightful 772 to investigate the effects of lubrication at the interface.

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993	Sup	oporting Information
994	S2 A	ppendix. Micropillar Array Fabrication Process. Details included for each process step.
995		
996	S2 F	igure: Experimental apparatus setup. (a) Solid model of test apparatus with annotation of
997	key f	features. Inset shows replica finger on drive shaft with tangential and normal force sensors.
998	(b) P	hotograph of test apparatus with inset showing approximate position of replica finger prior
999	to co	ntact with substrate and mass loading.
1000		
1001	S3 F	igure. Contact model geometry. (a) Our determination of indentation depth from measured
1002	quan	tities for average fingerprint ridge radius and average fingerprint ridge width. (b) Solid
1003	mod	eling using Autodesk Fusion 360 allowed us to sum the lengths of fingerprint ridges and to
1004	solve	e for total fingerprint ridge area for the simple representative geometry shown. (c)
1005	Micr	opillar density is the inverse of the area of a hexagonal unit cell, a function of diameter and

spacing. We were then able to solve for the total number of microcontacts as product of totalfingerprint ridge area and micropillar density.

1009	S4 Figure. Location of transverse load, W. Transverse load W is applied across span of length
1010	a where a is determined by the lessor value of spacing or indentation depth. The inset showing
1011	forces applied to a deflecting micropillar are simplified for clarity. In our calculations, the actual
1012	distance of a concentrated transverse load W is a/2 from the free end to approximate a distributed
1013	load with rectangular profile applied along length a.
1014	
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1015	S5 Appendix. Additional Error Analysis on Contact Model Calculations.
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1017	S6 Appendix. Finite Element Analysis.
1018	