

Zintl Phase Compounds $Mg_3Sb_{2-x}Bi_x$ (x = 0, 1, and 2) Monolayers: Electronic, Phonon and Thermoelectric Properties From ab Initio Calculations

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The Mg₃Sb_{2-x}Bi_x family has emerged as the potential candidates for thermoelectric applications due to their ultra-low lattice thermal conductivity (κ_l) at room temperature (RT) and structural complexity. Here, using ab initio calculations of the electron-phonon averaged (EPA) approximation coupled with Boltzmann transport equation (BTE), we have studied electronic, phonon and thermoelectric properties of Mg₃Sb_{2-x}Bi_x (x = 0, 1, and 2) monolayers. In violation of common mass-trend expectations, increasing Bi element content with heavier Zintl phase compounds yields an abnormal change in κ_l in twodimensional Mg₃Sb_{2-x}Bi_x crystals at RT (~0.51, 1.86, and 0.25 W/mK for Mg₃Sb₂, Mg₃SbBi, and Mg₃Bi₂). The κ_L trend was detailedly analyzed via the phonon heat capacity, group velocity and lifetime parameters. Based on quantitative electronic band structures, the electronic bonding through the crystal orbital Hamilton population (COHP) and electron local function analysis we reveal the underlying mechanism for the semiconductor-semimetallic transition of Mg₃Sb_{2--x}Bi_x compounds, and these electronic transport properties (Seebeck coefficient, electrical conductivity, and electronic thermal conductivity) were calculated. We demonstrate that the highest dimensionless figure of merit ZT of Mg₃Sb_{2-x}Bi_x compounds with increasing Bi content can reach ~1.6, 0.2, and 0.6 at 700 K, respectively. Our results can indicate that replacing heavier anion element in Zintl phase Mg₃Sb_{2-x}Bi_x materials go beyond common expectations (a heavier atom always lead to a lower κ_L from Slack's theory), which provide a novel insight for regulating thermoelectric performance without restricting conventional heavy atomic mass approach.

Keywords: two-dimensional zintl phase compounds, phonon thermal transport, thermoelectric performance, electron-phonon averaged approximation, Boltzmann transport equation

INTRODUCTION

The term Zintl phase was firstly proposed by F. Laves (Kauzlarich et al., 2007; Kauzlarich et al., 2016), as a German scientist, indicating a collection of materials within the general class of intermetallics, and the compounds can be understood by a formal electron transfer from a positively-charged metal to a negativelycharged element. In particular, the rich chemistry and evolution of structural complexity of Zintl phase compounds become a series of promising thermoelectric (TE) materials because of their "phonon-glass electron-crystal (PGEC)" (Shuai et al., 2017; Rowe, 2018) structures. The ideal concept presents that a highperformance TE material should have an excellent electrical conductivity of crystals, but also have a higher phononscattering rate like glass, where the cation region act as "phonon-glass" and the anion region play as "electron crystal" to alter phonon thermal and electrical transport properties. More interestingly, the structural complexity of Zintl phase compounds is mainly manifested in the diversity of anionic frameworks composed of internal covalent bonds, and the anionic framework can be roughly divided into zero-dimensional (0D) cluster, one-dimensional (1D) chain, two-dimensional (2D) planar, and complex three-dimensional (3D) network structures in accordance with the spatial extension. The 0D cluster structures include Sr₃AlSb₃ (Zevalkink et al., 2013) and Yb₁₄MnSb₁₁ (Brown et al., 2006), and Yb₁₄MnSb₁₁ in the high temperature region can reach 1, in which the maximum Seebeck coefficient of Sr₃AlSb₃ is 500 μ V K⁻¹ in the medium temperature region. Herein, the figure of merit defined as ZT $(ZT = \sigma S^2 T / (\kappa_e + \kappa_L))$, where σ stands for the electrical conductivity, S represents the Seebeck coefficient, and T is the Kelvin temperature. κ_e and κ_L are the electronic and the lattice thermal conductivities, respectively. Next, Sr3GaSb3 (Zevalkink et al., 2012) and $A_5Sn_2As_6$ (A = Sr and Eu) (Wang et al., 2012) represent the 1D chain structures, where the maximum ZT of Sr₃TGaSb₃ at 1000 K can exceed 0.9 by doping with Zn element. Meanwhile, the 2D planar structures incorporate $BaGa_2Pn_2$ (A = P, As) (He et al., 2010) and YbGd₂Sb₂ (Xia and Bobev, 2007). The representative of the 3D network structures is skutterudite (CoSb3) (Shi et al., 2005; Liu et al., 2020), which is a nearideal "PGEC" with the higher S (200 μ V K⁻¹) and power factor (σS^2) (30 µW cm⁻¹ K⁻¹), while the higher lattice thermal conductivity would suppress its TE performance.

Recently, the $Mg_3Sb_{2-x}Bi_x$ compounds have become one of the most widely studied TE materials owing to their abundant and inexpensive constituent elements. Experimental measurements and theoretical calculations suggested that the ZT of Mg₃Sb₂ can reach 1 in the high temperature region, and it has simple synthesis, a high melting point, and excellent mechanical stability (Ohno et al., 2018; Shi et al., 2018). It is worth noting that $Mg_3(SbBi)_2$ alloys would reduce the effective mass of Mg_3Sb_2 and further help to increase the carrier mobility (Imasato et al., 2018). Meanwhile, it was reported that increasing the Bi content in N-type Mg₃Sb_{2-r}Bi_r compounds can significantly improve the low-temperature ZT value (Imasato et al., 2018; Shu et al., 2019), which is even comparable to N-type Bi2Te3. However, it was designed and shown that а ZTof 1.85 for

 $Mg_{3.195}Mn_{0.05}Sb_{1.5}Bi_{0.49}Te_{0.01}$ at 723 K can reach 1.85 (Chen et al., 2018), which is still lower than that of a class of superior TE materials such as SnSe (~2.8 at 773 K) (Zhao et al., 2014; Zhao et al., 2016; Chang et al., 2018). The above studies mainly focus on the TE transport properties of 3D Zintl phase Mg₃Sb_{2-x}Bi_x (x = 0, 1, and 2) family. According to the 2D quantum confinement effect (Hicks and Dresselhaus, 1993; Zeng et al., 2018), we know that decreasing dimension in 3D materials can not only reduce the κ_I but also avoid appearing the poor TE performance in some crystalline orientations. The previous work suggested that the ZT value of 2D Mg₃Sb₂ can increase to 2.5 at 900 K, and the near record-high value is larger than that of 3D structure (Huang et al., 2019). The TE performance of 3D Zintl phase $Mg_3Sb_{2-x}Bi_x$ compounds, as a typical layered TE materials family, may be further enhanced through the dimensionality reduction approach. Yet, few 2D Zintl phase Mg₃Sb_{2-x}Bi_x compounds have been studied, and it is necessary to further explore the behind mechanism for the excellent TE performance.

In this work, we performed the first-principles calculations combining with the BTE and the EPA approximation (as a more predictive approach than the deformation potential approximation method) (Samsonidze and Kozinsky, 2018) to systematically calculate and detailedly analyze the phonon thermal and TE transport properties of 2D Mg₃Sb_{2-x}Bi_x within a wide range of temperature. It is found that, through our theoretical calculations, 2D Mg₃Sb_{2-x}Bi_x (x = 0, 1, and 2) $\begin{array}{ll} \text{compounds} & \text{possess} & \text{an} & \text{abnormal} & \kappa_L & \text{trend} \\ (\kappa_L^{Mg_3SbBi} > \kappa_L^{Mg_3Sb_2} > \kappa_L^{Mg_3Bi_2}), \text{ which violates the common theory} \end{array}$ (Heavier atomic mass in similar materials usually corresponds to lower κ_L). We elucidate the reason why this anomaly occurs in 2D $Mg_3Sb_{2-x}Bi_x$ structures by quantitatively comparing the phonon heat capacity, the phonon group velocities, the phonon lifetime, the anharmonicity, the transferred and shared charge, and the characteristics of bonds. Meanwhile, we further calculated the electrical transport properties in 2D Mg₃Sb_{2-x}Bi_x including the σ , S, κ_e , and TE performance as a function of chemical potential with respect to the Fermi energy under different temperatures. Our results will provide a theoretical basis for accelerating TE application of 2D Zintl phase materials and pave a new way for predicting and exploring the ultra-high TE performance in PGEC family materials.

Computational Details

The phonon thermal and electrical transport properties have been calculated by the plane-wave pseudopotential approach within the density functional theory (DFT) (Hohenberg and Kohn, 1964), which is employed in the Vienna Ab-initio Simulation Package (VASP) (Kresse and Furthmüller, 1996) software along with projector augmented-wave (PAW) potential (Bliichl, 1994). To ensure the good convergence of electrons and ions during structural optimizations, the plane-wave cutoff energy of the 2D Mg₃Sb_{2-x}Bi_x compounds was set as 500 eV, and a Monkhorst-Pack *k*-point grid of 15 × 15 × 1 was used to ensure accurate calculation. A Hellmann-Feynman force convergence threshold of 10^{-4} eV A⁻¹ was adopted, and the energy convergence threshold between the two steps was set to be 10^{-6} eV. To avoid the effect of the interaction between adjacent layers, 2D



Mg₃Sb_{2-x}Bi_x unit cells were added a 20 Å thickness of vacuum slab along the out-of-plane direction. We next calculated the electronic band structures using the Perdew, Burke, and Ernzerhof (PBE) functional (Perdew et al., 1996) and the hybrid Heyd-Scuseria-Ernzerhof (HSE06) functional (Paier et al., 2006), and different functionals are designed to obtain accurate band results for 2D Mg₃Sb_{2-x}Bi_x materials. The κ_L is computed by solving the linearized BTE as implemented in ShengBTE software (Li et al., 2014), then considering Born effective charges and dielectric constants effect in the selected compounds. Meanwhile, electronic transport coefficients are calculated exactly by solving semi-classical BTE within the EPA approximation (fully first-principles computations of electron-phonon interactions) as described detailedly (see Supplementary material) in the excellent work (Samsonidze and Kozinsky, 2018).

RESULTS AND DISCUSSIONS

Herein, 2D Mg₃Sb_{2-x}Bi_x (x = 0, 1, and 2) compounds belong to a typical hexagonal structure with the space group P3m1 (No. 156) which is made up of the cationic layer of Mg²⁺ and the anionic layer of $[Mg_2(Sb_{2-x}Bi_x)]^{2-}$ as shown in Figure 1. It has been found that the bonds between ionic Mg²⁺ layers and covalent $[Mg_2(Sb_{2-x}Bi_x)]^{2-}$ layers can be broken to produce a corresponding 2D materials (Gorai et al., 2016; Zhang et al., 2018). Figures 1A, B represents schematic illustration of 2D $Mg_3Sb_{2-x}Bi_x$ (x = 0, 1, and 2), and their calculated lattice constants within the PBE-level are 4.736 Å, 4.794 Å, and 4.843 Å, respectively, which are close to the lattice parameters for corresponding 3D Mg₃Sb₂ (4.573 Å) (Huang et al., 2019) and 3D Mg₃Bi₂ (4.666 Å) (Zhang and Iversen, 2019). Meanwhile, during the structural relaxation of 2D Mg₃Sb_{2-x}Bi_x, we did not consider the too weak van der Waals effect, which has been reported and investigated in previous work (Zhang et al., 2018). Meanwhile, we also present the first Brillouin zone path (Γ-M-K-

Γ) with high-symmetry points, named Γ (0, 0, 0), M (1/2, 0, 0), and K (1/3, 1/3, 0), as illustrated in **Figure 1C**. It is obviously seen that two cases of Mg atoms exist in the primitive cell of 2D Mg₃Sb_{2-x}Bi_x, named by Mg1 and Mg2 (see the inset of the **Figures 2B, D, F**. Interestingly, between Mg and Sb atoms interactions caused by the corresponding electrical properties has been confirmed, which can occur in a Mg-Sb bonding interaction for the all Mg1 and Mg2 cases in N-type doping Mg₃Sb₂ (Sun et al., 2019). Therefore, it should be noted that the bonding characteristic in 2D Mg₃Sb_{2-x}Bi_x compounds may directly determine their electronic and phononic structures and thus play a crucial role in the calculations of TE properties.

The 2D Mg₃Sb_{2-x}Bi_x family has five atoms in the primitive cell, and the corresponding phonon dispersion curves and phonon harmonicity results are depicted in Figure 2. We found that the above compounds have not imaginary vibrational frequency in the phonon dispersion curves, indicating the dynamic stability of the 2D Mg₃Sb_{2-x}Bi_x compounds in this study (Chang et al., 2021). Meanwhile, it can be seen from Figure 2 that the mixing of acoustic phonons and low-frequency optical phonons exist a stronger phonon scattering processes, which indicates a lower κ_L in these materials. From Figures 2A, C, F, it can be clearly observed that the region of colored phonon band-gap (Significant dispersion in the high-frequency optical phonons) are gradually decreased with increasing Bi atom content, and these optical phonons in the current compounds holds non-zero phonon group velocities and then has a certain contribution to phonon heat transport. We further track the phenomenon by comparing atom-projected phonon DOS of the Mg, Sb, and Bi atoms in these related compounds, as depicted in Figures 2A, C, E. The total phonon DOS of Mg₃Sb₂ and Mg₃SbBi monolayers decomposes into two separate regions: Mg-site mainly dominated between 6 and 9 THz, and Sb/Bi-sites mainly dominated below ~3 THz. Surprisingly, for Mg₃Bi₂ monolayer, the total phonon DOS decomposes into three separate regions: Mg1-site mainly dominated between 6 and 8 THz, Mg2-site mainly dominated between 2 and five THz, and Bi-sites mainly dominated below



~2 THz. The above results show that all of phonon vibration frequencies would be more compressed with increasing Bi atomic mass, which benefits for becoming high-performance TE materials, while it is not enough to explain the anomalous κ_L changes in 2D Mg₃Sb_{2-x}Bi_x compounds by the increased Bi atomic mass. Therefore, it is urgent to study the interatomic force constants (IFCs) effect in Mg₃Sb_{2-x}Bi_x family, which can directly determine phonon heat conduction behavior.

Figures 2B, D, F show the presence of long-ranged interaction among these compounds, and to further compare and analyze the IFCs between Mg atom and Sb/Bi atoms, traces of IFC tensors are normalized by the trace values of the self-interacting IFC tensor in the above compounds. For instance, second-nearest neighbours, separated by ~4 Å (including Mg1-Sb1, Mg1-Sb2, and Mg1-Mg2, etc.,), have interactions that are comparable to those of tenth-nearest neighbours, spaced ~9 Å apart, and much weaker than first-neighbours interactions in **Figure 2B**. Clearly, there are very similar phenomenon for normalized trace of IFC in 2D Mg₃SbBi and Mg₃Bi₂ structures, excepting for the reduced distances at same nearest neighbours cases by the increased Bi content. Herein, we calculate the IFC tensor on the basis of first-principles calculations as follow (Lee et al., 2014; Li et al., 2020a; Li et al., 2020b):

$$\frac{\partial^{2} E}{\partial R_{I} \partial R_{J}} = \begin{bmatrix} \frac{\partial^{2} E}{\partial R_{x} \partial R_{x}} & \frac{\partial^{2} E}{\partial R_{x} \partial R_{y}} & \frac{\partial^{2} E}{\partial R_{x} \partial R_{z}} \\ \frac{\partial^{2} E}{\partial R_{y} \partial R_{x}} & \frac{\partial^{2} E}{\partial R_{y} \partial R_{y}} & \frac{\partial^{2} E}{\partial R_{y} \partial R_{z}} \\ \frac{\partial^{2} E}{\partial R_{z} \partial R_{x}} & \frac{\partial^{2} E}{\partial R_{z} \partial R_{y}} & \frac{\partial^{2} E}{\partial R_{z} \partial R_{z}} \end{bmatrix},$$
(1)

where *E* and R_{α} represent energy and atomic position along α direction, respectively. By computing the trace of IFC tensors, we



FIGURE 3 | (A) Calculated κ_L of 2D Mg₃Sb_{2-x}Bi_x with respect to the temperature ranging from 300 to 800 K. (B) Cumulative κ_L of these compounds and their derivatives versus phonon frequency at 300 K. (C) Calculated changes of phonon heat capacity of the above compounds as a function of temperature. The phonon frequency-dependent behavior of (D) the phonon group velocities, (E) phonon lifetime, (F) phonon scattering phase space, and (G) Grüneisen parameters in 2D Mg₃Sb_{2-x}Bi_x.

can assess bonding stiffness regardless of crystal structure or coordinate system:

Trace of IFC =
$$\frac{\partial^2 E}{\partial R_x \partial R_x} + \frac{\partial^2 E}{\partial R_y \partial R_y} + \frac{\partial^2 E}{\partial R_z \partial R_z}$$
, (2)

Finally, the normalization is calculated by the trace value of self-interaction force constants:

Normalized trace of IFC =
$$\frac{\frac{\partial^2 E}{\partial R_{0,x} \partial R_{n,x}} + \frac{\partial^2 E}{\partial R_{0,y} \partial R_{n,y}} + \frac{\partial^2 E}{\partial R_{0,z} \partial R_{n,z}}}{\frac{\partial^2 E}{\partial R_{0,x} \partial R_{0,x}} + \frac{\partial^2 E}{\partial R_{0,y} \partial R_{0,y}} + \frac{\partial^2 E}{\partial R_{0,z} \partial R_{0,z}}}.$$
(3)

In addition, to describe accurately the related IFCs in the calculation of κ_L , we choose a cutoff distance of the tenth-nearest neighbor in 2D Mg₃Sb_{2-x}Bi_x family. We need to point out that

Mg1 atom exists at the octahedral site surrounded by 6 corresponding atoms, which would provide 2 electrons to the $[Mg_2(Sb_{2-x}Bi_x)]^{2-}$ network, while Mg2 atom exists at the tetrahedral site surrounded by 4 corresponding atoms. In terms of its configuration, a detailed chemical bonding analysis of 3D Mg₃Sb₂ has been reported that the two different Mg atom sites present a similar bonding character responding to the transferred charges of +1.51 and +1.47, respectively (Zhang et al., 2019), and exists dominantly ionic bonds with partial covalent bonds in 3D Mg₃Sb₂ system (Zhang et al., 2018). These results offers a rational explanation of the relation to phonon heat conduction properties of 3D Mg₃Sb_{2-r}Bi_r family. To deeply understand bonding character and quantify the bond hierarchy strengths of a pair of atoms in 2D Mg₃Sb_{2-r}Bi_r compounds, we next compute and analyze the transferred and shared charges and COHP along with integrated "-COHP" (ICOHP) for the nearest-neighbor atom in the following section.

Based on the more accurate second- and third-order IFCs from the normalized trace of IFC data, we firstly calculate the κ_L of the selected three Zintl-phase compounds as shown in Figure 3A. Each material would demonstrate roughly the common $\kappa_L \sim 1/T$ behavior. Meanwhile, it is well known that the calculation of κ_L is more sensitive to the selection of *q*-mesh grids, and we set a *q*-mesh grid of $100 \times 100 \times 1$ to solve phonon BTE and then obtain the convergence of κ_L . Because of the symmetry of 2D Mg₃Sb_{2-x}Bi_x, the κ_L along two in-plane directions shows isotropy, so only a value are depicted. As seen from Figure 3A, 2D Mg₃SbBi alloy holds a higher lattice thermal conductivity, while its average atomic mass is between those of 2D Mg₃Sb₂ and 2D Mg₃Bi₂. For instance, our calculated κ_L of Mg₃Sb₂, Mg₃SbBi, and Mg₃Bi₂ monolayers at 300 K are 0.51, 1.86, and 0.25 W/mK, respectively, which may originate from a smaller displacement and the mass difference (related to bonding strength) caused by a heavier atom (Li and Mingo, 2014; Yang et al., 2020). As presented in the inset of Figure 3A, we further study the κ_L changes between the relaxation time approximation (RTA) and the iteratively solving (ITE) methods among the three materials, and the RTA results are below the ITE data, indicating the main function of the Umklapp processes in phonon heat conduction behavior. To deeply understand the behind mechanism of the intriguing phenomena, we perform a detailed analysis on phonon frequency-dependent cumulative κ_L , decomposing κ_L to three separate parts (phonon heat capacity, group velocity, and phonon lifetime), and phonon anharmonicity information, as presented in Figures 3B-G.

Obviously, with the increase of cumulative κ_L can become negligible above a frequency value of ~2 THz among the three 2D Zintl phase compounds, suggesting the major contribution of the lower optical and acoustic phonons to κ_L (Figure 2). What we need to notice is that 2D Mg₃SbBi and 2D Mg₃Bi₂ exist two relatively small shape areas (blue and red marked) between 6 and 8 THz, because the higher optical phonons would be compressed and then benefit three-phonon scattering processes. To further check the contribution of all phonons vibrations to the calculated κ_L , the phonon heat capacity (C_ν) of among 2D Mg₃Sb₂, 2D Mg₃SbBi and 2D Mg₃Bi₂ with respect to temperature were obtained and illustrated in Figure 3B, which agree well with the previous experimental data by using the PPMS measurement (Xin et al., 2018). The C_{ν} (obeying $\kappa_L \propto C_{\nu}$) of these compounds at temperatures within the range of 400-800 K are very close (~122 J/K mol) to each other for all the three materials, and obey the classical limit of Dulong-Petit law (Fitzgerel and Verhoek, 1960) as shown in the inset of Figure 3C. Therefore, these tiny difference in C_{ν} are not the primary cause of the anomalous κ_L trend in 2D Mg₃Sb_{2-x}Bi_x systems. For three compounds, the phonon group velocity (v_{σ}) as a function of frequency is plotted in Figure 3D, and it can be seen that the group velocity of 2D Mg₃Sb₂ is higher than that of 2D Mg₃Bi₂, closing to that of 2D Mg₃SbBi in the cutoff frequency below 1.5 THz, which suggests the calculated κ_L of 2D Mg₃Sb₂ and 2D Mg₃SbBi might be roughly close (following the rule $\kappa_L \propto \nu_{\alpha}$). On average level, we show that the average group velocities of 2D Mg₃Sb_{2-x}Bi_x are 0.43, 0.39, and 0.32 km/s, respectively. However, it is clearly observed in Figure 3D that the three v_g data exist similar distribution, excepting for having the significant differences (the non-negligible velocities for Mg₃SbBi) around a frequency ranging between 6.5 and 8 THz, while the changes are consistent with the above the slope of phonon dispersion curves.

Interestingly, none of the C_{ν} and the ν_g can explain the relatively higher κ_L of 2D Mg₃SbBi compared to 2D Mg₃Sb₂ systems. Therefore, we can conclude that the abnormal κ_L trends in the three materials must lie in the unusual phonon lifetimes (τ) as plotted in Figure 3E. The calculated τ of 2D Mg₃SbBi were considerably larger than those of the other two materials in the lower- (0-2 THz) and higher-frequency (6-8 THz) regions, which might be because of the suppressed three-phonon scattering processes in 2D Mg₃SbBi, caused by the alloying (a mass difference occurring in [Mg₂(SbBi)]²⁻). Obviously, these variation trends of the τ in Mg₃Sb_{2-x}Bi_x were consistent with the cumulative κ_L results as seen in Figure 3B. In the light of the theory of lattice dynamics, the calculated τ is strongly dependent on three-phonon scattering phase space (P_3) and Grüneisen parameter (γ), as presented in Figures 3F, G. Herein, the P_3 is defined as (Lindsay and Broido, 2008; Peng et al., 2016; Yang et al., 2020):

$$P_{3} = \frac{2}{3\Theta} \left(P_{3}^{+} + \frac{1}{2} P_{3}^{-} \right), \tag{4}$$

$$P_{3}^{\pm} = \sum_{\lambda} \int d\boldsymbol{q} D_{\lambda}^{\pm}(\boldsymbol{q}), \qquad (5)$$

$$D_{\lambda}^{\pm}(\boldsymbol{q}) = \sum_{\lambda'\lambda''} \int d\boldsymbol{q}' \delta(\omega_{\lambda}(\boldsymbol{q}) \pm \omega_{\lambda'}(\boldsymbol{q}') - \omega_{\lambda''}(\boldsymbol{q} \pm \boldsymbol{q}'' - \boldsymbol{G})),$$
(6)

where Θ represents a normalization factor, $D_{\lambda}^{\pm}(\boldsymbol{q})$ represents two types of three-phonon scattering channels, and it is also the two phonon DOS and momentum conservation were imposed on \boldsymbol{q}'' (Okubo and Tamura, 1983). From **Figure 3F**, it is shown that the P_3 of 2D Mg₃SbBi is smaller than these of the other two compounds in the entire phonon frequency ranges, which suggests that phonons in 2D Mg₃SbBi have less phonon scattering channels, leading to relatively larger τ (**Figure 3E**) compared to 2D Mg₃Sb₂ and 2D Mg₃Bi₂ materials. The other important factor that the number of phonons scattering



Reconstruction (LOBSTER) program (Maintz et al., 2016).

channels determined exists the strength of phonon anharmonicity, quantitatively described by the γ , which characterizes how many phonon frequencies vary with the crystal volume. As revealed in the inset of **Figure 3G**, the calculated total γ for 2D Mg₃SbBi is ~ -4.0, which is lower than that of 2D Mg₃Sb₂ (γ = ~ -2.1) and 2D Mg₃Bi₂ (γ = ~ 2.2) at the temperature ranging from 300 to 800 K. Consequently, anomalously increase of the κ_L from 2D Mg₃Sb₂, 2D Mg₃SbBi, and 2D Mg₃Bi₂ has been demonstrated by breaking up into the relative contribution of the C_{ν} , ν_g , and τ as discussed above.

It is well known that the superior TE performance in a material results from an intrinsic ultra-low κ_L , from the above phonon heat conduction results, and it is very necessary to confirm the potential TE transport properties from 2D Mg₃Sb₂ to 2D Mg₃Bi₂. We firstly calculated the electronic band structures in 2D Mg₃Sb_{2-x}Bi_x using the two function potentials as plotted in **Figures 4A–C**, which can directly explain the reason for the high TE performance of a material. Since Sb and Bi atoms possessed the same outermost valence electrons (including 3*p* and 2*s*), the slope of these band structures would be very similar. Meanwhile, the calculated band-gaps with PBE and HSE06 potentials are 0.17 and 0.56 eV for 2D Mg₃Sb₂.

Therefore, to obtain more accurate values, we carried out the HSE06 to correct the band structures, and a negative band-gap was occurred in 2D Mg₃Bi₂ (Figure 4C). In addition, we found that the valence band maximum is located at Γ point for all of the selected compounds, due to the domination of Mg-Sb/Bi bonding interactions (Sun et al., 2019; Wood et al., 2020), while location of the conduction band minimum are between Γ and M paths, the same Γ point, and around Γ point for 2D Mg₃Sb₂, 2D Mg₃SbBi, and 2D Mg₃Bi₂, respectively. To further characterize and explore the behind mechanism of chemicalbonding properties in 2D Mg₃Sb_{2-x}Bi_x, we also calculated the ELF and COHP with integrated pCOHP (-pCOHP) as plotted in Figures 4D-I. Meanwhile, three ELF values of 0, 0.5, and 1.0 reflect non-localized electrons (none-charge density), completely delocalized electrons (electron gas-like pair phenomenon), and fully localized electrons (the occurrence probability of the electrons), respectively (Silvi and Savin, 1994; Yue et al., 2017; Wu et al., 2020). It can be clearly seen that the value of the ELF between Mg atoms and Sb/Bi atoms gradually decrease with increasing Bi element in 2D Mg₃Sb_{2-r}Bi_r systems, suggesting a weaker covalent bond in 2D Mg₃Bi₂ and then proved its semimetallic feature. The lower value of ELF in Mg3Bi2 monolayer also confirms the weaker and lower shared charges as listed in

Materials	Transferred charge	Shared charge	Transferred charge of each element		
			Mg1-site	Mg2-site	Sb/Bi-sites
Mg ₃ Sb ₂	0.76	0.92	0.93	0.80 (0.91)	-1.47 (-1.17)
Mg ₃ SbBi	0.88	0.92	0.86	0.79 (0.90)	-1.17 (-1.38)
Mg ₃ Bi ₂	0.85	0.89	0.84	0.68 (0.72)	-1.34 (-0.86)

TABLE 1 | Comparison of transferred and shared charges (|e|) and the corresponding transferred charge (|e|) of each element in 2D Mg₃Sb₂, (h) 2D Mg₃SbBi, and (i) 2D Mg₃Bi₂.

Table 1 in the material compared to the other two structures which have higher shared electrons and stronger covalent bonding. The corresponding charges changes in the family of Mg₃Sb_{2-x}Bi_x monolayers were calculated through the densityderived electrostatic and chemical (DDEC6) approach as implemented in CHARGEMOL package (Manz and Limas, 2016). Meanwhile, the higher ELF values in Mg₃Sb₂ and Mg₃SbBi monolayers also verify the higher transferred charges as seen in Table 1 since a higher ELF usually suggests a higher concentration of localized electrons in both Mg₃Sb₂ and Mg₃SbBi compared to Mg₃Bi₂ monolayers. From Table 1, our analysis shows that the higher difference in electronegativity between two atoms enhances the transferred electrons which is illustrated in 2D Mg₃Sb₂ with higher difference in electronegativity between Mg and Sb atoms (higher transferred charge) compared to 2D Mg3Bi2 with lower difference in electronegativity between Mg and Bi atoms (lower transferred charge). On the other hand, the value of Mg-Sb atoms around the ELF distribution in 2D Mg₃SbBi is much larger when compared 2D Mg₃Sb₂ and the results is in agreement with the corresponding calculations as depicted in Figures 4G,H. Herein, the negative value on the abscissa represents antibonding interactions, otherwise represents "-pCOHP" curves. bonding interactions in the three Meanwhile, the absolute ICOTF (using $ICOHP = \int_{-\infty}^{E} pCOHP(E)dE$) serves as an indicator toward indicate the d₁ interaction trends in 2D Mg₃Sb_{2-x}Bi_x (Mg₃SbBi > Mg₃Sb₂ > Mg₃Bi₂), and it is consistent with the κ_L changes. However, comparing for d₁ interactions in these compounds, we found that the absolute ICOHP for d_2 is always smaller. Typically, a weaker bond might cause phonons rattling behavior, leading the phonon modes softened, which supports the above κ_L results.

Usually, the several approaches, including the constant relaxation time approximation (Singh and Mazin, 1997; Madsen, 2006; Madsen and Singh, 2006; Yang et al., 2008), the deformation potential approximation (Sjakste et al., 2006; Murphy-Armando et al., 2010; Wang et al., 2011), and Wannier interpolation (Giustino et al., 2007; Bernardi et al., 2014; Qiu et al., 2015), can directly determine the electronic transport coefficients by solving the BTE theory. Herein, we used the EPA method to compute the corresponding parameters (S, σ , and κ_e) for the family of 2D Mg₃Sb_{2-x}Bi_x compounds, which was widely verified in the previous work (Nam et al., 2021; Biele and D'Agosta, 2022). For the above compounds, we presented the variation of *S* versus on the values of μ at three different temperatures in **Figure 5A**. It is cleared from the figure that

the maximum value of the S are 900 μ V/K (Mg₃Sb₂), 750 μ V/K (Mg₃SbBi), and 650 µV/K (Mg₃Bi₂) at 300 K, respectively, which are superior to those of some commercial TE materials such as SnSe (~500 μ V/K) (Zhang and Zhao, 2015)and Bi₂Te₃ (~200 μ V/ K) (Poudel et al., 2008), suggesting the high-performance TE candidate materials for P/N-type doping 2D Mg₃Sb_{2-x}Bi_x. Meanwhile, there are two notable peaks around the μ - E_f value of ~0 Ry, characterizing the S curves, and the calculated S would be decreased rapidly when beyond the ranges. The negative S values of the three studied compound are smaller than that of the corresponding positive values at ~ 0 Ry region, and the discrepancy can be understood by the above band structures (mainly attributing to the band-gaps) as displayed in Figures **4A–C.** By increasing Bi content from 2D Mg₃Sb₂ to 2D Mg₃Bi₂, the bandgap decrease gradually and thereby the absolute value of the maximum S decreases as well. As illustrated in Figure 5B, because of the similar electronic band structures among the three compounds, the σ curves represents a close slope at different temperatures. Moreover, we can see that the calculated σ values almost roughly increase with increasing the value of μ for all studied materials, while it is opposite for the S, indicating the two coefficients coupled unfavorably for enhancing TE performance. Furthermore, the maximum σ values for negative chemical and positive chemical potentials in the family of 2D Mg₃Sb_{2-x}Bi_x compounds are almost equal at 300 K, 500 K, and 700 K.

It is well known that the trends of κ_e is tied to the σ curves, and **Figure 5C** shows the variation of κ_e with response to the μ - E_f at different temperatures. Interestingly, we can observe that the maximum values of the κ_e for negative μ region are 2.4 W/mK (2D Mg₃Sb₂), 2.6 W/mK (2D Mg₃SbBi), and 2.8 W/mK (2D Mg₃Bi₂), while for positive chemical potential region these are 1.9 W/mK (2D Mg₃Sb₂), 0.8 W/mK (2D Mg₃SbBi), and 1.6 W/ mK (2D Mg₃Bi₂) at 300 K, respectively, where the calculated κ_e data is close to several commercial TE materials such as SnSe (~2 W/mK) (Wang et al., 2015) and Bi2Te3 (~1 W/mK) (Hicks and Dresselhaus, 1993). The results indicates that the N-type doping 2D Mg₃Sb_{2-x}Bi_x composition may possess a higher TE performance compared with the corresponding P-type doping samples. Based on the phonon thermal transport and electronic transport properties computed above, we show the ZT of 2D Mg₃Sb_{2-x}Bi_x compounds as a function of the μ -E_f at three typical temperatures (300 K, 500 K, and 700 K) as seen in Figure 5D. Obviously, the ZT in the three studied materials exhibit different trends, and the maximum ZT at 700 K can reach about 1.6 (2D Mg₃Sb₂), 0.2 (2D Mg₃SbBi), and 0.6 (2D Mg₃Bi₂), respectively. It can been clearly observed in Figure 5D that the TE performance of N-type doping is inferior to that of P-type doping for 2D



Mg₃SbBi and 2D Mg₃Bi₂ compounds, while it is opposite for 2D Mg₃Sb₂, and the behavior has been mainly dominated by Bi element content and then changing electronic band engineering.

CONCLUSION

In summary, we have systematically investigated the TE transport properties of the family of Mg₃Sb_{2-x}Bi_x (x = 0, 1, and 2) monolayers. Our results present that the three typical materials possess extremely lower lattice thermal conductivities, including 2D Mg₃Sb₂ (~0.51 W/ mK), 2D Mg₃SbBi (~1.86 W/mK), and 2D Mg₃Bi₂ (~0.25 W/mK) at 300 K, respectively, while a heavier atomic mass in a compound usually possesses a lower κ_L on the basis of the conventional (Keyes' and Slack's) theory. By decomposing the κ_L , it is concluded that the abnormal phenomenon is mainly due to the effect of phonon lifetime, which is significantly larger in Mg₃SbBi alloying system. Meanwhile, all these samples exhibit a transformation from semiconductor to semimetallic with increasing Bi element content, indicating a heavier compound having a narrower bandgap. Moreover, coupling with the κ_L above, we further obtained that the maximum *ZT* values of 1.6, 0.2, and 0.6 at 700 K are founded in N-type doping 2D Mg₃Sb₂, P-type doping 2D Mg₃SbBi, and P-type doping 2D Mg₃Bi₂, respectively. All the results of the analysis above suggest that increasing Bi element to Zintl phase 2D Mg₃Sb_{2-x}Bi_x alloy, which is beneficial to the reduction of the electronic thermal conduct ivies, might not necessarily improve the TE performance and offer a novel regulation approach which can be generalized in other Zintl phase monolayer compounds. Therefore, to obtain the optimal *ZT* in 2D Mg₃Sb_{2-x}Bi_x alloys, both Sb and Bi element

contents (except for x = 0, 1, and 2) need be further demonstrated by coupling theoretical calculations and experimental measurements.

DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/**Supplementary Material**, further inquiries can be directed to the corresponding authors.

AUTHOR CONTRIBUTIONS

ZC, JM, KY, XZ, and DT designed research. ZC: Conceptualization, Software, Formal analysis, Writing—original draft and editing, Data curation. KY, MA-F, and MH: Formal analysis, Writing—review and editing. JZ, YG, and HS performed the part calculations. All authors analyzed data and discussed results.

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SUPPLEMENTARY MATERIAL

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