

**The FreqTag toolbox: A principled approach to analyzing electrophysiological time series
in frequency tagging paradigms**

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ABSTRACT

Steady-state visual evoked potential (ssVEP) frequency tagging is an increasingly used method in electrophysiological studies of visual attention and perception. Frequency tagging is suitable for studies examining a wide range of populations, including infants and children. Frequency tagging involves the presentation of different elements of a visual array at different temporal rates, thus using stimulus timing to “tag” the brain response to a given element by means of a unique time signature. Leveraging the strength of the ssVEP frequency tagging method to isolate brain responses to concurrently presented and spatially overlapping visual objects requires specific signal processing methods. Here, we introduce the FreqTag suite of functions, an open source MATLAB toolbox. The purpose of the FreqTag toolbox is three-fold. First, it will equip users with a set of transparent and reproducible analytical tools for the analysis of ssVEP data. Second, the toolbox is designed to illustrate fundamental features of frequency domain and time-frequency domain approaches. Finally, decision criteria for the application of different functions and analyses are described. To promote reproducibility, raw algorithms are provided in a modular fashion, without additional hidden functions or transformations. This approach is intended to facilitate a fundamental understanding of the transformations and algorithmic steps in FreqTag, and to allow users to visualize and test each step in the toolbox.

Keywords: steady-state visual evoked potential (ssVEP); frequency tagging; frequency domain; time-frequency domain; MATLAB; FreqTag

1 **1-Introduction**

2 The electroencephalogram (EEG) relies on the non-invasive recording of brain electric
3 activity through sensors that are placed on the scalp to provide a rich source of information about
4 ongoing brain activity at a millisecond scale (Jackson & Bolger, 2014; Nunez et al., 2006). EEG
5 signals have been used to study a wide range of neural processes, including spectral properties of
6 resting EEG (Donoghue et al., 2020; Rogala et al., 2020), task-driven studies measuring event-
7 related potentials (ERP, for review see: Luck & Kappenman, 2013; Handy, 2004; Woodman,
8 2013) and steady-state visual evoked potentials (ssVEPs, for review see: Norcia et al., 2015;
9 Vialatte et al., 2010). EEG methods are also extensively used in developmental populations from
10 early infancy through adolescence (for review see: Barry-Anwar et al., 2020; Bell & Cuevas, 2012;
11 Riggins & Scott, 2020). The present report focuses on one specific EEG-based method: frequency-
12 tagging with steady-state visual evoked potentials (Norcia et al., 2015; Wieser et al., 2016). Studies
13 measuring ssVEPs in adults have substantially contributed to our understanding of visual processes
14 including selective attention, figure-ground segregation, and adaptation (for review see Norcia et
15 al., 2015).

16 The ssVEP is a neurophysiological response to a periodic visual stimulus. It is evoked by
17 stimuli that are periodically modulated in luminance (i.e., flickered) or contrast (e.g., pattern-
18 reversed) typically at temporal rates above 3 Hz (Odom et al., 2004). Both the luminance-evoked
19 and contrast-evoked ssVEP possess high signal-to-noise ratio and are robust to noisy recording
20 conditions, allowing researchers flexibility regarding dimensions of interest within stimuli
21 (Appelbaum et al., 2006; Keil, 2013). Luminance-evoked ssVEPs reflect visuocortical activation
22 based on input across the retina, whereas contrast-evoked ssVEPs at constant luminance tend to
23 emphasize foveal inputs which are more circumscribed in the visual cortex (Di Russo et al., 2006).

24 Because they are defined by their temporal frequency, ssVEPs may be extracted from scalp-
25 recorded EEG signals in the frequency domain, by calculating the amplitude spectrum of the EEG
26 segments of interest.

27 The ssVEP response typically consists of robust oscillatory activity at the exact modulation
28 frequency—driving frequency—as well as at its higher harmonics (integer multiples of the driving
29 frequency). Thus, an LED light flickering at 12 Hz evokes ssVEPs at 12 Hz, but may also prompt
30 responses at 24 Hz, 36 Hz, etc., depending on the composition of the stimulus array and the extent
31 to which the visual response is linear or non-linear (Norcia et al., 2015). Source estimation of
32 scalp-recorded ssVEPs (Di Russo et al., 2006) as well as combined ssVEP-fMRI work (Petro et
33 al., 2017) have converged to show that ssVEPs appear to be generated primarily in the striate
34 cortex (V1) with contributions from extrastriate regions (for review see; Vialatte et al., 2010).

35 One key feature of the ssVEP outlined in the present report is its use in frequency tagging.
36 This technique enables researchers to independently quantify the visuocortical response to multiple
37 stimuli, even when these stimuli are presented at the same time and at overlapping screen locations
38 (Tononi et al., 1998; Wang et al., 2007; Zhigalov et al., 2019). Thus, complex stimulus arrays may
39 be used and a unique visuocortical response to each element of the complex array is evoked by
40 periodically modulating each element at a different frequency. Frequency domain (spectral)
41 analyses can then be used to independently quantify the response of each stimulus in the amplitude
42 spectrum of the EEG data. For example, frequency tagging has been previously used for
43 quantifying neural competition between concurrent visuocortical representations evoked by
44 simultaneously present and overlapping stimuli (Appelbaum et al., 2006; Bach & Meigen, 1992),
45 which is difficult to accomplish with other neuroscience methods.

46 In developmental samples, ssVEPs have been used to assess lower-level sensory processes
47 in infants (Braddick et al., 1986; Gilmore et al., 2007; Hamer & Norcia, 1994), but also to
48 investigate higher cognitive processes such as overt and covert visual attention (Christodoulou et
49 al., 2018; Robertson et al., 2012), contour integration (Baker et al., 2011), face or object processing
50 (Barry-Anwar et al., 2018; Buiatti et al., 2019; de Heering & Rossion, 2015; Farzin et al., 2012;
51 Leleu et al., 2014; Lochy et al., 2019; Peykarjou et al., 2017; Vettori et al., 2020), number sense
52 (Park, 2018), and event processing (Köster et al., 2019). Studying development using recordings
53 of ssVEPs are particularly useful relative to other EEG measures for a variety of reasons. First,
54 infant and child EEG data often include an increased amount of noise relative to adults. Because
55 ssVEP analyses focus on a narrow set of frequency bands, the signal to noise ratio is very high
56 because only the noise present in the driving frequency bins is relevant (Regan, 1989). Second,
57 the amount of time required to collect high quality ssVEP responses from infants is less than what
58 is typically needed for ERPs. Furthermore, several conditions or tasks can be combined in a single
59 session, reducing attrition and increasing statistical power. The shorter session duration
60 requirement for ssVEP tasks compared to other EEG tasks is also important because it is often
61 difficult for infants to complete tasks that take longer than about 15 minutes (including breaks).

62 Studies using frequency tagging of multiple stimuli highlight the promise of using this
63 technique for studying cognitive and perceptual development (Baker et al., 2011; Buiatti et al.,
64 2019; Vettori et al., 2020). The present report demonstrates key analytical procedures for analyzing
65 frequency tagging data for both developmental and adult samples. The report is accompanied by
66 example adult and infant data and a MATLAB toolbox (FreqTag, <https://github.com/csealab/freqTag>) containing algorithms for performing analyses on frequency tagged data. Several
67 methodological details not covered in this paper are explained in the documentation accompanying
68

69 the toolbox. Many existing EEG analysis tools may be used for the same purpose (e.g., see
70 Mouraux & Iannetti, 2008 - Letswave, RRID:SCR_016414). The aim of the present toolbox is to
71 illustrate core analytical principles using barebones algorithms, with the intention to promote a
72 deeper understanding of the method and increase user confidence. Specifically, this report
73 illustrates spectral analysis based on discrete Fourier transform, and analysis in the time-frequency
74 domain, where the neural time course at each tagging frequency is individually extracted using the
75 Hilbert transformation. We also demonstrate the use of the sliding window averaging technique,
76 suitable for studies with fewer trials, as is sometimes the case for developmental EEG work. The
77 code (<https://github.com/csea-lab/freqTag>) and example datasets (<https://osf.io/e5vuf/>) are
78 publicly available.

79

80 **2-Methods and Materials**

81 2.1- Hardware and software needed to implement a frequency tagging protocol

82 As discussed above, many different research questions may be pursued using frequency
83 tagging. Thus, many different types of stimuli may be used, including stimuli in multiple
84 modalities (Giabbiconi et al., 2016; Riels et al., 2021). Regardless of the stimulus type and
85 modality used, it is crucial that researchers ensure accurate timing of each stimulus. For visual
86 stimuli, the tagging frequencies available are primarily determined by the display device used. The
87 refresh rate denotes the frequency (in Hz) at which the display can update its content. Not all visual
88 displays are suitable for evoking ssVEPs, and some of the key properties needed for regular,
89 accurate, periodic stimulation are more likely to be found in Cathode-ray tube (CRT) monitors,
90 compared to light-emitting diode displays (LED), and liquid crystal displays (LCD), since both
91 LCD and LED may present (a) response delays caused by digital processing time as well as (b)

92 temporal smearing due to slow and non-symmetric black to white and white to black response
93 times, especially at high stimulation rates. Several companies offer non-CRT solutions that provide
94 high refresh rates and rapid transition times from black to white and vice versa.

95 Successful implementations of tagging protocols are also accomplished with hardware
96 solutions where custom circuit boards drive individual light-emitting diodes controlled by a
97 microcomputer (e.g., Gulbinaite et al., 2019). A comprehensive discussion of display systems is
98 outside the scope of this report, and readers are referred to the extant discussions in the literature
99 (e.g., Wang & Nikolic, 2011). Likewise, graphic processing demands are high when using
100 frequency tagging, and researchers should consider state-of-the art graphics cards rather than on-
101 board graphics, which are often insufficient for ensuring accurate ssVEP stimulation.

102 Not all software used to generate and control visual stimuli in the cognitive neuroscience
103 laboratory is suitable for use with ssVEP frequency tagging given that the technique exerts high
104 demands regarding graphic card control and timing accuracy (Jaganathan et al., 2005). It is
105 therefore highly recommended to test and validate the intended timing before beginning data
106 collection. Light sensitive diodes and similar devices are readily available to capture and store
107 luminance changes directly from the display device, allowing researchers to examine the overlap
108 between the control software's specifications and the reality on the display. Suitable software
109 packages for experimental control include psychtoolbox, psychopy, and presentation, in addition
110 to low-level code written in various programming languages. We provide example code written in
111 Psychtoolbox (taggingdemo.m) together with the FreqTaq toolbox.

112 2.2-Implementing the stimulus array

113 There are several parameters to be considered when using frequency tagging tasks such as
114 the monitor refresh rate, the duration of the stimulus presentation within each trial, and the EEG

115 sampling rate. When using on-off flicker, the frequencies available for tagging on a 60 Hz monitor
116 are at the ratio of 60 and the integers from 2 to 20, i.e., at 60/2, 60/3, 60/4, ... 60/20, resulting in
117 potential frequencies at 30, 20, 15, 12, 10, 8.571, 7.5, 6.667, 6.0, 5.455, 5.0, 4.615, 4.286, 4.0,
118 3.75, 3.529, 3.333, 3.158, and 3.0 Hz. This is equivalent to determining the tagging frequencies
119 based on the wavelength of the refresh rate, also known as the refresh interval, which in the case
120 of the 60 Hz monitor is $1000/60 = 16.66\text{ms}$. Here, the available tagging frequencies can be
121 computed by dividing 1000 by the product of the refresh interval and the integers between 2 and
122 20, resulting in the same potential tagging frequencies for on-off flicker. Note that periodic
123 presentations with other stimulation (e.g., sinusoidal, rather than on-off, modulation of luminance)
124 may result in additional frequencies becoming available, as discussed for example by Andersen &
125 Müller (2015).

126 For some applications, researchers may prefer that the two components of the ssVEP duty
127 cycle (e.g., the on and off periods of the stimulus in a flicker-ssVEP) be of equal duration. This
128 reduces the available tagging frequencies by 50%. In the example above, frequencies resulting
129 from multiplying odd numbers with the refresh interval will be unavailable if on and off-periods
130 (in luminance ssVEPs) or pattern one versus pattern two (in pattern reversal ssVEP) are to be of
131 the same duration. Furthermore, when using multiple frequencies for many visual objects
132 simultaneously, researchers will want to ensure that the tagging frequencies do not exhibit
133 harmonic relations (in which one tagging frequency is an integer multiple of another; 6 Hz and 12
134 Hz for example), because this prevents the independent analysis of the two spectral responses (in
135 the example, the second harmonic of the 6 Hz stimulus is located at the fundamental driving
136 frequency of the other stimulus, i.e., at 12 Hz).

137 The epoch duration, the duration of the EEG data segment used for frequency analysis,
138 determines the spectral resolution used to quantify the ssVEP at each frequency. If the epoch is
139 too short in duration, frequency resolution may not suffice for discriminating between the two or
140 more frequencies used for tagging. In these cases, many researchers use padding with zeros or
141 other suitable values, which increases the number of the bins on the x-axis of the spectrum and
142 thus facilitates the separation of the tagging frequencies in the spectrum. It is important to note,
143 however, that increasing the number of bins does not increase the true underlying spectral
144 resolution because zero-padding only interpolates the information already contained in the data. It
145 is also advisable to use epoch durations that hold integer numbers of cycles for a given tagging
146 frequency, based on integer numbers of sample points. For example, 60 full cycles of flicker
147 ssVEPs evoked for 6000 ms at a frequency of 10 Hz, on a 60 Hz monitor, are captured by the 6000
148 ms window when sampling at 500 or 1000 Hz, but not when sampling at 512 Hz. Ensuring that
149 the data segment of interest contains integer numbers of cycles and sample points will result in
150 frequency spectra that contain bins at the exact stimulation frequency, without additional
151 preprocessing steps such as up-sampling and padding (for an extensive discussion of these points,
152 see Bach & Meigen, 1999).

153 Planning the epoch duration and selecting the tagging frequencies such that integer cycles
154 are available in the epoch of interest, at the sample rate used, also minimizes distortions related to
155 so-called "spectral leaking." This term refers to the smearing of oscillatory responses across two
156 or more bins of the spectrum, which may occur for example when there is no bin available at the
157 exact tagging frequency. Such leaking may lead to misinterpretation of condition differences,
158 especially when the mapping of tagging frequencies to stimuli and experimental condition is not
159 counterbalanced across the experiment. The reader is directed to reviews and guidelines regarding

160 the technical aspects of ssVEP procedures (Bach & Meigen, 1999; Keil et al., 2014; Norcia et al.,
161 2015; Vialatte et al., 2010; Wieser et al., 2016).

162 **3-Analyzing frequency tagging data: a step-by-step demonstration**

163 3.1-The example data sets

164 Example data from one adult (Silva et al., 2021) and one infant (Barry-Anwar et al., in
165 preparation) are provided on the Open Science Framework companion site of this paper. Both data
166 sets have undergone initial segmenting, filtering, and artifact control. The functions provided in
167 the FreqTag toolbox expect a 3-dimensional MATLAB array with dimensions of sensors, time
168 points, and trials, as produced by widely used preprocessing tools including EEGLAB (Delorme
169 & Makeig, 2004), ERPLAB (Lopez-Calderon & Luck, 2014) as well as other preprocessing
170 pipelines used for infant data including HAPPE (Gabard-Durnam et al., 2018); MADE (Debnath
171 et al., 2020), PREP (Bigdely-Shamlo et al., 2015), and ADJUST (Leach et al., 2020) and readily
172 exported from environments such as BrainVision Analyzer (BrainVision Analyzer, Brain Products
173 GmbH, Gilching, Germany), fieldtrip (Oostenveld et al., 2011), MNEPython (Gramfort et al.,
174 2013).

175 3.1.1- Adult data set

176 The first example data set data comes from a study with adult observers (Silva et al., 2021).
177 The full data set for this study can be found at:
178 https://osf.io/a53s9/?view_only=1966f70fac954bac886381f908c7a275. For the sample data
179 provided here, EEG was recorded from 129 channel geodesic EEG recording net (Philips EGI,
180 OR, USA) while faces and novel objects (Sheinbugs, see Jones et al., 2018) were concurrently
181 presented, fully spatially overlapping with each other, and rapidly contrast-modulated. Two
182 different temporal rates, 5 Hz and 6 Hz, one used for faces and one for objects (counterbalanced

183 across participants). The experimental design is depicted in Figure 1. Both stimuli periodically
184 emerged at their tagging frequency from a Brownian noise (spatial noise with a $1/f^2$ characteristic)
185 patch with the same mean luminance and contrast as the experimental stimuli for a duration of
186 6000 ms for 70 trials.

187 [Insert Figure 1 here]

188 3.1.2- Infant data set

189 The second example data set is taken from a recently completed infant investigation using
190 frequency tagging. The entire data set, and stimuli are available at: Barry-Anwar et al., in
191 preparation; OPEN NEURO- BIDS format. Parents of all participants gave informed consent prior
192 to testing. EEG data were collected using a 129-channel Electrical Geodesic system (Net Amps
193 400, Phillips EGI, Eugene, OR). A subset of 109 sensors were kept for analysis. Infants viewed up
194 to 20 6-second trials (sample data are from a 9-month-old). Frequency tagging parameters, stimuli,
195 and trial duration were the same as in the adult sample.

196

197 3.2 Using this document and planning the analyses

198 The following step-by-step instructions reflect operations that are part of prototypical
199 pipelines for visualizing and analyzing data from a frequency-tagging study. Readers are
200 encouraged to follow along with the example pipeline code supplied on the github companion site
201 in the matlab live script (.mlx) format (freqtag_pipeline_example1.mlx, and
202 freqtag_pipeline_example2.mlx), or the corresponding .m file scripts. Live scripts allow users to
203 read background documentation and execute the code stepwise, while examining inputs and
204 outputs along with visualizations of each step. Thus, these live scripts and their accompanying
205 documentation detail many technical aspects and usage of the functions employed in the pipeline.

228 3.3.1 Assessing data quality and preparing a barebones spectral analysis

229 The first step towards quantifying the ssVEP amplitude for the tagging frequencies is the
230 computation of the amplitude spectrum using the Discrete Fourier Transform (DFT). This
231 transform produces an amplitude spectrum, in which frequency is shown on the x-axis and
232 amplitude at each frequency is plotted on the y-axis. In a spectral analysis not all frequencies are
233 available and their distribution along the x-axis is determined by the Fourier uncertainty principle
234 (for detailed discussion see: Bach & Meigen, 1999; Keil, 2013). According to this principle, the
235 frequency resolution is determined by the duration of the EEG data segment used for the frequency
236 analysis. Specifically, the smallest possible step-width on the x-axis of a spectrum is given as the
237 inverse of the duration of the data segment entering the analysis, in cycles per second, measured
238 in Hertz (Hz). Thus, transforming a time segment of 2 seconds from the time into the frequency
239 (spectral) domain results in a spectrum with $\frac{1}{2} = 0.5$ Hz frequency resolution and a frequency axis,
240 drawn on the x, which contains the frequency from 0 to half of the sampling rate in steps of .5 Hz.
241 By the same token, transforming a time segment with a duration of 5 seconds will result in a
242 spectrum spaced at $\frac{1}{5} = 0.2$ Hz.

243 After establishing these cornerstones of the planned analysis, we apply them to the example
244 data files. The first dataset (exampledata_1.mat) was recorded with a sample rate of 500 Hz and
245 has already been filtered by means of a 30-Hz low-pass (18th order Butterworth) and a 1-Hz high-
246 pass (4th order Butterworth). The epochs were extracted from continuous EEG data, containing
247 400ms pre- and 7400ms post-stimulus onset (see Silva et al., 2021 for detailed description). Thus,
248 if researchers were to transform the entire segment, including the pre-stimulus data, into the
249 frequency domain, the frequency resolution would be 0.1282 (frequency resolution = $1/7.802$, i.e.,
250 one divided by the segment's duration in seconds). However, in studies with frequency tagging it

251 is likely that researchers are interested in determining the spectrum selectively for the period of
252 time during which ssVEP stimulation was present. In addition, it is often preferred to exclude the
253 early portion of the stimulation epoch. This practice eliminates confounds of the ssVEP signal with
254 potential transient ERPs evoked by the onset of the frequency tagging array and assists in focusing
255 the analysis on the segment during which the ssVEP has reached a steady, stationary state.

256 In the example adult data, we select a segment starting 1 second after the onset of the
257 frequency tagging array and ending at 7 seconds after the onset of the Brownian noise. In the
258 pipeline this segment is called “data_ssvep”. Considering the Nyquist Theorem and the sampling
259 rate (500 Hz), we know that the highest frequency to be analyzed for the dataset is 250 Hz.
260 Therefore, between 0 Hz and 250 Hz, in steps of 0.2 Hz (1/5 seconds), the spectrum contains 1251
261 frequencies.

$$262 \quad \text{Highest (Nyquist) Frequency} = \frac{\text{Sampling Rate}}{2};$$

$$263 \quad \text{Frequency Resolution} = \frac{1}{\text{Epoch Duration in secs}};$$

265
266

267 To implement ssVEP frequency-tagging in this task, Silva and colleagues (2021) used two
268 different rates, 5 Hz and 6 Hz, one used for faces and one for objects. An initial manipulation
269 check includes making sure that the dataset’s frequency resolution can discriminate between the
270 frequencies used for tagging and that the x-axis of the spectrum contains a bin at the exact
271 stimulation frequencies. It is common practice to remove frequencies unrelated to the focus of
272 your analysis and frequencies that are not related to brain activity. In this case, the frequencies
273 kept for further analysis are those between 0 and 32.33Hz, called *faxis* in
274 `freqtag_pipeline_example1.mlx`.

275 In general, it is good practice to visualize the data after each step of the analysis. Using the
276 plot command, readers can plot the data in the time domain as an event-related potential (see Figure
277 3). In Figure 3, the x-axis represents time, and the y-axis represents the amplitude. Examples for
278 plotting the data are provided throughout the `freqtag_pipeline_example1.m` script.

279

280 [Insert Figure 3 here]

281

282 3.3.2 – Conducting a barebones Fourier Transform: the `freqtag_FFT` function

283 The Fourier Theorem states that any given time domain signal can be represented in the
284 frequency domain by a sum of sine and cosine waves with different frequencies, amplitudes, and
285 phases. Several excellent tutorials on the foundations of Fourier analysis in EEG research are
286 available for readers interested in learning more about its mathematical principles (Cohen, 2011;
287 Keil, 2013). Many implementations of spectral analyses for EEG data exist, most of which involve
288 application of so-called taper windows, within-segment averaging, zero-padding, or differential
289 weighting of time points entering spectral analysis. However, for ssVEP analyses, a Fourier
290 transform with no or minimal modifications (i.e., a barebones implementation) may yield the most
291 unbiased estimate of ssVEP amplitude and phase (for a discussion, see Bach & Meigen, 1999).

292 At this stage of the pipeline, researchers make a key conceptual decision regarding the
293 nature of the ssVEP signal: Traditionally, the ssVEP has been regarded an “evoked” response,
294 which means that it is defined by being exactly time and phase-locked to the tagging stimulus, and
295 thus analyzed analogous to event-related potentials. Specifically, a sufficient number of trials, with
296 the same driving stimulus array, are collected and averaged in the time domain to suppress activity
297 that is not locked to the timing of the periodically modulated stimulus. In the present case, this is

298 accomplished by averaging across the third dimension of the data array (trials). The resulting 2-
299 dimensional time-domain average (sensors by time points) is then submitted to a spectral analysis.
300 This is accomplished by the function `freqtag_FFT.m`, which uses the MATLAB built-in Discrete
301 Fourier Transform algorithm (`FFT.mat`) without windowing or padding. This function outputs the
302 amplitude spectrum, the phase spectrum, the complex spectrum of Fourier components, and a
303 vector (list) of the frequency bins available in the spectrum.

304 3.3.3 – Conducting a Fourier Transform on single trials: the `freqtag_FFT3D` function

305 A second approach to conceptualizing the ssVEP is to emphasize the flexible entrainment
306 of ongoing brain oscillations by the driving stimulus array. Under this assumption, not all of the
307 ssVEP signal is exactly time- and phase-locked across trials and trial averaging may thus cause
308 information loss (Gulbinaite et al., 2019). Researchers adopting this view have often analyzed the
309 ssVEP by transforming each individual trial into the spectral domain followed by averaging the
310 resulting single-trial amplitude spectra, thus avoiding cancellation of activity at the driving
311 frequency that is not exactly time-locked across trials. In the present pipeline, this is accomplished
312 by the function `freqtag_FFT3D.m`, which uses the initial 3-D data array (`data_ssvep`) containing
313 electrodes, time points, and trials (for the third dimension). This function applies the Fourier
314 Transform on each trial and averages the resulting spectra.

315 This latter approach is suggested for researchers who are interested in quantifying ssVEP
316 activity while assuming that the phase may vary from trial to trial. For more experienced users,
317 `freqtag_FFT3D` also outputs the complex spectrum for each trial, which can be used to calculate
318 measures of variability and consistency of the ssVEP response, such as the circular T^2 statistic
319 proposed by Victor and Mast (1991), or the Rayleigh statistic. The present paper cannot provide
320 an in-depth discussion of these metrics, but readers are encouraged to consider metrics based on

321 complex representations, including when planning a study, as discussed in Baker et al. (2021). The
322 toolbox also includes a version of the circular T^2 statistic, for application with the output of
323 `freqtag_FTT3D`, or `freqtag_slidewin`, discussed below.

324 The typical way of illustrating the results of the Fourier Transform is a 2-D plot with
325 frequency on the x-axis and amplitude on the y-axis. For visualization purposes, readers may wish
326 to select a subset of the available frequencies. In the present example, both the evoked spectrum
327 (after averaging in the time domain; Figure 4 – top panel) and the single-trial based spectrum
328 (averaging the single trial spectra; Figure 4 – bottom panel) show not only the activity at the
329 stimulus tagging frequency (5 Hz and 6 Hz peaks) but also at other frequencies. These frequencies
330 include multiples of each tagging frequency (harmonics, e.g., at 10 and 12 Hz) but also some linear
331 combinations of the two driving frequencies (intermodulation frequencies, e.g., at 4 Hz). There is
332 a growing literature on how these additional responses may be used to test hypotheses regarding
333 neural function (Appelbaum et al., 2006; Kim et al., 2005; Kim & Verghese, 2012). In a typical
334 application, the amplitude at occipital sensors will serve as the dependent variable for statistical
335 analysis, potentially after being converted to a signal-to-noise ratio (see 3.4.3 for an
336 implementation of this step).

337 [Insert Figure 4 here]

338

339 3.3.4 – Using the Hilbert Transform to extract time-varying ssVEP amplitude envelopes:
340 the `freqtag_HILB` function

341 Research questions addressed in frequency tagging studies often involve the time course
342 of visuocortical activity assessed separately for stimuli in the tagging array. One method for
343 extracting the time course of a narrow-band oscillatory waveform is the Filter-Hilbert method.

344 This method involves the Hilbert transform, a mathematical approach to generate a 90° phase-
345 shifted version of the empirical time series, which then directly translates into a time-varying
346 envelope measure. A core requirement for accurately determining and shifting the phase of the
347 empirical signal is that the data used to perform the Hilbert transform are narrowly bandpass
348 filtered. Although the Hilbert method can be readily applied to broadband signals containing
349 activity at multiple frequencies, its results will range from difficult to interpret to meaningless
350 because it uses phase-shifting, and the phase of a signal is only defined for a specific frequency.

351 Given the importance of digital bandpass filtering in the context of the Hilbert transform,
352 readers may wish to peruse suitable tutorials and reviews of digital filtering as used in human
353 electrophysiology (Luck, 2005; Nitschke et al., 1998; Rousselet, 2012; Widmann et al., 2015). The
354 present paper uses simple and straightforward Butterworth filters. In brief, bandpass filtering is
355 achieved by the construction of a kernel that is convolved with the EEG data to both preserve the
356 frequencies of interest and attenuate the undesired frequencies. To create such kernel, it is
357 necessary to define the filter shape and the frequency characteristics that define that shape.
358 Designing a Butterworth filter in Matlab involves two input arguments: the filter order and the
359 cutoff frequency. The filter order determines the precision of the filter's frequency response.
360 Sharper roll-offs produced by higher filter order may increase the edge artifact expected to arise
361 from filtering segmented data, and they heighten the delay of the filter onset response. Therefore,
362 readers should carefully select the filter and visualize the data in order to control these artifacts.
363 Once the kernels are built, the data can be filtered by means of the “filtfilt” function which is a
364 zero-phased forward and reverse digital infinite-impulse filtering procedure. The function
365 `freqtag_HILB` contains all of these steps such that the filtered version of the data is computed
366 within the function and passed into the built-in MATLAB function “Hilbert”.

367 The results of the Hilbert Transform are the outputs “hilbamp,” “phase,” and “complex.”
368 The variables “hilbamp” and “phase” contain the information of how amplitude and phase of the
369 tagging frequency change over time. The variable “complex” contains both the empirical (real
370 part) and phase-shifted (imaginary part) of the ssVEP, combined into one complex number for
371 each time point. To visualize how the ssVEP amplitude at the frequency of interest changes over
372 time, readers may plot the time-varying amplitude (“hilbamp”; see Figure 5).

373

374 [Insert Figure 5 here]

375

376 3.4 – Example 2. Using the sliding window approach to estimate the ssVEP in single trials

377 Not all research questions are readily addressed using information that is pooled across
378 trials. Experimenters may wish to quantify the trial-by-trial change of visuocortical processing
379 across only one experimental session or may wish to apply trial-based modeling of learning,
380 habituation, adaptation, or other concepts that are at odds with trial averaging. Furthermore,
381 limitations specific to the design or the population may prevent researchers from obtaining enough
382 trials to enable the approach discussed in 3.3 above. Figure 6 represents the amplitude spectra
383 obtained after the Fourier Transform, the expected driving frequencies and harmonic peaks are not
384 as clear as the adult amplitude spectra shown in Figure 4. In many of these cases, it is possible to
385 quantify the ssVEP amplitude evoked by a specific tagging stimulus at the level of single trials,
386 using a simple sliding window method (Morgan et al., 1996; Wieser et al., 2016). Here, we use an
387 example data set obtained from infants to illustrate this method, which may be particularly helpful

388 in developmental studies with few available trials. The procedures are illustrated in the
389 accompanying live script `freqtag_pipeline_example2.mlx`.

390 [Insert Figure 6 here]

391 3.4.1. Implementing the sliding window analysis: the `freqtag_slidewin` function

392 Sliding window analyses capitalize on the regularity of the driving stimulus and its evoked
393 brain electric response, at a known frequency. The rationale is simple: given sufficient trial
394 durations, a sliding average window that contains a suitable number of integer cycles of the driving
395 frequency (in our example, 4 cycles) can be shifted across the ssVEP segment of interest, in steps
396 that correspond to a full cycle of the oscillation (e.g., Morgan et al., 1996). Continuous averaging
397 of the contents of these sliding windows amplifies any oscillation that is time and phase-locked to
398 the driving stimulus and attenuates oscillations that vary in terms of their phase or frequency.

399 The example infant data set (`exempladata_2.mat`) has a 3-dimensional MATLAB array
400 with channels (109), time points (2500), and trials (after artifact detection 15 out of 20). During
401 preprocessing and segmenting, the time points that were not of interest have been removed and the
402 remaining 2500 sample points represent the duration of the frequency tagging array containing
403 faces and objects, tagged at 5 and 6 Hz. To implement the sliding window analysis, we use the
404 function `freqtag_slidewin.m`, which executes all steps needed for this analysis, including the
405 sliding window averaging and subsequent spectral analysis. This function applies a sliding window
406 analysis as described in Wieser et al., 2016 to each trial, at a given frequency.

407 The `freqtag_slidewin` function requires as input arguments: the data in a 3-D format
408 (sensor-by-time points-by-trials), a flag to determine whether or not to plot the sliding window
409 process (`plotflag`), a vector containing the sample points to be used for baseline subtraction (`bslvec`),

410 a vector containing the sample points to be used in the sliding window procedure (`ssvepvc`), the
411 driving frequency (`foi = 5` or `6`), a new sample rate if needed (`fsampnew`, see below), the sampling
412 rate (`fsamp = 500Hz`), and an out name. The baseline correction is necessary to remove drift, which
413 may induce spectral leaking. In the present example, `exampledata_2` only contains the data
414 segment during which the stimuli were flickering. If users are working with epochs containing
415 other stimuli, they may assign only the time window of interest using the `ssvepvec` argument.

416 The function computes the duration, the onset times, and the number of sliding windows.
417 These windows contain 4 cycles of the driving frequency of interest and are stepped across the
418 ssVEP segment in steps of one cycle. For example, when extracting the 5 Hz ssVEP, the sliding
419 window contains 4 cycles of 200 ms (the wavelength at 5 Hz), thus being 800 ms long. Second,
420 the window is then moved across the EEG segment of interest in each trial, in steps of 200 ms,
421 corresponding to one full cycle of the driving frequency at 5 Hz.

422 At a driving rate of 6 Hz, the corresponding window length is 666.667 ms, to be moved
423 over the EEG segment in steps of 166.667 ms. Thus, at a sampling rate of 500 Hz, there will be no
424 integer numbers of sample points that accommodates the step-width or window length. As
425 explained above (section 2.2), this will lead to spectral leaking due to including incomplete cycles
426 entering the analysis. It is thus necessary to upsample the data to a rate that allows representation
427 of integer cycles of the driving frequency. As discussed in Bach & Meigen, 1999, an integer
428 relation between monitor retrace and sample rate is required to ensure the capture of each available
429 driving frequency by an integer number of sample points. In our example, this can be accomplished
430 by upsampling the data to 600 Hz, implemented by setting the “`sampnew`” input argument
431 accordingly. Setting the plotting flag to 1 produces a time-varying representation of each new

432 sliding window and the running average. Default outputs of the function are the trial-by-trial
433 spectral amplitude at the frequency of interest, at each electrode (trialamp), and a 3-dimensional
434 array that contains the sliding average in the time domain, for each trial and sensor (winmat).

435 One potential concern when using short segments of data is the cross-contamination of one
436 tagging frequency by the other frequency, which is present in the signal, but not centered at another
437 frequency bin. This concern may be particularly relevant when tagging frequencies occupy nearby
438 spectral bins, as is the case in the example data sets used here: When applying the sliding window
439 method to extract 6 Hz ssVEP responses from single trials, there is no bin at 5 Hz in the spectrum
440 used to measure the 6 Hz response, which has bins at steps of $1/0.666 = 1.5$ Hz. In most practical
441 situations, the sliding window average technique however suppresses responses outside the target
442 frequency. To illustrate this, the toolbox contains a simulation (simulsidebands.m) of how varying
443 the amplitude of one tagging frequency affects the ssVEP amplitude measurement at the other
444 (target) frequency and vice versa, when using the sliding window approach. Across a range of
445 signal and noise levels, this simulation (See Appendix C and accompanying code) shows that,
446 given typical trial lengths and stimulation rates, cross-talk between tags does not significantly
447 affect amplitude estimation with the sliding window average method. As is also shown in appendix
448 C, crosstalk does affect certain measures of signal-to-noise ratio, especially in cases where the tags
449 are nearby and when the signal-to-noise ratio of the frequency of interest is low. Thus, users are

450 encouraged to use caution when using signal-to-noise ratios in combination with the sliding
451 window method.

452

453 3.4.2. Computing variables of interest: amplitude and phase-stability

454 The default outputs of the sliding window function may not always be suitable for testing
455 the hypothesis of interest in a given study. For example, if researchers are not interested in the
456 trial-wise variation of the ssVEP they may wish to combine spectral information across trials, or
457 to calculate amplitude after pooling the time-domain sliding window averages for each trial. For
458 example, in studies with few trials in which the analyses described in 3.3 are unavailable. Like the
459 rationale explained in 3.3 for time-domain averaging prior to spectral analysis, researchers may
460 combine the single trial averaged windows into a cross-trial average, emphasizing the portion of
461 the oscillation that is time and phase locked to the driving stimulus across repeated trials.

462 This can be accomplished by averaging the time-domain information contained in the
463 `winmat` (`winmat3d5Hz` or `winmat3d6Hz`) in the third dimension (trials). The new time series
464 (`meanwinmat`, electrode-by-time-points) can, then, be used as the input argument for the
465 `freqtag_FFT` function. The frequency spectrum of the sliding windows can be plotted using the
466 `bar` built-in MATLAB function (Figure 7, left panel), where the y-axis is the amplitude at each
467 time-point (variable “amp”) and the x-axis is the frequency axis (variable “freq”). Alternatively,
468 the spectral amplitude extracted from each trial may be averaged across trials, allowing

469 contributions to the trial averaged amplitude independent of the within-trial phase, using the
470 function `freqtag_FFT3D`.

471

472 [Insert Figure 7 here]

473 As discussed in Wieser et al., 2016 researchers may also wish to test hypotheses regarding
474 the stability of the tagged oscillation within each trial, measured as the phase similarity between
475 all of the sliding windows. If the phase or latency of the ssVEP changes within a trial, relative to
476 the periodic driving stimulus, then the phase similarity will be lower. If the phase relationship
477 between the ssVEP and the driving stimulus remains stable across the duration of the trial, then
478 the phase at the driving frequency should be similar across all sliding windows. Phase similarity
479 is readily quantified using the phase-locking index, in which normalized complex phase values
480 (real and imaginary part of the Fourier transform) are averaged and the absolute value (vector
481 length or the Euclidean norm) of the average is the phase similarity index. The `freqtag_slidewin`
482 function computes the phase stability index for each trial and outputs a value for each electrodes
483 and trial as 2-dimensional matrix (electrodes by trials), which can then be statistically analyzed
484 and plotted using EEGLAB/ERPLAB.

485 3.4.3 – Computing the signal-to-noise ratio: `freqtag_simpleSNR`

486 Finally, as was visible from the amplitude spectra shown in 3.3.2 (see Figure 4), spectral
487 peaks located at the ssVEP amplitude often sit on top of other spectral phenomena which may
488 include ongoing oscillatory activity or non-periodic activity. Thus, a comparison of raw amplitude
489 often is difficult, as the amplitude estimate may confound ssVEP with non-ssVEP amplitude at the
490 frequency of interest. Researchers have addressed this problem by computing signal-to-noise ratios

491 or similar measures (e.g., baseline corrected amplitude) for determining the distance between the
492 ssVEP amplitude peak of interest from spectral noise in the same region of the spectrum (see e.g.
493 Rossion et al., 2012). This issue has also been discussed for non-ssVEP spectral signals, which are
494 often difficult to distinguish from non-periodic activity: Several advanced methods have been
495 developed to separate oscillatory activity from other contributions to the spectrum (Donoghue et
496 al., 2020). These methods often rely on estimating the overall shape of the amplitude spectrum
497 which tends to take the shape of an exponential ($1/f$) function.

498 In the case of ssVEP spectra after trial averaging however, or with shorter segments as used
499 in sliding window analyses, the spectrum tends to be overall flat, with the ssVEP tagging frequency
500 visible as a signal. In the present report, we provide a widely used and simple approach for
501 addressing this issue and measure the ratio of the amplitude at a given driving frequency over the
502 mean amplitude measured at suitable neighboring (non-ssVEP) frequencies, by means of the
503 `freqtag_simpleSNR` function.

504 As shown in the example, the selection of adjacent frequencies for the noise estimation
505 aims to avoid other tagging frequencies, harmonics, and intermodulation frequencies (linear
506 combinations of the tagging frequencies). The resulting ratios can be exported for hypothesis
507 testing as unitless ratios, but also converted into decibels. One way to plot the result as decibels,
508 using the `bar` built-in MATLAB function, is using the `SNRdb` output of this function (`SNRdb5Hz`
509 or `SNRdb6Hz`) as the y-axis and the “freq” as the x-axis (Figure 8). “freq” is a variable originated
510 through the `freqtag_FFT` and contains all the available frequencies as a vector.

511 To fully take advantage of the barebones functions provided in this toolbox, readers are
512 invited to consult extant review papers on ssVEPs and the frequency tagging approach (Norcia et

513 al., 2015; Wieser et al., 2016). Furthermore, the functions provided here are readily combined with
514 functions from other MATLAB-based analysis environments, which may add additional
515 functionality. Finally, the code provided is intended to be tailored to specific research questions
516 and populations. Many of the intermediate results computed in this pipeline may be used in ways
517 that suit researchers interested in concepts like connectivity, neural competition, source
518 distribution, and inter-trial variability of visuocortical signals (e.g., see Barry-Anwar et al., under
519 review; Silva et al., 2021)

520 **4- Summary and outlook**

521 The goal of this article was to provide readers with conceptual and practical building blocks
522 for ssVEP analysis for data collected using frequency tagging. The ability to individually quantify
523 the individual visuocortical responses evoked by multiple concurrent and overlapping stimuli is a
524 unique strength of this approach. Thus, frequency tagging allows testing hypotheses not typically
525 addressable with other methods, including hypotheses regarding interactions between multiple
526 items. Given its robust underlying signal, the method is highly suited for investigating populations
527 that may be unable to sit through lengthy experimental sessions including infants, young children,
528 and clinical populations.

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536

537

538 **6 -References**

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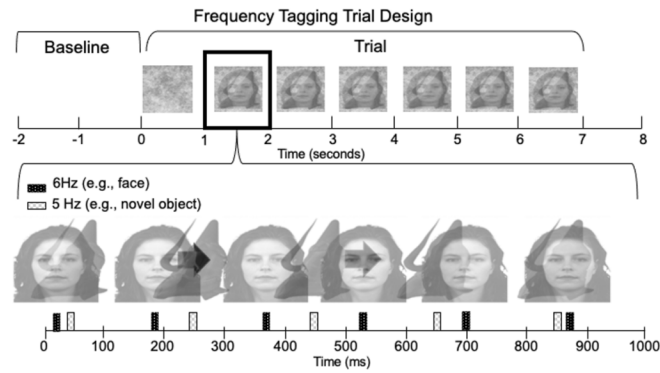
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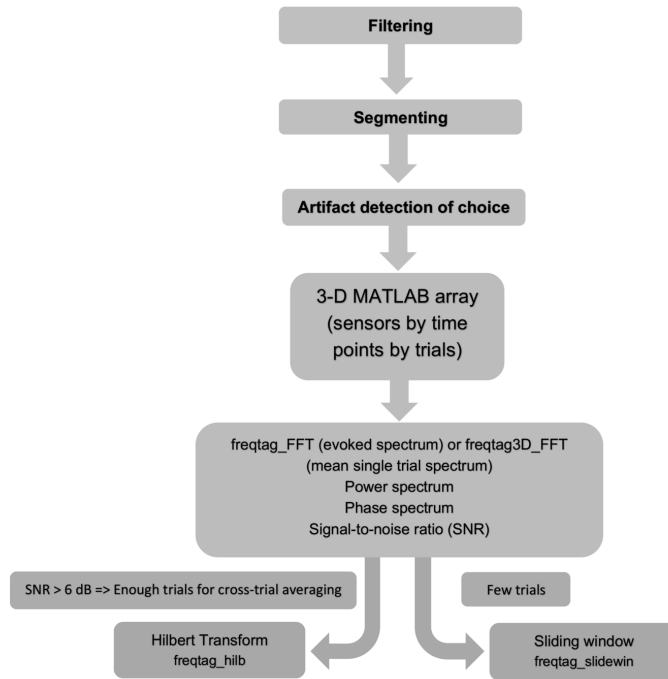
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790 Figure 1: Experimental design modified from Silva et al., 2020. Segments used for Frequency and Time-
 791 Frequency analysis were 6 seconds long. The stimuli (faces and objects, flickering in 5hz and 6Hz)
 792 concurrently emerged from a Brownian noise background.



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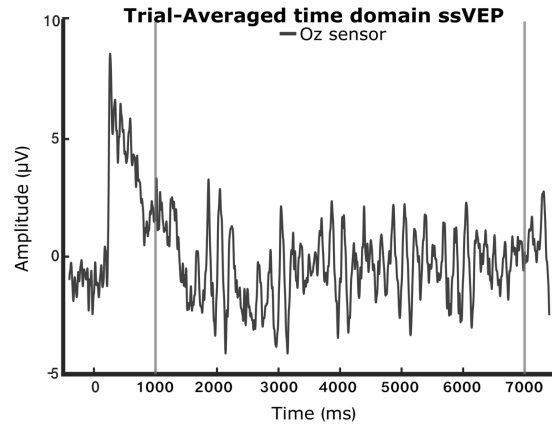
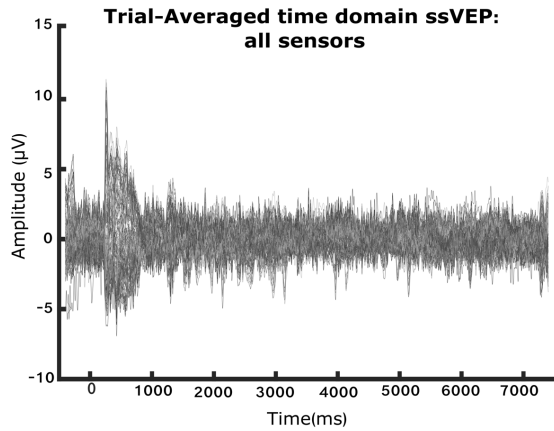
795 Figure 2: A decision tree for the choice of analysis purposes showing how the number of trials lead to two
 796 sets of different analyses.

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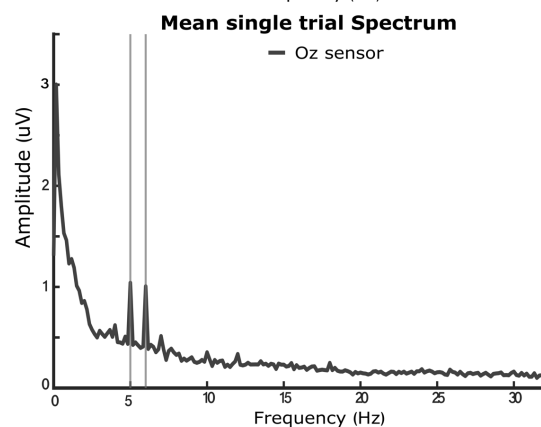
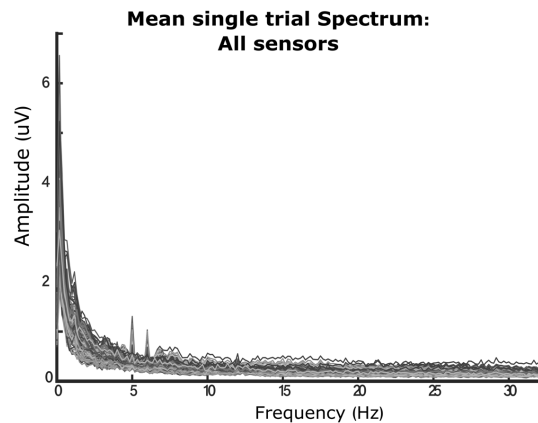
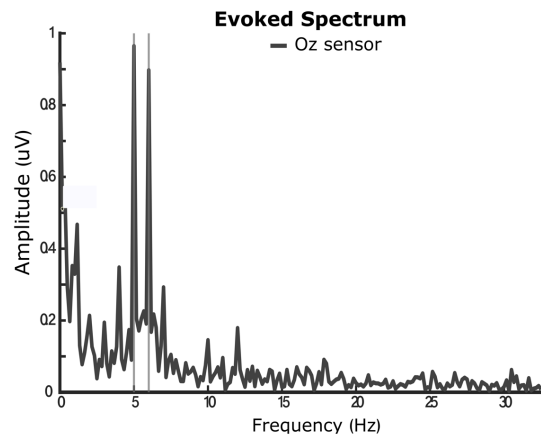
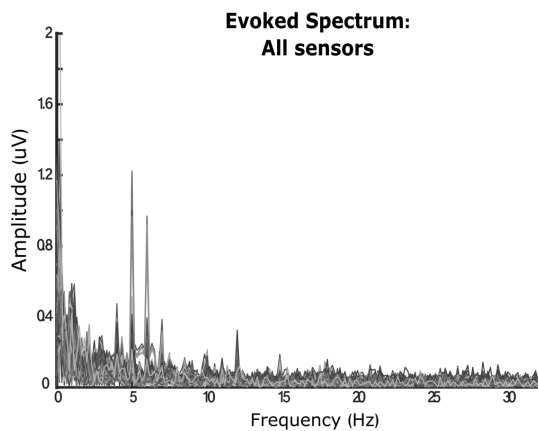
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802 Figure 3: Adult dataset plotted in the time domain as an event-related potential by averaging the trials in
 803 the third dimension. On the left, all 129 sensors are plotted. On the right, only the Oz sensor is plotted. The
 804 two vertical bars indicate the 6-second analysis time-window.

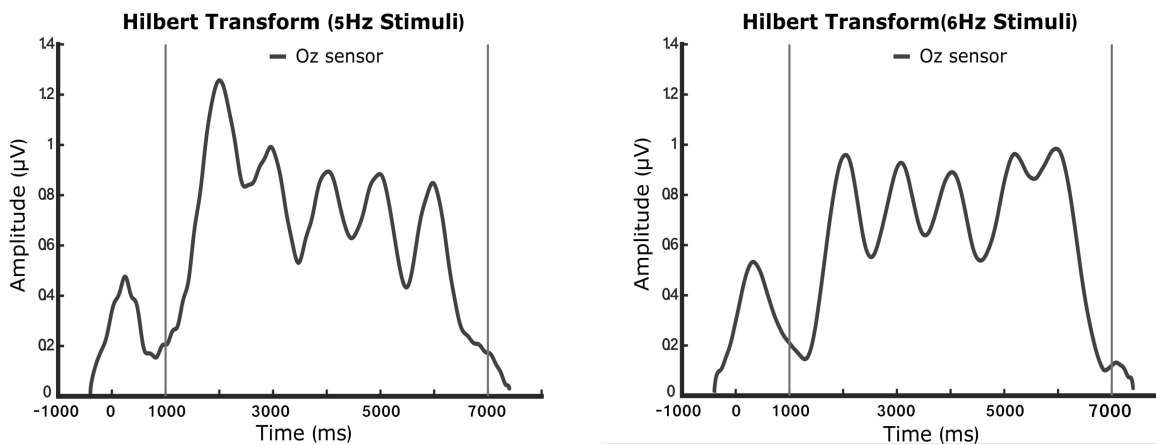
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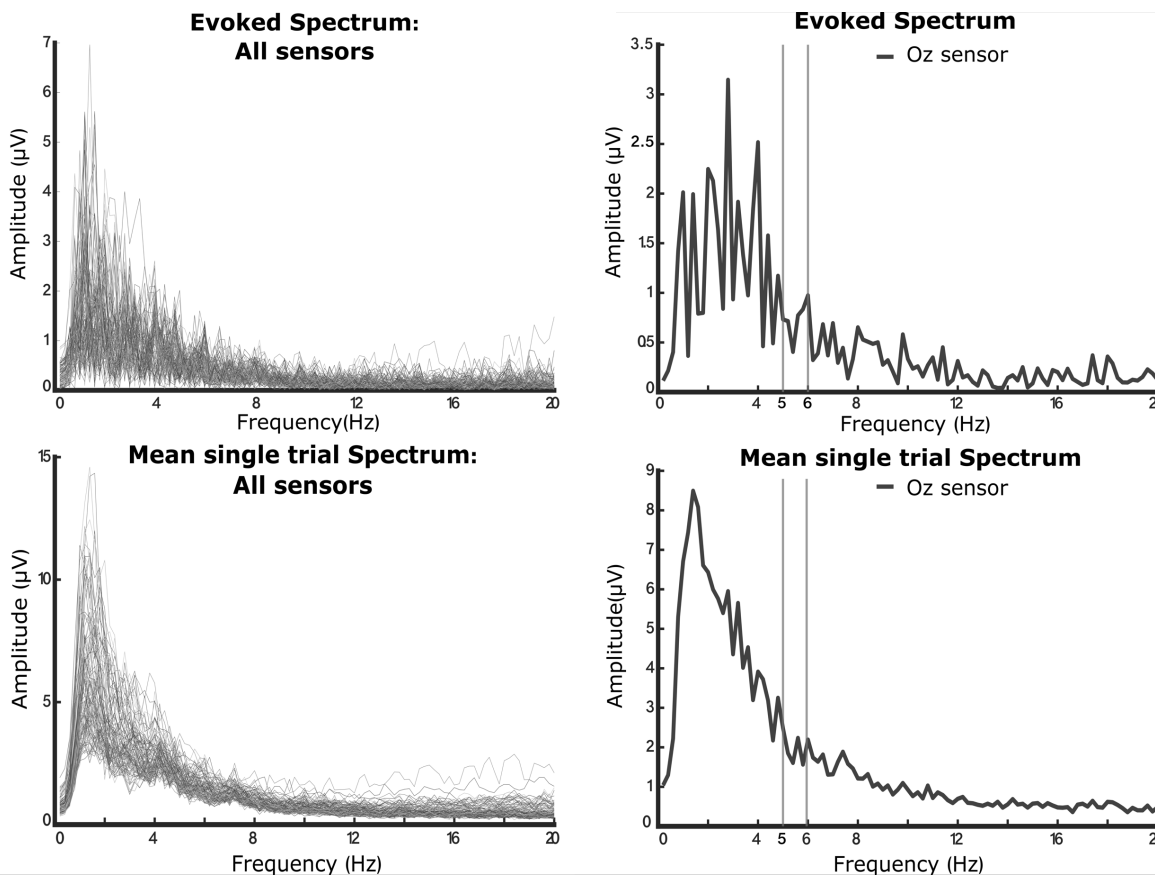
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807 Figure 4: Two ways of applying the Fourier Transform: On the top panel, trials are averaged in the time
 808 domain followed by the execution of the freqtag_FFT.m function. In this case, the averaging procedure
 809 aims at suppressing the activity that is not time-locked to the driving frequency. On the bottom panel, a
 810 Fourier Transform is applied in each trial and the resulting spectra is averaged, this is accomplished by the
 811 freqtag3D_FFT.m. If the phase varies across trials, researchers can benefit from the later approach. Plots

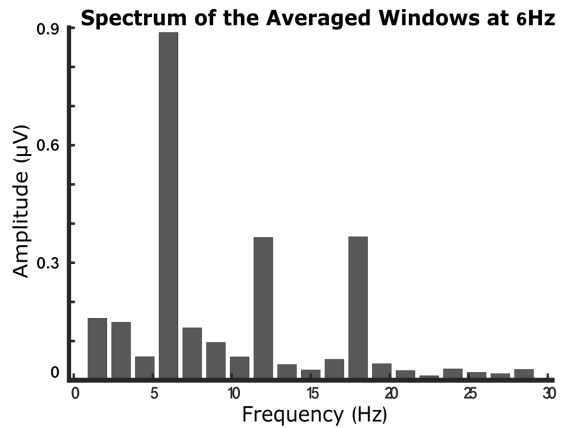
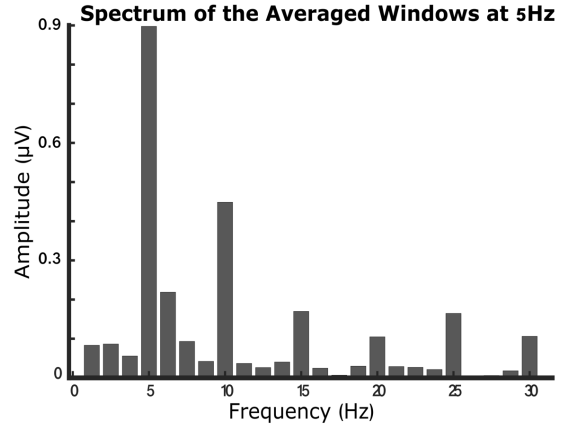
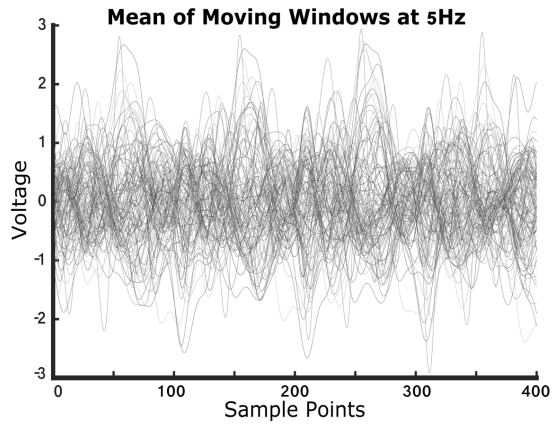
812 on the left column contain the amplitude information for each frequency; each sensor is a line. Plots on the
 813 right column, contain the information from the Oz sensor.



814
 815 Figure 5: The time-varying ssVEP amplitude envelopes of the 5Hz (on the left) and 6Hz (on the left) tagging
 816 frequencies. This plot can be drawn using the results from the freqtag_HILB.m function.



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 818 Figure 6: Amplitude spectra from the Fourier Transform applied to the infant data. The vertical bars indicate
 819 the tagging frequencies (5 and 6Hz). Although the spectra look as expected, it is not possible to obtain
 820 robust ssVEP response given the insufficient number of trials (less than 20). The evoked amplitude
 821 spectrum can be seen in the top panel, on the left, each electrode is a line and on the right the line represents
 822 the ssVEP amplitude at Oz. The mean amplitude of the single trial spectra is plotted on the bottom panel.



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824 Figure 7: Moving window estimates. On the left panel, each line is a sensor that combines the single trials
 825 time-domain information of the evoked ssVEP at 5Hz (top) and 6Hz (bottom). The time series
 826 (meanwinmat) obtained from the freqtag_slidewin.m can be projected in the frequency domain by means
 827 of Fourier Transform (freqtag_FFT.m). The right panel shows the amplitude spectra of the sliding-window
 828 at 5Hz (top) and 6hz (bottom).

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