1 Post-extinction recovery of the Phanerozoic oceans and the rise of biodiversity

- 2 hotspots
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23 Abstract

24 The fossil record of marine invertebrates has long fueled the debate as to whether or not there are limits to global diversity in the sea^{1–5}. Ecological theory states that as diversity grows 25 26 and ecological niches are filled, the strengthening of biological interactions imposes limits on diversitv^{6,7}. However, the extent to which biological interactions have constrained the growth 27 of diversity over evolutionary time remains an open question^{1–5,8–11}, largely because of the 28 incompleteness and spatial heterogeneity of the fossil record¹²⁻¹⁴. Here we present a regional 29 30 diversification model that reproduces the main Phanerozoic trends in the global diversity of marine invertebrates after imposing mass extinctions. We find that the dynamics of global 31 diversity is best described by a diversification model that operates broadly within the 32 exponential growth regime of a logistic function. A spatially resolved analysis of the diversity-33 34 to-carrying capacity ratio reveals that < 2% of the global flooded continental area throughout the Phanerozoic exhibits diversity levels approaching ecological saturation. We attribute the 35 overall increase in global diversity during the Late Mesozoic and Cenozoic to the 36 development of diversity hotspots under prolonged conditions of Earth system stability and 37 maximum continental fragmentation. We call this the "diversity hotspots hypothesis", which is 38 proposed as a non-mutually exclusive alternative to the hypothesis that the Mesozoic marine 39 revolution led this macroevolutionary trend^{15,16}. 40

41 **Main**

42 The guestion of whether or not there is an equilibrium diversity that the biota, or portions of the biota, cannot exceed has led to decades of debate between those who think that there is 43 44 a limit to the global diversity that the Earth can carry^{2,3,10} (i.e., a carrying capacity or saturation level) and those who think that diversity can increase in an unlimited fashion over time or, 45 alternatively, that the biosphere is so far from the equilibrium diversity (i.e., its carrying 46 47 capacity) that we can ignore the existence of any limit^{4,5,11}. This question has traditionally been addressed by examining the shape of global fossil diversity curves^{3,17}. For example, the 48 Paleozoic plateau in marine invertebrate diversity is generally taken as strong evidence for 49 the existence of ecological limits to further diversification^{3,18}. However, because diversity 50 varies dramatically among geographic regions, and each geographic region has its own 51 geological and environmental history, addressing this guestion requires simultaneously 52 reconstructing the dynamics of regional diversity in both space and time^{13,19}. If diversity 53 dynamics were governed by diversity-dependent feedbacks on speciation and extinction 54 rates, then regional diversity should remain stable regardless of time once carrying capacity 55 has been reached (i.e., the logistic model). The reasoning is the same as that used to explain 56 the logistic growth model in population dynamics in which the per capita rate of increase 57 decreases as the population approaches its maximum size or carrying capacity. Conversely, 58 if evolutionary rates were independent of standing diversities, then we should observe 59 60 positive relationships between evolutionary time-within-regions (or time-for-speciation) and diversity; the older the habitat the longer the lineages have had to diversify and fill empty 61 niches or explore new ones (i.e., the exponential model). The reasoning in this case is the 62 same as that used to explain the exponential growth model in population dynamics in which 63 the per capita rate of increase does not depend on the population size but only on the 64 modulating effects of environmental conditions. Determining which diversification model best 65

describes the dynamics of regional diversity over time is key to understanding the
mechanisms underlying biogeographic patterns and macroevolutionary trends. However, the
fossil record is biased by uneven geographic and stratigraphic sampling effort^{12,13} and
variation in the rock record available for sampling²⁰, hindering our ability to investigate the
effect of geographic variability in evolutionary time and diversification rate.

In order to overcome this limitation, we couple two alternative models of diversification -71 72 logistic and exponential - to a global model of palaeogeography and plate-motion that 73 constrains evolutionary time-within-regions (i.e. the age of the seafloor for the deep ocean and the time underwater for the flooded continental regions). In both diversification models, 74 the net diversification rate varies within a fixed range of values as a function of seawater 75 temperature and food supply, which are reconstructed using a spatially explicit Palaeo-Earth 76 77 system model (Methods). In the logistic model, the spatially resolved effective carrying capacities (Keff) are allowed to vary within a fixed range of values (Kmin and Kmax) as a positive 78 linear function of the food supply in each ocean region and time. We set relatively low Kmin 79 and K_{max} values (4 and 16 genera, respectively) to enforce diversity saturation, hereinafter 80 81 referred to as 'saturated' logistic model. Mass extinctions are imposed by imputing negative 82 net diversification rates to regional communities and assuming non-selective extinction. The 83 percentage of diversity loss as well as the starting time and duration of mass extinctions are extracted from three fossil diversity curves of reference, namely Sepkoski²¹, Alroy²² and 84 Zaffos et al²³. Each of these curves provides alternative insights into the Phanerozoic history 85 of marine animal diversity based on uncorrected range-through genus richness estimates^{21,23} 86 and sampling standardized estimates²². 87

88 Reconstructing global diversity dynamics

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Each of the two diversification models tested here produces a total of 82 spatially-explicit 89 reconstructions of diversity spanning from the Cambrian (541 Ma) to the present 90 (Supplementary Videos 1-2). On each of the 82 diversity distribution maps, we trace 91 hundreds of line transects from diversity peaks to their nearest diversity troughs and integrate 92 93 the total diversity in each transect by assuming a decay function in taxonomic similarity with geographic distance (Methods, Extended Data Fig. 1). Then, for each of the 82 time 94 intervals, all integrated diversities along transects are re-integrated step-wise, from the 95 96 transect with the greatest diversity to the transect with the lowest one, assuming the same 97 distance-decay function applied to individual transects. The resulting global diversity estimates are plotted against the mid-point value of the corresponding time interval to 98 generate a synthetic global diversity curve. Both the saturated logistic model and the 99 exponential model produce relatively similar global diversity dynamics (Fig. 1). This is 100 101 expected since the global diversity curves produced by both models were equally influenced 102 by mass extinctions as well as long-term variations in the global area of shallow shelf seas (Extended Data Fig. 2), which harbour the vast majority of the diversity of marine 103 104 invertebrates. However, while both models show similar diversity dynamics, the amplitudes of 105 global diversity variations differ markedly between models depending on whether or not regional-scale diversities self-limit their increase over time (Fig. 1). The exponential model 106 107 gives rise to conspicuous increases in global diversity from the Cambrian to Late Ordovician, Silurian to Early Devonian, Carboniferous (Early to Late Pennsylvanian), Early to Late 108 109 Cretaceous, and Paleocene to present. The Permian-Triassic mass extinction event lowered global diversity to Early Palaeozoic levels, but later diversification led Late Cretaceous and 110 Neogene faunas to exceed the Mid-Palaeozoic global diversity peak. These trends emerge 111 consistently regardless of the mass extinctions pattern imposed, be it Sepkoski²¹, Alroy²², or 112 Zaffos et al.²³ (Fig. 1). Nevertheless, it is worth noting how well the exponential model 113 reproduces the Sepkoski 'uncorrected' fossil diversity curve. The logistic model also 114

reproduces the initial increase in diversity, from Cambrian to Late Ordovician and from
Silurian to Early Devonian (Fig. 1). However, unlike the exponential model, in the saturated
logistic model this initial upward trend is followed by a convex diversity pattern interrupted by
a modest increase during the Cretaceous, which rarely exceeds the mid-Palaeozoic global
diversity peak in our set of simulations.

120 The calibrated logistic model

121 The logistic model allows the spatially-resolved effective carrying capacities (K_{eff}) to vary within a fixed range of values (from Kmin to Kmax) as a positive linear function of food 122 availability in each ocean region and time (Methods). All other things being equal, the higher 123 the K_{min} and K_{max} values, the longer the evolutionary time required to reach diversity 124 125 saturation. Consequently, the choice of K_{min} and K_{max} critically influences the extent to which regional biotas reach saturation. In order to calibrate the Kmin and Kmax parameters, we run 126 127 simulations of pair-wise K_{min} and K_{max} combinations in a geometric sequence of base 2, from 2 to 256 genera, and test the effect of changing the K_{min} and K_{max} values on the concordance 128 between the normalized diversities generated by the model and those estimated from the 129 fossil record. Unlike other correlation coefficients, Lin's concordance correlation 130 coefficient²⁴ (CCC) combines measures of both precision and accuracy to determine how far 131 the modelled data deviate from the line of perfect concordance. We focus the analysis on the 132 time series data between the end of one mass extinction and the beginning of the next, that 133 is, considering those time intervals dominated by rising diversity trajectories. Lin's CCC 134 increases with increasing K_{min} and K_{max} until reaching a plateau except for the mass extinction 135 pattern of Sepkoski for which it continues to increase even at the highest Kmin and Kmax values 136 (Extended Data Figs. 3-5). These results are consistently replicated using alternative values 137

for the parameters of the model that define the temperature- and food-dependence of the net
diversification rate (Extended Data Fig. 6, grey lines in insets, Extended Data Table 1).

Then, we re-run the logistic model using the average of all K_{min} and K_{max} combinations giving 140 141 a CCC greater than 0.70, hereinafter referred to as 'calibrated' logistic model. The calibrated model generates global diversity curves half way between the two end-member diversification 142 models, the saturated logistic and the exponential (Fig. 1). Most of the diversity is 143 144 concentrated in shallow marine environments, where high temperatures and abundant food 145 supplies increase the rates of diversification compared to the deep sea habitats (Fig. 2a-f, Extended Data Figs. 7-8). Diversity hotspots occur in tropical shelf seas of the Early 146 Devonian, Permian, Late Cretaceous and Cenozoic (Fig. 2c-f, Supplementary Video 3). 147 During the Early Devonian, diversity hotspots developed on the western continental margins 148 149 of Laurentia and Siberia as well as on the tropical shelves of Gondwana. The recovery of 150 Laurentian diversity hotspots after the Late Devonian mass extinction led to the onset of 151 Permian hotspots, which eventually disappeared during the Permian-Triassic mass extinction. Diversity hotspots became particularly prominent during the Late Cretaceous and Cenozoic in 152 the western basins of the Tethys Ocean, the Arabian Peninsula, the Atlantic Caribbean-East 153 Pacific and the Indo-West Pacific provinces (Fig. 2e-f). This temporal trend in the prominence 154 of diversity hotspots cannot be explained by a secular increase in the maximum lifetime of 155 shelf seas, a proxy for the maximum potential evolutionary time-within-regions. Geological 156 data from ancient continental margins trapped within orogenic belts²⁵ and global tectonic 157 reconstructions²⁶ (see seafloor age in **Supplementary Fig. 1**), show no evidence of an 158 increase in the lifespan of passive continental margins or in the maximum ages of the 159 seafloor over the Phanerozoic. Rather, we argue that the temporal proximity between the 160 Ordovician-Silurian (Hirnantian), Late Devonian (Frasnian-Famennian), and Permian-Triassic 161 162 mass extinctions, coinciding with a long-lived phase of continental coalescence and

destruction of marine shelves during the assembly of Pangaea, interrupted the full 163 development of diversity hotspots during the Palaeozoic. By contrast, the comparatively long 164 expanse of time that separated the mass extinctions of the end-Triassic and end-Cretaceous 165 extended the time-for-speciation under conditions of increasing continental fragmentation, 166 167 giving rise to exceptionally high-diversity regions before the Cretaceous-Paleogene mass extinction. The extraordinary diversity of Late Cretaceous hotspots ensured the continuity of 168 relatively high diversity levels in the aftermath of the end-Cretaceous mass extinction, 169 170 facilitating the subsequent development of diversity hotspots during the Cenozoic.

In order to evaluate the model's performance in reconstructing the spatial distributions of 171 diversity, we compare the results of the calibrated logistic model for the recent (i.e., 0 Ma) 172 with observations of marine invertebrates (crustaceans and molluscs) extracted from the 173 174 Ocean Biodiversity Information System (OBIS), a global database of occurrence records of 175 marine taxa (Methods). The regional diversity map generated by the model shows reasonable similarities to the observed diversity distributions along the continental margins (Fig. 2g-h). 176 The main discrepancies between the model and the OBIS data occur in the surroundings of 177 Australia and New Zealand, where the model underestimates diversity. Although the model 178 accounts for coastal re-colonization during marine transgressions, it lacks long-distance 179 dispersal, which precludes a more detailed reconstruction of the spatial structuring of diversity 180 in such a highly interconnected ocean region. Despite some regional discrepancies, both 181 182 observed and modeled diversity decline from the equator towards the poles (Fig. 2i-j), with most diversity concentrated in the Indo-West Pacific, the Atlantic Caribbean-East Pacific, and 183 the Mediterranean (Fig. 2g-h). 184

Using the outputs of the calibrated logistic model, we analyse the spatial and temporal
 variability of the diversity-to-carrying capacity (K_{eff}) ratio. This ratio provides a quantitative

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index of how far (ratios close to zero) or how close (ratios close to one) are the regional
faunas from noticing the effect of diversity-dependent ecological factors (i.e. the proximity to
diversity saturation). The diversity-to-K_{eff} ratio falls below 0.25 in most of the ocean and
throughout the Phanerozoic (**Fig. 3a-I**, **Supplementary Video 4**), supporting the idea that the
dynamics of regional diversity have been systematically operating below K_{eff} and, therefore,
far from diversity saturation.

Finally, we calculate the diversity-to- K_{eff} ratio along the flooded continental regions using the combinations of K_{min} and K_{max} that resulted from simulations with different parameter values (**Extended Data Fig. 6**, grey lines in insets, **Extended Data Table 1**), and represent its frequency distributions (**Fig. 3m-o**). Most of the estimates fall within the exponential growth regime of the logistic function (i.e. diversity-to- K_{eff} ratio < 0.25). On average, less than 10% of the estimates exceed the threshold of 0.25, and only < 2% of the estimates, those associated with well-developed diversity hotspots, exceed the threshold of 0.5.

200 A deliberate decrease of 25% in the K_{min} and K_{max} values of the model does not significantly 201 alter the shape of the diversity-to-K_{eff} ratio frequency distributions (Extended Data Fig. 9), 202 indicating that the resulting patterns are robust. Furthermore, the relatively short time elapsed 203 between successive Palaeozoic mass extinctions interrupted the development of diversity hotspots, preventing them from reaching saturation. In fact, by deactivating the Late 204 205 Devonian mass extinction in the model, we find that the full development of diversity hotspots before the end of the Permian leads to global diversities two to three times greater than those 206 generated by the same calibrated logistic model with all mass extinctions enabled (Extended 207 208 Data Fig. 10).

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209 Discussion

Our model corroborates earlier claims that Earth's environmental history^{5,27,28} and the patterns 210 of continental fragmentation and reassembly^{23,29,30} have been major determinants of marine 211 212 animal diversification. For example, we find that turning off plate tectonics prevents continental shelf habitats from repositioning along the latitudinal temperature gradient, 213 causing diversity to grow disproportionately in shelf seas that lie within the tropical belt 214 215 (Methods, Supplementary Fig. 2). The result is a rapid increase in global diversity that even 216 mass exitinctions cannot dampen (Supplementary Fig. 3a-c), and only effective carrying capacities prevent diversity from running away (Supplementary Fig. 3d-f). A static 217 geographic configuration also prevents diversity hotspots from disappearing at convergent 218 plate boundaries, further limiting the model's ability to reproduce the spatial distributions of 219 220 diversity and its global dynamics. Alternatively, by disabling the temperature and/or food dependence of the net diversification rate, the model produces unrealistic biogeographic 221 distributions, such as the occurrence of diversity hotspots in high-latitudes, leaving the growth 222 of diversity as a function of age (Methods, Supplementary Fig. 4). 223

224 Caveats? Sensitivity analyses (Extended Data Fig. 11) (this could be inserted HERE?)

Overall, we find that the temporal proximity between successive mass extinctions, along with 225 the long-term reduction in the global area of marine shelf during the assembly of Pangea, 226 interrupted the development of diversity hotspots throughout the Palaeozoic. In contrast, we 227 also find evidence of regional biota approaching diversity saturation at post-Palaeozoic 228 229 diversity hotspots, the development of which helps explain the increase in global diversity during the Late Mesozoic and Cenozoic. It has been hypothesized that the Mesozoic marine 230 revolution^{15,16}, that is, the emergence of shell-crushing predators and the consequent 231 232 ecological restructuring of marine ecosystems, was primarily responsible for the increase in 233 global diversity over the last 150 million years. The fact that our model can reproduce such an increase in diversity without the need to invoke evolutionary innovations like the emergence 234 of new modes of predation^{15,16}, defence^{15,31}, mobility³¹ or reproduction³², among others, raises 235 a new hypothesis based on how Earth's environmental history and palaeogeographic 236 237 evolution interacted in concert to allow the development of diversity hotspots. We call this the "diversity hotspots hypothesis", which is proposed as a non-mutually exclusive alternative to 238 the hypothesis that evolutionary innovation and new ecospace occupation led this 239 macroevolutionary trend. 240

We cannot reject the hypothesis that diversity saturation slowed down diversification in ocean 241 regions where marine faunas i) had long development times, ii) evolved rapidly and/or iii) 242 evolved from relatively high initial diversities. The differences between the global diversity 243 curves resulting from the exponential model and those generated by the calibrated logistic 244 model reveal the effect of ecological saturation on the dynamics of global diversity (Fig. 1). 245 However, with the possible exception of tropical diversity hotspots, our results indicate that 246 the diversity of marine invertebrates has remained below saturation throughout their 247 evolutionary history, shedding light on one of the most controversial topics in evolutionary 248 ecology^{1-5,8-11}. A taxonomic diversification model operating widely within the exponential 249

250 growth regime of the logistic function implies a concave-upward relationship between the magnitude of diversity loss (x-axis) and the subsequent rebuilding time. This mode of 251 diversification provides a plausible explanation for the observed decoupling between mass 252 extinctions and explosive evolutionary radiations over the Phanerozoic³³. We envision that 253 254 our spatially-explicit reconstructions of diversity could shed light on other long-standing questions in (palaeo)biogeography and macroevolution and, increasing a synthetic spatially-255 resolved history of biodiversity through geological time, will provide a means of exploring 256 sampling biases in the fossil record. 257

258 Methods

259 Palaeogeographic model

We use palaeogeographic reconstructions describing Earth's palaeotopography and
palaeobathymetry for a series of time slices from 541 Ma to the present day. The
reconstructions merge existing models from two published global reconstruction datasets,
those of Merdith et al³⁴ and Scotese and Wright³⁵ (https://doi.org/10.5281/zenodo.5348492),
which themselves are syntheses of a wealth of previous work.

For continental regions, estimates of palaeoelevation and continental flooding rely on a 265 diverse range of geological evidence such as sedimentary depositional environments and the 266 267 spatio-temporal distribution of volcanic activity. For a full description, see the recent review of Scotese³⁶. Together, these data can be used to define the past locations of mountain ranges 268 and palaeoshorelines³⁶. For this part of our reconstruction, we use the compilation of Scotese 269 and Wright³⁵ with updated palaeoshorelines based on depositional environment information in 270 current fossil databases³⁷. This compilation comprises 82 palaeotopography maps covering 271 the entire Phanerozoic. It is important to note that each palaeogeographic map is a time-slice 272 representing the concatenation of geological data over several million years³⁸. Eustatic sea-273 level is thought to have varied by ~100 m at timescales much shorter than the duration of the 274 time-slices throughout the Phanerozoic³⁹, so that the extent of continental flooding could have 275 varied within each time-slice by an amount significant for our analysis. For this reason, and to 276 assess the uncertainty of our results to continental palaeogeography in general, we compute 277 additional maps of continental flooding for the analysis below in which the sea-level is raised 278 279 or lowered by 100 m compared to the original paleoDEM grids of Scotese and Wright³⁵. The

curves obtained differ very little from the original curves except for Zaffos et al²³ in which the
 Cenozoic rise in diversity is more prominent (Extended Data Fig. 11).

For deep ocean regions, the primary control on seafloor depth is the age of the seafloor, so 282 283 reconstructing palaeobathymetry relies on constructing maps of seafloor age back in time⁴⁰. Consequently, we rely on reconstruction models that incorporate a continuous network of 284 plate boundaries. These models allow us to derive maps of seafloor age in deep time. For 285 this part, we use the reconstruction of Merdith et al³⁴ and derive maps of seafloor age from 286 287 the plate tectonic model using the method of Williams et al⁴¹, for which source code is available at https://github.com/siwill22/agegrid-0.1. Palaeobathymetry is derived from the 288 seafloor age maps following the steps outlined by Müller et al⁴⁰. It is important to note that 289 seafloor age maps for most of the Phanerozoic (i.e. pre-Pangea times) are not directly 290 291 constrained by data due to recycling of oceanic crust at subduction zones. Rather, they are model predictions generated by constructing plate motions and plate boundary configurations 292 from the geological and palaeomagnetic record of the continents. Nonetheless, the first-order 293 294 trends in ocean-basin volume and mean seafloor age are consistent with independent 295 estimates for at least the last 410 Myr⁴¹.

The reconstructions of Merdith et al³⁴ and Scotese and Wright³⁵ differ in the precise locations 296 of the continents through time. To resolve this discrepancy, we reverse reconstruct the 297 Scotese and Wright³⁵ continental palaeoelevation model to present-day coordinates using 298 their rotation parameters, then reconstruct them back in time using the rotations of Merdith et 299 al³⁴. Due to the differences in how the continents are divided into different tectonic units, this 300 process leads to some gaps and overlaps in the results⁴², which we resolve primarily through 301 302 a combination of data interpolation and averaging. Manual adjustments are made to ensure 303 that the flooding history remains consistent with the original palaeotopography in areas where interpolation gives a noticeably different history of seafloor ages. The resulting
 palaeotopography maps are thus defined in palaeomagnetic reference frame³⁴ appropriate for
 use in Earth System models.

For the biodiversity modelling, we generate estimates of the age of the seafloor for discrete points within the oceans and flooded continents, and track these ages through the lifetime of each point. For the oceans, this is achieved using the method described by Williams et al⁴¹ where the seafloor is represented by points incrementally generated at the mid-ocean ridges for a series of time-step 1 Myr apart, with each point tracked through subsequent timesteps based on Euler poles of rotation until either present-day is reached, or they arrive at a subduction zone and are considered destroyed.

314 For the continents, tracking the location of discrete points is generally simpler since most crust is conserved throughout the timespan of the reconstruction. Unlike the deep oceans 315 (where we assume that crust is at all times submerged), we model the 'age' of the seafloor 316 317 from the history of continental flooding and emergence within the palaeogeographic 318 interpretation³⁵. The continents are seeded with uniformly distributed points at the oldest timeslice (541 Ma) where they are assigned an age of zero. These points are tracked to 319 320 subsequent time slices where the palaeogeography is used to determine whether the point lies within a flooded or emergent region. Points within flooded regions of continents are 321 322 considered to be seafloor, and the age of this seafloor is accumulated across consecutive time slices where a given point lies within a flooded region. When a point is within an 323 emergent region, the seafloor age is reset to zero. Following this approach, individual points 324 within stable continents may undergo several cycles of seafloor age increasing from zero 325 before being reset. At the continental margins formed during Pangea breakup, the age of the 326 seafloor continuously grows from the onset of rifting. Intra-oceanic island arcs represent an 327

additional case, which can appear as new tectonic units with the reconstructions at various
times. In these cases, we assume that the seafloor has a zero-age at the time the intraoceanic arc first develops, then remains predominantly underwater for the rest of its lifetime.
The estimated age of the seafloor of open ocean regions and the estimated time that flooded
continental shelves spend underwater using the approach described in this section is shown
in Supplementary figure 1.

Therefore, for each of the 82 palaeogeographic reconstructions, we annotate 0.5° by 0.5° grids as continental, flooded continental shelf, or oceanic for later use in model coupling and production of regional diversity maps.

337 Palaeo-environmental conditions: cGenie Earth System model

We use cGENIE⁴³, an Earth System model of intermediate complexity, to simulate palaeoenvironmental conditions of seawater temperature and organic carbon export production (as a surrogate for food supply) throughout the Phanerozoic (from 541 Ma to present day).

cGENIE is based on a 3-dimensional (3D) ocean circulation model coupled to a 2D energymoisture-balance atmospheric component and a sea-ice module. We configure the model on
a 36×36 (lat, lon) equal area grid with 17 unevenly spaced vertical levels in depth, down to a
maximum ocean depth of 5,900 m. The cycling of carbon and associated tracers in the ocean
is based on a size-structured plankton ecosystem model with a single (phosphate)
nutrient^{44,45}, and adopts an Arrhenius-type temperature-dependent scheme for the
remineralization of organic matter exported to the ocean interior⁴⁶.

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cGENIE provides a spatially resolved representation of ocean physics and biogeochemistry, which is a prerequisite for the present study to be able to reconstruct the spatial patterns of biodiversity in deep time. However, because of the computational impracticality of generating a single transient simulation of physics (i.e., temperature) and biogeochemistry (i.e., export production) over the entire Phanerozoic, we therefore generate 30 model equilibria at regular time intervals throughout the Phanerozoic which are subsequently used as inputs for the regional diversification model (see the Methods section Model coupling).

356 We employed 30 Phanerozoic palaeogeographic reconstructions through time (~20 Myr evenly spaced time intervals) produced by the plate tectonic/palaeo-elevation model to 357 represent key time periods. For each continental configuration corresponding to a given age 358 in Earth history, we generate idealized 2D wind speed and wind stress, and 1D zonally-359 360 averaged albedo forcing fields⁴⁷ required by the cGENIE model using the 'muffingen' opensource software (see code availability section below). For each palaeogeographic 361 362 reconstruction, the climatic forcing (i.e., solar irradiance and carbon dioxide concentration) is adapted to match the corresponding geological time interval. The pCO_2 is taken from the 363 recent update of the GEOCARB model⁴⁸. Solar luminosity is calculated using the model of 364 stellar physics of Gough⁴⁹. We impose modern-day orbital parameters (obliquity, eccentricity 365 and precession). The simulations are initialized with a sea-ice free ocean, homogeneous 366 oceanic temperature (5 °C), salinity (34.9 ‰) and phosphate concentration (2.159 µmol kg⁻¹). 367 Because variations in the oceanic concentration of bio-available phosphate remain 368 challenging to reconstruct in the geological past^{50,51}, we impose a present-day mean ocean 369 phosphate concentration in our baseline simulations. We quantify the impact of this 370 uncertainty on our model results by conducting additional simulations using half and twice the 371 present-day ocean phosphate concentration (Extended Data Fig. 11). For each ocean 372 phosphate scenario (i.e., 0.5×, 1× and 2× the present-day value), each of the 30 model 373

simulations is then integrated for 20,000 years, a duration ensuring that deep-ocean temperature and geochemistry reach equilibrium. For each model simulation, results of the mean annual values of the last simulated year are used for the analysis. Note that although cGENIE makes projections of the distribution of dissolved oxygen ([O2]) in the ocean, our diversification model does NOT currently consider oxygenation as a limit on diversity. We hence assumed modern atmospheric pCO₂ in all 30 palaeo simulations and did not utilize the resulting projected [O₂] fields.

381 Regional diversification model

We test two models of diversification, the logistic model and the exponential model, describing the dynamics of regional diversity over time. In both models, the net diversification rate (p), with units of inverse time (Myr⁻¹), varies within a pre-fixed range of values as a function of seawater temperature and food availability. The net diversification rate is then calculated for a given location and time according to the following equation:

387
$$\rho = \rho_{max} - (\rho_{max} - \rho_{min})(1 - Q_{temp}Q_{food})$$
 Equation 1

where ρ_{min} and ρ_{max} set the lower and upper net diversification rate limits within which ρ is allowed to vary, and Q_{temp} and Q_{food} are non-dimensional limitation terms with values between 0 and 1 that define the dependence of ρ on temperature and food, respectively (see **Supplementary Table 1**). These temperature and food supply limitation terms vary in space and time as a result of changes in seawater temperature and particulate organic carbon export rate, respectively, thereby controlling the spatial and temporal variability of ρ .

394 The temperature-dependence of ρ is calculated using the following equation:

$$Q_{temp} = \frac{\frac{Q_{10}^{T-Tmin}}{Q_{10}^{Tmax-Tmin}}}{Q_{10}^{Tmax-Tmin}}$$

395

Equation 2

where the Q₁₀ coefficient measures the temperature sensitivity of the origination rate. In the 396 equation 2 above, T is the seawater temperature (in °C) at a given location and time, while 397 T_{min} and T_{max} are the 0.01 percentile and the 0.99 percentile, respectively, of the temperature 398 frequency distribution in each time interval. In the model, the values of T_{min} and T_{max} used to 399 calculate Q_{temp} are thus recomputed every time interval (~ 5 Myr) according to the 400 temperature frequency distribution of the corresponding time interval. This allows having 401 updated T_{min} and T_{max} in each Phanerozoic time interval and account for the thermal 402 adaptation of organisms to ever-changing climate conditions. 403

404 The food limitation term is parameterized using a Michaelis-Menten formulation as follows:

405
$$Q_{food} = \frac{POC flux}{(K_{food} + POC flux)}$$
 Equation 3

where POC flux (mol m⁻² year⁻¹) is the particulate organic carbon export flux, which is used as 406 a surrogate for food availability, at a given location and time of the simulated seafloor. The 407 parameter K_{food} (mol m⁻² year⁻¹) in equation 3 is the half-saturation constant, that is, the POC 408 flux at which the diversification rate is half its maximum value, provided that other factors 409 were not limiting. Supplementary figure 5 shows the interactive effect of temperature and 410 411 food supply on net diversification rate for the Q₁₀ and K_{food} coefficients used to run the main simulations (i.e. $Q_{10} = 1.75$, $K_{food} = 0.5$ mol C m⁻²y⁻¹) and two extreme parameter settings (i.e. 412 Q_{10} = 1.5 and 2.5, K_{food} = 0.25 and 1 mol C m⁻²y⁻¹). Supplementary figure 6 shows the 413

spatial variability of the net diversification rate for 6 representative time-slices in the
Phanerozoic using the default settings.

The model considers a direct relationship between seawater temperature, food supply and 416 417 the rate of net diversification based on the theoretical control that temperature and food supply exert on the rates of origination and extinction (Supplementary Fig. 5). Temperature 418 rise is expected to accelerate the biochemical kinetics of metabolism⁵² and shorten the 419 development times of individuals⁵³, leading to higher rates of mutation and origination. 420 421 Greater food availability increases population sizes, which increases the rates of mutation and reduces the probability of extinction⁵⁴. Furthermore, a large body of observations shows 422 the existence of a positive relationship between resource availability (i.e. food supply) and the 423 standing stock of species in marine and terrestrial communities^{55,56}. A larger food supply 424 425 would support a greater number of individuals. A greater diversity of food resources could 426 also lead to a finer partitioning of resources and a more efficient exploitation of the ecospace.

The net diversification rate becomes negative i) in the event of mass extinctions or ii) in 427 response to regional-scale processes, such as sea-level fall and/or seafloor deformation 428 along convergent plate boundaries. Mass extinction events are imposed as external 429 perturbations to the diversification model by imputing negative net diversification rates to all 430 active seafloor points (ocean points and flooded continental points) and assuming non-431 selective extinction. The percentage of diversity loss as well as the starting time and duration 432 of mass extinctions are extracted from three fossil diversity curves of reference, namely 433 Sepkoski²¹, Alroy²² and Zaffos et al²³ (**Supplementary Fig. 7**). Each of these fossil diversity 434 curves provides different insights into the Phanerozoic history of marine animal diversity 435 based on uncorrected range-through genus richness estimates^{21,23} and sampling 436 standardized estimates²². Regional-scale processes, such as sea level fall during marine 437

regressions and/or seafloor destruction at plate boundaries, either by subduction or uplift, are
simulated by the combined plate tectonic/palaeo-elevation model, and constrain the time that
seafloor habitats have to accumulate diversity.

441 The model assumes non-selective extinction during mass extinction events (i.e., the field of bullets model of extinction; everything is equally likely to die, no matter the age of the clade 442 and regardless of adaptation)⁵⁷. However, there is much fossil evidence supporting extinction 443 selectivity^{58,59}. It could be argued that higher extinction rates at diversity hotspots would have 444 445 delayed their subsequent recovery, flattening global diversity trends. This is so considering that, in an exponential diversification model, diversity enhances diversification, leading to a 446 non-linear relationship between the magnitude of diversity loss and the subsequent rebuilding 447 time. This argument is difficult to reconcile with Sepkoski's genus-level global diversity curve 448 but could be consistent with Alroy's standardized diversity curve. Likewise, the model is also 449 not suitable for reproducing the explosive radiations of certain taxonomic groups after mass 450 extinctions, which could explain the offset between the model and fossil observations in the 451 Early Mesozoic (Fig. 1). 452

Letting D represent regional diversity (number of genera within a given seafloor point) and t represent time, the logistic model is formalized by the following differential equation:

455 $\frac{\partial D(t)}{\partial t} = \rho D [1 - \frac{D}{K_{\text{eff}}}]$ Equation 4

where D(t) is the number of genera at time t and K_{eff} is the effective carrying capacity or
maximum number of genera that a given seafloor point (i.e., grid cell area after gridding) can
carry at that time, t. In our logistic model, K_{eff} is allowed to vary within a fixed range of values

(from K_{min} to K_{max}) as a positive linear function of the POC flux at a given location and time as
follows:

461
$$K_{eff} = K_{max} - (K_{max} - K_{min}) \frac{POC flux_{max} - POC flux}{POC flux_{max} - POC flux_{min}}$$
 Equation 5

where POC flux_{min} and POC flux_{max} corresponds to the 0.01 and 0.99 quantiles of the POC
flux range in the whole Phanerozoic dataset.

In the logistic model, the net diversification rate decreases as regional diversity approaches its K_{eff}. The exponential model is a particular case of the logistic model when K_{eff} approaches infinity and, therefore, neither the origination rate nor the extinction rate depend on the standing diversities. In this scenario, diversity grows in an unlimited fashion over time only truncated by the impact of mass extinctions and/or by the dynamics of the seafloor (creation versus destruction). The exponential model is thus as follows:

470
$$\frac{\partial D(t)}{\partial t} = \rho D$$
 Equation 6

where the rate of change of diversity (the time derivative) is proportional to the standing diversity *D* such that the regional diversity will follow an exponential increase in time at a speed controlled by the temperature- and food-dependent net diversification rate. Even if analytical solutions exist for the steady-state equilibrium of the logistic and exponential functions, we solved the ordinary differential equations (4) and (6) using numerical methods with a time lag of 1 Myr to account for the spatially- and temporally-varying environmental constraints, seafloor dynamics, and mass extinction events. Because the analysis of global fossil diversity curves is unable to discern the causes of diversity loss during mass extinctions, our imputation of negative diversification rates could have overestimated the loss of diversity in those cases in which sea level fall, a factor already accounted for by our model, contributed to mass extinction. This effect was particularly recognizable across the Permo-Triassic mass extinction (**Extended Data Fig. 10**), and supports previous claims that the decline in the global area of the shallow water shelf exacerbated the severity of the end-Permian mass extinction³⁶.

485 Model coupling

As stated above, the coupled plate tectonic/palaeo-elevation (palaeogeographic) model 486 corresponds to a tracer-based model (a Lagrangian-based approach) that simulates and 487 tracks the spatio-temporal dynamics of ocean and flooded continental points. The 488 diversification models start at time 541 Ma with all active points having a D₀ = 1 (one single 489 genus everywhere) and we let points accumulate diversity heterogeneously with time 490 according to seafloor age distributions (for ocean points) and the time that continents have 491 been underwater (for flooded continental points). The ocean points are created at mid-ocean 492 ridges and disappear primarily at subduction zones. Between their origin and demise, the 493 points move following plate tectonic motions and we trace their positions while accumulating 494 diversity. The flooded continental points begin to accumulate diversity from the moment they 495 are submerged, starting with a D value equal to the nearest neighbour flooded continental 496 point with D > 1, thereby simulating a process of coastal re-colonization (or immigration). The 497 diversification process remains active while the seafloor points remain underwater, but it is 498 interrupted, and D set to 0, in those continental points that emerge above sea level. Likewise, 499 seafloor points corresponding to ocean domains disappear in subduction zones, and their 500 501 diversity is lost. We track the geographic position of the ocean and flooded continental points

approximately every 5 Myr, from 541 Ma to the present. Each and every one of the tracked
points accumulates diversity over time at a different rate, which is modulated by the
environmental history (seawater temperature and food availability) of each point, as
described in equations 1-3. When a point arrives in an environment with a carrying capacity
lower than the diversity it has accumulated through time, we reset the diversity of the point to
the value of the carrying capacity, thereby simulating local extinction.

508 Seawater temperature (T) and food availability (POC flux) are provided by the cGENIE 509 model, which has a spatial and temporal resolution coarser than the palaeogeographic model. The cGENIE model provides average seawater T and POC flux values in a 36×36 510 equal area grid (grid cell area equivalent to 2° latitude by 10° longitude at the equator) and 30 511 time slices or snapshots (from 541 Ma to present: each ~20 Myr time intervals). To have 512 513 environmental inputs for the 82 time slices of the plate tectonic/palaeo-elevation model, we first interpolate the cGENIE original model output data on a 0.5° by 0.5° grid to match the 514 annotated grids provided by the plate tectonic/palaeo-elevation model. Because the relatively 515 coarse spatial resolution of the cGENIE model prevents rendering the coast-ocean gradients, 516 we assign surface T and POC flux at the base of the euphotic zone to the flooded continental 517 shelf grid cells, and deep ocean T and POC flux at the bottom of the ocean to the ocean grid 518 cells. Because there are time slices without input data of seawater T and POC flux, we 519 inter/extrapolate seawater T and POC flux values into the 0.5° by 0.5° flooded continental 520 shelf and ocean grids independently. Finally, we interpolate values from these 0.5° by 0.5° 521 flooded continental shelf and ocean grids into the exact point locations in each time frame. 522 Therefore, each active point is tracked with its associated time-varying T and POC flux values 523 throughout its lifetime. On average, 6,000 flooded continental points and 44,000 oceanic 524 points were actively accumulating diversity in each time frame. The model cannot simulate 525 the singularities of relatively small enclosed seas for which the spatial resolution of the 526

palaeogeographic and Earth system models is insufficient to capture relevant features (palaeobathymetry, seawater temperature, etc) in detail. The method is also likely to underestimate the diversity of epeiric (inland) seas due to the difficulty of simulating immigration, a process that is strongly influenced by the effect of marine currents and is not considered here. However, as stated above, the model considers recolonization of recently submerged areas from nearby coastal environments, which partially explains coastal immigration.

534 Estimation of global diversity from regional diversity

Our regional diversity maps are generated by separately interpolating ocean point diversity 535 and flooded continental point diversity into the 0.5° by 0.5° annotated grids provided by the 536 537 palaeogeographic model. We calculate global diversity at each time step from each of the regional diversity maps following a series of steps to integrate diversity along line transects 538 from diversity peaks (maxima) to diversity troughs (minima) (Extended Data Fig. 1). To 539 select the transects, first, we identify on each of the regional diversity maps the geographic 540 position of the diversity peaks. We identify local maxima (i.e., grid cells with diversity greater 541 than their neighbour cells), and define the peaks as those local maxima with diversity greater 542 than the 0.75 quantile of diversity values in all local maxima in the map. In the case of grid 543 cells with equal neighbour diversity, the peak is assigned to the grid cell in the middle. We 544 subsequently identify the geographic position of the diversity troughs, which are defined as 545 newly formed ocean grid cells (age = 0 Myr) and, therefore, with diversities equal to one. The 546 troughs are mostly located at mid-ocean ridges. 547

548 On each of the 82 spatial diversity maps, we trace a line transect from each diversity peak to 549 its closest trough, provided that the transect does not cross land in more than 20 % of the grid cells along the linear path. On average, for each spatial diversity map, we trace 400 ($\sigma = \pm 75$) linear transects. This sampling design gives rise to transects of different lengths, which may bias the estimates of global diversity. To minimize this bias, we cut the tail of the transects to have a length of 555 km equivalent to 5° at the equator. We test an alternative cutoff threshold; 1110 km, and the results do not alter the study's conclusions.

We apply Bresenham's line algorithm⁶⁰ to detect the grid cells crossed by the transects and 555 556 annotate their diversity. To integrate regional diversity along the transects, we develop a 557 method to simplify the scenario of peaks and troughs heterogeneously distributed on the 2D diversity maps. The method requires i) a vector (the transect) of genus richness (α_n) at n 558 different locations (grids) arranged in a line (1D) of L grids, and ii) a coefficient of similarity 559 $(V_{n,n+1})$ between each two neighbouring locations, n and n+1. $V_{n,n+1}$, the coefficient of 560 561 similarity, follows a decreasing exponential function with distance between locations. The number of shared genera between n and n+1 is $V_{n,n+1}$ *min(α_n ; α_{n+1}). We integrate diversity 562 from peaks to troughs and assume that, along the transect, α_{n+1} is lower than α_n . We further 563 assume that the genera present in n and n+2 cannot be absent from n+1. Using this method, 564 we integrate the transect's diversity (γ_i) using the following equation: 565

566
$$\gamma_i = \alpha_1 + \sum_{n=1}^{L-1} (1 - V_{n,n+1}) \alpha_{n+1}$$
 Equation 7

To integrate the diversity of all transects (γ_i) on each 2D diversity map (or time slice), we apply the same procedure as described above (**Extended Data Fig. 1**). We first sort the transects in descending order from the highest to the lowest diversity. Then, we assume that the number of shared genera between transect i and the rest of the transects with greater diversity {1, 2,..., i -1} is given by the distance of its peak to the nearest neighbour peak [NN(i)] of those already integrated {1,2,... i -1}. Thus, we perform a zigzag integration of transects' diversities down gradient, from the greatest to the poorest, weighted by the nearest neighbour distance among the peaks already integrated. As a result, the contribution of each transect to global diversity will depend on its diversity and its distance to the closest transect out of all those transects already integrated. With this method, we linearize the problem to simplify the cumbersome procedure of passing from a 2D regional diversity map to a global diversity estimate without knowing the identity (taxonomic affiliation) of the genera. If γ_{total} is the global diversity at time t:

580
$$\gamma_{\text{total}} = \gamma_1 + \sum_{i=2}^{I} (1 - V_{NN(i),i}) \gamma_i$$
 Equation 8

581 Finally, the resulting global estimates are plotted against the mid point value of the 582 corresponding time interval to generate a synthetic global diversity curve. In order to compare the global diversity curves produced by the diversification models with those composed from 583 the fossil record, Lin's concordance correlation coefficient (CCC)²⁴ is applied to the data 584 normalized to the min-max values of each time series (i.e., rescaled within the range 0-1). 585 Lin's CCC combines measures of both precision and accuracy to determine how far the 586 observed data deviate from the line of perfect concordance or gold standard (that is, the 1:1 587 line). Lin's CCC increases in value as a function of the nearness of the data's reduced major 588 axis to the line of perfect concordance (the accuracy of the data) and of the tightness of the 589 590 data around its reduced major axis (the precision of the data).

591 Model parameterization and calibration

The diversification models are parameterized assuming a range of values that constrain the lower and upper limits of the genus-level net diversification rate (ρ_{min} and ρ_{max} , respectively) (**Supplementary Table 1**) according to previously reported estimates from fossil records (Figures 8 and 11 of Stanley⁵). A range of realistic values is assigned for the parameters Q₁₀ and K_{food} (**Supplementary Table 1**), determining, respectively, the thermal sensitivity and food dependence of the net diversification rate. We test a total of 40 different combinations of parameter settings (**Extended Data Table 1**). The resulting estimates of diversity are then compared against the fossil diversity curves of Sepkoski²¹, Alroy²², or Zaffos et al.²³, and the 15 parameter settings providing the highest CCCs are selected.

601 The results of the logistic diversification model rely on the values of the minimum and 602 maximum carrying capacities (K_{min} and K_{max}, respectively) within which the spatially-resolved effective carrying capacities (Keff) are allowed to vary. The values of Kmin and Kmax are thus 603 calibrated by running 28 simulations of pair-wise Kmin and Kmax combinations increasing in a 604 geometric sequence of base 2, from 2 to 256 genera (Extended Data Figs. 3-5). We perform 605 606 these simulations independently for each of the 15 parameter settings selected previously (Extended Data Fig. 6, Extended Data Table 1). Each combination of Kmin and Kmax 607 produces a global diversity curve, which is evaluated as described above using Lin's CCC. 608

609 Calculating estimates of global diversity from regional diversity maps in the absence of 610 information on genus-level taxonomic identities requires we assume a spatial turnover of taxa with geographic distance (Extended Data Fig. 1). Distance-decay curves are routinely fitted 611 by calculating the ecological similarity (e.g. Jaccard similarity index) between each pair of 612 613 sampling sites, and fitting an exponential decay function to the points on a scatter plot of similarity (y-axis) versus distance (x-axis). Following this method, we fit an exponential decay 614 function to the distance-decay curves reported in Miller et al⁶¹, depicting the decrease in the 615 Jaccard similarity index (J) of fossil genera with geographic distance (great circle distance) at 616 617 different Phanerozoic time intervals:

618

Equation 9

where $J_{off} = 0.06$ (n.d.) is a small offset, $J_{max} = 1.0$ (n.d.) is the maximum value of the genusbased Jaccard similarity index, and $\lambda = 0.0024$ (Km⁻¹) is the distance-decay rate.

The Jaccard similarity index (J) between consecutive points n and n+1 is bounded between 0 621 and min(α_n ; α_{n+1})/max(α_n ; α_{n+1}). A larger value for J would mean that there are more shared 622 623 genera between the two communities than there are genera within the least diverse 624 community, which is ecologically absurd. However, using a single similarity decay function can lead the computed value of J to be locally larger than min(α_n ; $\alpha_{n+1}/\max(\alpha_n; \alpha_{n+1})$). To 625 prevent this artefact, we use the Simpson similarity index or "overlap coefficient" (V) instead 626 of J. V corresponds to the percentage of shared genera with respect to the least diverse 627 628 community $(\min(\alpha_n; \alpha_{n+1}))$. V is bounded between 0 and 1, whatever the ratio of diversities. As the pre-existing estimates of similarity are expressed using J⁶¹, we make the conversion 629 from J to V using the algebraic expression V = (1 + R) * J / (1 + J) where R = max(α_n ; 630 α_{n+1} /min(α_n ; α_{n+1}) (see **Annex 1**). In the cases in which J exceeds the min(α_n ; α_{n+1})/max(α_n ; 631 α_{n+1}), V becomes > 1 and, in those cases, we force V to be <1 by assuming R = 1, that is α_n 632 633 $= \alpha_{n+1}$.

The model considers a single distance-decay function for the spatial turnover of taxonomic composition. However, the degree of provinciality (i.e., the partitioning of life into distinct biogeographic units) varies in space and time as a result of environmental gradients⁶² and plate tectonics⁶³. In fact, the increase in provinciality has been invoked as the main driver of the increase in global diversity, especially in the Late Cretaceous and Cenozoic^{23,62,63}. This is a deficiency of the model. Unfortunately, information on the extent to which marine provinciality has varied in space and time throughout the Phanerozoic is limited^{61,62}, and there

is no simple (mechanistic) way to implement different distance-decay functions of taxonomic 641 similarity in the model. We speculate that including some degree of provincialism in our 642 643 model could produce the following. There is a clear difference between longitudinal and latitudinal distance, the latter being a more significant source of taxonomic turnover⁶². This 644 645 effect would add to the observation that tropical diversity hotspots became more prominent towards the end of the Phanerozoic, offering two complementary explanations for the 646 increase in diversity in the Mesozoic: i) favourable conditions for the development of diversity 647 648 hotspots and ii) a higher degree of provinciality.

649 Regarding the comparison of model outputs with the fossil record, because the purpose of 650 this modeling study is to reconstruct the unknown dynamics of diversity within regions, we 651 adopted the strategy of spatially integrating regional diversity from our maps and comparing the resulting global diversity curves with the global diversity curves reconstructed from the 652 fossil record (see next section). The comparison between the modelled and fossil global 653 diversity curves is justified by the fact that the dynamics of global diversity should be 654 655 quantitatively less biased than the dynamics of diversity within regions. Ultimately, our spatially resolved diversification model is intended to provide a benchmark for exploring 656 diversity in those contrasting regions and/or time intervals for which the fossil record is most 657 biased, incomplete, or non-existent. However, it would be interesting to compare the results 658 659 of the model against the fossil record, at least for those contrasting regions and/or time intervals for which the fossil record is better preserved/sampled. This comparison would allow 660 us to further test the reliability of the model and identify issues from which to improve the 661 model. 662

663 Fossil data

We use three fossil diversity curves of reference, namely, Sepkoski, Alroy, and Zaffos et al, in 664 order to i) extract the patterns of mass extinctions (starting time, duration and magnitude) 665 imposed on the model, and ii) compare the global diversity curves produced by the model 666 with those generated from fossil data. Sepkoski's global diversity curve corresponds to 667 668 marine invertebrates listed in Sepkoski's published marine genus compendium²¹ (data downloaded from Sepkoski's Online Genus Database at the following link: 669 http://strata.geology.wisc.edu/jack/). Alroy's and Zaffos et al's global diversity curves are 670 digitized from the original sources, i.e., figure 3 in Alroy²² and figure 2a in Zaffos et al.²³, 671 respectively. The curve reported by Alroy²² corresponds to genus-richness estimates 672 obtained after correcting for sampling effort using the shareholder guorum subsampling 673 technique. This curve is binned at approximately 11-Myr time intervals and includes non-674 tetrapod marine animals of which Anthozoa, Trilobita, Ostracoda, Linguliformea, "Articulata", 675 676 Bryozoa, Crinoidea, Echinoidea, Graptolithina, Conodonta, Chondrichthyes, Cephalopoda, 677 Gastropoda, and Bivalvia are the major taxonomic groups. The curve reported in Zaffos et al's study corresponds to 1 Myr range-through richness estimates of marine skeletonized 678 invertebrate genera including Brachiopoda, Bivalvia, Anthozoa, Trilobita, Gastropoda, 679 Crinoidea, Blastoidea, Edrioasteroidea, Ammonoidea, Nautiloidea, and Bryozoa. All digitized 680 (and interpolated) diversity data and the net diversification rate data imputed by the model to 681

simulate mass extinctions are provided as source data files 1 and 2, respectively.

683 OBIS data

We use the occurrence records of genera belonging to the most diverse marine invertebrate
groups: Subphylum Crustacea and Phylum Mollusca, as downloaded from the Ocean
Biodiversity Information System (OBIS) on 22nd October 2021 (www.obis.org). The list of
genera is validated with the genera names in WoRMS (https://www.marinespecies.org) and

only the accepted, extant and marine names are selected for the analysis. This corresponds 688 689 to a total of 10,018,142 records of 9,750 genera (6,540,489 records and 5,533 genera of 690 crustaceans and 3,477,653 records and 4,217 genera of molluscs) collected from 1920 to 2021. The records are gridded into hexagons (800,000 km² at the equator) to account for 691 692 different gamma (regional) diversity across latitudes, otherwise, a bias would occur in the resulting estimates. To ensure sufficient sampling size, we select only those hexagons with 693 more than or equal to 10 occurrence records and with more than three genera. Furthermore, 694 695 we use the frequencies of the genera to estimate the number of unobserved genera per 696 hexagon. We do so by extrapolating the number of genera based on bias-corrected Chao estimate according to the tail of rare genera (i.e., those genera that have only one or two 697 occurrence records in a hexagon)^{64,65}. The final number of genera per hexagon is the sum of 698 the observed and unobserved estimates of genera. The analysis is performed with the 699 700 package "vegan"⁶⁶ in R version 4.1.2. Finally, we spatially overlap the hexagons and 0.5x0.5 degrees square grid to match the map of the palaeo analysis and extract the value of the 701 diversity index per coastal grid in QGIS version 3.22.0. The comparison between model and 702 703 observations is made on the normalised diversities (0-1) bounded between the 0.05 and 0.95 704 quantiles to minimise the effect of outliers in the observed pattern.

705 Testing a static (null) palaeogeographic model

In order to evaluate the relative effects of mass extinctions and palaeogeography on global diversity dynamics, we carry out simulations for three static palaeogeographic configurations: the Devonian (400 Ma), the Carboniferous (300 Ma) and the present. For each of these three configurations, the model runs for 541 million years in a 'static mode', that is, diversity accumulates steadily at a pace determined by the temperature and food assigned to each grid at the selected static configuration. Mass extinctions are imposed the same way we do in

the default model with variable palaeogeography. The test is performed for the exponential 712 diversification model and the 'calibrated' logistic model and for each of the three mass 713 714 extinction patterns (aka Sepkoski, Alroy and Zaffos et al). Supplementary Figure 2 shows the differences between the log-transformed normalized diversities (between 0 and 1) 715 716 produced by the diversification models with static palaeogeography (nDiv tectonics OFF) and with variable palaeogeography (nDiv tectonics ON). Red and blue colours denote, 717 respectively, the extent to which the static model produces diversity estimates above or below 718 719 those produced by the model with plate tectonics. Tropical regions are dominated by reddish 720 colors indicating that the static model particularly overestimates diversity in these regions, where high temperatures accelerate diversification. 721

In the exponential model, the absence of plate tectonics leads to a scenario of uncontrolled 722 723 diversity growth (mainly in the tropical shelf seas - reddish areas on maps) that even mass 724 extinctions cannot dampen (Supplementary Fig. 3a-c). These results support the idea that Earth's palaeogeographic evolution and sea level changes, by creating, positioning and 725 destroying seafloor habitats, have played a key role in constraining the growth of diversity 726 throughout the Phanerozoic. In the calibrated logistic model (Supplementary Fig. 3d-f), 727 regional diversity is constrained by a carrying capacity that prevents diversity from running 728 away. In this case, diversity accumulates in each region at a pace determined by temperature 729 and food until its carrying capacity is reached. Thus, global diversity is steadily increasing 730 731 over time as a result of the gradual saturation of biological communities within regions.

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733

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878 Code Availability

The coupled palaeogeographic-diversification model presented here uses input data of 879 seafloor age distributions and palaeoenvironmental conditions from the siwill22/agegrid-0.1 880 881 v1-alpha palaeogeographic model and the cGENIE Earth System Model, respectively. We 882 provide code availability for each of these two models. The code for the palaeogeographic 883 model reconstructing seafloor age distributions from GPlates full-plate tectonic 884 reconstructions is assigned a DOI: 10.5281/zenodo.3271360. The code for the version of the 'muffin' release of the cGENIE Earth System Model used in this study, is tagged as v0.9.20, 885 and is assigned a DOI: 10.5281/zenodo.4618023. 886

The code and data for the coupled palaeogeographic-diversification (INDITEK) model are 887 888 available on GitHub (https://github.com/CarmenGarciaComas/INDITEK, last access: October 2021). The model is written in MATLAB 2013b and tested with MATLAB 2021a in a MacOS 889 890 2.3 GHz 8-Core Intel Core i9, and with MATLAB 2020b on Windows with a 2.5 GHz Intel i5-3210M and on Linux Debian with a 2.6 GHz Intel Core 9th Gen i9-9980HK processor. A 891 manual (README.md) detailing the main code modules, basic model configuration, input 892 data files (including those required from the palaeogeographic model and the cGENIE Earth 893 894 System model simulations), and how to run the model and plot the results is provided through 895 the link above.

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907 Author contributions

- 908 P.C. and C.G-C. proposed and designed the study. P.C., C.G-C. and S.M.V. developed the
- 909 diversification model. A.P. and A.R. performed the cGENIE model simulations. S.W. and
- 910 R.D.M. prepared the plate tectonic/palaeo-elevation model reconstructions. C.G-C. performed
- 911 the coupling of the diversification model to the plate tectonic/paleo-elevation model. C.G-C.
- and G.L-G. developed the method to estimate global diversity from regional diversity. C.C.
- analysed OBIS data for marine invertebrates. P.C., C.G-C., A.P., S.W., M.J.B., C.C, G.L-G.,
- 914 R.D.M., A.R. and S.M.V. contributed to data analysis and discussion of results. P.C., C.G-C.,
- A.P., S.W. wrote the manuscript with inputs from all authors.

916 **Competing interests**

- 917 The authors declare no competing interests.
- 918 **Supplementary Information** is available for this paper.
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- 921 Reprints and permissions information is available at <u>www.nature.com/reprints</u>.



922 FIGURE 1: Global diversity dynamics across the Phanerozoic.

- 923 a-c, Global diversity dynamics reconstructed from the 'saturated' logistic model (red), the exponential model (blue) and the 'calibrated' logistic model
- 924 (blue dashed line, see Figure 2 for calibration) after imposing the pattern of mass extinctions of Sepkoski²¹ (**a**), Alroy²²(**b**), and Zaffos et al.²³ (**c**). In
- 925 each panel, the corresponding fossil diversity curve is superimposed (grey). Cm, Cambrian; O, Ordovician; S, Silurian; D, Devonian; Cb,
- 926 Carboniferous; P, Permain; T, Triassic; J, Jurassic; K, Cretaceous; Cz, Cenozoic. Shaded areas represent mass extinctions.



927 FIGURE 2: Re-diversifying the Phanerozoic oceans.

a-f, Spatial distribution of marine animal diversity (# genera / area) in the Cambrian 928 (Guzhangian, 500 Ma), Late Ordovician (Katian, 450 Ma), Early Devonian (Emsian, 400 Ma), 929 930 Late Carboniferous (Pennsylvanian, 300 Ma), Late Cretaceous (Maastrichtian, 70 Ma) and 931 present generated by the calibrated logistic model after imposing the pattern of mass 932 extinctions extracted from the fossil diversity curve of Sepkoski²¹. This model run uses the following parameters: $Q_{10} = 1.75$, $K_{food} = 0.5$ molC m⁻²y⁻¹, net diversification rate limits (ρ_{min} -933 ρ_{max}) = 0.001-0.035 Myr⁻¹ (per capita), and a K_{min} to K_{max} range between 12 and 123 genera 934 per unit area according to the calibration analysis presented in **Extended Data Fig. 6**. The 935 same plots but for the mass extinction patterns extracted from the fossil diversity curves of 936 Alroy²² and Zaffos et al²³ are shown in Extended Data Figs. 7-8. See Supplementary Video 937 3 for the full Phanerozoic sequence. g-h, Current spatial distributions of diversity along the 938 continental margins from model simulations and observations extracted from the Ocean 939 Biodiversity Information System (OBIS) database (genera belonging to Subphyllum 940 Crustacea and Phyllum Mollusca). For the purpose of comparison, normalized diversities (0-941

- 1) bounded between quantiles 0.05 and 0.95 are represented. **i-j**, Latitudinal distributions of
- 943 diversity averaged in 10 degree zonal bands.





- 945 Spatial distribution of the diversity-to-carrying capacity (K_{eff}) ratio (colourbar) in deep sea
- habitats and flooded continental regions of the Early Devonian (Emsian, 400 Ma), Late
- 947 Carboniferous (Pennsylvanian, 300 Ma), Late Cretaceous (Maastrichtian, 70 Ma) and present
- ⁹⁴⁸ using the 'calibrated' logistic model after imposing the mass extinction patterns of
- 949 Sepkoski²¹ (**a-d**), Alroy²² (**e-h**), and Zaffos et al²³ (**i-l**). See **Supplementary Video 4** for the full

- 950 Phanerozoic sequences. m-o, Frequency distributions (% area) of the diversity-to-K_{eff} ratio for
- 951 the flooded continental regions. The grey lines are frequency distributions generated from
- simulations using the 15 different parameter settings listed in **Extended Data Table 1**. The
- 953 colour dots are average values for different Phanerozoic times.



954 **EXTENDED DATA FIGURE 1: Computing global diversity from diversity maps.**

- 955 For each time interval or regional diversity map, (1) we plot hundreds of transects (white
- lines) from diversity peaks to their nearest troughs, (2) we integrate diversity along the
- 957 transects (from α_n to α_L) according to the distance between pairs of grids using the overlap
- 958 coefficient (V), which gives the proportion of shared genera with respect to the grid with the
- least diversity, i.e. $V_{n,n+1}$ *min(α_n ; α_{n+1}) [see Annex 1], (3) we order the resulting transects'
- 960 diversity (γ_i) from maximum diversity (γ_{max}) to minimum diversity (γ_{min}), calculate the pair-wise

- 961 distance between transects (the distance between their peaks), and integrate the diversity of
- 962 transects from the greatest to lowest according to the nearest-neighbour distance of the
- 963 corresponding transect to those transects already integrated (γ_{total}).



EXTENDED DATA FIGURE 2: Continental configuration and global diversity dynamics.
a-f, Global diversity dynamics (# genera) reconstructed from the 'calibrated' logistic model (a,
c, e) and the exponential model (b, d, f) overimposed on the temporal variability of the
fragmentation index (a, b), global mean shelf area (c, d), mean shelf age (e, f) and mean
shelf K_{eff} (g, h).



969 EXTENDED DATA FIGURE 3: Calibrating the K_{min} and K_{max} values of the logistic model.

- Normalized model diversity (0-1) versus normalized fossil diversity (0-1) for different
- $_{971}$ $\,$ combinations of the K_{min} and K_{max} values of the model. These simulations use the pattern of
- 972 mass extinctions extracted from the fossil diversity curve of Sepkoski²¹. Lin's Concordance
- 973 Correlation coefficient (CCC), which quantifies the alignment of the model estimates to the
- 1:1 line, is shown in each panel with colour code.



975 EXTENDED DATA FIGURE 4: Calibrating the K_{min} and K_{max} values of the logistic model.

- 976 As Extended Data Figure 3 but for the pattern of mass extinctions extracted from the fossil
- 977 diversity curve of Alroy²², and the fossil diversity estimates reported in Alroy²².



978 EXTENDED DATA FIGURE 5: Calibrating the K_{min} and K_{max} values of the logistic model.

979 As Extended Data Figure 3 but for the pattern of mass extinctions extracted from the fossil

980 diversity curve of Zaffos et al²³ and the fossil diversity estimates reported in Zaffos et al²³.



EXTENDED DATA FIGURE 6: Calibrating the logistic model's carrying capacities. a-c, 981 Lin's concordance correlation coefficients (CCC) for the relationship between the global 982 diversities resulting from the model and the fossil diversity estimates of Sepkoski²¹ (a), Alroy²² 983 (b), and Zaffos et al²³(c) using different combinations of K_{min} and K_{max} in the model (Extended 984 Data Figs. 3-5 for details on correlations). The inset in each panel shows the CCCs in 985 ascending order for the different combinations of Kmin and Kmax. The black curve in the insets 986 is for the simulation run using the selected parameters (**Supplementary Table 1**). The grey 987 curves are for each of the first 15 combinations of parameters listed in Extended Data Table 988 1. The dashed line denotes the CCC value of 0.7 and the cross in each panel is the average 989 990 of all K_{min} and K_{max} combinations giving a CCC greater than 0.7. These are the values of K_{min} and K_{max} used to run the 'calibrated' logistic model. 991



992 **EXTENDED DATA FIGURE 7: Re-diversifying the Phanerozoic oceans.**

- 993 **a-f**, Spatial distribution of marine animal diversity (# genera / area) in the Cambrian
- 994 (Guzhangian, 500 Ma), Late Ordovician (Katian, 450 Ma), Early Devonian (Emsian, 400 Ma),
- ⁹⁹⁵ Late Carboniferous (Pennsylvanian, 300 Ma), Late Cretaceous (Maastrichtian, 70 Ma) and
- 996 present generated by the calibrated logistic model after imposing the pattern of mass
- 997 extinctions extracted from the fossil diversity curve of Alroy²². These model runs use the
- 998 following parameters: $Q_{10} = 1.75$, $K_{food} = 0.5$ molC m⁻²y⁻¹, net diversification rate limits (ρ_{min} -
- ρ_{max} = 0.001-0.035 Myr⁻¹ (per capita), and a K_{min} to K_{max} range between 11 and 119 genera
- 1000 per unit area. These carrying capacity values are derived from the analysis presented in
- 1001 **Extended Data Fig. 6**. See also **Supplementary Video 3** for the full Phanerozoic sequence.



1002 EXTENDED DATA FIGURE 8: Re-diversifying the Phanerozoic oceans.

- 1003 **a-f**, Spatial distribution of marine animal diversity (# genera / area) in the Cambrian
- 1004 (Guzhangian, 500 Ma), Late Ordovician (Katian, 450 Ma), Early Devonian (Emsian, 400 Ma),
- Late Carboniferous (Pennsylvanian, 300 Ma), Late Cretaceous (Maastrichtian, 70 Ma) and
- 1006 present generated by the calibrated logistic model after imposing the pattern of mass
- 1007 extinctions extracted from the fossil diversity curve of Zaffos et al.²³ {Formatting Citation}.
- 1008 These model runs use the following parameters: $Q_{10} = 1.75$, $K_{food} = 0.5$ molC m⁻²y⁻¹, net
- 1009 diversification rate limits (ρ_{min} ρ_{max}) = 0.001-0.035 Myr⁻¹ (per capita), and a K_{min} to K_{max} range
- 1010 between 11 and 117. These carrying capacity values are derived from the analysis presented
- in Extended Data Fig. 6. See also Supplementary Video 3 for the full Phanerozoic
 sequence.



1013 EXTENDED DATA FIGURE 9: Robustness of the diversity-to-K_{eff} frequency distribution

- 1014 **pattern.** Frequency distributions (% area) of the diversity-to-K_{eff} ratio for the flooded
- 1015 continental regions after decreasing the values of K_{min} and K_{max} in the model by 25% with
- respect to the calibrated values [i.e., 12-123 (for Sepkoski), 11-119 (for Alroy), 11-117 (for
- 1017 Zaffos et al)].



EXTENDED DATA FIGURE 10: Testing the effect of enabling/disabling mass
extinctions. Global diversity (# genera) trajectories reconstructed from the calibrated logistic
model after disabling (blue) and enabling (red) the Late Devonian and Permo-Triassic mass
extinctions from the mass extinction pattern of Sepkoski²¹ (a, b), Alroy²² (c, d) and Zaffos et
al²³ (e, f), respectively. The mass extinctions marked in bold represent those
disabled/enabled in each panel.



1024 EXTENDED DATA FIGURE 11: Testing the effect of different model configurations and

- 1025 parameter values (sensitivity analyses). a-c, Global diversity dynamics (# genera)
- 1026 reconstructed using the exponential model for two alternative palaeogeographic
- 1027 reconstructions, Kocsis and Scotese³⁷ (K&S2021) and Scotese and Wright³⁵ (S&W2018). d-f,
- 1028 Effect of changing the sea level +/- 100 m compared to the original paleoDEM grids of
- 1029 Scotese and Wright³⁵. g-i, Effect of changing the ocean phosphate concentration (x2 and x0.5
- 1030 with respect to present day concentrations, i.e., default scenario).

1031 EXTENDED DATA TABLE 1. Lin's Concordance Correlation Coefficient (CCC) using
 1032 different parameter settings in the model.

SEPKOSKI 2002						ALROY 2010						ZAFFOS et al 2017				
Model parameters Lin's CCC*					Γ	Model parameters Lin's CC			CCC*	-	Model parameters Li				CCC*	
Q10	kfood	ρmax	Ехр	Log	C	210	kfood	ρmax	Ехр	Log	_	Q10	kfood	ρmax	Ехр	Log
1.5	1	0.035	0.91	0.60		.5	1	0.035	0.73	0.64		1.5	1	0.035	0.78	0.64
1.5	0.75	0.035	0.91	0.61		.5	0.75	0.035	0.71	0.66		1.75	1	0.035	0.77	0.60
1.75	1	0.035	0.91	0.55	1	.75	1	0.035	0.70	0.60		1.75	0.75	0.035	0.76	0.63
1.75	0.75	0.035	0.91	0.56	1	.75	0.75	0.035	0.70	0.62		2	1	0.035	0.75	0.57
2	0.75	0.035	0.91	0.53		2	0.75	0.035	0.70	0.60		2	0.75	0.035	0.75	0.59
2	1	0.035	0.91	0.52		.5	1	0.04	0.68	0.64		1.5	0.75	0.035	0.75	0.66
2.25	0.75	0.035	0.91	0.51		2	1	0.035	0.68	0.58		2.25	1	0.035	0.74	0.55
2.5	0.75	0.035	0.91	0.49		.5	0.5	0.035	0.68	0.69		2.25	0.75	0.035	0.74	0.57
2.25	1	0.035	0.90	0.50	1	.75	0.5	0.035	0.68	0.65		2.5	1	0.035	0.74	0.53
2.5	1	0.035	0.90	0.49		2	0.5	0.035	0.67	0.62		2.5	0.75	0.035	0.73	0.56
1.5	0.5	0.035	0.90	0.61	2	.25	0.75	0.035	0.68	0.60		1.75	0.5	0.035	0.72	0.63
1.75	0.5	0.035	0.90	0.57	2	2.5	0.75	0.035	0.68	0.59		2.5	0.5	0.035	0.72	0.58
2.5	0.5	0.035	0.90	0.50	2	2.5	1	0.035	0.68	0.56		2.25	0.5	0.035	0.72	0.59
1.5	1	0.04	0.90	0.59		2	1	0.04	0.67	0.58		1.75	1	0.04	0.72	0.61
2.25	0.5	0.035	0.90	0.52	2	.25	1	0.035	0.66	0.57	_	1.5	1	0.04	0.72	0.65
2	0.5	0.035	0.90	0.54	2	2.5	1	0.04	0.66	0.56		2	0.5	0.035	0.71	0.61
2	1	0.04	0.89	0.51	1	.75	1	0.04	0.66	0.60		2	1	0.04	0.71	0.58
2.5	1	0.04	0.89	0.49	2	2.5	0.5	0.035	0.65	0.62		2.25	1	0.04	0.70	0.56
1.75	1	0.04	0.89	0.55	2	.25	1	0.04	0.65	0.57		2.5	1	0.04	0.70	0.55
2.25	1	0.04	0.89	0.50	2	.25	0.5	0.035	0.65	0.61		1.5	0.5	0.035	0.69	0.67
1.5	0.75	0.04	0.88	0.59		1.5	0.75	0.04	0.64	0.66		1.75	0.75	0.04	0.68	0.62
1.75	0.75	0.04	0.88	0.54	1	.75	0.75	0.04	0.64	0.62		2.5	0.75	0.04	0.67	0.56
1.75	0.25	0.035	0.88	0.57		2	0.75	0.04	0.63	0.59		2	0.75	0.04	0.67	0.59
1.5	0.25	0.035	0.87	0.60		2	0.25	0.035	0.62	0.65		2.25	0.75	0.04	0.67	0.57
2	0.75	0.04	0.87	0.51	1	.75	0.25	0.035	0.62	0.67		2.5	0.25	0.035	0.66	0.60
2.25	0.75	0.04	0.87	0.51	2	2.5	0.25	0.035	0.62	0.63		1.5	0.75	0.04	0.65	0.67
2	0.25	0.035	0.87	0.54	2	.25	0.75	0.04	0.61	0.57		2.25	0.25	0.035	0.65	0.62
2.5	0.75	0.04	0.87	0.50	2	2.5	0.75	0.04	0.60	0.58		2	0.25	0.035	0.64	0.63
2.5	0.25	0.035	0.87	0.51	2	.25	0.25	0.035	0.60	0.65		2.5	0.5	0.04	0.63	0.57
2.25	0.25	0.035	0.87	0.53		.5	0.25	0.035	0.60	0.69		2.25	0.5	0.04	0.62	0.59
1.5	0.5	0.04	0.86	0.58	1	.75	0.5	0.04	0.59	0.65		1.75	0.25	0.035	0.62	0.65
1.75	0.5	0.04	0.85	0.55		2	0.5	0.04	0.59	0.62		2	0.5	0.04	0.62	0.60
2	0.5	0.04	0.85	0.52		.5	0.5	0.04	0.58	0.68		1.75	0.5	0.04	0.61	0.63
2.5	0.5	0.04	0.84	0.50	2	2.5	0.5	0.04	0.57	0.60		1.5	0.25	0.035	0.58	0.68
2.25	0.5	0.04	0.84	0.50	2	.25	0.5	0.04	0.56	0.60		1.5	0.5	0.04	0.57	0.67
1.5	0.25	0.04	0.83	0.59		2	0.25	0.04	0.52	0.64		2.5	0.25	0.04	0.54	0.59
2.25	0.25	0.04	0.82	0.51		1.5	0.25	0.04	0.51	0.69		2.25	0.25	0.04	0.53	0.60
1.75	0.25	0.04	0.82	0.55	1	.75	0.25	0.04	0.51	0.66		2	0.25	0.04	0.51	0.62
2	0.25	0.04	0.82	0.53	2	2.5	0.25	0.04	0.51	0.62		1.75	0.25	0.04	0.51	0.64
2.5	0.25	0.04	0.81	0.50	_2	.25	0.25	0.04	0.50	0.63	_	1.5	0.25	0.04	0.47	0.68

*The CCCs are for the relationship between the normalized diversities estimated from the fossil record

and those generated by the exponential (Exp) and the logistic (Log) models. The 15 combinations of

1035 model parameters that gave the highest CCC for each mass extinction pattern were selected. Of these,

the combination that gave the highest CCC for the relationship between the fossil diversities and the

1037 diversities generated by the calibrated logistic (Cal. Log) model was selected as the best (Extended1038 Data Table 1 continued).

	SEPI	KOSKI 2	2002		ALROY 2010					ZAFFOS et al 2017				
Model parameters Li			Lin's CCC	Model parameters			Lin's CCC	Model parame			meters	Lin's CCC		
Q10	kfood	ρmax	Cal. Log	Q10	kfood	ρmax	Cal. Log	Q	10	kfood	ρmax	Cal. Log		
1.5	0.25	0.035	0.95	1.5	0.5	0.035	0.80	1.	5	0.75	0.035	0.82		
1.5	0.5	0.035	0.95	1.5	0.75	0.035	0.77	1.	5	1	0.04	0.81		
1.5	0.75	0.04	0.95	1.75	0.5	0.035	0.77*	1.	75	0.5	0.035	0.81*		
2	0.5	0.04	0.94	1.5	1	0.04	0.76	1.	5	1	0.035	0.80		
2	0.25	0.04	0.94	1.5	1	0.035	0.75	1.	75	0.75	0.035	0.79		
1.75	0.5	0.035	0.94*	1.75	0.75	0.035	0.75	2.2	25	0.5	0.035	0.79		
1.5	0.25	0.04	0.93	2	0.75	0.035	0.73	1.	75	1	0.04	0.78		
1.5	0.75	0.035	0.93	2.25	0.75	0.035	0.72	1.	75	1	0.035	0.78		
2.25	0.75	0.04	0.93	1.75	1	0.035	0.72	2	2	0.75	0.035	0.78		
1.75	1	0.04	0.92	2.5	0.75	0.035	0.72	2.	5	0.5	0.035	0.78		
1.75	0.75	0.035	0.91	2.25	1	0.04	0.71	2.2	25	0.75	0.035	0.77		
1.5	1	0.035	0.90	2	1	0.035	0.71	2	2	1	0.035	0.76		
2	0.75	0.035	0.89	2.5	1	0.04	0.70	2.	5	0.75	0.035	0.76		
2.25	0.75	0.035	0.88	2.25	1	0.035	0.69	2.2	25	1	0.035	0.75		
2.5	0.75	0.035	0.87	2.5	1	0.035	0.69	2.	5	1	0.035	0.74		

1039 **EXTENDED DATA TABLE 1.** (Continued).

1040 *The bold numbers show the combination of parameters selected.



SUPPLEMENTARY FIGURE 1: Model estimates of seafloor age. a-d, Age of the seafloor
in open ocean and time that the flooded continental shelves have been underwater in the
Cambrian (Guzhangian, 500 Ma), Late Ordovician (Katian, 450 Ma), Early Devonian (Emsian,
400 Ma), Late Carboniferous (Pennsylvanian, 300 Ma), Late Cretaceous (Maastrichtian, 70
Ma) and present (Methods).



1046 SUPPLEMENTARY FIGURE 2: Testing the impact of plate tectonics on the spatial

1047 **distributions of diversity. a-i**, Comparison of the results of the exponential diversification

- 1048 model without plate tectonics and with plate tectonics. The color code represents the
- 1049 difference between the log-transformed normalized diversities (0-1) produced by the model
- 1050 with static palaeogeography (nDiv tectonics OFF) and the model with variable
- 1051 palaeogeography (nDiv tectonics ON) for three time frames (panels row-wise 400 Ma, 300

- 1052 Ma and 0 Ma) and three extinction patterns (panels column-wise Sepkoski, Alroy and Zaffos
- 1053 et al). j-r, As in panels a-i but for the calibrated logistic model.



1054 SUPPLEMENTARY FIGURE 3: Testing the impact of plate tectonics on global diversity

1055 dynamics. a-c, Global diversity dynamics produced by the exponential diversification model

1056 with static palaeogeography (light blue, yellow and red for 400 Ma, 300 Ma and 0 Ma,

1057 respectively) and with variable palaeogeography (blue line) for each of the three mass

1058 extinction patterns (panels column-wise Sepkoski, Alroy and Zaffos et al). The corresponding

1059 fossil diversity curve is superimposed on each panel (grey dashed line). **d-f**, As in panels a-c

1060 but for the calibrated logistic model.





SUPPLEMENTARY FIGURE 4: Testing the effect of disabling the environamnetal

1062 **forcings. a-f**, Spatial distribution of marine animal diversity (# genera / area) in the Cambrian

1063 (Guzhangian, 500 Ma), Late Ordovician (Katian, 450 Ma), Early Devonian (Emsian, 400 Ma),

- Late Carboniferous (Pennsylvanian, 300 Ma), Late Cretaceous (Maastrichtian, 70 Ma) and
- 1065 present generated by the calibrated logistic model after imposing the pattern of mass
- 1066 extinctions extracted from the fossil diversity curve of Sepkoski. This model run uses the
- 1067 following parameters: Q10 = 1 (no temperature dependence), K_{food} = 0.5 molC m⁻²y⁻¹, net

- 1068 diversification rate limits ($\rho_{min} \rho_{max}$) = 0.001-0.035 Myr⁻¹ (per capita), and a K_{min} to K_{max} range
- 1069 between 12 and 123 genera. **g-I**, As in panels a-f but disabling both the temperature and food
- 1070 dependence of net diversification rate, i.e. Q10 = 1 (no temperature dependence), $K_{food} = 0$
- 1071 (no food dependence), net diversification rate limits ($\rho_{min} \rho_{max}$) = 0.001-0.035 Myr⁻¹ (per
- 1072 capita), and a K_{min} to K_{max} range between 12 and 123 genera.



1073 SUPPLEMENTARY FIGURE 5: Interactive effect of seawater temperature and food

1074 supply on net diversification rate. a, Combined effect of seawater temperature and food

1075 supply on net diversification rate (ρ) for the set of parameters used to run the main

1076 simulations (i.e. Q_{10} = 1.75; K_{food} = 0.5 molC m⁻²y⁻¹; ρ = 0.001 - 0.035 Myr⁻¹). **b**, Same as

1077 upper panel but for two extreme parameter settings (Q_{10} = 1.5; K_{food} = 0.25 molC m⁻²y⁻¹; ρ =

1078 0.001 - 0.035 Myr⁻¹, and **c**, Q_{10} = 2.5; K_{food} = 1 molC m⁻²y⁻¹; ρ = 0.001 - 0.035 Myr⁻¹.



- 1079 SUPPLEMENTARY FIGURE 6: Model estimates of net diversification rate. a-d, Spatially-
- resolved net diversification rate in the Cambrian (Guzhangian, 500 Ma), Late Ordovician
- 1081 (Katian, 450 Ma), Early Devonian (Emsian, 400 Ma), Late Carboniferous (Pennsylvanian, 300
- 1082 Ma), Late Cretaceous (Maastrichtian, 70 Ma) and present.



1083 SUPPLEMENTARY FIGURE 7: Mass extinction patterns extracted from the global

1084 **diversity curves of Sepkoski, Alroy and Zaffos et al.** These data are provided as Source

1085 Data file 2.

Symbol	Description	Value	Range tested	units
ρ _{min}	Minimum net diversification rate	0.001		Myr ⁻¹
$ ho_{max}$	Maximum net diversification rate	0.035	0.03 - 0.04	Myr ⁻¹
Q ₁₀	Thermal sensitivity	1.75	1.5 – 2.5	n.u.
K_{food}	Half-saturation constant for food	0.5	0.25 – 1	mol m ⁻² yr ⁻¹
lat-lon	Radius of search for immigration	278	0 – 278	Km

1086 **SUPPLEMENTARY TABLE 1**. Model parameters and range of parameter values tested.

SUPPLEMENTARY VIDEOS 1-4. Full Phanerozoic sequences for the spatial reconstructions
 of diversity based on the saturated logistic model (Supp. Video 1), the exponential model
 (Supp. Video 2) and the calibrated logistic model (Supp. Video 3). Full Phanerozoic
 sequences for the spatial reconstructions of diversity-to-carrying capacity ratio (Supp. Video
 These videos are uploaded along with the manuscript to the journal server. Video format:
 MP4 (video codec: H264 / AVC)

1093 **SOURCE DATA FILE 1**. Digitized global diversity curves from original reports.

SOURCE DATA FILE 2. Mass extinction patterns, including the magnitude of diversity loss
 (represented as negative net diversification rate) as well as the starting time and duration of
 the mass extinction events imposed in this study as extracted from the fossil diversity curves
 of Sepkoski, Alroy and Zaffos et al. See also Supplementary Figure 4 for a graphical
 representation.

SOURCE DATA FIGURES. The source data for the figures and extended data figures
 presented in this article are available on GitHub

1101 (https://github.com/CarmenGarciaComas/INDITEK). The revised version of the model will be

1102 published in ZENODO upon acceptance of the manuscript.

1103 ANNEX 1. Converting Jaccard coefficient to Overlap coefficient

1104 The Jaccard similarity index (J) is the metric most commonly used to express the similarity 1105 between two communities. Let us call the intersection of two samples $\alpha_n \cap \alpha_{n+1}$ and their 1106 union $\alpha_n \cup \alpha_{n+1}$ The cardinal (number of elements) of a set will be represented by vertical 1107 bars, i.e. $\alpha_n = |A_n|$. The Jaccard similarity (J) of α_n and α_{n+1} is then defined as the cardinal of 1108 the intersection divided by that of the union:

$$J(A_{n}, A_{n+1}) = \frac{|A_{n} \cap A_{n+1}|}{|A_{n} \cup A_{n+1}|} = \frac{|A_{n} \cap A_{n+1}|}{|A_{n}| + |A_{n+1}| - |A_{n} \cap A_{n+1}|}$$

The J index between points n and n+1 is bounded between 0 and min(α_n ; α_{n+1})/max(α_n ; α_{n+1}), 1109 where α_n ; α_{n+1} are the diversities of two samples. A larger value for J (J > 1) would mean that 1110 there are more shared species between the two communities than there are species within 1111 1112 the least diverse community, which is ecologically absurd. Yet, using a single similarity decay function can lead the computed value of J to be locally larger than min(α_n ; α_{n+1})/max(α_n ; α_{n+1}). 1113 To correct this artifact, we used the overlap coefficient (V) instead of J. The overlap 1114 coefficient is bounded between 0 and 1, whatever the ratio of diversities. Therefore, using an 1115 overlap decay function never creates artifacts. 1116

1117 The overlap coefficient (V), also known as the Szymkiewicz–Simpson coefficient, is defined 1118 as the cardinal of the intersection divided by that of the smallest set:

$$V(A_n, A_{n+1}) = \frac{|A_n \cap A_{n+1}|}{(\min(|A_n|, |A_n+1|))}$$

1119 Without loss of generality, let us consider that α_{n+1} is smaller than α_n . We will call R = α_n/α_{n+1} 1120 the ratio of the two cardinals. V can be estimated from J and vice-versa as follows:

$$V(A_{n}, A_{n+1}) = J(A_{n}, A_{n+1}) \frac{|A_{n}| + |A_{n+1}| - |A_{n} \cap A_{n+1}|}{|A_{n+1}|} = J(A_{n}, A_{n+1})(1 + R - V(A_{n}, A_{n+1}))$$

$$J(A_{n}, A_{n+1}) = \frac{V(A_{n}, A_{n+1})}{1 + R - V(A_{n}, A_{n+1})}$$

$$V(A_{n}, A_{n+1}) = J(A_{n}, A_{n+1})(1 + R) - J(A_{n}, A_{n+1})V(A_{n}, A_{n+1})$$

$$V(A_{n}, A_{n+1})(1 + J(A_{n}, A_{n+1})) = J(A_{n}, A_{n+1})(1 + R)$$

$$V(A_{n}, A_{n+1}) = \frac{(1 + R)J(A_{n}, A_{n+1})}{1 + J(A_{n}, A_{n+1})}$$

$$V(A_{n}, A_{n+1}) = \frac{(1 + R)J(A_{n}, A_{n+1})}{1 + J(A_{n}, A_{n+1})}$$