# Blood flow modeling reveals improved collateral artery performance during the regenerative period in mammalian hearts

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Article

# Blood flow modeling reveals improved collateral artery performance during the regenerative period in mammalian hearts

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## **Abstract**

Collateral arteries are a vessel subtype that bridges two artery branches, forming a natural bypass that can deliver blood flow downstream of an occlusion. These bridges in the human heart are associated with better outcomes during coronary artery disease. We recently found that their rapid development in neonates supports heart regeneration, while the non-regenerative adult heart displays slow and minimal collateralization. Thus, inducing robust collateral artery networks could serve as viable treatment for cardiac ischemia, but reaching this goal requires more knowledge on their developmental mechanisms and functional capabilities. Here, we use whole-organ imaging and 3D computational fluid dynamics (CFD) modeling to identify the spatial architecture of and predict blood flow through collaterals in neonate and adult hearts. We found that neonate collaterals are more numerous, larger in diameter, and, even when similar in size/number, are predicted to more effectively re-perfuse an occluded coronary network when compared to adults. CFD analysis revealed that collaterals perform better in neonates because of decreased differential pressures along their coronary artery tree. Furthermore, testing of various collateral configurations indicated that larger, more proximal collaterals are more beneficial than many smaller ones, identifying a target architecture for therapeutic interventions. Morphometric analysis revealed how the coronary artery network expands during postnatal growth. Vessel diameters do not scale with cardiac muscle growth. Instead, the coronary tree expands solely by adding additional branches of a set length, a burst of which occurs during murine puberty. Finally, we compared mouse structural and functional data to human hearts. Surprisingly, fetal human hearts possessed a very large number of small, but mature, smooth muscle cell covered collaterals while angiogram data indicated adult patients with chronic coronary occlusions contained at least two. Comparing size ratios with modeled mouse data suggested low re-perfusion capabilities of the embryonic collaterals but higher functional benefits of those in diseased adults. Our unique interdisciplinary approach allowed us to quantify the functional significance of collateral arteries during heart regeneration and repair–a critical step towards realizing their therapeutic potential.

## Introduction

Cardiovascular disease, including coronary artery disease (CAD), is the leading cause of death worldwide[1]. Atherosclerosis causes coronary arteries to become partially or completely occluded, decreasing blood flow to the myocardium and jeopardizing cardiac muscle function and viability. Current treatments include percutaneous interventions and coronary artery bypass graft surgery, but these are highly invasive and a significant number are unsuccessful, especially in diffuse multi-vessel CAD, which calls for new treatments[2]. Humans and some other mammals can develop specialized blood vessels called collateral arteries that function as natural coronary bypasses. Collateral arteries are defined as an artery segment directly bridging two artery branches without intervening capillaries, such that they directly provide blood flow distal to a coronary blockage. Although only a minority of adult humans have functionally significant collateral arteries, clinical observations indicate that they can successfully shunt blood around a stenosis to protect against myocardial ischemia and reduce the risk of cardiac death[3–6]. Thus, inducing collateral development could be a promising therapeutic approach for treating CAD[7]. However, a major roadblock to this goal is the severe lack of knowledge about collateral developmental mechanisms and their ability to restore blood flow.

While studies have characterized the presence or absence of native collateral arteries across different mammals[8], mice are the most common model for investigating their function during cardiac injury, usually through surgically-induced myocardial infarctions (MI)[9–13]. Mice do not generally have pre-existing collateral arteries, but they can be observed in adults by 7 days post-MI when using vascular filling approaches, i.e. Microfil injection into the vasculature. This method detects 6-10 collaterals per adult heart at approximately 18 μm in diameter[10]. Genetic deletions in chemokine receptors that inhibit macrophages reduces collateral numbers[10]. Furthermore, mouse strains with decreased collateral development have genetic variants that lower *Rabep2* expression, which encodes a protein involved in VEGFR2 endosomal trafficking and signaling[14]. Thus, mice have been a useful model for understanding various aspects of collateral biology.

84       We recently used a different technique to identify collaterals—whole-mount immunofluorescence—coupled with lineage tracing and mouse genetics to identify the cellular and molecular mechanisms driving collateral development post-MI[9]. We found that, in the regenerating neonate heart, collaterals form post-MI when arterial endothelial cells migrate into the infarct zone in response to hypoxia-induced CXCL12 and coalesce into collateral arteries. This process was termed artery reassembly and did not occur in the non-regenerative adult heart, suggesting that the collaterals observed during vascular filling (described above) utilized a different mechanism. Exogenous CXCL12 application induced artery reassembly in adults to create collaterals up to 40 μm in diameter. Although these collaterals were positively correlated with heart regeneration and repair, and vascular filling methods established direct connections, a detailed description of how blood flows through these relatively small vascular connections is required to fully understand the functional capabilities and therapeutic potential of collateral arteries.

98      How structural parameters affect collateral hemodynamics in these injury models remains an unanswered question due to technical barriers of directly imaging blood flow. Clinical measurements of collateral flow rely on qualitative assessments from angiograms or indirect pressure measurements[15–17]. More accurate measurements of collateral flow in humans are not only invasive, but somewhat unreliable since conclusive relationships cannot be made without knowing the number and size of all collaterals, many of which cannot currently be imaged in the human heart via angiogram. Visualizing blood flow is even more difficult in experimental animals due to their small size. Conclusions regarding collateral flow are usually reached from *ex-vivo* data, but not without significant limitations. Methods include: 1. Filling coronary vessels through the aorta (Microfil casting, μCT and fluorescent conjugates)[18–23], which creates a non-cell specific volumetric map of coronary vessels, and 2. Whole mount immunostaining fixed hearts from postnatal transgenic mice[9]. None of these approaches provide a precise picture of how flowing blood will distribute through collaterals.

113      Because the physical laws governing fluid motion are known, computational fluid dynamics (CFD) modeling tools can directly and precisely estimate blood flow. CFD has

115    contributed to patient-specific surgical and treatment planning in numerous human

116    cardiovascular diseases[24–28]. CFD modeling has also been applied to the cardiovascular

117    systems of various animals to estimate hemodynamic forces that would otherwise be

118    difficult to directly measure[29–32]. In mice, computational studies have modeled blood

119    flow in the retinal vasculature, thoracic aorta, and even feto-placental vessels for the

120    purpose of defining how hemodynamic forces influence arterial remodeling events at the

121    cellular and molecular levels[33–35]. An additional major advantage of CFD modeling is the

122    ability to systematically alter certain parameters while keeping others constant, leading

123    to rapid conclusions on the reparative capabilities of different vascular architectures[36].

124         To obtain correct estimates from CFD modeling, it is critical to have high-

125    resolution images of a vascular network with intact volumetric dimensions. To date, the

126    vascular labeling methods utilized have not had the resolution required to generate

127    detailed anatomic models suitable for CFD modeling. However, recent innovations in

128    tissue clearing and whole-organ microscopy now provide the possibility of generating

129    sufficiently high resolution images suitable for CFD model building[37–40]. Thus, CFD is

130    perfectly poised to push forward our understanding of collateral function.

131         In this study, we sought to interrogate how different collateral configurations

132    affect blood flow post-injury. We optimized whole-organ immunostaining and clearing to

133    label and image the entire intact artery tree, allowing quantification of hemodynamic

134    forces via CFD using high-fidelity 3D models constructed in the neonate and adult. We

135    computationally generated virtual occlusions and various collateral configurations,

136    keeping other model parameters fixed, to measure levels of flow restoration. The results

137    showed that naturally forming collaterals in adult mouse hearts perform poorly and

138    restore little flow. The virtual equivalent of CXCL12-induced collaterals performs better

139    but remain sub-optimal. In contrast, naturally forming collaterals in neonate hearts are

140    highly restorative because the structural parameters of the early coronary tree and

141    cardiac output at this stage results in lower overall pressure loss along the coronary

142    tree. We additionally investigated collateral arteries in human hearts by generating

143    whole-organ images of fetal hearts and analyzing angiograms from patients with chronic

144    coronary occlusions. Surprisingly, we found both fetal hearts contained greater than 40

145    mature, smooth muscle covered collateral arteries, while only an average of two

146 collaterals with measurable flow in patient angiograms. Comparing diameters to CFD

147 mouse models where flow restoration was quantified suggested that human fetal

148 collaterals may be too small to be functionally significant and that those in patients may

149 lie between the capabilities of neonate and adult mouse collaterals. In total, the

150 combination of whole-organ artery labeling with 3D CFD modeling provides a powerful

151 tool to accurately analyze hemodynamic forces in collateral arteries to broaden our

152 understanding of their functional significance and therapeutic potential.

153

154 ## Results

155 **Imaging the entire coronary artery tree in neonate and adult mouse hearts**

156 To utilize 3D CFD for modeling coronary blood flow at high resolution and with

157 controlled parameter perturbations, we required a method to image the entire intact

158 artery tree in three dimensions. A whole-organ immunostaining and clearing method

159 based on iDISCO was optimized for cardiac tissue using postnatal day 6 (P6) mice[37,39],

160 which allowed us to image smooth muscle actin (α-SMA)-positive arterial smooth

161 muscle cells throughout the heart using Light sheet microscopy (Fig. 1a). The signal-to-

162 noise ratio of α-SMA staining was high, allowing sharp contrast of arteries throughout

163 the entire myocardium (Fig. 1b). Rendering the arterial immunolabeling in 3D using

164 Imaris software revealed vast improvements over our previous method[9]. Specifically,

165 the 3D architecture was retained (Fig. 1c), and we could fully observe the septal artery

166 (SpA) in addition to the left (LCA) and right (RCA) coronary arteries (Fig 1c$_{ii}$). Another

167 improvement was the ability to fully immunolabel and image intact adult hearts (Fig. 1d).

168 Immunostaining of α-SMA labeled arterial vessels throughout the entire adult heart (Fig.

169 1e), even deep within the septum (Fig. 1f). Co-staining with arterial endothelial marker,

170 Connexin40, confirmed extensive overlap in both neonate and adults (Fig. 1b$_{iii-v}$ and

171 data not shown). Qualitatively, the density of arteries is much greater in neonates

172 compared to adult (Compare Fig.1a and 1d), and more branches were detected when

173 compared to μCT methods, both in neonatal and adult stages[41]. These data

174 demonstrate that iDISCO and Light sheet microscopy together, are capable of

175 effectively labeling and imaging smooth muscle covered arteries throughout neonatal

and adult hearts.

## Neonate (P6) Wild Type



**a** Max Intensity Projection  **b** Z-stack subset  **c** 3D Tracing

RCA · SpA · LCA · α-SMA · Connexin40

## Adult (P60) Wild Type



**d** Max Intensity Projection  **e** Z-stack subset  **f** ROI

α-SMA

Anbazhakan* and Rios Coronado* et al., Figure 1

**Figure 1: Whole-organ imaging of coronary arteries at cellular resolution.** Neonate and adult hearts (atria removed) subjected to tissue clearing and immunolabeling with alpha-smooth muscle actin (α-SMA) and imaged using a Light sheet microscope. (**a**) Maximum intensity projection of entire neonate heart. (**b**) Z-Stack subset projections of Light sheet images (**b**$_{i-ii}$) or those captured using a confocal microscope (**b**$_{iii-v}$). High magnification of septum shows complexity of the septal artery (**b**$_{iii}$) and of LCA shows

184 colocalization of α-SMA+ branches with artery marker Connexin40 (purple
185 arrowheads)($b_{iii-v}$). An α-SMA$^{low}$Connexin40- vein (orange arrowheads) is also present
186 in $b_{iii-v}$. (c) 3D rendering of myocardial volume (red)($c_i$) and main coronary artery
187 branches: Right (RCA), Septal (SpA) and Left (LCA)($c_{ii}$). (d) Maximum intensity
188 projection of entire adult heart. (e and f) Z-Stack subsets of indicated heart regions (e)
189 and region-of-interest (ROI) images (f) reveal the high resolution and specificity of
190 immunolabeling with this technique. Scale bars: a-c, 300 µm; d-f, 500 µm.
191
192        To characterize collateral arteries using this novel method, we imaged neonatal

193 and adult mice subjected to myocardial infarction (MI)(uninjured mouse hearts do not

194 generally contain collaterals)[9,10]. Collateral arteries form faster in neonates than in

195 adults[9]. Thus, injured neonatal hearts were harvested 4-days post MI while adult hearts

196 were collected 28-days post-MI, followed by arterial immunolabeling and clearing. A

197 collateral tracing pipeline was developed first using images of neonatal hearts (Fig. 2a).

198 ImageJ's Simple Neurite Tracer plugin[42,43] was used to trace, in a semi-automated way,

199 every α-SMA+ vessel that originated downstream of the LCA occlusion (suture) and

200 connected to either the RCA, SpA, or the LCA upstream of the occlusion. Traced paths

201 were isolated and masked so that 3D rendering in Imaris created a map of every

202 collateral artery found post-MI (Fig. 2b). The resolution of our method allowed us to

203 annotate the precise collateral segments that bridged two artery branches (Fig. 2$b_{ii}$). A

204 collateral bridge was defined as the segment of continuous smooth muscle covered

205 vessel that existed between two branch tips with opposing branch angles (Fig. 2c).

206 Tracing did not detect collateral connections in non-injured neonate hearts (Fig. S1).

207 Thus, this method reliably identifies collateral arteries in whole heart images.

208        To ascertain where collateral bridges were localized with respect to injured

209 myocardium, we labeled all coronary vessels in the neonate with Podocalyxin and used

210 the autofluorescence signal to observe surviving cardiac muscle. Areas lacking

211 autofluorescence, which were not present in uninjured hearts, delineated injured

212 myocardium, which was confirmed by accompanying disrupted vasculature (Fig. 2d).

213 Injured regions were outlined and overlaid onto collateral models (Fig. 2$b_i$). Collateral

214 bridges were usually located at the edge of the infarcted area, connecting regions of

215 muscle and vascular death to unaffected sites in the heart (Fig. 2d). These same

216 methods were then used to identify collaterals and injured myocardium in adult hearts.

217 Similar patterns were observed (Fig. 2e-g).

218        We next quantified collateral connection type, numbers, and relative sizes in our

219    images. Collateral connections were categorized based on which artery they connected

220    (Fig. 2h). The majority of connections in both neonate and adult hearts were SpA-LCA.

221    Neonate hearts formed more LCA-LCA and fewer RCA-LCA connections than adults

222    (Fig. 2h). Neonate hearts also formed approximately 40% more collaterals than adults

223    (Fig. 2i), and their diameters were larger, both absolutely and relative to the proximal

224    LCA (Fig. 2j and data not shown). (Normalization to proximal LCA was performed to

225    account for small differences in individual mouse body size.) These data highlight the

226    importance of advanced imaging methods for observing accurate vascular remodeling

227    patterns, i.e., those involving the septal artery, and underscore the significant

228    differences between young and old hearts.

**Neonate 4 days post-MI**

**a** MIP

**b** 3D rendering of collateral traces

**c** 3D reconstruction

**d** Z-stack subset

**Adult 4 weeks post-MI**

**e** MIP

**f** 3D rendering of collateral traces

**g** 3D reconstruction

**h** Septal connections are the most abundant collateral type

Neonate n = 152

Adult n = 62

LCA-LCA  SpA-LCA  RCA-LCA

**i** More collaterals post-MI in neonate

**j** Neonatal collaterals are larger than adult
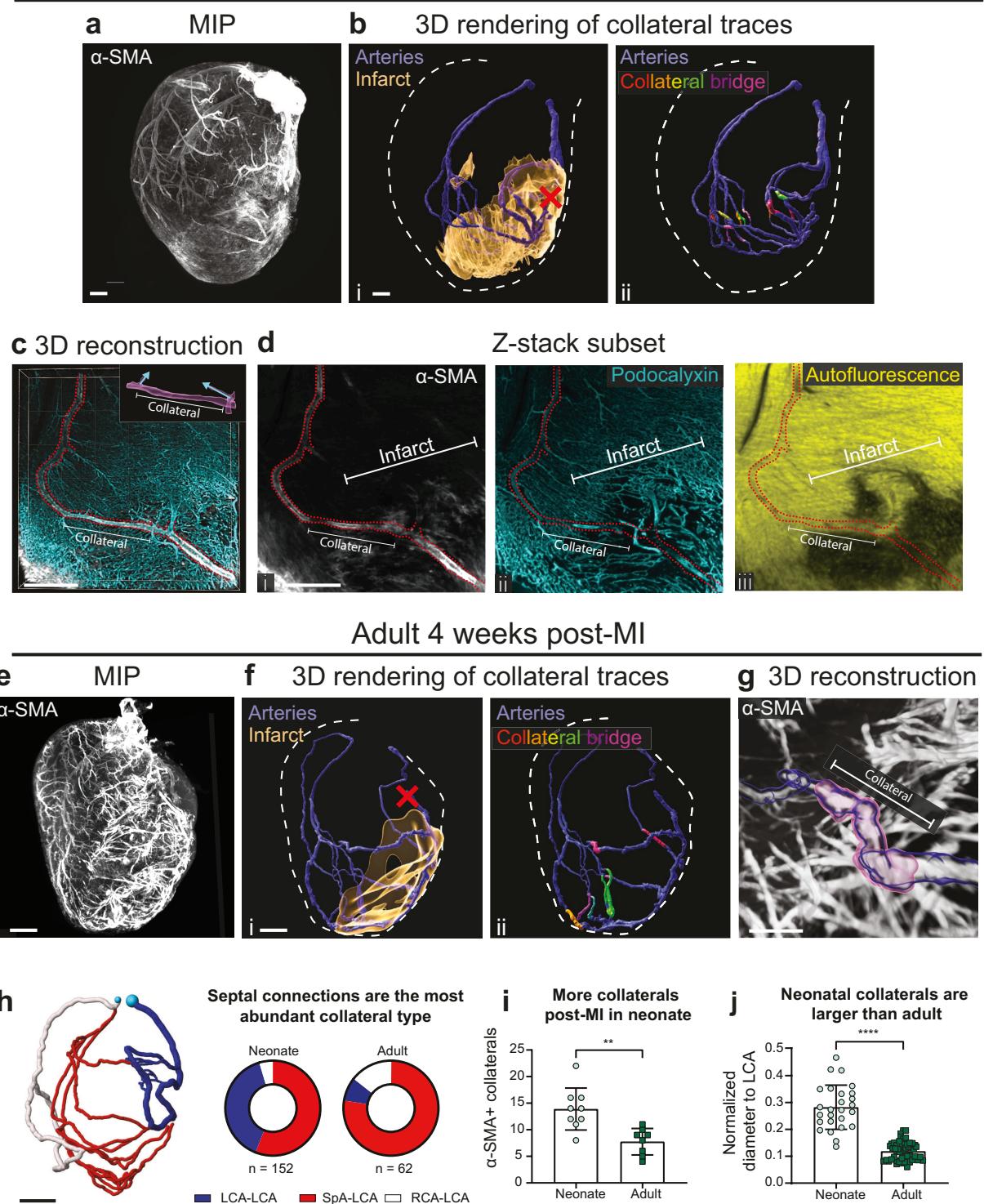
Anbazhakan* and Rios Coronado* et al., Figure 2

229

**Figure 2: Increased collateral arteries in neonate versus adult hearts post injury.**
(**a-d**) Whole organ imaging of P6 neonatal heart labeled with α-SMA post myocardial

10

232 infarction (MI). (**a**) Maximum intensity projection (MIP) of entire heart. (**b**) Collateral
233 connections traced from downstream of suture (red X) were 3D rendered and overlaid
234 with infarct volume (**b$_i$**) and collateral bridges (**b$_{ii}$**). (**c**) 3D reconstruction of 100 μm Z-
235 stack containing a representative collateral bridge within a traced vessel (red dotted
236 line). (**d**) MIP of a 35 μm Z-stack within **c** highlighting an α-SMA+ collateral (**d$_i$**) and its
237 relation to Podocalyxin labeling all vessels (**d$_{ii}$**) and Autofluorescence labeling surviving
238 myocardium (**d$_{iii}$**). (**e-g**) Adult (16-week-old) injured hearts labeled with α-SMA. (**e**) MIP
239 of entire heart. (**f**) 3D rendering of collateral connections overlaid with infarct volume (**f$_i$**)
240 or collateral bridges (**f$_{ii}$**). (**g**) 3D reconstruction of representative collateral bridge (pink).
241 (**h**) Classification and distribution of collateral connections. (**i**) Collateral numbers in
242 neonate (n=9 hearts) and adult (n=8 hearts) post-MI. (**j**) Collateral diameters in neonate
243 (n=26 hearts) and adult (n=55 hearts) post-MI normalized to the proximal LCA. Scale
244 bars: **a-b** and **e-f**, 300 μm; **c-d** and **g-h**, 150 μm. Right (RCA), left (LCA), and septal
245 (SpA) coronary arteries. Error bars are st dev: **, p≤.01; ****, p≤.0001.

**Modeling coronary blood flow**

247     We next sought to understand how these collaterals might restore blood flow in

248 the presence of a vascular occlusion. An *in silico* approach was employed that would

249 allow us to computationally estimate blood flow while at the same time manipulating

250 different parameters in isolation, such as collateral number, size, and location. First, an

251 anatomically representative model of the native adult coronary tree was created using

252 the open-source software, SimVascular (www.simvascular.org)[44], from a Light sheet

253 image of a non-injured adult heart labeled with α-SMA (Fig. 3a). The Light sheet images

254 (Fig. 3a$_i$) were used as a guide for drawing path lines through every artery in the heart

255 up to tertiary branches (Fig. 3a$_{ii}$, Methods). Arteries were then segmented by drawing a

256 circle that encompassed the entire width at even intervals along the vessel (Fig. 3a$_{iii}$).

257 SimVascular was used to convert the segmentations into a 3D model (Fig. 3a$_{iv}$). We

258 next measured the amount of tissue shrinkage that occurs during iDISCO by calculating

259 heart volumes pre- and post-clearing (Fig. 3b$_i$). Shrinkage was on average 37% (Fig.

260 3b$_{ii}$), and, thus, the model was computationally uniformly scaled up by 1.58-fold (Fig.

261 3b$_{iii}$). The result was a model reflecting the realistic anatomic 3D architecture of an adult

262 mouse coronary artery tree.

263     This model was then used to computationally estimate physiologically realistic

264 blood flow parameters throughout the arterial network. The simulations first required

265 setting boundary conditions. At the aortic inlet, a flow waveform was set based on

266 experimentally measured blood velocities from the literature for the neonate[45] and

11

267    adult[46]. Two outlet boundary conditions were set: 1. An RCR Windkessel model

268    representing the systemic circulation at the aortic outlet[47], and 2. A lumped parameter

269    network (LPN) representing the coronary vessels downstream of the 3D model[48,49] (Fig.

270    3c). The lumped parameters included values accounting for vessel resistance at

271    downstream arteries, capillaries, and veins and intramyocardial pressure due to

272    contraction of the ventricle (Fig. 3c). Simulations were run on initial estimated

273    parameters (see Methods) and were subsequently tuned to match expected flow splits

274    between coronary branches to ensure our CFD simulation was distributing the flow

275    proportionally. Flow splits were calculated based on perfusion territories for each of the

276    3 main branches of the coronary arteries. Each region of the myocardium was

277    connected to its closest arterial end branch, and all the subregions were identified as

278    belonging to branches of either the LCA, RCA, or SpA (Fig. 3d$_{i-ii}$). The method

279    estimated the LCA, RCA, and SpA to perfuse 60%, 25%, and 15% of the myocardium,

280    respectively (Fig. 3d$_{ii}$). Using this information to tune outlet boundary conditions (Fig.

281    S2, Methods) resulted in close agreement between estimated perfusion territory and

282    simulated flow splits (Fig. 3d$_{iii}$). Outlet boundary conditions were held constant as

283    stenosis severity was increased. While this doesn't account for remodeling events due

284    to the stenosis, we are specifically modeling the immediate flow of collaterals arteries

285    that exist before a stenosis would develop. In total, the adjustments to the model and

286    boundary conditions provided a model with close concordance to native physiology.

287          Our next goal was to investigate collateral blood flow, and one benefit of a

288    computational approach is that parameters, such as collateral number/size and stenosis

289    severity, can be virtually modified and systematically tested (Fig. 3e). We placed virtual

290    collaterals within the native coronary tree model described above, using post-injury

291    imaging data to guide general placement (see Fig. 2). Computationally derived pressure

292    values were then used to precisely adjust placement at each branch so that collaterals

293    joined two regions of equal pressure. This minimized flow across collaterals without

294    stenosis, which is important to establish a consistent baseline so that different

295    configurations could be properly compared (Fig. 3e, Fig. S3). These guidelines were

296    used to produce 5 different collateral configurations in the adult heart (Fig. S3). We

297    compared pressure difference, flow, and shear stress in all collaterals from each

298 configuration to Poiseuille's law, which analytically describes flow through a circular

299 cylinder, to ensure the results of our simulations were reasonable (Fig. S4, Methods).

300 These data verified virtually-placed collaterals for use in computational flow modeling.

301 　　　Because we wanted to make comparisons between adult and neonate hearts, we

302 performed the same workflow with an uninjured P6 heart. Perfusion territories were

303 similar, but a lower aortic inflow was prescribed for neonates to match lower mean

304 pressures following published values[45,50]. Four collateral configurations were produced

305 for neonates (Fig. S3). Then, adult and neonate models were used to investigate re-

306 perfusion upon virtual stenosis.

**a  3D Modeling Pipeline**

i. Image Stack → ii. Path Lines → iii. Segmentations → iv. 3D Model

**b  Accounting for Tissue Reduction**

i.

ii.

iii. Original → 1.58x → Final

**c  CFD Simulation**

Aortic Inflow
Aortic RCR     Coronary LPN

**d  Perfusion Territories**

i. Individual Outlets → ii. Integrated Outlets

32.6 mm³
RCA
LCA
SpA
15.8 mm³      8.93 mm³

iii.

| Branch | Perfusion Territory | | CFD Simulation | | Percent Error (%) |
|---|---|---|---|---|---|
| | Volume (mm³) | Volume Fraction | Flow (mm³/s) | Flow Fraction | |
| LCA | 32.6 | 0.568 | 5.67 | 0.599 | 5.18% |
| RCA | 15.8 | 0.272 | 1.7 | 0.254 | -6.62% |
| SpA | 8.93 | 0.159 | 0.98 | 0.147 | -7.54% |
| Total | 57.3 | 1 | 8.35 | 1 | N/A |

**e  Virtual Collaterals**

Collateral Sizes
20µm
28µm
40µm

Stenosis Level
0%
75%
90%
95%
97%
99%

60 — 30 Pressure (mmHg)

Anbazhakan* and Rios Coronado* et al., Figure 3

307

308  **Figure 3: Building a physiologically representative 3D model of mouse coronary**
309  **arteries.** (**a**) Pipeline for generating 3D models from Light sheet images. (**b**) Scaling
310  model to account for tissue volume reduction during iDISCO procedure. Measuring
311  heart volumes pre- and post-processing (**b**$_i$) yielded an average reduction value (**b**$_{ii}$)
312  used to generate a scaling factor for models (**b**$_{iii}$). (**c**) Schematic of coronary simulation
313  with a prescribed flow waveform at the inlet, RCR boundary condition at the aortic
314  outlet, and coronary LPN at each coronary outlet. (**d**) Determining perfusion territories

14

315  required first utilizing the Voronoi algorithm to outline perfusion subvolumes for each
316  individual outlet (**d_i**). Then, subvolumes were grouped by right (RCA), left (LCA), and
317  septal (SpA) coronary branches (**d_ii**). Outlet boundary conditions were tuned by
318  matching simulated flow splits to perfusion territories (**d_iii**). (**e**) Schematic depicting
319  variations on collateral and stenosis parameters used in this study. Collaterals were
320  placed to connect approximately equal pressure zones (white arrows). RCR, 3-element
321  Windkessel model; LPN, lumped parameter network; $P_{im}$, intramyocardial pressure.

**Investigating flow recovery by collateral arteries**

323      We next sought to understand the level of flow recovery by virtual collaterals in

324  the presence of coronary occlusions. One way to quantify re-perfusion is to sum the

325  flows from all outlets downstream of the virtual stenosis and compare this to a

326  normalized baseline flow with no stenosis (set at 100%). As expected, with no

327  collaterals in adults total flow downstream of stenosis decreases when percent

328  occlusion increases, especially above 90% (Fig. 4a, top row in chart). When comparing

329  all the configurations tested at all stenosis levels, the configuration with 9 collaterals at

330  40 µm (9col, 40µm) provides the most flow recovery benefit, especially at 99% stenosis

331  where it restores almost 25% of the non-stenotic flow compared to just 1% without

332  collaterals (Fig. 4a, right-most column in chart). However, this extent of collateralization

333  does not occur naturally with coronary artery ligation in adult mice (see Fig. 2i and refs

334  9,10). We noted that configurations similar to those observed experimentally, i.e. 6-

335  12col, 20µm, recovered very little flow as measured by this method (Fig. 4a). These

336  data demonstrate that collateral arteries as they naturally form after adult coronary

337  occlusion are not expected to appreciably recover blood flow, but that increasing

338  diameters, which is a major factor in reducing overall resistance, could enhance their

339  function.

340      In contrast to the poor function of adult collaterals, those of the same size and

341  number in neonates performed well. The configuration that naturally forms in neonates

342  (i.e. 12col, 20µm, see Fig. 2i and ref 9) is estimated to recover up to 60% of total flow

343  downstream of a 99% stenosis (Fig. 4b). Remarkably, the largest diameter tested (40

344  µm) only required one vessel to provide massive recovery in neonates (Fig. 4b, last row

345  in chart). As mentioned above, to compare adult and neonate flow recoveries, it is

346  important to confirm that collaterals generally connect equal pressure zones (+/- 10

347    mmHg) so that all configurations start with a similar collateral flow. This was further

348    evident by the observation that adding collaterals did not change total downstream flow

349    without stenosis and primarily increased flow only with increasing stenosis severity (Fig.

350    S3). We concluded that collaterals in neonate hearts perform better than in adults.

351          The above analysis calculated overall recovery of pre-stenosis levels, but clinical

352    data indicate that myocardial tissue could be supported at approximately 30% of

353    baseline flow[51,52]. Thus, we next sought to gain a more nuanced understanding of

354    recovery by considering individual outlet perfusion territories downstream of the

355    stenosis, so that we could observe if certain regions were receiving sustainable re-

356    perfusion (i.e. >30% re-perfusion). First, we grouped all perfusion territories downstream

357    of the stenosis to obtain the full volume-at-risk (Fig. 4c) and then plotted the percentage

358    of that volume that is re-perfused above a certain threshold (Fig. $4c_i$). This revealed that

359    while there were still no sustainably re-perfused regions in the 12col, 20µm and 6col,

360    28µm configurations, the 3col, 40µm and 9col, 40µm configurations were able to sustain

361    10 and 25% of the volume-at-risk, respectively (Fig. $4c_{i-iii}$). However, in the neonate, the

362    6col, 20µm re-perfused 80% of the volume-at-risk over the 30% threshold while the

363    12col, 20µm and 1col, 40µm configurations re-perfused the entire volume-at-risk (Fig.

364    $4d_{i-iii}$). These data emphasized that collateral configurations of the same size, and thus

365    same resistance, function better in the neonatal heart.

**a  Adult Flow Recovery**
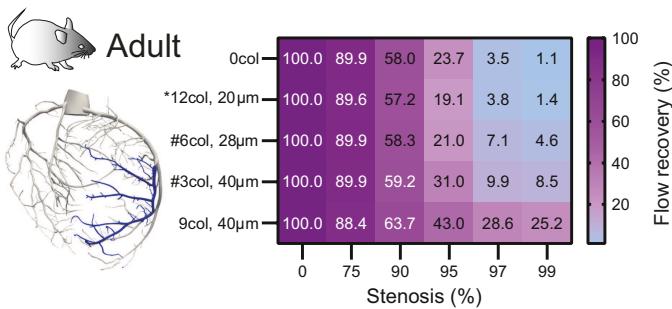
**b  Neonate Flow Recovery**
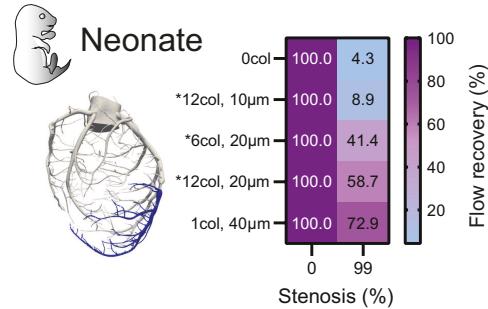
**c  Adult Volume-at-Risk Re-perfused**
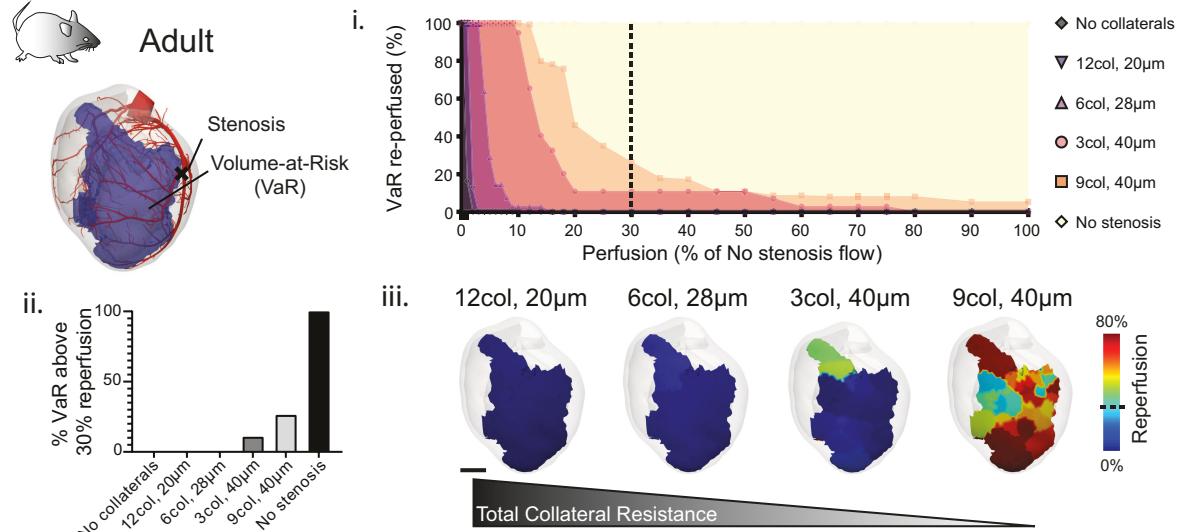
**d  Neonate Volume-at-Risk Re-perfused**

Anbazhakan* and Rios Coronado* et al., Figure 4

366
367
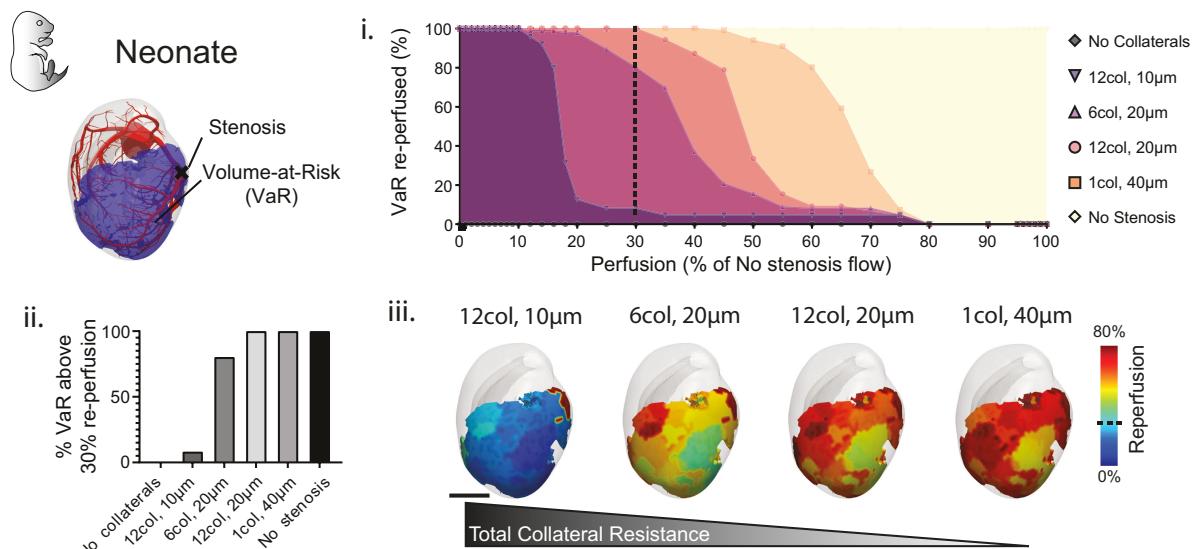
**Figure 4: Collateral arteries are predicted to perform better in neonate hearts.** (**a** and **b**) Measuring re-perfusion capacity by calculating percent of total non-stenotic flow in vessels downstream of the virtual occlusion (blue vessels). Asterisks denote configurations observed experimentally; hashtags denote sizes observed following CXCL12 injection[9]. Functionally significant re-perfusion is only seen in neonates under physiological conditions. (**c** and **d**) Percent re-perfusion of myocardial volume-at-risk (VaR)(blue region) in adult (**c**) and neonatal (**d**) models. Cumulative histogram ($c_i$, $d_i$), bar graph of percent VaRs above 30% ($c_{ii}$, $d_{ii}$), and visual maps of re-perfusion within the VaR ($c_{iii}$, $d_{iii}$). Dotted line marks the ischemia threshold of 30% non-stenotic flow. Scale bar: 1000 µm.

We next explored whether a more favorable placement of collaterals could improve the poor performance seen in adults. We started with a 3col, 40µm configuration (Fig. 5a, blue) and moved each collateral to a more proximal location in the coronary tree (Fig. 5a, red). This manipulation almost doubled total flow recovery (Fig. 5b) and approximately tripled the volume of myocardium re-perfused above the 30% threshold (Fig. 5c-e).  Thus, variation in location can improve collateral function, likely because the pressure difference with more proximal attachments is much greater, resulting in increased flows.

The above data suggested that fewer, larger collaterals are better than many, smaller ones (see Fig. 4). However, in those experiments, the total collateral resistance varied between the configurations. We tested this hypothesis by varying the number and size of the collaterals while keeping the total resistance equal. Simulations were performed on 2 configurations—16col, 20µm and 1col, 40µm (Fig. 5f). While total flow recovery was approximately equivalent (Fig. 5g), the 1col, 40µm configuration was uniquely able to re-perfuse 5% of the volume-at-risk above 30% (Fig. 5h-j). This analysis shows that fewer, larger collaterals could be more beneficial because they at least protect a portion of the myocardium while many, smaller collaterals distribute the re-perfusion so that none reach protective levels.

18

Placement of collateral affects flow

**a** 3col, 40µm (a) / 3col, 40µm (b) — $\Delta P_{Col}$

Pressure (mmHg): C1, C3, C2 — (a), (b)

**b**

| | Stenosis (%) 0 | 99 |
|---|---|---|
| 0col | 100.0 | 1.1 |
| 3col, 40µm (a) | 100.0 | 11.8 |
| 3col, 40µm (b) | 100.0 | 19.4 |

Flow recovery (%)

**c** Volume-at-Risk Reperfused (%) vs Perfusion (% of No stenosis flow)
No collaterals / 3col, 40µm (b) / 3col, 40µm (a) / No stenosis

**d** % Volume-at-Risk Reperfused: No collaterals, 3col, 40um (a), 3col, 40um (b), No stenosis

**e** 3col, 40µm (a) / 3col, 40µm (b) — Reperfusion 0%–30%
Equal Total Collateral Resistance

Tradeoff between many and few collaterals

**f** 16col, 20µm $\Delta P_{Col} \approx 30$mmHg / 1col, 40µm (a) $\Delta P_{Col} \approx 30$mmHg

**g**

| | Stenosis (%) 0 | 95 | 97 | 99 |
|---|---|---|---|---|
| 0col | 100.0 | 23.7 | 3.5 | 1.1 |
| 16col, 20µm | 100.0 | 32.6 | 8.2 | 5.8 |
| 1col, 40µm | 100.0 | 28.6 | 6.3 | 4.9 |

Flow recovery (%)

**h** Volume-at-Risk Reperfused (%) vs Perfusion (% of No stenosis flow)
No collaterals / 16col, 20µm / 1col, 40µm / No stenosis

**i** % Volume-at-Risk Reperfused: No collaterals, 1col, 40µm, 16col, 20µm, No stenosis

**j** 16col, 20µm / 1col, 40µm — Reperfusion 0%–30%
Equal Total Collateral Resistance

Anbazhakan* and Rios Coronado* et al., Figure 5

397

398 **Figure 5: Evaluating collateral placement and the tradeoff between collateral**
399 **number and size. (a-e)** Investigating how collateral placement affects re-perfusion

400   using two collateral configurations. (**a**) 3 collaterals with either high (red square) or low
401   $\Delta P_{Col}$ (blue square). (**a**) Graph showing the $\Delta P_{Col}$ changes caused by altering placement
402   for each collateral. (**f-j**) Investigating re-perfusion tradeoff between many, small and few,
403   large collaterals using two configurations: 16 collaterals at 20µm (red circle) and 1
404   collateral at 40µm (blue circle). (**b, g**) The total non-stenotic flow in vessels downstream
405   of the virtual occlusion. Cumulative histogram (**c, h**), bar graph of percent volume-at-risk
406   (VaR) above 30% (**d, i**), and visual maps of re-perfusion within the VaR (**e, j**). Dotted
407   line marks the ischemia threshold of 30% non-stenotic flow. $\Delta P_{Col}$, pressure difference
408   across collaterals.

409   **Adult vs. neonate coronary artery morphology**

410        Given that collaterals of the same size and total resistance were predicted to

411   proportionally recover more flow in the neonate, we sought to understand why and first

412   investigated arterial pressures at collateral formation sites at both ages. To facilitate

413   comparisons between the two time points, Strahler ordering was used to classify branch

414   segments into orders based on hierarchal position in the coronary tree and vessel

415   diameter[53,54]. Order 13 represented the aorta, order 12 represented the most proximal

416   coronary artery segments, and subsequent orders represented downstream vessels

417   until 8, which were the most distal branches modeled (Fig. 6a). This was used to

418   compare hemodynamic and anatomical quantities at similar points in the coronary tree

419   in both the adult and neonate. While absolute aortic and proximal coronary (order 12)

420   pressures were vastly increased in the adult, the pressures at the most distal coronary

421   tips (order 8) were approximately equal (Fig. 6b and c). Quantification revealed that the

422   pressure drop along the coronary tree was ~20 and ~50 mmHg in neonate and adults,

423   respectively (Fig. 6c). This is also true when considering just the segments downstream

424   of the stenosis, making $\Delta P_{Ad} > \Delta P_{Neo}$ (Fig. 6b and c). Thus, the collateral pressure

425   difference ($\Delta P_{Col}$) required to restore pre-stenotic flow downstream of the occlusion is

426   higher in the adult. Specifically, the $\Delta P_{Col}$ needs to be about ~2-fold more in the adult to

427   restore the same flow. Given that we see similar distal pressures at both stages, this

428   explains why, even though collaterals in both recover the same absolute flow, it is much

429   lower than the baseline, non-stenotic flow in the adult.

430        Our next experiments were aimed at understanding why $\Delta P_{Ad}$ was greater than

431   $\Delta P_{Neo}$. Two factors critical for determining $\Delta P$ are flow rate and total resistance of the

432   coronary tree. First, we compare the flow rate at each Strahler order between the

433    neonate and the adult coronary models. Literature values indicated that aortic flow in

434    adults is approximately ten times more than neonate, which was used as the inflow

435    boundary condition for the computational model (see Fig. 3c)[45]. Simulations revealed

436    that flow was also 10-fold greater for every vessel order modeled in the coronary tree

437    (Fig. 6d). Shear stress was lower in neonates compared to adults, particularly in higher

438    order vessels (Fig. 6e). We confirmed this trend held true when increasing the mesh

439    size from 1.8 to 10 million elements; there was less than 10% difference in average

440    shear stress with increased mesh resolution. Flow values were in line with increases in

441    myocardial volume over time, i.e. volumes at P32 were more than 10-fold of P0 (Fig. 6f).

442    The ability to rapidly determine volumes allowed us to analyze additional timepoints,

443    which revealed a linear increase in myocardial volume during the first two weeks of life,

444    a plateau between P18-25, and a burst of growth from P25-32. Second, we used the

445    simulated flows and pressures to calculate the total resistance of the 3D coronary

446    model. Neonate total vascular resistance was 3-fold that of adults (Fig. 6g). Since flow

447    was increased by 10-fold, the 3-fold decrease in total resistance is not enough to offset

448    flow increases. Thus, while the resistance of the coronary vasculature decreases in the

449    adult, it's not able to lower the resistance enough to balance the much greater flow,

450    which manifests in a greater $\Delta P$ in adults.

**a** Strahler ordering

Aorta ... Tips
13 ... 8
Strahler Order of segment

**b** Pressure distribution

Neonate

Adult

Potential stenosis

$\Delta P_{Col}$ ... $\Delta P_{Neo}$

0 ... 100
Pressure (mmHg)

Potential stenosis

$\Delta P_{Ad}$

$\Delta P_{Col}$
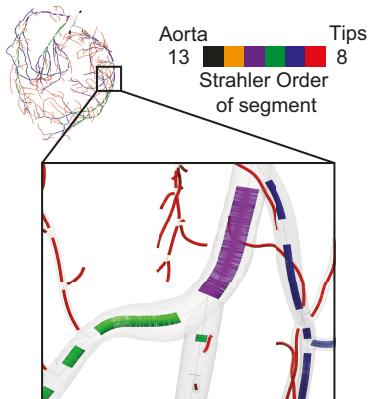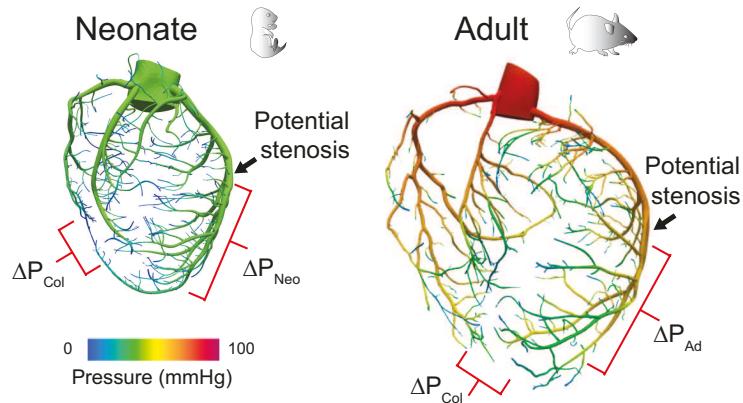
**Greater pressure loss due to increased flow**

**c** Mean Pressure

Potential stenosis

$\Delta P_{Ad}$

$\Delta P_{Neo}$

$\Delta P_{Col} \approx \Delta P_{Neo} < \Delta P_{Ad}$
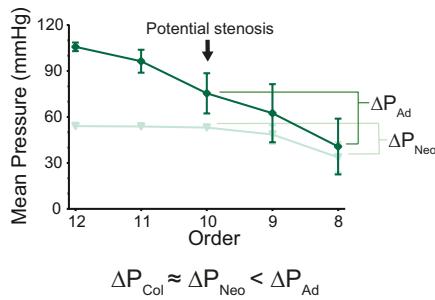
**d** Flow
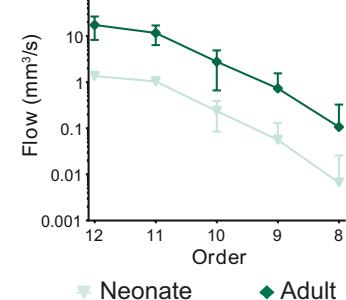
**e** Wall Shear Stress
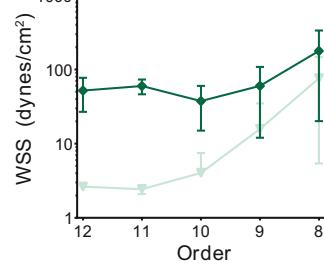
▽ Neonate  ◆ Adult

**f** Heart volume increases proportional to flow

****  ***  **
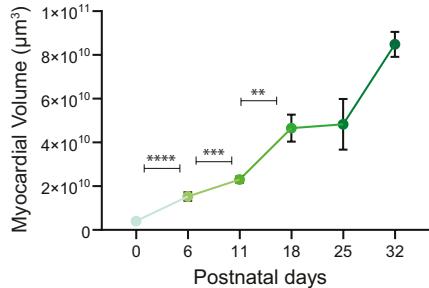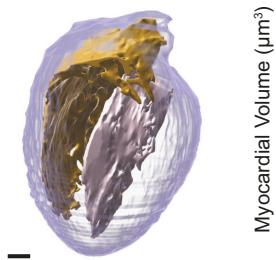
**g** Resistance moderately decreases in adult

■ Neonate
■ Adult

Total Vascular Resistance
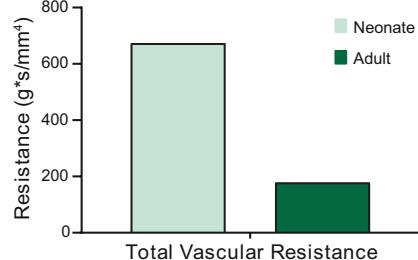
Anbazhakan* and Rios Coronado* et al., Figure 6

**Figure 6: Investigating hemodynamic differences between neonate and adult.** (**a**) Strahler ordering categorizes segments of the arterial tree from order 13 (aorta) to order 8 (distal tips). (**b**) Pressure distribution in the neonate and adult coronary models. (**c-e**) Quantification of pressure (**c**), flow (**d**), and wall shear stress (**e**) vs. Strahler order (n=1 P6, n=1 P60 heart model). (**f**) Heart volume segmentation (left) and quantification (n=3 P0, n=7 P6, n=3 P11, n=2 P18, n=2 P25, n=2 P32 hearts). (**g**) Total 3D resistance of the coronary tree in neonate and the adult models revealed a 3-fold decrease in adults. $\Delta P_{Col}$, pressure difference across collaterals; pressure difference downstream of a

22

460    potential stenosis in the neonate, $\Delta P_{Neo}$, and the adult, $\Delta P_{Ad}$. Error bars are st dev: **,
461    p≤.01; ***, p≤.001; ****, p≤.0001.
462
463         We next investigated what features contribute to the nonproportional decrease in
464    resistance with respect to the flow increase from neonate to adult. Two factors critical
465    for determining resistance are vessel diameter and number of branches. Increases in
466    these parameters both work to lower total resistance, diameter being the most
467    impactful. Surprisingly, we found that the diameters were the same across all Strahler
468    orders in each model (Fig. 7a). We validated this by comparing diameters of the most
469    proximal segments of the RCA, SpA, LCA and aorta in multiple replicates of neonatal
470    and adult hearts (Fig. 7b). The coronary stem diameter remains virtually the same while
471    aortic diameter increased with age (Fig. 7b), a result we validated using an orthogonal
472    method (Fig. 7c). Thus, coronary diameters do not grow proportionally to heart volume,
473    which suggests that diameter expansion does not function to relieve vascular resistance
474    in the face of increased flow demand in adults.
475         If arteries do not increase in diameter, additional branches must be added to at
476    least partially offset the increased flow that accompanies heart growth. We next
477    quantified branching during postnatal development. Comparing the Strahler ordering of
478    the two stages revealed that the number of distal vessels (order 9 and 8) were vastly
479    increased (Fig. 7d), aligning with qualitative observations from imaging (see Fig. 1).
480    Since the 3D SimVascular models did not contain arterioles distal to tertiary branches,
481    we further investigated morphometry by manually tracing all α-SMA vessels in a
482    representative branch—the Left Circumflex (LCx)(Fig. 7e, red). Imaris software filament
483    tracing binned each segment of the LCx according to branching levels and quantified
484    the number of arteriole tips (Fig. 7f). The number of branching levels spiked between
485    P0-6 and then hit a plateau until another spike between P25-32 (Fig. 7g). Number of
486    tips increased linearly up to P18 with another spike between P25-32 (Fig. 7h). The P6-
487    18 plateau in number of branch levels compared to the linear increase in number of tips
488    over the same time period indicated that the coronary arteries grow by adding branch
489    segments along the entire length of existing branches. We also observed that the length
490    of each segment was constant among all ages tested (Fig 7i). This results in a coronary
491    tree with many lateral branch segments of a set length.

## Coronary diameters remain constant



**a** Diameter of Segments (n=1)

**b** Coronary diameter (n=3)

**c** Coronary diameter (n=3)
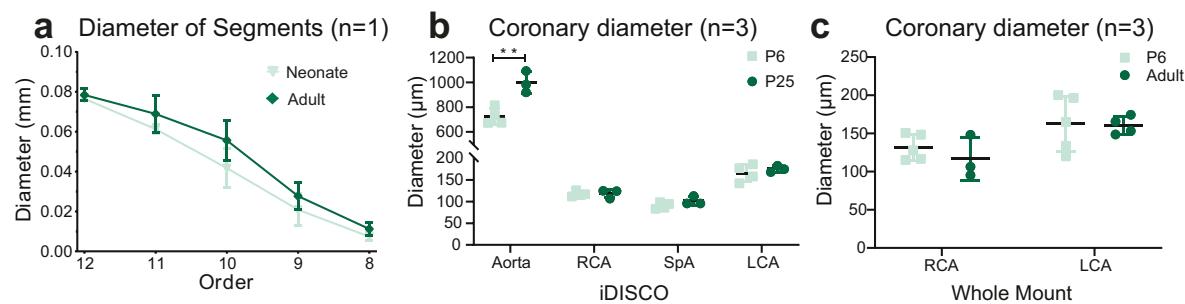
## Branching and number of tips increase



**d** Number of Segments (n=1)

**e** Schematic of LCx

**f** LCx Branch Levels

P0    P6    P18    P32

**g**    0.98  0.16  0.23  0.03  0.79  Level per day

**h**    30.4  25.5  27.6  2.4  75.7  Art.tip per day

**i**
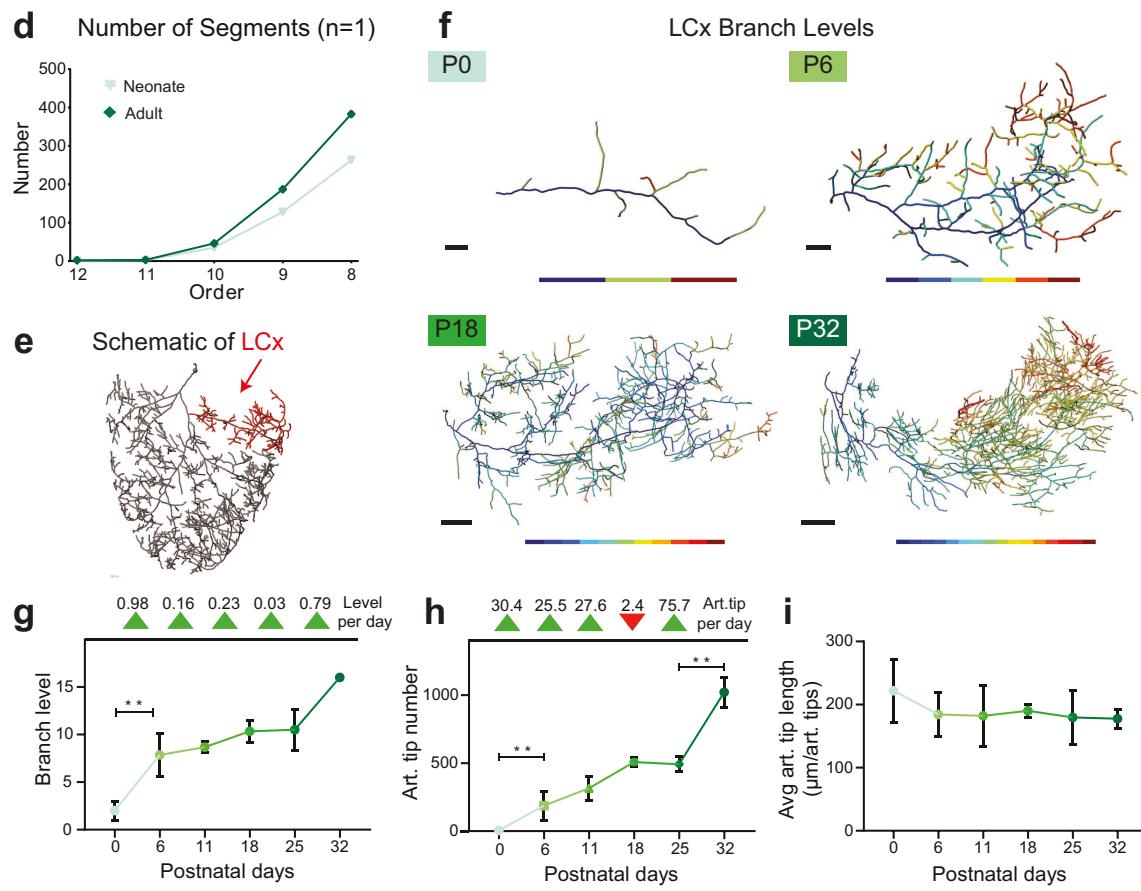
Anbazhakan* and Rios Coronado* et al., Figure 7

**Figure 7: Main branch coronary artery diameters remain constant while branching increases throughout postnatal development.** (**a**) Quantification of diameter vs. Strahler order. (**b** and **c**) Main branch coronary diameter measurements from additional hearts processed through iDISCO (**b**) or conventional whole mount immunostaining without clearing (**c**). (**d**) Number of artery segments per Strahler order. (**e**) Semi-manual segmentation of LCA, highlighting the left coronary circumflex branch (LCx, red). (**f**) Visual representation of branch levels in 3D reconstructed LCx traces. (**g**)

501    Number of branch levels of LCx at each timepoint. Arrowheads indicate rate of change
502    per day. (**h**) Number of arterial (art.) tips in the LCx at each age. Arrowheads indicate
503    rate of change per day. (**i**) Average art. segment length in LCx at each timepoint. (**a**,**d**)
504    n=1 P6, n=1 P60 hearts; (**b**) n=4 P6, n=3 P25 hearts; (**c**) n=5 P6, n= 4 P60 hearts;
505    (**g**,**h**,**i**) n=3 P0, n=7 P6, n=3 P11, n=2 P18,  n=2 P25, n=2 P32 hearts. Scale bars: **f**, P0,
506    100 µm; P6, 200 µm; P18, 400 µm; P32, 500 µm. Error bars are st dev: **, p≤.01**.**

## Human fetal and adult coronary collateral arteries

508        A subset of human hearts contains collateral arteries, which are easily observed

509    during an angiogram and are correlated with increased survival in heart disease

510    patients[55,56]. We sought to identify how our computational modeling studies could help

511    us better understand human collateral function. Thus, we compared the data available

512    from human hearts to our mouse models. We measured vessel diameters for the

513    collaterals observable in angiograms from five patients living with chronic total

514    occlusions (Fig. 8a). This patient population was chosen because their collaterals would

515    be expected to sufficiently support myocardial perfusion downstream of the occlusion

516    without exercise. To compare to mouse data, we also normalized human diameters to

517    the most proximal segment of the LCA. Collateral diameters were on average 15

518    percent of the LCA (Table 1). These values were in between those observed in the

519    neonate and adult mouse hearts (Table 1). However, a limitation of this comparison is

520    that diameters in angiograms were measured in a 2D projection, which may affect

521    accuracy of absolute values. We also found an average of 2 collaterals per heart (Table

522    1), but comparisons with mouse data using this parameter are less desirable because

523    angiograms will only highlight a subset of the collaterals that immunostaining would

524    label. These data provide a foundation to determine re-perfusion benefit, but a very

525    precise understanding in humans will need to consider the different pressure

526    distributions resulting from human specific morphology.

527        Using post-mortem perfusions, studies from the 1960s reported the presence of

528    coronary collateral arteries in infants and children[57,58], but no one has reported whether

529    collaterals develop during embryogenesis. Furthermore, using smooth muscle coverage

530    to identify collateral connections in humans has not been done. We processed two fetal

531    hearts aged 17 and 22 weeks with the same whole-organ immunolabeling method used

532    for murine hearts (Fig. 8b_{i-ii} and Fig. S5). Both hearts had visible collaterals on the

533    dorsal and ventral sides (Fig. 8b$_{iii-iv}$ and Fig. S5). Remarkably, >17 collaterals were

534    detected per side (Fig. 8c), which suggests that the whole human heart has at least 40

535    pre-existing, smooth muscle covered collaterals forming during embryonic development.

536    On the ventral side, most connections bridged distal branches of the RCA and LCA

537    while the majority on the dorsal side connected two LCA branches (Fig. 8d). Collateral

538    diameters were not significantly different across locations or between ages and were on

539    average 7 percent of the most proximal LCA segment (Fig. 8e). Thus, unlike mouse,

540    human hearts have mechanisms in place to form native collateral arteries as part of

541    normal development, which we hypothesize could be the precursors for those that

542    preserve myocardium downstream of an occlusion.
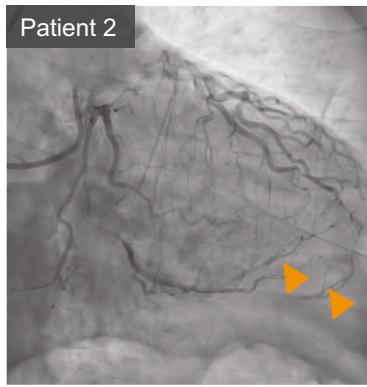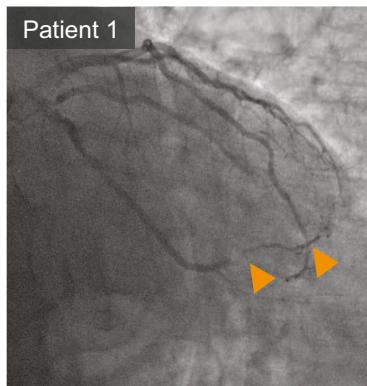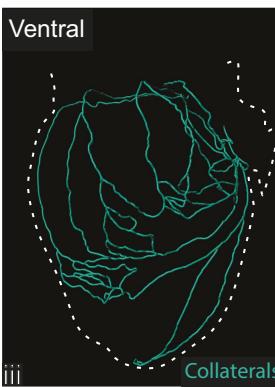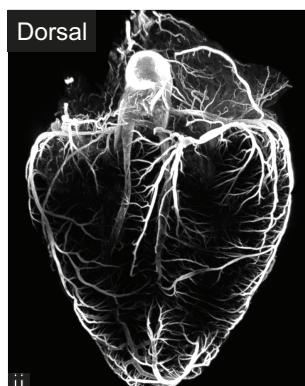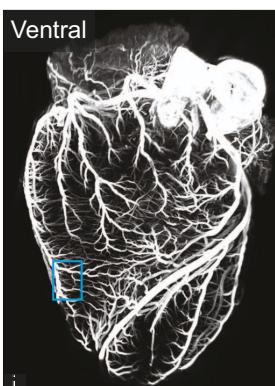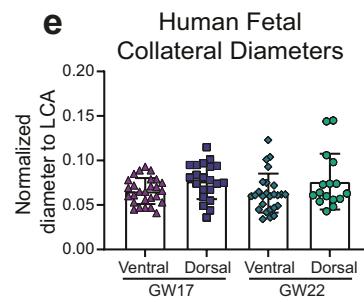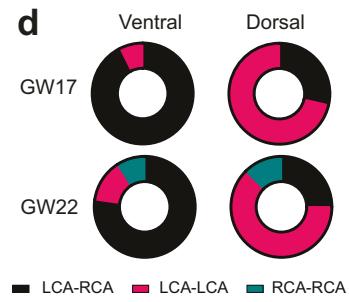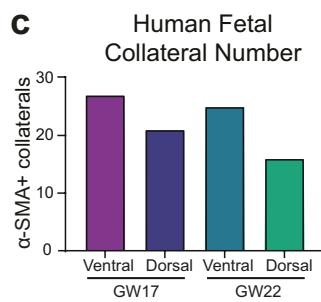
**Figure 8: Collateral arteries in adult and fetal human hearts.** (**a**) Representative invasive angiograms from adult chronic total occlusion (CTO) patients. Orange arrowheads indicate collaterals. (**b$_{i-ii}$**) Maximum intensity projections of fetal human heart, ventral (**b$_i$**) and dorsal (**b$_{i-ii}$**) sides. (**b$_{iii}$**) Traced collateral connections on the ventral side. (**b$_{iv}$**) High magnification (boxed in **b$_i$**) of collateral bridges (arrowheads). (**c-e**) Quantification of collateral bridge numbers (**c**), connection types (**d**), and diameters (**e**). GW, gestational week. Scale bars: 1 mm.

| Species | Age | Condition | Number of Collaterals | Diameter Ratio to LCA | LCA Diameter (mm) | Measurement |
|---|---|---|---|---|---|---|
| Human | Adult | CTO | 1.80±0.84 | 0.15±0.06 | 5.67±1.09 | Angiogram |
| | Fetal GW17 | Native | 48 | 0.07±0.02 | 0.42 | LSM |
| | Fetal GW22 | Native | 43 | 0.07±0.03 | 0.53 | LSM |
| Mouse | Neonate | MI-4 days | 13.9±3.95 | 0.28±0.08 | 0.12±0.04 | LSM |
| | Adult | MI-4 weeks | 7.75±2.49 | 0.12±0.03 | 0.13±0.04 | LSM |

**Table 1. Human fetal hearts have many relatively small collateral arteries.**
Quantification of collateral artery parameters in human adult CTO patients (n=5), fetal
GW17 (n=1) and GW22 (n=1) hearts, neonate (P6) 4 days post-MI (n=9), and adult (16-
weeks) 4 weeks post-MI (n=8) mouse hearts. GW, gestation week; P, postnatal day;
CTO, chronic total occlusion; MI, myocardial infraction; LCA, left coronary artery; LSM,
light sheet microscopy. Reported values are mean ± st dev.

## Discussion

This study is, to our knowledge, the first-time 3D CFD has been used to quantify
hemodynamic forces in the adult and neonatal mouse coronary vasculature. The
findings here suggest the possible benefit of promoting the growth of fewer, larger
arteries and the natural benefit collaterals have in restoring pressure downstream of a
stenosis in neonatal hearts.

Our whole-organ immunolabeling method identifying the structural relationship of
collaterals to coronary artery branches suggested that, in mice, the septal artery could
play a more critical role in cardiovascular recovery than previously thought. Recent
studies utilizing flattened hearts for whole-mount imaging failed to distinguish the SpA
from the RCA[9]. Here, tissue clearing and Light sheet microscopy allowed visualization
of the intact 3D structure and the complete septal artery, revealing its architectural
complexity in healthy hearts. Recent studies have outlined SpA development and
proposed that the location of its origin from the aorta could significantly impact cardiac
recovery during injury models[59]. Our imaging results suggest a potential route to
investigate how positional interactions between these branches could impact vascular
repair.

577    While other studies have performed automatic segmentation and flow modeling
578    of mouse brain and retinal vasculature, there is currently no standard for segmentation
579    and 3D flow simulations in the entire mouse coronary vasculature[35]. We manually
580    segmented over 300 vessels of the adult and over 200 vessels of the neonate coronary
581    network to ensure accurate representation and high model fidelity for fluid simulations
582    using SimVascular. Manual segmentations are currently required because the signal-to-
583    noise ratios, even with high performing antibodies such as anti-α-SMA, are easily
584    recognized by the human eye, but can cause errors in fully automatic segmentations.
585    Methods are in development to improve automation, such as TubeMap, which utilizes
586    machine learning algorithms to produce high fidelity automated segmentations of the
587    brain vasculature[60]. Future work will focus on using or developing similar methods to
588    automate segmentation for cardiac vasculature.
589    One major advantage of CFD modeling over *ex vivo* measurements of
590    experimental samples is the capability to easily modify one feature, i.e. collateral
591    structure, while keeping all other parameters constant. We tested multiple collateral
592    configurations within the same model to understand the relationship of number, position,
593    and diameter on flow recovery, without potential secondary effects from mouse-to-
594    mouse variations in coronary structure. In this study, we considered values above 30%
595    of non-stenotic perfusion levels as being beneficial. This was based on previous *in vivo*
596    and *in vitro* studies suggesting that myocardial tissue receiving less than 25-30% of
597    baseline flow begins to display measurable signs of cardiac dysfunction. For *in vivo*,
598    when patients were subjected to balloon occlusion of the LCA, only those with greater
599    than approximately 30% coronary flow index maintained normal ST-segments during
600    electrocardiogram[51]. During Langendorff perfusion preparations, heart rate and left
601    ventricle pressures began recovering to normal values above 25% of normal perfusion
602    rates[52]. Simulations demonstrated that increasing diameters or positioning collaterals
603    more proximally allowed them to restore a greater volume of cardiac tissue to this 30%
604    re-perfusion value, more so than increasing numbers of smaller collaterals. One
605    limitation here is that we are not able to test the exact re-perfusion level required for
606    myocyte viability specific to each heart However, we believe that these data are
607    valuable to other scientists in the field studying collateral arteries by giving them general

29

608    guidelines of how tested factors affect collateral flow and re-perfusion. With this

609    understanding, physical differences between phenotypes or conditions can be more

610    confidently related to functional differences.

611          It was surprising that even the most effective collateral configuration modeled in

612    the adult—9col, 40µm—re-perfused only ~20% of myocardium above the 30% ischemic

613    threshold. This is consistent with studies showing significant scar formation in MI

614    models in mice (permanent coronary ligation), even in the presence of collaterals[10]. This

615    underscores the importance of understanding blood flow through experimentally-

616    induced collateral arteries when considering inducing these vessels as a therapeutic

617    option. Conversely, the virtual collaterals in the neonate with the same characteristics

618    were predicted to have a remarkable ability to shunt flow to the ischemic volume-at-

619    risk—consistent with studies demonstrating the resilience of neonates after total

620    occlusion MI experiments. This, combined with our data that neonates form more

621    numerous and larger collaterals naturally in response to injury, may explain why studies

622    show great recovery post-MI in the neonate via collateral arteries in contrast to adults[9].

623          This innate difference in collateral function was attributed to a low pressure drop

624    in the neonatal coronary tree compared to adults due to the increased flow in the adult

625    not being compensated by an equal reduction in vascular resistance. It is important to

626    note that at both ages, the pressure at the tips is approximately 40 mmHg, indicating

627    that our two models were segmented to a similar extent. The gradual, steady decrease

628    in pressure in the adult arises from the more extensive branching observed compared to

629    the neonate, which is in agreement with studies of pig coronary arteries[61]. While we

630    demonstrated there is very little pressure drop in native neonate coronary arteries, the

631    pressure downstream of the 3D model is expected to abruptly drop to capillary levels.

632    The reduction in total coronary resistance from neonate to adult is in concordance with

633    general trends found with µCT measurements of coronary vessels >40 µm in mice aged

634    1 week to 6 weeks old, but quantitatively much greater in our models[41,62]. While these

635    studies described the coronary tree morphology with quantitative scaling laws, they

636    were not able to quantify small diameter arteries, which is evident by the noticeably

637    missing arteries in their 1-week mouse coronary model compared to our Light sheet

638    imaged P6 hearts. Future work could investigate how these quantitative scaling laws

639    apply to vessels we are able to visualize with our method.

640    We next sought to compare our mouse results to human data. It was unexpected

641    that fetal human hearts contained more native collaterals than the injured neonate and

642    adult mouse as well as diseased adult human hearts, although it is difficult to make

643    comparisons between whole-organ α-SMA staining and angiograms. This finding

644    corresponds with data that suggests collaterals tend to decrease during adolescent

645    years because more were found in the fetal stages compared to neonate humans[57,58].

646    Since these collaterals are much smaller than those found in adult human diseased

647    hearts via angiogram, it may indicate that small collaterals in the adult heart go

648    undetected. In addition, if we can preserve and enlarge these collaterals in adulthood,

649    they have the potential to greatly improve cardiac perfusion in patients suffering from

650    CAD.

651    Overall, by combining advanced computational and imaging techniques, a novel

652    connection between collateral flow and native morphological differences, and thus

653    pressure distributions, was established. By bridging these two fields, we uncovered how

654    fundamental coronary morphology changes from embryonic to adult in both mouse and

655    humans affect collateral flow. These findings provide insight into why coronary collateral

656    arteries are better suited for recovering from an injury in young hearts compared to old.

657

658    **Limitations**

659    One limitation of this study is that we were not able to measure subject-specific

660    aortic flows and pressures for each mouse coronary vasculature *in vivo* to use for

661    boundary conditions. However, with literature-derived averaged flows scaled to the

662    model size, we expect this to have a very minor effect on the absolute quantities of

663    collateral flow as described here and thus little effect on the overall relative differences

664    between the collateral configurations and ages.

665    Another limitation is that it is not currently possible to measure the outlet

666    pressure of the coronary tree *in vivo* to validate computational modeling. Due to the

667    small size and inaccessibility of the coronary vasculature in mice, it is challenging to

668    determine *in vivo* flows and pressures at the pre-capillary level. Pressure

669 measurements taken from rabbits and dogs suggest that 50-70% of the pressure is lost

670 when blood reaches the capillary bed[63,64]. In our study, we tuned the outlet boundary

671 conditions such that the resistance of the 3D model was 65% of the total coronary

672 resistance, which matches expected values from literature[63]. We tested the sensitivity of

673 our results to changes in outlet pressure by adjusting the outlet resistances and found

674 that relative differences between the collateral configurations remained the same.

675       In our modeling approach, we assumed that the downstream arteries and

676 capillaries do not undergo remodeling. While this assumption is not valid for estimating

677 flow in collaterals that form in response to injury, we first sought to develop our

678 modeling to test the effectiveness of pre-existing collaterals. In future studies, we would

679 enhance our computational methods to capture capillary remodeling events that occur

680 due to the re-routing of blood flow.

681

682 ## Methods

683 ### Animals

684       All mouse colonies were housed and bred in the animal facility at Stanford

685 University in accordance with institutional animal care and use committee (IACUC)

686 guidance.

687 ### Immunolabeling and iDISCO clearing

688       Whole heart vasculature staining was performed following the modified iDISCO+

689 protocol previously described[37,39]. For all following steps, tissue was always agitated

690 unless noted otherwise. Briefly, animals were perfused with PBS through the dorsal

691 vein, and fixed in 4% paraformaldehyde (Electron Microscopy Science 15714) at 4°C for

692 1hr (neonatal hearts) or 2hr (adult hearts), washed 3X in PBS and stored in PBS with

693 0.01% sodium azide (w/v, Sigma-Aldrich S8032) until ready to process. Hearts were

694 dehydrated in increasing series of methanol/ddH$_2$O dilutions (20%, 40%, 60%,

695 80%,100% 2X) for 1hr each, followed by overnight incubation in 66% dichloromethane

696 (DCM, Sigma-Aldrich 34856) and 33% methanol. Next, tissue was washed 2X in

697 methanol 100% for 4hrs and bleached overnight at 4°C in 5% hydrogen peroxide

698   (Sigma-Aldrich 216763) in methanol. Next, the hearts are rehydrated in methanol/ddH-

699   $_2$O dilutions (80%, 60%, 40%, 20%) for 1hr each, followed by PBS, 0.2% Triton X-100

700   PBS (2X) and overnight 20% dimethyl sulfoxide (DMSO), 2.3% Glycine (w/v, Sigma

701   G7126), 0.2% Triton X-100 PBS at 37°C for 2 days. For immunostaining, hearts were

702   blocked in 10% DMSO, 6% Normal Donkey Serum (NDS, Jackson ImmunoResearch

703   017-000-121) in 0.2% Triton X-100 for 2 days at 37C.  Primary antibodies, αSMA-Cy3

704   conjugated (1:300, Sigma C6198), Connexin-40 (1:300, Alpha diagnostic cx40A), and

705   Podocalyxin (1:1000, R&D Systems MAB1556) were prepared in PBS with 5%DMSO,

706   3% NDS in 0.2% Tween-20, 0.1% Heparin (w/v, Sigma-Aldrich H3393) and incubated at

707   37°C for 4-14 days. Secondary antibodies conjugated to Alexa 647 (Jackson

708   ImmunoResearch) were matched 1:1 in concentration to their primary target and in

709   prepared in PBS with 3% NDS in 0.2% Tween-20, 0.1% Heparin for the same primary

710   incubation days at 37°C. Washes after each antibody incubation in PBS with 0.2%

711   Tween-20, 0.1% Heparin were performed in 30min increment until the end of the day,

712   followed by an overnight wash. Before clearing, samples were embedded in 1% low-

713   melting agarose (Sigma-Aldrich A9414) in PBS and dehydrated in methanol/ddH$_2$O

714   dilutions (20%, 40%, 60%, 80%,100% 2X) for 1hr each and 100% overnight. Next,

715   hearts were incubated in 66% DCM and 33% Methanol for 2.5hrs, followed 2X 30min

716   100% DCM. Finally, samples were cleared in ethyl cinnamate (ECi, Sigma Aldrich

717   112372), manually inverted a few times, and kept at RT in the dark until and after

718   imaging.

719   **Light sheet imaging**

720        Samples were imaged with LaVision BioTec Ultramicroscope II Light sheet

721   microscope in a quartz cuvette filled with ECi. For imaging, we used a MVX10 zoom

722   body (Olympus) with a 2x objective (pixel size of 3.25 µm / x,y)  at magnification from

723   0.63x up to 1.6x. Up to 1400 images were taken for each heart and the z-steps are set

724   to 3.5µm z step size, and light sheet numerical aperture to 0.111 NA. Band-pass

725   emission filters (mean nm / spread) were used, depending on the excited fluorophores:

726   525/50 for autofluorescence; 595/40 for Cy3; 680/30 for AF647 and 835/70 for AF790.

727   Exposure time was 10ms for single channel and 25ms for multichannel acquisition.

**Perfusion territory mapping**

728

729       To determine the approximate volume of myocardium each outlet of the coronary

730 model was responsible for perfusing we used (1) a model of the myocardial tissue as

731 the total volume to be perfused and (2) the outlet coordinates as the seed points for the

732 subvolumes. We used the background signal from the staining to segment the model of

733 the myocardial tissue and the cap centers for the outlet coordinates. Then, we used a

734 Voronoi diagram algorithm to assign subvolumes of the myocardial tissue to each outlet

735 of the coronary model such that every point in the myocardial mesh was assigned to the

736 closest outlet. Distances to the closest outlet were determined using a dijkstra

737 algorithm. By integrating the subvolumes of every outlet on each of the 3 main branches

738 (LCA, RCA, and SpA), we were able to calculate the approximate percentage of the

739 total myocardial volume that each main branch is responsible for. We used these

740 percentages as targets for the flow splits when tuning the outflow boundary conditions

741 for the fluid simulations.

742       We used outlet coordinates instead of centerlines because we were able to

743 better resolve the small coronary arterioles compared to prior studies[65]. This allows us

744 to be certain that myocardial regions close to an outlet are perfused by that outlet,

745 rather than by a large artery nearby that has no outlet nearby.

**CFD simulation**

746

747       We constructed 3D subject-specific models of the mouse vasculature using

748 SimVascular's cardiovascular modeling pipeline[44]. Briefly, we created path lines for

749 each vessel (about 349 vessels for the adult and 244 for the neonate). Vessels distal to

750 the quaternary branches were ignored. For each path line, the image data was viewed

751 in planes orthogonal to the tangent of the path line to segment the cross-section. Circles

752 were used to approximate the cross-section, as some areas of the vasculature

753 appeared collapsed or deformed. All segmentations were lofted to create a solid model

754 of each branch, and the branches were then unioned together to form a complete

755 geometric model. Finally, the lofted model was discretized into a linear tetrahedral mesh

756 using the commercial meshing library, MeshSim (Simmetrix, Troy, NY), resulting in a

757  total of 600 thousand and 1.8 million elements for the neonatal and adult models,

758  respectively.

759      After obtaining the mesh, we uniformly scaled it to account for the shrinkage that

760  occurs via iDISCO. We quantified the volume change due to our specific clearing

761  protocol using water displacement pre- and post- iDISCO and found that the heart

762  shrank to about 63% of its original volume. So, we uniformly scaled the entire volumetric

763  mesh by the inverse (1.58-fold) to ensure that our model faithfully matched the pre-

764  iDISCO geometry.

765      Inlet boundary conditions were determined as follows. We first determined typical

766  neonate and adult mean pressure and aortic velocity values from literature[45,46,66] (Table

767  2, rows 1-2). Using the mean aortic velocity and the aortic cross sectional inlet area for

768  each mouse used, a subject-specific aortic inflow was calculated and applied. For

769  pulsatile flow simulations, we constructed representative flow waveforms for an adult

770  mouse by digitizing, smoothing, and scaling a waveform from the literature to match the

771  mean inflow at both ages as calculated previously[67]. At the aortic outlet, we applied a

772  simple RCR boundary condition[47] (Table 2, rows 3-5). At the coronary artery outlets, we

773  applied a specialized lumped parameter network to represent the downstream coronary

774  vasculature and the time-varying intramyocardial pressure due to the beating cardiac

775  tissue[48,49,68] (Table 2, rows 6-10). The resistance of each coronary outlet was estimated

776  using Murray's law and tuned such that each of the 3 main branches (LCA, RCA, and

777  SpA) had flow splits equal to the percent volume they perfused. To further tune the

778  capacitances and resistances of the coronary boundary conditions to match literature

779  pressure values[63,64], we used a 0D surrogate model for increased efficiency (Fig. S2).

| | Description | Adult Value | Adult Source | Neonate Value | Neonate Source |
|---|---|---|---|---|---|
| $Q_{aorta}$ | Aortic flow | $6 * 10^2$ | Input | $6.3 * 10^1$ | Input |
| $P_{mean}$ | Mean aortic pressure | $1 * 10^2$ | Target | $4 * 10^1$ | Target |
| $C_{RCR}$ | Aortic outlet capacitance | $1 * 10^{-2}$ | Tuned | $1 * 10^{-2}$ | Tuned |
| $Rp_{RCR}$ | Aortic proximal resistance | $4.8 * 10^{-1}$ | Tuned | $5 * 10^1$ | Tuned |
| $Rd_{RCR}$ | Aortic distal resistance | $1.9 * 10^1$ | Tuned | $2.2 * 10^2$ | Tuned |
| $Ra_{LPN}$ | Coronary artery resistance | $1.9 * 10^2$ | Tuned | $1.7 * 10^3$ | Tuned |
| $Ru_{LPN}$ | Coronary microvascular resistance | $3.1 * 10^2$ | Tuned | $2.8 * 10^3$ | Tuned |
| $Rv_{LPN}$ | Coronary vein resistance | $9.5 * 10^1$ | Tuned | $8.5 * 10^2$ | Tuned |
| $Ca_{LPN}$ | Coronary arterial capacitance | $3.96 * 10^{-6}$ | Tuned | $3.96 * 10^{-6}$ | Tuned |
| $Cim_{LPN}$ | Intramyocardial capacitance | $3.204 * 10^{-2}$ | Tuned | $3.204 * 10^{-2}$ | Tuned |

780 **Table 2. Simulation parameters used for mouse coronary flow modeling.** List of
781 parameters used for computational fluid simulations of the adult and neonate coronary
782 arteries. Input and target taken from literature. Tuned parameters were adjusted so that
783 the simulation matched target values given the input. Units: $Q, \frac{mm^3}{s}$; $P, mmHg$; $C, \frac{s^2 mm^4}{g}$;
784 $R, \frac{g}{mm^4 s}$.
785

786      We globally corrected the viscosity in our pulsatile simulations to 1.25cP to
787 account for the Fahraeus-Lindqvist effect; this is necessary because the apparent
788 viscosity of blood decreases in very small tube diameters (<100µm)[69]. While this may
789 significantly underestimate the shear stress in the aorta, the pressure drop in the
790 coronaries was more representative and important for the findings presented here (see
791 Limitations).
792      We ran blood flow simulations with rigid walls using the stabilized finite element
793 svSolver code in the open-source SimVascular software package[44] to determine
794 spatially and temporally resolved hemodynamic values, such as pressure, velocity, and
795 wall shear stress at every node in the computational mesh. Simulations ran for 5 cardiac
796 cycles with timesteps of .0001 seconds, and hemodynamic values were determined

797    based on the final cardiac cycle. This took approximately 40 hours on 96 cores via

798    XSEDE and 90 hours on 96 cores via Sherlock. Paraview was used for visualization of

799    the results.

800    **Virtual collateral placement**

801          Virtual collaterals were strategically added to native coronary vasculature to

802    minimize the initial pressure difference of the two points the collateral was connecting.

803    Specifically, based on an initial simulation of the native vasculature (without any virtual

804    collaterals), a pressure distribution was determined. Using this pressure distribution,

805    virtual collaterals were placed such that each connected equal pressure zones. We

806    replicated realistic connections as closely as possible given size and pressure

807    constraints (Fig. S3). The resistance of each collateral configuration was calculated via

808    Poiseuille's Law (equation 1).

809    $$Total\ Collateral\ Resistance = \frac{8\mu L}{\pi n r^4}\ (1)$$

810          Where µ is the viscosity, $L$ is length of the collateral, $n$ is the number of

811    collaterals in the configuration, and $r$ is the radius of the collateral.

812    **3D Resistance**

813          To calculate the resistance of the 3D model, we first generated vessel centerlines

814    via the Vascular Modeling Tool Kit (VMTK; vmtk.org). Each point in the centerline was

815    identified as a branch segment if a perpendicular cross-section at that point did not

816    intersect with any other centerline point. If the cross-section intersected more than one

817    centerline point, then it was labeled as a junction region. This separated the centerline

818    into junctions and branch segments between junctions. After labeling every point, we

819    determined the parent (upstream) branch segment and child (downstream) branch

820    segments for each junction region. We then calculated the resistance for each branch

821    segment based on the pressure difference from the most proximal to distal point and the

822    flow within that segment from the simulation. Finally, the overall 3D resistance was

823    calculated starting from the most distal branches using a recursive method to add the

824    segment resistances in parallel or in series based on the connectivity.

## Diameter-defined Strahler Ordering

825

826    We utilized the diameter-defined Strahler ordering system to compare

827    morphometric and hemodynamic quantities at similar positions in the coronary tree

828    between the neonate and adult. This system has been used in previous morphometric

829    studies to classify branch segments into orders that describe the hierarchical nature of a

830    vascular tree[53,70,71]. Using the same labels for branch segments and junction regions as

831    in the 3D resistance calculations, we determined the initial Strahler ordering by setting

832    the most distal segments to order 1 and working backwards up the coronary tree to the

833    aorta. Parent segment orders were set to either equal the greater child order if the two

834    children orders were different or incremented by one if the two child orders were the

835    same. Since neither 3D model of the mouse vasculature included all arteries down to

836    the capillary level (only 5 distinct orders here vs. 11 in other studies[54]), we translated all

837    the orders by a constant such that the order of the most proximal segment of the

838    coronaries was 12 and the aorta was order 13 to ensure consistency with previous

839    studies. Segments were then re-organized based on their diameter to ensure that

840    unbalanced branching (i.e. a very small vessel branching from a large one) was

841    properly accounted for. To do this, we iteratively moved segments to higher or lower

842    orders such that every segment within an order was within 1 standard deviation of that

843    order's mean diameter. With the final diameter-defined Strahler ordering, we compared

844    quantities such as diameter, length, flow, and pressure between the same orders of the

845    neonate and the adult.

## Semi-automated artery tracing

846

847    Subsequential images were imported into ImageJ stacks files, these stacks were

848    then converted into 8-bit and resolution reduced to one-fourth the original. Using

849    ImageJ's plug-in, Simple Neurite Tracer, the branch structures of the LCx were able to

850    be drawn by placing seed points along the length of α-SMA+ vessels[43]. Once every α-

851    SMA+ artery in the LCx branch was completely accounted for within the trace, isolation

852    of the traces was performed by the Fill Out option within the plug-in. The resulting image

853    stack was used as a 3D outline of the arterial structure as the foundation for further

854 modeling and analysis. After discontinuation of Simple Neurite Tracer, the updated

855 version SNT was used in similar manner as above[42].

## 3D Rendering

857 The non-traced image stack was overlaid with the filled LCx stack using the Add

858 Channel option in Imaris. Pixel dimensions were updated from the non-reduced 16-bit

859 image metadata. The Filament Object Tracer module was used to generate an Imaris

860 customizable 3D LCx branch model. Branch tips and length were measured by

861 automatically generated data under Number of Terminal Points, and Total Length fields,

862 respectively. Branch levels were obtained from the Filaments Branch Hierarchy field.

863 Surface objects in Imaris were used for quantifying the sample heart volumes.

864 Myocardium volume was calculated by creating surface objects surrounding the entire

865 sample surface and objects encompassing the lumen of the ventricles. The volumes of

866 the ventricles were then subtracted from the entire heart volume to result in the

867 myocardium tissue volume.

## Murine LCA ligations

869 Neonatal LCA ligations were performed as previously described[9] with minimal

870 modifications. P2 neonates were cooled on ice for 6 minutes to induce hypothermic

871 circulatory arrest and placed in a supine position followed by disinfecting with iodine and

872 ethanol. Dissection was carried through the pectoralis major and minor muscles, and

873 the thoracic cavity was entered via the 4th intercostal space. The LCA was identified

874 and ligated at with a doble knot using 8-0 nylon suture, leaving the LCx intact. The chest

875 muscle and skin were then closed (independently) with interrupted 7-0 prolene sutures.

876 The neonate was then allowed to recover at 37°C warm plate and, when conscious,

877 returned to its mother's care.

878 Adult mice were performed as previously described[72]. Adult mice were subjected

879 to permanent coronary artery ligation, under anesthesia using initially 1.5%–4%

880 isoflurane chamber for induction. The chest cavity was opened, and a 7-0 silk suture

881 was placed around the left coronary artery, with occlusion verified by blanching of the

882 underlying myocardium. The chest was then sutured closed. Following surgery,

883 Buprenorphine (0.1 mg/kg) was used as an analgesic.

**Immunohistochemistry and confocal microscopy**

885 Neonatal or adult hearts were fixed in 4% PFA overnight at 4 °C, and then

886 cryopreserved in 30% sucrose in PBS for 1 day at 4°C. The following day, coronal heart

887 sections (50 μm in thickness) were cut on a cryostat. Sections were rinsed 3X with PBS,

888 blocked in 5% NDS, 0.5% Triton X-100 in PBS for 1hr at RT, and then incubated with

889 αSMA-Cy3 conjugated (1:300, Sigma C6198) in 0.5% Triton X-100 in PBS overnight at

890 4°C. Next, sections were rinsed 3X in 0.5% Triton X-100 in PBS and then mounted on

891 slides and covered with Fluoromount G (SouthernBiotech 0100-01). Tissue was imaged

892 using inverted Zeiss LSM-700 confocal microscope at 5x objective. Digital images were

893 captured with Zeiss Zen software and measured using ImageJ.

**Human hearts**

895 Under IRB approved protocols, human fetal hearts were collected for

896 developmental analysis from elective terminations[73]. Gestational age was determined

897 by standard dating criteria by last menstrual period and ultrasound[74]. Tissue was

898 processed within 1hr following procedure. Tissue was extensively rinsed with cold,

899 sterile PBS while placed on ice, followed by incubation in sterile 4% PFA for 4hrs at 4°C

900 before further iDISCO processing. Pregnancies complicated by multiple gestations and

901 known fetal or chromosomal anomalies were excluded.

902 Human adult samples were acquired from the Stanford Catheterization

903 Angiography Laboratory. All patients displayed symptoms of chronic angina and were

904 scheduled to receive conventional coronary angiography, which was performed

905 according to local clinical standards. Collateral number and size were confirmed by an

906 experienced cardiologist.

**Statistical Analysis**

908 Graphs represent mean values obtained from multiple experiments and error

909 bars represent standard deviation. Unpaired Student's t test was used to compare

910     groups within an experiment and the level of significance were assigned to statistics in

911     accordance with their p values (0.05 flagged as $*$, 0.01 flagged as $**$, less than 0.001

912     flagged as $***$, less than 0.0001 flagged as $****$). All graphs were generated using

913     GraphPad Prism software. Error bars represent ± standard deviation.

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1122 **Contributions**

1123    S.A., P.E.R.C., A.L.M., and K.R.-H. conceived and designed the project. S.A.,
1124 P.E.R.C., A.N.L.S.-Q., and C.K.C. performed experiments. S.A, P.E.R.C., A.N.L.S.-Q.,
1125 A.S., and A.M.H. analyzed data. S.A. performed fluid simulations. P.E.R.C., B.C.R.,
1126 M.Z., and D.B. performed murine cardiac injury studies. K.N. and A.M.P. contributed
1127 human adult and fetal samples, respectively. S.A., M.L.D., and M.P. provided analysis
1128 tools. S.A. and P.E.R.C. prepared figures. S.A., P.E.R.C., A.L.M., and K.R.-H. wrote the
1129 manuscript.

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