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### Abstract

Morphological and magnetic anisotropy can be combined in colloidal assembly to create unconventional secondary structures. We show here that magnetite nanorods interact along a critical angle depending on their aspect ratios and assemble into body-centered tetragonal (bct) colloidal crystals. Under a magnetic field, size-dependent attractive and repulsive domains develop on the ends and center of the nanorods, respectively. Our joint experiment-computational multiscale study demonstrates the presence of a critical angle in the attractive domain, which defines the equilibrium bonding states of interacting rods and leads to the formation of non-close-packed yet hard-contact tetragonal crystals. SAXS measurement attributes the perfect tetragonal phase to the slow assembly kinetics. The crystals exhibit brilliant structural colors, which can be actively tuned by changing the magnetic field direction. These highly ordered frameworks and well-defined 3D nanochannels may offer new opportunities for manipulating nanoscale chemical transformation, mass transportation, and wave propagation.

### Teaser

Nanorods can be magnetically assembled into tetragonal colloidal crystals along a size-dependent critical angle.

## MAIN TEXT

### Introduction

42 Colloidal crystals are ordered superstructures of colloidal particles whose repeating subunits are  
43 much larger than their analogous atomic and molecular crystals (1-4). The spatial configuration of  
44 matter and surface ligands in colloidal crystals, which control many physical and chemical  
45 properties, can be tailored in a nanometer precision by adjusting the subunit composites, sizes,  
46 shapes, and crystal structures (5-8). Therefore, the colloidal assembly has become an effective  
47 strategy in producing many functional materials in photonics (9-12), structural materials (13, 14),  
48 robotics (15-17), and catalysis (18, 19). The assembly of either spherical or highly faceted colloids  
49 is mainly dominated by entropic processes that involve depletion, hydrophobic forces, and polymer  
50 “elasticity,” producing densely packed colloidal crystals with close surface contact (3, 20, 21).  
51 Theoretical simulations and colloidal self-assembly at multiscale have demonstrated this common  
52 assembly manner (22-24).

53 For exploring more complex superstructures, sole or joint anisotropic interactions have been  
54 introduced (25), including specific binding between biomolecules (particularly DNA) (26-29), van  
55 der Waals forces of ligands (1, 30), magnetic forces (31-33), and electrostatic forces (3, 34, 35). A  
56 few advanced strategies use directed interactions between Janus microparticles for creating  
57 emerging superstructures (36-40). Among these established methods, the nanoscale magnetic  
58 assembly provides precise control over colloidal crystal symmetry and orientation; and the dynamic  
59 interplay between magnetic forces and other underlying forces of different length scales offers great  
60 opportunities in creating emerging superstructures and smart materials. A great benefit in this  
61 regard is the widely accessible range of monodisperse magnetic colloids with defined shapes,  
62 tunable properties, and delicate structures. Scientists are achieving even more exquisite control over  
63 the synthesis of magnetic particles, including those with various shapes (41-44), core/shell  
64 nanoparticles (45-47), and Janus particles with magnetic patches (39, 48, 49), setting the stage ready  
65 for exploiting their assembly into complex superstructures with remarkable collective properties.  
66 In this work, we demonstrate that body-centered tetragonal (*bct*) superstructures with reduced  
67 crystal symmetry can be developed by the magnetic assembly of nanorods in colloidal solutions. It  
68 has been known since 1269 that opposite magnetic poles attract, favoring dipole-to-dipole end-on  
69 attachment (50). At the nanoscale, however, magnetic nanorods assemble along a size-dependent  
70 critical angle. The shape-induced anisotropic interaction generates two attractive domains separated  
71 by a magnetically repulsive center domain. It directs nanorods to assemble along the critical axis  
72 into *bct* crystals, rather than the side-on attachment favored in entropy-dominated assembly or end-  
73 on attachment favored by magnet opposite pole attraction. A simple extension of the nanoscale  
74 magnetic assembly to different nanorods yields *bct* crystals with tunable lattice constants, tailorable  
75 physical properties, readily accessible surfaces, and interconnected nanochannels.

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## 78 Results

79 FeOOH nanorods (aspect ratios from 3 to 30) were synthesized by hydrolysis of FeCl<sub>3</sub> (Figs. S1  
80 and S2, Table S1) and further reduced to magnetic nanorods after being coated with silica of  
81 controllable thickness (Fig. S3)(43, 51). In this surface-protected reduction, the silica shell  
82 maintains the rod shape during the phase transition of FeOOH to Fe<sub>3</sub>O<sub>4</sub> and alleviates the  
83 considerable volume shrinkage. A transmission electron microscopy (TEM) image in Fig. 1a  
84 reveals the high uniformity of the magnetic rods (322×70 nm). The magnetic assembly was  
85 performed by simply sitting a rod dispersion above a permanent magnet with a field strength of 150  
86 mT. As shown in Figs. 1b, 1c and Fig. S4, stripe-like, green crystals formed. The scanning electron  
87 microscope (SEM) image in Fig. 1c reveals that the magnetic nanorods are packed into a centered  
88 rectangular lattice on the crystal surface. The apparent orthogonality and different periodicity  
89 between transverse and longitudinal directions demonstrate the reduced symmetry of the crystals  
90 and exclude any triclinic, monoclinic, or cubic crystal systems. These observations suggest a few

91 possible Bravais lattices, including body-centered orthorhombic, face-centered orthorhombic, and  
92 body-centered tetragonal structures.

93 The silica fixation allows the colloidal crystals to be transformed into other colloid lattices by post-  
94 assembly wet chemical processes. For example, selectively etching away  $\text{Fe}_3\text{O}_4$  yields crystals of  
95  $\text{SiO}_2$  shells (**Fig. 1d**). In a 2D projection, the contact joints between neighboring rods form high-  
96 density areas (dark regions in the 2D projection) separated by low-density, low-contrast domains  
97 (**Figs. S5-S7**). The projection of the assembled crystals along different crystallographic directions  
98 produced characteristic 2D TEM images, with two typical lattices being observed, rectangular  
99 phase (**Fig. 1e** and **2f**) and centered rectangular phase (**Fig. 1g** and **1h**). In **Fig. 1e**, the periodic  
100 empty spaces indicate that the rods are in hard contact but not closely packed. Crystals sharing this  
101 characteristic projection have identical transverse periodicity. These observations approve that the  
102 assembled structures are body-centered tetragonal (*bct*) crystals since the hard contact between  
103 neighboring rods and the same transverse periodicity do not support the different interplanar  
104 spacing of (100) and (010) facets in orthorhombic crystals. A high-magnification image of the same  
105 area reveals overlaps of rod ends, creating defined joints and interconnected nanometer poles (**Fig.**  
106 **1f**). In **Fig. 1g** and **1h**, we observed layer-by-layer stacking of crystal planes with apparent periodic  
107 nodes because of the partial rod overlap. The projection of rod packing along this crystallographic  
108 direction is a rectangular 2D lattice. The arrangements of rods in the two typical planes are  
109 illustrated in the 2D rendering (**Fig. 1i**). The rods packing in (110) facets is consistent with the SEM  
110 images in **Fig. 1c**. The projection patterns (ball-stick bond diagram in **Fig. 1i**) of (100) and (110)  
111 facets are consistent with TEM images in **Fig. 1e** and **1f**, respectively.

112 The rod positions in the crystals are identified and mapped in **Fig. 2a**. Their radial distribution  
113 ( $r_{cc}$ ) in **Fig. 2b** demonstrates the excellent orders and defines the lattice spacing ( $d$ ) of (110), (100),  
114 (101), and (001) facets. The 3D rod arrangement and the crystal rotational symmetry were  
115 systematically studied by electron tomography (**Movie S1**). In **Fig. 2c**, we started with a projection  
116 of (110) facets,  $P_{(110)}$ , and acquired TEM images by continuously rotating crystals along [001] and  
117 [110] crystallographic directions, denoted as  $R_{[001]}$  and  $R_{[110]}$ , respectively. The initial  $P_{(110)}$  exhibits  
118 a layer-by-layer structure with a centered rectangular rod packing in (110) facets (**Fig. 2d**). When  
119  $R_{[001]}=45^\circ$ , we observed a gradual evolution to  $P_{(100)}$ , with rectangular rod arrangements in (100)  
120 facets. In  $R_{[110]}$ , the initial  $P_{(100)}$  transforms to  $P_{(111)}$  when the tilting angle increased to  $60^\circ$ , leading  
121 to a rectangular out-of-plane topography of rods (**Fig. 2e**). A 3D rendering model and ball-stick  
122 bond diagram are illustrated in **Fig. 2f**. In a unit cell, eight rods occupy the vertex sites, with one in  
123 the center, forming a *bct* lattice. Its length along the a- and c-axis is 210.6 nm and 513.9 nm,  
124 respectively. The angle between [111] and [110] is  $30^\circ$ . Using nanorods with different sizes and  
125 silica thicknesses, we obtained several *bct* colloidal crystals with tunable critical angles, lattice  
126 constants, and packing densities (**Figs. S8-S14**). In **Fig. 2g**, projections of (100) crystal facets are  
127 obtained with rod aspect ratio increasing from 2.25 to 18.5. Due to the dipole-dipole attractions,  
128 isotropic nanospheres were assembled into 1D nanochains (52, 53). In the phase diagram (inset in  
129 **Fig. 2h**), long nanorods (aspect ratio > 20) self-assembled into disordered fibers largely because of  
130 the segregation of magnetic cores during reduction.

131 For  $\text{Fe}_3\text{O}_4@SiO_2$  colloids with abundant surface charges, the electrostatic repulsion is a major  
132 counterforce to the magnetic attraction (54). Its classic use involves the multipolar expansion of an  
133 analytical equation, whose direction is mainly along the connecting line of interacting colloids. The  
134 monopole approximation is operational for isotropic, homogeneously charged spheres (**Fig. S15**)  
135 or anisotropic colloids with considerably large separation (55). As colloids approach, their  
136 morphological anisotropy becomes more effective. Our finite element analysis (**Fig. S16**) points  
137 out that the electrostatic repulsion is highly dependent on interparticle separation and that, in closely  
138 packed assemblies, it gradually approaches the surface normal of interacting rods. At  
139 thermodynamic equilibrium, the tangent component of the magnetic attraction is expected to vanish  
140 to avoid any relative translational shifts between nanorods, and the normal component is balanced

141 by the electrostatic and steric repulsion. For understanding the force dynamics, one nanorod (in red  
142 color in **Fig. 3a**) is continuously swept along a defined trajectory in hard contact with a primary rod  
143 (in blue color). The magnetic force between them is dependent on silica thickness ( $t$ ) and azimuth  
144 angle ( $\Theta$ ) (**Fig. S17** and **Movie S2**). To identify the critical angles ( $\phi_c$ ) along which interacting rods  
145 thermodynamically equilibrate, we decompose the overall magnetic force into tangent ( $F_{\text{tang}}$ ) and  
146 normal components ( $F_{\text{norm}}$ ). In **Fig. 3b**,  $F_{\text{norm}}$  changes from negative to positive values at  $\Theta=43^\circ$ ,  
147 which defines the repulsion and attraction domains, respectively. In the attraction regime, we  
148 specify a critical point at  $F_{\text{tang}}=0$ , where the magnetic attraction is along the surface normal. For 50-  
149 nm silica shells, the theoretical  $\phi_c$  is  $68.1^\circ$ , and its good agreement with the measured value of  $63.5^\circ$   
150 from TEM images appreciates the reasonable accuracy of this simple calculation. The normal  
151 component in the right panel of **Fig. 3c** demonstrates the presence of the two attractive poles and  
152 the repulsive center, with their boundary shifting to small  $\Theta$  regions as silica thickness increased  
153 from 5 to 50 nm. We observed the first decrease and then increase in  $\phi_c$  in the attractive domain  
154 (dashed blue line in the left panel of **Fig. 3c**). To understand the deterministic role of aspect ratios,  
155 we analyzed  $\phi_c$  for different magnetic rods and map their  $\phi_c$  in a 3D surface in **Fig. 3d**. For isotropic  
156 nanospheres,  $\phi_c$  remains  $90^\circ$  due to the dipole-dipole attraction, producing 1D chains with end-on  
157 attachment (**Figs. S18** and **S19**). Anisotropic nanorods favor offset packing with a defined  $\phi_c$ , which  
158 finally degenerate to  $90^\circ$  as the  $\text{SiO}_2$  thickness increases. The  $\phi_c$  increased as aspect ratios simply  
159 because of rod elongation (**Figs. S20-S27**).

160 The offset binding between two rods initiated the nucleation of *bct* crystals as neighboring rods  
161 assemble at preferential crystalline sites along a predicted critical angle. It likely breaks the lateral  
162 symmetry of rods, creating a few preferred sites for rod deposition. The crystal growth features  
163 preferential in-plane rod tessellation in  $\{110\}$  facets, as evidenced by contrast differences in TEM  
164 images; the uniform contrast of TEM images along  $\langle 110 \rangle$  projection (**Fig. S28b-d**) implies even,  
165 sequent rod packing in the exposed (110) facets. Along  $\langle 100 \rangle$  (**Fig. S28e-g**) projections, a  
166 contrasting gradient implies a gradual decrease of crystal thickness from crystal center to edge.  
167 These observations suggest a defined rectangular cross-section of *bct* crystal grains (**Fig. S28a**) and  
168 the preferential in-plane rod packing in (110) facets. While the critical angle analysis demonstrates  
169 the offset packing of interacting nanorods, the formation of 3D tetragonal crystals requires higher  
170 dimension analysis of the assembly dynamics. We extended the force computation to a 3D model  
171 (**Figs. S29-S32** and **Movie S3**). The force field in **Fig. 3e** suggests a strong repulsion (red arrows)  
172 when the rod overlaps the bottom ones. We observe a gradual shift to a strong attraction when the  
173 rod moves to positions above cavities (blue arrows). In the magnetic potential landscape (**Fig. 3f**),  
174 we recognize periodic bonding sites above bottom cavities due to the localized low magnetic  
175 potential. There exist four active sites above and below each rod in the 2D sheet, resulting in eight  
176 bonded rods shared by its neighbors.

177 To resolve the assembly kinetics, we analyzed the crystallization by *in situ* synchrotron-based  
178 small-angle X-ray scattering (SAXS) based on the geometry shown in **Fig. S33** (56). The  
179 representative 2D SAXS patterns are shown in **Figs. 4a, S34, and Movie S4**. At 0 min, the  
180 anisotropic scattering pattern implies the liquid crystal phase of rods with only orientational orders  
181 and parallel alignment to a vertical magnetic field. At 33 min, a defined rectangular diffraction  
182 pattern appeared as nanorods began to crystalize, which is the reciprocal lattice of  $\{110\}$  facets  
183 (**Fig. S35**). The high-order diffraction peaks confirm the perfect structures of the *bct* crystals. For  
184 example, the linear profiles in **Fig. 4b** (horizontal) and **4c** (vertical) show a 9<sup>th</sup> diffraction of  $\{110\}$   
185 facets and 5<sup>th</sup> diffraction of  $\{001\}$  facets, respectively. **Fig. 4d** represents a time-dependent  
186 contraction of the lattice under external magnetic fields with exponential superlattice densification.  
187 The lattice contraction rate along both the *a* and *c* directions was initially at  $\sim 4$  nm/min and slowed  
188 down when approaching thermodynamic equilibrium at  $\sim 90$  min. The considerably slow assembly  
189 kinetics provide rods with sufficient spatiotemporal degrees of freedom to anneal out defects. **Fig.**  
190 **4e** shows the evolution of local rod position along  $\langle 111 \rangle$  crystallographic directions, indicating

191 nearly linear spatial lattice contraction (**Fig. S36**). The overall magnetic assembly was compiled  
192 and depicted in **Fig. 4f** with lattice shrinkage of 31.7% and 22.4% for a and c axis, respectively.  
193 The *bct* crystals exhibit brilliant structural colors that are dependent on crystal orientation (**Movie**  
194 **S5**). In the dark-field optical microscopy images in **Fig. 5a**, we observed structural colors diffracted  
195 from two types of facets: red from {110} and green from {100} facets. The uniform structural  
196 colors elucidate the good crystallinity of the superstructures. The incident light was kept vertical  
197 along the crystal surface for measuring the angle-dependent optical properties (**Fig. 5b**). A  
198 horizontal magnetic field (0°) was applied, and spectra were measured by gradually changing the  
199 field to the vertical direction (90°). The three primary colors, blue, green, and red, can be observed  
200 at 0°, 20° and 45°, respectively (**Fig. 5c**). The diffraction spectra in **Fig. 5d** further demonstrated a  
201 gradual redshift of the diffraction peaks because of the increasing periodicity when the crystal  
202 orientation increased to 90°. Their diffraction could cover the whole visible range from blue to cyan,  
203 green, yellow, orange, and finally red by simply changing the magnetic field directions (**Fig. 5e**,  
204 **Movie S6 and S7**). A simple extension to different nanorods yields photonic crystals with tunable  
205 lattice constants and structure colors (**Fig. S37**).

## 206 **Discussion**

207  
208 In summary, we report the magnetic assembly of magnetite nanorods into tetragonal colloidal  
209 crystals and show that the magnetic nanorods assemble along a size-dependent critical angle rather  
210 than the simple end-on attachment. The coupled shape and magnetic anisotropy in nanorods is  
211 responsible for the unconventional assembly manner and leads to the non-close packed and hard  
212 contact phase. The unique 3D tetragonal architectures and tunable, interconnected porosity provide  
213 a unique platform to modulate many chemical transformations and physical processes in energy  
214 conversion and optical devices. This work demonstrates that manipulating magnetic interactions of  
215 various anisotropically shaped nanostructures can break the limitation of the dense packing phase  
216 in the conventional entropy-dominated colloidal assembly systems, thereby opening the door to  
217 creating many complex colloidal crystals.

## 218 **Materials and Methods**

### 219 **Synthesis of FeOOH nanorods.**

220  
221 The synthesis of nanorods with different aspect ratios was achieved by hydrolysis of FeCl<sub>3</sub> in an  
222 aqueous solution (57, 58). The details about the concentration and reaction temperature are  
223 summarized in **Table. S1**. The synthesis of FeOOH nanorods with small aspect ratios was carried  
224 out at room temperature without HCl. Due to relatively low temperature, it takes about 3 months  
225 for the formation of uniform FeOOH nanorods. To synthesize FeOOH nanorods with larger aspect  
226 ratios (**Fig. S2**), we added HCl to the solution and raised the reaction temperature to 87°C. The  
227 reactions were kept at this temperature for 25.5 hours. Notably, this hydrolysis method can be easily  
228 scaled up without a significant change in size and aspect ratios. In the example of rods with aspect  
229 ratios of 4.6 (#F2), the total volume was 4 L during room-temperature hydrolysis. The concentration  
230 of FeCl<sub>3</sub>·6H<sub>2</sub>O is 0.04 M. During the reaction, the formed FeOOH nanorods precipitated to the  
231 bottom of the reaction containers. After removing the supernatants, the FeOOH nanorods were  
232 washed by water three times and then dispersed in 400 mL of water, which served as stock solutions.

### 233 **PAA modification.**

234 For PAA modification, 3 mL of the stock solution with a theoretical concentration of 90 mg/mL  
235 was added into 120 mL of PAA solution (43.2 mg) and stirred for 8 hrs. Excess PAA was removed  
236 by centrifugation and washing with water three times. The FeOOH-PAA was further dispersed in  
237 9 mL of water for SiO<sub>2</sub> coating.

238 **SiO<sub>2</sub> coating.** In a typical coating process, 3 mL of FeOOH-PAA dispersion was added into a flask.  
239 The mixture was sonicated for 3 min to fully disperse the rods after 1 mL of ammonia solution was  
240 added. Then, 20 mL of ethanol was added to the dispersion. To control the thickness of silica, we

241 added different volumes of TEOS to the mixture. In #F2, for example, 30  $\mu\text{L}$  and 100  $\mu\text{L}$  of TEOS  
242 were added to the mixture to achieve thicknesses of 20.5 and 44.2 nm, respectively, after a 30 min  
243 reaction. For thicker silica ( $\sim 72.8$  nm), two batches of 130  $\mu\text{L}$  TEOS were added to the mixture  
244 each 30 min to prevent the formation of free silica nanoparticles. Half an hour after the second  
245 addition, the  $\text{FeOOH}@SiO_2$  nanorods were precipitated by centrifugation and further washed three  
246 times by water.

### 247 **High-temperature reduction.**

248 Magnetic nanorods were synthesized by reduction of  $\text{FeOOH}@SiO_2$  nanorods in high-temperature  
249 calcination.  $\text{FeOOH}@SiO_2$  nanorods were dried in crucibles and placed in a tubular furnace (**Fig.**  
250 **S3**). The system was de-gassed for 10 min by forming gas (5%  $\text{H}_2$  and 95%  $\text{N}_2$ ). The reduction  
251 occurred at 360°C for 2 hours. After cooling down to room temperature, the prepared  $\text{Fe}_3\text{O}_4@SiO_2$   
252 nanorods were fully dispersed in water by sonication and then washed by water three times. To  
253 further increase the surface charges and facilitate the fixation of colloidal crystals by silica coating,  
254 the  $\text{Fe}_3\text{O}_4@SiO_2$  nanorods were modified by PAA (20mL, 5 mg/mL) overnight.

### 255 **Magnetic assembly of nanorods into tetragonal crystals**

256 The assembly of colloidal crystals took place in aqueous dispersions of  $\text{Fe}_3\text{O}_4@SiO_2$  nanorods (**Fig.**  
257 **S4**). The dispersion was vertically placed above the center of a permanent magnet. For measuring  
258 the diffraction of the crystals, colloidal dispersion of  $\text{Fe}_3\text{O}_4@SiO_2$  nanorods with an initial volume  
259 fraction of  $\sim 45\%$  was sealed in a flat capillary. After assembling under the magnetic field,  
260 diffraction spectra were measured by continuously varying the directions of the applied magnetic  
261 field, and the pictures were also taken at the corresponding angles (**Fig. 5C**). To fix the assembled  
262 crystals, we used a small well of the 96 well plates as the container. In a typical reaction, 25  $\mu\text{L}$  of  
263 an aqueous dispersion of  $\text{Fe}_3\text{O}_4@SiO_2$  nanorods (volume fraction of  $\sim 45\%$ ) was transferred into  
264 the well. 3  $\mu\text{L}$  of ammonia, 100  $\mu\text{L}$  of ethanol, and 10  $\mu\text{L}$  of TEOS were added in sequence. The  
265 mixture was sonicated for  $\sim 30\text{s}$  and then placed above a permanent magnet. Additional 3  $\mu\text{L}$  of  
266 ammonia was added after 10 min, and the reaction was continued for another 10 min. The  
267 precipitated crystals were washed with ethanol three times. During each cycle of washing, the  
268 crystals were collected by magnetic separation. Sonication and centrifugation would destroy the  
269 fixed crystal structures and therefore are not recommended. The crystals were stored in ethanol for  
270 further characterization. The positional order of the colloidal crystals decayed because long  
271 nanorods were synthesized in high-temperature hydrolysis, and the relatively fast crystal growth  
272 produces widely dispersed particles. More TEM images of the *bct* crystals are shown in **Fig. S5**.  
273 According to the projection patterns, we typically observed two types of crystal orientations. Fixing  
274 neighboring rods by silica overcoating imparts considerable mechanical stability to the crystals, as  
275 demonstrated by twisting and bending the *bct* crystals under mechanical forces (**Fig. S6**). Instead  
276 of being destroyed, the crystals deformed to release the internal strains, exhibiting interesting,  
277 combined states of colloid rigidity and mechanical elasticity.

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434 Conceptualization: ZWL, YDY

435 Methodology: ZWL, CQ

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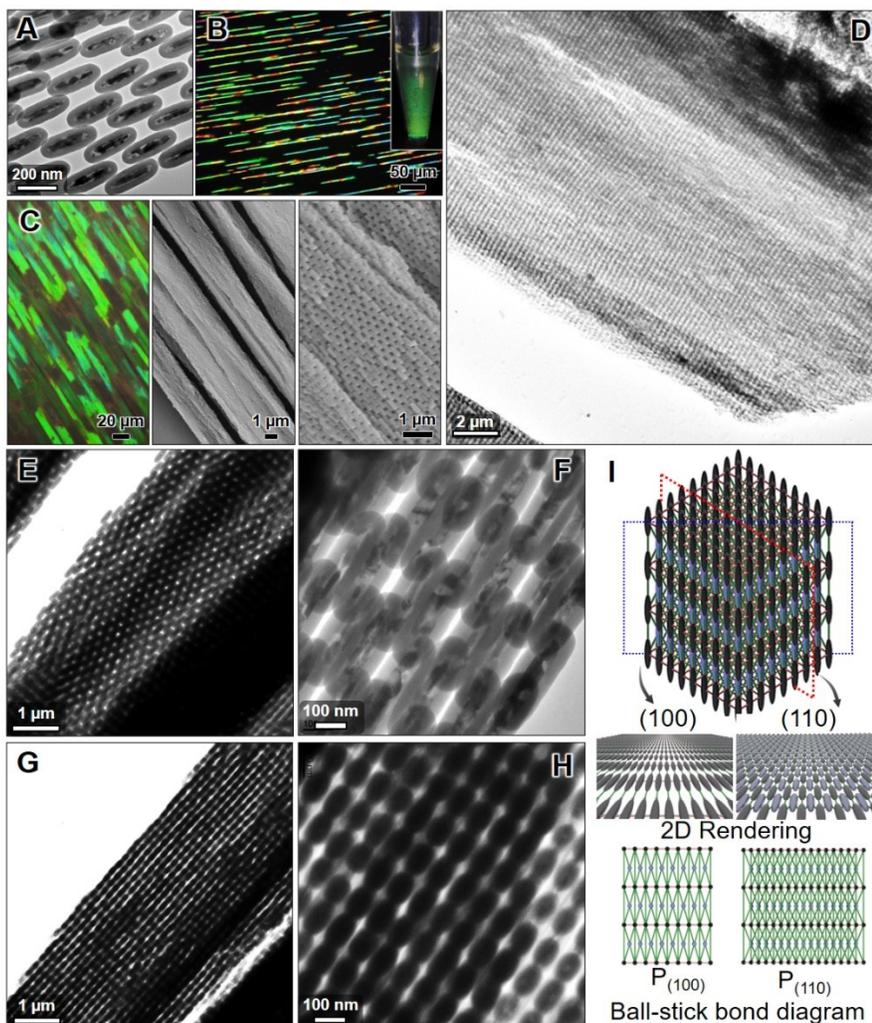
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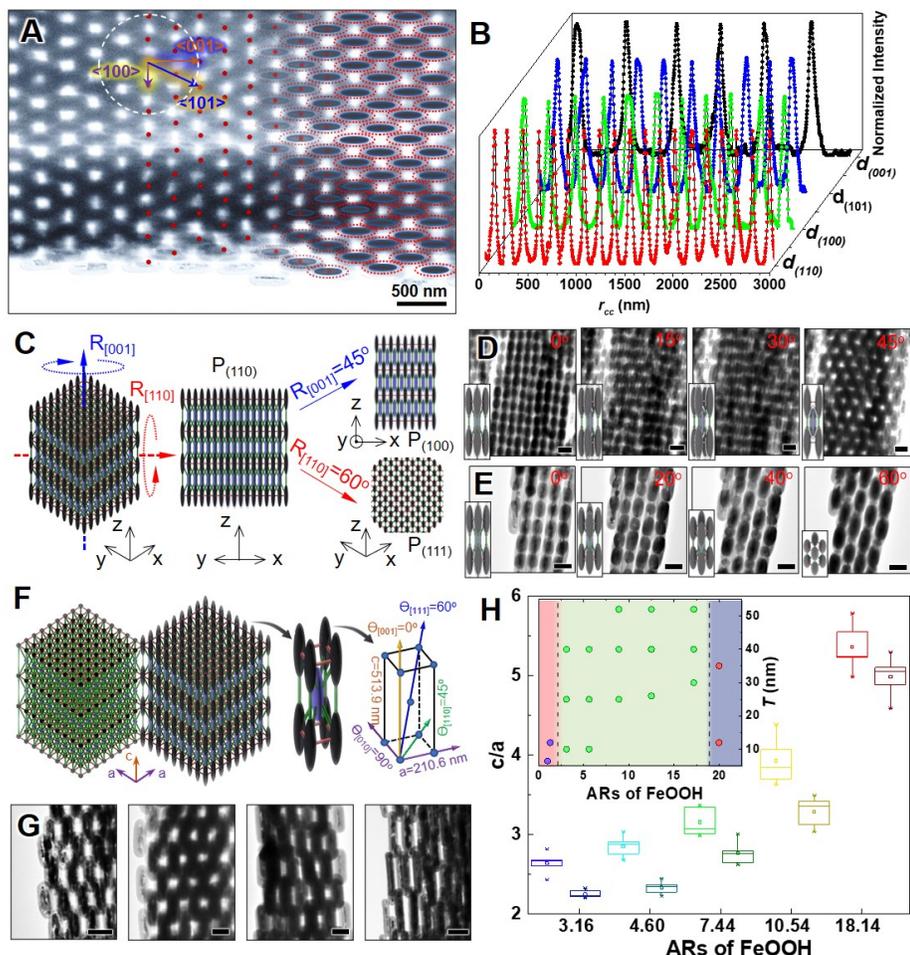
439 Writing—review & editing: YDY

440  
441 **Competing interests:** YDY and ZWL have filed a patent application covering the magnetic  
442 assembly of nanorods into tetragonal photonic crystals. All other authors declare they have  
443 no competing interests.  
444

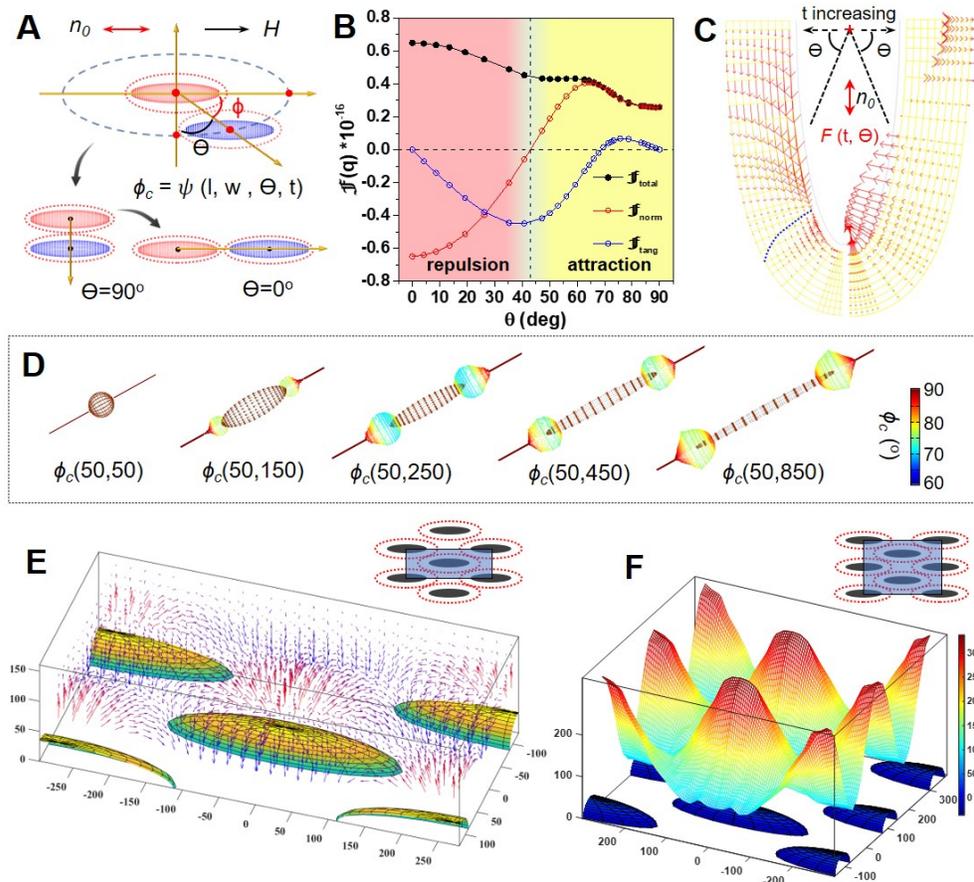
445 **Data and materials availability:** All data needed to evaluate the conclusions in the paper  
446 are present in the paper and/or the Supplementary Materials. Additional dataset used to  
447 analyze the critical angles, phase diagram, electrostatic forces, and magnetic forces are  
448 available online at <https://zenodo.org/record/4950032#.YMqqbvKSk2w>.  
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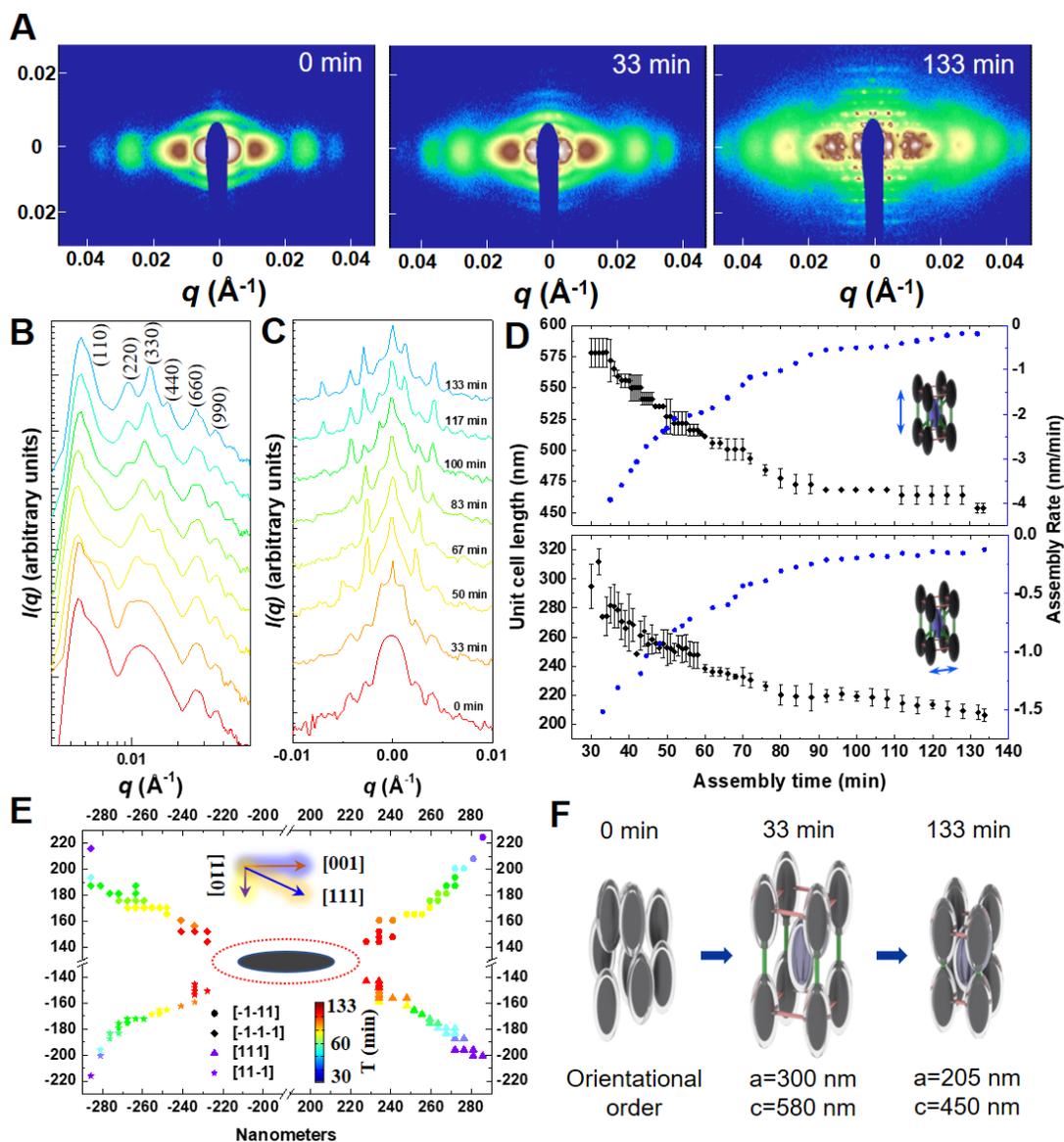
**Fig. 1. Magnetic assembly of nanorods into *bct* colloidal crystals.** (A) TEM image of  $\text{Fe}_3\text{O}_4@ \text{SiO}_2$  nanorods. (B) Dark-field optical microscopy image of the needle-like colloidal crystals under an external magnetic field. Inset shows a digital photo of a rod dispersion in a vertical magnetic field. (C) Left: Optical microscopy image of the colloidal crystals in a colloidal dispersion. Middle to right: low-magnification SEM image showing the fixed needle-like structures and high-magnification SEM image showing the characteristic rod packing on the crystal surfaces. (D) Low-magnification TEM image of assembled hollow  $\text{SiO}_2$  ellipsoids formed by post-assembly etching of  $\text{Fe}_3\text{O}_4$  core. (E-H) TEM images of the assembled crystals under the projections of different crystal facets. (I) The 3D rendering and ball-stick bond diagram of the *bct* colloidal crystal and its facets.



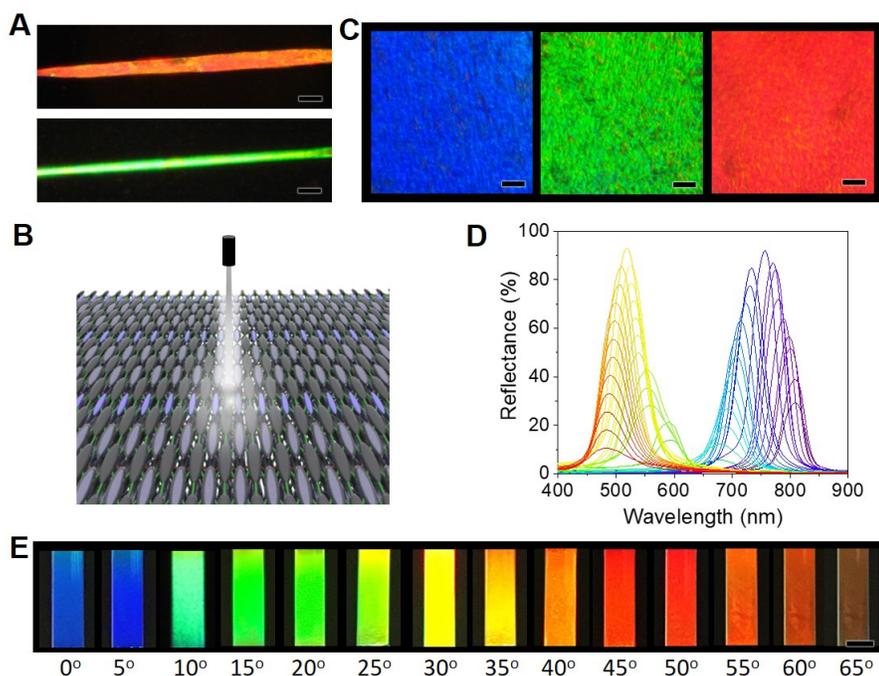
**Fig. 2. Structure characterization of *bct* colloidal crystals.** (A) TEM image of the *bct* crystal showing the projection of (100) facets. Positions of rods are identified and mapped to a *bct* lattice. (B) Normalized distribution intensity of nanorods inside the crystals in (A) along different crystallographic directions. (C) Schematics of *bct* crystals under different orientations by rotating along given crystallographic directions. TEM images in (D) and (E) show *bct* crystals under various orientations by rotating along [001] and [110], respectively. (F) Simulated *bct* colloidal crystals. (G) TEM images of *bct* crystals assembled from magnetic nanorods with different sizes and aspect ratios. (H) The dependence of lattice constant ratio ( $c/a$ ) on the aspect ratio of magnetic nanorods. Inset is the experimental phase diagram showing the magnetic assembly behaviors of rods. Blue, green, and red dots represent linear colloidal chains, *bct* crystals, and disordered fibers with only orientational orders, respectively.



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 481 **Fig. 3. Assembly mechanism and force dynamics.** (A) Schematics showing the geometry  
 482 for calculating the pair interaction between two nanorods under a horizontal magnetic field.  
 483 (B) Plot of total force and its normal, tangent components against  $\Theta$  when  $\text{SiO}_2$  thickness is  
 484 50 nm. (C) Force field of the normal (left half) and tangent (right half) components of the  
 485 pair interactions between two magnetic nanorods ( $t=50$  nm) by varying separation and  
 486 angles ( $\Theta$ ) between  $r_{cc}$  and  $n_0$ . (D) 3D mapping of critical angles ( $\phi_c$ ) for nanorods  
 487 with different aspect ratios. (E) 3D force fields of magnetic interactions experienced by one  
 488 nanorod above the 2D assemblies. (F) Magnetic potential above the 2D assemblies at certain  
 489 separations.  
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491  
 492 **Fig. 4. Assembly kinetics.** (A) Temporal evolution of SAXS patterns during the *in-situ*  
 493 measurement of magnetic assembly of nanorods. (B-C) Representative linear profile of  
 494 SAXS patterns along the horizontal (B) and vertical (C) directions. (D) Magnetic assembly  
 495 kinetics of the *bct* crystals along c-axis (top) and a-axis (bottom). (E) The trajectory of the  
 496 magnetic nanorods during the assembly process. (F) The depiction of the magnetic  
 497 assembly and formation of *bct* crystals.  
 498



**Fig. 5. Optical properties of the assembled *bct* photonic crystals.** (A) Optical microscopy images of a *bct* crystal under different orientations. (B) Schematic illustration of measuring the crystal optical properties. Light was incident along the surface normal, and a horizontal ( $0^\circ$ ) magnetic field was applied. (C) Optical microscopy images of the *bct* crystals under different magnetic field directions: blue at  $0^\circ$ , green at  $20^\circ$ , and red at  $45^\circ$ . (D) Measured reflection spectra of rod dispersion under different magnetic fields. Increasing the field direction from  $0^\circ$  to  $65^\circ$  leads to a gradual redshift of the reflection peaks. (E) Structural colors of rods dispersion under different magnetic fields. Scale bars:  $20\ \mu\text{m}$  in (A) and (C);  $5\ \text{mm}$  in (E).