



The X-Ray Halo Scaling Relations of Supermassive Black Holes

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Abstract

We carry out a comprehensive Bayesian correlation analysis between hot halos and *direct* masses of supermassive black holes (SMBHs), by retrieving the X-ray plasma properties (temperature, luminosity, density, pressure, and masses) over galactic to cluster scales for 85 diverse systems. We find new key scalings, with the tightest relation being $M_{\bullet} - T_x$, followed by $M_{\bullet} - L_x$. The tighter scatter (down to 0.2 dex) and stronger correlation coefficient of all the X-ray halo scalings compared with the optical counterparts (as the $M_{\bullet} - \sigma_e$) suggest that plasma halos play a more central role than stars in tracing and growing SMBHs (especially those that are ultramassive). Moreover, M_{\bullet} correlates better with the gas mass than dark matter mass. We show the important role of the environment, morphology, and relic galaxies/coronae, as well as the main departures from virialization/self-similarity via the optical/X-ray fundamental planes. We test the three major channels for SMBH growth: hot/Bondi-like models have inconsistent anticorrelation with X-ray halos and too low feeding; cosmological simulations find SMBH mergers as subdominant over most of cosmic time and too rare to induce a central-limit-theorem effect; the scalings are consistent with chaotic cold accretion, the rain of matter condensing out of the turbulent X-ray halos that sustains a long-term self-regulated feedback loop. The new correlations are major observational constraints for models of SMBH feeding/feedback in galaxies, groups, and clusters (e.g., to test cosmological hydrodynamical simulations), and enable the study of SMBHs not only through X-rays, but also via the Sunyaev–Zel'dovich effect (Compton parameter), lensing (total masses), and cosmology (gas fractions).

Unified Astronomy Thesaurus concepts: Supermassive black holes (1663); Brightest cluster galaxies (181); Elliptical galaxies (456); Lenticular galaxies (915); Late-type galaxies (907); Intracluster medium (858); Circumgalactic medium (1879); Interstellar medium (847); X-ray astronomy (1810); Optical observation (1169); Hydrodynamical simulations (767)

1. Introduction

Supermassive black holes (SMBHs) are found at the center of most—if not all—galaxies (see, e.g., Kormendy & Ho 2013 for a review). High-resolution observations of stellar and cold gas kinematics in the central regions of nearby galaxies have enabled dynamical measurements of central SMBH masses in over a hundred objects (e.g., Magorrian et al. 1998; Ferrarese & Merritt 2000; Gebhardt et al. 2000; Gultekin et al. 2009; Beifiori et al. 2012; Saglia et al. 2016; van den Bosch 2016). The measured masses of the SMBHs are correlated with the luminosity (L_K) and effective velocity dispersion (σ_e) of the

host galaxy, suggesting a coevolution between the SMBH and the properties of their host environments. These findings further imply an interplay between the feeding/feedback mechanisms of the SMBH and its host galaxy (Silk & Rees 1998). During the active galactic nucleus (AGN) phase, outflows and jets from the central SMBH are thought to play a fundamental role in establishing the multiphase environment in their host halo, quenching cooling flows/star formation, and shaping the galaxy luminosity function (e.g., McNamara & Nulsen 2007, 2012; Fabian 2012; Tombesi et al. 2013, 2015; King & Pounds 2015; Fiore et al. 2017). For these reasons, AGN feedback has become a crucial ingredient in modern galaxy formation models (e.g., Sijacki et al. 2007; Borgani et al. 2008; Booth & Schaye 2009; Gaspari et al. 2011a, 2011b; Yang & Reynolds 2016b; Tremmel et al. 2017).

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While SMBH feedback is central to galaxy evolution, the mechanism through which the observed correlations between black hole (BH) mass M and galaxy (or halo) properties are established is still debated. In the simple, idealized gravitational scenario, BH seeds are thought to grow rapidly at high redshift, with the scaling relations arising from the bottom-up structure formation process in which large structures are formed through the merging of smaller structures under the action of gravity (leading to virialization and self-similarity; e.g., Kravtsov & Borgani 2012). In this scenario, the central SMBHs of the merging systems settle to the bottom of the potential well of the newly formed halo and eventually merge, inducing hierarchical scaling relations between M and galaxy properties (e.g., Peng 2007; Jahnke & Macciò 2011).

However, in recent years, measurements of BH masses in the most massive local galaxies (ultramassive black holes—UMBHs) have challenged the hierarchical formation scenario (e.g., McConnell et al. 2011; Hlavacek-Larrondo et al. 2012, 2015; McConnell & Ma 2013; Thomas et al. 2016). Some studies reported dynamical masses in excess of $10^{10} M_\odot$, i.e., about an order of magnitude greater than expected from the M – σ_e and M – L_K relations. A prominent example of such an outlier is M87 (NGC 4486), for which the BH mass of $6.5 \times 10^9 M_\odot$ lies an order of magnitude above that expected from the M – σ_e relation (Gebhardt et al. 2011). Spectacular observations by the Event Horizon Telescope (EHT) have recently confirmed the extreme mass of this object (Event Horizon Telescope Collaboration et al. 2019a, 2019b). Recent works have suggested that the environment and location of such UMBHs at the bottom of the potential well of galaxy clusters and groups, where the most massive galaxies are formed (known as brightest cluster/group galaxies—BCGs/BGGs), could be responsible for the observed deviations (Gaspari & Sadowski 2017; Bogdán et al. 2018; Bassini et al. 2019).

Beyond the stellar component, an important ingredient for SMBH feeding is the surrounding X-ray emitting plasma halo. At scales beyond the effective galactic radius, the majority of baryons are found in the form of a diffuse ($n_e < 0.1 \text{ cm}^{-3}$) and hot ($T_x > 0.1 \text{ keV}$) plasma, often referred to as the circumgalactic (CGM), intragroup (IGrM), or intracluster medium (ICM)—e.g., Sarazin 1986; Mathews & Brighenti 2003; Kravtsov & Borgani 2012; Sun 2012; Gonzalez et al. 2013; Eckert et al. 2016). In the central regions of relaxed, cool-core (CC) systems, the plasma densities are such that the cooling time of the hot ICM/IGrM becomes much smaller than the Hubble time. Thus, a fraction of the hot gas²³ cools and condenses in the central galaxy, forming extended warm filaments detected in H α and cold molecular clouds that fuel star formation (e.g., Fabian et al. 2002; Peterson & Fabian 2006; Combes et al. 2007; McDonald et al. 2010, 2011, 2018; Gaspari 2015; Tremblay et al. 2015, 2018; Molendi et al. 2016; Temi et al. 2018; Nagai et al. 2019). A portion of the cooling gas ignites the central AGN, which triggers the SMBH response via outflowing material that regulates the cooling flow of the macro-scale gaseous halo (e.g., Birzan et al. 2004; Rafferty et al. 2006; McNamara & Nulsen 2007; Gaspari & Sadowski 2017). Such SMBHs follow an intermittent duty cycle (Birzan et al. 2012), as evidenced by the common presence of radio-emitting AGN, especially in massive galaxies (Burns 1990; Mittal et al. 2009; Bharadwaj et al. 2014; Main et al. 2017).

²³ For consistency with the literature, we refer interchangeably to the diffuse plasma component by using the “gas” nomenclature.

Over the past decade, extensive investigations have been carried out in order to understand the mechanism through which AGN inject energy into the surrounding medium and how the condensed filaments/clouds form out of the hot halos (Gaspari et al. 2009, 2011a, 2011b, 2017; Pizzolato & Soker 2010; McCourt et al. 2012; Sharma et al. 2012; Li & Bryan 2014; Prasad et al. 2015, 2017; Voit et al. 2015a, 2017; Valentini & Brighenti 2015; Soker 2016; Yang et al. 2019). A novel paradigm has emerged in which the AGN feedback cycle operates through chaotic cold accretion (CCA; Gaspari et al. 2013, 2015, 2017), where turbulent eddies induced by AGN outflows (and cosmic flows; Lau et al. 2017) are responsible for the condensation of multiphase gas out of the hot halos via nonlinear thermal instability. The condensed gas then rapidly cools and rains toward the central SMBH. Within $r < 100 \text{ pc}$, the clouds start to collide inelastically and get efficiently funneled inward within a few tens of Schwarzschild radii, where an accretion torus rapidly pushes the gas through the BH horizon via magneto-rotational instability (MRI; e.g., Balbus 2003; Sadowski & Gaspari 2017). A growing body of studies suggests that, in spite of the mild average Eddington ratios,²⁴ the mass accreted through CCA over long timescales can account for a substantial fraction of the SMBH masses (e.g., Gaspari et al. 2013, 2015; Voit et al. 2015b; Tremblay et al. 2016, 2018; Prasad et al. 2017). Alternative models treat BH accretion purely from the single-phase, hot gas perspective, following the seminal work by Bondi (1952) and related variants (e.g., Narayan & Fabian 2011), predicting unintermittent accretion rates inversely tied to the plasma entropy. Further models, such as hierarchical major/minor mergers and high-redshift quasars, are tackled in Section 4, in particular by means of cosmological simulations.

This work is part of the *BlackHoleWeather* program (PI: M. Gaspari), which aims at understanding the link between the central SMBH and its surrounding halo, both from the theoretical and observational points of view. Historically, this paper was initiated five years ago, inspired by the thorough review by Kormendy & Ho (2013). We make use of precise dynamical (direct) SMBH mass measurements collected from the literature (Kormendy & Ho 2013; McConnell & Ma 2013; van den Bosch 2016) over a wide range of systems—including central galaxies and satellites, and early- and late-type galaxies (ETGs, LTGs)—and correlate them with the properties of the surrounding hot X-ray atmosphere (X-ray luminosity, temperature, gas mass, pressure/thermal energy, and entropy). A tight correlation between M – T_x and M – L_x is indeed expected based on first-principle arguments initially proposed by Gaspari & Sadowski (2017). We focus here only on hot X-ray plasma halos and related SMBHs, leaving halos falling below such a band to future work (e.g., UV and related intermediate mass BHs—IMBHs). We further compare the X-ray scalings with the optical counterparts via both univariate and multivariate correlations. We discover new correlations between the various hot gas properties and SMBH mass, which help us to test the main models of macro-scale BH feeding, i.e., hot Bondi-like accretion, CCA, and hierarchical mergers. With the advent of gravitational-wave astronomy (*LISA*), direct SMBH imaging (EHT), and next-generation X-ray instruments with superb angular resolution and sensitivity (*Athena*, *XRISM*, and the

²⁴ The Eddington ratio is defined as follows: $\dot{M}_{\text{Edd}} \equiv L_{\text{Edd}}/(0.1 c^2) \simeq 22.8(M_\odot/10^9 M_\odot) M_\odot \text{ yr}^{-1}$, where $L_{\text{Edd}} = 10^{47}(M_\odot/10^9 M_\odot) \text{ erg s}^{-1}$ is the Eddington luminosity.

proposed *Lynx* and *AXIS*), it is vital to understand how SMBHs form and grow.

This work is structured as follows. In Section 2, we present the retrieved data sample (85 galaxies) from a thorough literature search. In Section 3, we describe the main results in terms of a robust Bayesian statistical analysis of all the X-ray and optical properties (via univariate and multivariate correlations; see Table 1). In Section 4, we probe the main models of BH feeding and discuss key astrophysical insights arising from the presented correlations. In Section 5, we summarize the major results of the study and provide concluding remarks. As used in most literature studies, throughout the work we adopt a flat concordance cosmology with $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$ ($h = 0.7$) and $(\Omega_m, \Omega_\Lambda) = (0.3, 0.7)$. The Hubble time is $t_H \equiv 1/H_0 \simeq 13.9 \text{ Gyr}$, which well approximates the age of the universe.

2. Data Analysis

2.1. Data Sample and Fundamental Properties

The main objective of this study is to measure the observed correlations between direct SMBH masses and both the stellar and plasma halo properties. To achieve this goal, we performed a thorough search of the past two decades of the related observational literature, aimed at assembling the fundamental observables in both the optical and X-ray band for a large sample of (85) galaxies. The selection is straightforward: we inspected any SMBH with a direct/dynamical BH mass measurement (van den Bosch 2016) and looked for an available X-ray detection, in terms of galactic, group, and cluster emission from diffuse hot plasma. We tested combinations of these data sets, with comparable results. The potential role of selection effects is discussed in Section 4.4. The retrieved, homogenized fundamental variables are listed in Appendix B, including the detailed references and notes for each galaxy in the sample. In the next two subsections, we describe their main optical and X-ray features.

2.1.1. Optical Stellar Observables and BH Masses

Table 2 lists all the optical properties and BH masses of the galaxies in our sample. The vast majority of the BH masses come from van den Bosch (2016), who compiled high-quality, dynamical measurements, mostly from Gultekin et al. (2009), Sani et al. (2011), Beifiori et al. (2012), McConnell & Ma (2013), Kormendy & Ho (2013), Rusli et al. (2013), and Saglia et al. (2016). Direct methods imply resolving the stellar or (ionized)

gas kinematics shaped by the BH influence region $G M_*/\sigma_v^2 \sim 1\text{--}100 \text{ pc}$ (for a few galaxies, water masers or reverberation mapping are other feasible methods; see Kormendy & Ho 2013 for a technical review). Such scales require observations with arcsecond or subarcsecond resolution (the majority of which have been enabled by *HST*), thus limiting direct BH detections to the local universe (distance $D < 150 \text{ Mpc}$ or redshift $z < 0.04$).²⁵ One case (M87) includes the first direct imaging of the SMBH horizon available via EHT (Event Horizon Telescope Collaboration et al. 2019a). In this study we focus on X-ray halos and related SMBHs, leaving BHs associated with gaseous halos emitting below the X-ray band to future

²⁵ The evolution factor is negligible, given the low-redshift sample: $E(z) = \sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda} < 1.02$.

investigations (i.e., IMBHs with $M_* \lesssim 3 \times 10^7 M_\odot$). Further, we do not include SMBH masses with major upper limits (e.g., NGC 4382, UGC 9799, and NGC 3945) or which are substantially uncertain in the literature (e.g., Cygnus A, NGC 1275). The direct BHs with reliable X-ray data are listed, in ascending order, in column (vi) of Table 2, for a total robust sample of 85 BHs, spanning a wide range of masses $M_* \sim 4 \times 10^7\text{--}2 \times 10^{10} M_\odot$. We remark that it is crucial to adopt *direct* BH mass measurements, instead of converting a posteriori from the M_* - σ_e and M_* - L_K relations, or from the AGN fundamental plane (Merloni et al. 2003), which can lead to biased, nonindependent correlations with unreliable conversion uncertainty $\gtrsim 1 \text{ dex}$ (Fujita & Reiprich 2004; Mittal et al. 2009; Main et al. 2017; Phipps et al. 2019).

Unless noted in Table 2, the stellar velocity dispersion, effective radius, and total luminosity are from the collection by van den Bosch (2016), who further expanded the optical investigations by Cappellari et al. (2013), Kormendy & Ho (2013), McConnell & Ma (2013), and Saglia et al. (2016). All the collected properties are rescaled as per our adopted distances D (column (v) in Table 2; e.g., $M_* \propto D$ and $L_K \propto D^2$). The measurement of the (effective) stellar velocity dispersion σ_e is typically carried out via long-slit or integral-field-unit (IFU) spectroscopy, by measuring the optical emission-line broadening of the spectrum integrated within the effective half-light radius R_e (or by the luminosity-weighted $—\text{LW}$ —average of its radial profile; McConnell & Ma 2013). Note that σ_e is a one-dimensional (1D), line-of-sight velocity dispersion. An excellent proxy for the total (bulge plus eventual disk) stellar luminosity is the near-infrared (NIR) luminosity in the K_s band (rest-frame $2.0\text{--}2.3 \mu\text{m}$),²⁶ given its very low sensitivity to dust extinction (and star formation efficiencies). van den Bosch (2016) carried out a detailed photometric growth-curve analysis based on a nonparametric determination of the galaxy L_K and half-light radii. This Monte-Carlo method fits each galaxy several hundred times with Sérsic profiles in which the outermost index is incrementally varied ($0.5 < n < 4$) until convergence is reached, thus leading to the listed total luminosity and effective radius R_e (column (viii) and (x) in Table 2; the latter related to the major axis of the isophote containing 50% of the emitted NIR light). In our final sample, the range of stellar luminosities spans $L_K \sim 10^{10}\text{--}10^{12} L_\odot$, with effective radii between 1 and 100 kpc. Total luminosities can be further converted to stellar masses by using the mean stellar mass-to-light ratio (Kormendy & Ho 2013):

$$\log M_*/L_K = 0.29 \log(\sigma_e/\text{km s}^{-1}) - 0.64 \pm 0.09. \quad (1)$$

About one-third of our galaxies have a significant disk component, which is reflected in a bulge-to-total luminosity ratio $B/T < 1$ (column (xi) in Table 2, from the photometric decomposition, mostly by Beifiori et al. 2012; Kormendy & Ho 2013; Saglia et al. 2016). The collected B/T , together with the above mass-to-light ratio, also allows us to compute the bulge mass M_{bulge} , in case they are not directly available (e.g., Beifiori et al. 2012).

Besides the commonly adopted galaxy name (usually from NGC), Table 2 lists the PGC identification number (HyperLEDA), which is useful to track the position of the galaxy

²⁶ We drop the “s” (short) subscript throughout the manuscript, using only the K band nomenclature.

within the group/cluster halo (Section 2.1.2) and to identify the number of members N_m in the large-scale, gravitationally bound cosmic structure. As shown in column (iv), N_m covers values of 1–2 (isolated galaxies), 2–8 (fields), 8–50 (groups), and 50–1000 (clusters of galaxies). Because our search is carried out blindly in terms of the optical galactic properties, we have inherited a diverse mix of Hubble morphological types (Beifiori et al. 2012; Kormendy & Ho 2013; Saglia et al. 2016), spanning from strong ETGs (E0–E4, including massive cD galaxies), to intermediate lenticulars S0s, and non-barred/barred spiral LTGs (see column (iii) in Table 2). Moreover, it is evident by visual inspection that late types/early types correlate with both low/high B/T and N_m values (poor/rich environments), as well as low/high BH masses. In all the subsequent correlation plots, LTGs, S0s, and ETGs are marked with cyan, green, and blue circles, respectively. However, unlike a few previous works, we do not attempt to divide a posteriori LTGs and ETGs in the Bayesian analysis in order to seek a smaller scatter, as we want to retain a sample that is as unbiased as possible.

2.1.2. X-Ray Plasma Observables

Table 3 lists all the fundamental X-ray and environmental properties of the 85 galaxies, groups, and clusters in our sample, as well as related references and single-object notes. As introduced in Section 2.1.1, we carefully inspected the literature, choosing representative works with the deeper high-resolution *Chandra* and wide-field *ROSAT/XMM-Newton* data sets of hot halos (e.g., for the galactic scale, O’Sullivan et al. 2003; Diehl & Statler 2008; Nagino & Matsushita 2009; Kim & Fabbiano 2015; Su et al. 2015; Goulding et al. 2016, to name a few).

The first fundamental plasma observable is the X-ray luminosity, which is constrained from the X-ray photon flux (through either the count rate estimated in CCD images or the normalization of the energy spectra), $L_x = f_x 4\pi D^2$. Wherever necessary, given the cosmological distance dependence, luminosities (and radii) are rescaled via our adopted D (or alternatively via our $h = 0.7$).²⁷ Several of the above studies constrain L_x within the (*Chandra*) X-ray broad band with a rest-frame energy range 0.3–7 keV, i.e., above the UV regime and including both soft and hard X-rays), making it our reference band, too. For data points in a different X-ray energy range (e.g., in the soft²⁸ 0.5–2 keV band or pseudo-bolometric 0.05–50 keV) we apply the appropriate correction by using PIMMS²⁹ tools. These corrections range between 5%–30%. Further, the considered studies aim to remove the contaminations due to foreground/background AGN, low-mass X-ray binaries (LMXBs) and fainter sources, such as active binaries/cataclysmic variables (ABs/CVs; see Goulding et al. 2016), as well as correcting for Galactic neutral hydrogen absorption ($\log N_{\text{H}}/\text{cm}^{-2} \sim 20\text{--}21$). As for the optical morphological types, our final sample contains both gas-poor and gas-rich galaxies and groups/clusters (though only a handful of very massive clusters), spanning a wide range of (unabsorbed) luminosities $L_x \sim 10^{38}\text{--}10^{45} \text{ erg s}^{-1}$.

²⁷ Luminosities scale as $\propto h^{-2}$ and radii as $\propto h^{-1}$.

²⁸ It is interesting to note that, by using the soft X-ray band, one can better separate the diffuse gas component from that associated with contaminating AGN/shocks (which dominate in hard X-rays; e.g., LaMassa et al. 2012).

²⁹ <http://cxc.harvard.edu/toolkit/pimms.jsp>

The second key observable of hot halos is the X-ray temperature, inferred from the detected energy spectrum (e.g., via ACIS-S or RGS instruments). Modern spectral codes with atomic lines libraries (including photoionization and recombination rates) are employed to achieve an accurate fitting, the majority using XSPEC with 1-T (or seldom 2-T) APEC models. A typical—though not unique—procedure among the collected studies of ETGs is as follows (e.g., Kim & Fabbiano 2015). After removal of the X-ray point sources (including the central AGN, e.g., via CIAO wavedetect), the spectra are fitted with a multicomponent model, including a thermal plasma APEC (diffuse plasma), hard X-ray power laws (residual AGN and AB/CV), and thermal 7 keV Bremsstrahlung radiation (unresolved LMXBs). The assumed metal abundances (ranging between $0.3\text{--}1 Z_{\odot}$) are usually a source of significant uncertainty. The temperature (and emission measure) retrieved in varying annuli are then deprojected into a three-dimensional (3D) profile (e.g., via XSPEC project). We remark that our focus is on the X-ray component related to the diffuse thermal gas. As tested by Goulding et al. (2016), using alternative plasma models (e.g., MEKAL or variations in AtomDB) leads to T_x variations up to 10%; hence, on top of statistical errors, we conservatively add (in quadrature³⁰) a 10% systematic uncertainty to allow for a more homogeneous comparison. For an analogous reason, we add a systematic error on L_x by propagating the distance errors (10%–20%). We note that whenever archival errors are given in linear space, we transform and symmetrize them in logarithmic space. The final range of hot halo temperatures for our sample covers the entire X-ray regime, spanning $T_x \sim 0.2\text{--}8 \text{ keV}$.

The diffuse hot plasma can fill different regions of the potential well, including the galactic scale, the core and outskirt regions of the macro group/cluster halo. We thus use three main extraction regions as proxies for three characteristic X-ray radii within the potential well. The radius $R_{x,g}$ is that describing the galactic/CGM potential. We thus searched for studies with L_x and T_x covering the region within $\approx 2 R_e$ ($\sim 0.03 R_{500}$; columns (iii–v) in Table 3), as X-ray halos are typically more diffuse than the stellar component. Beyond such radius, the background noise becomes significant for several of the isolated galaxies, and thus this radius defines a characteristic size within which most of the galactic X-ray halo is contained. Using the CGM region also helps to avoid inner, residual AGN contaminations. The second and third scales are related to $R_{x,c} \approx 0.15 R_{500}$ and $1 R_{500}$,³¹ i.e., the core and outskirt radius of the group/cluster halo, respectively (columns (viii) and (x) in Table 3). The latter is also a good proxy for the virial radius, $R_{500} \simeq R_{\text{vir}}/1.7$, and is directly given by the X-ray temperature, $R_{500} \simeq 860 \text{ kpc} (T_{x,500}/3 \text{ keV})^{1/2}$ (0.03 dex scatter; Sun et al. 2009).³² To recap, our final collected archival sample has

³⁰ We checked that adding such errors in a linear way has a negligible impact on the correlation results, since systematic errors are $\sim 2 \times$ larger than statistical errors. Further, given that all these errors are relatively small (in log space), using the sole statistical error induces only minor variations in the fit, with posterior parameters remaining comparable within the 1σ fitting uncertainty.

³¹ R_{500} is the radius that confines an average (total) matter density $500 \times$ the critical cosmic density ρ_c , such that $M_{\text{tot},500} = (4/3)\pi 500\rho_c R_{500}^3$, where $\rho_c = 3H^2/(8\pi G)$.

³² Errors on $R_{x,g}$ and $R_{x,c}$ are given by the systematic error on distance plus a random error with 0.2 dex rms; error on R_{500} is propagated from the Sun et al. (2009) scaling. We note that non-BCGs/BGGs without a macro halo have core radius = $0.15 R_{500}$.

the following three mean (with rms) extraction radii:

$$\begin{aligned}\log R_{x,g} &= (0.22 \pm 0.33) + \log R_e = (-1.59 \pm 0.30) + \log R_{500} \\ &= (1.00 \pm 0.35) + \log \text{kpc},\end{aligned}\quad (2)$$

$$\begin{aligned}\log R_{x,c} &= (1.00 \pm 0.28) + \log R_e \\ &= (-0.82 \pm 0.13) + \log R_{500} \\ &= (1.70 \pm 0.23) + \log \text{kpc},\end{aligned}\quad (3)$$

$$\log R_{500} = (2.55 \pm 0.16) + \log \text{kpc}. \quad (4)$$

The three extraction radii cover a healthy geometric progression of one-order-of-magnitude increments in spatial scale, $\sim 10^{-2} - 10^{-1} - 10^0 R_{500}$. Note that in a literature search we cannot control a sharp threshold, but only select approximate regions (Table 3). However, a sharp line in the sand is unphysical, since hot atmospheres are continuous in space. Having a dispersion on extraction radii also corroborates the robustness of any retrieved low intrinsic scatter.

To assess whether the galaxy is central, satellite, or isolated, we use the Tully (2015) PGC1 catalog (and correlated N_m in Table 2; in uncertain cases, we also inspected the X-ray halo peak). Whenever the considered system matches the brightest (PGC1) central galaxy of the cluster or group, we list it as BCG or BGG in column (ii) of Table 3; we then search in the cluster/group literature for X-ray data of the core luminosity/temperature ($L_{x,c}/T_{x,c}$; columns (vi–vii)) and global $L_{x,500}$ (column (ix); e.g., Reiprich & Böhringer 2002; Osmond & Ponman 2004; Hudson et al. 2010; Panagoulia et al. 2014; O’Sullivan et al. 2017; Babyk et al. 2018). Given the declining emissivity profile toward the outskirts, $T_{x,c}$ is comparable to $T_{x,500}$ within typical uncertainty (Vikhlinin et al. 2009). In the opposite regime, galaxies that are satellites (moving at hundreds km s^{-1} relative to the macro weather), isolated ($N \leq 2$) or brightest in a poor field (BFGs; both having rapidly dropping gas density beyond $2 R_e$) can only feed from the local hot halo, hence we use as “macro” X-ray properties (e.g., $L_{x,500}$) the CGM observables (this also avoids uncertain extrapolations).

We note that the large majority of the listed T_x/L_x are retrieved via single-aperture X-ray spectroscopy/photometry. Whenever such values are not tabulated by the authors, we integrate the given luminosity/density profile (Equation (9)) or compute the LW temperature from its deprojected profile within our median $R_{x,g}$ or $R_{x,c}$ (avoiding extrapolations beyond constrained data points). The 14 systems retrieved with this method are listed in the notes of Table 3 (e.g., Nagino & Matsushita 2009).

Finally, as for the optical properties, we do not include galaxies with unconstrained or unavailable X-ray data on extended hot halos (e.g., NGC 4751, NGC 7457, and NGC 4486A). Given the significant pile-up effects, we exclude objects that are heavily contaminated or show purely an X-ray AGN point source (often hosting nuclear fast outflows/winds), such as several of the available Markarian galaxies (e.g., Tombesi et al. 2013). We also exclude a few systems with X-ray emission completely swamped by the large-scale FR II-jet lobes or bubbles (Cygnus A, 3C66B/UGC 1841, and NGC 193), thus preventing a reliable determination of the diffuse hot halo. Nevertheless, as discussed in Section 4.4, we decided to include the vast majority of X-ray systems with robust hot halo constraints, regardless of the dynamical or

evolutionary stage, thus considering quiescent, fossil, feedback- and merger-heated systems, as well as major outliers (e.g., NGC 1600).

2.2. Data Fitting: Bayesian Estimator

One of the major advancements in statistical astronomy of the last decade has been the leverage of Bayesian inference methods, which substantially depart from classical methods (such as the simple least-squares estimator). As we are here concerned purely with linear fitting (in \log_{10} space³³), we adopt the widely tested and robust formalism proposed by Kelly (2007), which is coded into the (IDL³⁴ or Python³⁵) procedures `linmix` and `mlinmix`—for univariate and multivariate fitting, respectively. A key reason to use the Bayesian formalism for linear regression is that the intrinsic scatter (ϵ) is treated as a free parameter, together with the normalization/intercept (α) and slope (β). At the same time, `linmix`/`mlinmix` accounts for measurement errors in both the dependent and independent variable/s. Compared with previous statistical methods, such as the BCES estimator (Bivariate Correlated Errors and intrinsic Scatter; Akritas & Bershady 1996), `linmix` is more robust and unbiased even for small samples and large uncertainties (e.g., Sereno 2016).

Formally, the Bayesian `linmix` method has the objective to find the regression coefficients of the form (for univariate fitting)

$$Y = \alpha + \beta X + \epsilon, \quad (5)$$

with the measured values $x = X \pm \sigma_x$ and $y = Y \pm \sigma_y$; while for our multivariate model

$$Y = \alpha + \beta_1 X_1 + \beta_2 X_2 + \epsilon, \quad (6)$$

with the measured values $x_1 = X_1 \pm \sigma_{x_1}$, $x_2 = X_2 \pm \sigma_{x_2}$, and $y = Y \pm \sigma_y$. The covariance terms in measurement errors are typically negligible (e.g., Saglia et al. 2016). In this work, all the carried-out regressions are linear in logarithmic space (e.g., $y = \log M_* \pm \sigma_{\log M_*}$ and $x = \log T_x \pm \sigma_{\log T_x}$).

Procedurally, the `linmix` algorithm first approximates the independent variable distribution as a mixture of Gaussian distribution functions (three³⁶ is typically sufficient). The posterior probability distributions are then efficiently constrained through a Markov Chain Monte Carlo (MCMC) method known as Gibbs sampler.³⁷ We quote as best-fit parameters (in the top-left inset of each correlation plot; see Figure 1) the averages of these distributions with 1σ errors given by the related standard deviation. For the univariate fitting we use

$$\begin{aligned}\alpha &= \bar{\alpha} \pm \sigma_\alpha \text{ [intercept]}, \\ \beta &= \bar{\beta} \pm \sigma_\beta \text{ [slope on } X], \\ \epsilon &= \bar{\epsilon} \pm \sigma_\epsilon \text{ [intrinsic scatter]}, \\ \text{corr} &= \bar{\text{corr}} \pm \sigma_\text{corr} \text{ [correlation coefficient]},\end{aligned}\quad (7)$$

³³ Throughout the manuscript, we drop the “10” subscript and use the formalism $\log_{10} \equiv \log$.

³⁴ IDL `linmix`: https://idlastro.gsfc.nasa.gov/ftp/pro/math/linmix_err.pro; IDL `mlinmix`: https://idlastro.gsfc.nasa.gov/ftp/pro/math/mlinmix_err.pro.

³⁵ Python `linmix`: <https://github.com/jmeyers314/linmix>.

³⁶ We tested a larger number of initial Gaussians, finding no significant differences in the correlation results.

³⁷ A minimum/maximum number of MCMC iterations set as 5000/100000 (with four chains) is sufficient in most cases to reach convergence.

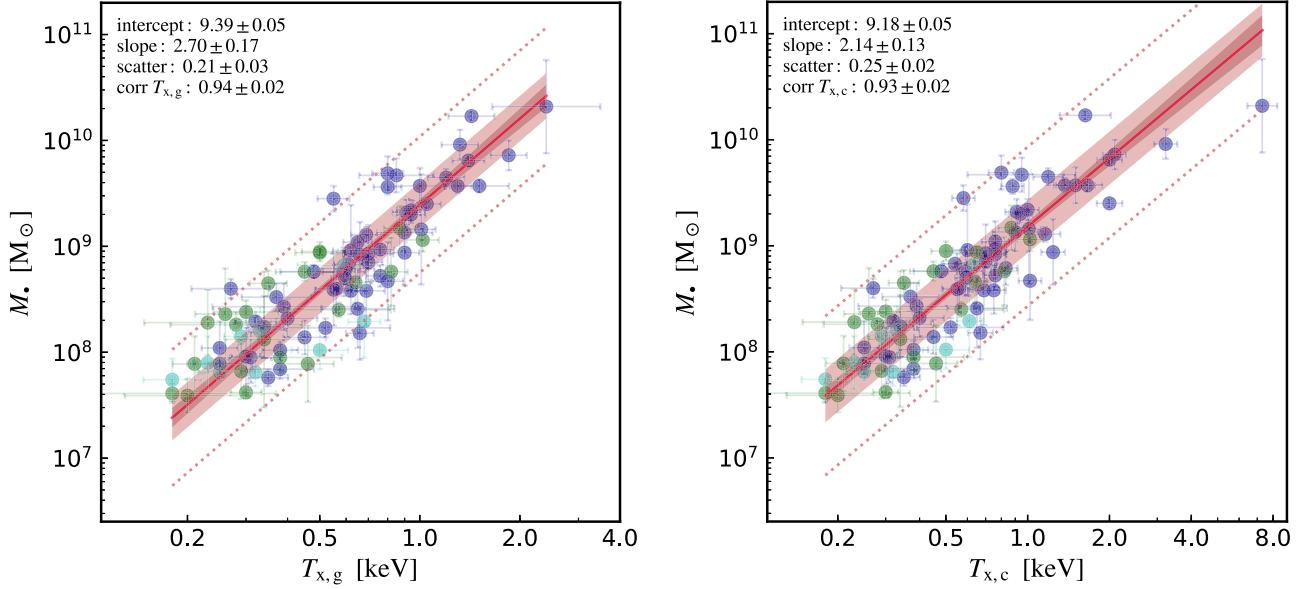


Figure 1. Black hole mass vs. X-ray temperature (Section 3.1.1) within the galactic/CGM scale (left; $R_{x,g} \approx 2 R_e \sim 0.03 R_{500}$; Equation (2)) and the group/cluster core (right; $R_{x,c} \approx 0.15 R_{500} \sim 10 R_e$; Equation (3)). We note that $T_{x,c} \approx T_{x,500}$. The inset shows the mean and errors of all the posteriors from the Bayesian linear fitting (Section 2.2), including the intercept, slope, intrinsic scatter (1σ interval plotted as a light red band, 3σ as dotted lines), and linear correlation coefficient. The solid red line and inner dark band are the mean fit and related 15.87–84.13 percentile interval. The points are color-coded based on the morphological type (blue: E; green: S0; cyan: S), which is also correlated with B/T and N_m . The key result is the very tight linear correlation retrieved ($M_* \propto T^{2.5}$), with the lowest scatter found among all analyzed properties, in particular compared with the optical counterpart, the $M_* - \sigma_e$ relation (Section 3.1.2).

while for the multivariate fitting we use

$$\begin{aligned} \alpha &= \bar{\alpha} \pm \sigma_\alpha \text{ [intercept]}, \\ \beta_{1,2} &= \bar{\beta}_{1,2} \pm \sigma_{\beta_{1,2}} \text{ [slope on } X_1 \text{ and } X_2\text]}, \\ \epsilon &= \bar{\epsilon} \pm \sigma_\epsilon \text{ [intrinsic scatter]}, \\ \text{pcorr}_{1,2} &= \bar{\text{pcorr}}_{1,2} \pm \sigma_{\text{pcorr}_{1,2}} \text{ [partial correlation coeff.],} \end{aligned} \quad (8)$$

where it is important to note that in the multidimensional fitting the meaningful correlation coefficient is the partial (conditional) pcorr, i.e., we want to understand the correlation between Y and one of the independent variables given the second control variable.

Unlike the classic Pearson correlation analysis, the Bayesian inference gives us precise errors (and distributions) on the correlation coefficient, bounded between $[-1, +1]$, which we can use to compare in a clear way the significance of multiple correlations. We quantify the strength of a positive correlation as follows: “very strong” ($\text{corr} > 0.85$), “strong” ($0.7 < \text{corr} < 0.85$), “mild” ($0.5 < \text{corr} < 0.7$), “weak” ($0.3 < \text{corr} < 0.5$), and “absent” ($0.0 < \text{corr} < 0.3$). Anticorrelations have simply the sign (negative) reversed. We remark the importance of providing uncertainties for all the parameters. In Section 3, we will dissect three kinds of major correlations, the univariate fitting between two fundamental X-ray/optical variables (Equation (5)), the univariate fitting between composite variables (again via Equation (5), which has minimal number of free parameters), and the multivariate fitting between the fundamental X-ray/optical observables (Equation (6)).

3. Results

We start the presentation of the results with the correlations of the fundamental X-ray/optical variables (Section 3.1), namely temperature/velocity dispersion and luminosities/masses. We then continue with the univariate correlations of

the derived variables (such as gas density and pressure) and conclude the analysis with the higher-dimensional correlations (Section 3.3). A synoptic table with all the analyzed correlations is given in Table 1, which may be directly used in other studies. The reader can also find in the top-left inset of each correlation plot all the posterior regression coefficients (Equations (5)–(6)). Needless to say, correlation does not necessarily imply causation. On the other hand, the combination of a tight intrinsic scatter, large correlation coefficient, and nonzero slope, all with small statistical errors, accumulate evidence that some properties are more central than others in shaping the growth of SMBHs (and vice versa).

3.1. Univariate Correlations: Fundamental Variables

3.1.1. X-Ray Temperature and Luminosity

One of the most fundamental X-ray properties is the plasma temperature (Section 2.1.2), which is also a measure of the gravitational potential $\phi(r)$. As the gas collapses in the potential wells of the dark matter (DM) halos during the formation of the galaxy, group, or cluster, the baryons thermalize (converting kinetic energy into thermal energy mainly via shock heating; Kravtsov & Borgani 2012) and reach approximate virial equilibrium, $k_b T_x \propto \phi$ (Section 3.3.2).³⁸ Unlike the X-ray luminosity depending on gas mass and thus experiencing evacuation (e.g., via feedback processes), the plasma T_x remains fairly stable in space and time (e.g., Gaspari et al. 2014). Typically, T_x is constant within the galactic region and shows at best a factor of two variations up to the outer regions (Vikhlinin et al. 2006; Diehl & Statler 2008), mostly due to radiative cooling. Given that most of the photons come from the core region, the core temperature is a reasonable proxy for

³⁸ As is customary, we use interchangeably the temperature in K and keV units ($1 \text{ keV} \simeq 1.16 \times 10^7 \text{ K}$), even though the latter technically has the dimensionality of energy.

Table 1
 Summary of the Main Analyzed Correlations between Direct SMBH Masses, X-Ray and Optical Properties for Our Sample of 85 Galaxies, Groups, and Clusters (Tables 2 and 3)

Bayesian univariate fitting $Y = (\bar{\alpha} \pm \sigma_{\alpha}) + (\bar{\beta} \pm \sigma_{\beta})X$	$\bar{\epsilon} \pm \sigma_{\epsilon}$	$\bar{\text{corr}} \pm \sigma_{\text{c}}$
X-ray/plasma correlations:		
$\log(M_{\star}/M_{\odot}) = (9.39 \pm 0.05) + (2.70 \pm 0.17) \log(T_{\text{x,g}}/\text{keV})$	0.21 ± 0.03	0.94 ± 0.02
$\log(M_{\star}/M_{\odot}) = (9.18 \pm 0.05) + (2.14 \pm 0.13) \log(T_{\text{x,c}}/\text{keV})$	0.25 ± 0.02	0.93 ± 0.02
$\log(M_{\star}/M_{\odot}) = (10.63 \pm 0.15) + (0.51 \pm 0.04) \log(L_{\text{x,g}}/10^{44} \text{ erg s}^{-1})$	0.30 ± 0.02	0.87 ± 0.02
$\log(M_{\star}/M_{\odot}) = (10.18 \pm 0.11) + (0.42 \pm 0.03) \log(L_{\text{x,c}}/10^{44} \text{ erg s}^{-1})$	0.29 ± 0.02	0.88 ± 0.03
$\log(M_{\star}/M_{\odot}) = (10.00 \pm 0.11) + (0.38 \pm 0.03) \log(L_{\text{x,500}}/10^{44} \text{ erg s}^{-1})$	0.31 ± 0.02	0.86 ± 0.03
$\log(M_{\star}/M_{\odot}) = (10.60 \pm 0.42) + (0.78 \pm 0.17) \log(n_{\text{e,g}}/\text{cm}^{-3})$	0.56 ± 0.04	0.54 ± 0.10
$\log(M_{\star}/M_{\odot}) = (12.75 \pm 0.41) + (1.13 \pm 0.11) \log(n_{\text{e,c}}/\text{cm}^{-3})$	0.39 ± 0.03	0.80 ± 0.05
$\log(M_{\star}/M_{\odot}) = (13.53 \pm 0.49) + (1.02 \pm 0.10) \log(n_{\text{e,500}}/\text{cm}^{-3})$	0.40 ± 0.03	0.79 ± 0.05
$\log(M_{\star}/M_{\odot}) = (8.29 \pm 0.07) + (0.75 \pm 0.09) \log(P_{\text{x,g}}/10^{-3} \text{ keV cm}^{-3})$	0.45 ± 0.03	0.73 ± 0.06
$\log(M_{\star}/M_{\odot}) = (9.15 \pm 0.05) + (0.80 \pm 0.06) \log(P_{\text{x,c}}/10^{-3} \text{ keV cm}^{-3})$	0.33 ± 0.02	0.87 ± 0.03
$\log(M_{\star}/M_{\odot}) = (9.96 \pm 0.10) + (0.75 \pm 0.05) \log(P_{\text{x,500}}/10^{-3} \text{ keV cm}^{-3})$	0.33 ± 0.02	0.87 ± 0.03
$\log(M_{\star}/M_{\odot}) = (3.88 \pm 0.42) + (0.57 \pm 0.05) \log(M_{\text{gas,g}}/M_{\odot})$	0.32 ± 0.03	0.87 ± 0.04
$\log(M_{\star}/M_{\odot}) = (2.46 \pm 0.46) + (0.64 \pm 0.05) \log(M_{\text{gas,c}}/M_{\odot})$	0.26 ± 0.03	0.92 ± 0.03
$\log(M_{\star}/M_{\odot}) = (1.61 \pm 0.49) + (0.64 \pm 0.04) \log(M_{\text{gas,500}}/M_{\odot})$	0.30 ± 0.02	0.90 ± 0.03
$\log(M_{\star}/M_{\odot}) = (10.16 \pm 0.11) + (0.46 \pm 0.03) \log(Y_{\text{x,g}}/10^{60} \text{ erg})$	0.32 ± 0.02	0.88 ± 0.03
$\log(M_{\star}/M_{\odot}) = (9.54 \pm 0.07) + (0.45 \pm 0.03) \log(Y_{\text{x,c}}/10^{60} \text{ erg})$	0.30 ± 0.02	0.89 ± 0.03
$\log(M_{\star}/M_{\odot}) = (8.98 \pm 0.04) + (0.49 \pm 0.03) \log(Y_{\text{x,500}}/10^{60} \text{ erg})$	0.29 ± 0.02	0.90 ± 0.03
$\log(M_{\star}/M_{\odot}) = (-6.03 \pm 1.45) + (1.28 \pm 0.13) \log(M_{\text{tot,g}}/M_{\odot})$	0.36 ± 0.03	0.83 ± 0.05
$\log(M_{\star}/M_{\odot}) = (-5.78 \pm 1.18) + (1.17 \pm 0.10) \log(M_{\text{tot,c}}/M_{\odot})$	0.35 ± 0.03	0.86 ± 0.04
$\log(M_{\star}/M_{\odot}) = (-9.56 \pm 1.16) + (1.39 \pm 0.09) \log(M_{\text{tot,500}}/M_{\odot})$	0.25 ± 0.03	0.91 ± 0.02
$\log(M_{\star}/M_{\odot}) = (11.67 \pm 0.31) + (0.95 \pm 0.10) \log(f_{\text{gas,g}})$	0.35 ± 0.04	0.85 ± 0.05
$\log(M_{\star}/M_{\odot}) = (11.79 \pm 0.26) + (1.18 \pm 0.10) \log(f_{\text{gas,c}})$	0.25 ± 0.04	0.92 ± 0.04
$\log(M_{\star}/M_{\odot}) = (11.02 \pm 0.24) + (1.11 \pm 0.11) \log(f_{\text{gas,500}})$	0.38 ± 0.03	0.81 ± 0.05
$\log(L_{\text{x,g}}/10^{44} \text{ erg s}^{-1}) = (-2.64 \pm 0.10) + (4.23 \pm 0.29) \log(T_{\text{x,g}}/\text{keV})$	0.49 ± 0.04	0.90 ± 0.03
$\log(L_{\text{x,c}}/10^{44} \text{ erg s}^{-1}) = (-2.53 \pm 0.08) + (4.42 \pm 0.23) \log(T_{\text{x,c}}/\text{keV})$	0.49 ± 0.04	0.93 ± 0.02
$\log(L_{\text{x,500}}/10^{44} \text{ erg s}^{-1}) = (-2.34 \pm 0.09) + (4.71 \pm 0.26) \log(T_{\text{x,c}}/\text{keV})$	0.57 ± 0.05	0.92 ± 0.02
$\log(M_{\star}/M_{\odot}) = (7.69 \pm 0.44) + (-0.55 \pm 0.24) \log(K_{\text{x,g}}^{-3/2}/\text{keV}^{-3/2} \text{ cm}^{-3})$	0.62 ± 0.04	-0.31 ± 0.14
$\log(M_{\star}/M_{\odot}) = (7.31 \pm 1.13) + (-0.46 \pm 0.38) \log(K_{\text{x,c}}^{-3/2}/\text{keV}^{-3/2} \text{ cm}^{-3})$	0.64 ± 0.04	-0.19 ± 0.15
$\log(M_{\star}/M_{\odot}) = (8.64 \pm 1.25) + (-0.01 \pm 0.30) \log(K_{\text{x,500}}^{-3/2}/\text{keV}^{-3/2} \text{ cm}^{-3})$	0.65 ± 0.04	0.00 ± 0.13
$\log(M_{\star}/M_{\odot}) = (-0.34 \pm 0.89) + (1.10 \pm 0.11) \log(M_{\text{cca,g}}/M_{\odot})$	0.39 ± 0.03	0.80 ± 0.05
$\log(M_{\star}/M_{\odot}) = (0.45 \pm 0.71) + (0.98 \pm 0.08) \log(M_{\text{cca,c}}/M_{\odot})$	0.30 ± 0.03	0.90 ± 0.04
$\log(M_{\star}/M_{\odot}) = (2.07 \pm 0.59) + (0.77 \pm 0.07) \log(M_{\text{cca,500}}/M_{\odot})$	0.38 ± 0.03	0.82 ± 0.05
$\log(M_{\star}/M_{\odot}) = (8.29 \pm 0.07) + (0.98 \pm 0.10) \log(R_{\text{cond}}/\text{kpc})$	0.32 ± 0.04	0.87 ± 0.05
Optical/stellar correlations:		
$\log(M_{\star}/M_{\odot}) = (-1.53 \pm 0.87) + (4.36 \pm 0.37) \log(\sigma_{\epsilon}/\text{km s}^{-1})$	0.36 ± 0.02	0.84 ± 0.04
$\log(M_{\star}/M_{\odot}) = (8.37 \pm 0.07) + (1.11 \pm 0.14) \log(L_{\text{K}}/10^{11} L_{\odot})$	0.46 ± 0.03	0.71 ± 0.07
$\log(M_{\star}/M_{\odot}) = (8.56 \pm 0.05) + (0.90 \pm 0.09) \log(M_{\text{bulge}}/10^{11} M_{\odot})$	0.40 ± 0.03	0.79 ± 0.05
Bayesian multivariate fitting $Y = (\bar{\alpha} \pm \sigma_{\alpha}) + (\bar{\beta}_1 \pm \sigma_{\beta_1})X_1 + (\bar{\beta}_2 \pm \sigma_{\beta_2})X_2$		
	$\bar{\epsilon} \pm \sigma_{\epsilon}$	$\bar{\text{pcorr}}_1 \pm \sigma_{\text{p}_1}$
		$\bar{\text{pcorr}}_2 \pm \sigma_{\text{p}_2}$
X-ray/plasma correlations:		
$\log(T_{\text{x,g}}/\text{keV}) = (0.58 \pm 0.14) + (0.21 \pm 0.02) \log(L_{\text{x,g}}/10^{44} \text{ erg s}^{-1}) + (-0.07 \pm 0.07) \log(R_{\text{x,g}}/\text{kpc})$	0.11 ± 0.01	0.88 ± 0.06
$\log(T_{\text{x,c}}/\text{keV}) = (-0.15 \pm 0.32) + (0.16 \pm 0.02) \log(L_{\text{x,c}}/10^{44} \text{ erg s}^{-1}) + (0.28 \pm 0.14) \log(R_{\text{x,c}}/\text{kpc})$	0.10 ± 0.01	0.78 ± 0.07
$\log(T_{\text{x,g}}/\text{keV}) = (1.85 \pm 0.25) + (0.21 \pm 0.02) \log(I_{\text{x,g}}/\text{erg s}^{-1} \text{ cm}^{-2}) + (0.39 \pm 0.05) \log(R_{\text{x,g}}/\text{kpc})$	0.10 ± 0.01	0.89 ± 0.05
$\log(M_{\star}/M_{\odot}) = (9.42 \pm 0.91) + (0.37 \pm 0.06) \log(L_{\text{x,c}}/10^{44} \text{ erg s}^{-1}) + (0.34 \pm 0.42) \log(R_{\text{x,c}}/\text{kpc})$	0.32 ± 0.02	0.71 ± 0.09
$\log(M_{\star}/M_{\odot}) = (9.43 \pm 0.19) + (1.64 \pm 0.37) \log(T_{\text{x,c}}/\text{keV}) + (0.10 \pm 0.08) \log(L_{\text{x,c}}/10^{44} \text{ erg s}^{-1})$	0.24 ± 0.02	0.66 ± 0.14
$\log(M_{\star}/M_{\odot}) = (9.17 \pm 0.85) + (2.13 \pm 0.33) \log(T_{\text{x,c}}/\text{keV}) + (0.01 \pm 0.45) \log(R_{\text{x,c}}/\text{kpc})$	0.26 ± 0.02	0.79 ± 0.10
Optical/stellar correlations:		
$\log(\sigma_{\epsilon}^2/\text{km}^2 \text{ s}^{-2}) = (5.22 \pm 0.11) + (1.43 \pm 0.17) \log(L_{\text{K}}/10^{11} L_{\odot}) + (-1.40 \pm 0.22) \log(R_{\text{e}}/\text{kpc})$	0.10 ± 0.02	0.92 ± 0.05
$\log(M_{\star}/M_{\odot}) = (9.55 \pm 0.35) + (2.99 \pm 0.58) \log(L_{\text{K}}/10^{11} L_{\odot}) + (-2.56 \pm 0.75) \log(R_{\text{e}}/\text{kpc})$	0.39 ± 0.04	0.77 ± 0.11
$\log(M_{\star}/M_{\odot}) = (0.54 \pm 1.11) + (1.71 \pm 0.24) \log(\sigma_{\epsilon}^2/\text{km}^2 \text{ s}^{-2}) + (0.42 \pm 0.15) \log(L_{\text{K}}/10^{11} L_{\odot})$	0.34 ± 0.02	0.75 ± 0.10
$\log(M_{\star}/M_{\odot}) = (-0.77 \pm 0.88) + (1.96 \pm 0.20) \log(\sigma_{\epsilon}^2/\text{km}^2 \text{ s}^{-2}) + (0.43 \pm 0.16) \log(R_{\text{e}}/\text{kpc})$	0.34 ± 0.03	0.85 ± 0.07
Mixed X-ray and optical correlations:		
$\log(M_{\star}/M_{\odot}) = (10.23 \pm 0.24) + (0.43 \pm 0.05) \log(L_{\text{x,c}}/10^{44} \text{ erg s}^{-1}) + (-0.06 \pm 0.19) \log(L_{\text{K}}/10^{11} L_{\odot})$	0.32 ± 0.02	0.80 ± 0.09
$\log(M_{\star}/M_{\odot}) = (5.67 \pm 1.14) + (1.65 \pm 0.21) \log(T_{\text{x,c}}/\text{keV}) + (0.73 \pm 0.23) \log(\sigma_{\epsilon}^2/\text{km}^2 \text{ s}^{-2})$	0.23 ± 0.02	0.83 ± 0.07
$\log(M_{\star}/M_{\odot}) = (4.67 \pm 0.59) + (2.19 \pm 0.39) \log(R_{\text{x,c}}/\text{kpc}) + (0.27 \pm 0.23) \log(R_{\text{e}}/\text{kpc})$	0.42 ± 0.03	0.70 ± 0.10

Note. Additional complementary univariate and multivariate correlations can be found in Appendix B.

the global/virial temperature ($T_{x,c} \approx T_{x,500}$), within total uncertainties.

Figure 1 shows that the (LW) X-ray temperature within the galactic scale $R_{x,g}$ (left; Equation (2)) or within the macro-scale group/cluster core $R_{x,c}$ (right; Equation (3)) are very tightly correlated with the BH mass. The intrinsic scatter $\sim 0.21\text{--}0.25$ dex is the smallest found among all the studied correlations (1σ level shown as a filled light red band), in particular compared with all the other optical/stellar properties (Section 3.1.2)—including the stellar velocity dispersion which has 0.1 dex larger scatter. This is a key result, given the large sample size and diversity of systems, spanning from massive clusters and groups to isolated S0s and spiral galaxies (top-right to bottom-left sectors, or blue to green and cyan color-coding). The best-fit slopes are both consistent with a power-law index of 2.1–2.7, with correlation coefficients in the very strong regime (0.93–0.94). In terms of normalization, a 0.8 keV halo corresponds to a $\sim 10^9 M_\odot$ SMBH.

We will dissect in Section 4 what is the role of the potential versus different accretion mechanisms arising from the hot plasma halo. For now, it is worthwhile to understand the notion that a hotter halo leads to substantially more massive black holes ($M_\bullet \propto T_x^{2.5}$), up to even UMBHs in BCGs. This means that the accretion process shall be stimulated by the presence of a larger plasma mass (e.g., in galactic coronae or the more extended IGrM/ICM), rather than hindered by its thermal pressure, which tends to oppose the gas gravitational infall. The high end of the $M_\bullet - T_{x,c}$ relation hints at a potential saturation, although at present it is unclear whether UMBHs with several tens of billions of solar masses exist in the universe.

Figure 2 shows the second fundamental X-ray variable, i.e., the plasma luminosity, enclosed within our three radial regions (top to bottom panel: $R_{x,g}$, $R_{x,c}$, and R_{500} , respectively; Equations (2)–(4)). As for the X-ray temperature, L_x shows a very strong positive correlation with the black hole mass (corr > 0.85). Regarding normalization, a typical SMBH of $10^9 M_\odot$ tends to reside in a plasma halo of $\sim 10^{41} \text{ erg s}^{-1}$. The log slope is now below unity, ranging between 0.5 and 0.4, adopting the galactic or cluster/virial scale, respectively (as L_x steadily increases with radius). However, the range covered by L_x is now over 6 dex, i.e., a $6 \times$ range increase compared with the temperature log scaling (we checked that the $L_x - T_x$ relation is consistent with that in other observational works that include low-mass galaxies; see Section 3.3.2 and Appendix A). It is a major result that the SMBH scaling holds over such a wide range of X-ray luminosities, reflecting very different (poor and rich) environments. We note the R_{500} scalings are the more uncertain correlations: their contained scatter might be a reflection of the currently low number of available central massive galaxies (i.e., those having macro properties, as $L_{x,500}$, set by the extended ICM and not the CGM; Section 2.1.2).

Another important difference with T_x is the relatively larger intrinsic scatter in $M_\bullet - L_x$, hovering in the range 0.29–0.31 dex, though still tighter than any optical scaling relation (Figure 3). Removing the 3.5σ outlier NGC 1600 (which could have stochastically suffered a ram-pressure halo stripping or AGN outburst) would reduce the scatter by 0.03 dex, approaching that of the temperature scalings. Conversely, a case of perfectly matching the mean best fit is provided by M87 ($L_{x,c} \simeq 1.2 \times 10^{43} \text{ erg s}^{-1}$), whose SMBH horizon has been recently imaged via EHT, constraining $\log M_\bullet/M_\odot \simeq 9.8$. Interestingly, the lowest scatter in L_x is found within the core region (though

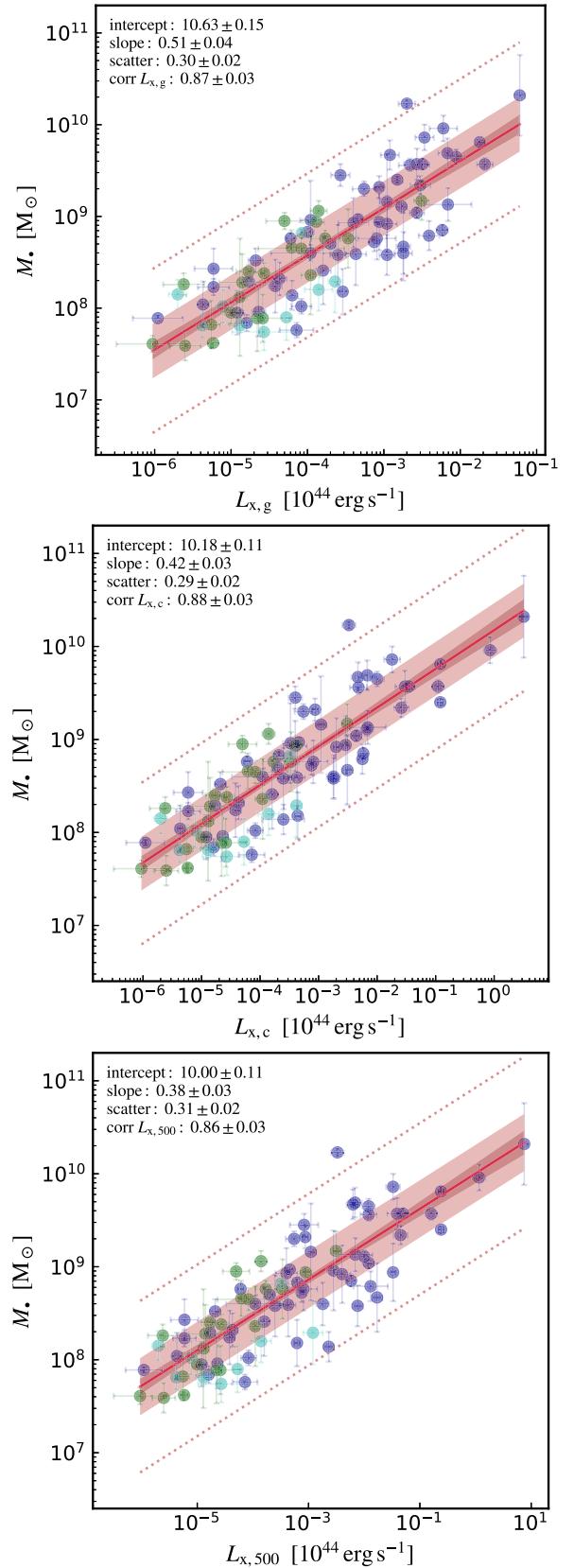


Figure 2. BH mass vs. X-ray luminosity (Section 3.1.1) within the galactic/CGM scale ($R_{x,g} \sim 0.03 R_{500}$; top), group/cluster core ($R_{x,c} \sim 0.15 R_{500}$; middle), and group/cluster R_{500} (bottom). Analog of Figure 1. The X-ray luminosity is tightly correlated with the SMBH mass (better than the optical L_K counterpart), in particular within the core region.

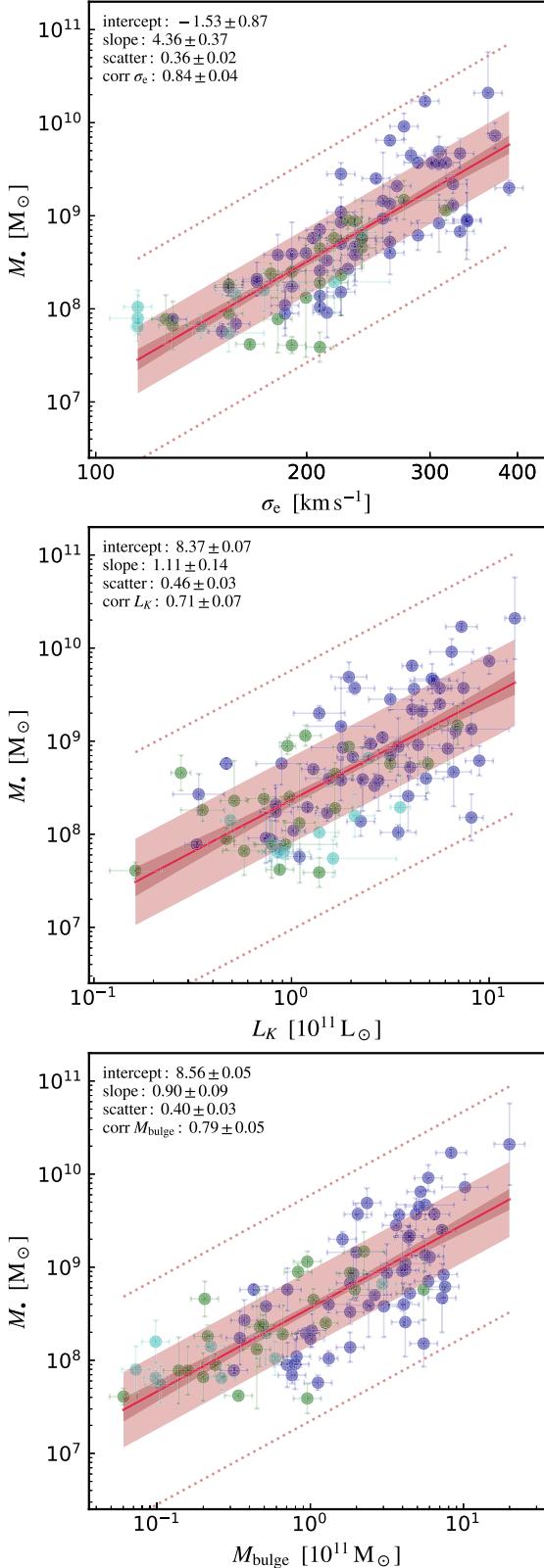


Figure 3. Black hole mass vs. galactic optical properties (Section 3.1.2), including the stellar velocity dispersion ($\langle R_e \rangle$; top), total (bulge and disk) K -band luminosity (middle), and bulge mass (bottom). Analog of Figure 1. The optical properties have larger scatter compared with the X-ray ones. The velocity dispersion is the tighter observable, though showing superlinear behavior at the high end.

with small significance), where radiative cooling is very effective. Since $L_x \propto M_{\text{gas}}^2(r)$, any gas evacuation (or phase transition) is associated with significant luminosity variations; indeed, feedback processes and mergers/cosmic inflows are particularly impactful in the inner and outer regions (e.g., Ghirardini et al. 2019), respectively, while the intermediate region is less affected by them (the $M^* - f_{\text{gas},c}$ relation will unveil this more clearly; Section 3.2.6). In Section 4.1.2, we will test the role of gas condensation and CCA-regulated AGN feedback; indeed, the existence of a tight correlation between BH mass and L_x/T_x is consistent with first-principle predictions (Gaspari & Sadowski 2017).

We note that more massive SMBHs are hosted by galaxies with more extended X-ray and effective radii (e.g., $M^* - R_{x,g}$ has a mild correlation with slope 1.1 ± 0.2), as more luminous halos have larger atmospheres (Figure 24). A stronger correlation emerges considering $M^* - R_{x,c}$ ($\beta = 2.4 \pm 0.3$), although the BH correlations with characteristic radii typically show a significant scatter (~ 0.4 dex; e.g., Figure 14). The correlation with R_{500} is tighter and steeper, being a pure reflection of the T_x scaling. The multivariate, partial correlation analysis in Section 3.3 combining all the fundamental observables will help to understand any potential X-ray virial relations or deviations from it via nongravitational processes.

While finishing our five-year project, another short work discussed a correlation between M^* and cluster halo temperature in 17 BCGs/BGGs (Bogdán et al. 2018; no X-ray value was used here from their paper). They find a best-fit $\log(M^*/10^9 M_\odot) = (0.20 \pm 0.09) + (1.74 \pm 0.16)\log(T_{x,c}/\text{keV})$ (with $T_{x,c}$ as proxy for $T_{x,500}$). The shallower slope is due to a massive-system bias: selecting only central galaxies in our sample leads to $\log(M^*/10^9 M_\odot) = (0.20 \pm 0.07) + (1.83 \pm 0.31)\log(T_{x,c}/\text{keV})$, which is consistent with the above. Given their smaller sample and less robust BCES method (Section 2.2), their scatter is ~ 0.1 dex higher, though still tighter than that of their $M^* - \sigma_e$. This marks the importance of collecting a larger and more complete sample covering different morphological, dynamical, and environmental types.

3.1.2. Optical/Stellar Velocity Dispersion, Luminosity, and Bulge Mass

We focus now on the counterpart variables in the optical band that are tracing the stellar component, rather than the plasma halo. Given that most stars are confined within a few effective radii, the optical properties can only trace the galactic scale, and not the larger scale core or virial region.

Figure 3 shows the SMBH mass as a function of the three fundamental variables adopted in several previous studies: the 1D velocity dispersion σ_e (within an aperture the size of effective radius R_e), bulge mass, and total (bulge plus disk) galactic luminosity in the NIR ($\sim 2.2 \mu\text{m}$) K band (Section 2). The first key result is the substantially larger intrinsic scatter of all the optical properties compared with that of the X-ray counterparts (Figures 1–2), which can reach values up to 0.5 dex for L_K , with the correlation coefficient dropping to the mild (~ 0.7) level.

The most reliable optical property is the stellar velocity dispersion σ_e (top panel), which represents another tracer of the (inner) galactic potential $\sigma_e^2 \propto \phi_g$ (Section 3.3.1). The retrieved

σ_e scatter is 0.36 dex, which is 0.15–0.11 dex larger than that of the galactic/core X-ray temperature (at over 99.9% confidence). The $M_\bullet - \sigma_e$ log slope is 4.4 ± 0.4 , which is consistent with twice that of the $M_\bullet - T_x$ scaling, i.e., $\sigma_e^2 \propto T_x$, as expected in virialized systems.³⁹ The retrieved $M_\bullet - \sigma_e$ slope is similar to that found by previous studies on bulge-dominated galaxies (e.g., Kormendy & Ho 2013); it would steepen to a value $\gtrsim 5$, almost doubling the intrinsic scatter, including the more uncertain low-mass BHs and related irregular galaxies (e.g., Saglia et al. 2016). The high-mass end of the $M_\bullet - \sigma_e$ is a significant source of scatter with increasingly over-massive BHs (five objects are approaching the top 3σ channel), in conjunction with the increased presence of BGGs/BCGs (see also Figure 21; some works interpret this as a nonlinear bend). The disk (low B/T) and spiral galaxies (green/cyan points) start also to show symptoms of a decline below the linear fit (despite measurements of σ_e remaining accurate), while $M_\bullet - T_x$ and $M_\bullet - L_x$ retain a stable linear behavior regardless of different morphological types and environment (Figure 21).

The second panel in Figure 3 shows the $M_\bullet - L_K$ scaling. While the total galaxy NIR luminosity is a good proxy for the total stellar mass (as it is not very affected by dust absorption), the hosted BH mass is only mildly tied to this galactic observable. Unlike the other quantities, the morphological types tend to be significantly mixed from low to large L_K values, corroborating the large ϵ value. On the other hand, the slope is consistent with unity, i.e., there is a direct 1:1 conversion in both logarithmic and linear space, with an average $10^{11} L_\odot$ galaxy hosting a $M_\bullet \simeq 2 \times 10^8 M_\odot$. Converting L_K to total stellar mass (Equation (1)) would show similar correlation slope and scatter, within the 1σ uncertainty (the total stellar mass correlations are thus redundant and not shown). At variance with temperatures, the X-ray versus optical luminosities (at all radii) show very different scaling with M_\bullet , since L_x covers four more orders of magnitude compared with L_K . In other words, the X-ray properties allow us to probe more extended regimes and regions than those traced by stars, better separating the loci occupied by LTGs and ETGs. The multivariate analysis (Section 3.3) will unveil that the X-ray and optical fundamental planes behave differently due to L_x breaking the self-similar gravitational collapse expectation.

A way to reduce the scatter is to consider purely the stellar bulge mass, instead of the total stellar luminosity/mass (which is contaminated by potential disk features). The bottom panel in Figure 3 shows the correlation with the stellar bulge mass (known as the “Magorrian relation”; Magorrian et al. 1998). Translating from a luminosity to a mass is nontrivial since the M_\bullet/L_K depends on complex stellar population models (Section 2.1). Moreover, the B/T ratio should be taken as approximate, as it can vary significantly between studies. Keeping in mind such hurdles, the $M_\bullet - M_{\text{bulge}}$ relation is able to reduce the scatter to 0.40 dex, albeit not yet reaching the lower level of σ_e . The log slope is slightly shallower than unity ($\beta \approx 0.9$). Regarding normalization, $M_{\text{bulge}}/M_\bullet \approx 360$, implying that stars continuously accumulate within the galaxy without substantially feeding the BH during cosmic time, given their collisionless nature.

The $M_\bullet - \sigma_e$ appears to be the most stable optical estimator of BH mass. However, it presents signs of unreliability at the high-mass end, with several galaxies exceeding the 2σ scatter

³⁹ Specifically, $\sigma_e^2 = k_b T_x / \mu m_p$ (with $\mu = 0.62$ the plasma particle mean weight); while we find a unity slope (0.93 ± 0.08) for $\sigma_e^2 - T_{x,g}$, the normalization is lower than the virial expectation by $\approx 40\%$, implying extra heating due to feedback processes.

band. None of the optical variables shows better correlations than the X-ray counterparts, in terms of intrinsic scatter and correlation coefficient ($> 99\%$ confidence level). Moreover, performing a pairwise correlation analysis on residuals (see Shankar et al. 2019), we find that $\log M_\bullet - \langle \log M_\bullet | \log \sigma_e \rangle$ versus $\log T_x - \langle \log T_x | \log \sigma_e \rangle$ has 60% larger correlation coefficient (0.8) than $\log M_\bullet - \langle \log M_\bullet | \log T_x \rangle$ versus $\log \sigma_e - \langle \log \sigma_e | \log T_x \rangle$, suggesting that X-ray properties are more fundamental than optical properties. There are two reasons that we deem to be important to explain this. First, the stellar component is tracing purely the inner part of the whole gravitational potential, thus missing the macro group/cluster halo. Second, stars are the residual by-product of a more wide-spread top-down multiphase condensation process, which originates in the X-ray plasma atmosphere (particularly in the core, $r \lesssim 0.1 R_{500}$; Section 4).

3.2. Univariate Correlations: Composite X-Ray Variables

We now move on to the univariate correlations of the composite variables, again focusing on their interplay with BH mass. Indeed, the equations of thermodynamics and hydrodynamics for a diffuse gas/plasma are linked to properties such as pressure and particle number density. The concept to keep in mind is to derive these properties only from the fundamental observables, i.e., X-ray luminosity and temperature (while propagating the related errors), thus keeping any parameterization and assumption to the minimum.

3.2.1. Electron Number Density

The plasma luminosity is given by

$$L_x = \int n_e n_i \Lambda(T_x, Z) dV, \quad (9)$$

where $\Lambda(T_x, Z)$ is the radiative plasma cooling function in collisional ionization equilibrium (Sutherland & Dopita 1993)⁴⁰ adopting metallicity $Z \simeq 0.7, 0.4, 0.3 Z_\odot$ for the galactic, core, and R_{500} region, respectively (Mernier et al. 2017).⁴¹ By differentiating and discretizing Equation (9) over finite spherical shells, $\Delta V = (4/3)\pi(R_{\text{out}}^3 - R_{\text{in}}^3)$, the plasma electron number density can be retrieved as

$$n_e \simeq \left(\frac{\Delta L_x}{\Delta V} \frac{\mu_i / \mu_e}{\Lambda(T_x, Z)} \right)^{1/2}, \quad (10)$$

where $(\mu_i, \mu_e) \simeq (1.30, 1.18)$ are the ion and electron mean weights (for a plasma with solar composition). Given finite discretization of Equation (9), the computed n_e should be understood as a mean density inside our three radial shells ($0 - R_{x,g}$, $R_{x,g} - R_{x,c}$, $R_{x,c} - R_{500}$).⁴² Over our entire sample and bins, we find a median density gradient $d \log n_e / d \log r = -1.6 \pm 0.3$, which is consistent with that in other works (e.g., Babyk et al. 2018 and Hogan et al. 2017). We remark that gas

⁴⁰ The cooling curve includes spectral calculations for H, He, C, N, O, Fe, Ne, Na, Si, Mg, Al, Ar, S, Cl, Ca, Ni, and all related stages of ionization. We tested different cooling curves (e.g., Schure et al. 2009), finding comparable results.

⁴¹ We tested the full observational scatter of observed abundance values, finding no major change in results. Further, we note that such changes in metallicity alter μ_i by less than 1%.

⁴² For noncentral galaxies, the core/outskirt gradients are approximated as $dL_x/dV \sim L_x/V$.

density is a composite variable given by the combination of X-ray luminosity, temperature, and R_x^3 (Equation (10)).

Figure 4 shows the correlation between SMBH mass and plasma electron density, inside our three adopted radial shells. For the inner scale the correlation is weak (absent at the 2σ level), corroborated by the substantial scatter ($\epsilon \simeq 0.6$) and the large errors in the posterior distributions (broad red bands). Indeed, most of the galaxies have an average galactic/CGM gas number density ranging between $n_{e,g} \sim 10^{-5}$ – 10^{-2} cm $^{-3}$ (consistently with other studies, e.g., Lakhchaura et al. 2018). The correlation enters instead the strong regime (almost halving the scatter) if we consider the core or R_{500} region. This corroborates the result highlighted by the M – $L_{x,c}$ (Section 3.1.1), i.e., the halo core region (where the cooling time is typically below the Hubble time) is one of the best predictors for the SMBH growth. The slope is consistent with unity, with a typical SMBH mass of a few $10^9 M_\odot$ (massive galaxies) linked to $n_e \approx 10^{-3}$ – 10^{-4} cm $^{-3}$ in the macro-scale core/outskirt region (in agreement with values retrieved by Sun 2012 and Hogan et al. 2017 for BGGs and BCGs). Since L_x (via $n_e^2 \Lambda$) is a direct manifestation of the plasma radiative emission, these findings suggest that condensation processes could play a major role in the evolution of SMBHs (Section 4.1.2).

3.2.2. Total Gas Pressure

A key thermodynamic variable which determines the hydrostatic balance of a stratified atmosphere is the total gas/plasma pressure ($P = P_e + P_i$) defined as

$$P = n k_b T_x, \quad (11)$$

where $n = n_e + n_i \simeq 2 n_e$ is the total gas particle number density. Figure 5 shows the M – P_x correlation for our three radial shells (Section 3.2.1). All the gas pressure scalings reside in the regime of strong correlation with BH mass ($\text{corr} \approx 0.7$ – 0.9). The direct combination of density and temperature seems to ameliorate the galactic scaling, although the scatter remains large at 0.5 dex. The best-fit slope is stable at sublinear values, $\beta \approx 0.75$. As for L_x , the core region displays the lowest scatter ($\epsilon \simeq 0.3$) and highest corr coefficient, with a characteristic gas pressure of $\sim 10^{-3}$ keV cm $^{-3}$ for halos hosting a $10^9 M_\odot$ BH.

Interestingly, more pressure-supported halos harbor larger SMBHs. If we think in terms of classical hot-mode accretion (Bondi, ADAF, etc.), in which a larger atmospheric pressure suppresses accretion (Section 4.1.1), such a trend seems difficult to develop. However, if accretion proceeds through the cold mode, then a more pressurized gas implies larger available internal energy, $P/(\gamma - 1)$,⁴³ to be radiated away, and thus a larger condensing neutral/molecular gas mass available to rain onto the SMBH (dropping out of the diffuse atmosphere in quasi hydrostatic equilibrium).

3.2.3. Gas Mass

The plasma mass within a given enclosed radius can be retrieved (integrating over our bins) via

$$M_{\text{gas}}(< r') = \int_0^{r'} \rho 4\pi r^2 dr, \quad (12)$$

⁴³ The (nonrelativistic) plasma adiabatic index is $\gamma = 5/3$.

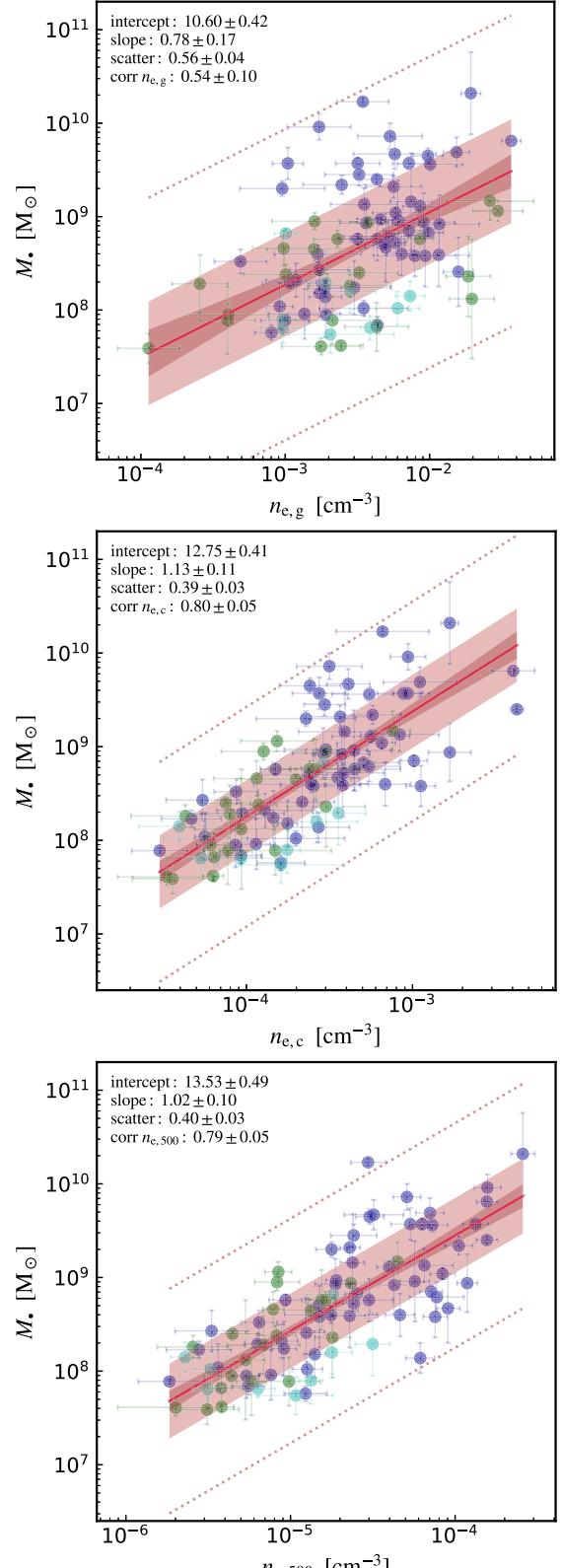


Figure 4. Black hole mass vs. electron number density (Section 3.2.1) within the galactic/CGM $R_{x,g}$ (top), group/cluster $R_{x,c}$ (middle), and R_{500} (bottom) shells. Analog of Figure 1. Density is derived from the L_x gradient and $\Lambda(T_x, Z)$ (propagating the related errors; Equation (10)). While the CGM scale displays very weak correlation, the core plasma density is strongly correlated with BH mass.

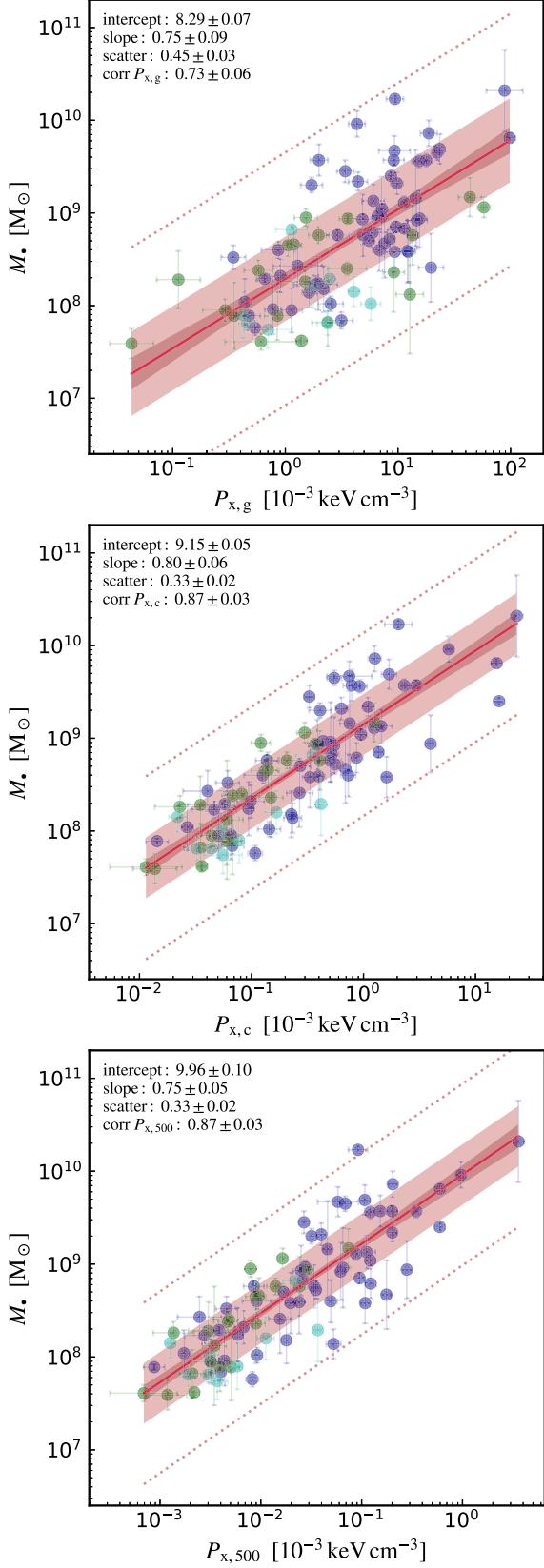


Figure 5. Black hole mass vs. gas pressure (Section 3.2.2) inside the $R_{x,g}$ (top), $R_{x,c}$ (middle), and R_{500} (bottom) shells. Analog of Figure 1. Similar to the X-ray luminosity, the core plasma pressure is a good and tight indicator of the central BH growth, although it loses efficacy in the galactic region.

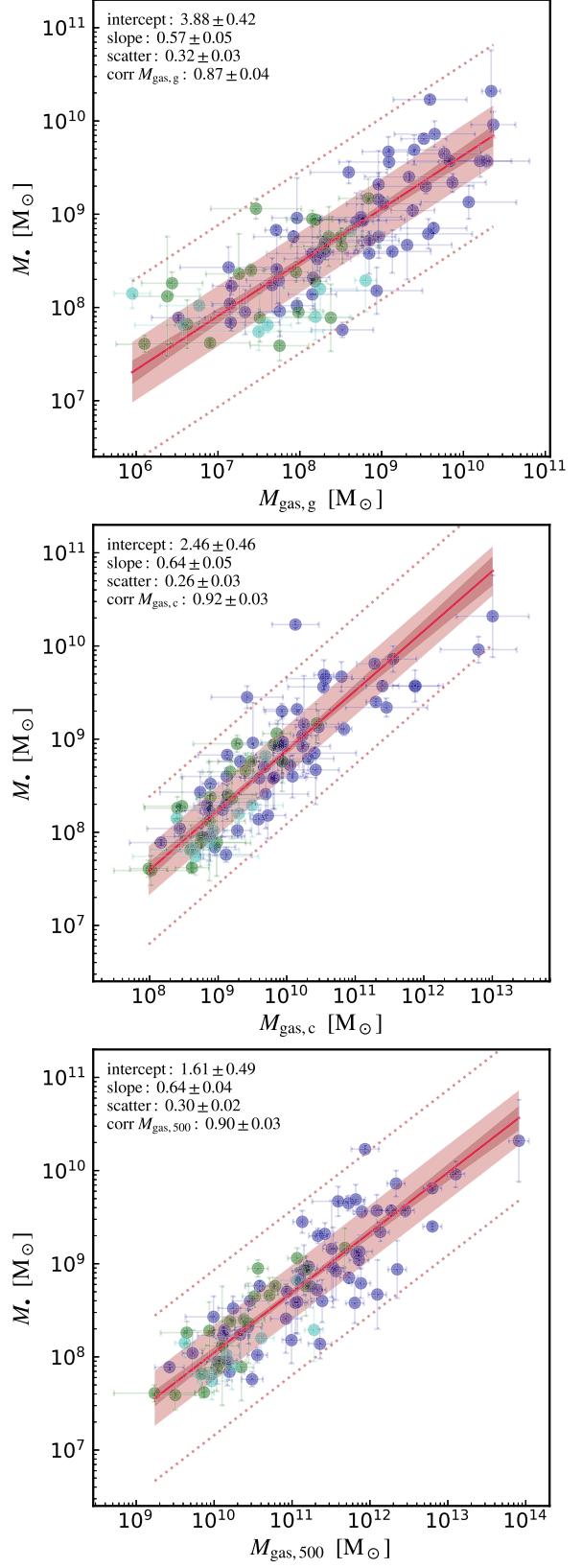


Figure 6. Black hole mass vs. enclosed gas mass (Section 3.2.3) within $R_{x,g}$ (top), $R_{x,c}$ (middle), and R_{500} (bottom) shells. Although M_{gas} is a derived property, M_* – M_{gas} is tight across all regions, and shows a nearly maximal positive correlation coefficient in the core region. Compared with the stellar mass (Magorrian) relation, the scatter is halved and is analogous to the fundamental T_x correlations.

where the total gas density is $\rho = n_e \mu_e m_p = n \mu m_p$. Figure 6 shows the M_{\bullet} – M_{gas} correlations. In spite of being (here) a derived variable, M_{gas} is very well correlated with the BH mass, lowering the intrinsic scatter to $\epsilon \simeq 0.26 \pm 0.03$, comparable to that of the fundamental X-ray temperature scalings. Being an integrated quantity, gas mass has a smoothening advantage compared with local properties. In the core region (middle panel), the Bayesian posterior of the corr coefficient shows a value 0.92 ± 0.03 , which is consistent with a maximal positive correlation at the 3σ level. Evidently, the gas mass plays a key role in the evolution of SMBHs. The slope is similar across all radial bins, with values $\beta \approx 0.6$. The galactic (top panel) and virial (bottom panel) relations bound the locus of optimal correlation.

Regarding normalization, the median $10^9 M_{\odot}$ BHs occupy core halos that have $\sim 10 \times$ more gas mass. As a ratio, this is over an order of magnitude lower compared with that involving the stellar bulge mass (the Magorrian relation; Section 3.1.2). We note that the retrieved range of core gas masses $M_{\text{gas},c} \sim 10^9$ – $10^{11} M_{\odot}$ is consistent with that of similar samples (e.g., Babyk et al. 2018), corroborating our derivation method. Considering the galactic scale (top panel), the median SMBH has M_{gas} roughly equivalent to M_{\bullet} (at least at $z \sim 0$). This suggests that, while a major fraction of the BH mass can be built up in time via gas accretion due to collisional processes (e.g., CCA inelastic collisions, hydrodynamical instabilities, viscosity, shocks, and turbulent mixing), stars remain largely unaffected by the accretion process being collisionless systems. This may also explain why most stellar properties present substantial scatter as estimators of M_{\bullet} , being linked to the BH growth via secondary/indirect effects.

3.2.4. Y_x Compton Parameter—Thermal Energy

Another key quantity that has become central to cluster and cosmological studies is the X-ray analog of the Compton Y_{sz} parameter (Kravtsov et al. 2006), which describes the strength of the thermal Sunyaev–Zel’dovich (SZ) effect.⁴⁴ We define such an X-ray analog as follows:

$$Y_x \equiv E_{\text{th}} = \frac{3}{2} \frac{k_b T_x}{\mu m_p} M_{\text{gas}}. \quad (13)$$

Multiplying by the relevant thermodynamic constants, Y_x represents another form of the plasma thermal energy content (or integrated pressure). Recent studies (e.g., Planelles et al. 2017 and references within) agree that $Y_{x,500}$ is a good proxy for the total mass, being relatively insensitive to feedback processes (e.g., the diffuse atmosphere is heated while being evacuated at the same time).

Figure 7 shows the M_{\bullet} – Y_x relation within our three X-ray radii. The Compton parameter correlation is able to reduce the scatter compared with the linked (punctual) M_{\bullet} – P_x : the galactic scaling indeed reduces the scatter by 30%, which is near $\epsilon \simeq 0.30$ across all regions. This is analogous to that of the gas mass scalings, except for the core region. The correlation coefficient remains in the very strong regime (corr ≈ 0.9). The slope is shallow, down to a value of approximately one-half;

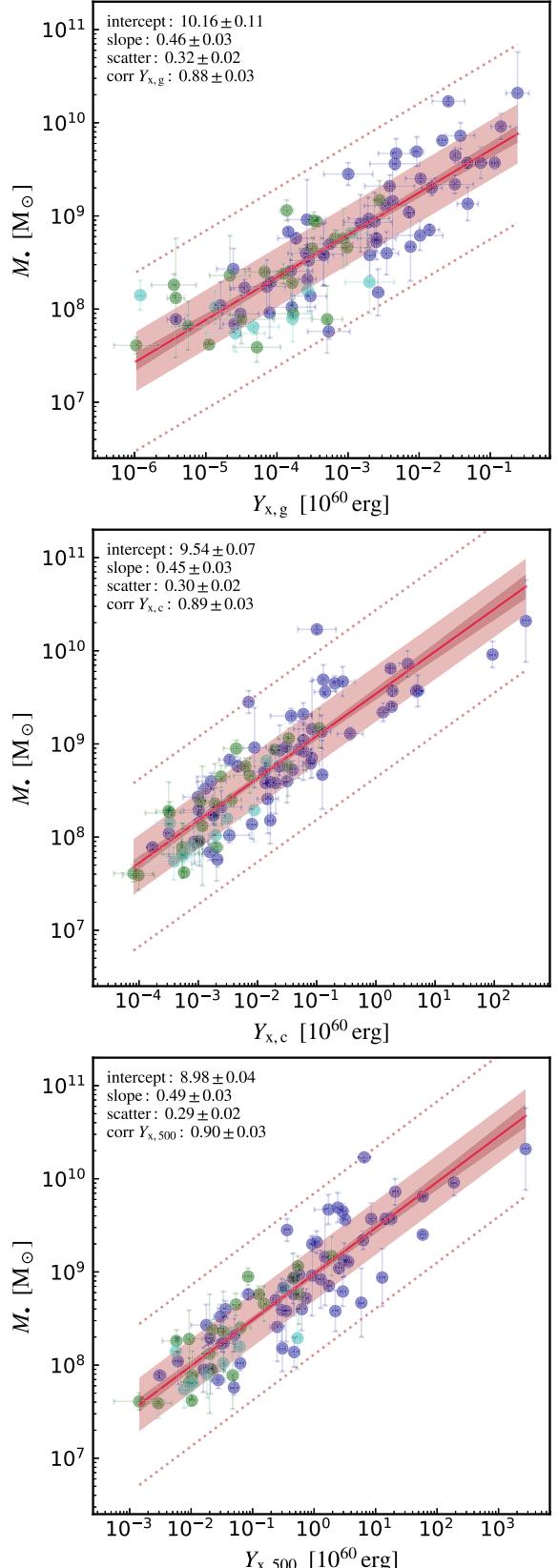


Figure 7. BH mass vs. Y_x parameter (gas thermal energy; Section 3.2.4) within $R_{x,g}$ (top), $R_{x,c}$ (middle), and R_{500} (bottom). Unlike P_x and n_e , the Compton parameter shows very stable behavior among all the inner and outer regions. The strong and tight correlation with M_{\bullet} , particularly over the whole cluster/group, can be leveraged by the next-generation radio/SZ telescopes.

⁴⁴ The distortion of the cosmic microwave background spectrum via inverse Compton scattering by the hot plasma electrons (e.g., Khatri & Gaspari 2016).

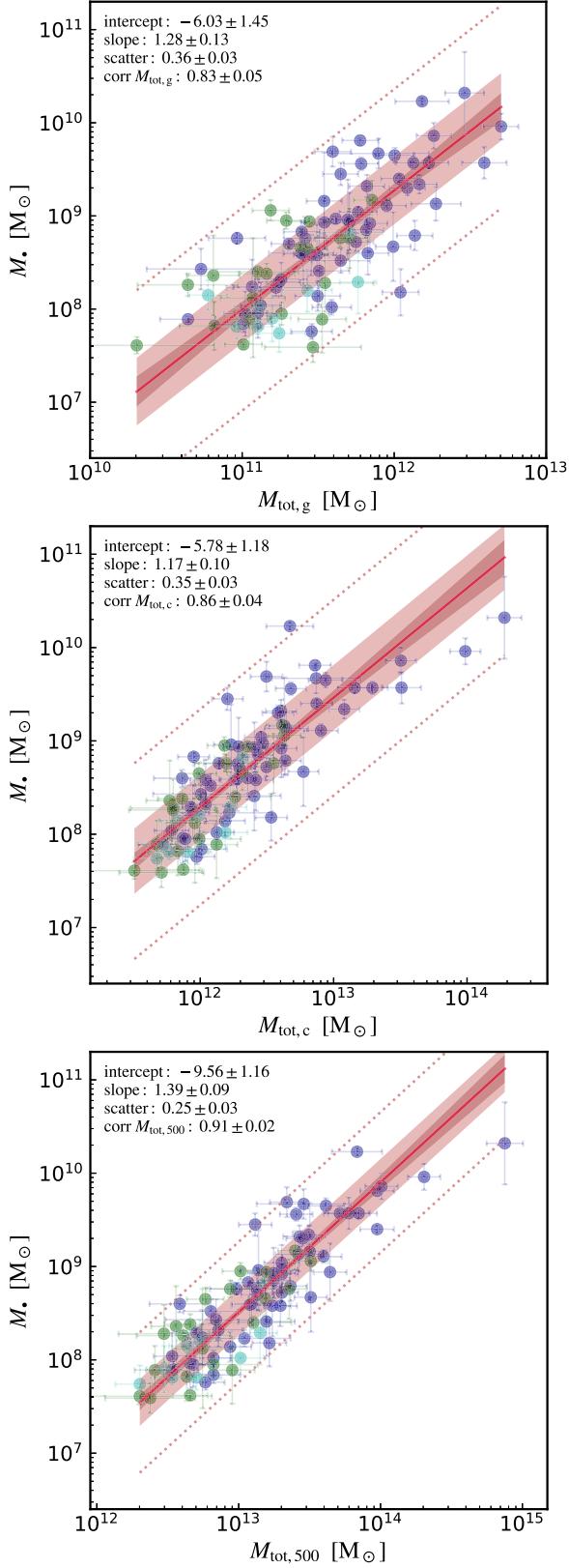


Figure 8. Black hole mass vs. total mass (dark matter, gas, stars; Section 3.2.5) within $R_{x,g}$ (top), $R_{x,c}$ (middle), and R_{500} (bottom). Besides $M_{\text{tot},500}$ (that is a simple reflection of $T_{x,500}$), the total mass scalings still show a significant correlation with M_* , albeit less tight than most gas scalings, in particular M_{gas} . This suggests that gaseous halos may play a more central role than DM halos in the growth of SMBHs.

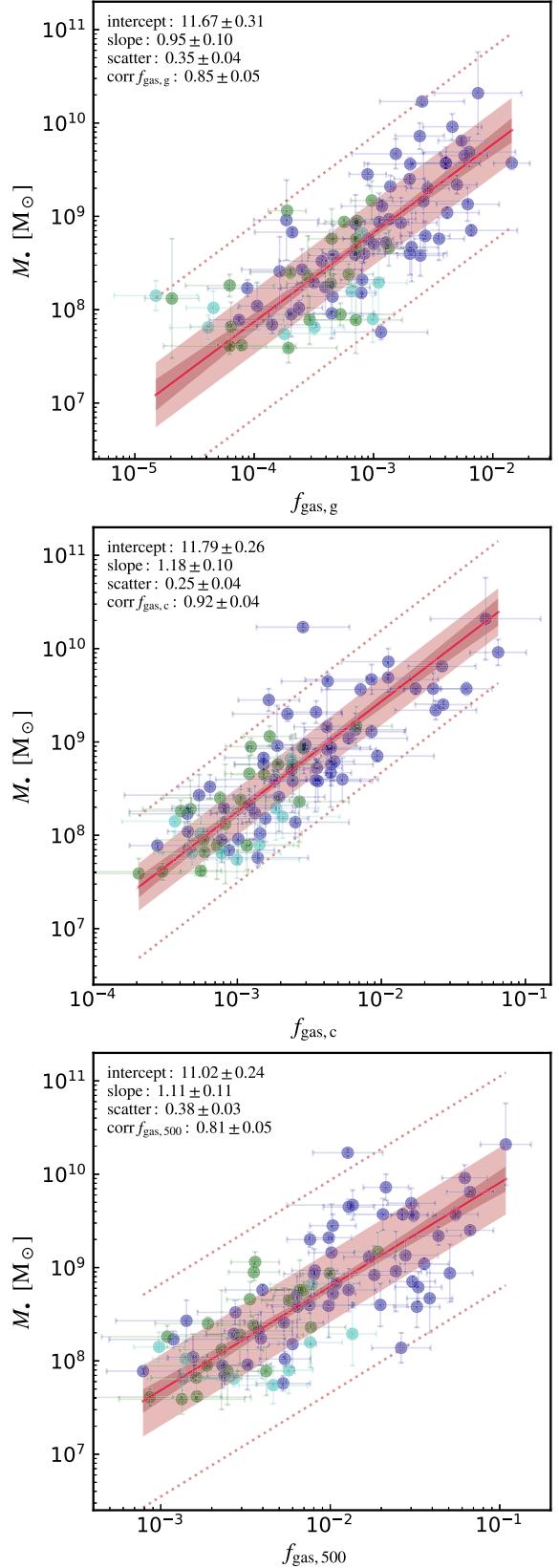


Figure 9. Black hole mass vs. gas fraction within $R_{x,g}$ (top), $R_{x,c}$ (middle), and R_{500} (bottom). A strong correlation is again found in the core, while the enclosing regions show substantial intrinsic scatter. The inclusion of total mass seems to weaken the stronger relation with gas mass. Overall, SMBHs seem to grow faster in halos that host relatively larger amounts of diffuse plasma.

indeed, thermal energy covers a wide range of values from small spirals to massive BCGs, $E_{\text{th,c}} \approx 10^{56}\text{--}10^{62}$ erg.

Interestingly, an SMBH of $10^9 M_{\odot}$ has an available rest-mass feedback energy of $E_* = \eta M_* c^2 \sim 2 \times 10^{60}$ erg (using a median mechanical efficiency $\eta \sim 10^{-3}$; Gaspari & Sadowski 2017) which can potentially unbind the galactic/core region if released in short time. However, such ejective (quasar-like) feedback matching the gas gravitational binding ($\sim M_{\text{gas}} \phi \simeq 2E_{\text{th}}$) energy would induce $M_* \sim 2 Y_x / (\eta c^2) \propto M_{\text{gas}} \sigma_e^2$ (the latter via $\sigma_e^2 \propto T_x$; Section 3.1.2), leading to much steeper scaling than that found in Figure 3 or 7. Thereby a gentler AGN feeding/feedback self-regulation and gradual deposition is required (Section 4; see also Gaspari et al. 2014).

Overall, the stability and tightness across largely different radial regions (varying each by one order of magnitude; Section 2.1.2) corroborates the importance of using Y_x over other thermodynamic observables (such as pressure or entropy). Such strong and tight correlations with the Compton parameter, particularly for the large-scale R_{500} region, imply that we can use the thermal SZ signal from hot halos to probe or trace SMBHs. This novel approach presents several advantages over the X-ray counterpart, since we can fully leverage the new ground-based radio facilities (instead of the more expensive X-ray space telescopes), which have recently entered a golden age (e.g., Atacama Large Millimeter/submillimeter Array (ALMA), MUSTANG-2, NIKA-2, SPT).

3.2.5. Total Mass (Dark Matter, Gas, Stars)

We analyze now the total (gravitational) mass, which is the sum of the baryonic (gas and stars) and DM component. The latter dominates (>90%) the total matter content, particularly in the core and outskirt regions of the group/cluster. Studies show that the DM distribution can be well described by a Navarro-Frenk-White (NFW) profile (Navarro et al. 1996) in most galaxies and clusters (e.g., Humphrey et al. 2006; Ettori et al. 2019), which is shaped by one minimal parameter. While the global mass is given via R_{500} (Section 2.1.2), $M_{\text{tot},500} = (4/3)\pi R_{500}^3 500\rho_c$, the DM mass enclosed within smaller radii can be retrieved via the NFW profile

$$M_{\text{DM}}(< r) = 4\pi\rho_s R_s^3 \left[\ln\left(\frac{R_s + r}{R_s}\right) - \frac{r}{R_s + r} \right], \quad (14)$$

where the scale radius is $R_s \equiv R_{500}/c_{500}$ and the concentration parameter is given by observations of galaxies and groups (Sun et al. 2009), $c_{500} \simeq 5.0(M_{\text{tot},500}/10^{13} M_{\odot})^{-0.09}$ (with 0.1 dex scatter). The characteristic DM density is defined as

$$\rho_s = \frac{500\rho_c}{3} \frac{c_{500}^3}{\ln(1 + c_{500}) - c_{500}/(1 + c_{500})}. \quad (15)$$

As secondary components of the total matter content, we add the enclosed gas mass (Section 3.2.3) and galaxy stellar mass (Section 3.1.2)⁴⁵ to the above DM mass. The retrieved total masses within R_{500} span a range of $M_{\text{tot},500} \sim 10^{12}\text{--}10^{15} M_{\odot}$ from isolated galaxies to massive clusters (consistently with Forbes et al. 2016 and Lovisari et al. 2015, respectively), and decrease by one/two orders of magnitude in the core/galactic regions. In agreement with analogous samples (Babyk et al. 2018), most of

⁴⁵ Although it has a minor role, we adopt a stellar profile $M_*(< r) = M_{*,\text{tot}} [r^2/(r + a)^2]$, where $a = R_c/(1 + \sqrt{2})$ (Hernquist 1990).

the objects have $M_{\text{tot,c}} \sim 2 \times 10^{11}\text{--}2 \times 10^{13} M_{\odot}$ within $r \lesssim 0.15 R_{500}$ (see Humphrey et al. 2009 for comparable $M_{\text{tot,g}}$). Moreover, we retrieve a $M_{\text{tot,c}} \propto Y_{x,c}^{0.40 \pm 0.03}$ scaling which is consistent with that found by Babyk et al. (2018) with slope 0.38 ± 0.05 .⁴⁶ Additional permutations of the halo properties can be retrieved via the total mass-to-light ratios shown in Figure 23.

Figure 8 shows the $M_{*}\text{--}M_{\text{tot}}$ correlations retrieved via our customary Bayesian analysis (Section 2.2), together with the 1- to 3σ scatter bands. As expected, $M_{\text{tot},500}$ is purely a reflection of the X-ray temperature via $R_{500} \propto T_{x,500}^{1/2}$ (Section 2.1.2), thus preserving the small scatter of $M_{*}\text{--}T_x$. On the other hand, the correlation between M_{*} versus total mass within the core and galactic scale shows a significant intrinsic scatter, which is comparable to that of the $M_{*}\text{--}\sigma_e$ and larger than that of most gas scalings. In particular, compared with the gas mass relation (Section 3.2.3), adding the DM component does not improve the mean corr coefficient and induces it to drop to a lower value. Under our assumptions, these results suggest that the plasma halos, and related baryonic properties, may play a more central role than the sole gravitational/DM potential in growing SMBHs. A positive correlation with M_{tot} is nevertheless established because hotter plasma halos are created in larger potential wells, as they get shock heated during the primordial halo formation. While a correlation cannot probe causation, we devote Section 4 to testing the BH mass growth via either gas accretion or mergers (which purely increase the gravitational potential), finding that the latter channel is subdominant over most of cosmic time (Section 4.1.4).

DM halos still represent a reasonable, useful proxy to predict the central SMBH mass. The correlation slopes are mildly superlinear, $\beta \simeq 1.2\text{--}1.4$ (with outliers becoming more frequent at the high-mass end). Such simple total mass scalings can be used by large-scale cosmological simulations (including both LTGs and ETGs) and semianalytic models (SAMs) to either test their results or calibrate the subgrid parameters on the $M_{*}\text{--}M_{\text{tot}}$ relation (instead of the more complex stellar scalings; Section 4.3). Another potential application is the inclusion of the AGN feedback power modeled directly from the DM mass; the latter is one of the best resolved and convergent properties in cosmological simulations (Sembolini et al. 2016).

Interestingly, equating the total BH feedback energy $E_* = \eta M_* c^2$ (Section 3.2.4) to the DM gravitational binding energy $\sim M_{\text{tot}} \phi \simeq M_{\text{tot}} [3 k_b T_x / (\mu m_p)]$ changes the above superlinear scaling into a quasi-linear mass scaling with $\beta \sim 0.8\text{--}0.9$ (outskirt to galactic scale; not shown). The retrieved BH mass (normalization) is similar to the observed one at the galactic scale, but is overestimated for the outer regions. In other words, $M_{*} \sim M_{\text{tot,g}} \phi / (\eta c^2)$ is a better proxy for BH mass than purely $M_{\text{tot,g}}$.

3.2.6. Gas Fraction

Now that we have M_{tot} , it is possible to analyze the gas fraction, which is the ratio between the gas mass and total mass, within the three enclosed radii, $f_{\text{gas}} = M_{\text{gas}} / M_{\text{tot}}$. Figure 9 shows that the inclusion of total mass weakens the likely more fundamental correlation with M_{gas} . The core region

⁴⁶ We note that as our sample extends down to isolated/low-mass galaxies, our scaling relations show a larger departure from self-similarity than those solely including massive ETGs and clusters (e.g., Vikhlinin et al. 2009; see also Appendix A).

(where radiative cooling plays a key role) still preserves a low intrinsic scatter (≈ 0.25 dex), with the two enclosing regions showing 35% larger ϵ . We note that the propagated errors have now become substantial, given that f_{gas} is a highly composite variable. Remarkably, the slope is consistent with unity (considering 1σ uncertainty), which allows for a straightforward linear-space conversion between gas fractions and BH masses.

Overall, it is evident that larger BHs prefer to grow in halos that host larger amounts—both in absolute and relative senses—of diffuse gas, despite this being only a small fraction of the whole matter budget. Indeed, the retrieved core gas fraction for galaxies/groups hosting a few $10^9 M_{\odot}$ BHs is a few percent (consistent with Sun et al. 2009; Babyk et al. 2018). Such fractions tend to approach the cosmic baryon fraction (~ 0.1) when we consider the R_{500} of the cluster halo and the most massive BCGs (e.g., NGC 4889, NGC 3842; see also Eckert et al. 2019). In this regime, feedback processes cannot easily evacuate the gas mass due to the large binding energy (Gaspari et al. 2014). Conversely, the inner galactic/CGM region (strongly affected by AGN and stellar feedback) show values below the percent level (e.g., as found by Humphrey et al. 2008, 2009), in particular for isolated galaxies, thus requiring deeper and more challenging observations.

Moving forward, it will be crucial to obtain observations via X-ray telescopes with significantly improved sensitivity and resolution, for both imaging and spectroscopy, to test the faintest hot halos at the low-mass end and thus extending the sample to more late-type objects. A series of dedicated X-ray missions with such characteristics will operate in the upcoming decade, such as *eROSITA*, *XRISM*, *Athena*, and possibly *AXIS* and *Lynx* (see Section 4.4 for more details on future developments).

3.3. Multivariate Correlations

A further key investigation angle that is worth dissecting is the Bayesian multivariate correlation analysis (Section 2.2) of the fundamental X-ray/optical variables. We limit the analysis here to a three-dimensional (3D) space, i.e., a correlation plane (with thickness given by ϵ) with some inclination and position angle. In principle, higher-dimensional hyperplanes can be explored; however, the free parameters also increase substantially, thus diminishing the physical and predicting value of the fitting. This is also why the univariate correlations on the composite variables are in general preferred, given that the composite variables are set by physical intuition, rather than by a statistical random parameter search.

While the Bayesian prior/posterior procedure and MCMC analysis is essentially identical, an important difference with the univariate fitting is that, with `mlinmix` (Equation (8)), we are carrying out a dual *partial* (conditional) correlation analysis, implying that we will retrieve two partial correlation coefficients (related to X_1 via the control variable X_2 , and vice versa). Before dissecting the multivariate relations with BH mass, it is essential to first analyze the “fundamental” planes in the optical and X-ray bands, in order to understand the major differences between the stellar and hot halos, and in which kind of environment the SMBHs reside and grow. Such planes are also crucial probes for competing evolution models of galaxies, groups, and clusters of galaxies.

3.3.1. Optical/Stellar Fundamental Plane (oFP)

A key motivation to analyze multivariate correlations resides in the virial theorem (VT): a stationary system of particles bound by gravity is expected to have an average kinetic energy \mathcal{T} directly related to the average gravitational potential energy U such that

$$2\langle \mathcal{T} \rangle = -\langle U \rangle. \quad (16)$$

For a virialized stellar system with $\sigma_{\text{e,tot}}^2 = 3 \sigma_{\text{e}}^2$, we can write

$$\sigma_{\text{e}}^2 = \frac{\kappa}{3} \frac{GM_{*}(<R_{\text{e}})}{R_{\text{e}}} \propto \frac{L_K}{R_{\text{e}}}, \quad (17)$$

where $\kappa/3 \approx 0.1\text{--}0.3$ ⁴⁷ is a structural parameter, and the second conversion mainly depends on the stellar mass-to-light ratio M_{*}/L_K (note that within R_{e} the stellar mass dominates over the other mass components). It is important to note that the optical observables are only proxies for the intrinsic VT properties; the existence of an optical fundamental plane (oFP) among galaxies requires also significant (structural and dynamical) homology and tight M_{*}/L_K (e.g., Ciotti 1997 and references within).

Figure 10 shows the edge-on view of the best-fit plane correlating (in logarithmic space) the three key stellar observables $\sigma_{\text{e}}^2 - L_K - R_{\text{e}}$. Because the virial theorem is centrally important, in this section we will adopt the velocity variance instead of the velocity dispersion. Note that the plot abscissa implies a rotation about the Y axis, given by the two nonzero slopes. As is customary, the error bars are obtained by propagating the single errors weighted by β_1 and β_2 . The top-left inset lists the mean and standard deviation of all the posterior distributions of the Bayesian `mlinmix` analysis (Equation (8)).

Two are the key results. First, the measured multivariate optical properties are consistent with the VT prediction of a plane, as both β_1 and β_2 slopes have identical value but opposite signs. Second, the intrinsic scatter is very small ($\epsilon \simeq 0.1$ dex). If we consider only the univariate correlations, the scatter increases up to $3\times$ and the corr coefficient decreases to the weak regime (as for the size versus velocity variance; Figure 24); some of these univariate scalings indeed represent highly inclined projections of the best-fit oFP. In more detail, the multivariate result indicates that, over our whole sample, the virial relation $\sigma_{\text{e}}^2 \propto L_K/R_{\text{e}}$ holds tightly but with a mild tilt (1.4) in the slope, which departs from unity (below 2 standard deviations). The pcorr coefficients (0.9) further reflect the very strong positive/negative partial correlation related to L_K and R_{e} , respectively. On the other hand, propagated error bars can reach relatively large uncertainty for lower mass galaxies.

The thin oFP is a well-known property, in particular for ETGs (e.g., Djorgovski & Davis 1987; Dressler et al. 1987). The tilt in the observed plane can mainly be attributed to the dependence of the stellar mass-to-light ratio on the velocity dispersion, $M_{*}/L_K \propto \sigma_{\text{e}}^{0.3\text{--}0.4}$ (Kormendy & Ho 2013). Further minor variations are due to DM, nonhomology, and projection effects (see van den Bosch 2016). Applying our stellar mass-to-light conversion (Equation (1)), we find a univariate correlation $\sigma_{\text{e}}^2 = (0.20 \pm 0.02)(GM_{*}/R_{\text{e}})^{1.16 \pm 0.11}$, which is close to Equation (17) with $\kappa \sim 3/5$.

⁴⁷ The normalization factor of the potential energy is tied to the detailed geometry of the particle spatial distribution; e.g., for a sphere with uniform density, $\kappa = 3/5$.

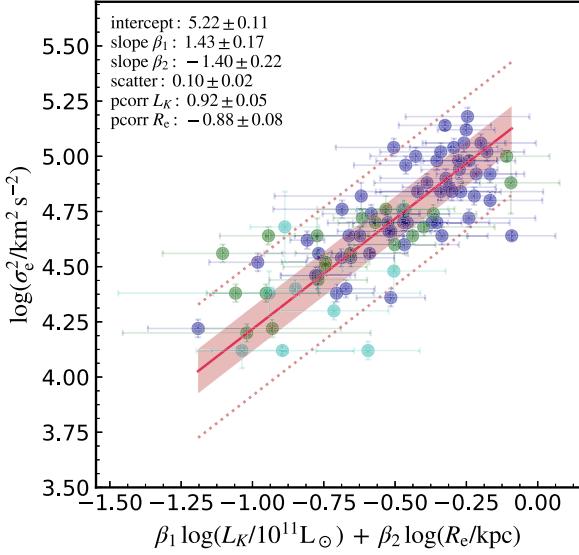


Figure 10. Optical/stellar fundamental plane (edge-on view): multivariate correlation between the stellar velocity variance, total K -band luminosity, and effective radius. The inset lists the mean and errors of all the posteriors from the `mlinmix` analysis, including the intercept, slope, intrinsic scatter (1σ interval plotted as a filled red band, 3σ as dotted lines), and the two partial correlation coefficients. The points are color-coded as per morphological type (blue: E; green: S0; cyan: S). The retrieved galactic oFP can be understood via the VT (Equation (17)) plus quasi homology and a mild tilt due to M_*/L_K , as supported by the strong correlation between σ_e^2 and L_K/R_e and the very tight scatter.

Overall, the optical scalings can be filtered down to a single key variable, σ_e^2 , or its virial analog L_K/R_e . Using M_{bulge} instead of L_K would show similar results (Figure 25), although with significantly larger scatter due to the larger presence of disk-dominated galaxies at the low-mass end. In Appendix A, we include additional variants of the oFP, which may be of interest for other observational and theoretical studies.

3.3.2. X-Ray/Plasma Fundamental Plane (xFP)

We now dissect the X-ray fundamental plane (xFP) of hot halos, testing if the virial relation manifests so evidently in the plasma atmosphere too. This plane should not be confused with the AGN X-ray fundamental plane (Merloni et al. 2003), which focuses on the *nuclear* X-ray luminosity of the central point source, instead of the ISM/IGM/ICM L_x and T_x . The analog of the virial relation (Equation (17)) for a thermal plasma can be retrieved by using the specific thermal energy for the average kinetic energy such that

$$c_{s,i}^2 \equiv \frac{k_b T_x}{\mu m_p} = \frac{\kappa}{3} \frac{GM_{\text{tot}}(<R_x)}{R_x} \propto \frac{L_x}{R_x}, \quad (18)$$

where the first term is the gas isothermal sound speed. Since X-ray halos cover more extended regions than the stellar R_e (Figure 24), the probed total mass is no longer dominated by the stellar component, but by the DM. Interestingly, the hydrostatic equilibrium equation (neglecting the nonthermal pressure support term) is

$$\frac{GM_{\text{tot}}(<R_x)}{R_x} = -c_{s,i}^2 \left(\frac{d \ln n_e}{d \ln r} + \frac{d \ln T_x}{d \ln r} \right), \quad (19)$$

which is akin to a virial relation with the normalization κ given by the gas density and temperature log slopes.⁴⁸

Figure 11 shows the edge-on view of the $T_x - L_x - R_x$ best-fit plane. As for the optical properties, introducing a multivariate fitting substantially reduces the intrinsic scatter, showing a notable $\epsilon \approx 0.1$ dex for both the galactic (top) and macro-scale core region (middle panel). At variance with the oFP, the $\beta_{1,2}$ slopes are significantly different and much shallower than for a VT relation. The β_2 slope is also consistent with null (within 1–2 standard deviations), meaning that the multivariate correlation reduces to the simple $L_x - T_x$ relation. If we inspect pcorr, the conditional correlation is strongest for L_x , for both the galactic and macro scale. We note that this is different from the univariate, nonconditional analysis, which indicates that the characteristic radii positively correlate with L_x or T_x (corr ≈ 0.7 –0.8, $\epsilon \approx 0.2$ dex; e.g., Figure 24). Adopting the intensity $I_x = L_x/(4\pi R_x^2)$ better equilibrates the pcorr coefficients and lowers the scatter (bottom panel).

The xFP deviates significantly from the simple virial expectation, $L_x \propto T_x R_x$ (Equation (18); also called “self-similarity” in cluster studies, modulo the cooling function $L_x \propto T_x R_x \Lambda$). While stars are strongly collisionless systems solely driven by gravitational effects, the plasma halos are complex systems shaped also by thermodynamical processes (e.g., radiative cooling and feedback heating) as well as hydrodynamical/collisional features (e.g., turbulence, shocks, Kelvin–Helmholtz and Rayleigh–Taylor instabilities). Indeed, on top of the virialization process within the DM halo, the hot halos continuously experience multiphase condensation and feedback heating (from both stars and AGN; e.g., Gaspari et al. 2014, 2017), which evacuate and induce circulation throughout the macro atmosphere. The evacuation process is particularly important to reduce the density and thus the X-ray emission ($\propto n^2$) in less bound objects, ultimately leading to $L_x \propto T_x^{4.5}$ (Figure 22). This observed steep scaling is consistent with other studies extending the luminosity–temperature relation down to low-mass and satellite galaxies (Diehl & Statler 2005; Kim & Fabbiano 2013, 2015; Goulding et al. 2016; Babyk et al. 2018).

We can investigate in more detail the main reason for the difference between the oFP and xFP. Is the characteristic radius scaling the main culprit? If we analyze the univariate $R_e - \sigma_e^2$ (Figure 24), the optical log slope is 0.6 ± 0.1 , which is consistent with the X-ray slope of $R_{x,c} - T_{x,c}$ (0.7 ± 0.1). The culprit is mainly the major difference between the optical and X-ray mass-to-light ratios. The optical M_*/L_K shows only very minor variations as a function of optical “temperature” ($T_* \propto \sigma_e^2$), with a log slope ≈ 0.2 (Equation (1)). The observed⁴⁹ X-ray counterpart instead shows a steep anticorrelation with X-ray temperature, $M_{\text{tot}}/L_x \propto T_x^{-3}$ (Figure 23). There are crucial differences between the X-ray and stellar emission. First, while L_K is essentially the sum of many blackbody spectra with a given stellar age and metallicity, L_x is instead given by plasma collisional ionization processes ($\propto n_e n_i \Lambda(T_x, Z)$; Section 3.2.1). In addition, the abovementioned heating processes break self-similarity, introducing a steep dependency between f_{gas} and halo mass (which otherwise would remain constant; Figure 9 and Sun 2012). In sum, the observed fundamental planes are a composition of more than three VT

⁴⁸ Typical large-scale gradients observed in groups/clusters give reasonable consistency between Equations (18) and (19) normalizations.

⁴⁹ Assuming simple cluster self-similarity, the predicted X-ray mass-to-light ratio would be $M_{\text{tot}}/L_x \propto T_x^{-1/2}$.

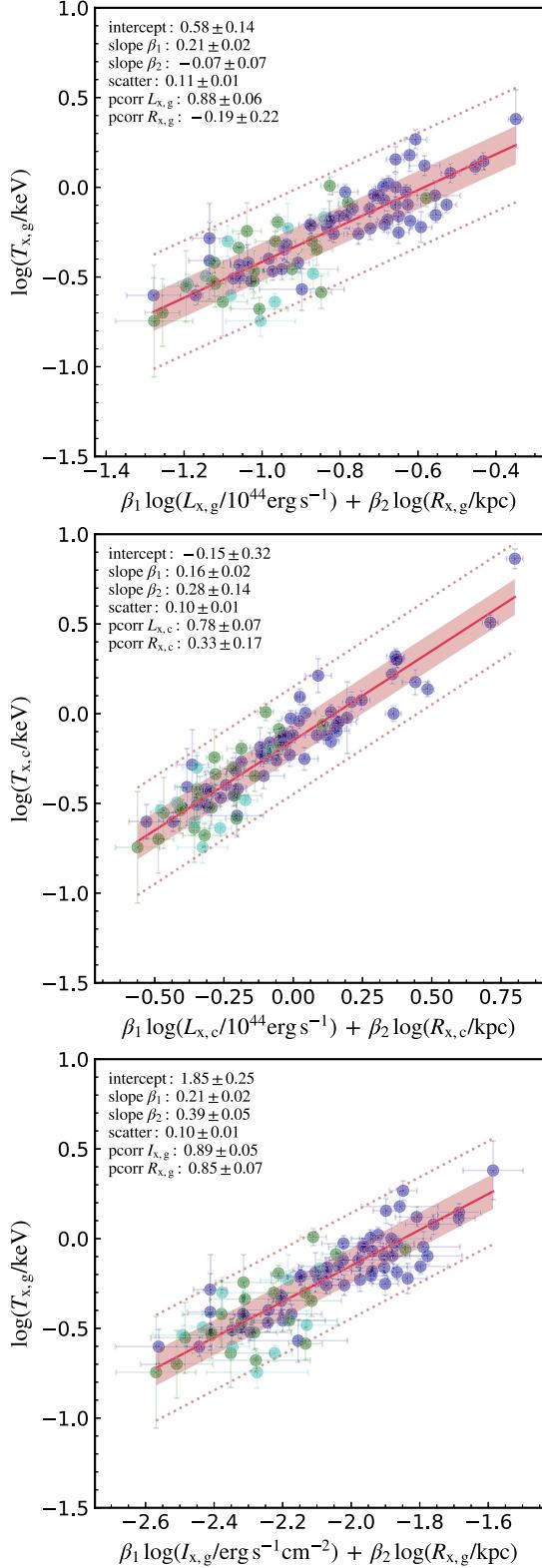


Figure 11. X-ray/plasma fundamental plane (edge-on view): multivariate correlation between the X-ray temperature, luminosity, and characteristic radius, for the galactic (top) and core region (middle). The bottom panel shows the galactic X-ray intensity scaling. The R_{500} scaling is not shown, because R_{500} is redundant with $T_{x,c}$. The xFP substantially reduces the intrinsic scatter, but shows a dominant correlation with L_x , departing from the VT expectation. Unlike the oFP, the xFP is shaped by thermo- and hydrodynamical collisional processes rather than experiencing a pure virialization.

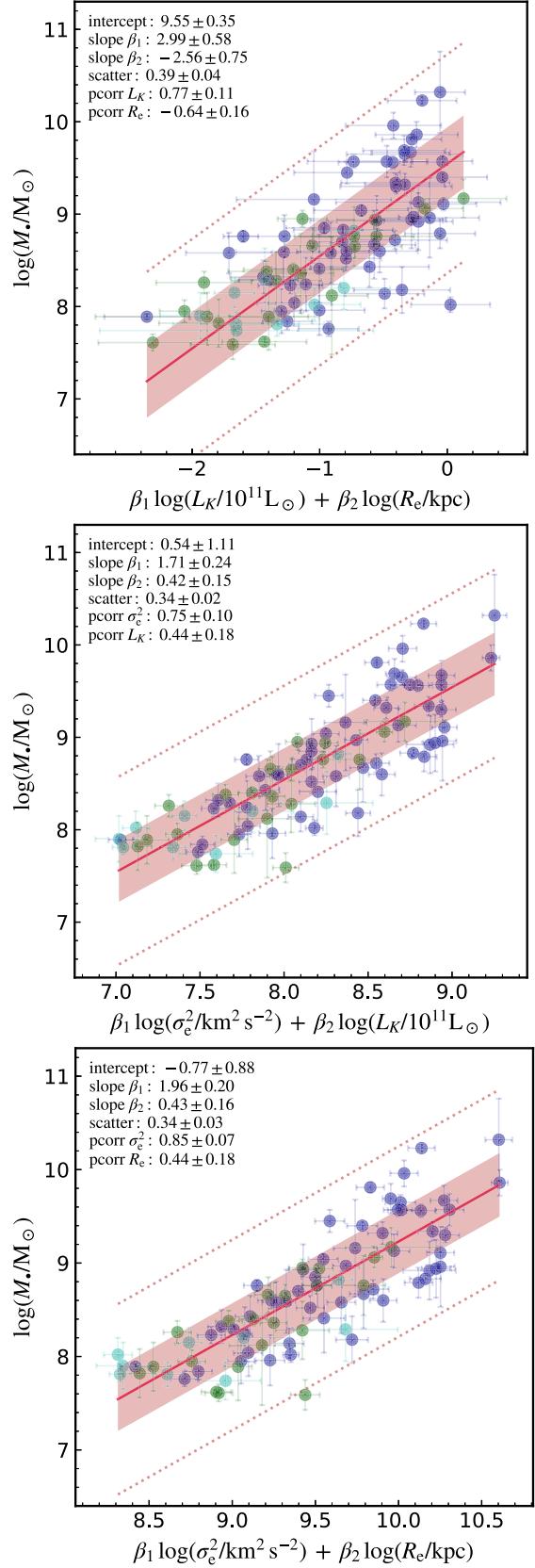


Figure 12. BH mass vs. dual properties of the oFP (edge-on view), permutating the stellar luminosity, size, and velocity variance. Analog of Figure 10. The $M - \sigma_e$ can be directly converted into the $M - L_K/R_e$, given the tightness of the oFP, which follows very well the virial prediction.

variables, including a mass-to-light ratio, such as

$$\frac{L}{R} \propto \frac{T}{(M/L)} \propto T_*^{0.8} \text{ (stellar)} \mid T_x^4 \text{ (gas)}, \quad (20)$$

i.e., while galaxies with larger stellar velocity dispersion emit less optical light relative to mass, hotter plasma halos emit increasingly more X-ray photons. Since the shallow X-ray radius scaling is swamped by the stronger $(M_x/L_x) - T_x$ correlation, the observed xFP tends to closely approach the $L_x - T_x$ projection (Figure 11). Aggravating the difference is the several times larger intrinsic scatter of the X-ray (Figure 23) versus optical (~ 0.1 dex) mass-to-light ratio, which can be interpreted as a form of nonhomology.

Recently, Fujita et al. (2018) showed a variant of the xFP for 20 massive clusters ($M_{\text{tot,vir}} \gtrsim 10^{15} M_\odot$; $T_{x,\text{vir}} \gtrsim 8$ keV) by analyzing lensing masses. While their mass/temperature range is far beyond that of our sample, it is interesting to note that they also find a tight (0.05 dex) xFP, involving $T_x - R_s - M_s$ (where M_s is the mass within the NFW scale radius R_s ; Equation (14)). The significant thinness of the xFP is analogous to that in our Figure 11, albeit 2× larger, likely due to the inclusion of galactic X-ray halos. Their plane substantially deviates from the simple virial expectation too, although it is unfeasible to compare absolute values, given the different observables and the more pronounced self-similarity break of low-mass systems via nongravitational processes.

3.3.3. Black Hole Mass versus oFP

We are now able to test the role of the SMBH mass in relation to the oFP and xFP. Figure 12 shows M_\bullet versus at least two of the oFP variables, with the usual posterior results of the Bayesian `mlinmix` analysis. The top panel shows that the BH mass-luminosity-size in the optical band is essentially equivalent to the $M_\bullet - \sigma_e$ relation (Figure 3; see also Beifiori et al. 2012; van den Bosch 2016). Both have scatter consistent within 1 σ . As for the oFP (Section 3.3.1), the stellar luminosity/size shows pcorr strongly correlated/anti-correlated, with $\beta_{1,2}$ slopes being specular at a value of approximately ± 3 . Indeed using the oFP, $M_\bullet \propto (\sigma_e^2)^{2.2} \propto [(L_K/R_e)^{1.4}]^{2.2} \propto (L_K/R_e)^3$, as retrieved here. Overall, given the tight correlation between stellar velocity variance and L_K/R_e , we can on average convert from one to the other, making stellar “temperature” the unique fundamental variable for the optical component.

The middle and bottom panels show instead the multivariate correlations between M_\bullet and the other two combinations of optical variables. Given the always higher pcorr (0.8 versus 0.4) and steeper $\beta_1 > \beta_2$, it is clear that the dominant variable is σ_e^2 . However, compared with the L_K/R_e correlation, the scatter is reduced slightly, even below that of the $M_\bullet - \sigma_e$. The major improvement is in comparison with the univariate $M_\bullet - L_K$ (Figure 3), reducing its scatter by 30%. By using the bulge mass instead of L_K , similar results would apply (Figure 26). Overall, this shows that the multivariate optical correlations can improve the scatter, although only by a mild amount, and yet not below the level of most X-ray correlations.

3.3.4. Black Hole Mass versus xFP

Figure 13 shows the BH mass as a function of two other fundamental X-ray properties, varying between luminosity, temperature, and size, for the core region (the galactic region

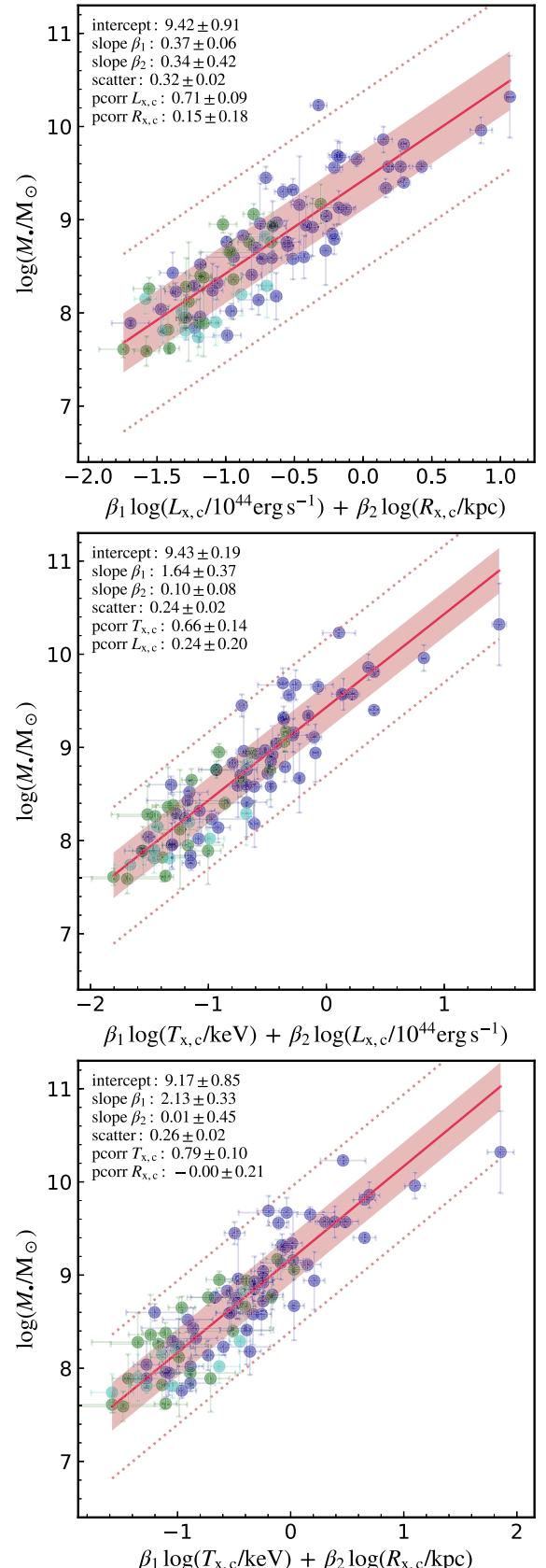


Figure 13. BH mass vs. dual properties of the xFP (edge-on view), permuting the X-ray luminosity, size, and temperature for the core region. Analog of Figure 10. The multivariate fitting on the X-ray properties does not significantly reduce the intrinsic ϵ , although it remains lower than for the optical counterparts.

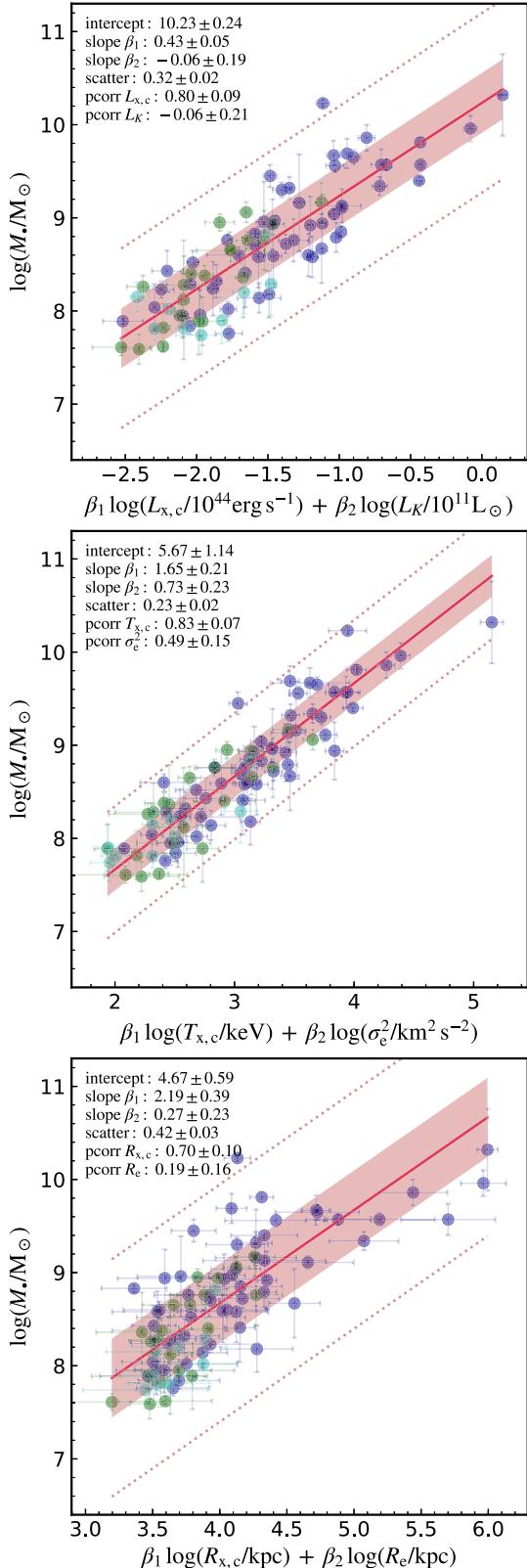


Figure 14. BH mass vs. counterpart properties of the xFP and oFP, including luminosities, temperatures, and sizes. Analog of Figure 10. In all cases, the X-ray properties are more deeply linked to the BH mass, with dominant partial correlation coefficients. Similar results apply considering the X-ray galactic region (not shown).

leads to similar results; Figure 27). In all cases, the scatter remains on an almost identical level compared with the X-ray univariate correlations. When the size is involved (top and

bottom panels), the L_x or T_x always dominates the pcorr coefficient. Indeed, as discussed in Section 3.3.2, the xFP is mostly driven by $L_x - T_x$ (and related plasma processes). The thinnest plane involving the SMBH mass is achieved with $M_* - T_x - L_x$ (middle panel). The intrinsic scatter is significantly below any other optical multivariate scaling (Section 3.3.3).

Looking at the slopes, temperature displays the largest values. A drawback of the multivariate fitting is that it tries to statistically optimize the parameters, regardless of a potential physical meaning (this becomes progressively more severe with increasing number of dimensions). For example, the linear slopes retrieved for $M_* - T_{x,c} - L_{x,c}$ are polar opposites, $\beta_1 \simeq 1.6$ and $\beta_2 \simeq 0.1$; combining $T_x^{3/2}$ and $L_x^{1/10}$ does not lead to any evident thermodynamic property. Inspecting all the univariate scalings as a function of temperature, the closer composite variables are $f_{\text{gas},c}$ and R_{cond} (Section 4.1.2), which uncoincidentally are among the properties with the lowest scatter. On a similar note, the normalization values do not evidently relate to physical constants. By investigating the alternative $M_* - I_x - T_x$ scaling (not shown), we find again that temperature dominates the partial correlations, for all the considered regions.

Overall, the fact that $\beta_1 \gg \beta_2$ and $\text{pcorr}_1 \gg \text{pcorr}_2$ implies that the X-ray univariate fitting is minimally sufficient and better physically motivated. The tightness and simplicity of the xFP suggest that we can adopt either T_x or L_x as the key driver for the black hole mass growth, in a more confident way than the optical counterparts. To better quantify the last statement, we show in Figure 14 the multivariate scalings (for the core region) between the xFP and specular oFP variable. While these planes are not significantly tighter than the pure $M_* - xFP$ scalings, they are instructive in showing how, in all cases, the X-ray property has a much deeper link to the SMBH mass ($\text{pcorr}_1 \gg \text{pcorr}_2$), even when σ_e is involved, which is the key driver of the oFP (middle panel). Nevertheless, while the univariate scalings (Section 3.1) lead to a minimal and tighter interpretation (from the statistical and physical point of view), the presented multivariate (pure or mixed) scalings are additional stringent tests for theoretical/numerical models, which need to be passed to achieve a full theory of coevolving stars, diffuse gas, and SMBHs in galaxies and groups of galaxies.

4. Discussion—Physical Interpretation

In Section 3, we focused on the observed statistical correlations and comparison between X-ray and optical properties, at face value. Here, we discuss potential physical interpretations, caveats, and future developments.

4.1. Testing SMBH Growth Mechanisms

By now, it is clear that the X-ray gaseous atmospheres play some relevant role in the growth of SMBHs. The models concerning the feeding of SMBHs arising from macro-scale properties⁵⁰ can be grouped into two major categories, hot/smooth plasma accretion (Section 4.1.1) versus cold/chaotic gas accretion (Section 4.1.2), which show different correlations

⁵⁰ Since we are not probing relations with the AGN luminosity and given that we are concerned with the integrated BH mass over long timescales, accretion models dealing with the microscale of a few $10 R_S$ are beyond the scope of this work (see also Section 4.1.2).

between M_\bullet and X-ray properties. Binary SMBH mergers are a third viable growth channel, which we probe in Section 4.1.4.

4.1.1. Hot Gas Accretion

The majority of hot accretion models are directly (or indirectly) based on the seminal work led by Bondi (1952). In a spherically symmetric, steady, and adiabatic gaseous atmosphere, the equations of hydrodynamics reduce to a simple formula for the accretion rate onto the central compact object (as per classical Bondi 1952):

$$\dot{M}_B = \lambda 4\pi (GM_\bullet)^2 \frac{\rho_\infty}{c_{s,\infty}^3}, \quad (21)$$

where $\lambda(\gamma)$ is a normalization factor of order unity ($\lambda(5/3) = 1/4$), and with the gas density and adiabatic sound speed, $c_s^2 = \gamma c_{s,i}^2 = \gamma k_b T_x / (\mu m_p)$, taken at large radii from the accretor, $r_\infty \gg r_B \equiv GM_\bullet / c_s^2$. The first drawback of the Bondi rate is that, as absolute value, it produces a very low accretion rate. Even assuming a fully formed SMBH for a median 1 keV galaxy, then $\dot{M}_B \sim 10^{-4} M_\odot \text{ yr}^{-1}$, i.e., a maximal accretion for 10 Gyr would grow the BH only by $10^6 M_\odot$. The inclusion of additional physics breaking the steady-state assumption (e.g., turbulence), spherical geometry (e.g., rotation), or adiabaticity (e.g., nonthermal support via radiation or magnetic fields), each leads to a further suppressed Bondi rate by over 1 order of magnitude (Proga & Begelman 2003; Park & Ricotti 2012; Gaspari et al. 2013, 2015; Ciotti & Pellegrini 2017). Similar low/suppressed values apply to analogous hot accretion models, such as ADAF (advection dominated accretion flow) and related variants (e.g., Narayan & Fabian 2011). A key property characterizes all hot, single-phase models: in order to accrete, the flow has to overcome the large thermal pressure support of the hot halo that strongly counterbalances (with negative radial gradient) the gravitational pull of the SMBH, galaxy, and cluster core. Equation (21) is thus a firm upper limit for hot gas accretion models.

The last term in Equation (21) is the key dependency tied to the hot X-ray halo. Combining the plasma density and sound speed, it can be rewritten as a steep inverse function of plasma entropy:

$$\dot{M}_B = \lambda 4\pi (GM_\bullet)^2 \frac{(\mu m_p)^{5/2}}{\gamma^{3/2}} K_{x,\infty}^{-3/2}, \quad (22)$$

where the X-ray plasma entropy (related to the thermodynamic entropy as $S \propto \ln K$) is defined as

$$K_x \equiv \frac{k_b T_x}{n^{\gamma-1}} = \frac{k_b T_x}{n^{2/3}}. \quad (23)$$

Figure 15 shows the BH mass versus the gas scaling of the Bondi rate (i.e., the plasma entropy⁵¹ for a nonrelativistic gas with $\gamma = 5/3$). It is evident that the SMBH mass does not correlate well with the plasma entropy (thus hot-mode accretion), adopting any radial bin. All the corr coefficients reside in the absent or weak regime, even within the 1σ level. The scatter is one of the largest reported in this study, $\epsilon \sim 0.6$ dex, which is 3× that of the tightest X-ray relations,

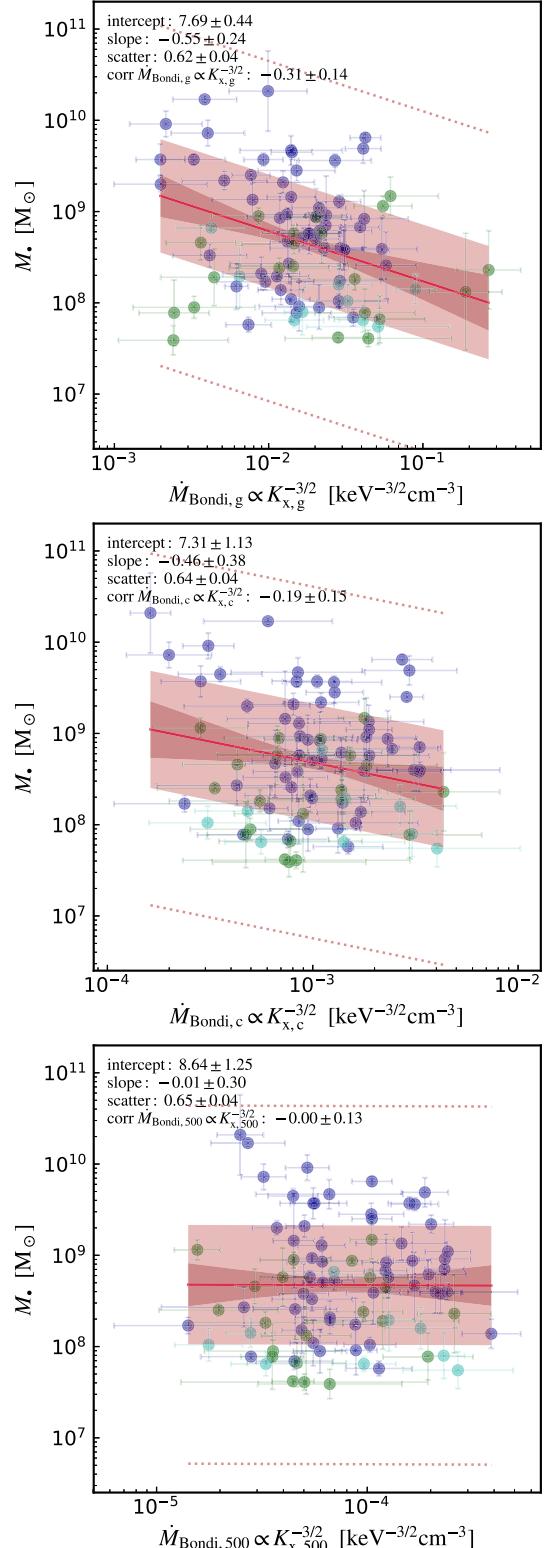


Figure 15. BH mass vs. hot halo scaling (X-ray plasma entropy) of the Bondi rate for the CGM scale (top), group/cluster core (middle), and R_{500} (bottom). The black hole mass poorly correlates with the Bondi rate ($\propto K_x^{-3/2}$; Section 4.1.1), even showing a weak negative trend. Both the slope and nearly null corr coefficient rule out hot accretion models as major drivers of BH growth.

essentially spanning the entire observed BH mass range within the 3σ channel. Even for the galactic case with mild slope (top), the weak correlation is negative, meaning hotter halos accrete

⁵¹ The M_\bullet^2 dependence is a trivial self-correlation, which is unrelated to the X-ray halo. Equation (24) also shows the key role of entropy.

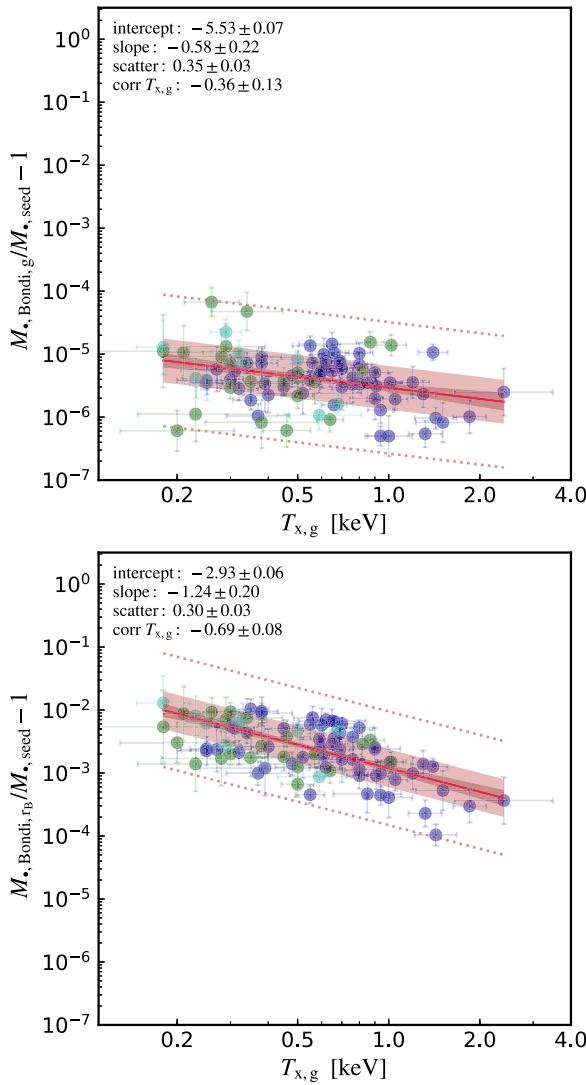


Figure 16. Bondi-driven BH mass growth as a fraction of the high- z seed (Equation (24); $M_{\star,0} = 10^5 M_{\odot}$), adopting as boundary condition the galactic scale (top) and the extrapolation down to the Bondi radius r_B (bottom). During the entire cosmic time, pure Bondi accretion can only grow a tiny percentage of the initial seed ($< 1\%$), proving a minor impact of hot-mode accretion in the evolution of SMBHs.

relatively less gas mass, as stifled by the plasma pressure support (conversely to cold models which condense more heavily in more massive halos; Section 4.1.2).

We can further test whether the integrated Bondi rate is capable of growing an SMBH to the current level throughout the cosmic history of the galaxy, group, or cluster. Integrating Equation (22) (nonlinear ODE), $\int_{t_0}^{t_H} \dot{M}_B dt$, and adopting a decreasing entropy with redshift $K_x(t) = K_{x,\text{now}}(t/t_H)^\theta$, yields

$$M_{\star,B}(t_H) = \frac{M_{\star,0}}{1 - M_{\star,0} K_{x,\text{now}}^{-3/2} A (t_H^{1-3\theta/2} - t_0^{1-3\theta/2})}, \quad (24)$$

with integration constant given by the following: $A \equiv \lambda 4\pi G^2 (\mu m_p)^{5/2} t_H^{3\theta/2} / [\gamma^{3/2} (1-3\theta/2)]$. We note there is no duty cycle for hot-mode accretion, since the diffuse atmosphere cannot be removed and accretion remains continuous. Figure 16 shows the fractional increase of the BH mass given a typical high- z seed of $M_{\star,0} = 10^5 M_{\odot}$ and $\theta = 4/3$ entropy evolution (Voit 2005).

Assuming as boundary condition the galactic scale (top panel), the BH grows only a tiny mass fraction during the cosmic evolution ($t_H - t_0 \simeq 13$ Gyr), and it would worsen by adopting the large-scale $R_{x,c}$ and R_{500} . The bottom panel shows the extrapolation of the Bondi rate down to the inner r_B of each galaxy (< 100 pc) by using the average observed CC entropy profile ($K \propto r^{2/3}$; Panagoulia et al. 2014).⁵² Even under such a best-case scenario the fractional increase reaches 1% and decreases toward the (hotter) BCGs due to the entropy dependence.

Overall, all the above tests rule out (even adopting favorable parameter values) hot-mode accretion as the primary mechanism of SMBH growth. This is consistent with high-resolution hydrodynamical simulations finding hot accretion subdominant compared with cold accretion (e.g., Gaspari et al. 2012b, 2013). Moreover, applying the macro AGN mechanical efficiency ($\eta = 10^{-3}$; Section 3.2.4), the driven kiloparsec-scale jet/outflow power for our median system is $P_{\text{mech}} = \eta \dot{M}_B c^2 \sim 10^{39} \text{ erg s}^{-1}$, several orders of magnitude below the core X-ray cooling luminosity. This implies an inefficient AGN feedback mechanism (see also McNamara et al. 2011; Russell et al. 2013), together with a low-variability behavior inconsistent with most of the observed (X-ray) AGN light curves (e.g., Peterson et al. 2001; LaMassa et al. 2015).

4.1.2. Chaotic Cold Accretion

We test now the other main BH feeding theory, CCA, i.e., the raining of warm optical filaments and cold molecular clouds condensing out of the X-ray atmosphere via nonlinear thermal instability (Section 1). CCA behaves in a different manner from the above hot accretion models, displaying two distinct properties. First, the accretion rates can be boosted intermittently up to several orders of magnitude compared with the Bondi rate, given the recurrent chaotic inelastic collisions between the cold and warm clouds or filaments. Second, CCA displays large variability, with power spectral density described by a flicker noise, as shown by other natural chaotic and fractal processes, including AGN, quasars, meteorological data, and semiconductors (see Gaspari et al. 2017). Moreover, this duty cycle is more frequent toward low-mass systems. In CCA-driven BH growth, the feeding and feedback processes are closely intertwined. While the rain recurrently triggers the AGN down at the horizon scale⁵³ (Sadowski & Gaspari 2017), the AGN feedback quickly responds by injecting back a substantial amount of energy in the form of massive outflows and jets, which deposit their energy at the macro scale, in a gentle self-regulated feedback loop (e.g., Gaspari et al. 2012a, 2012b; Li & Bryan 2014; Barai et al. 2016; Yang & Reynolds 2016b, 2016a; Yang et al. 2019). Such mechanical AGN feedback, on the one hand quenches cooling flows, on the other hand induces over the long term an irreducible level of subsonic turbulence that shapes the halo weather (Lau et al. 2017; Hitomi Collaboration 2018; Simionescu et al. 2019).

While expensive hydrodynamical simulations are required to track the detailed chaotic process (e.g., Gaspari et al. 2013;

⁵² By using the non-CC profile, the entropy would remain flat in the core, with no variation in \dot{M}_B .

⁵³ Once CCA funnels the clouds within ~ 20 Schwarzschild radii ($r_S \equiv 2 G M_{\star} / c^2$; Gaspari et al. 2013), the Maxwell and Reynolds stresses generated via MRI turbulence in the inner torus induce the gas to radially accrete within ~ 10 orbital periods (Sadowski & Gaspari 2017; Jiang et al. 2019), i.e., $10 \times 2\pi [(20 r_S)^3 / G M_{\star}]^{1/2} \sim 2$ yr (for $M_{\star} = 10^9 M_{\odot}$), which is negligible compared with the macro-scale plasma halo timescales.

Prasad et al. 2017), analytic predictions can be retrieved from the macro-scale properties (Gaspari & Sadowski 2017). CCA is tightly linked to the cooling rate of the X-ray plasma:

$$\dot{M}_{\text{cool}} = \frac{q \mu m_p}{(3/2) k_b} \frac{L_x}{T_x}, \quad (25)$$

where $q \approx 10\%$ is the evidence that most pure cooling flows are significantly quenched via AGN feedback (Peterson & Fabian 2006; Gaspari et al. 2012b; McNamara & Nulsen 2012). Since $L_x/T_x \propto t^{-1}$ (Maughan et al. 2012) and accounting for the CCA variability, the integral of Equation (25) over cosmic time ($t_{\text{H}} - t_0 \simeq 13$ Gyr) leads to

$$M_{*,\text{cca}}(t_{\text{H}}) \simeq [\dot{M}_{\text{cool,now}} t_{\text{H}} \ln(t_{\text{H}}/t_0)] \frac{\nu_{\text{cca}}}{\tilde{\nu}_{\text{cca}}}, \quad (26)$$

where the last term is related to the CCA rain active cycle, with a characteristic frequency given by the turbulent eddy turnover frequency (Gaspari et al. 2018), $\nu_{\text{cca}} = (2\pi r^{2/3} L^{1/3} / \sigma_{v,L})^{-1}$ ⁵⁴. Indeed, turbulence is the key physics enabling the generation of significant overdensities in the stratified hot halo, which then nonlinearly condense in multiphase filaments and clouds. By using the ensemble warm-gas single spectra for 72 galaxies in groups and clusters, the above authors show that the (3D) turbulent velocity dispersion is contained in a fairly narrow range, $\sigma_{v,L} \approx 240 \pm 30 \text{ km s}^{-1}$, with a minor halo scaling $\propto (T_x/2 \text{ keV})^{1/3}$. The injection scale L is related to the AGN feedback influence region and can be retrieved from the observed size and distance covered by the pair of inflated AGN bubbles, scaling as $L \approx 10 \text{ kpc} (T_x/1 \text{ keV})^2$ (Shin et al. 2016) and reaching up to 200 kpc for massive clusters (e.g., MS 0735.6+7421). Further, the frequency of the CCA rain increases from massive clusters to low-mass galaxies due to the relatively stronger radiative cooling (Gaspari et al. 2011a, 2012a; Sharma et al. 2012; Prasad et al. 2015). While for low-mass systems the AGN feeding/feedback events are so frequent to be nearly continuous, massive clusters experience longer duty cycles, with powerful AGN outbursts (up to $10^{45} \text{ erg s}^{-1}$) followed by quiescent periods of a few hundred Myr. The last term in Equation (26) models such CCA duty cycle, with normalization $\tilde{\nu}_{\text{cca}}$ taken as the eddy frequency at the low-mass end of the halo distribution ($\tilde{\nu}_{\text{cca}} \approx 0.05 \text{ Myr}^{-1}$). The retrieved median CCA frequency (with 1 rms) over the whole sample is $\log \nu_{\text{cca}}/\text{Myr}^{-1} \simeq -2.1 \pm 0.5$.

The tight correlation between BH mass and X-ray luminosity (Figure 2) already implies an important connection with the plasma cooling (and thus CCA), since its rate \dot{M}_{cool} is a strong function of L_x . At variance with hot-mode accretion models (Section 4.1.1), the CCA driven accretion rate is capable of generating SMBHs, and even UMBHs, over the whole Hubble time. Indeed, for a typical ETG cooling rate of $0.1\text{--}1 M_{\odot} \text{ yr}^{-1}$, steady feeding would imply BHs with $M_* \sim 10^9\text{--}10^{10} M_{\odot}$. While in hot accretion models the hotter the halo the lower the accretion rate, in CCA hotter—thus more luminous—halos drive stronger radiative emissivity and condensation. Similarly, the tight correlations found for $M_* - M_{\text{gas}}$ (Figure 6) and $M_* - f_{\text{gas}}$ (Figure 9), particularly in the core region ($\epsilon \simeq 0.25$), support the key role of the gas mass in feeding the BH. On the other

⁵⁴ We note that for $r > L$, the eddy time reduces to $\propto L/\sigma_{v,L}$, since the injection scale is the maximum driving scale.

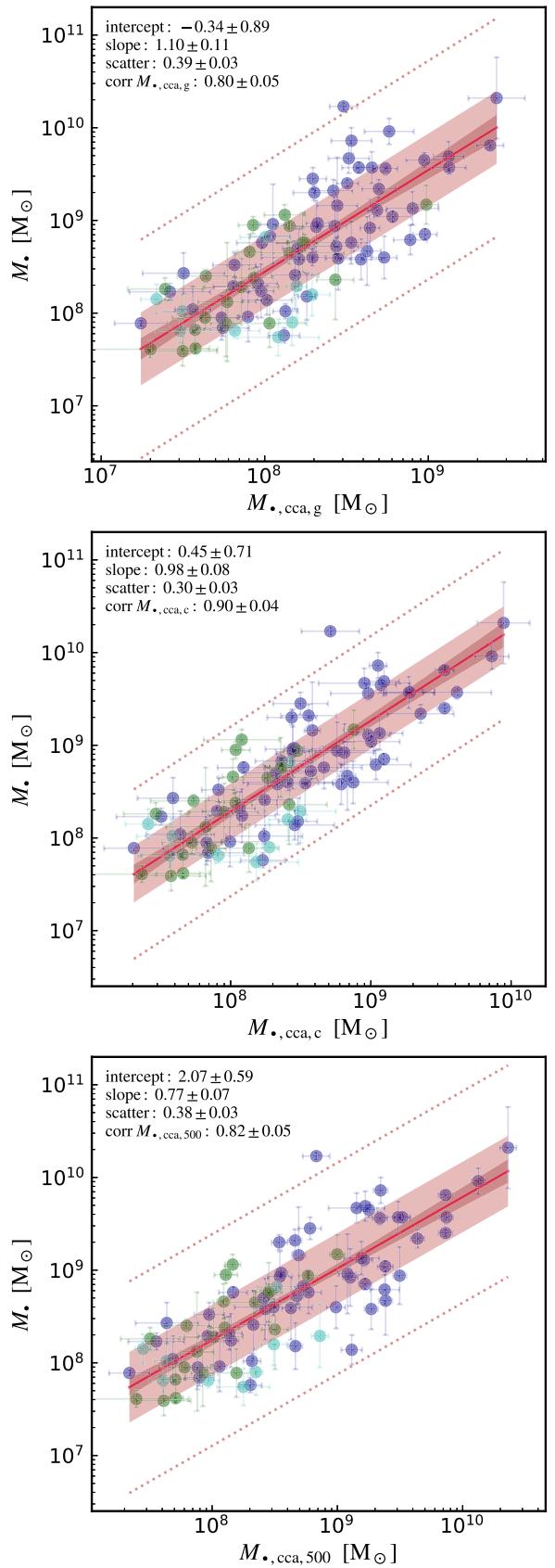


Figure 17. CCA-driven BH mass growth (Equation (26)). The substantial boosting of the accretion rate via CCA (due to the direct link to the halo L_x and related cooling rate, in particular in the core region), coupled with the lower CCA frequency toward more massive halos, leads to a consistent build-up of SMBHs throughout the Hubble time, generating also $10^{10} M_{\odot}$ UMBHs in BCGs.

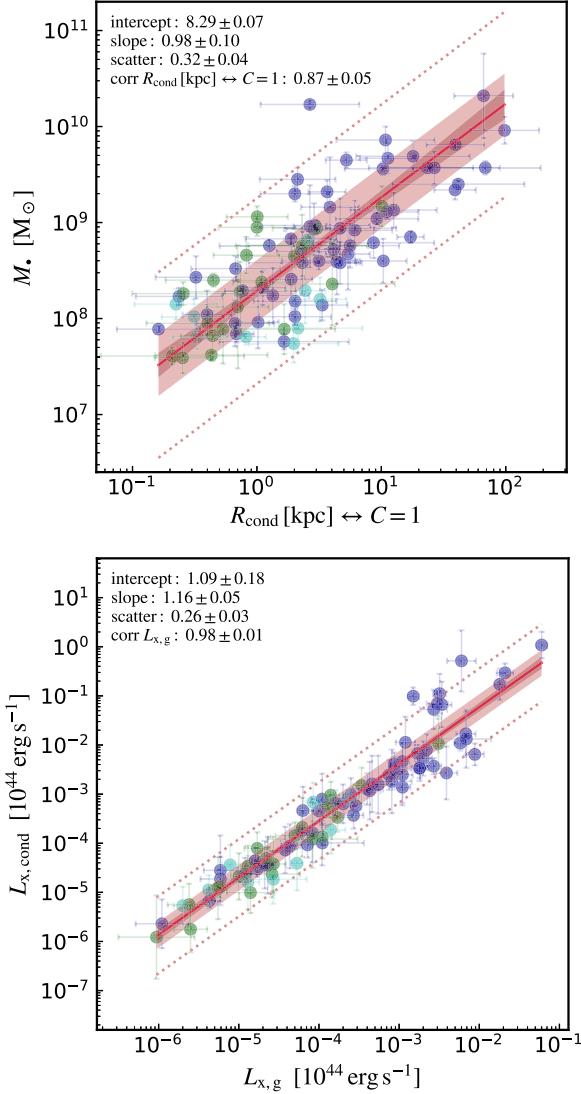


Figure 18. Top: condensation radius for the precipitating warm optical filaments and cold molecular clouds, provided by the C -ratio reaching unity inside the core region. The BH masses are linearly and strongly linked to the condensation region, suggesting a key interplay between CCA and the secular growth of SMBHs. Bottom: X-ray luminosity predicted by the CCA condensation criterion $C \equiv t_{\text{cool}}/t_{\text{eddy}} = 1$ (Equation (29)), compared with the observed galactic X-ray luminosity of the sample. The CCA prediction is consistent with the data over a similar extent radius, supporting the key role of the C -ratio in describing the diffuse gas properties.

hand, the fact that M_* – L_x deviates from a pure linear scaling ($\beta \sim 1/2$) rules out cold accretion models that are perennially turned on over the entire mass range. Indeed, for massive clusters, such a model would generate UMBHs with masses in excess of $10^{11} M_\odot$ during the Hubble time. The intrinsic chaotic variability of CCA, with retrieved lower frequency toward more luminous/extended halos, makes it a compelling model to solve such a hurdle.

Figure 17 shows the quantitative CCA-driven BH mass growth computed via Equation (26) and the X-ray properties of our sample. The best-consistent region to extract the CCA variables (as the cooling rate) is the core region ($\sim 0.1 R_{500}$; middle panel). For the core region, the observed and predicted BH masses match in a linear way within 1σ ($\beta \simeq 0.98$), covering the full range of detected masses from $3 \times 10^7 M_\odot$ to $10^{10} M_\odot$. The intrinsic

scatter is the lowest among the three regions and tight ($\epsilon \simeq 0.30$), with the correlation coefficient in the very strong regime ($\text{corr} \simeq 0.9$). The galactic region instead shows a superlinear slope (top), since the M_* at the high-mass end are underestimated; the correlation is also weaker, displaying 30% larger scatter. Conversely, using the outskirt properties (bottom) leads to an overestimate of the BH masses in BCGs, inducing a too shallow slope; however, the correlation is still in the strong regime. Overall, the X-ray cooling rate initiating from the halo core region and then feeding the central BH appears to be the optimal predictor for the long-term⁵⁵ BH growth. This is further consistent with the core region correlating with the drop in temperature that differentiates CC versus non-CC systems (Vikhlinin et al. 2006; Ghirardini et al. 2019). It is also worth noting that the CCA average Eddington ratio is $\log M_{*,\text{cca},c}/M_{\text{Edd}} = -2.7 \pm 0.4$, i.e., significantly sub-Eddington at the present time (but expected to slowly increase at higher z ; e.g., to -2 at $z \sim 2$), as found by X-ray AGN surveys (e.g., Aird et al. 2018).

Another key property that is worth testing is the CCA condensation radius, R_{cond} . While significant X-ray cooling initiates in the core, the inner region where the condensed ionized ($\text{H}\alpha + [\text{N II}]$) filaments and molecular (CO) clouds end up precipitating is given by R_{cond} , the radius at which the eddy time ($t_{\text{eddy}} = \nu_{\text{cca}}^{-1}$) and cooling time $t_{\text{cool}} \simeq 3 k_b T_x / (n_e \Lambda)$ become comparable, $C \equiv t_{\text{cool}}/t_{\text{eddy}} = 1$ (Gaspari et al. 2018). Given the electron density profile, $n_e(r) = n_{e,c}(r/R_{x,c})^{-a}$ (with median $a \simeq 1.6$ found in Section 3.2.1; see also Hogan et al. 2017; Babyk et al. 2018), a C -ratio of unity translates into

$$R_{\text{cond}} = \left(\frac{3}{2\pi} \frac{k_b T_x}{\Lambda n_{e,c} R_{x,c}^a L^{1/3}} \frac{\sigma_v}{\sigma_v} \right)^{\frac{3}{2-3a}}. \quad (27)$$

Adopting the core properties, the M_* – R_{cond} scaling shown in Figure 18 (top) displays a tight correlation and linear slope ($\epsilon \simeq 0.32$ and $\beta \simeq 0.98$) with corr coefficient in the very strong regime. This corroborates the above result (Figure 17) that the growth of SMBHs is tightly linked to the CCA physics and related multiphase rain occurring in galaxies, groups, and clusters (see also Voit et al. 2015a, 2015b; Soker 2016; Voit 2018). In terms of normalization, ETGs in groups have $R_{\text{cond}} \sim 0.6\text{--}6$ kpc, while typical BCGs have $R_{\text{cond}} \sim 7\text{--}40$ kpc, which is in good agreement with the extent of $\text{H}\alpha$ nebulae observed in low- to high-mass halos (McDonald et al. 2010, 2011; Werner et al. 2014; NGC 5044/A1795 a notable group/cluster with nebular warm gas). Using instead the galactic/ R_{500} variables (not shown) leads to an underestimate/overestimate of the nebular radius by ~ 1 dex; the correlation with M_* is also weaker, with 40% larger scatter, signaling that we are moving away from the main thermally unstable plasma source (the core region).

It is important to note that R_{cond} is a function of predominantly T_x (log slope ~ 2), thus, the tight M_* – T_x correlation found in Figure 1 may be thought of as a reflection of the residual condensed phase recurrently feeding the central BH. This correlation is also linked to the gravitational potential (or R_{500} /total mass): hotter halos have larger gas mass, and thus more vigorous precipitation; in other words, larger, hotter

⁵⁵ The instantaneous accretion rates in one cycle can be quickly estimated via L_x ; the total BH mass requires the integrated cooling rate, which is essentially the raining mass through several cycles.

halos have a more extended raining region (the role of mergers, also affecting the potential, is tested in Section 4.1.4). Conversely, the characteristic radius of Bondi/hot models (Section 4.1.1) is $r_B \propto T_x^{-1}$, i.e., anticorrelated with hotter halos, hence going against the observed positive trend with BH masses, as well as being disconnected from the group/cluster properties (given its size of a couple orders of magnitude smaller than R_{cond}).

We can further test whether the CCA theory can self-consistently predict the $L_x - T_x$ scaling relation based on the C-ratio criterion. As the C-ratio becomes unity, this yields a characteristic electron number density

$$n_{\text{e,cond}} = \frac{3}{2\pi} \frac{k_b T_x}{\Lambda} \frac{\sigma_{v,L}}{r^{2/3} L^{1/3}}. \quad (28)$$

The X-ray luminosity can then be retrieved via the integral shown in Equation (9), adopting $n_{\text{e,cond}}^2$ (Equation (28)) in the emission measure, thus yielding

$$L_{x,\text{cond}} = \frac{27}{5\pi} \frac{(k_b T_x)^2}{\Lambda} \frac{\sigma_{v,L}^2}{L^{2/3}} R_{\text{cond}}^{5/3}, \quad (29)$$

with $\sigma_{v,L}$ and L given by the observational scalings (as a function of T_x) discussed after Equation (25). Figure 18 (bottom) shows the CCA prediction, by using the above R_{cond} in Equation (29), compared with the independently observed $L_{x,g}$, with the condensation radius typically being ± 0.3 dex from the galactic/CGM scale. The match with the observed X-ray luminosity is good, with both normalization and scaling reproduced up to $\sim 10^{42}$ erg s $^{-1}$, above which the scatter increases due to R_{cond} exceeding the CGM region. By extrapolating the density profile, Equation (28) and (29) may be further generalized and applied in observational or theoretical studies to interpret or model the thermodynamic properties of diffuse media at different radii in a (semi)analytic framework. Summarizing, the predictions of CCA in terms of both the hot halo properties and SMBH masses are well in agreement with the analyzed observational data.

4.1.3. Stars

As introduced in Section 3, the tightness of the X-ray temperature/luminosity/gas mass scalings ($\epsilon \sim 0.2\text{--}0.3$), compared with the optical correlations ($\epsilon \sim 0.4\text{--}0.5$) is an indicator that the gaseous atmospheres play a key role in the coevolution of SMBHs. Besides the above quantitative tests, first principles suggest the stellar component is not the main source of fueling. Once rapidly collapsed from the progenitor molecular cloud, stars become collisionless, with negligible dynamical friction to feed the BH (this drag force is proportional to the square of the moving object mass). While SMBHs can efficiently accrete the collisional gas (in particular via chaotic collisions), the stellar component represents the residual, unaccreted mass that is progressively stored in the galactic potential.

The stellar mass is still linked to the gas condensation (hence the $M_{\bullet} - M_{\text{bulge}}$); however, the link with the BH growth is progressively washed out during the recurrent CCA cycles. Taking the potential ($\propto \sigma_{\text{e}}^2$ or $L_{\text{e}}/R_{\text{e}}$) as reference improves the BH mass optical correlations, since the potential is less affected by the baryonic physics. While the stellar component can be well described via the VT and homology (as proven by the

oFP; Section 3.3.1), X-ray halos are primarily affected by thermohydrodynamical processes (as found via the xFP; Section 3.3.2), rather than solely experiencing a virialization in a gravitational potential. The above results (and cosmological simulations in Section 4.1.4) point toward gas accretion and condensation as the dominant mechanism establishing the relations with T_x and L_x , instead of such scalings being a pure passive tracer of the total mass/DM (Bogdán et al. 2018). Needless to say, the secondary connection with the potential will be always present to some degree, as it sets an upper dynamical limit to any gas accretion,⁵⁶ as well as being linked to the hierarchical merger growth—the focus of the next section.

4.1.4. SMBH Mergers

Another potentially important channel for BH growth is the hierarchical merger build-up throughout the cosmological evolution of galaxies and clusters. Let us discuss first a simple statistical approach, and then the more detailed realistic cosmological simulation. In the concordance Λ CDM universe, the first galaxies form after ~ 1 Gyr after the big bang and start to stochastically merge into large-scale structures, such as proto-groups and then proto-clusters. Beyond a scale of tens of kiloparsecs, the hosted SMBHs slowly sink (in a few Gyr) toward the new, merged potential center via dynamical friction onto stars, until the SMBH pair forms a hard binary. At the parsec scale, three-body scattering with nuclear stars leads to the ejection of the stellar bodies and shrinking of the binary orbit to the milliparsec scale, where gravitational-wave radiation drives the final coalescence of the two SMBHs (e.g., Begelman et al. 1980).

It is thus expected that, in a hierarchical universe, SMBH masses and any halo property positively correlate, including those of the X-ray plasma (which is heated up via the virialization shock during the infall in the DM potential). However, the key differentiating point is how well they correlate, in terms of slope and scatter. Idealized SAMs (Peng 2007; Jahnke & Macciò 2011) show that, starting from an uncorrelated random distribution of seeded intermediate BHs, a sequence of mergers will naturally lead to a linear correlation ($\beta = 1$) between SMBH mass and bulge/total mass, being both the results of a large number of summation events, which are independent from any gas feeding/feedback physics. In this “central-limit-theorem” (CLT)⁵⁷ view, the ensemble averaging ensures that the fractional dispersion in both coordinates should decrease with increasing halo mass as $\propto N^{-1/2}$, assuming a very large number of experienced mergers N . Rule of thumb for “large” statistical samples is at least $N = 30$, hence a relative drop of the scatter down to $1/\sqrt{30} \simeq 0.18$.

Figure 3 shows that the $M_{\bullet} - M_{\text{bulge}}$ has a slope below unity ($\beta = 0.90$); the dispersion (from the best fit) for the bottom/top half of the bulge masses is 0.39/0.46 dex, which is inconsistent with the CLT prediction of a decreasing scatter. Figure 8 shows that the $M_{\bullet} - M_{\text{tot}}$ has a slope above unity for all the three main regions ($\beta = 1.2\text{--}1.4$); moreover, the dispersion in the top half

⁵⁶ For an isothermal sphere $\rho_{\text{gas}} = f_{\text{gas}} \sigma_{\text{e}}^2 / (2\pi G r^2)$, the dynamical limit is given by $\dot{M}_{\text{dyn}} = 4\pi \rho_{\text{gas}} r^2 \sigma_{\text{e}} \approx 10^3 \sigma_{\text{e},300} M_{\odot} \text{ yr}^{-1}$ for $f_{\text{gas}} = 0.1$. The cooling rate is much lower than this, as the X-ray halo is not collapsing in freefall. Integration by a timescale $\propto \sigma_{\text{e}}^{1.5}$ would lead to the observed $M_{\bullet} - \sigma_{\text{e}}$ relation (e.g., King 2003).

⁵⁷ We preserve the CLT nomenclature adopted in the astrophysics literature; however, a better term would be to refer to this effect as an attractor in the evolution of a stochastic process.

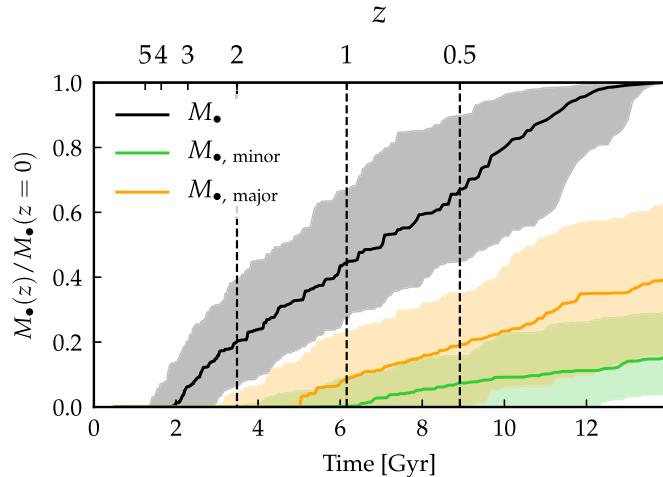


Figure 19. Cosmological hydrodynamical zoom-in simulation of 135 groups/clusters, showing the median and 1σ of the fractional SMBH mass increase during the Hubble time, for central galaxies only. The redshift/linear time is depicted on the top/bottom x -axis. The black line indicates the total SMBH mass (due to gas accretion and mergers), while the orange and green lines show the relative contribution of major and minor mergers (above/below a mass ratio of 1:4), respectively. Even for central galaxies (which experience the largest amount of major mergers; Figure 20), merger-driven BH growth is subdominant over most of the cosmic time and driven by infrequent major mergers.

of the total masses within $R_{x,g}$, $R_{x,c}$, or R_{500} is in all cases $1.1\times$ that in the bottom half, i.e., opposite to the CLT prediction. This is supported by the below-described cosmological simulations (see also Figure 4 in Bassini et al. 2019), which further show that starting from a purely random uncorrelated distribution at large redshift is unrealistic, invalidating the CLT assumption. Analogous nondecreasing dispersion applies to the M – M_{gas} correlations, which also have slopes deviating below unity ($\beta \approx 0.6$). All these results suggest that, while mergers are part of the evolutionary process, they are likely not the overwhelming force in the build-up of the SMBH–X-ray halo scaling relations.

To better quantify the above finding in a more realistic setup, we use state-of-the-art cosmological hydrodynamical simulations with subgrid models for baryon astrophysics, including radiative cooling, star formation, metal enrichment, and stellar/AGN feedback, which well reproduce the observed properties of X-ray hot halos (Rasia et al. 2015; Planelles et al. 2017; Biffi et al. 2018; Bassini et al. 2019 for the simulation setup). Such Lagrangian (SPH) zoom-in simulations of 135 groups/clusters of galaxies ($M_{\text{tot},500} \sim 10^{13}\text{--}10^{15} M_{\odot}$) are particularly useful to track the evolution and merging of the SMBHs (~ 6000 ⁵⁸ hosted by each galaxy, in a large and robust statistical sample. Moreover, the simulations include subgrid modeling for both hot and cold gas accretion, as well as ejective (quasar-mode) and maintenance (radio-mode) AGN feedback (Ragone-Figueroa et al. 2018 for the numerical details). Figure 19 shows the median growth of the SMBH masses (normalized to the final mass) for the central galaxies over the ~ 14 Gyr cosmological evolution (black), involving a combination of (predominantly cold) gas accretion and BH mergers. The orange/green line indicates the contribution of mergers, separating them into major/minor events, defined as having a mass ratio above/below 1:4, respectively. The first key result is that mergers contribute a subdominant fraction of the growing M over most of the

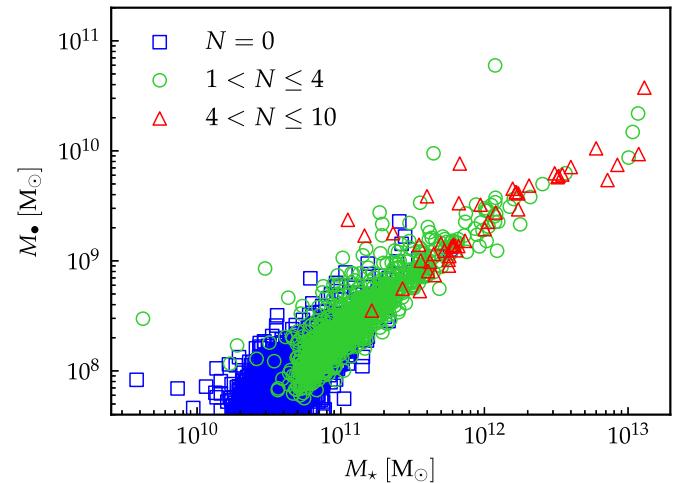


Figure 20. Magorrian relation developed in our cosmological simulation (Section 4.1.4) at $z = 0$, color-coding the number of major ($>1:4$ mass ratio) BH mergers experienced by each final SMBH. It is clear that major mergers are rare events: the majority of objects experience only a few major mergers, while most of the mass is built via gas accretion. Moreover, the dispersion for SMBHs above $10^8 M_{\odot}$ with $N = 0$, $N < 2$, or $N > 2$ remains similar at 0.2 dex.

cosmic evolution; only in the last Gyr they start to catch up with the level of gas accretion. It is important to note that Figure 19 shows the SMBHs solely grown in central galaxies, thus experiencing the largest amount of mergers. As shown below (Figure 20), over 70% of the total BHs do not experience a major merger and are entirely driven by (cold) gas accretion. Indeed, even with no mergers, the seeded BHs (starting at $\sim 10^5 M_{\odot}$) evolve toward the Magorrian relation. Overall, gas accretion is the main channel of SMBH growth for most of the population and over the long-term evolution, even in the best-case merger scenario of massive BCGs.

The second key result from Figure 19 is that infrequent major mergers dominate the BH growth, rather than frequent small substructure accretion. The low rate of major galaxy mergers ($\sim 0.03\text{--}0.5 \text{ Gyr}^{-1}$ for $z \sim 0\text{--}3$; see also Rodriguez-Gomez et al. 2015) means that for each final massive galaxy we expect ~ 2 major events during its evolution. In a similar vein, Figure 20 shows our simulated Magorrian relation at $z = 0$ (for the entire galaxies), with the number of major BH-BH mergers highlighted with different colors for each final object. The SMBHs with a final mass of $\sim 5 \times 10^7$, 5×10^8 , and $5 \times 10^9 M_{\odot}$ have on average experienced 0, 2, and 4 total major mergers (along the full tree), respectively. If we weight each major merger by the fraction of mass contributed to the final SMBH mass, such N values are roughly halved. These results show that binary BH major mergers are rare events, hence breaking down the CLT requirement of a significantly large $N > 30$. Moreover, computing the scatter in the simulated Magorrian relation for the subsample with $N = 0$, $N < 2$, or $N > 2$ leads to very similar dispersions of 0.2 dex, in contrast with the CLT expectation. The above combined results rule out hierarchical BH mergers and related CLT averaging as dominant drivers of the M versus (X-ray) halo scaling relations, making gas accretion the preferred—although not unique—channel. It is also important to point out that 75% of the simulated major mergers contain or bring a significant amount of gas very near the BH (“wet” mergers), meaning that they further enhance the gas accretion channel rather than the pure SMBH binary merging.

⁵⁸ Softening/merging length of the sink particles is $\sim 3 h^{-1} \text{ kpc}$.

We note that another evolutionary formation scenario could be the full growth of SMBHs at very high redshift ($z \gg 3$). However, as shown by our cosmological hydrodynamical simulations (Figure 19), over 99% of the BH mass is built at $z < 3$, since at very early cosmic times mergers are extremely rare and gas accretion is inefficient. Moreover, high-resolution simulations have still major hurdles in achieving the build-up of high- z intermediate BHs with $M_* < 10^5 M_\odot$, e.g., via direct gas collapse or supermassive/Population III stars (e.g., Latif et al. 2013; Luo et al. 2018; Wise et al. 2019), well before the SMBH regime. The handful of SMBHs observed at $z \gtrsim 7$ (e.g., Mortlock et al. 2011) might thus represent the far tail of the random BH population; in addition, such measurements have highly uncertain masses due to the lack of direct dynamical measurements and large systematic errors in the modeling of the broad-line region. Instead of requiring all BHs to accrete at high- z via unrealistically high gas accretion and/or mergers, the models and data suggest a gentler, long-term coevolution of SMBHs (Section 4.1.2) and host galaxies during the entire Hubble time.

4.2. Relic Galaxies, Galactic Coronae, Environment, and Morphology

Interesting astrophysical laboratories for testing the growth of SMBHs are compact relic galaxies, which appear to be the local analogs of high-redshift ($z \sim 2$) “red nuggets”, the progenitors of massive ETGs (e.g., Ferré-Mateu et al. 2017; Werner et al. 2018; Buote & Barth 2019). These compact elliptical galaxies are thought to have formed 13 Gyr ago through early dissipative processes; however, at variance with other ETGs, they managed to randomly avoid the subsequent series of merging events, remaining fairly isolated until $z = 0$ with a passively evolving stellar population. They thus represent a direct probe for pure gas accretion models. Mrk 1216 and NGC 1277 are exemplary cases discovered in the local universe ($D \sim 70$ –90 Mpc) with dynamically detected BH masses (Graham et al. 2016; Walsh et al. 2017). Both compact relic galaxies are among the major outliers in $M_* - R_e$ and $M_* - M_{\text{bulge}}$ (up to 1 dex from the mean relations). Since they have not experienced the slow $z < 3$ nondissipative phase that enlarges the stellar envelopes, their effective radii and bulge masses have remained relatively low, $R_e \sim 1$ –3 kpc and $M_{\text{bulge}} \sim 10^{11} M_\odot$, respectively (see Table 2). On the other hand, such compact galaxies host SMBHs with significant masses ($M_* \sim 1$ –5 $\times 10^9 M_\odot$); indeed, they possess galactic X-ray emitting atmospheres with $T_x \sim 1$ keV. As they have been untouched by mergers for 13 Gyr, the only available source for accretion is the plasma atmosphere. Bondi hot-mode gas accretion drives too low accretion rates (Section 4.1.1). Conversely, CCA mode is directly linked to the X-ray luminosity and can drive substantial accretion rates via the multiphase condensation of cold/warm clouds out of the persistent hot halo (Section 4.1.2) from high to low z , hence leading to the steady growth of BHs up to several $10^9 M_\odot$ at the present time (regardless of the stellar component). Both relic galaxies consistently fit within $\sim 1\sigma$ of the BH mass versus $L_{x,g}$ relation, indistinguishable from other normal ETGs in our sample.

Coronae are another class of dense X-ray atmospheres shrunk to ~ 1 –5 kpc scale. They appear to be ubiquitous in ETGs (Sun et al. 2007). Analogs of the above compact systems, they represent the irreducible hot X-ray atmosphere

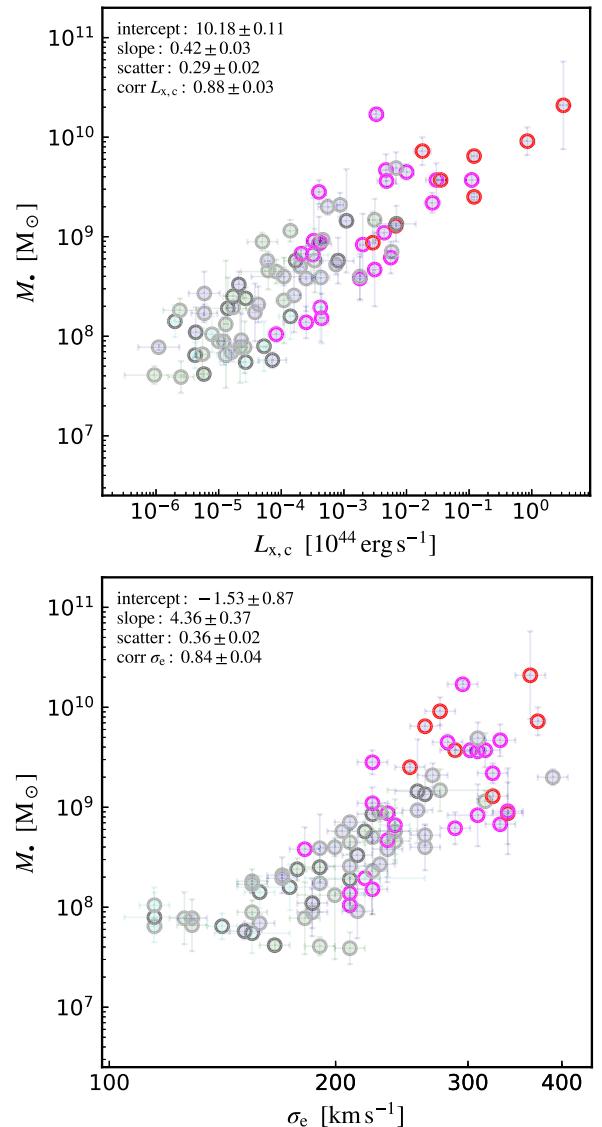


Figure 21. BH mass vs. core X-ray luminosity (top) and stellar velocity dispersion (bottom), differentiating brightest central group/cluster galaxies (BGGs with magenta circles; BCGs in red) and other field or isolated/satellite galaxies (gray; BFGs have bold gray circles). Analog of Figures 2 and 3. More massive SMBHs (e.g., UMBHs) reside at the center of hotter and more luminous clusters and groups (as well as in E types—pale blue). Conversely low-mass BHs tend to be hosted by galaxies in poor environments (correlated with late morphological types, as S0s/spirals—pale green/cyan).

that coevolves with the central SMBH; indeed, the relatively high gas density makes them survive stripping, evaporation, and AGN outflows. Thereby, even central ETGs in non-CC systems or satellites in poor environments can feed the SMBH via the condensation rain stimulated in the corona (for a very long time). Two examples of residual coronae are NGC 4889 and 3842 in the Coma and A1367 non-CC clusters, in which the galactic (corona) temperature seems to provide a better fit than $T_{x,c}$. We note that non-CC systems might have been CCs at higher z , thus experiencing long periods of past macro rain.

Focusing on the environment, Figure 21 (top panel) shows that satellite/isolated galaxies (gray) tend to have both low BH masses and low X-ray luminosity/temperature. Such galaxies are also correlated with late-type galaxies, such as S0s and spirals (with $B/T < 0.5$), mostly being in poor environments

($N_m < 10$). While central galaxies sitting at the bottom of the group/cluster potential can feed from the macro plasma halo, satellite (and merging) galaxies are left to feed from the inner weather/corona, as they move at several 100 km s^{-1} relative to the external weather. If the stripping is, however, substantial, even the corona could be lost leading to undermassive BHs (perhaps the fate of dwarf galaxies as NGC 4486A with $M_* \lesssim 10^7 M_\odot$). Similarly, isolated/field⁵⁹ galaxies are naturally starved of the large-scale gas reservoir. BCGs (red circles) host instead the largest BH masses up to $10^{10} M_\odot$ of UMBHs, while BGGs (magenta) occupy the intermediate $10^9 M_\odot$ SMBH locus (with NGC 1600 as an outlier, likely due to pure stochasticity). About 95% of such BCGs/BGGs are E-type galaxies ($B/T \approx 1$) and essentially all in rich environments ($N_m \sim 10\text{--}500$). The more central the galaxy in a group/cluster potential, the more massive the X-ray halo and the larger the condensation radius (Section 4.1.2), hence, with raining clouds and filaments that can be quickly ($\lesssim 100 \text{ Myr}$) funneled toward the center of the group/cluster from larger BH distances. Conversely, as shown in Section 4.1.4, group/cluster mergers are rare, with the formation of a binary SMBH via dynamical friction onto stars requiring several Gyr.⁶⁰ Adopting instead the optical properties as σ_e (bottom panel) shows that BCGs drive a major scatter and rough upward trend at the high end of the distribution (see also Section 3.1.2); thereby, the large-scale environment plays an important role in the evolution of SMBHs. In other words, the BH physics at the microscale is substantially linked to the macro gaseous atmosphere thermodynamics, thus creating a unified symbiotic system (which may be referred to as “BH weather”) covering over ~ 10 orders of magnitude in spatial (and temporal) scale.

4.3. Scaling Relations as Test/Calibration for Cosmological Simulations

In Section 3, we presented a large set of scalings related to each of the thermodynamic quantities of hot halos, including the X-ray luminosity, temperature, electron density, pressure, thermal energy, and gas/total mass, both as univariate and multivariate correlations. Such a study is vital (i) to advance our observational constraints on the observable universe; (ii) to test/falsify models of BH accretion/growth; (iii) to carefully calibrate and check the predictive power of cosmological simulations. While the first two points have been amply dissected in the previous sections, let us focus on the last one.

Granted the relevant progresses in the past decade, state-of-the-art cosmological simulations still lack substantial resolution to implement all the baryonic physics in a self-consistent manner, thus having to rely on a simplified analytic approach known as “subgrid” modeling (e.g., Sijacki et al. 2007; Rasia et al. 2015; Schaye et al. 2015; Tremmel et al. 2017; Weinberger et al. 2018). This is particularly challenging for AGN feeding/feedback physics as it has to operate on scales spanning 10 dex. Most—if not all—subgrid models tend to calibrate the impact of AGN feedback and related SMBH growth on the optical scalings, in particular the $M_*\text{--}\sigma_e$ or Magorrian relations. However, Sections 3.1.1–3.1.2 show that the optical scalings have significantly larger scatter than the

⁵⁹ Brightest field galaxies (BFGs; bold gray circles) can be considered analog of isolated galaxies, since the other field galaxies typically have a negligible contribution to the hot halo.

⁶⁰ The timescale of BH dynamical friction onto stars is (Combes 2002) $t_{\text{df}} \sim 2.5 \text{ Gyr} (v_{\text{circ}}/300 \text{ km s}^{-1}) (R_e/5 \text{ kpc})^2 (M_*/10^8 M_\odot)$.

X-ray halo properties and tend to steepen at the high-mass end due to UMBHs. As discussed in Section 4.1.2, stars are indeed the final by-product of the top-down multiphase gas condensation that occurs throughout the cosmic time. Instead, the plasma halos are the primordial reservoir out of which the raining matter will feed recurrently the central SMBHs.

It is crucial to calibrate first the AGN feedback/feeding parameters of cosmological simulations on a few selected X-ray halo relations (e.g., $M_*\text{--}T_x$). The next step would be to check the predictions for all other thermodynamic properties (e.g., $M_*\text{--}M_{\text{gas}}$) and/or stellar counterparts. The calibration should be as minimal as possible, in order to avoid overfitting. We note that calibrating first on $M_*\text{--}M_{\text{tot}}$ might lead to a large parameter-space uncertainty; as shown in Section 4.1.4, the total (DM dominated) potential is likely a secondary element of the BH growth, while it is primary to model the hot gas physics first (e.g., galaxies without hot halos appear to show significant decorrelation from BH properties, regardless of DM mass). The dozen scaling relations presented in this paper should allow for multiple independent calibration tests to check the robustness of the subgrid model (see the recent work by Bassini et al. 2019 for such an example). In parallel, subgrid prescriptions should gradually move toward physically motivated—rather than fitting-oriented—models. For example, a minimal subgrid approach based on a realistic AGN raining/outflow self-regulation is provided in Gaspari & Sadowski (2017). Needless to say, the same scaling relations can be readily applied in purely SAMs of galaxy (e.g., Hirschmann et al. 2012) and cluster (e.g., Flender et al. 2017) formation.

4.4. Caveats, Selection Effects, and Future Prospects

Before concluding, it is important to remark the limitations of the current work, selection effects, and expansions worth pursuing in future investigations.

The selection is first done in optical, as it is based on the available direct dynamical BH masses (Section 2). Since optical telescopes have to resolve the BH influence region, this limits our analysis to systems in the local universe ($z < 0.04$). Given the tight coevolution of SMBHs and hot halos retrieved in simulations (e.g., Bassini et al. 2019), we expect the retrieved $M_*\text{--}$ X-ray halo correlations to hold at least up to $z \sim 2$ with similar scatter, albeit with steeper slope given the relatively slower growth of macro-scale cluster halos (Bassini et al. 2019) find a $M_*\text{--}T_x$ slope increase of $2 \times$ from $z = 0$ to 2 .

Regarding the X-ray selection, we only included direct BH masses with X-ray halo detections, except for a handful of contaminated systems (Section 2.1.2). The final sample of 85 systems includes a very diverse mix of morphological, dynamical, and environmental types (Tables 2 and 3), hence we do not expect major biases in these directions. The vast majority of the galaxies with direct BH masses without X-ray detections are low-mass galaxies, which are expected to fall below a halo temperature of 0.2 keV and $M_* < 3 \times 10^7 M_\odot$, i.e., the IMBH regime. This is also related to $L_x < 10^{38} \text{ erg s}^{-1}$, which current X-ray instruments have severe difficulties constraining. Extrapolating the $M_*\text{--}T_x$, these IMBHs should reside in the UV regime (e.g., NGC 2787 and NGC 7582 at 0.18 keV show already signs of being unconstrained in X-rays), which is not sufficiently covered by any current telescope. This IMBH regime corresponds to low-mass galaxies with $M_* < 5 \times 10^9 M_\odot$. Bulgeless disk galaxies have been shown to start to deviate from the mean optical scalings (Kormendy &

Ho 2013), and might present a challenge for those involving hot halos too. Such departures can be due to the low binding energy of small halos and thus higher susceptibility to AGN feedback evacuation. Moreover, low-mass galaxies experience rotation as dominant physics, which changes the formation and frequency of the condensation rain (Gaspari et al. 2015), reducing the accreted gas mass via the stronger centrifugal barrier (as a function of the turbulent Taylor number $T_a \equiv v_{\text{rot}}/\sigma_v$, linked to B/T ; e.g., Juráňová et al. 2019). Overall, given the above effects, we envision an increased scatter and steeper/lower slope/normalization in the correlations including such unprobed low-mass regime. Further, rapid rotation triggers different accretion mechanisms such as disk shearing and bar/ring instabilities (Hopkins & Quataert 2010); it may be thus worthwhile to explore other correlations, as that between M and the spiral-arm pitch angle (Davis et al. 2017).

Another relevant problem moving toward IMBHs and low-mass galaxies/halos is the fact that X-ray binaries (XBs) start to swamp the diffuse hot gas emission. As shown by the stacking of the *ROSAT* X-ray emission of over 250 000 galaxies (Anderson et al. 2015; their Figure 5), at $\log M_*/M_{\odot} < 10.7$, XB dominate the X-ray luminosity. Similarly, X-ray AGN/quasars with high Eddington ratio ($\gtrsim 0.05$) can introduce significant uncertainty in the X-ray halo detection, especially in Seyfert galaxies (conspicuously contaminating AGN can even be hosted in BCG, as in NGC 1275). Active starbursts drive plasma energized via stellar winds and supernovae, thus creating a marked soft X-ray excess (LaMassa et al. 2012; e.g., NGC 7582) and often require uncertain 2- T models (the hotter component tied to the starburst/spiral arms, the cooler component to the diffuse gas; Li & Wang 2013). Interestingly, for one of the closest dwarf galaxies M32 (NGC 0221; $D \simeq 0.8$ Mpc), it is possible to put a crude constraint on $\log L_x/10^{44} \text{ erg s}^{-1} \approx -7.9 \pm 0.2$ (Boroson et al. 2011), which is consistent within 1σ from the extrapolated mean M — $L_{x,g}$ (Figure 2); however, such measurement remains tentative considering the 2 dex larger L_x by XB (plus ABs and CVs).

While the X-ray properties are in general a more robust indicator of the BH mass growth compared with the stellar properties, extreme events driving shocks can cause the hot halo to become overheated up to R_{500} . In particular, ongoing wet major mergers can drive strong shocks (Mach > 10) over large regions of the group/cluster (e.g., Vazza et al. 2009), thus temporarily biasing the halo T_x toward larger values. Violent AGN jet cocoon shocks and hotspots lead to analogous bias (enhancing L_x too via major density compressions), albeit being contained mostly in the CGM/core region. We have retained in our sample the large majority of such systems (e.g., NGC 5128, NGC 1316, NGC 7626, UGC 12064, and NGC 1399), except for the dramatic case of 3C405 (Cygnus A), whose X-ray emission is fully dominated by the bipolar lobes driven via the 100 kpc FRII jets. All the above objects increase the scatter. To achieve tighter M —X-ray halo correlations, future studies may thus aim to mask the strong anisotropic merger/jet features (e.g., as done for NGC 3801) or to separate the shocked medium from the diffuse halo via a 2- T fit analysis (e.g., as carried out for NGC 2110).

Given the above limitations, future investigations should be aimed to better probe the low-mass, disk ($B/T \ll 0.3$) regime, in terms of direct dynamical BH mass measurements (e.g., by using ALMA subarcsecond resolution to detect circumnuclear

molecular disks; Barth et al. 2016), while moving toward the very soft X-ray (e.g., *Athena*) or UV emission regime (e.g., *HST/COS*). At the same time, the community should aim to expand the *direct* BH mass measurements in the BCGs of massive clusters with $T_{x,c} > 2$ keV, of which there are only a handful available at the present. The very-high-end regime is important to fill: can the universe develop UMBHs with masses in excess of 20 billion M_{\odot} or will a saturation develop? Enlarging the cluster sample is also crucial to test whether the scatter of the (more uncertain) R_{500} scalings remains smaller than that of the optical scalings. In terms of evolution, we should aim to push BH mass detections at higher z , understanding whether the presented M —X-ray scaling relations develop already with the formation of the first CC clusters (e.g., McDonald et al. 2017).

Future X-ray observations—leveraging next-generation telescopes like *Athena*⁶¹ (Ettori et al. 2013; Nandra et al. 2013), *XRISM*⁶² (Kitayama et al. 2014), *eROSITA*⁶³ (Merloni et al. 2012), and possibly *AXIS*⁶⁴ (Mushotzky et al. 2019) and *Lynx*⁶⁵ (Gaskin et al. 2018)—should aim to improve the exposure, not only of hot halos in LTGs, but also in the outer regions of the host group and cluster (e.g., as carried out with the X-COP program; Eckert et al. 2019). Expanding the sample toward isolated galaxies ($N_m = 1$; e.g., NGC 7457) and compact relic galaxies is also crucial, albeit very challenging, requiring very deep X-ray observations (with exposure $\gg 300$ ks); however, such systems are excellent laboratories to test the differences with BCGs/BGGs and disentangle the gas accretion versus merger channel. Further, achieving a finer radial profiling of the hot halo properties for the whole sample would help to better elucidate the variation of the BH scaling relations over more homogeneous extraction radii. A more accurate determination of the X-ray half-light radius would also facilitate the comparison with R_e , and better determine the virialization of hot halos in the multivariate xFP. Finally, direct detections of total masses (e.g., via lensing) and other gas mass properties as Y_{sz} (e.g., via CMB) would help to relax our derived properties assumptions and better probe the large scales, in particular at and beyond R_{500} .

5. Conclusions

We thoroughly probed the thermodynamical correlations between SMBHs and X-ray emitting plasma halos for 85 systems (Table 1), through a large literature search and Bayesian analysis approach (Section 3), as well as from a theoretical perspective testing different theories and mechanisms (Section 4). We probed univariate and multivariate (FPs) correlations over three major radial extraction regions, galactic, group/cluster core, and outskirt regions ($r \sim 0.03, 0.15, 1.0 R_{500}$), including a wide range of systems, spanning from massive galaxies to isolated S0s and spiral galaxies. The main results are as follows.

1. We found key novel BH mass versus X-ray halo (univariate) correlations, first in terms of fundamental variables, with the tightest relation being the M — T_x (slope 2.1–2.7), followed by M — L_x (slope 0.4–0.5). The

⁶¹ <https://www.the-athena-x-ray-observatory.eu>

⁶² <https://heasarc.gsfc.nasa.gov/docs/xrism>

⁶³ <https://www.mpe.mpg.de/eROSITA>

⁶⁴ <http://axis.astro.umd.edu>

⁶⁵ <https://www.lynxobservatory.com>

intrinsic scatter is significantly low, $\epsilon = 0.2\text{--}0.3$ dex, in particular adopting the galactic/core region for the temperature/luminosity. The correlation coefficients are in the very strong regime (corr $\gtrsim 0.9$). X-ray halos are thus excellent indicators for SMBH masses hosted by diverse types of galaxies (BCGs/satellites or ETGs/LTGs) with luminosities spanning over 6 dex. On average, a 0.8 keV or 10^{41} erg s $^{-1}$ hot halo is expected to host an SMBH with $10^9 M_\odot$.

2. We compared the X-ray/plasma scalings with the optical/stellar counterparts ($M_\bullet - \sigma_e$, $M_\bullet - L_K$, Magorrian), finding that the stellar scalings have significantly larger scatter, $\epsilon \approx 0.4\text{--}0.5$. This and the pairwise residual correlation analysis suggest a more fundamental role of gaseous halos in growing and tracing SMBHs. The UMBH regime is well fitted via the X-ray scalings (including the cluster/group halo), while it increases the scatter in the stellar scalings; indeed, unlike satellites and field/isolated galaxies, central BCGs/BGGs can efficiently feed from the macro plasma halo. A median $10^9 M_\odot$ SMBH is hosted by galaxies with $\sigma_e \approx 260$ km s $^{-1}$, $L_K \approx 4 \times 10^{11} L_\odot$, and $M_{\text{bulge}} \approx 3 \times 10^{11} M_\odot$.
3. We presented new BH mass (univariate) correlations in terms of the composite/derived X-ray variables: $M_\bullet - M_{\text{gas}}$ (slope 0.5–0.6) is among the tightest and strongest correlations (corr ~ 0.9), in particular within the group/cluster core region, with half the scatter of the Magorrian; remarkably, a $10^9 M_\odot$ SMBH is hosted by a hot halo with same $M_{\text{gas,g}} \approx 10^9 M_\odot$. $M_\bullet - P_x$ and $M_\bullet - n_e$ have significantly larger scatter (especially in the galactic region), the latter approaching a quasi linear scaling. $M_\bullet - Y_x$ is instead stable (slope $\simeq 1/2$) and tight ($\epsilon \simeq 0.3$) over all regions, and can be leveraged by SZ observations up to R_{500} (hot halos with $Y_{x,c} \approx 6 \times 10^{58}$ erg typically host $10^9 M_\odot$ SMBHs).
4. Besides the trivial $M_\bullet - M_{\text{tot},500}$ inherited from T_x , the total mass M_{tot} is less correlated with BH mass than most gas relations, showing superlinear slopes ($\beta \simeq 1.2\text{--}1.4$) and significant scatter comparable to that of the $M_\bullet - \sigma_e$ (a better alternative is to use the binding energy $M_\bullet \propto M_{\text{tot}}\phi$). The $M_\bullet - f_{\text{gas}}$ unveils a tighter connection with the BH mass (as for M_{gas}), establishing a linear relation ($\beta \simeq 1$) over all regions. Under our assumptions, this and above gas scalings suggest that M_\bullet correlates better with X-ray halos rather than DM halos.
5. The multivariate correlation analysis of the optical fundamental plane and X-ray fundamental plane shows that, while the stellar observables can be well described via the virial theorem (plus homology) in a multivariate fundamental plane ($\sigma_e^2 \propto L_K/R_e$), X-ray halos are better described by the univariate scalings (e.g., $L_x \propto T_x^4$), with major deviations from self-similarity and primarily driven by plasma physics, rather than a pure virialization. The main difference between the optical and X-ray component resides in the mass-to-light ratios ($M_*/L_K \propto T_*^{0.2}$ versus $M_{\text{tot}}/L_x \propto T_x^{-3}$).
6. Given the existence of the oFP/xFP, multivariate correlations between M_\bullet and (statistical) combinations of X-ray/optical properties leads to a minor scatter improvement; the above univariate correlations (especially involving T_x and σ_e^2) are a better minimal

interpretation of BH growth. The partial correlation analysis of the mixed X-ray and optical properties (e.g., $M_\bullet - T_x - \sigma_e^2$ and $M_\bullet - L_x - L_K$) corroborates that hot halos are more tightly linked to M_\bullet rather than the stellar component.

7. We tested the three major channels for M_\bullet growth: hot gas (Bondi-like) accretion, chaotic cold accretion, and mergers. Hot/smooth accretion models are rejected by the data being anticorrelated with plasma-halo properties and inducing too low feeding levels. Hierarchical binary BH mergers are subdominant during most of the cosmic time, with CLT predictions and assumptions inconsistent with our data and cosmological simulation; the latter shows that major mergers are rare and do not substantially decrease the scatter at the high-mass end. The X-ray scaling relations and simulations indicate a key role of CCA (with predictions consistent with the observed BH mass growth, halo dependence, and condensation radius), whose rain is induced by the cooling of the turbulent plasma halo (tied to L_x/T_x and M_{gas}) and balanced by the AGN feedback cycling through the Hubble time.
8. Relic galaxies (descendant of high- z red nuggets) and galactic coronae, both having sizes of a few kiloparsecs, are vital astrophysical laboratories to test the SMBH growth via purely gas accretion, since the former have been untouched by mergers for 13 Gyr and the latter can survive extreme or poor environments, thus enabling the recurrent inner feeding via gas condensation. On the other hand, galaxies at the center of rich environments (large N_m or B/T , and early types) can feed from the macro-scale rain forming UMBHs.
9. The new X-ray halo correlations can be leveraged to calibrate and test large-scale cosmological simulations with AGN feeding/feedback subgrid schemes, as well as SAMs of galaxy and cluster formation. These can be now carried out from multiple angles not only in terms of L_x and T_x (plasma studies), but also via gas pressure/thermal energy (SZ studies), gas fractions (cosmological studies), and total/DM masses (lensing studies).

In sum, the BH physics at the microscale is tightly linked to the macro gaseous atmosphere thermodynamics, thus creating a unique symbiotic system (which we refer to as “black hole weather”) spanning over ~ 10 orders of magnitude in space and time (as predicted by first-principle arguments; Gaspari & Sadowski 2017). This study highlights the importance of combining both observational analysis (and exquisite single studies produced in the literature) with a deep theoretical/numerical interpretation. We live exciting times for multiphase SMBH feeding/feedback observations and modeling, with new missions directly probing and discovering the multiphase halo rain and AGN outflows (*Chandra*, *XMM*, *ALMA*, *MUSE*, *MUSTANG-2*, *LOFAR*, *SOFIA*) and with next-generation telescopes that might be able to open new windows on multimessenger processes related to SMBHs and gaseous halos (*Athena*, *eROSITA*, *XRISM*, *EHT*, *JWST*, *SPT-3G*, *LSST*, *SKA*, and *LISA*). These programs will lead to order-of-magnitude leaps in sample size, sensitivity, and accuracy, and thus, in our understanding of BHs and their coevolution with the host galaxies, groups and clusters of galaxies.

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M. Rossetti, N. Caplar for constructive feedback. This work made use of public databases: HyperLEDA (Paturel et al. 2003),⁶⁶ SAO/NASA Astrophysics Data System (ADS),⁶⁷ and NASA/IPAC Extragalactic Database (NED).⁶⁸

Appendix A Complementary Scalings

We include here additional univariate and multivariate scalings complementary to the discussion in Sections 3–4. The scaling relations presented in Figures 22–27 can be useful for other studies that intend to probe and/or calibrate their parameters on a wider range of observational constraints. Being secondary and mentioned in the above sections, we do not dissect each scaling, although we provide insights in each caption. The interested reader can assess the quantitative properties of the correlations from the inset, listing the mean and standard deviations for all the posterior distributions (Section 2.2). Additional permutations of the scalings can be easily computed by combining the below correlations and/or those in Table 1.

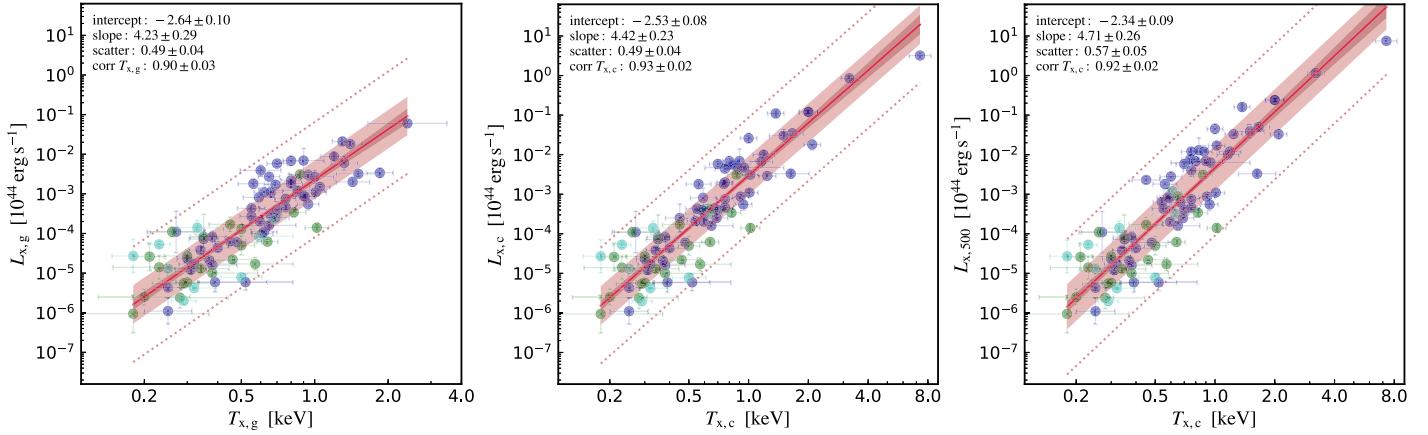


Figure 22. X-ray luminosity vs. temperature within the galactic/CGM $R_{x,g}$ (left), group/cluster $R_{x,c}$ (middle), and R_{500} scale (right; note that $T_{x,500} \approx T_{x,c}$). The inset lists the posterior mean and errors for the intercept, slope, intrinsic scatter (1σ interval plotted as a filled light red band, 3σ as dotted lines), and correlation coefficient. The solid red line and inner dark band show the mean fit and related 15.87–84.13 percentile interval. The blue, green, and cyan points correspond to E, S0, and S morphological types, respectively. The steep, non-self-similar scalings are consistent with that found by other works including a significant number of isolated galaxies down to the 0.3 keV regime (e.g., Kim & Fabbiano 2015; Goulding et al. 2016; Babyk et al. 2018).

⁶⁶ <http://leda.univ-lyon1.fr>

⁶⁷ <http://www.adsabs.harvard.edu>

⁶⁸ <https://ned.ipac.caltech.edu>

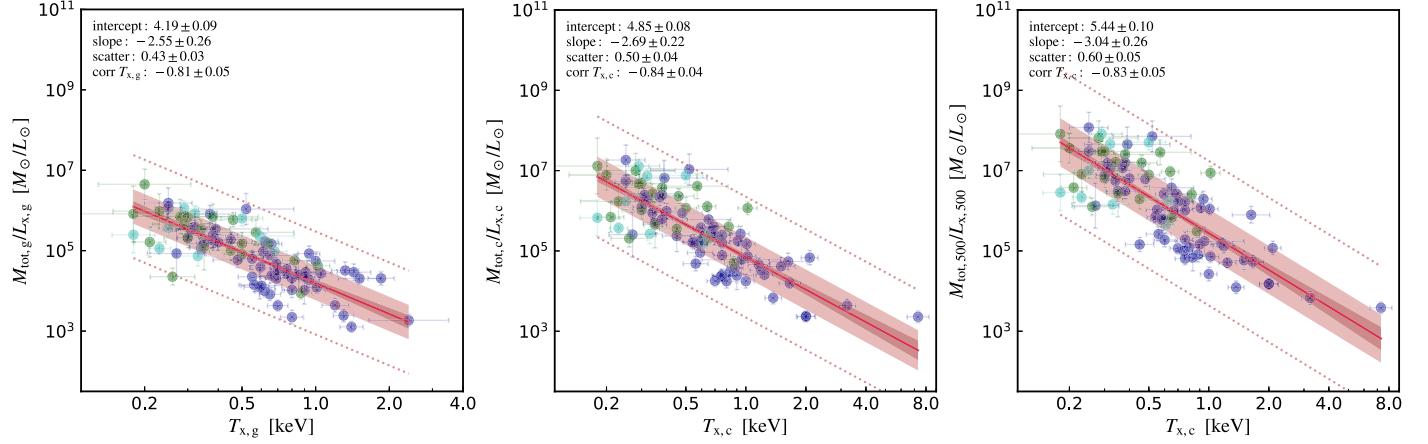


Figure 23. Total mass (dominated by DM) to X-ray light ratio vs. X-ray temperature contained within $R_{x,g}$ (left), $R_{x,c}$ (middle), and R_{500} (right). Analog of Figure 22, which we can also use to convert to an average $M_{\text{tot}} \propto T_x^{1.7}$ and $L_x \propto M_{\text{tot}}^{2.5}$ scalings; such relations are steeper than the self-similar expectations (3/2 and 4/3, respectively), particularly in the latter case (as found in other studies, e.g., Anderson et al. 2015). We note that, due to the larger photon counts, the majority of previous investigations on X-ray scalings focused on massive/central BCGs (hence leading to shallower slopes for relations involving L_x and M_{gas}), while here we also include a large variety of lower mass objects, such as gas-poor galaxies, isolated Es, S0s, and disky LTGs. See Section 3.3.2 for further discussion on the mass-to-light ratios.

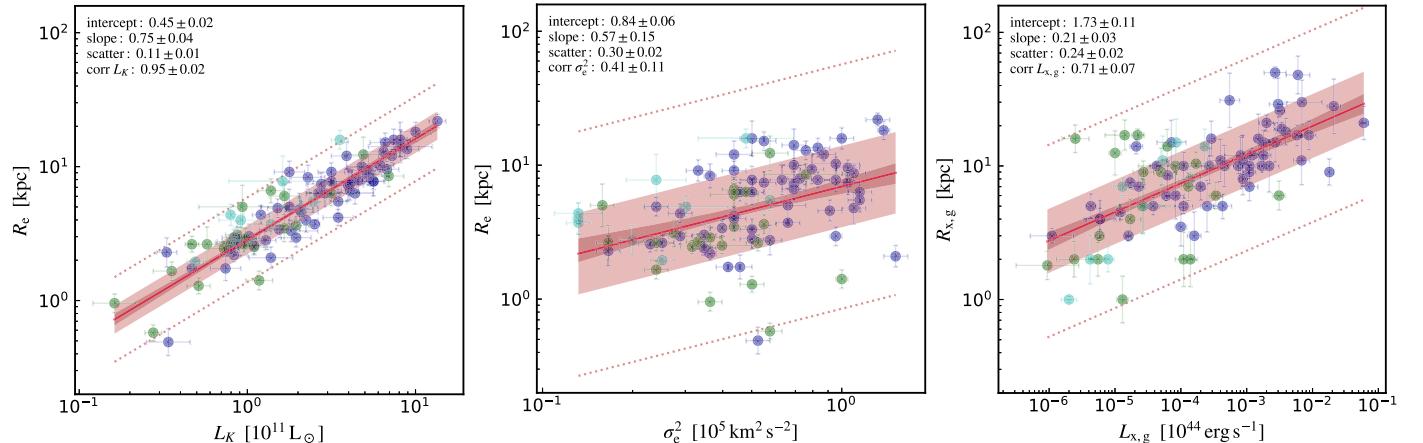


Figure 24. Size vs. luminosity or temperature scaling relations for the considered galaxies in optical (left and middle) and X-ray band (right). Analog of Figure 22. Note the strong and tight stellar size-luminosity scaling, which is consistent with the recent version of the Kormendy relation for bulge-dominated galaxies (e.g., Läsker et al. 2014). LTGs have instead a major impact on the correlation between stellar size and σ_e^2 , making it fairly shallow and weaker, with 3× larger scatter. The X-ray size-luminosity scaling shows scatter in between, but substantially lower slope than the optical counterpart, although now probing three more orders of magnitude in luminosity. It is clear from the normalization that hot halos are generally more extended even at the galactic scale.

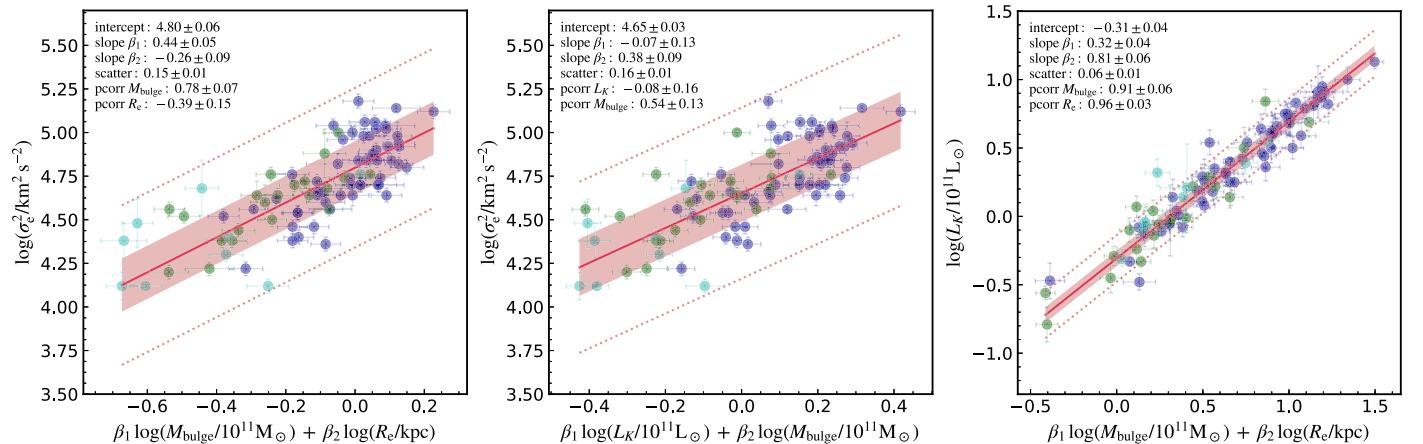


Figure 25. Variants of the optical fundamental plane including the bulge mass. Edge-on view of the multivariate correlation plane (red line is the best-fit with the 1 σ and 3 σ intrinsic scatter bands overplotted). The inset shows all the retrieved mlinmix Bayesian posterior parameters (mean and standard deviation; Section 2.2). Although not necessarily linked to the VT, all the above multivariate correlations show a small scatter. The first two panels show 50% larger scatter compared with the standard OFP (Figure 10), while the scatter of the luminosity- M_{bulge} -size relation is 40% smaller (with high significance). This is partly due to the fairly stable optical mass-to-light ratios, although both $\text{pcorr}_{1,2}$ are in the very strong regime, signaling that R_e also plays a role.

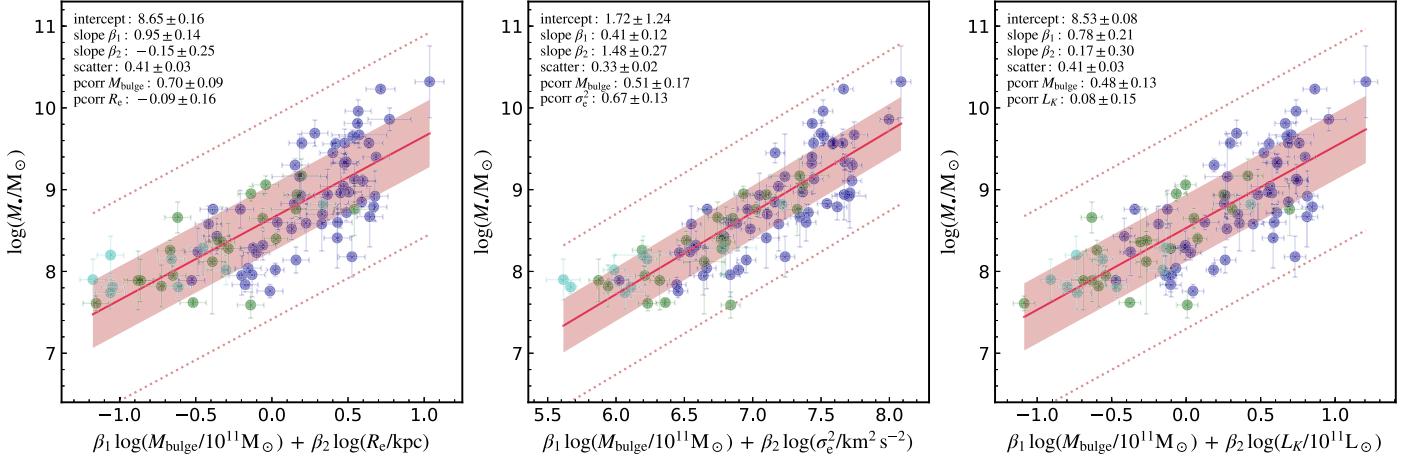


Figure 26. BH mass vs. bulge mass and another fundamental optical variable, including stellar size (left), velocity variance (middle), or luminosity (right). Analog of Figure 25. Using the bulge mass instead of L_K shows similar results for the multivariate correlations (Section 3.3.3), albeit M_{bulge} tends to emerge even over the second independent variable ($\text{pcorr}_1 \gg \text{pcorr}_2$; except for the σ_e^2 case).

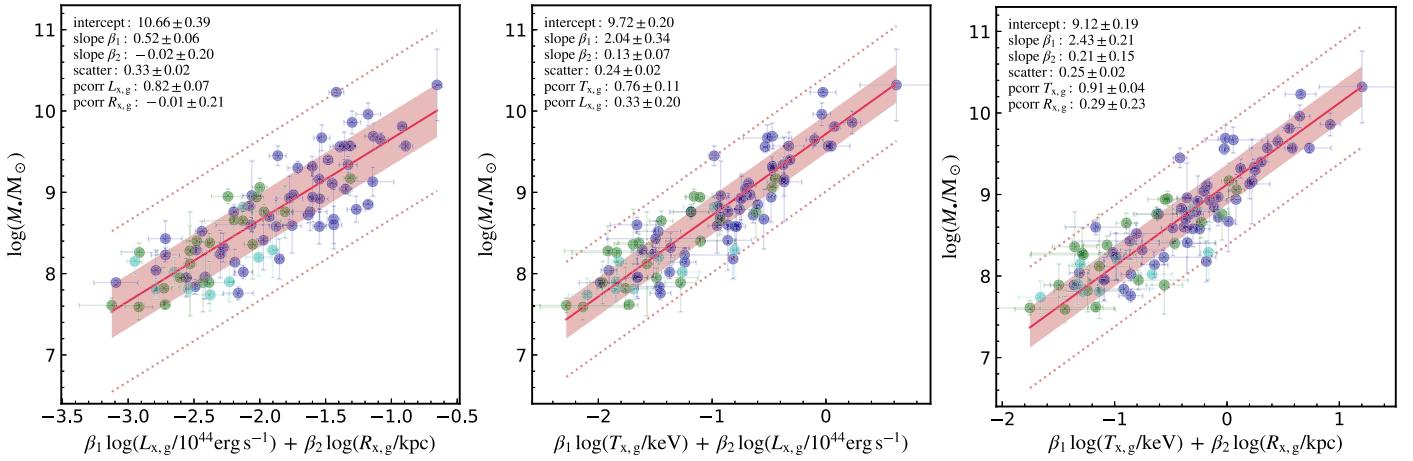


Figure 27. BH mass vs. dual properties of the xFP (edge-on view), permuting the X-ray luminosity, size, and temperature for the galactic/CGM region. Analog of Figure 25. As for the other radial regions (Section 3.3.4), using a multivariate fitting for the X-ray properties does not significantly improve the intrinsic scatter.

Appendix B Optical And X-Ray Data Sample Tables

Table 2 lists the optical properties of our samples of 85 host galaxies with direct dynamical SMBH measurements. The related X-ray hot halo properties (within the galactic and group/cluster scales) and environment are shown in Table 3.

Table 2
Optical Properties of Our Sample

Galaxy Name (i)	PGC # (ii)	Type (iii)	N_m (iv)	D (Mpc) (v)	M_\star $\log(M_\odot)$ (vi)	σ_e $\log(\text{km s}^{-1})$ (vii)	L_K $\log(L_\odot)$ (viii)	M_{bulge} $\log(M_\odot)$ (ix)	R_e $\log(\text{kpc})$ (x)	B/T (xi)	References and Notes (xii)
N0821	8160	S0/E6	1	23.4 ± 1.8	7.59 ± 0.16	2.32 ± 0.02	11.14 ± 0.08	10.98 ± 0.09	0.82 ± 0.09	0.95	(d,a,b);(1)
N2787	26341	SB0	2	7.4 ± 1.2	7.61 ± 0.09	2.28 ± 0.02	10.21 ± 0.13	9.78 ± 0.09	-0.02 ± 0.07	0.26	(a,b);(2)
N1023	10123	SB0	4	10.8 ± 0.8	7.62 ± 0.05	2.22 ± 0.02	10.94 ± 0.07	10.53 ± 0.09	0.49 ± 0.10	0.39	(a,b);(3)
N7582	71001	SBab	8	22.3 ± 9.8	7.74 ± 0.20	2.19 ± 0.05	11.21 ± 0.32	10.02 ± 0.10	0.89 ± 0.19	0.1	(a,b);(4)
N5128	46957	E/S0	6	3.6 ± 0.2	7.76 ± 0.08	2.18 ± 0.02	11.04 ± 0.06	11.05 ± 0.09	0.41 ± 0.06	1.0	(a,b);(5)
N3031	28630	SAab	3	3.6 ± 0.1	7.81 ± 0.13	2.15 ± 0.02	10.93 ± 0.08	10.42 ± 0.09	0.44 ± 0.11	0.34	(a,c);(6)
N4151	38739	Sab	65	20.0 ± 2.8	7.81 ± 0.08	2.06 ± 0.01	10.96 ± 0.13	9.99 ± 0.08	0.60 ± 0.12	0.33	(a,c,o,p);(7)
N4203	39158	SAB0	1	14.1 ± 1.4	7.82 ± 0.26	2.11 ± 0.02	10.76 ± 0.11	10.30 ± 0.14	0.42 ± 0.13	0.37	(a,d);(8)
N4459	41104	E2	197	16.0 ± 0.5	7.84 ± 0.09	2.20 ± 0.02	10.94 ± 0.04	10.88 ± 0.09	0.42 ± 0.06	1.0	(a,b);(9)
N4596	42401	SB0	197	16.5 ± 6.2	7.89 ± 0.26	2.10 ± 0.02	10.97 ± 0.26	10.20 ± 0.09	0.70 ± 0.16	0.78	(a,d);(10)
N3377	32249	E5	11	11.0 ± 0.5	7.89 ± 0.03	2.11 ± 0.02	10.52 ± 0.06	10.50 ± 0.09	0.36 ± 0.11	1.0	(e,a,b);(11)
N4036	7930	S0	3	19.0 ± 1.9	7.89 ± 0.36	2.26 ± 0.02	10.90 ± 0.09	10.14 ± 0.10	0.43 ± 0.06	0.17	(a,d);(12)
N4258	39600	SABbc	5	7.3 ± 0.5	7.90 ± 0.25	2.06 ± 0.04	10.90 ± 0.08	9.86 ± 0.09	0.64 ± 0.08	0.12	(s,a,b);(13)
N4564	42051	S0	197	15.9 ± 0.5	7.95 ± 0.12	2.19 ± 0.02	10.67 ± 0.04	10.38 ± 0.09	0.42 ± 0.06	0.67	(a,b);(14)
N4473	41228	E5	197	15.2 ± 0.5	7.95 ± 0.24	2.27 ± 0.02	10.89 ± 0.03	10.85 ± 0.09	0.38 ± 0.05	1.0	(a,b);(15)
N4278	39764	E1-2	15	15.0 ± 1.5	7.96 ± 0.27	2.33 ± 0.02	10.87 ± 0.09	10.90 ± 0.09	0.24 ± 0.09	1.0	(a,d);(16)
N5018	45908	E3	5	40.5 ± 4.9	8.02 ± 0.08	2.32 ± 0.01	11.54 ± 0.09	11.12 ± 0.06	0.62 ± 0.06	0.51	(a,c);(17)
N7331	69327	Sab	2	12.2 ± 1.2	8.02 ± 0.18	2.06 ± 0.02	11.14 ± 0.10	10.77 ± 0.13	0.57 ± 0.08	0.47	(a,n);(18)
N3379	32256	E0	11	10.7 ± 0.5	8.04 ± 0.25	2.27 ± 0.02	11.01 ± 0.06	10.91 ± 0.09	0.48 ± 0.09	1.0	(d,a,b);(19)
N2110	18030	SAB0	2	29.1 ± 2.9	8.12 ± 0.64	2.30 ± 0.05	11.04 ± 0.08	10.65 ± 0.09	0.40 ± 0.06	0.39	(a,p);(20)
N3607	34426	E1	16	22.6 ± 1.8	8.14 ± 0.16	2.32 ± 0.02	11.35 ± 0.07	11.26 ± 0.09	0.60 ± 0.09	1.0	(a,b);(21)
N0224	2557	Sb	>4	0.77 ± 0.03	8.15 ± 0.16	2.20 ± 0.02	10.69 ± 0.05	10.35 ± 0.09	0.29 ± 0.02	0.57	(a,r);(22)
N1316	12651	E4	49	18.6 ± 0.6	8.18 ± 0.25	2.35 ± 0.02	11.91 ± 0.06	11.74 ± 0.09	1.20 ± 0.13	1.0	(a,b);(23)
N1667	16062	SABC	4	56.1 ± 5.6	8.20 ± 0.23	2.24 ± 0.07	11.32 ± 0.10	9.99 ± 0.09	0.69 ± 0.08	0.16	(a,j);(24)
N5576	51275	E3	5	25.7 ± 1.7	8.23 ± 0.09	2.19 ± 0.02	11.18 ± 0.06	11.00 ± 0.09	0.69 ± 0.07	1.0	(d,a);(25)
N1052	10175	E4	8	18.1 ± 1.8	8.24 ± 0.29	2.28 ± 0.01	10.92 ± 0.08	10.54 ± 0.09	0.34 ± 0.05	1.0	(a,h);(26)
N4026	37760	S0	65	13.4 ± 1.7	8.26 ± 0.12	2.19 ± 0.02	10.55 ± 0.11	10.33 ± 0.09	0.22 ± 0.07	0.61	(a,b);(27)
N3801	36200	S0	7	46.3 ± 4.6	8.28 ± 0.31	2.32 ± 0.04	11.22 ± 0.09	10.82 ± 0.09	0.78 ± 0.09	0.38	(a,h);(28)
N4697	43276	E5	15	12.5 ± 0.4	8.29 ± 0.04	2.23 ± 0.02	11.08 ± 0.05	10.97 ± 0.09	0.64 ± 0.07	1.0	(e,a,b);(29)
N1961	17625	SABB	9	48.6 ± 4.9	8.29 ± 0.34	2.34 ± 0.08	11.55 ± 0.05	10.71 ± 0.10	1.20 ± 0.07	0.15	(a,j);(30)
N3608	34433	E1	16	22.8 ± 1.5	8.32 ± 0.18	2.23 ± 0.02	10.92 ± 0.07	11.01 ± 0.09	0.47 ± 0.06	1.0	(d,a);(31)
N3998	37642	S0	65	14.3 ± 1.3	8.36 ± 0.43	2.35 ± 0.02	10.71 ± 0.07	10.67 ± 0.09	0.11 ± 0.06	0.85	(d,a,b);(32)
N3245	30744	S0	4	21.4 ± 2.0	8.38 ± 0.11	2.25 ± 0.02	10.86 ± 0.09	10.69 ± 0.09	0.39 ± 0.05	0.7	(a,b);(33)
N3414	32533	S0	5	25.2 ± 2.7	8.40 ± 0.07	2.28 ± 0.02	10.99 ± 0.11	11.10 ± 0.08	0.46 ± 0.08	0.79	(a,c);(34)
N3862	36606	E	61	84.6 ± 8.5	8.41 ± 0.37	2.32 ± 0.03	11.59 ± 0.09	11.62 ± 0.09	1.08 ± 0.10	1.0	(a,d);(35)
N5845	53901	E3	13	25.9 ± 4.1	8.43 ± 0.22	2.36 ± 0.02	10.53 ± 0.13	10.57 ± 0.09	-0.31 ± 0.10	1.0	(e,a,b);(36)
N3585	34160	E6/S0	3	20.5 ± 1.7	8.52 ± 0.13	2.33 ± 0.02	11.42 ± 0.07	11.26 ± 0.09	0.80 ± 0.07	0.93	(a,b);(37)
N7626	71140	E	16	38.1 ± 3.8	8.58 ± 0.33	2.37 ± 0.02	11.44 ± 0.09	11.48 ± 0.09	0.87 ± 0.08	1.0	(a,d);(38)
N4636	42734	E0-1	11	13.7 ± 1.4	8.58 ± 0.22	2.26 ± 0.02	11.25 ± 0.09	10.71 ± 0.09	0.96 ± 0.08	0.28	(a,d);(39)
N0541	5305	E	43	63.7 ± 6.4	8.59 ± 0.34	2.28 ± 0.01	11.36 ± 0.10	11.38 ± 0.13	0.92 ± 0.09	1.0	(a,m);(40)
N7052	66537	E3	1	70.4 ± 8.4	8.60 ± 0.23	2.42 ± 0.02	11.68 ± 0.09	11.61 ± 0.10	1.00 ± 0.05	1.0	(a,b);(41)
N4621	42628	E5	197	18.3 ± 3.0	8.60 ± 0.09	2.30 ± 0.02	11.19 ± 0.12	11.12 ± 0.12	0.53 ± 0.06	1.0	(a,c);(42)
N4526	41772	SAB0	197	16.4 ± 1.8	8.65 ± 0.12	2.32 ± 0.02	11.22 ± 0.09	11.02 ± 0.09	0.54 ± 0.10	0.65	(a,b);(43)
N4342	40252	S0	197	22.9 ± 1.4	8.66 ± 0.19	2.38 ± 0.02	10.44 ± 0.05	10.31 ± 0.09	-0.24 ± 0.06	0.7	(a,b);(44)
N0741	7252	E0	8	65.7 ± 6.6	8.67 ± 0.37	2.37 ± 0.02	11.82 ± 0.09	11.86 ± 0.09	1.18 ± 0.07	1.0	(a,b);(45)
N4552	41968	E0-1	197	15.3 ± 1.0	8.70 ± 0.05	2.35 ± 0.02	11.11 ± 0.06	11.42 ± 0.11	0.45 ± 0.07	1.0	(a,c);(46)
N4261	39659	E2	39	32.4 ± 2.8	8.72 ± 0.10	2.42 ± 0.02	11.60 ± 0.09	11.65 ± 0.09	0.86 ± 0.12	1.0	(a,b);(47)
N4291	39791	E2	7	26.6 ± 3.9	8.76 ± 0.23	2.38 ± 0.02	10.95 ± 0.13	10.85 ± 0.09	0.44 ± 0.11	1.0	(a+e,b);(48)
N3665	35064	SA0	4	34.7 ± 6.7	8.76 ± 0.09	2.34 ± 0.02	11.50 ± 0.15	11.29 ± 0.17	0.80 ± 0.09	0.58	(a,g);(49)
N1374	13267	E0	49	19.2 ± 0.7	8.76 ± 0.06	2.31 ± 0.02	10.67 ± 0.03	10.63 ± 0.09	0.24 ± 0.03	1.0	(a,b);(50)
N0383	3982	S0	48	59.2 ± 5.9	8.76 ± 0.32	2.38 ± 0.03	11.69 ± 0.11	11.74 ± 0.14	1.09 ± 0.13	1.0	(a,f);(51)
N6251	58472	E1	17	108.4 ± 9.0	8.79 ± 0.16	2.46 ± 0.02	11.95 ± 0.07	11.88 ± 0.09	1.13 ± 0.07	1.0	(a,b,q);(52)

Table 2
(Continued)

Galaxy Name (i)	PGC # (ii)	Type (iii)	N_m (iv)	D (Mpc) (v)	M_* $\log(M_\odot)$ (vi)	σ_e $\log(\text{km s}^{-1})$ (vii)	L_K $\log(L_\odot)$ (viii)	M_{bulge} $\log(M_\odot)$ (ix)	R_e $\log(\text{kpc})$ (x)	B/T (xi)	References and Notes (xii)
N4594	42407	Sa	15	9.9 ± 0.8	8.82 ± 0.05	2.38 ± 0.02	11.39 ± 0.08	11.47 ± 0.09	0.74 ± 0.08	0.93	(a,b);(53)
N1332	12838	E6/S0	10	22.3 ± 1.9	8.83 ± 0.04	2.52 ± 0.02	11.31 ± 0.08	11.26 ± 0.09	0.68 ± 0.12	1.0	(a,b);(54)
N5813	53643	E1-2	13	32.2 ± 2.7	8.85 ± 0.06	2.32 ± 0.02	11.50 ± 0.08	11.77 ± 0.09	0.96 ± 0.07	1.0	(a,c);(55)
N0315	3455	E/cD	14	57.7 ± 2.8	8.92 ± 0.31	2.49 ± 0.04	11.79 ± 0.08	11.87 ± 0.09	1.01 ± 0.05	1.0	(a,b);(56)
N5077	46456	E3	5	38.7 ± 8.4	8.93 ± 0.27	2.35 ± 0.02	11.26 ± 0.16	11.28 ± 0.09	0.52 ± 0.08	1.0	(a,b);(57)
N0524	5222	S0	9	24.2 ± 2.2	8.94 ± 0.05	2.37 ± 0.02	11.29 ± 0.08	11.26 ± 0.09	0.56 ± 0.07	0.92	(a,b);(58)
N1399	13418	E1	49	20.9 ± 0.7	8.94 ± 0.31	2.53 ± 0.02	11.54 ± 0.05	11.50 ± 0.09	0.74 ± 0.09	1.0	(a,b);(59)
N3115	29265	S0	2	9.5 ± 0.4	8.95 ± 0.09	2.36 ± 0.02	10.98 ± 0.04	10.92 ± 0.09	0.42 ± 0.06	0.9	(a,b);(60)
IC1459	70090	E4	6	28.9 ± 3.7	8.96 ± 0.43	2.53 ± 0.02	11.64 ± 0.11	11.60 ± 0.09	0.80 ± 0.08	1.0	(a+i,b);(61)
N4374	40455	E1	197	18.5 ± 0.6	8.97 ± 0.05	2.41 ± 0.02	11.40 ± 0.03	11.62 ± 0.09	0.57 ± 0.03	1.0	(a,b);(62)
N5846	53932	E0-1	13	24.9 ± 2.3	9.04 ± 0.06	2.35 ± 0.02	11.46 ± 0.09	11.62 ± 0.16	0.80 ± 0.10	1.0	(a,c);(63)
N1277	12434	S0	180	71.0 ± 7.1	9.06 ± 0.11	2.50 ± 0.01	11.07 ± 0.08	10.98 ± 0.09	0.15 ± 0.07	0.55	(t,a,b);(64)
IC4296	48040	E0	64	49.2 ± 3.6	9.11 ± 0.07	2.51 ± 0.02	11.83 ± 0.07	11.78 ± 0.09	0.98 ± 0.06	1.0	(a,b);(65)
N7768	72605	E4	9	116.0 ± 27.5	9.13 ± 0.18	2.42 ± 0.02	11.91 ± 0.19	11.75 ± 0.09	1.15 ± 0.12	1.0	(a,b);(66)
U12064	69055	E/S0	7	72.5 ± 6.7	9.16 ± 0.52	2.41 ± 0.03	11.25 ± 0.17	11.30 ± 0.19	0.70 ± 0.13	1.0	(a,f);(67)
N6240S	59186	S0/I0	2	105.0 ± 10.5	9.17 ± 0.21	2.44 ± 0.07	11.84 ± 0.09	11.35 ± 0.13	0.93 ± 0.08	0.28	(a,k);(68)
N6861	64136	E4/SAO	12	27.3 ± 4.5	9.30 ± 0.08	2.59 ± 0.02	11.14 ± 0.13	11.21 ± 0.09	0.32 ± 0.08	1.0	(a,b);(69)
N4649	42831	E2	197	16.5 ± 0.6	9.32 ± 0.12	2.43 ± 0.02	11.66 ± 0.06	11.64 ± 0.09	0.90 ± 0.10	1.0	(d,a);(70)
N7619	71121	E3	16	51.5 ± 7.4	9.34 ± 0.10	2.51 ± 0.02	11.61 ± 0.12	11.65 ± 0.09	0.87 ± 0.09	1.0	(b,a);(71)
N4472	41220	E2	197	17.1 ± 0.6	9.40 ± 0.04	2.40 ± 0.02	11.75 ± 0.07	11.86 ± 0.09	0.89 ± 0.11	1.0	(a,b);(72)
N3923	37061	E4	10	20.9 ± 2.7	9.45 ± 0.12	2.35 ± 0.02	11.50 ± 0.11	11.56 ± 0.09	0.89 ± 0.10	1.0	(a,c);(73)
N3091	28927	E3	10	51.2 ± 8.3	9.56 ± 0.07	2.49 ± 0.02	11.62 ± 0.12	11.58 ± 0.09	0.89 ± 0.09	1.0	(a,b);(74)
N1150	14880	E1/cD	15	51.6 ± 5.6	9.57 ± 0.07	2.48 ± 0.02	11.32 ± 0.10	11.31 ± 0.09	0.66 ± 0.08	1.0	(a,b);(75)
N6086	57482	E/cD	37	138.0 ± 11.5	9.57 ± 0.17	2.50 ± 0.02	11.87 ± 0.08	11.69 ± 0.09	1.20 ± 0.08	1.0	(a,b);(76)
A1836 _B	49940	E	41	152.4 ± 8.4	9.57 ± 0.06	2.46 ± 0.02	11.75 ± 0.06	11.81 ± 0.10	0.89 ± 0.06	1.0	(a,b);(77)
N1407	13505	E0	15	28.0 ± 3.4	9.65 ± 0.08	2.45 ± 0.02	11.72 ± 0.12	11.71 ± 0.09	0.97 ± 0.11	1.0	(a,b);(78)
N5328	49307	E1	11	64.1 ± 7.0	9.67 ± 0.16	2.52 ± 0.02	11.71 ± 0.09	11.75 ± 0.19	0.94 ± 0.06	1.0	(a,c);(79)
M1216	23789	E	2	94.0 ± 9.4	9.69 ± 0.16	2.49 ± 0.01	11.29 ± 0.09	11.37 ± 0.09	0.47 ± 0.07	1.0	(l,a);(80)
N4486	41361	E1/cD	197	16.7 ± 0.6	9.81 ± 0.05	2.42 ± 0.02	11.61 ± 0.05	11.72 ± 0.09	0.82 ± 0.07	1.0	(v,a,b);(81)
N5419	50100	E	43	56.2 ± 6.1	9.86 ± 0.14	2.57 ± 0.01	12.00 ± 0.09	12.01 ± 0.15	1.26 ± 0.07	1.0	(a,c);(82)
N3842	36487	E1	117	92.2 ± 10.6	9.96 ± 0.14	2.44 ± 0.02	11.81 ± 0.11	11.77 ± 0.09	1.11 ± 0.07	1.0	(a,b);(83)
N1600	15406	E3	30	64.0 ± 6.4	10.23 ± 0.04	2.47 ± 0.02	11.86 ± 0.08	11.92 ± 0.10	1.08 ± 0.05	1.0	(a,u);(84)
N4889	44715	E4/cD	583	102.0 ± 5.2	10.32 ± 0.44	2.56 ± 0.02	12.13 ± 0.05	12.30 ± 0.10	1.34 ± 0.05	1.0	(a,c);(85)

Note. (6, 13, 19, 22, 42, 46, 53, 62, 65, 67, 70, 77, 81, 85) Other common names (respectively): M81, M106, M105, M31/Andromeda, M59, M89, M104, M84, A3565_{BCG}, 3C449, M60, PKS B1358-113, M87, and A1656_{BCG}. (8, 10, 12, 16, 18, 20, 22, 24, 26, 28, 35, 38, 39, 40, 49, 51, 67, 68). Bulge mass computed via B/T in conjunction with Equation (1) (Kormendy & Ho 2013). (13) N_m from de Vaucouleurs (1975). (48) Geometric average between (a) and (e) dynamical BH masses. (52) N_m from Chen et al. (2011). (61) Geometric average between the stellar (a) and gas (i) dynamical BH masses. (65, 76, 77, 83) N_m from Abell et al. (1989) catalog. (67) NED redshift/distance adopted. (68) BH in the major southern (S) structure (merging pair). (77) “B” subscript stands for BCG. (81) Direct SMBH horizon imaging via EHT. (85) N_m from Beijersbergen (2003). Columns: (i) Galaxy name, with prefixes defined as N = NGC (New General Catalogue); IC (Index Catalogue); A = Abell Catalogue; M = Mrk (Markarian Catalogue); U = UGC (Uppsala General Catalogue). Top to bottom: galaxies are in order of ascending M_* . (ii) Principal Galaxies Catalog (PGC) identification number (HyperLEDA). (iii) Hubble morphological type (from RC3, de Vaucouleurs et al. 1991; Beifiori et al. 2012; Kormendy & Ho 2013; NED). (iv) Number of group/cluster members (from 2MASS 11.75 catalog; Tully 2015). (v) Distance (from surface brightness fluctuations or redshifts; van den Bosch 2016; Saglia et al. 2016). (vi) Dynamical BH masses measurements via stellar/gas kinematics (mostly from van den Bosch 2016 and refs. therein). (vii) Stellar velocity dispersion within the optical half-light radius R_e (mostly from van den Bosch 2016). (viii) Total K_s -band luminosity (mostly from van den Bosch 2016). (ix) Stellar bulge mass (mostly from Kormendy & Ho 2013). (x) Effective, optical half-light radius (mostly from van den Bosch 2016). (xi) (Classical or pseudo) bulge-to-total luminosity ratio (mostly from Kormendy & Ho 2013). (xii) References used for the listed optical properties and single-object notes (if any).

References. (a) van den Bosch (2016); (b) Kormendy & Ho (2013); (c) Saglia et al. (2016); (d) Beifiori et al. (2012); (e) Graham & Scott (2013); (f) Donzelli et al. (2007); (g) Graham et al. (2015); (h) Beifiori (2010); (i) Cappellari et al. (2002); (j) Dong & De Robertis (2006); (k) Medling et al. (2015); (l) Walsh et al. (2017); (m) de Souza et al. (2004); (n) Bottema (1999); (o) Onken et al. (2014); (p) Gadotti (2008); (q) Chen et al. (2011); (r) Seigar et al. (2008); (s) Pastorini et al. (2007); (t) Graham et al. (2016); (u) Thomas et al. (2016); (v) Event Horizon Telescope Collaboration et al. (2019a).

Table 3
X-Ray Properties and Environment of Our Sample

Galaxy Name (i)	Central Galaxy (ii)	$L_{x,g}$ log(erg s ⁻¹) (iii)	$T_{x,g}$ log(keV) (iv)	$R_{x,g}$ log(kpc) (v)	$L_{x,c}$ log(erg s ⁻¹) (vi)	$T_{x,c}$ log(keV) (vii)	$R_{x,c}$ log(kpc) (viii)	$L_{x,500}$ log(erg s ⁻¹) (ix)	R_{500} log(kpc) (x)	References and Notes (xi)
N0821	isolated	38.40 ± 0.21	-0.70 ± 0.19	1.20	38.40 ± 0.21	-0.70 ± 0.19	1.48	38.40 ± 0.21	2.31	(a,b);(1)
N2787	isolated	37.97 ± 0.48	-0.74 ± 0.31	0.26	37.97 ± 0.48	-0.74 ± 0.31	1.46	37.97 ± 0.48	2.28	(C);(2)
N1023	BFG:N1023	38.76 ± 0.07	-0.52 ± 0.05	0.48	38.76 ± 0.07	-0.52 ± 0.05	1.58	38.76 ± 0.07	2.40	(a);(3)
N7582	BFG:Grus	39.43 ± 0.42	-0.74 ± 0.09	0.70	39.43 ± 0.42	-0.74 ± 0.09	1.46	39.43 ± 0.42	2.28	(w,C);(4)
N5128	BFG:CenA	39.86 ± 0.22	-0.46 ± 0.06	1.18	39.86 ± 0.22	-0.46 ± 0.06	1.61	39.86 ± 0.22	2.44	(v);(5)
N3031	BFG:M81	38.62 ± 0.03	-0.49 ± 0.09	0.30	38.62 ± 0.03	-0.49 ± 0.09	1.59	38.62 ± 0.03	2.42	(Q);(6)
N4151	N4258(M106)	39.11 ± 0.14	-0.60 ± 0.07	0.85	39.11 ± 0.14	-0.60 ± 0.07	1.54	39.11 ± 0.14	2.36	(J);(7)
N4203	isolated	38.74 ± 0.11	-0.54 ± 0.13	0.30	38.74 ± 0.11	-0.54 ± 0.13	1.57	38.74 ± 0.11	2.39	(c);(8)
N4459	N4486/N4472	39.20 ± 0.04	-0.42 ± 0.10	0.48	39.20 ± 0.04	-0.42 ± 0.10	1.63	39.20 ± 0.04	2.46	(c);(9)
N4596	N4486/N4472	39.41 ± 0.35	-0.68 ± 0.07	0.70	39.41 ± 0.35	-0.68 ± 0.07	1.49	39.41 ± 0.35	2.32	(a);(10)
N3377	N3379	38.04 ± 0.33	-0.60 ± 0.10	0.48	38.04 ± 0.33	-0.60 ± 0.10	1.53	38.04 ± 0.33	2.36	(j,n);(11)
N4036	N3945	39.34 ± 0.09	-0.34 ± 0.08	1.23	39.34 ± 0.09	-0.34 ± 0.08	1.68	39.34 ± 0.09	2.50	(b);(12)
N4258	BFG:CVnI	39.72 ± 0.07	-0.64 ± 0.05	1.04	39.72 ± 0.07	-0.64 ± 0.05	1.52	39.72 ± 0.07	2.34	(R);(13)
N4564	N4486/N4472	39.00 ± 0.09	-0.42 ± 0.19	1.10	39.00 ± 0.09	-0.42 ± 0.19	1.63	39.00 ± 0.09	2.46	(b);(14)
N4473	N4486/N4472	39.08 ± 0.08	-0.51 ± 0.06	0.65	39.08 ± 0.08	-0.51 ± 0.06	1.59	39.08 ± 0.08	2.41	(a);(15)
N4278	N4414	39.36 ± 0.09	-0.52 ± 0.04	0.85	39.36 ± 0.09	-0.52 ± 0.04	1.58	39.36 ± 0.09	2.40	(a);(16)
N5018	BGG:N5018	39.92 ± 0.13	-0.42 ± 0.05	0.78	39.92 ± 0.13	-0.42 ± 0.05	1.63	39.92 ± 0.13	2.46	(l);(17)
N7331	isolated	38.89 ± 0.10	-0.30 ± 0.09	0.30	38.89 ± 0.10	-0.30 ± 0.09	1.70	38.89 ± 0.10	2.52	(F,G);(18)
N3379	BFG:N3379	38.63 ± 0.08	-0.60 ± 0.05	0.70	38.63 ± 0.08	-0.60 ± 0.05	1.54	38.63 ± 0.08	2.36	(a);(19)
N2110	isolated	39.11 ± 0.09	-0.47 ± 0.12	0.00	39.11 ± 0.09	-0.47 ± 0.12	1.61	39.11 ± 0.09	2.43	(O);(20)
N3607	BGG:LeoII	39.80 ± 0.07	-0.35 ± 0.06	0.93	40.40 ± 0.36	-0.35 ± 0.07	1.69	41.36 ± 0.09	2.50	(f,v,d);(21)
N0224	BFG:LG	38.30 ± 0.12	-0.54 ± 0.05	0.00	38.30 ± 0.12	-0.54 ± 0.05	1.57	38.30 ± 0.12	2.39	(M,N);(22)
N1316	BGG:FornaxA	40.46 ± 0.05	-0.18 ± 0.04	1.20	40.64 ± 0.05	-0.17 ± 0.05	1.80	40.79 ± 0.05	2.59	(e);(23)
N1667	BFG:N1667	40.15 ± 0.18	-0.48 ± 0.08	0.90	40.15 ± 0.18	-0.48 ± 0.08	1.60	40.15 ± 0.18	2.42	(w);(24)
N5576	N5566	38.77 ± 0.21	-0.28 ± 0.19	0.60	38.77 ± 0.21	-0.28 ± 0.19	1.71	38.77 ± 0.21	2.53	(a);(25)
N1052	N0988	39.58 ± 0.09	-0.47 ± 0.05	0.70	39.58 ± 0.09	-0.47 ± 0.05	1.61	39.58 ± 0.09	2.43	(j);(26)
N4026	N4258(M106)	38.38 ± 0.27	-0.55 ± 0.20	0.30	38.38 ± 0.27	-0.55 ± 0.20	1.56	38.38 ± 0.27	2.39	(a);(27)
N3801	BFG:N3801	39.15 ± 0.30	-0.64 ± 0.19	1.23	39.15 ± 0.30	-0.64 ± 0.19	1.52	39.15 ± 0.30	2.34	(x);(28)
N4697	N4594(M104)	39.23 ± 0.08	-0.49 ± 0.06	0.88	39.23 ± 0.08	-0.49 ± 0.06	1.59	39.23 ± 0.08	2.42	(f);(29)
N1961	BGG:N1961	40.36 ± 0.09	-0.17 ± 0.05	1.15	40.62 ± 0.09	-0.21 ± 0.05	1.62	41.08 ± 0.17	2.57	(y);(30)
N3608	N3607(LeoII)	39.63 ± 0.09	-0.40 ± 0.09	1.00	39.63 ± 0.09	-0.40 ± 0.09	1.64	39.63 ± 0.09	2.47	(a);(31)
N3998	N4258(M106)	40.04 ± 0.12	-0.59 ± 0.09	0.30	40.04 ± 0.12	-0.59 ± 0.09	1.55	40.04 ± 0.12	2.37	(a);(32)
N3245	BFG:N3245	39.43 ± 0.16	-0.52 ± 0.10	0.95	39.43 ± 0.14	-0.52 ± 0.10	1.58	39.43 ± 0.14	2.40	(a);(33)
N3414	BFG:N3414	39.23 ± 0.16	-0.24 ± 0.16	0.60	39.23 ± 0.16	-0.24 ± 0.16	1.73	39.23 ± 0.16	2.55	(a);(34)
N3862	N3842	40.20 ± 0.10	-0.19 ± 0.11	0.48	40.20 ± 0.10	-0.19 ± 0.11	1.76	40.20 ± 0.10	2.58	(H);(35)
N5845	N5846	38.77 ± 0.25	-0.41 ± 0.21	0.60	38.77 ± 0.25	-0.41 ± 0.21	1.64	38.77 ± 0.25	2.46	(a);(36)
N3585	BFG:N3585	39.32 ± 0.10	-0.43 ± 0.10	1.15	39.32 ± 0.10	-0.43 ± 0.10	1.63	39.32 ± 0.10	2.45	(e);(37)
N7626	N7619(Pegasus)	40.40 ± 0.10	-0.16 ± 0.06	0.70	40.40 ± 0.10	-0.16 ± 0.06	1.77	40.40 ± 0.10	2.59	(c);(38)
N4636	BGG:N4636	41.04 ± 0.10	-0.21 ± 0.04	0.95	41.26 ± 0.09	-0.12 ± 0.04	1.49	41.88 ± 0.09	2.61	(e,b,d);(39)
N0541	N0547	40.63 ± 0.14	-0.26 ± 0.06	0.70	40.63 ± 0.14	-0.26 ± 0.06	1.72	40.63 ± 0.14	2.54	(k,B);(40)
N7052	isolated	41.26 ± 0.11	-0.25 ± 0.06	1.08	41.26 ± 0.11	-0.25 ± 0.06	1.72	41.26 ± 0.11	2.55	(c);(41)

Table 3
(Continued)

Galaxy Name (i)	Central Galaxy (ii)	$L_{x,g}$ log(erg s ⁻¹) (iii)	$T_{x,g}$ log(keV) (iv)	$R_{x,g}$ log(kpc) (v)	$L_{x,c}$ log(erg s ⁻¹) (vi)	$T_{x,c}$ log(keV) (vii)	$R_{x,c}$ log(kpc) (viii)	$L_{x,500}$ log(erg s ⁻¹) (ix)	R_{500} log(kpc) (x)	References and Notes (xi)
N4621	N4486/N4472	40.04 ± 0.52	-0.57 ± 0.12	1.00	40.04 ± 0.52	-0.57 ± 0.12	1.55	40.04 ± 0.52	2.38	(u,a);(42)
N4526	N4486/N4472	39.92 ± 0.56	-0.46 ± 0.06	1.00	39.92 ± 0.56	-0.46 ± 0.06	1.60	39.92 ± 0.56	2.44	(u);(43)
N4342	N4486/N4472	39.79 ± 0.05	-0.19 ± 0.04	1.15	39.79 ± 0.05	-0.19 ± 0.04	1.75	39.79 ± 0.05	2.58	(b);(44)
N0741	BGG:N0741	41.26 ± 0.09	-0.10 ± 0.05	1.18	41.49 ± 0.09	0.01 ± 0.04	1.93	42.23 ± 0.09	2.68	(c,b,d);(45)
N4552	N4486/N4472	40.30 ± 0.06	-0.23 ± 0.04	0.85	40.30 ± 0.06	-0.23 ± 0.04	1.74	40.30 ± 0.06	2.56	(a);(46)
N4261	N4303(M61)	40.88 ± 0.08	-0.12 ± 0.04	1.00	40.88 ± 0.08	-0.12 ± 0.04	1.79	40.88 ± 0.08	2.62	(a);(47)
N4291	BFG:N4291	40.91 ± 0.25	-0.23 ± 0.06	1.08	40.91 ± 0.25	-0.23 ± 0.06	1.73	40.91 ± 0.25	2.56	(v);(48)
N3665	BFG:N3665	40.23 ± 0.19	-0.35 ± 0.09	1.02	40.23 ± 0.19	-0.35 ± 0.09	1.67	40.23 ± 0.19	2.50	(f);(49)
N1374	N1316(ForA)	39.78 ± 0.05	-0.32 ± 0.10	0.78	39.78 ± 0.05	-0.32 ± 0.10	1.69	39.78 ± 0.05	2.51	(k,c);(50)
N0383	N0410	40.53 ± 0.10	-0.09 ± 0.05	0.78	40.53 ± 0.10	-0.09 ± 0.05	1.81	40.53 ± 0.10	2.63	(c);(51)
N6251	BGG:N6251	41.59 ± 0.13	-0.22 ± 0.08	1.26	41.75 ± 0.07	-0.08 ± 0.04	1.83	42.11 ± 0.31	2.64	(K,b,L);(52)
N4594	BGG:Sombrero	39.93 ± 0.08	-0.23 ± 0.14	1.18	40.51 ± 0.25	-0.20 ± 0.12	1.72	40.51 ± 0.25	2.57	(U,V,X);(53)
N1332	BGG:N1332	40.00 ± 0.09	-0.21 ± 0.04	0.54	40.32 ± 0.08	-0.27 ± 0.04	1.45	40.80 ± 0.09	2.54	(e,d);(54)
N5813	N5846	41.76 ± 0.07	-0.15 ± 0.04	1.23	41.76 ± 0.07	-0.15 ± 0.04	1.77	41.76 ± 0.07	2.60	(f);(55)
N0315	BGG:N0315	41.04 ± 0.13	-0.18 ± 0.05	0.85	41.30 ± 0.05	-0.12 ± 0.04	1.86	41.60 ± 0.15	2.62	(c,b,h);(56)
N5077	BFG:N5077	40.60 ± 0.20	-0.15 ± 0.07	1.04	40.60 ± 0.20	-0.15 ± 0.07	1.77	40.60 ± 0.20	2.60	(k,c);(57)
N0524	BGG:N0524	40.11 ± 0.10	-0.30 ± 0.07	0.85	40.62 ± 0.09	-0.19 ± 0.06	1.75	40.95 ± 0.09	2.58	(a,d);(58)
N1399	BCG:Fornax	40.94 ± 0.05	-0.05 ± 0.04	0.90	41.46 ± 0.05	0.09 ± 0.04	1.54	42.52 ± 0.04	2.73	(e,i);(59)
N3115	isolated	39.70 ± 0.24	-0.30 ± 0.05	0.95	39.70 ± 0.24	-0.30 ± 0.05	1.70	39.70 ± 0.24	2.52	(k,u);(60)
IC1459	BGG:IC1459	40.04 ± 0.14	-0.21 ± 0.05	0.70	40.52 ± 0.12	-0.22 ± 0.06	1.59	41.45 ± 0.12	2.56	(e,d);(61)
N4374	N4486/N4472	40.66 ± 0.06	-0.12 ± 0.04	1.00	40.66 ± 0.06	-0.12 ± 0.04	1.79	40.66 ± 0.06	2.62	(f);(62)
N5846	BGG:N5846	41.43 ± 0.09	-0.19 ± 0.04	1.18	41.64 ± 0.09	-0.12 ± 0.05	1.78	42.08 ± 0.09	2.62	(e,d);(63)
N1277	N1275(Perseus)	40.15 ± 0.11	0.01 ± 0.05	0.30	40.15 ± 0.11	0.01 ± 0.05	1.86	40.15 ± 0.11	2.68	(T);(64)
IC4296	BCG:A3565	41.23 ± 0.07	-0.16 ± 0.05	1.00	41.83 ± 0.11	0.06 ± 0.06	2.00	42.00 ± 0.08	2.71	(l,m);(65)
N7768	BFG:A2666	41.84 ± 0.31	-0.05 ± 0.08	1.48	41.84 ± 0.31	-0.05 ± 0.08	1.83	41.84 ± 0.31	2.66	(k,c);(66)
U12064	BFG:3C449	41.04 ± 0.09	0.00 ± 0.04	1.00	41.04 ± 0.09	0.00 ± 0.04	1.86	41.04 ± 0.09	2.68	(g);(67)
N6240S	isolated	41.49 ± 0.10	-0.06 ± 0.05	0.78	41.49 ± 0.10	-0.06 ± 0.05	1.82	41.49 ± 0.10	2.65	(z);(68)
N6861	N6868(Tel.)	40.74 ± 0.15	-0.03 ± 0.04	1.49	40.74 ± 0.15	-0.03 ± 0.04	1.84	40.74 ± 0.15	2.67	(n);(69)
N4649	N4486/N4472	40.94 ± 0.05	-0.04 ± 0.04	1.04	40.94 ± 0.05	-0.04 ± 0.04	1.83	40.94 ± 0.05	2.66	(f);(70)
N7619	BGG:Pegasus	41.48 ± 0.13	-0.03 ± 0.04	1.46	42.41 ± 0.13	0.00 ± 0.04	2.20	42.65 ± 0.13	2.68	(n,o);(71)
N4472	BCG ₁ :Virgo	41.18 ± 0.07	0.02 ± 0.04	1.20	43.08 ± 0.05	0.30 ± 0.05	1.86	43.38 ± 0.05	2.84	(f,p,q);(72)
N3923	BGG:N3923	40.43 ± 0.12	-0.26 ± 0.05	1.00	40.60 ± 0.11	-0.24 ± 0.04	1.62	40.92 ± 0.25	2.55	(e,b,d);(73)
N3091	BGG:HCG42	41.34 ± 0.15	-0.10 ± 0.04	1.00	41.68 ± 0.15	-0.06 ± 0.04	1.90	42.08 ± 0.15	2.65	(g,d,b);(74)
N1550	BGG:N1550	42.32 ± 0.10	0.11 ± 0.04	1.45	43.04 ± 0.10	0.14 ± 0.04	2.28	43.20 ± 0.11	2.75	(n,r,i);(75)
N6086	BGG:A2162	41.43 ± 0.17	0.00 ± 0.08	1.70	42.48 ± 0.17	0.18 ± 0.07	2.45	42.59 ± 0.18	2.77	(S);(76)
A1836B	BCG:A1836	41.51 ± 0.08	0.18 ± 0.09	1.41	42.54 ± 0.05	0.22 ± 0.05	2.11	42.70 ± 0.10	2.80	(P);(77)

Table 3
(Continued)

Galaxy Name (i)	Central Galaxy (ii)	$L_{x,g}$ log(erg s ⁻¹) (iii)	$T_{x,g}$ log(keV) (iv)	$R_{x,g}$ log(kpc) (v)	$L_{x,c}$ log(erg s ⁻¹) (vi)	$T_{x,c}$ log(keV) (vii)	$R_{x,c}$ log(kpc) (viii)	$L_{x,500}$ log(erg s ⁻¹) (ix)	R_{500} log(kpc) (x)	References and Notes (xi)
N1407	BGG:Eridanus	41.94 ± 0.11	0.08 ± 0.06	1.23	42.00 ± 0.11	0.08 ± 0.06	2.03	42.08 ± 0.11	2.72	(s);(78)
N5328	BGG:N5328	41.08 ± 0.12	-0.07 ± 0.11	1.08	41.67 ± 0.11	-0.02 ± 0.20	2.03	41.80 ± 0.11	2.67	(I,k);(79)
M1216	isolated	41.83 ± 0.12	-0.10 ± 0.05	1.04	41.83 ± 0.12	-0.10 ± 0.05	1.80	41.83 ± 0.12	2.63	(A);(80)
N4486	BCG ₂ :Virgo	42.26 ± 0.06	0.15 ± 0.05	0.95	43.08 ± 0.05	0.30 ± 0.05	1.86	43.38 ± 0.05	2.84	(l,p,q);(81)
N5419	BCG:AS753	41.53 ± 0.12	0.27 ± 0.05	1.28	42.26 ± 0.14	0.32 ± 0.04	2.32	42.52 ± 0.12	2.85	(t);(82)
N3842	BCG:A1367	41.78 ± 0.18	0.12 ± 0.06	1.68	43.93 ± 0.11	0.51 ± 0.04	2.58	44.06 ± 0.12	2.95	(k,c,D,i,E);(83)
N1600	BGG:N1600	41.30 ± 0.11	0.16 ± 0.07	1.32	41.52 ± 0.11	0.21 ± 0.09	1.75	41.52 ± 0.11	2.79	(ë);(84)
N4889	BCG:Coma	42.78 ± 0.07	0.38 ± 0.16	1.32	44.51 ± 0.07	0.86 ± 0.06	2.56	44.88 ± 0.06	3.14	(k,Y,Z,ä);(85)

Note. (4, 13, 20) Cooler component of the 2-T thermal plasma fit (the hotter one driven by a starburst or jet-driven shock). (23, 30, 37, 39, 54, 59, 61, 63, 73, 77, 78, 80, 82, 84) L_x and/or T_x retrieved via the integration of the plasma density (emissivity) profile and/or LW temperature profile within the given R_x (avoiding extrapolations). (28) Only the diffuse ISM component is considered (excluding the shock-heated lobes). (50, 57, 66, 76) Temperature available only via the $L_x - T_x$ relation (Goulding et al. 2016; full aperture). (65, 76, 77) $L_{x,500}$ newly retrieved via archival ROSAT data by using Eckert et al. (2012) procedure. (71) BGG of LGG 473 (Lyon Galaxy Group catalog). (72, 81) N4472 and N4486 are equally massive and central to Virgo cluster. *Columns.* (i) Galaxy name, with prefixes defined as N = NGC (New General Catalogue); IC (Index Catalogue); A = Abell Catalogue; M = Mrk (Markarian Catalogue); U = UGC (Uppsala General Catalogue). Top to bottom: galaxies are in order of ascending M_* . (ii) Central galaxy of the macro-scale cluster, group, or field halo (from Tully 2015 PGC1 catalog and (xi) references); whenever matching the considered galaxy, we label it “brightest cluster/group/field galaxy” (BCG/BGG/BFG) of the related macro-scale halo (e.g., “BGG: Pegasus”). Clusters typically have $N_m \sim 50-1000$; groups $N_m \sim 8-50$; fields $N_m \sim 2-8$; galaxies with $N_m \leq 2$ are labeled as “isolated” (which includes pairs). (iii) X-ray luminosity (0.3–7 keV) of the hot halo within the galactic/CGM radius. (iv) X-ray temperature within the galactic/CGM radius. (v) Galactic/CGM radius ($\sim 1-3 R_e$). (vi) X-ray luminosity (0.3–7 keV) of the hot halo within the core radius (different from (iii) only for BCGs/BGGs). (vii) X-ray temperature within the core radius (analog of $T_{x,500}$ and group/cluster virial temperature; different from (iv) only for BCGs/BGGs). (viii) Group/cluster core radius ($\sim 0.15 R_{500}$). (ix) X-ray luminosity (0.3–7 keV) of the hot halo within the macro-scale cluster/group halo ($\sim R_{500}$; different from (iii) only for BCGs/BGGs). (x) Group/cluster R_{500} ($\simeq R_{\text{vir}}/1.7$). (xi) References used for the listed X-ray properties and single-object notes (if any).

References. (a) Kim & Fabbiano (2015); (b) Babyk et al. (2018); (c) Goulding et al. (2016); (d) Osmond & Ponman (2004); (e) Nagino & Matsushita (2009); (f) Su et al. (2015); (g) Lakhchaura et al. (2018); (h) Helsdon & Ponman (2000); (i) Reiprich & Böhringer (2002); (j) Boroson et al. (2011); (k) O’Sullivan et al. (2001); (l) Athey (2007); (m) Horner (2001); (n) Fukazawa et al. (2006); (o) O’Sullivan et al. (2017); (p) Peres et al. (1998); (q) Urban et al. (2011); (r) Sun et al. (2003); (s) Su et al. (2014); (t) Eckmiller et al. (2011); (u) Diehl & Statler (2008); (v) O’Sullivan et al. (2003); (w) LaMassa et al. (2012); (x) Croston et al. (2007); (y) Anderson et al. (2016); (z) Grimes et al. (2005); (A) Buote & Barth (2019); (B) Bogdán et al. (2011); (C) Li & Wang (2013); (D) Hudson et al. (2010); (E) Ebeling et al. (1996); (F) Tyler et al. (2004); (G) Gallo et al. (2006); (H) Sun et al. (2007); (I) Trinchieri et al. (2012); (J) Wang et al. (2010); (K) Gliozzi et al. (2004); (L) Mulchaey et al. (2003); (M) Supper et al. (2001); (N) Liu et al. (2010); (O) Evans et al. (2006); (P) Stawarz (2014); (Q) Swartz et al. (2003); (R) Konami et al. (2009); (S) Burns et al. (1994); (T) Fabian et al. (2013); (U) Pellegrini et al. (2002); (V) Li et al. (2007); (X) Benson et al. (2000); (Y) Sanders et al. (2014); (Z) White et al. (1997); (ä) Mittal et al. (2011); (ë) Sivakoff et al. (2004).

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