

## Probabilistic Seismic Analyses of Earthen Levees with Finite Element Modeling

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**Abstract:** Earthen levees are critical civil infrastructure of coastal regions for flood protection. Earthquake can cause significant deformation and damage to earthen levees. Seismic performance of such levees under the earthquake hazards is a major concern in their safety evaluation. However, there are significant uncertainties in assessing the seismic behavior of earthen levees and geotechnical uncertainties play a critical role in the probabilistic assessment of earthquake-induced deformation and failures. This paper presents a simplified probabilistic framework for assessing the seismic performance of earthen levees with dynamic analysis and finite element modeling. In this framework, the effects of geotechnical uncertainties are explicitly considered in the uncertainty propagation for probabilistic evaluation of seismic deformations of earthen levees under earthquake hazards. The probability curves are developed to describe the correlations among the probability of exceedance, limiting deformation value, and input peak ground acceleration. The derived probability curves can provide valuable information for risk assessment and risk-informed decision-making of earthen levee infrastructure. The effectiveness of the proposed probabilistic framework is demonstrated through a case study of earthen levee example.

29

30      **Keywords:** Displacement; Earthen Levee; Earthquake; Finite Element Method; Uncertainty.

31        **Introduction**

32            Earthen levees are critical civil infrastructure protecting coastal regions for flood hazards  
33            due to various drives such as coastal water level, precipitation, and river discharge (Jasim et al.  
34            2020). It is estimated that there are over 100,000 miles of levees in the United States  
35            (Zevenbergen et al. 2017). Many of the levees have lived out their design life, and some are over  
36            100 years old. The safety evaluation of the earthen levees under hazard conditions is a major  
37            concern to prepare the infrastructure for the disaster resilience, especially for those located in the  
38            seismically active zone. For example, the levee system in the Sacramento-San Joaquin Delta,  
39            which protects one of the most at-risk regions in the United States for catastrophic flooding, is  
40            also highly susceptible to earthquake-induced damage and failure. Thus, it is critical to evaluate  
41            the reliability of earthen levees in the face of earthquake hazards since the failure of such  
42            structures can be catastrophic and cause loss of lives, damage to properties, and significant  
43            adverse economic and societal impacts.

44            The earthquake-induced deformation and damages to earthen levees due to expected  
45            ground shaking levels are difficult to predict due to a variety of factors, and geotechnical  
46            variability is an important contributing factor to the variability of earthquake-induced  
47            deformations. The stability and performance of the slopes and levees have been investigated by  
48            many researchers using deterministic methods including pseudo-static analysis, permanent-  
49            displacement analysis, and stress-deformation analysis (Newmark 1965; Sarma et al. 1975;  
50            Makdisi and Seed 1978; Rathje and Bray 2000; Jibson 2011; Stark et al. 2012; Wang et al. 2021).  
51            Among these methods, stress-deformation analysis can utilize dynamic methods such as dynamic  
52            finite element and finite difference methods to incorporate sophisticated soil-constitutive models  
53            in evaluating the stress-strain behavior of soil slopes (Jibson 2011). However, in such analysis,

54 significant uncertainties exist in the modeling of the dynamic soil behavior due to limited site  
55 investigation and difficulties to obtain high-quality samples for soil testing. Many existing  
56 probabilistic studies on the earthen levees and embankments focus on static analyses or using  
57 pseudo static methods in seismic analyses (Duncan 2000; Xiao et al. 2016; Wang et al. 2020;  
58 Zhang et al. 2022). In addition, when the seismic performance of levees is evaluated using stress-  
59 deformation analysis implemented in a numerical model without an explicit solution, the  
60 computational efforts of probabilistic seismic analyses could be challenging (Zhang et al. 2013).  
61 This paper aims to: 1) establish dynamic finite element models for evaluating the seismic  
62 performance of earthen levees; 2) develop a probabilistic framework to explicitly consider the  
63 geotechnical uncertainties through the combined advanced reliability assessment and numerical  
64 methods; 3) demonstrate the efficiency and effectiveness of the proposed methods with a case  
65 study for earthen levees. The probabilistic framework is formulated using an efficient reliability  
66 method that accounts for the propagation of uncertainties from the input random variables  
67 through the dynamic finite element modeling. The derived probability curves can provide useful  
68 references for more informed decision-making for the stakeholders in risk management of levees.  
69 A case study is utilized to demonstrate the effectiveness of the proposed probabilistic framework  
70 in assessing the seismic performance of earthen levees.

## 72 **Dynamic Analysis of Earthen Levees**

73 Finite element method (FEM) and finite difference method (FDM) are widely employed  
74 in predicting the performance of earthen levees under earthquake loads. These methods involve  
75 dividing the entire model domain into deformable sub-domains and calculating the stress and  
76 strain at the connected nodes. The dynamic analysis implemented in the finite element method,

77 namely the dynamic finite element method, is employed in this study, which can accurately  
78 simulate complex geological conditions and soil behaviors under dynamic loads. The dynamic  
79 finite element method enables seismic geotechnical analyses of the propagation of waves through  
80 the soil and their impacts on geotechnical structures. The ground motion data will be used to  
81 evaluate the levee's seismic response, which can determine the deformation characteristics of the  
82 levee over the time history. The numerical model for analyzing the earthen levee performance is  
83 built using the finite element program PLAXIS 2D under the plane-strain condition. In the  
84 dynamic analysis, the Hardening Soil Model with Small Strain Stiffness (HS Small) is utilized  
85 for modeling the soil behavior. The model is a built-in constitutive model in PLAXIS 2D for  
86 seismic geotechnical analyses. The HS Small model can capture the nonlinear and inelastic  
87 stress-strain behavior of both stiff and soft soils, especially for the nonlinear stiffness decay at  
88 the small strain levels. The hysteretic damping subjected to cyclic shear loading is also  
89 considered in the HS Small model (Brinkgreve et al. 2007). Compared with the classic hardening  
90 soil model, two additional parameters are used to model the variation of stiffness with strain,  
91 including the initial shear modulus  $G_0$  and the shear strain level at which the secant shear  
92 modulus  $G_s$  is reduced to approximately 70% of  $G_0$  (Brinkgreve et al. 2017). In the dynamic  
93 finite element analysis, since the dynamic motion is applied to the base of soil deposits, a  
94 compliant base boundary condition is applied at the bottom boundary and free-field boundary  
95 conditions are applied at the lateral boundary of the model (e.g., the left and right sides of the  
96 model as shown in Figure 1). The fine mesh is used for modeling with enhanced mesh  
97 refinement at the embankment section.

98

99 **Probabilistic Framework for Seismic Performance of Earthen Levees**

100 Here a probabilistic framework for seismic performance of levees is developed by  
101 combining the advanced reliability theory and the dynamic finite element modeling. In this paper,  
102 the deformation characteristics of levees under various earthquake hazard levels in terms of peak  
103 ground acceleration will be assessed using a quantitative probabilistic assessment framework.  
104 The probabilistic framework includes four steps as follows: 1) uncertainty characterization of  
105 input parameters for the dynamic analyses; 2) establishment of a deterministic numerical model;  
106 3) uncertainty propagation using advanced moment methods combined with point estimate  
107 method (PEM); 4) derivation of probabilistic curves for decision-making.

108 The probability of levee damage under the given earthquake hazard can be evaluated  
109 using the probability of exceedance, which is the probability that the predicted maximum  
110 displacement of the levee ( $D_{\max}$ ) exceeds a given limiting displacement threshold value ( $D_{\lim}$ ).  
111 The maximum permanent displacement of the earthen levee is evaluated using the dynamic finite  
112 element method. Then the performance function, denoted as  $G$ , for determining the probability of  
113 exceedance can be written as:

$$114 \quad G = D_{\lim} - D_{\max} \quad (1)$$

115 where the levee is safe if the obtained performance function  $G$  is greater than 0 (i.e.,  $D_{\lim} > D_{\max}$ ).

116 The probability of exceedance can be determined using an advanced point estimate  
117 method (PEM). Here the PEM method uses selected five points sampled from the probability  
118 distribution function to estimate the four moments of the performance function, namely the mean,  
119 standard deviation, skewness, and kurtosis. The accuracy of the advanced point estimate method  
120 has been demonstrated with many engineering examples (Zhao and Ono 2000&2001).

121 In the PEM procedure, the estimating points are obtained from the space of standard  
122 normal distribution. For other probability distributions, the Rossenblatt transformation can be

123 used to transform estimating points in the original space ( $x_j$ ) into the counterparts in the standard  
 124 normal space ( $u_j$ ). The Hermite integration can then be used to obtain the estimated points and  
 125 their corresponding weights in the standard normal space, which can be used to evaluate the  $k^{\text{th}}$   
 126 central moment of a function in the original space,  $y = y(x)$  using the following equation (Zhao  
 127 and Ono 2000):

$$128 \quad \mu_y = \sum_{j=1}^m P_j y[T^{-1}(u_j)] \quad (2)$$

$$129 \quad M_{ky} = \sum_{j=1}^m P_j (y[T^{-1}(u_j)] - \mu_y)^k \quad (3)$$

130 where  $\mu_y$  is the mean value,  $M_{ky}$  is  $k^{\text{th}}$  dimensionless central moment of  $y(x)$ ,  $T^{-1}$  is the inverse  
 131 Rosenblatt transformation.  $u_1, u_2, u_3, \dots, u_m$  are the estimating points and  $P_1, P_2, \dots, P_m$  are the  
 132 corresponding weights.

133 For the levee problem with multiple uncertain parameters as input random variables  
 134 (assuming  $N$  uncertain input parameters for illustration purpose), and the performance function  
 135 can be written as  $G = G(\mathbf{Z}) = G(Z_1, Z_2, Z_3, \dots, Z_N) = D_{\text{lim}} - D_{\text{max}}(Z_1, Z_2, Z_3, \dots, Z_N)$ , where  $G(\mathbf{Z})$  is  
 136 the performance of the levee for evaluating the probability of exceedance. Since there is no  
 137 explicit solution for evaluating the seismic performance, the PLAXIS 2D model is treated as the  
 138 implicit performance function in the proposed probabilistic framework. The performance  
 139 function is a function of all the uncertain input parameters, which will be evaluated based on the  
 140 uncertainty propagation through the dynamic finite element modeling to obtain  $D_{\text{max}}$  under the  
 141 given earthquake loading.

142 The four moments of  $G = G(\mathbf{Z}) = G(Z_1, Z_2, Z_3, \dots, Z_N)$  can be evaluated following the  
 143 below equations:

$$144 \quad \mu_G = (\mu_1 - G_\mu) + (\mu_2 - G_\mu) + \dots + (\mu_N - G_\mu) + G_\mu \quad (4)$$

145 
$$\sigma_G^2 = \sigma_1^2 + \sigma_2^2 + \dots + \sigma_N^2 \quad (5)$$

146 
$$\alpha_{3G}\sigma_G^3 = \alpha_{31}\sigma_1^3 + \alpha_{32}\sigma_2^3 + \dots + \alpha_{3N}\sigma_N^3 \quad (6)$$

147 
$$\alpha_{4G}\sigma_G^4 = \alpha_{41}\sigma_1^4 + \alpha_{42}\sigma_2^4 + \dots + \alpha_{4N}\sigma_N^4 + 6 \sum_{i=1}^{N-1} \sum_{j>1}^N \sigma_i^2 \sigma_j^2 \quad (7)$$

148 where  $G_\mu$  is the performance function  $G(Z_1, Z_2, Z_3, \dots, Z_N)$  evaluated at the mean of input random  
 149 variables ( $Z_1, Z_2, Z_3, \dots, Z_N$ );  $\mu_1, \sigma_1, \alpha_{31}, \alpha_{41}$  are the mean, standard deviation, skewness  
 150 coefficient and kurtosis coefficient of  $G(Z_1, Z_2 = \mu_2, Z_3 = \mu_3, \dots, Z_N = \mu_N)$  evaluated with only one  
 151 random variable  $Z_1$  using Eq. (2) and Eq. (3).  $\mu_2, \sigma_2, \alpha_{32}, \alpha_{42}, \mu_3, \sigma_3, \alpha_{33}, \alpha_{43}$  and  $\mu_N, \sigma_N, \alpha_{3N}, \alpha_{4N}$   
 152 can be evaluated using the similar procedures. Based on the above results, the four moments of  
 153 the performance function of the earthen levee problem can then be evaluated using Eqs. (4-7).  
 154 By correlating the probability of exceedance with central moments using different formulations  
 155 (Zhao and Ono 2001; Ang and Tang 2007), the moment methods can be employed to assess the  
 156 probability of exceedance for the given earthquake load (e.g., in term of peak ground  
 157 acceleration). Three moments methods, namely, Second moment (SM) method, Third Moment  
 158 (TM) method, and Fourth Moment (FM) method are described. The main difference of three  
 159 moments methods lies in their difference in the approximation of the distribution of the  
 160 performance function using different orders of the moment. The third moment method can  
 161 consider asymmetric random variables by introducing a three-parameter lognormal distribution,  
 162 and a higher-order moments standardization technique (HOMST) is utilized in the fourth  
 163 moment formulation (Zhao and Ono 2001).

164 The second moment method has the same basic principle with the First-order second  
 165 moment method (Ang and Tang 2007). The following equation can be used to evaluate the  
 166 reliability index and probability of exceedance:

167 
$$\beta_{SM} = \frac{\mu_G}{\sigma_G} \quad (8)$$

168 
$$P_{E-SM} = \Phi(-\beta_{SM}) \quad (9)$$

169 where  $\mu_G$  and  $\sigma_G$  are the mean and standard deviation of  $G = G(\mathbf{Z})$ , respectively;  $\Phi(\cdot)$  is the  
170 standard normal cumulative distribution function.

171 For the third moment method, the standardized variable of the performance function  $G =$   
172  $G(\mathbf{Z})$  is considered to follow the three-parameter lognormal distribution (Tichy 1994):

173 
$$Z_u = \frac{Z - \mu_G}{\sigma_G} \quad (10)$$

174 The intermediate variable in terms of a standard normal random variable  $u$ , for evaluation  
175 of reliability index, is expressed as a function of first three moments of the performance function  
176 as (Tichy 1994; Zhao and Ono 2001):

177 
$$u = \frac{\text{sign}(\alpha_{3G})}{\sqrt{\ln(A)}} \ln \left[ \sqrt{A} \left( 1 - \frac{Z_u}{u_b} \right) \right] \quad (11)$$

178 where  $A$  and  $u_b$  are functions of  $\alpha_{3G}$  based on formulations documented in Zhao and Ono (2001).

179 Following the formulation of third moment method (Tichy 1994), the reliability index  
180 and probability of exceedance are determined as:

181 
$$\beta_{TM} = \frac{-\text{sign}(\alpha_{3G})}{\sqrt{\ln(A)}} \ln \left[ \sqrt{A} \left( 1 + \frac{\beta_{SM}}{u_b} \right) \right] \quad (12)$$

182 
$$P_{E-TM} = \Phi(-\beta_{TM}) \quad (13)$$

183 The fourth moment method is built upon the principle of high-order moment  
184 standardization (Ono and Idota 1986), the standard normal variable can be expressed using the  
185 following equation (Zhao and Ono 2001):

186

$$u = \frac{\alpha_{3G} + 3(\alpha_{4G} - 1)z_u - \alpha_{3G}z_u^2}{\sqrt{(5\alpha_{3G}^2 - 9\alpha_{4G} + 9)(1 - \alpha_{4G})}} \quad (14)$$

187 The reliability index and probability of exceedance can be evaluated using the  
188 formulation documented by Ono and Idota (1986) as:

189

$$\beta_{FM} = \frac{3(\alpha_{4G} - 1)\beta_{SM} + \alpha_{3G}(\beta_{SM}^2 - 1)}{\sqrt{(9\alpha_{4G} - 5\alpha_{3G}^2 - 9)(\alpha_{4G} - 1)}} \quad (15)$$

190

$$P_{E-FM} = \Phi(-\beta_{FM}) \quad (16)$$

191

192 **Example Application**

193 This section uses a case study of an existing earthen levee to demonstrate the  
194 probabilistic seismic assessment framework. The studied levee is adapted from a real levee built  
195 in 1990s for flood protection, which runs along a parking lot holding back a substantial area  
196 including wetlands. The earthen levee is built on top of a permanent soil foundation and  
197 composed of three types of geotechnical materials (i.e., embankment soil, rockfill zone, and No.  
198 57 stone). The representative cross section of the levee is shown in Figure 1. The widths of the  
199 levee base and crown are 16.4 m and 0.3 m, respectively. The height of the levee is 3.35 m, and  
200 both sides of the levee have a slope ratio of 2:1 (horizontal to vertical). The rockfill zone has a  
201 base width of 6.7 m and a height of 2.1 m. The water level is 2.1 m above the ground level,  
202 which corresponds to a flood hazard of a 100-year returning period. The groundwater table of the  
203 downstream side is 0.6 m below the ground level according to subsurface exploration results. A  
204 total of eight borings were drilled at the crown and toe of representative levee sections to  
205 estimated depths of 6 to 9 m. Nine undisturbed soil samples (Shelby tube samples) were obtained,  
206 and disturbed soil samples (split-spoon samples) were taken at regular intervals. Twenty-four

207 sieve analysis and Atterberg limits tests were performed for selected disturbed soil samples. Two  
208 direct shear tests and one consolidation test were performed for selected undisturbed soil samples.  
209 The results from field exploration and laboratory testing are used to estimate the strength  
210 parameters of soils and the geotechnical parameters for each layer of the earthen levee used in  
211 the analysis are listed in Table 1.

212

### 213 **Finite element modeling for the seismic performance of earthen levee**

214 Firstly, a deterministic analysis using the dynamic finite element modeling is performed  
215 to assess the seismic performance of the earthen levee. Since the earthen levee of concern is a  
216 long linear infrastructure, it can be well analyzed using 2D finite element modeling in a plane  
217 strain configuration. Constitutive behaviors of each soil layer are modeled using the HS small  
218 model with corresponding soil parameters listed in Table 1. The earthquake loading is applied to  
219 the bottom boundary of the model. The input ground motion is obtained from the 1990  $M_w$  5.7  
220 Upland Earthquake in California, USA. It is a left-lateral strike-slip earthquake that occurred  
221 west of the San Andreas Fault Systema with a maximum Mercalli Intensity of VII. The input  
222 ground motion is the North-South component of the ground motions recorded during the 1990  
223 Upland Earthquake. The peak ground acceleration (PGA) of the input ground motion is 0.24 g.  
224 The acceleration time history of the input ground motion and its Fourier amplitude spectrum are  
225 shown in Figures 2 and 3, respectively. In the dynamic analysis, the input ground motion is  
226 applied to the base of the FEM model, which is taken from rock outcropping motion.

227 One of the main concerns in the seismic assessment of earthen levees is to evaluate the  
228 damage levels based on the permanent deformation, which is related to the crack and subsidence  
229 of the levee (Kwak et al. 2016). In this paper, the maximum permanent total displacement from

230 the dynamic finite element modeling is used as a performance indicator to evaluate the  
231 probability of damage due to the earthquake load. Allowable permanent displacement is decided  
232 by damage levels of levee structures under different permanent displacements. For example, a  
233 limiting displacement value of 10 cm is typically used for classification between slight damage  
234 and moderate damage, while a limiting displacement value of 30-50 cm is typically used to  
235 distinguish between moderate damage and severe damage. A displacement of more than 100 cm  
236 generally indicates the levee collapse. The limiting deformation values are adapted from the  
237 study by Kwak et al. (2016) based on the post-earthquake reports for the levee segments  
238 throughout the Shinano River System.

239 Figure 4 shows the contour map of the permanent displacement of the levee, which is  
240 residual displacement at the end of the shaking. The land side of the earthen levee has a larger  
241 displacement than the flooding side. The maximum deformation contour passes through the crest  
242 to the toe of the levee in the land side. The maximum permanent displacement is 7.9 cm, which  
243 occurs around the top of the land side.

244 Five measurement points (i.e., the levee top-left, levee top-right, levee bottom-left, levee  
245 bottom-right, and middle-bottom points) are selected to monitor the time history of seismic  
246 response of the levee under the earthquake impacts (see Figure 1). The time histories of  
247 horizontal (X-direction) acceleration, velocity, and displacement of the five measurement points  
248 are shown in Figures 5-7, respectively. Figure 5 shows that the levee's top-left and top-right  
249 points generally have the highest horizontal peak acceleration. A similar trend is also observed  
250 for the horizontal peak velocity as shown in Figure 6. However, the horizontal velocity tends to  
251 converge at the end of the time history compared with the horizontal acceleration. The maximum  
252 transient velocity of the levee is 0.233 m/s occurs at 2.8 s located on the top-right of the levee.

253 The maximum transient horizontal displacement of the levee is 0.138 m occurs at 7.2 s located  
254 on the bottom-left of the levee, and the maximum permanent (residual) horizontal displacement  
255 of the levee is 0.068 m located on the bottom-left of the levee. The resulting time history profile  
256 of horizontal displacement also indicates a larger deformation on the land side.

257

258 **Probabilistic seismic assessment of earthen levee**

259 In this section, the probabilistic seismic assessment of the example earthen levee is  
260 conducted by evaluating the probability of exceedance, which is in terms of the probability of  
261 exceeding an allowable permanent displacement value. In the probabilistic assessment,  
262 uncertainties in the strength and permeability parameters of each material layers of the levee are  
263 considered. The mean values of the soil parameters of each layer adopt the values reported in  
264 Table 1 and the coefficient of variation of these parameters are estimated based on the published  
265 literature (e.g., Phoon and Kulhawy 1999; Luo and Hu 2018; Wang et al. 2018). The statistics of  
266 uncertain soil parameters used in the probabilistic analyses are listed in Table 2 and it should be  
267 noted that the coefficient of variation (COV) of the permeability coefficient represents the COV  
268 of the permeability coefficient in its logarithmic form. The uncertainties in these parameters are  
269 propagated into the dynamic finite element modeling through the moments method formulation  
270 in evaluating the probability of exceedance.

271 In the evaluating of the probability of exceedance, a limiting displacement value needs to  
272 be specified, which is related to the desired performance of the levee under the given earthquake  
273 load. For demonstration purpose, a limiting permanent displacement value of 30 cm is used in  
274 the evaluation of the probability of exceedance. Using any of the moment method, the  
275 probability of exceedance evaluated under the given ground motion (PGA = 0.24 g) for a

276 limiting displacement of 30 cm is 13.4%. Repeating this process with each of a series of limiting  
277 displacement values ranged between 5 cm to 100 cm, a probability of exceedance curve for this  
278 levee under the given ground motion is obtained, as shown in Figure 8. As can be found from  
279 Figure 8, the second moment (SM) method, third moment (TM) method, and fourth moment  
280 (FM) method generally yield similar results for the calculated probability of exceedance. For  
281 demonstration purposes, all the afterward probability of exceedance evaluations adopt the third  
282 moment method. It can be found that the probability of exceedance generally decreases with the  
283 increase in the limiting displacement values, which is expected since the less stringent  
284 performance requirement will reduce the probability of violating that requirement. The  
285 probability of exceedance curve under the given ground motion can provide a useful reference to  
286 evaluate the damage potential based on different limiting displacement values. The probability of  
287 exceedance under different limiting values can be readily obtained using Figure 8 to assess the  
288 probability in terms of different damage levels. For example, from Figure 8, it is found that the  
289 levee has a considerable probability of exceedance for a limiting displacement of 10 cm, which  
290 indicates a good possibility for slight damage. The probability of exceedance for a limiting  
291 displacement of 100 cm, which indicates levee collapse, is almost negligible.

### **PGA Effects on probability of exceedance curves**

294 To evaluate the PGA effects on the probability of exceedance curves, we scale the  
295 acceleration time history in Figure 2 to different PGA values, and repeat the probabilistic  
296 analyses in the previous section using scaled input ground motions. The probability of  
297 exceedance curves under different PGA levels are shown in Figure 9. Under all three PGA levels,  
298 the probability of exceedance generally decreases with the increase in the limiting displacement

299 value. It can be found that under the peak ground acceleration of 0.1 g, the probability of  
300 exceedance is less than 10% even with very stringent limiting displacement requirements (e.g., 5  
301 cm) and the probability of exceedance becomes negligible after 10 cm. However, when the peak  
302 ground acceleration is 0.6 g, the probability of exceedance for a limiting displacement of 10 cm  
303 is 87%, which indicates a very high likelihood of slight damage when a displacement exceeding  
304 10 cm is treated as the criteria for slight damage. Under the peak ground acceleration of 0.6 g,  
305 the probability of exceedance for a limiting displacement of 100 cm is about 5.8%, which  
306 suggests there could be about 5.8% chance for levee collapse under the high earthquake load  
307 when a displacement exceeding 100 cm is treated as the criteria for levee collapse.

308

309 **Effect of different limiting displacement values on the probability of exceedance**

310 In this paper, the susceptibility of the levee with regard to earthquake loads is expressed  
311 using the probability of exceedance versus the peak ground acceleration for the given limiting  
312 displacement value. Taking a limiting displacement value of 10 cm as an example, the  
313 probability of exceedance is evaluated at different peak ground acceleration levels and the  
314 resulting curve is illustrated in Figure 10. It can be found that the probability of exceedance  
315 steadily increases with the increase of the peak ground acceleration. However, the rate of  
316 increase is gradually reducing. Similar trends are also observed for the limiting displacement of  
317 30 cm, 50 cm, and 100 cm, respectively. The levee is very susceptible to slight damage with the  
318 increase of the earthquake load. However, it generally becomes less susceptible to the relaxed  
319 damage criteria (e.g., an increase in the limiting displacement value). For example, the  
320 probability of exceedance for 100 cm (indicating collapse) is less than 10% even under the high  
321 earthquake load. The results in Figure 10 can provide useful guidance for the decision makers to

322 consider the susceptibility of the levee with regard to earthquake loads under different damage  
323 criteria.

324

325 **Concluding Remarks**

326 This paper presents a probabilistic seismic assessment of the earthen levees using the  
327 finite element method and advanced moment method formulations. A deterministic dynamic  
328 finite element analysis of the earthen levee is first conducted based on the ground motions  
329 recorded during the 1990 Upland Earthquake in California. The resulting time histories of  
330 acceleration, velocity and displacement of represented locations are evaluated, and it is found  
331 that the maximum permanent displacement of the levee occurs in the land side of the levee. The  
332 results from the deterministic assessment are used as the basis for the probabilistic assessment. In  
333 the probabilistic assessment, the uncertainties in the geotechnical parameters are propagated  
334 through finite element simulations and the probability of exceedance curve can be readily  
335 derived to depict the relationship between the probability of exceedance with the limiting  
336 displacement value, in which different limiting displacement values correspond to different  
337 damage levels. The effects of different peak ground accelerations on the derived probability of  
338 exceedance curves are also obtained. Furthermore, the susceptibility of the levee with regard to  
339 earthquake loads is developed by expressing the probability of exceedance with respect to the  
340 increasing peak ground acceleration for the given limiting displacement requirement. It can be  
341 found that the probability of exceedance steadily increases with the increase of the peak ground  
342 acceleration for different limiting displacement values, and the results can help guide the  
343 evaluation of the susceptibility of the levee with regard to incremental earthquake loads. The  
344 effectiveness of the proposed approach is demonstrated with a case study of seismic assessment

345 of earthen levee. The proposed approach has the potential as a practical tool for seismic  
346 assessment and allows engineers to make more informed risk-based decisions in the face of  
347 earthquake hazards.

348

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353

354 **CONFLICT OF INTERESTS**

355 The authors declare that they have no known competing financial interests or personal  
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Table 1. Geotechnical parameters for the earthen levee for deterministic analysis

Parameter	Foundation Soil	Embankment Soil	Rock Fill Zone	No. 57 Stone
Unit weight, kN/m <sup>3</sup>	18.85	18.06	18.85	18.85
Secant stiffness in standard drained triaxial test, kN/m <sup>2</sup>	20000	20000	30000	30000
Tangent stiffness for primary oedometer loading, kN/m <sup>2</sup>	25610	25610	36010	36010
Unloading/reloading stiffness, kN/m <sup>2</sup>	94840	94840	110800	110800
Power for stress-level dependency of stiffness	0.5	0.5	0.5	0.5
Effective cohesion, kN/m <sup>2</sup>	1.2	1.2	1.2	0
Effective friction angle, °	32	30	30	36
Shear strain at which $G_s = 0.722G_0$	0.00012	0.00012	0.00015	0.00015
Shear modulus at very small strains, kN/m <sup>2</sup>	270000	270000	100000	100000
Poisson's ratio	0.2	0.2	0.2	0.2
Permeability coefficient, m/sec	0.000001	0.000001	0.00001	0.001

Table 2. Statistics of uncertain geotechnical parameters in probabilistic assessment (after Wang et al. 2018)

Uncertain Soil Parameter	Embankment Soil		Rockfill Zone		No. 57 Stone		Foundation Soil	
	Mean	COV	Mean	COV	Mean	COV	Mean	COV
Effective Cohesion (kN/m <sup>2</sup> )	1.2	10%	1.2	10%	0	-	1.2	10%
Effective Friction Angle (°)	30	15%	30	10%	36	10%	32	15%
Permeability coefficient (m/sec)	$1 \times 10^{-6}$	25%	$1 \times 10^{-5}$	25%	$1 \times 10^{-3}$	25%	$1 \times 10^{-6}$	25%

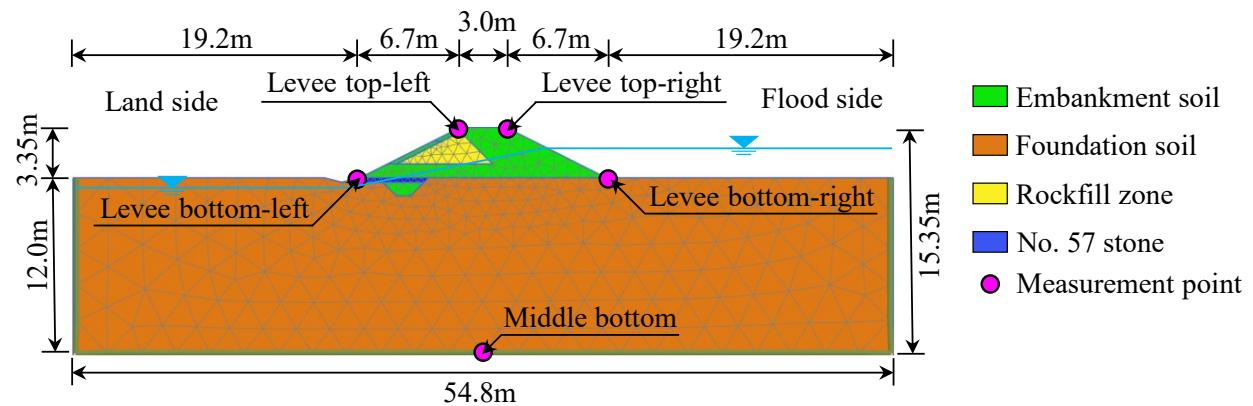


Figure 1: Illustration of the geometric layout of the earthen levee

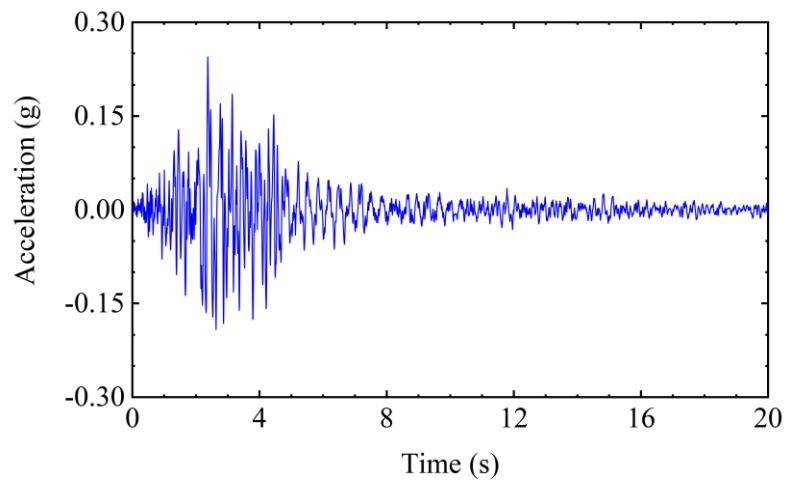


Figure 2. Acceleration time history of the input ground motion

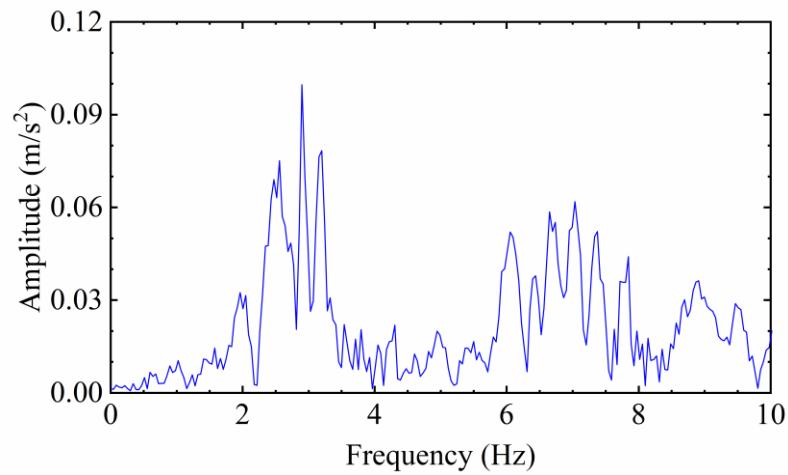


Figure 3. Fourier amplitude spectrum of the input ground motion

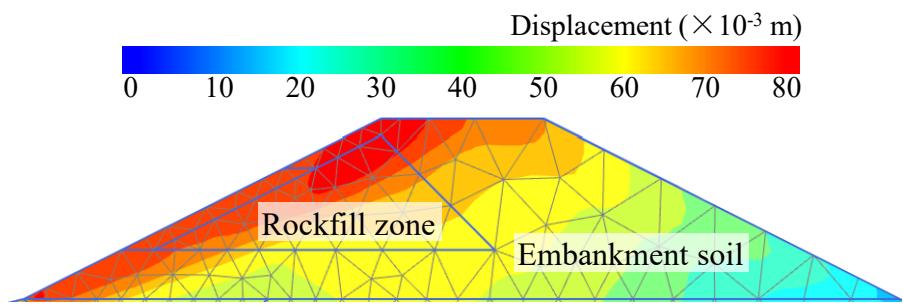


Figure 4. Contour plot of total permanent displacement of the levee at the end of shaking

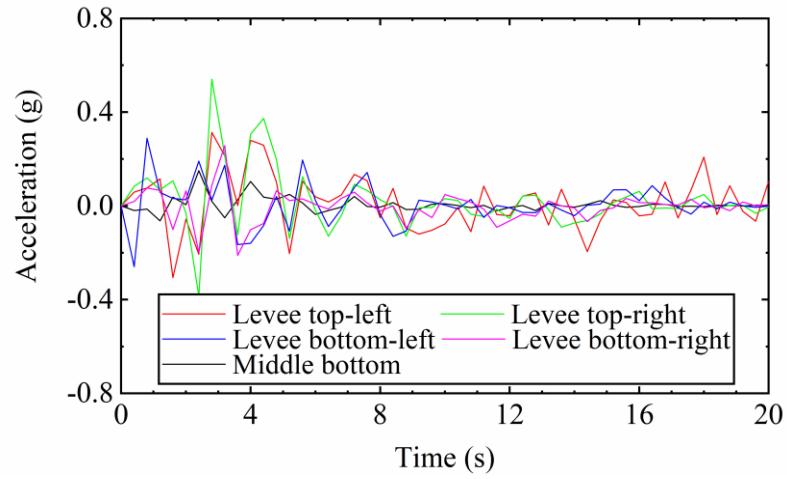


Figure 5. Horizontal acceleration time history on the five measurement points of the levee

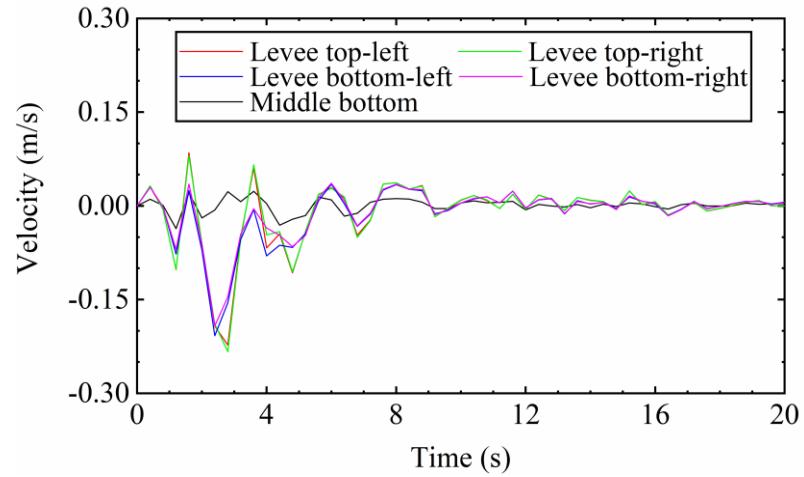


Figure 6. Horizontal velocity time history on the five measurement points of the levee

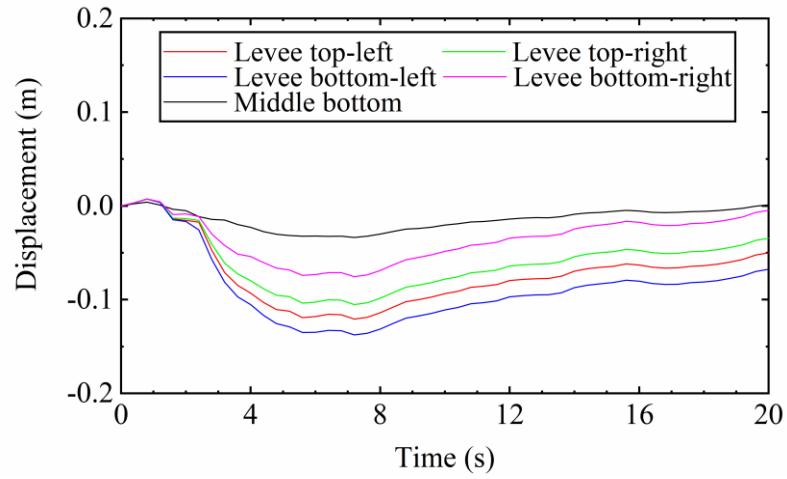


Figure 7. Horizontal displacement time history on the five measurement points of the levee

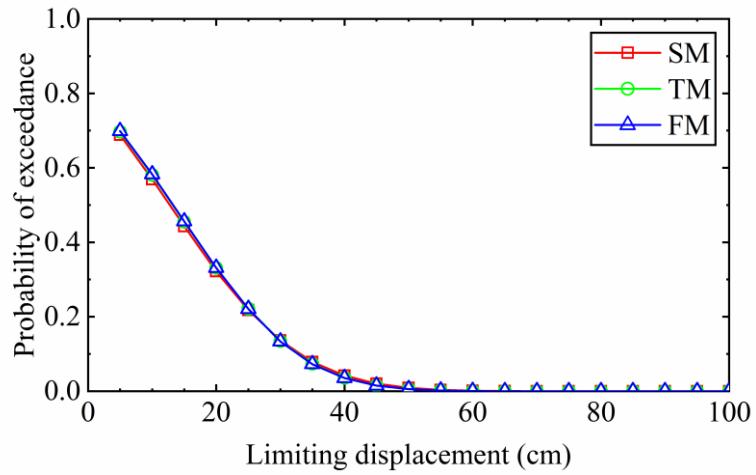


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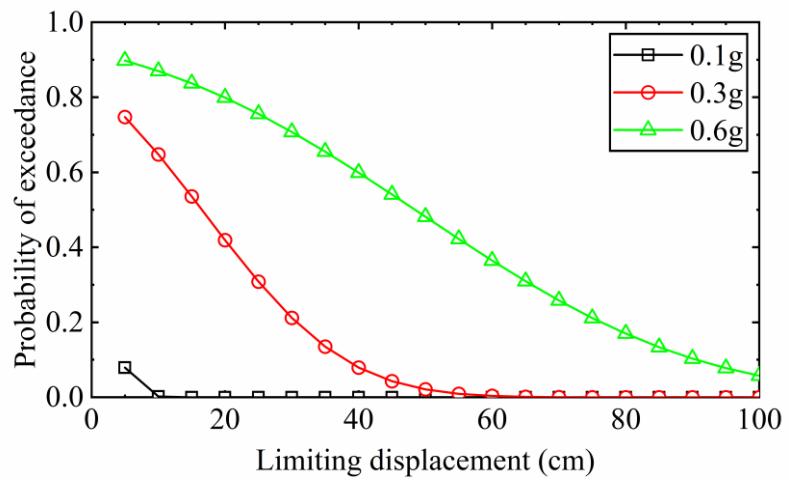


Figure 9. Probability of exceedance curve under different peak ground acceleration levels

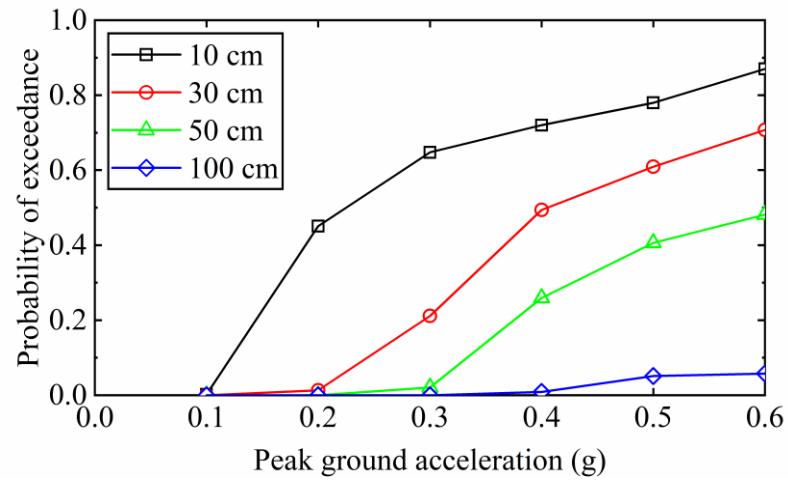


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