

Fluorescent wavefront shaping using incoherent iterative phase conjugation

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Wavefront shaping correction makes it possible to image fluorescent particles deep inside scattering tissue. This requires determining a correction mask to be placed in both the excitation and emission paths. Standard approaches select correction masks by optimizing various image metrics, a process that requires capturing a prohibitively large number of images. To reduce the acquisition cost, iterative phase conjugation techniques use the observation that the desired correction mask is an eigenvector of the tissue transmission operator. They then determine this eigenvector via optical implementations of the power iteration method, which require capturing orders of magnitude fewer images. Existing iterative phase conjugation techniques assume a linear model for the transmission of light through tissue, and thus only apply to fully coherent imaging systems. We extend such techniques to the incoherent case. The fact that light emitted from different sources sums incoherently violates the linear model and makes linear transmission operators inapplicable. We show that, surprisingly, the nonlinearity due to incoherent summation results in an order-of-magnitude acceleration in the convergence of the phase conjugation iteration. © 2022 Optica Publishing Group under the terms of the

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1. INTRODUCTION

One of the core challenges when performing linear fluorescence microscopy inside tissue is the fact that biological tissue is highly scattering at visible wavelengths. This limits the clinical applicability of linear fluorescence microscopy techniques to thin superficial layers, as incoming and outgoing light propagating through the tissue is highly aberrated. In turn, this precludes widespread clinical use for tasks such as vasculature imaging, laser light therapy, and tumor detection.

A promising approach to overcome the multiple scattering challenge is wavefront shaping correction: If one reshapes the incoming (or outgoing) coherent wavefront, such that its aberration is conjugate to the aberration that will happen inside the tissue, then after propagation the wavefront will focus into a sharp spot inside the tissue.

Adaptive optics techniques [1–3] were first used to correct modest aberrations, for example, due to imperfect optics or refractive index variations in the tissue. More recently, wavefront shaping techniques [4,5] have shown that it is possible to focus light through thick, highly scattering layers [6–9]. Wavefront shaping ideas have found applications in a wide range of imaging modalities, including sound and light, coherent imaging and OCT, and incoherent fluorescence imaging using single-photon and multi-photon excitation. Our interest in this work is wavefront shaping for linear, single-photon fluorescence feedback.

The practical application of wavefront shaping is hindered by the difficulty of finding the wavefront correction to apply. This wavefront correction varies between different tissue layers, and even between different positions inside the same tissue sample. The simplest approach for finding the wavefront correction is to use a so-called guide star [10–19]: In this case, scattering arises from a strong single point source inside the tissue, and a wavefront sensor [9,14] directly measures the scattered wavefront.

Finding a wavefront shaping correction in the presence of multiple sources is more challenging, and typically involves optimization strategies relying on a variety of feedback mechanisms [6–8,11–13,20–32]. This optimization is tractable when the wavefront correction can be described by a small number of parameters (e.g., using Zernike polynomials [33,34]). However, to focus inside thick highly scattering media, it is desirable to use all the degrees of freedom of a modern spatial light modulator (SLM), often in the megapixel range. As a result, this approach poses nontrivial optimization challenges [6,12,30,35]. Even if we can test every such free parameter only once [32], the very large number of images captured for optimization limits any real-time applicability.

For fully coherent imaging systems, an alternative class of techniques estimating the wavefront correction is iterative phase conjugation. These techniques use the observation that a wavefront shaping correction focusing on a single point inside tissue is an eigenvector of the transmission matrix of the scattering sample [35]. They then find these eigenvectors using an optical implementation of the power method [36], which iterates between sending

in a wavefront, measuring the scattered wavefront, and using the measurement as the successive input. Often this procedure converges after a very small number of iterations, leading to an order-of-magnitude acquisition speedup compared to standard optimization approaches. Iterative phase conjugation has found successful applications for sound [37,38] and acousto-optics [39,40], where the propagation is fully coherent. Although not presented this way, a similar iterative scheme was also applied for two-photon fluorescent imaging [41].

An important assumption underlying the coherent iterative phase conjugation scheme is that light scatters only once. This greatly limits its applicability to thin or sparse volumes. Our goal in this work is to develop an iterative phase conjugation approach that is applicable to linear (single-photon) fluorescent imaging. As the emitted light does not excite the tissue or the particles again, by working with fluorescent sources we can greatly relax the single scattering assumption, making our approach applicable to much thicker volumes in a particular tissue.

The primary technical challenge in this setting is that any uncorrected incident wavefront (such as the wavefronts used during the power method) will excite more than one fluorescing point inside the tissue sample, and the excited points will emit light that sums *incoherently*. Consequently, we cannot model the relation between the input excitation and output fluorescent emission using a linear transmission operator, as fully coherent iterative phase conjugation techniques do. To overcome this challenge, we analyze the incoherent case, and report two findings: First, we show that the same power method procedure as in the fully coherent case can be used to recover the correction pattern also in the incoherent case. Second, we show that, whereas for the fully coherent case the power method converges at an exponential rate, for the incoherent case it converges at a doubly exponential rate. We demonstrate these findings experimentally, focusing light on fluorescent beads attached at the back of the chicken breast tissue layers. Our technique achieves wavefront correction after capturing as few as 10–30 images, compared to thousands of

images captured by existing optimization-based wavefront shaping strategies for fluorescent imaging [21].

2. PRINCIPLE

Figure 1 shows our imaging setup. A laser beam illuminates a tissue sample via a microscope objective. A phase SLM at the Fourier plane of the illumination arm modulates the illumination pattern. The modulated laser light excites the fluorescent beads at the back of the sample. The emitted light is collected via the same objective, and reflected at a dichroic beam splitter. A second phase SLM at the Fourier plane of the imaging arm modulates the emitted light. Finally, the modulated light is measured by the front camera, which captures the images used by our algorithm. The setup includes a second validation camera behind the tissue sample. In our experiments we attached fluorescent beads at the back of the tissue layer, so that the validation camera can image them directly. We emphasize that measurements from this camera are not used by our algorithm, and that we only use the camera for validation purposes, to assess the focusing quality and to image an undistorted reference of the bead layout.

We derive a strategy to efficiently find a wavefront shaping modulation pattern for the illumination arm, allowing us to focus all light into a single spot inside the tissue sample. Once we have found the modulation pattern, we use the same modulation to also correct the emitted light in the imaging arm. This is possible because, in our linear fluorescent imaging setting, emission and excitation wavelengths are relatively close. Our approach extends to the incoherent imaging case iterative phase conjugation ideas that were previously used with coherent illumination. We begin our presentation by reviewing the coherent case, and then introduce the incoherent one.

A. Coherent Iterative Phase Conjugation

Consider a set of K scattering (nonfluorescent) particles inside a sample, and denote their positions by $\mathbf{o}_1, \dots, \mathbf{o}_K$. We denote by $\mathbf{u}$ the value of an incoming 2D electric field at the input plane, and

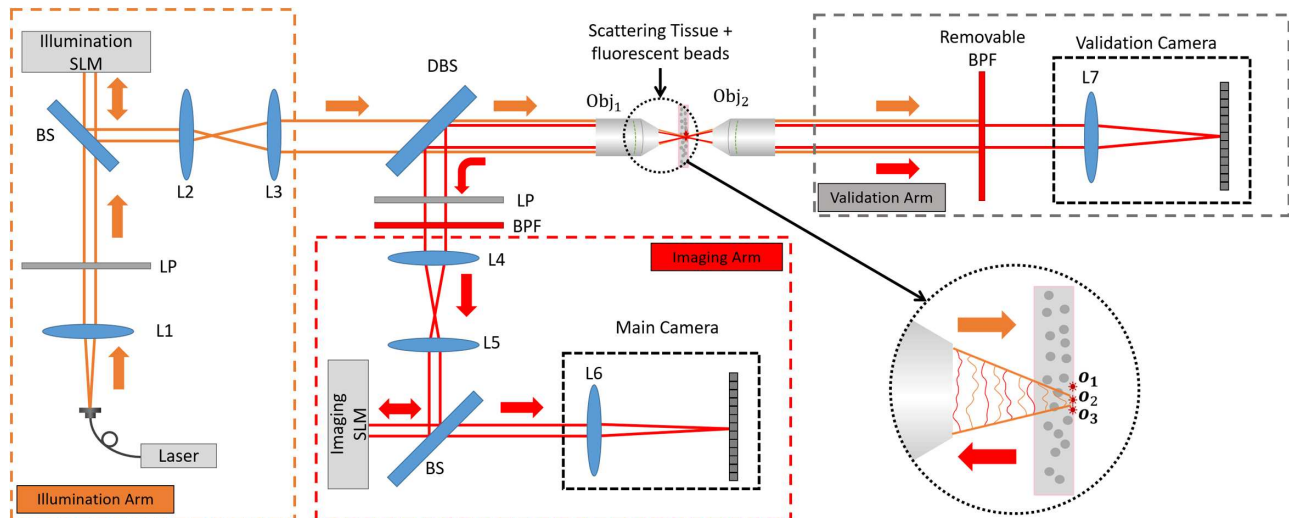


Fig. 1. Our wavefront correction fluorescent microscope setup: A laser beam is exciting fluorescent beads at the back of a tissue layer, and fluorescent emission is scattered again through the tissue, reflects at a dichroic beam splitter and is collected by a main (front) camera. We place two SLMs in the Fourier planes of both illumination and imaging arms to allow reshaping these wavefronts. A validation camera views the beads at the back of the tissue directly. This camera is not actually used by the algorithm, and is only assessing its success. LP, linear polarizer; BS, beam splitter; DBS, dichroic beam splitter; BPF, band-pass filter; L1 ... L7, lenses; and Obj, objective.

by $\mathbf{v}$ a $K \times 1$ vector of the field propagating through the sample at each of the K scatterers. Although $\mathbf{u}$ is a 2D field, we reshape it as a 1D vector and relate $\mathbf{v}$ to $\mathbf{u}$ as $\mathbf{v} = \mathcal{T}^i \mathbf{u}$, where $\mathcal{T}^i$ is the incoming transmission matrix describing coherent light propagation. $\mathcal{T}^i$ is specific to the tissue sample being tested. Likewise, we denote by $\mathcal{T}^o$ the back-propagation transmission matrix, describing the light returning from the particles to the sensor. The propagation of light to the particles and back to the sensor is then modeled using the combined transmission matrix

$$\mathcal{T}^a \equiv \mathcal{T}^o \cdot \mathcal{T}^i. \quad (1)$$

Note that Eq. (1) offers a simplistic description of light propagation, assuming there is not much light backscattered from other structures in the medium apart of the listed particles $\mathbf{o}_1, \dots, \mathbf{o}_K$, and multiple scattering between the particles is negligible.

Under fully coherent illumination, the input illumination and the measured speckle intensity are related as

$$I = |\mathcal{T}^a \mathbf{u}|^2. \quad (2)$$

Our goal is to find an illumination pattern $\mathbf{u}$ that will focus on one of the particles, so that $\mathbf{v}$ is a one-hot vector—nonzero only at a single point $\mathbf{o}_k$ for some k value. We note that focusing at any of the particles is sufficient for our setting; below, we show that once we focus at one point, we can use the memory effect to focus at nearby ones.

To find a wavefront modulation we need access to $\mathcal{T}^i$, but in practice we can only measure $\mathcal{T}^a$. The wave conjugation principle states that the returning transmission matrix is the transpose of the incoming one, $\mathcal{T}^o = \mathcal{T}^{i^\top}$ [42]. With this assumption, consider an illumination field $\mathbf{u}$ that, after propagating through the tissue sample, generates a one-hot $\mathbf{v}$ vector. If we focus all light at one particle, then by the wave conjugation principle the returning field is proportional to the incoming one. Therefore, we can express the returning intensity in Eq. (2) as

$$I = s |\mathbf{u}|^2 = |\mathcal{T}^a \mathbf{u}|^2, \quad (3)$$

where s is a scale factor; that is, a focusing wavefront is an *eigenvector* of the combined transmission matrix $\mathcal{T}^a$. Consequently, if we can compute eigenvectors efficiently, we can find a wavefront that focuses all the light in a single spot.

A common class of numerical algorithms for computing matrix eigenvectors follows the power method [36]. This algorithm relies on the fact that the sequence $\mathbf{u}, \mathcal{T}^a \mathbf{u}, (\mathcal{T}^a)^2 \mathbf{u}, (\mathcal{T}^a)^3 \mathbf{u} \dots$ converges exponentially fast to the largest eigenvector of $\mathcal{T}^a$. Iterative phase conjugation algorithms [37–40] do not acquire the full transmission matrix $\mathcal{T}^a$, but instead directly measure its optical operation on wavefronts of interest. They begin by illuminating the sample with a random wavefront $\mathbf{u}^0$, then iteratively measure the resulting output wavefront, and use its conjugate as a successive illumination pattern. That is, at the t -th iteration, the incident wavefront is $\mathbf{u}^{(t)} = (\mathcal{T}^a \mathbf{u}^{(t-1)})^*$, where $*$ denotes complex conjugation. When measuring intensity images $I = |\mathcal{T}^a \mathbf{u}^{(t)}|^2$, computing $\mathbf{u}^{(t+1)}$ also requires estimating the phase of the measured intensity pattern.

Using the exponential convergence property of the power method, it can be shown [36], and we review the derivation in Supplement 1 that the energy focused on the k -th particle at the t -th iteration follows a geometric sequence of the form

$$|\mathbf{v}_k^{(t)}| = \frac{1}{N_t} \lambda_k^t \cdot c_k, \quad (4)$$

for constants λ_k, c_k and a normalization factor N_t that we derive in Supplement 1. Equation (4) implies that the energy at the k -th particle scales exponentially with the iteration number t . Thus, each iteration increases the gap in energy between the strongest and second strongest particles, and the sequence quickly converges to a one-hot $\mathbf{v}$ vector.

B. Incoherent Phase Conjugation

The main limitation of coherent iterative phase conjugation is that to describe the propagation using the model of Eq. (1) one neglects multiple scattering between the particles, as well as backscattering from any other tissue components. This in turn limits the applicability of the technique to thin or sparse volumes. By using fluorescent emission, we remove this restriction, because even in thick tissue it is reasonable to assume that the emitted light does not excite the tissue or the other beads again. Moreover, we show that the incoherent summation of fluorescent emission results in largely accelerated convergence. However, an adaptation of the power method to the incoherent case is not straightforward due to the nonlinearity imposed by incoherent emission.

To study the incoherent case, we need to adjust the model above in two ways. First, we now mark by $\mathbf{o}_1, \dots, \mathbf{o}_K$ the positions of the fluorescent particles rather than all scatterers in the volume. We use $\mathcal{T}^i$ to describe propagation at the excitation wavelength λ_i , and $\mathcal{T}^o$ to describe propagation at the emission wavelength λ_o . Despite the small difference between the emission and excitation wavelengths, we still assume that $\mathcal{T}^o \approx \mathcal{T}^{i^\top}$. Note that $\mathcal{T}^i, \mathcal{T}^o$ describe multiple scattering events by other tissue components apart from the listed fluorescent particles $\mathbf{o}_1, \dots, \mathbf{o}_K$.

Second, whereas in the coherent case the output wavefront is a linear function of the input $\mathcal{T}^a \mathbf{u}^{(t)}$, this linear model no longer holds when incoherently summing light from different emitters. To derive an image formation model for this case, we again use $\mathbf{v} = \mathcal{T}^i \mathbf{u}$ to denote the field arriving at the fluorescent emitters. Fluorescent emission is proportional to the intensity of $\mathbf{v}$, and the recorded intensity equals an incoherent summation

$$I = \sum_k |\mathcal{T}_{:,k}^o|^2 |\mathbf{v}_k|^2, \quad (5)$$

where $\mathcal{T}_{:,k}^o$ is the k -th column of $\mathcal{T}^o$.

If we manage to focus and $\mathbf{v}$ is a one-hot vector, then there is only a single nonzero term in the summation of Eq. (5). Denoting the index of this nonzero entry by k_o , we can express the intensity in Eq. (5) as

$$\begin{aligned} I &= |\mathcal{T}_{:,k_o}^o|^2 |\mathbf{v}_{k_o}|^2 = |\mathcal{T}_{:,k_o}^o \mathbf{v}_{k_o}|^2 = |\mathcal{T}^o \mathbf{v}|^2 \\ &= |\mathcal{T}^o \mathcal{T}^i \mathbf{u}|^2 = |\mathcal{T}^a \mathbf{u}|^2. \end{aligned} \quad (6)$$

Therefore, when focusing is achieved, Eq. (5) effectively reduces to Eq. (2), and the measured intensity is equivalent to $|\mathcal{T}^a \mathbf{u}|^2$. Then, in the incoherent case, a focusing wavefront is still an eigenvector of the transmission operator $\mathcal{T}^a = \mathcal{T}^o \cdot \mathcal{T}^i$.

Motivated by this observation, we apply iterative phase conjugation as in the coherent case. As we measure only the intensity of the emitted light, to recover the phase of the wavefront, we use a phase diversity acquisition scheme [43]. We place $J = 5$ known

modulation patterns H^j on the phase SLM of the imaging arm. At the t -th iteration, we measure speckle intensity images

$$I^{(t,j)} = \sum_k |h^j \star \mathcal{T}_{:,k}^o|^2 |\mathbf{v}_k^{(t)}|^2, \quad (7)$$

where $\star$ is a convolution, h^j is the Fourier transform of the pattern we placed on the SLM, and $|\mathbf{v}_k^{(t)}|^2$ is the intensity arriving at the k -th particle in the t -th iteration. We use gradient descent optimization to find a complex wavefront $\mathbf{u}^{(t+1)}$ minimizing

$$\sum_j |I^{(t,j)} - |h^j \star \mathbf{u}^{(t+1)}|^2|^2. \quad (8)$$

We then use the conjugate of the estimated wavefront as the excitation of the next iteration, and display it on the SLM of the illumination arm.

When the intensity image is an incoherent summation from multiple sources, there is typically no wavefront minimizing Eq. (8) with zero error. Despite this, we show in the supplement that the resulting wavefront is approximately equal to a weighted linear combination of the wavefronts $\mathcal{T}_{:,k}^o$ generated by the individual sources. Sources with a stronger emission receive a higher weight in the reconstruction, which further increases their weight in the next iteration of the algorithm.

In the supplement, we analyze the differences between the coherent and incoherent models, and we show that the incoherent summation results in an asymptotically faster convergence rate. In particular, we prove the following claim:

Claim 1. *The convergence of the power iterations in the incoherent case follows a doubly exponential sequence of the form*

$$|\mathbf{v}_k^{(t)}|^2 = \frac{1}{N(t)} (\lambda_k)^{2^t} \cdot c_k \quad (9)$$

for scalars λ_k , c_k derived in Supplement 1.

To understand the difference, we note that in the coherent case of Eq. (4), the energy at the different particles scales as λ_k^t . In the incoherent case, we get another exponential factor, and energy scales as $(\lambda_k)^{2^t}$. Intuitively, this is because the fluorescent emission is proportional to the intensity of the field $|\mathbf{v}^{(t)}|^2$ arriving at the particles, rather than to the field $\mathbf{v}^{(t)}$ itself. As $\mathbf{v}^{(t)}$ is squared in every iteration, the squaring is accumulated into another exponential term.

To visualize the faster convergence, in Fig. 2 we simulated coherent and incoherent power iterations on a random transmission matrix sampled as described in Supplement 1.

In practice, in the hardware implementation described below, our algorithm converged within about 2–6 iterations. Accounting for the five images used for phase acquisition at each step, our approach can find a wavefront correction pattern using about 10–30 image measurements. This provides orders of magnitude speedup compared to recent optimization-based approaches recovering a wavefront shaping correction pattern using a single-photon fluorescent feedback, which requires capturing thousands of images [21].

3. RESULTS

In our experimental implementation, we use fluorescent microspheres each with a diameter of 200 nm (FluoSpheres (dark red), ThermoFisher), excited and imaged with $NA = 0.5$ objectives

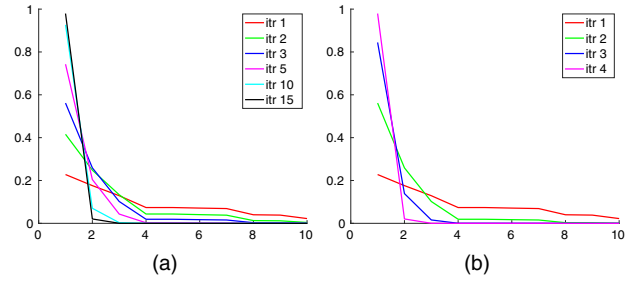


Fig. 2. Simulating coherent and incoherent convergence: We plot the power of scatterers $|\mathbf{v}_k^{(t)}|^2$, for different iterations of the iterative phase conjugation algorithm. As predicted by theory, the incoherent case converges into a one-hot vector within a smaller number of iterations (compare four incoherent iterations to 15 coherent ones). The x axis of our plot corresponds to scatterer index k , where for ease of visualization we sort these in decreasing order of power.

so that the particles are slightly smaller than the diffraction limit. For excitation, we use a 637 nm laser, and to measure the emission we use a bandpass filter with a center wavelength of 680 nm and a bandwidth of 10 nm. In the main paper, we use chicken breast tissue slices with thicknesses of 200–400 μm as scattering samples. In Supplement 1, we also show results using other scattering phantoms, including parafilm and polystyrene beads dispersed in agarose. For all examples, significant scattering is present, and a standard microscope cannot image the actual source pattern. The beads are attached at the back of the tissue layer, separated only by a 150 μm microscope cover glass. We use two SLMs (Pluto, HOLOEYE Photonics), and a prime BSI sCMOS sensor for imaging fluorescent emission.

Figure 3 visualizes the power iterations of our algorithm from both the main camera and the validation camera. In the beginning, the main camera sees a wide speckle pattern, and from the validation camera we can see that a wide speckle pattern reaches the back of the tissue. We also use a bandpass filter on the validation camera to image the beads excited by each modulation pattern. The validation camera confirms that as the algorithm proceeds the illumination reaching the back of the tissue converges into a single spot. Even if we manage to excite a single bead, the emitted light can scatter on its way to the main camera and generate a speckle pattern. In Fig. 3, we first visualize this scattering by showing the views of the main camera when modulation is used in the illumination SLM to focus the excitation, but with no modulation at the imaging arm. In addition, we show what happens if the modulation pattern of each iteration is also placed on the SLM of the imaging arm. As the iterations proceed and the modulation pattern improves, the imaging SLM refocuses the light emitted from the excited bead into a single sensor spot.

When multiple fluorescing particles are present in the field of view, the algorithm typically converges to the strongest one. However, the particle at which the algorithm converges may vary due to multiple reasons such as imaging noise, fluorescence bleaching or local minima of the phase diversity optimization. Convergence can also change if the optimization is initialized with a different speckle pattern.

In Fig. 4, we demonstrate the final iteration of our algorithm on a few additional examples. In Fig. 4(c), we also visualize the actual scattering of the tissue layer. To this end, we place the correction mask on the illumination SLM only, bringing all light to excite a

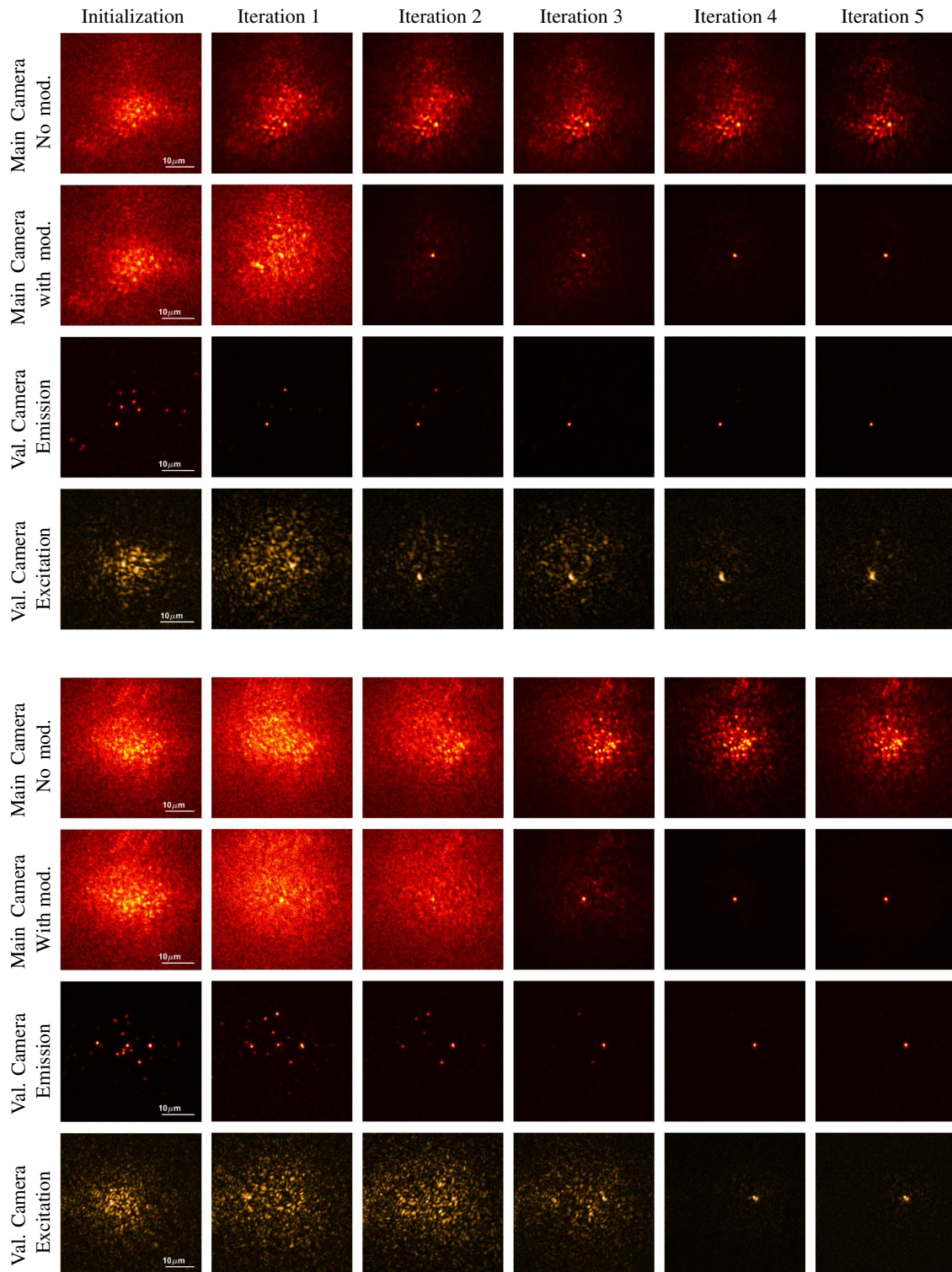


Fig. 3. Algorithm convergence: We show the iterations of our power algorithm on two different tissue samples. We demonstrate views via the main camera seeing the front of the tissue with and without the modulation correction, and the validation camera observing fluorescent beads directly. To better appreciate the focusing we used, the validation camera to capture both the excitation and emission wavelengths. In the first iteration, we see a speckle image, but as power iterations proceed the illumination wavefront converges and focuses on a single bead. When the same modulation pattern is placed at the imaging arm, imaging aberrations are corrected and one can see a sharp image of the excited bead. Note that images in different iterations have very different ranges and, for better visualization, each image was normalized to its own maximum.

single bead. We use no correction on the imaging arm, allowing us to visualize the speckles from this source. This image corresponds to a column of the transmission matrix $\mathcal{T}^o$.

In Fig. 5, we visualize the phase diversity acquisition results at the first and last iterations of the algorithm. Figure 5(a) shows the image from the main camera in both iterations when the imaging

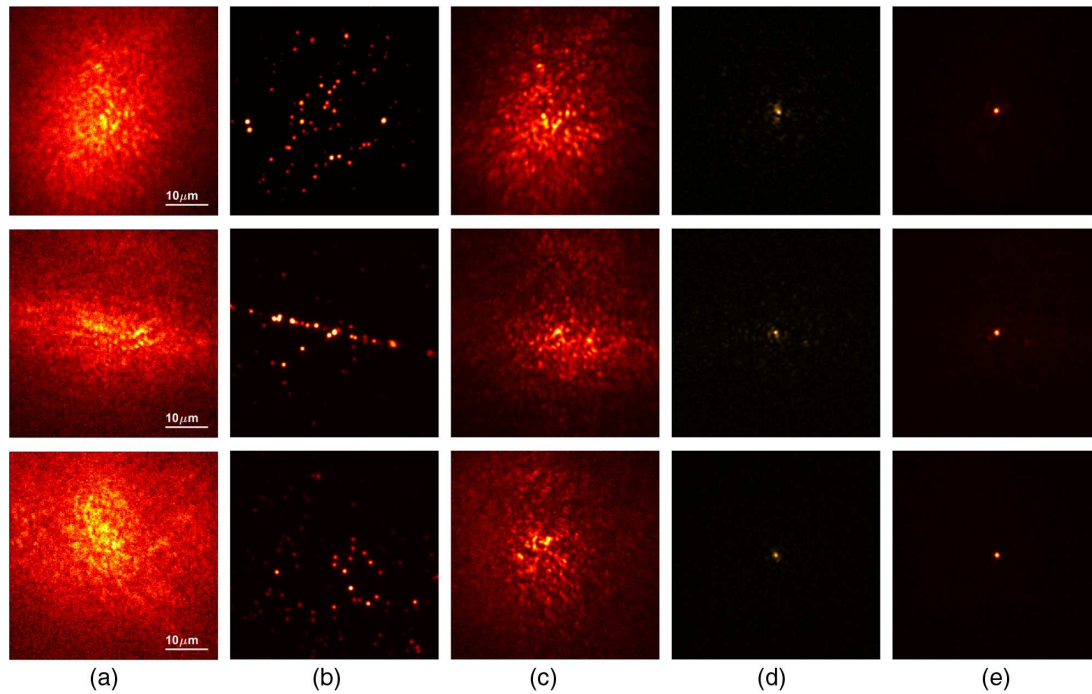


Fig. 4. Analyzing focusing inside a tissue: Each row visualizes a different experiment on a different tissue slice. (a) Main camera when SLMs are blank, demonstrating initial speckles. (b) Validation camera when illumination SLM is blank, demonstrating the enlightened bead layout at the emission wavelength. (c) Speckles from one bead (imaging SLM is blank and illumination SLM is corrected), demonstrating the amount of aberration. (d) Validation camera when illumination is corrected, demonstrating that most light gets into a single spot (excitation wavelength). (e) Main camera when both SLMs are corrected, demonstrating focusing in a single spot.

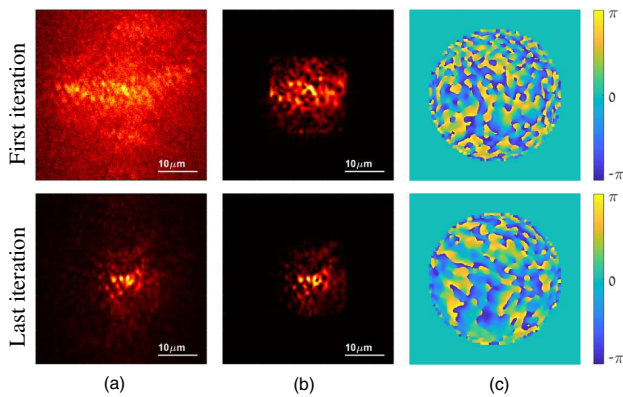


Fig. 5. Phase reconstruction: (a) Speckle image captured by the main camera in the first and last iteration of the algorithm. (b) Intensity of the recovered aberration correction in the sensor plane. In the first iteration, when multiple incoherent beads are excited, we cannot fully explain the image as a single coherent wavefront. However, as the algorithm converges to excite a single bead, the recovered wavefront better matches with the captured image. (c) Phase of the recovered aberration correction in the Fourier plane, which is the mask presented on the SLM.

SLM applies no correction. Figure 5(b) shows the intensity of the recovered wavefront at the plane of the camera sensor, which is set conjugate to the plane of the fluorescent sources. The phase diversity optimization attempts to explain the images in Fig. 5(a). However, in the first iteration, the captured speckle image is an incoherent summation from multiple particles, which the optimization objective of Eq. (8) attempts to explain with a single coherent wavefront; thus, the result is imperfect. In the last iteration, the algorithm excites a single particle, and the estimated

wavefront better explains the captured intensity. Finally, Fig. 5(c) shows the retrieved phase in the frequency domain, which is essentially the pattern displayed on the SLM. We note that because we use a phase-only SLM we effectively correct only the phase of the wavefront and neglect its amplitude.

A. Imaging a Wide Field of View

The recovered modulation pattern is designed to focus at a single particle inside the tissue sample. However, due to the memory effect, the corrections of nearby spots are similar. We demonstrate this experimentally in the second row of Fig. 6: We place a random pattern on the illumination arm, which results in exciting multiple fluorescing particles. We then place the correction pattern recovered to focus on one of the fluorescing particles on the imaging arm. We observe that, thanks to the memory effect, the camera can image a small neighborhood of particles around the focus points, and not just the single particle the correction pattern corresponds to. To further improve on this, we use the tilt-shift memory effect [44,45] and shift the modulation mask in the Fourier plane. As we explain in the supplement, this shift allows us to focus at nearby regions using the same correction pattern. In the third row of Fig. 6, we image a wider range of particles behind the tissue sample, by scanning 21×21 such shifts. We acknowledge that by placing the SLM at a plane conjugate to the sample itself [44,46] rather than in the Fourier plane, we can probably expand the region corrected by a single modulation and reduce the number of required shifts. Even after exploiting the tilt-shift, the extent of the memory effect is limited, and beads at the periphery of the images of the last row in Fig. 6 are either not recovered or strongly aberrated. Imaging beyond this region would require the application of another set

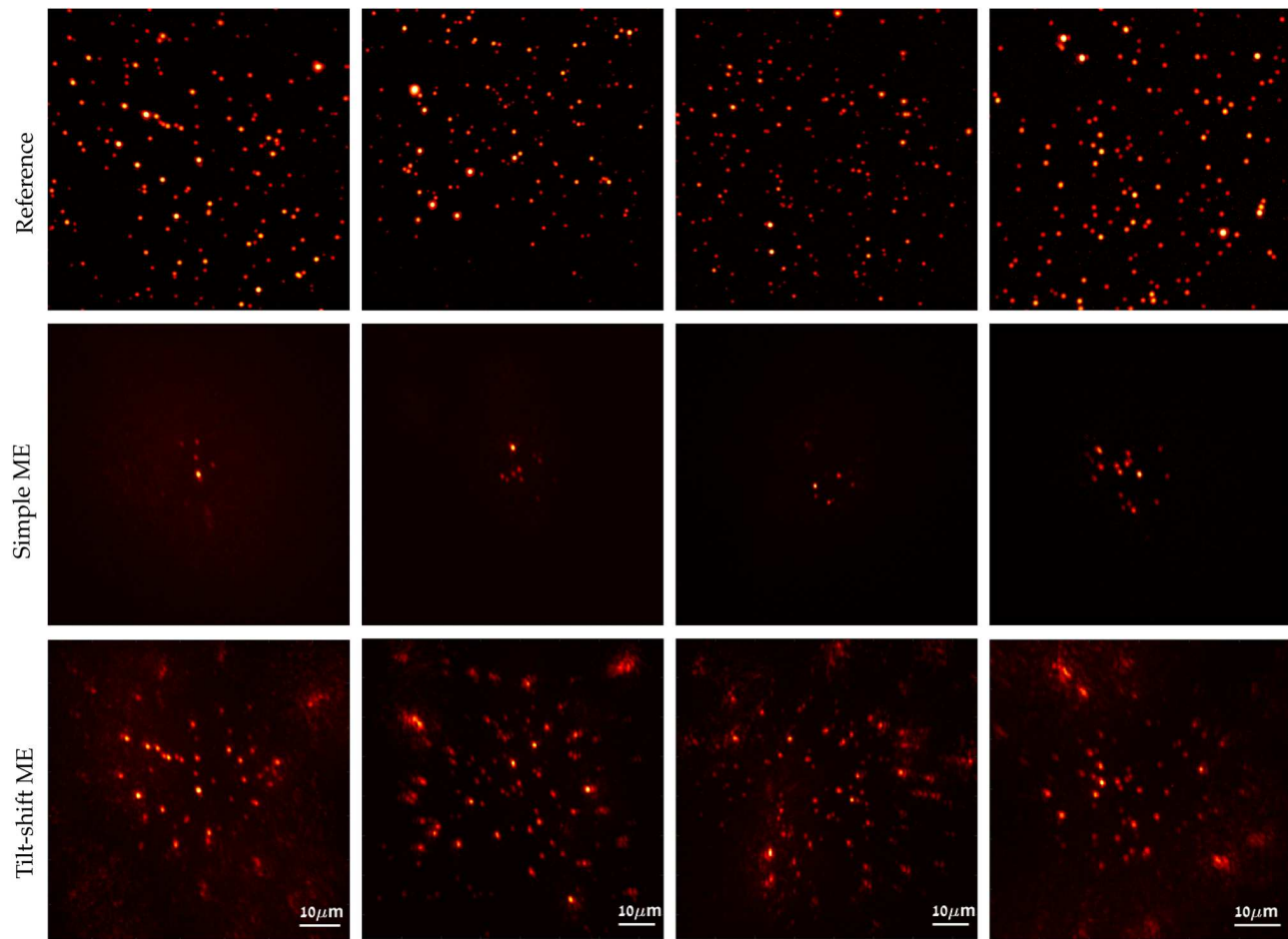


Fig. 6. Imaging a wide area of fluorescent sources, behind four different tissue slices. Top: Reference image from the validation camera. Second row: Imaging fluorescent sources within a small region behind the tissue using a simplified memory effect. We use the correction mask on the imaging arm, and use wide illumination to excite multiple beads. Third row: Using the tilt-shift memory effect to image a wider area, by shifting the imaging mask in the Fourier plane.

of power iterations to calibrate a different wavefront modulation, amplifying the importance of the faster convergence of our proposed procedure.

4. DISCUSSION

We extended iterative phase conjugation algorithms to apply to incoherent fluorescent imaging. Even though the incoherent contribution of different sources alters the linear transmission model from which these algorithms are derived, we show that the nonlinear incoherent model accelerates convergence rate, from exponential to doubly exponential. To find a wavefront correction pattern, we need to excite the tissue with a very small number of trial patterns and measure the resulting excitation. The number of measurements is orders of magnitude smaller than that of previous optimization-based techniques.

We used the recovered modulation pattern to image fluorescent particles placed behind a tissue sample. However, wavefront correction in thick tissue is spatially varying, and each modulation pattern is only usable for imaging a limited region, with size determined by the memory effect. To image a wider region behind the tissue sample, we have to apply the modulation recovery algorithm multiple times in different subregions. This makes it even more important to have fast wavefront shaping algorithms. One way to

further reduce the number of acquired images is to use a tilt-shift adaptation of the aberration correction estimated in one region, and initialize with it the power iteration in neighboring subregions.

Our current results apply only on a sparse set of fluorescent particles. Increasing the density of the sources is challenging because as speckle contrast decays [47], it is harder for the phase diversity acquisition scheme to recover phase. To alleviate this problem, we could adopt other phase acquisition schemes, such as using a Shack–Hartmann sensor [48].

Another issue that may challenge the convergence with a dense continuous fluorescent object is two nearby spots emitting similar power. This is due to the fact that when a transmission matrix contains multiple eigenvectors with the same eigenvalue, power iterations may not separate them, and can converge to a linear combination of the two eigenvectors. We note, however, that the incoherent convergence rate as analyzed in Supplement 1, Eq. (26), depends not only on the actual eigenvalues, but also on the initial excitation $\mathcal{T}_{k,:}^i \mathbf{u}^{(0)}$. As this excitation is usually a highly varying speckle pattern, there is a better chance to separate between nearby illuminators of similar power. Our approach also relies on the assumption that the excitation and emission wavelength are close enough so that the excitation and emission transmission matrices are sufficiently similar. As the emitted light contains multiple wavelengths, these also can produce somewhat different speckle

patterns. There is evidence in the literature that speckle patterns produced by nearby wavelengths are correlated [49], but this similarity degrades as the tissue sample thickness increases [50]. In our experimental implementation, there is a 40 nm gap between the emission and excitation wavelengths. In linear fluorescence imaging, the gap between excitation to emission can be made lower than that, leading to even stronger correlation between the wavefronts.

A. Relationship to Memory-Effect Techniques

Our work is orthogonal to approaches for imaging fluorescent sources through tissue using speckle statistics and, in particular, the memory effect [47,51,52]. Recently, such approaches were successful in imaging a sparse set of fluorescent particles inside tissue, using hundreds [22,53] or even just dozens [54] of images. While the field of view of a wavefront shaping modulation is constrained by the extent of the memory effect, as demonstrated in Fig. 6, approaches based on the memory effect can recover full-frame patterns with much wider fields of view. By contrast, memory effect correlations only exist in thin tissue layers, while approaches based on phase conjugation can theoretically achieve larger penetration depths. However, in practice, the penetration depth is greatly constrained by the very weak SNR of the fluorescent emission. Approaches based on phase conjugation make it possible to not only image through scattering, but also focus light inside scattering tissue, a capability that memory effect approaches lack. Focusing inside tissue is important for applications such as laser treatment therapy, confocal microscopy, and STED microscopy. Finally, a modulation recovered from fluorescent sources also can be used to image adjacent nonfluorescent tissue structures.

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Data availability. Data underlying the results presented in this paper are available in [55].

Supplemental document. See Supplement 1 for supporting content.

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