

# Ecological Diversity Methods Improve Quantitative Examination of Student Language in Short Constructed Responses in STEM

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First author performed data analysis and primarily drafted the manuscript. Second author assisted in data analysis and in drafting the manuscript. Third author provided feedback on the data analysis and manuscript. All three authors were involved in project design, execution, and editing of the manuscript.

### ***Keywords***

text analysis, Ecological diversity, constructed response, assessment, Student thinking, Ordination

### ***Abstract***

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We novelly applied established ecology methods to quantify and compare language diversity within a corpus of short written student texts. Constructed responses (CRs) are a common form of assessment but are difficult to evaluate using traditional methods of lexical diversity due to text length restrictions. Herein, we examined the utility of ecological diversity measures and ordination techniques to quantify differences in short texts by applying these methods in parallel to traditional text analysis methods to a corpus of previously studied college student CRs. The CRs were collected at two time points (Timing), from three types of higher-ed institutions (Type), and across three levels of student understanding (Thinking). Using previous work, we were able to predict that we would observe the most difference based on Thinking, then Timing and did not expect differences based on Type allowing us to test the utility of these methods for categorical examination of the corpus. We found that the ecological diversity metrics that compare CRs to each other (Whittaker's beta, species turnover, and Bray-Curtis Dissimilarity) were informative and correlated well with our predicted differences among categories and other text analysis methods. Other ecological measures, including Shannon's and Simpson's diversity, measure the diversity of language within a single CR. Additionally, ordination provided meaningful visual representations of the corpus by reducing complex word frequency matrices to two-dimensional graphs. Using the ordination graphs, we were able to observe patterns in the CR corpus that further supported our predictions for the data set. This work establishes novel approaches to measuring language diversity within short texts that can be used to examine differences in student language and possible associations with categorical data.

### ***Contribution to the field***

This work describes a novel method for quantitatively examining student language in short texts. Language is traditionally examined using lexical diversity, but these methods are lacking for texts under 100 words and are difficult to apply to STEM assessments. While these limitations have been discussed in the literature, no solution has been proposed that can be applied to STEM constructed response assessments, which are being increasingly used to assess student thinking in undergraduate STEM classes. This work applies methods commonly used in the field of ecology, including quantitative ecological diversity measures and ordination analysis, to examine differences in student language based on categorical data. The utility of these methods is demonstrated using a set of constructed responses that test student understanding of the Pathways and Transformations Energy and Matter within the context of human weight loss. Data was collected before and after an online tutorial on cellular respiration (Timing), from three different institutional Types, and coded for different levels of Thinking. We conclude that these methods aid in analyzing student language and demonstrate these methods can then be linked to student thinking in a manner that aids teaching and learning.

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In review

1 **Ecological Diversity Methods Improve Quantitative Examination of Student Language in Short  
2 Constructed Responses in STEM**

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12 **Keywords: text analysis, ecological diversity, constructed response, assessment, student  
13 thinking, ordination.**

14 **Abstract**

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16 corpus of short written student texts. Constructed responses (CRs) are a common form of assessment  
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18 restrictions. Herein, we examined the utility of ecological diversity measures and ordination  
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24 Type allowing us to test the utility of these methods for categorical examination of the corpus. We  
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26 turnover, and Bray-Curtis Dissimilarity) were informative and correlated well with our predicted  
27 differences among categories and other text analysis methods. Other ecological measures, including  
28 Shannon's and Simpson's diversity, measure the diversity of language within a single CR.  
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30 complex word frequency matrices to two-dimensional graphs. Using the ordination graphs, we were  
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32 work establishes novel approaches to measuring language diversity within short texts that can be  
33 used to examine differences in student language and possible associations with categorical data.

34 **1 Introduction**

35 *Assessment of Student Thinking in STEM through Constructed Response:*

36 Assessment of student understanding and skills is an essential component of teaching,  
37 learning, and education research. For this reason, science education standards have pushed for  
38 increased use of assessment practices that test authentic scientific practices, such as constructing

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39 explanations, and assessments that measure knowledge-in-use (NGSS Lead States, 2013; Gerard &  
40 Linn 2016; Krajcik, 2021). Constructed responses (CRs) are an increasingly used type of assessment  
41 that provide valuable insight to both instructors and researchers, as students express their  
42 understanding or demonstrate their ability using their own words (Gerard & Linn 2016, Birenbaum et  
43 al, 1992; Nehm & Schonfeld, 2008). Through CRs, students reveal differing levels of performance,  
44 complex thinking, and unexpected language in a variety of STEM topics including evolution (Nehm  
45 & Reilly, 2007), tracking mass across scales (Sripathi et al., 2019), statistics (Kaplan et al. 2014),  
46 mechanistic reasoning in chemistry and genetics (Noyes et al. 2020; Uhl et al, 2020), and  
47 covariational reasoning (Scott et al., 2022). Due to their value and expanded use, it is increasingly  
48 important for assessment developers and researchers to have methods to carefully and quantitatively  
49 examine the language within CRs. Such methods could allow for comparison of expert and novice  
50 language, determine if substantial differences in student language occur due to instruction, regions or  
51 institutional type, or help examine bias in written assessments. Unfortunately, quantitative methods  
52 of examining and comparing the words within corpuses of short texts, such as CRs, are limited.  
53

### 54 *Current Methods of Written Language Analysis and Their Limitations:*

55 Text analysis falls into two major categories: qualitative and quantitative. For qualitative text  
56 analysis, researchers typically use “coding,” in which expert coders categorize “the text in order to  
57 establish a framework of thematic ideas about it” (p. 38; Gibbs, 2007). Coding is the most common  
58 approach for qualitative analysis in content based CRs in STEM, as it gives insight into student  
59 thinking by examining student produced text or words. In previous work with CRs, coding has  
60 reflected various frameworks in STEM, including cognitive models such as learning progressions  
61 (Scott et al, 2022; Jescovitch et al., 2021), the use of scientific skills (Uhl et al. 2021; Wilson et al.  
62 accepted), or the presence of key conceptual ideas (Sripathi et al., 2019, Nehm & Schonfeld, 2008;  
63 Noyes 2021). Qualitative coding can be done by reading the responses or using text mining programs  
64 that use computer-based dictionaries and natural language processing to pull out themes from the  
65 text. Through these qualitative methods, researchers often observe words or phrases that are  
66 associated with the coding of the text. These observations can often be statistically supported using  
67 quantitative analysis. Quantitative text analysis is typically performed via content or dictionary  
68 analysis, in which the text is reduced to word and phrase frequency lists that can be examined and/or  
69 compared between CRs or groupings of the CRs that are based on the qualitative coding. These types  
70 of analyses can be useful; however, these approaches do not examine the CRs holistically or examine  
71 the diversity of language used. While dictionary analysis allows for comparison of individual words  
72 or phrases between groups, this analysis seems overly reductive, since the words and phrases are  
73 typically interpreted as a part of the overall response by human coders. To assist with this gap,  
74 machine learning and natural language processing have also been used to better analyze texts for  
75 meaning (Boumans & Trilling, 2016). One approach currently used in text analysis to holistically  
76 examine language is through latent semantic analysis (LSA). LSA uses natural language processing  
77 and machine learning to compare the language in different texts to each other based on the words  
78 within the texts (Deerwester et al., 1990; Landauer & Psotke, 2000). While this method and others  
79 related to it have been used to help identify themes in CRs (Sripathi et al. 2019) and even in the  
80 creation of computer scoring models for automated analysis of student thinking (LaVoie et al., 2019),  
81 their purpose is to identify meaning or common topics in the text. The identified themes or topics  
82 must be interpreted for relevance by an expert in the domain. In contrast, we are interested in  
83 comparing and quantifying the diversity of words students use in written explanations.  
84

85 Our interest in comparing the words students use could also be approached through lexical  
86 diversity, which measures the range of words in a given text, with high lexical diversity values  
87 indicating more varied language (Jarvis, 2013). Many lexical diversity measures, most commonly  
Type to Token (TTR) and several derivatives, calculate the proportion of words in a text that are

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unique. These measures are helpful predictors of linguistic traits, including vocabulary and language proficiency (Malvern et al. 2004, Voleti et al. 2020). Unfortunately, these lexical diversity measures cannot be applied to CRs, as many are sensitive to the text length and cannot be applied to texts under 100 words (Tweedie & Baayen 1998; Choi et al. 2014). Although some lexical diversity measures, such as MATTR (Covington & McFall, 2010; Zenkar & Kylie. 2021), allow use of shorter texts of 50-100 words, most content-based CRs in STEM can frequently be as short as 25-35 words (Haudek et al., 2012; Shiroda et al., 2021). Beyond the length requirement, we find these lexical measures somewhat lacking for our intended use in that they do not present a full picture of diversity, as they only measure the repetition of words within a single response. In contrast to linguistics for which repetition does often indicate language proficiency, word repetition is not necessarily indicative of proficiency in STEM assessments. This could be especially true when considering the importance of discipline specific language which restricts word choice. In particular, we are interested in holistically comparing responses to one another based on word frequency. Such an approach could be used to determine if certain variables (e.g. question prompt, timing) are associated with more similar or varied language in student CRs.

Quantifying such diversity between two CRs or within a group of CRs is more similar to measures of ecological diversity than any current form of text analysis. Indeed, Jarvis (2013) previously compared lexical diversity to ecological diversity (ED) approaches and proposed applying ecological definitions and practices to texts. Within his work, Jarvis comments, “Both fields view diversity as a matter of complexity, but ecologists have gone much further in modeling and developing measures for the different aspects of that complexity. Ecologists have also held to a literal and intuitive understanding of diversity, and this has resulted in a highly developed, intricate picture of what diversity entails.” (p. 99; 2013). Indeed, ED metrics quantify not only diversity within a sample but between samples within data sets. Further, ecologists also commonly use a data reduction technique called ordination to explore data sets and test hypotheses. To our knowledge, this idea of applying ecological methods to language has never been empirically tested and its application to a corpus of short, content rich CRs is novel.

*Ecological Diversity Metrics:*

In ecology, Robert Whittaker articulated three diversity metrics that are now central to ecology: alpha, gamma, and beta diversity (Figure 1A, Whittaker, 1972). Alpha ( $\alpha$  or species richness) diversity is the count of the number of species in a sample. This idea is similar to counting unique words (also called Types in lexical diversity) in a CR. For example, as shown in Figure 1A, Sample A has a higher alpha than Sample B. Both samples have 4 individuals, but all four in A are unique, while Sample B has three of the same species. Gamma ( $\gamma$ ) is the count of the total number of species in a pair or set of samples, similar to the total words (also called Tokens in lexical diversity) in a CR. Beta diversity ( $\beta$ ) compares the species occurrences between samples (Whittaker 1967; 1969) and does not have an equivalent in lexical diversity or text analysis. This is the simplest calculation of  $\beta$  diversity; however, other metrics can be used to represent this kind of relatedness, including absolute species turnover (McCune, 2018; Tuomisto, 2010). The species turnover measure uses presence-absence data of species in samples and is considered a better indicator of relatedness than  $\beta$ , as  $\beta$  can be heavily affected by rare species (Vellend, 2001; Lande 1996). Another method of comparing two or more samples is using dissimilarity measures, such as Bray-Curtis dissimilarity (Bray & Curis, 1957). This is calculated by comparing every pair of species within two samples. While these measures may appear redundant, each can be biased in different ways (Roswell et al, 2021). Examining a collection of diversity metrics results in a more equitable description of the data, in much the same way that mean, median, and mode all offer different values for a measure of central tendency (Zeleny, 2021).

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136 In addition to comparing species between samples, other measures examine the diversity of  
137 individual communities or samples. These types of measures include Evenness (E), Shannon's  
138 diversity index ( $H'$ ; Shannon, 1948) and Simpson's diversity index (D; Simpson, 1949). Evenness  
139 describes the proportional abundance of species across a given sample and indicates if a sample is  
140 dominated by one or a few species. Similar to Whittaker's  $\beta$ , species turnover and Bray-Curtis  
141 Dissimilarity,  $H'$  and D both represent the diversity of a single community or sample but are  
142 calculated slightly differently.  $H'$  represents the certainty of predicting a *single* species of a randomly  
143 selected individual, while D is the probability of two random species being the same. Each measure  
144 has potential biases associated with it, resulting in most researchers examining both metrics for a  
145 clearer picture of the data (Zeleny, 2021).

146  
147 *Ecological Diversity Visualization:*  
148 In addition to diversity metrics, ecological studies also apply ordination methods to visualize  
149 and extract patterns from complex data (Gauch, 1982; Symes, 2008; Palmer, *n.d.*). Ordination  
150 methods use dimension reduction to project multivariate data into two or three dimensions that can  
151 be visualized in a map-like graph. This technique arranges samples with greater similarity more  
152 closely to each other as points in the graph, while samples with lower similarity are further apart.  
153 These ordination methods are often used in combination with ED metrics as the ordination  
154 techniques provide unique benefits. First, diversity is complex in a way that an individual measure or  
155 even a collection of measures do not fully relate to the whole of an object. Jost (2006) said, "a  
156 diversity index itself is not necessarily a 'diversity'. The radius of a sphere is an index of its volume  
157 but is not itself the volume and using the radius in place of the volume in engineering equations will  
158 give dangerously misleading results" (p. 363). Ordination attempts to collapse the diversity in a  
159 different way compared to ED metrics through extracting patterns while attempting to account for as  
160 much variation in the data as possible. Second, extracting, and prioritizing patterns that best explain  
161 the data focuses researchers on the most important patterns, allowing them to ignore noise in the data.  
162 Ecologists have found that even if ordinations result in a low percentage of variance in the data being  
163 explained, the ordinations are still meaningful and, more importantly, provide insight into the system  
164 being studied (Goodrich et al. 2014). Further, different patterns can be observed when a data set is  
165 examined holistically as opposed to examination of categorical sub-groups. In comparison, ED  
166 metrics need to be calculated by defining subsets of the data to obtain a single value for categorical  
167 data, while ordination analysis is performed on the entire data set and categorical data is overlaid.  
168 Finally, ordination results in an intuitive graph whose patterns can be more easily interpreted to better  
169 understand communities and how they relate to each other. For these reasons, ordination is used in  
170 diverse fields including image analysis, psychology, education research, and text analysis. Within  
171 education research, Graesser et al. (2011) used ordination to examine attributes of long texts in order  
172 to curate reading assignments for students. Borges et al. (2018) proposed the use of ordination to  
173 predict student performance and gain understanding of important student attributes, while another  
174 group used ordination to create models to evaluate teacher quality (Xian et al., 2016; Si, 2006).

175 For any of these applications, a data matrix is created that contains the objects of interest as  
176 rows and their attributes as columns. In ecological work, the matrix contains rows as samples and  
177 columns are species recorded in these samples (Figure 2A). The species in each row are compared for  
178 every pair in the matrix, resulting in a pairwise comparison of the entire matrix. The resulting  
179 distance or similarity values are a necessary prerequisite for distance-based ordination methods (ex:  
180 PCoA) and eigen analysis-based methods (ex: DCA), both of which we use in this work. The patterns  
181 found in these data are used to create a map-like visualization that projects the distances or  
182 similarities between samples in two or three dimensions. While the idea of ordination is maintained,  
183 different methods of ordination vary in how they work. Each has their own strengths and weaknesses;  
184 therefore, it is common in ecology to apply multiple ordination methods in order to strengthen the

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conclusions made via one method. Selection between the different methods is based on the overarching question being investigated, the qualities of the data matrix, and the advantages or disadvantages of each method (Peck, 2010; McCune & Mefford, 2018; Palmer, 2019). Ordination methods fall into two general categories: indirect (unconstrained) and direct (constrained) methods (Syms, 2008). Indirect ordination is used to explore data for patterns from a species matrix (described above), while direct ordination is used to test if patterns in the species matrix are attributable to a secondary matrix of data (measured environmental factors associated with samples). In general, indirect ordination is considered exploratory and is used to generate hypotheses, while direct ordination is confirmatory and used to test hypotheses. Since we want to use ordination methods to explore our data set, we selected only indirect methods of ordination. When selecting a specific ordination method, it is important to recognize the limitations of the method and the data itself. For example, many ordination methods, including Principal Component Analysis (PCA) and Non-metric multidimensional scaling (NMDS), do not handle high numbers of zeros in the data set well (Peck, 2010). However, high-zero data exists in many instances and methods exist to circumvent this limitation, including Detrended Correspondence Analysis (DCA) and Principal Coordinate Analysis (PCoA).

*Applying Ecological Methods to Language Analysis and Its Potential Benefits:*

Addressing the challenge of language analysis and comparisons for short texts, we propose applying ecological methods of diversity analysis to a corpus of CRs, in which each individual response is equivalent to a sample, and each word is analogous to a species within that sample (Figure 1B). In these examples, each response is a single sentence; however, in our data set, CRs can range from one word to multiple sentences. They are still counted as a single CR. Similarly, for each of the measures described above, we substitute the species with unique words in a single CR. With this application,  $\alpha$  is the count of unique words in a CR and  $\gamma$  is the total abundance of words in a pair or larger grouping of responses. (Figure 1B).  $H'$  and  $D$  are similar to the lexical diversity measures (e.g. TTR and its derivatives) described above. However, in contrast,  $H'$  and  $D$  do not have specific cutoffs for their use with smaller sample sizes (i.e. number of words in a CR). Low alpha data sets are common in ecology as some environments do not support a large variety of species (e.g. Roswell et al, 2021). Similarly, it is common to observe large differences in  $\alpha$  within ecological samples. These differences are often accounted for using a standardization method, such as equalizing effort, sample size or coverage. In this work, we are using an equalizing effort approach in that each student was presented the same opportunity (assessment item and online text box) to supply their CR (sample). However, it is important to note that ED metrics are still sensitive to  $\alpha$  as many are calculated using  $\alpha$  either directly or indirectly. They should therefore be interpreted carefully if there are stark differences in  $\alpha$ . In addition to offering a solution to the length requirement of lexical diversity measures, Whittaker's  $\beta$ , species turnover, and Bray-Curtis Dissimilarity allow holistic comparison of the CRs to each other in a way that no current text analysis methods do.

Ordination methods add to this holistic comparison by visualizing language differences in the CR corpus. To accomplish this, each CR is a row in our matrix and each column is the frequency of that word in the CR, similar to a term-document matrix in text analyses (Figure 2B). The nature of a large corpus of CRs results in a high number of zeros as the majority of words are used infrequently, resulting in a sparse data set. The high percentage of zeros results in a non-normal distribution of the data, restricting the ordination methods that can be used. However, these types of data sets are increasingly common with microbial diversity studies, which established best practices for sparse data sets, including Principal Coordinate Analysis (PCoA). We elected to use this method because it is most commonly used for sparse data but note one potential drawback in its utility for language diversity in comparison to an ecological study. PCoA ignores zero-zero pairs (when two separate

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rows being compared each have matching zero values). In ecology, zeros can mean that a species was not detected or that the species is truly not present, making it, in a way, favorable to ignore them. In comparison, with language a zero represents a known absence, and this absence can be as important as its presence. To ensure ignoring zero-zero pairs does not drastically change the observed patterns, we also applied another ordination approach. DCA is one of the most widely used methods in ecology (Palmer, 2019, Palmer, n.d.). This method is a type of Correspondence Analysis (CA) that reduces the dimensionality of a data set with categorical data. In addition to handling sparse data, this method has an additional benefit for our purposes as the x-axis is uniquely scaled in beta-diversity units, which allows users to calculate species turnover. In combination, DCA and PCoA complement each other and provide unique approaches that together support the results of the other. These approaches to diversity are similar to other types of text analysis techniques, including LSA described above, which can be visualized using ordination techniques similar to those described above. An important difference is that these DCA and PCoA techniques do not attempt to extract meaning from the texts and instead compare and contrast responses based solely on word frequencies without any weighting or dictionaries. This distinction is important to our goals because we are interested in measuring language diversity, not meaning.

Finally, in addition to the methods themselves, we appreciate the approach of ecology in interpreting diversity. Specifically, each metric is treated as a single view of the diversity, meaning that interpretation of diversity is done by taking into account each measure to provide a more comprehensive picture (Jost, 2006). This multifaceted approach will allow for full appreciation of the diversity of language students use in STEM CRs and will be more likely to reveal differences observed based on categorical data.

### *Present Study:*

To test the application of ecological methods in analysis of short CR, we utilized a corpus of 418 explanatory CRs collected from undergraduates that explore student understanding of the Pathways and Transformations Energy and Matter (Vision & Change, 2011) within the context of human weight loss. The question asks “You have a friend who lost 15 pounds on a diet. Where did the mass go?” We chose this data set as we have worked heavily with it and are very familiar with the language within the student CRs. Additionally, this corpus has three types of categorical data that can be used to test the method's ability to find differences in corpus based on word usage, as we have expectations on which categories are likely to have different language. First, the CRs were previously coded for the presence or absence of seven ideas, categorized as normative (correct) or non-normative (naïve) (Table 1; Sripathi et al., 2019). Using the presence and absence of these ideas, the CRs can be further categorized into Developing, Mixed, or Scientific Thinking (Sripathi et al., 2019). We expect this categorization to result in the greatest difference in language as the ideas in the CRs should directly reflect the ideas written by students. In addition, these CRs were collected before and after an online tutorial on cellular respiration (Timing) and from three different institutional Types (Uhl et al., 2021; Shiroda et al., 2021). We have previously found that student performance was affected by engaging with the tutorial (Uhl et al., 2021) and therefore expect some differences in language to be observed based on Timing. In previous work, we did not observe striking differences in student ideas based on the institutional type (i.e. Research Intensive Colleges and Universities [RICUs]; Primarily Undergraduate Institutions [PUI] and Two Year Colleges [TYCs]); therefore, we are expecting these categories to result in the lowest language differences in this analysis.

In this paper, we apply common text analysis techniques to support our expectations that these three categorizations (Thinking, Timing and Types) have varying amounts of difference in student language. Next, we outline the various methods and ED measures we applied to examine differences in short texts and demonstrate which ED methods reflect the differences in the categorical data to support their use in the analysis of short texts.

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## 283 2 Materials and Methods

### 284 *Constructed response (CR) corpus collection and description.*

285 CRs were collected in collaboration with the SimBiotic Company as described by Uhl et al.  
286 (2021). Subsequently, Shiroda et al. (2021) examined a subset of 418 student responses. These  
287 studies were considered exempt by an institutional review board (x10-577). Briefly, college students  
288 enrolled in biology courses were asked to write a response to the prompt “You have a friend who lost  
289 15 pounds on a diet. Where did the mass go?” in an online system. The subset of CRs used by  
290 Shiroda et al. (2021) and in this study are from 239 students from 19 colleges and universities across  
291 the United States. Shiroda et al (2021) grouped the colleges and universities into three general  
292 categories of institutional type: Two Year Colleges (TYCs; n = 137), Primarily Undergraduate  
293 Institutions (PUIs; n = 142) and Research-Intensive Colleges and Universities (RICUs; n = 139). This  
294 information is reflected in the categorical data as *Type*. Students answered the prompt both before (n  
295 = 205) and after (n = 213) completing an online tutorial on cellular respiration. This information is  
296 reflected in the categorical data as *Timing*. For this study, we required that each response had at least  
297 one idea assigned to it (described below) to be included in the study. Therefore, student responses are  
298 not paired pre- and post-tutorial.

299 As part of previous work, Shiroda et al. (2021) coded these CRs using a rubric previously  
300 described by Sripathi et al. (2019; Table 1). Each response is dichotomously scored for each of the  
301 seven ideas, to indicate the presence (1) or absence (0) of the underlying idea in the rubric (described  
302 below). Briefly, a previous study validated ideas predicted for each response using a machine-  
303 learning model. As part of that validation process, an expert (MS) with a PhD in biology  
304 independently assigned ideas using the rubric for the full set of 418 responses. Human and computer  
305 assigned ideas were then compared; any disagreements between human and computer ideas were  
306 examined by a second coder (KH) with a PhD in biology. The two human coders discussed all  
307 human-human disagreements until agreement was met between the two human coders. The full  
308 coding procedure and validation are detailed further in Shiroda et al. (2021). This produced a data set,  
309 with each response having values for seven ideas (i.e. a zero or one for each of seven ideas).

310 The applied rubric targets seven common ideas used by college students in response to the  
311 assessment item: Correct Molecular Products (carbon dioxide and water), physiological Exhalation  
312 (the weight leaves the body via exhalation in the form of carbon dioxide and water), and Molecular  
313 Mechanism (cellular respiration), *General Metabolism*, *Matter Converted to Energy*, *How to Lose*  
314 *Weight*, and *Excretion* (described further in Table 1). The first three ideas (underlined) are normative  
315 or scientific. The last four (italics) are non-normative or naïve ideas, in that they are not a part of an  
316 expert answer (Sripathi et al. 2019). All ideas can co-occur within the same answer, except General  
317 Metabolism and Molecular Mechanism. Molecular Mechanism is more specific than General  
318 Metabolism; therefore, Molecular Mechanism is coded in preference to General Metabolism if they  
319 both occur in the same CR.

320 Using these seven ideas, CRs were further categorized into one of three exclusive Thinking  
321 groups (Developing, Mixed, or Scientific) based on the inclusion of ideas associated with normative  
322 and non-normative ideas (Sripathi et al. 2019). This information is reflected in the categorical data as  
323 *Thinking*. Briefly, Developing responses contain one or more non-normative ideas and no normative  
324 ones (n = 181). Scientific responses contain one or more normative ideas and no non-normative ideas  
325 (n = 88). Mixed responses contain at least one normative and at least one non-normative idea  
326 (n=149). Responses that have none of the seven coded ideas were not included in the study.

### 327 *Text Analysis.*

328 We compared the frequencies of words within categories of CRs between or among the  
329 categories of data (Thinking, Timing, or Type) in WordStat (v.8.0.23, 2004-2018, Provalis

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331 Research). We used the default program settings including a Word Exclusion list which removes  
332 common words and a preprocessing step of stemming (English snowball). Stemming removes the  
333 end of a word in order to mitigate the effect of different tenses, singular/plural, and common spelling  
334 errors. Words that have undergone stemming are noted in the text as the stemmed root with a dash  
335 (e.g. releas-). We did post processing of the text to keep only words with a frequency greater than or  
336 equal to 30 in the whole data set, and a maximum of 300 words were kept based on TF-IDF. TF-IDF  
337 stands for Term Frequency–Inverse Document Frequency and is a common statistic in text analysis  
338 used to reflect the importance of a word in a corpus. This measure weights words based on how  
339 much they are used but also accounts for those that are consistently used, meaning conjunctions and  
340 articles are not prioritized (Rajaraman & Ullman, 2011). In combination, these are the default settings  
341 in WordStat and are a way of focusing the results and preventing finding arbitrary, unmeaningful  
342 statistical differences based on chance (Welbers et al, 2017). Significance was determined by  
343 tabulating case occurrence in each grouping using a Chi-square. Words with  $p < 0.05$  were considered  
344 significant.

345  
346 *Calculations and ED measures.*

347 All ED metrics were calculated in PC-ORD (version 7.08; McCune & Mefford, 2018). An  
348 ecological example of these calculations is provided in Figure 1A, while Figure 1B provides a text  
349 example. For the work presented in the body of the work, words were stemmed using Snowball  
350 (English) to limit the effect of tense. Misspellings were not corrected. No words were excluded.  
351 Other processing settings that we tried are described below. The resulting raw matrix has 418 rows  
352 (responses) and 694 columns (words).

353 Richness (S or  $\alpha$ ) is the number of non-zero elements in a row, or the number of unique words  
354 within a single response. Values provided for a categorical group are the averaged values for each  
355 response for the group.

356 Evenness (E) is a way of determining if a species (or word) is more common in an  
357 environment (or CR). In other words, a sample that is heavily dominated by a given species or word  
358 has a low evenness (0), while a sample that has the exact same frequency of each word has an  
359 evenness of 1. For example, in Figure 1A, samples A and C have an evenness of 1 as they are exactly  
360 the same. In contrast, sample B is more dominated by triangles, resulting in a lower evenness value.  
361 This calculated using the following equation:

$$E = \frac{H'}{\ln(S)}.$$

362 Beta diversity ( $\beta$ ) compares the species occurrences between samples (Whittaker 1967; 1969).  
363 A low  $\beta$  value indicates that two samples are very similar in species content, while a high  $\beta$  value  
364 indicates two samples are very different. This calculated using the following equation (PC-ORD  
365 version 7.08; McCune & Mefford 2018; Figure 1A):

$$B = \frac{\gamma^2}{\alpha} - 1 .$$

366 In cases where the researcher wishes to compare  $\beta$  between three or more samples, we divide  $\gamma$  by  
367 the mean of  $\alpha$  for all samples. The resulting value is  $\beta$  of all samples and represents how many  
368 samples there would be if  $\gamma$  and  $\alpha$  per sample did not change, and all the samples share no species in  
369 common.

370 Species turnover (also called Absolute Species Turnover or half-change) represents the  
371 amount of difference between two samples. A value of one represents 50% of the species being  
372 shared and the other 50% being unique. Ecologists often use the term “half-change” to describe this  
373 condition. At two half-changes, 25% of species are shared between two samples. At four half-  
374 changes, the two samples are said to essentially not share any species. In contrast to  $\beta$ , there is not a  
375 simple relationship between species turnover and S. Species turnover can still be affected by S, but

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378 the relationship between the two can be either positive or negative (Yuan et al., 2016). Species " 379 turnover is calculated by the formula: "

$$380 (s_1 - c) + (s_2 - c),$$

381 where  $s_1$  is the number of words in the first CR,  $s_2$  is the number of words in the second CR, and  $c$  is " 382 the number of words shared by both CRs (PC-ORD version 7.08; McCune & Mefford 2018). "

383 Bray-Curtis dissimilarity (or Sorenson dissimilarity) is a measure of percent dissimilarity. 384 This measure ranges from 0 to 1, with 0 indicating two samples share all the same species. It is is " 385 calculated using the formula: "

$$386 1 - \frac{W}{A+B},$$

387 where  $W$  is the sum of shared abundances and  $A$  and  $B$  are the sums of abundances in individual 388 responses (PC-ORD version 7.08; McCune & Mefford 2018).

389 Shannon's diversity index ( $H'$ ) represents the certainty of predicting a *single* species of a 390 randomly selected individual. This can be affected by both Richness ( $\alpha$ ) and Evenness. For example, 391 if a sample contains only one species, the uncertainty of selecting that species is 0. This uncertainty 392 can increase in two ways. First, uncertainty increases as more species are added (Figure 1A; sample 393 A vs C) or by changing evenness (sample A vs B). If a community is dominated by a single species 394 (low Evenness), it becomes more certain that the dominant species will be selected, thereby 395 decreasing  $H'$ . It is therefore important when interpreting this measure that both richness and 396 evenness be considered. Generally, this measure is more affected by richness than evenness (Zeleny, 397 2021). While not depicted in the figure,  $H'$  would be calculated individually for Responses A, B, and 398 C and then averaged to obtain a value for a category of responses or the corpus as a whole (Jurasinski 399 et al., 2009).  $H'$  is calculated using the formula:

$$400 - \sum P_i \times \ln(P_i),$$

401 where  $P_i$  is the proportion of the  $i$ -th word in the entire data set (Shannon, 1948).

402 Simpson's diversity index ( $D$ ) is the probability that *two* randomly selected individuals will 403 be the same species. The probability of this decreases as richness increases and increases as evenness 404 decreases (Zeleny, 2021). As with  $H'$ ,  $D$  would be calculated individually for Responses A, B, and C 405 and then averaged to obtain a value for a group of CRs (Jurasinski et al., 2009). In comparison to  $H'$ , 406  $D$  is more influenced by evenness than richness. This is calculated using the formula:

$$407 1 - \sum P_i \times P_i,$$

408 where  $P_i$  is the proportion of the  $i$ -th word in the entire data set (Simpson, 1949). The value of 409 Simpson's  $D$  ranges from 0 to 1, with 0 representing maximum diversity, and one denoting none. As 410 a larger value represents a lower diversity, this is often presented as the inverse Simpson Index, 411 which is calculated by dividing 1 by  $D$ . These values are provided in the Supplemental Material 412 (Supplemental Table 1).

### 413 *Ordination techniques.*

414 Ordinations were performed using a curated word matrix that was created using a custom 415 word exclusion list (containing articles, conjunctions, and prepositions) to reduce the number of 416 uninformative, but frequent words (Table 2) in the raw matrix described above. We chose to exclude 417 these words to focus the ordination analysis on informative language, pertinent to the science ideas, 418 in the responses. We also excluded any words that did not occur in at least three responses, as 419 patterns cannot be detected with a lower frequency and these words likely represent very infrequent 420 ideas or ways students use ideas in our corpus. The resulting final data matrix or term-document 421 matrix for ordination contained a total of 254 words (columns) and 418 responses (rows). We 422 performed DCA and PCoA in PC-ORD (version 7.08; McCune & Mefford 2018). Depending on the 423 data set, some ecologists will transform the raw data in order for it to be used with certain methods. 424 As we selected methods designed to work with our data set, we did not perform any transformations. 425

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426 The calculations needed to perform ordination techniques are performed within the software package  
427 in which several settings need to be selected. First, ordinations are calculated using a seed number  
428 which can be randomly selected or entered. Each seed number results in similar patterns, but with  
429 slightly different numbers; therefore, we selected the seed number 999. This ensures that the exact  
430 ordination calculations can be repeated. For DCA, we elected to down-weight rare words due to the  
431 large size of the data set. This focuses the ordination on overarching patterns in the data. For PCoA, a  
432 distance measure has to be selected. Similar to ordination itself, each measure has positive and  
433 negative attributes. We selected Bray-Curtis distance as it is optimal for non-normal data (Goodrich  
434 et al, 2014). Scores were calculated for words using weighted averaging. We examined the  
435 significance of each axis using 999 randomizations. The percent inertia (or variance explained) for  
436 each axis is provided in the outputs of the PC-ORD file and included in our results. We compiled  
437 categorical data (Type, Timing and Thinking) associated with the CRs into a separate secondary  
438 matrix for ordination and used this secondary matrix with PC-ORD software to visually distinguish  
439 data points of different categories to help further reveal patterns of (dis)similarity in the data. DCA  
440 ordinations were then visualized using the R software package “phyloseq” (McMurdie & Holmes,  
441 2013). Ellipses marking the 95% multivariate t-distribution confidence intervals were added to  
442 increase readability. PCoA ordinations were visualized in PC-ORD.  
443

### 444 *Testing of other text processing protocols for ED metrics and ordination.*

445 For the ED metrics and ordinations, we also generated raw matrices using lemmatization (in  
446 place of stemming) and correcting misspellings from CRs, as these approaches are also common in  
447 the field of lexical analysis. We supply results from this other trial in Supplemental Table . Overall,  
448 results from these other text processing methods resulted in similar patterns for the ED metrics  
449 further described in the Results from stemming and no misspelling correction. For ordination, we  
450 also tested multiple word exclusion lists and frequency thresholds. Our trials included using the  
451 Default Exclusion list from WordStat, removing only “a, and, in, the” and the custom exclusion list  
452 provided in Table 2. We also tested frequency thresholds of 3 (minimum needed for pattern), 5  
453 (present in 1% of responses), 22 (present in 5% of responses), and 50 (present in 10% of responses).  
454 Finally, we also tested using the raw matrix without any text processing. Each of these combinations  
455 resulted in a different number of words within the matrix, ranging from only 20 to 898 words (data  
456 not shown). When performing the ordination on these matrices, it affected the inertia explained but  
457 not the patterns in the graphs (data not shown). We selected the setting used herein as it was a middle  
458 number of words (264) and seemed to be the most representative of the language in the responses.  
459 However, others may choose a different exclusion list or frequency threshold, depending on their  
460 application.  
461

### 462 *Statistical analysis.*

463 PERMANOVAs (PERmutational Multivariate ANalysis Of VAriance) were calculated in PC-  
464 ORD (version 7.08; McCune & Mefford 2018). PERMANOVA is a statistical F-test on the  
465 differences in the mean within-group distances among all the tested groups (Anderson, 2017),  
466 meaning the relatedness of groups of data points in all dimensions. PERMANOVAs require that each  
467 group being tested has an equal number of samples in order to be performed. Since the categorical  
468 data is not balanced, we performed bootstrap or batched PERMANOVAs, meaning we created 1,000  
469 different random samples of each group and performed a PERMANOVA on each random sample.  
470 The number of responses in each test was limited by the lowest n of each category within the  
471 grouping (Thinking = 88; Timing = 205; Type = 137). Interpretation of this p-value is fundamentally  
472 the same as it would be for other statistical tests. ANOVAs were performed with Tukey HSD and a  
473 cutoff of 0.05 in SPSS (IBM Corp., 2020).  
474

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475 *Data Availability.*

476 The raw word matrix, curated matrix used for ordination, and associated categorical data are  
477 available on GitHub (<https://github.com/BeyondMultipleChoice/suppmats>). Researchers who are  
478 interested in the responses may contact the final author (haudekke@msu.edu).

479

## 480 3 Results

481 *Comparison of Categorical Groupings and Text Analysis*

482 We expected student language included in their CRs to be reflective of their ideas; therefore,  
483 we began by examining the distribution of ideas across the sub-groups within each of the Thinking,  
484 Timing and Types categories. To support these claims, we also performed traditional methods of text  
485 analysis to examine word usage within the different categories. These analyses are used to provide a  
486 point of comparison for findings of the ED methods, in addition to conclusions from previously  
487 published efforts.

488 *Distribution of Ideas:* There is no overlap in singular ideas between Developing and  
489 Scientific thinking responses. We therefore expect the difference in language between Developing  
490 and Scientific responses to be the greatest in the data set. In contrast, Mixed thinking responses share  
491 some ideas with both Developing and Scientific thinking. As Mixed responses can share ideas with  
492 both Scientific and Developing responses, we expect Mixed responses to be an intermediate between  
493 Scientific and Developing CRs, using some text common to both Scientific and Developing CRs.  
494 While four of the seven ideas are considered Developing in our coding scheme, there is a higher total  
495 number of Scientific ideas (267) within the Mixed Thinking responses than Developing ideas (212).  
496 We therefore expect that there will be more similarities between Mixed and Scientific responses than  
497 Mixed and Developing responses. We expect student language to also change based on Timing of  
498 collection. This expectation is supported using a larger data set, which found that student  
499 explanations after an online tutorial included more scientific ideas and fewer Developing ideas (Uhl  
500 et al. 2021). Uhl and colleagues found that six of the seven ideas were each significantly different  
501 based on whether they were collected pre- or post-tutorial (2021). As this data set is a subset of that  
502 data, we expect this pattern to hold, resulting in language differences based on Timing. Finally,  
503 Shiroda et al. also examined the idea distribution in this data set by Institutional Type in previous  
504 work (2021). Only three of the seven ideas were statistically different ( $p < 0.05$ ) among the  
505 Institutional Types; therefore, we expect there to be the least amount of variability based on  
506 institutional Type in comparison to Timing or Thinking.

507 *Text analysis:* Using quantitative text analysis, we found that 25 words were significantly  
508 different among the Thinking groupings ( $p < 0.05$ ). *H<sub>2</sub>O*, *water*, *releas-*, *cellular*, *respir-* and *form*  
509 were more common in Scientific responses. *CO<sub>2</sub>*, *carbon*, *respir-*, *convert*, and *dioxid-* were more  
510 common in both Mixed and Scientific responses. Mixed thinking responses were also more likely to  
511 have *exhal-*, *glucos-*, *sweat*, *urin-*, *breath-*, and *broken*. Finally, *energi*, *weight*, *burn*, *bodi*, *diet*, *cell*,  
512 *fat* and *store* were more frequently in Developing responses. The words *lost* and *mass* were more  
513 frequent in both Developing and Mixed responses. We performed similar quantitative text analysis  
514 for the Timing groups and found 13 words significantly different between responses that were  
515 collected Pre or Post-tutorial ( $p < 0.05$ ). Post-tutorial responses more frequently contained *CO<sub>2</sub>*,  
516 *glucos-*, *water*, *cellular*, *H<sub>2</sub>O*, *respir-*, *breath*, *sweat*, *dioxide*, *convert*, and *ATP*, while post-tutorial  
517 responses contained *fat*, *weight*, *energi*, *bodi*, and *diet* more frequently. Finally, we found the fewest  
518 number of significantly different words (5) among Types. TYCs more frequently contained the words  
519 *turn*, *urin-*, and *sweat*. TYCs and PUIs also contained the words *exhale* and *weight* in comparison to  
520 RICUs. In summary, by comparing the number of predictive words across the three possible  
521 groupings (Thinking, Timing, and Type), we found the most difference in text based on Thinking,

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522 followed by Timing and Type, respectively. The results from the quantitative text analysis agree with  
523 our expectations based on idea distribution and previous studies.

524

525 *Quantitative measures of ED quantify student language differences.*

526 Richness (S) is the number of unique non-zero elements in a response and is the same as  
527 alpha diversity. As S varies heavily for the responses, we provide a box plot of the data in the  
528 supplemental data (Supplemental Figure 1). The mean richness of all CRs is 18.5 (Table 3). The  
529 average response length is 22.5 words, indicating that students do not heavily repeat words in their  
530 responses. The S of responses grouped by Institutional Type are comparable (range: 16.7-18.4) to the  
531 overall data set and each other. We did not find any statistical difference among these groupings  
532 ( $p=0.41$ , ANOVA). Similarly, the S of Pre- and Post-tutorial responses is 18.3 and 16.8, respectively.  
533 This difference was statistically supported ( $p=0.045$ ; ANOVA). The greatest difference in S is  
534 observed among Thinking groups. Responses classified as Scientific have lower S (11.9) than  
535 Developing (18.1) or Mixed responses (21.7). This difference was statistically supported for the  
536 groupings overall ( $p<0.00001$ ) and between the individual pairings ( $p<0.02$ ; Tukey HSD). This  
537 suggests that Scientific responses use relatively few unique words in the responses. This fits with our  
538 prediction as Scientific responses include scientific ideas, often expressed with fewer possible terms.  
539 As richness is used to calculate some of the following metrics, these differences in S should be  
540 considered when interpreting those results.

541 Evenness (E) is the comparative frequency of words in a response. At an E of one, all words  
542 in a CR occur in equal frequencies, while low values mean that students heavily use certain words.  
543 The entire data set has a value of 0.98, indicating most words occur at the same frequency within an  
544 individual CRs. This is expected, as the CRs are relatively short, meaning most words are likely used  
545 once. Similar values for evenness are observed for each category within Type (range: 0.98-99;  $p =$   
546 0.98, ANOVA) and Timing (range: 0.98-99,  $p = 0.06$ , ANOVA). Differences in E are greatest within  
547 Thinking groups. Mixed and Developing responses have the lower values of 0.979 and 0.984,  
548 respectively, while Scientific Thinking responses have a higher value of 0.99 ( $p < 0.00001$ ), with  
549 each pairing being significantly different ( $p<0.05$ ; Tukey HSD). As S is the denominator in the E  
550 formula, this change in E is likely due to the observed differences in S.

551 The Simpson's index of diversity (D) is calculated using a single CR and averaged for a  
552 group. Higher numbers represent low diversity. The corpus has a value of 0.91, indicating the CRs  
553 have high diversity and are not repetitive. Type (range: 0.90-0.92;  $p = 0.14$ , ANOVA) and Timing  
554 (range 0.90-0.92;  $p = 0.42$ , ANOVA) have similar values. In contrast, within Thinking, Scientific  
555 responses have the lowest value of 0.87, while Developing and Mixed Thinking have values of 0.93  
556 and 0.90, respectively. This difference is significant between all pairings within Thinking ( $p < 0.05$ ;  
557 Tukey's HSD). This result means there is a higher probability that two random words are the same  
558 within a Scientific CR in comparison to the other individual CRs in the Thinking categories and the  
559 corpus overall. This could, in part, be due to the Scientific category having the lowest S of the  
560 categories.

561 Shannon Diversity ( $H'$ ) can be interpreted as the chance of predicting a random word in a CR.  
562 If a single word is very frequent in a dataset, then there is a higher likelihood a prediction will be  
563 correct (low  $H'$ ). The  $H'$  of the whole data set is 2.65. Type (range: 2.60-2.71;  $p = 0.34$ , ANOVA)  
564 and Timing (range: 2.59-2.70;  $p = 0.68$ ) have similar  $H'$  values among categories and in comparison,  
565 to the corpus as a whole. In contrast, Thinking groups have more varied  $H'$  values of 2.88, 2.64 and  
566 2.27 for Mixed, Developing and Scientific, respectively ( $p < 0.00001$ , ANOVA). Each pairing is  
567 significantly different within Thinking ( $p < 0.005$ , Tukey HSD). These results indicate that Scientific  
568 responses are more repetitive in comparison to other CRs. These results agree with findings using D,  
569 indicating the words in a Scientific response are more predictable. Again, this could be due to the  
570 large difference in S based within Thinking.

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Whittaker's beta ( $\beta$ ) diversity compares the shared words between two responses. Low values represent less diversity with many shared words between the responses, while high values indicate high diversity with fewer words being shared. Our entire dataset has a  $\beta$  diversity of 38.6, meaning diversity within categories is much lower than diversity across all responses. When we examined  $\beta$  diversity within the different Types, we found slightly varied  $\beta$  diversities, with RICUs, PUIs and TYCs having values of 36.7, 38.7 and 40.6, respectively. The relative similarity between the groups and the overall  $\beta$  diversity of the entire data set suggests there is little difference in student CRs based on Type. We found a similar result with Timing, as responses collected Pre- and Post- tutorial responses have  $\beta$  diversities of 37.0 and 40.4, respectively. As with the previous ED metrics, we found there is a more distinct difference in  $\beta$  diversity based on the groupings within Thinking. While  $\beta$  diversities of Developing and Mixed CRs are similar at 37.4 and 31.0, respectively, responses in the Scientific category have a much higher  $\beta$  diversity of 57.3. This measure supports our prediction that the largest difference would be within Thinking. These results suggest that Scientific CRs share the fewest words with each other, while Mixed CRs share the most words. We had expected that Scientific responses would share more words between responses than any other category in Thinking, as the ideas and thereby language would be the most restricted. The increased value may be due to the lower  $\alpha$  (or  $S$ ) of the Scientific CRs (9) in comparison to Mixed (21.7) and Developing (18.1) Thinking, as it is the denominator in the calculation of  $\beta$ .

Species turnover or half changes is calculated based on shared words between paired responses. As the number of half changes increases, responses share fewer and fewer words. We calculated species turnover for the entire data set and found the corpus has a mean of 2.3 half changes, meaning that, on average, two CRs in the corpus share less than 25% of words. We also calculated species turnover based on groupings in the categorical data. We found categories within Type, Timing, and Thinking all have similar half change ranges: Institution: 2.2-2.4 (about 21.5% to 19% words shared); Timing: 2.2-2.4 (about 21.5% to 19%), and Thinking: 2.0-2.3 (25% to about 20% words shared). Mixed and Scientific responses are the categories with the lowest values of 2.0 average half changes. These results also support our prediction that the greatest difference in text would be within Thinking. In contrast to findings using the  $\beta$  metric, Mixed and Scientific responses have more similar species turnover values than Developing CRs. This result agrees with our stated predictions.

A third way to examine variation is to calculate the compositional dissimilarity using a distance measure. The Bray-Curtis dissimilarity has a value of 0% when two responses are exactly the same and 100% when no words are shared between responses. We calculated this measure for each pairing in the entire corpus and found the data set has a dissimilarity of 80.36%, indicating that the text used in the entire response set is more dissimilar than similar. This indicates any CR is on average 80% different from any other, which is similar to findings from species turnover above. We also calculated the Bray-Curtis dissimilarity for the categorical groupings. Within Types, there are similar dissimilarities of 80.62%, 81.57% and 78.49% for TYCs, PUIs and RICUs, respectively. These values are also very similar to the overall data set, suggesting that each category shows similar patterns to the overall data set. For Timing, the dissimilarities are 80.94% and 78.54% for Pre- and Post-tutorial responses, respectively, suggesting there is little change in language based on Timing. In contrast, the Bray-Curtis dissimilarity of Developing responses (80.19%) is higher than that of Mixed (74.98%) or Scientific (74.94%) responses. As with species turnover, Mixed and Scientific responses have more similar values in comparison to Developing CRs.

*Ordination techniques aid in visualization and reveal patterns in the corpus.*

Each of the measures described above describes diversity *within groups* or *group averages* of single CRs; however, we are also interested in examining and measuring potential differences *between groups* of CRs. Using DCA (Figure 3A) and PCoA (Supplemental Figure 2), we created

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620 two-dimensional plots of the corpus, wherein each data point is an individual CR. Points that are  
621 close to each other are more similar based on word choice and frequencies in the CR. Each axis,  
622 beginning with the x-axis, explains a descending amount of variation in the data in an additive  
623 manner and likely has multiple aspects of the data contributing to it.

624 *Detrended Correspondence Analysis (DCA)*. DCA is uniquely suited to our purpose as the x-  
625 axis is defined exclusively as species turnover, meaning points (responses) that are the furthest away  
626 from each other on the x-axis have the highest difference in words. Additionally, every 100 units on  
627 the x-axis of the DCA graphs represents one half-change of words, allowing direct comparison of  
628 data by species turnover measure. The DCA of the entire data set results in two responses, 35 and 78,  
629 far removed from other data points. CR35 is located at (190, 5012) and reads, “Excretion.” CR78 is  
630 located at (1186, 179) and reads, “Into the air via C0<sub>2</sub>.” (Underlined words are removed during the  
631 matrix generation process; see Methods) These responses are very unique in comparison to other  
632 responses in the corpus (maximum axis 1 value: 449; maximum axis 2 value: 344) and render the rest  
633 of the graph uninterpretable (Supplemental Figure 3). These responses were therefore removed as  
634 outliers (McCune & Mefford, 2018) from the data set used for DCA, to better examine the remaining  
635 data. The results from the DCA explained 7.7% of the total inertia (variability) of the resulting  
636 matrix (Figure 3A). The first axis explains 4.9% of the total variability and the second axis explains  
637 3.8%. For large data matrices, it is expected that two axes will not explain large portions of the data  
638 (Goodrich et al. 2014). To ensure the patterns are still meaningful, randomization tests determine if  
639 the axes are significant in comparison to randomized orders of the data. We found that both axes  
640 significantly explained the data (999 randomizations;  $p < 0.003$ ). Data points range from 0 to 434.5  
641 on the x-axis (Figure 3A), demonstrating that extremes of this corpus do not share any words, as 4  
642 half changes between points is interpreted to be essentially unique.

643 *Principal Coordinate Analysis (PCoA)*. In contrast to DCA, PCoA does not have a specified,  
644 singular component or variable that is explained by any axis. As with DCA, close proximity of points  
645 means that they are more similar based on the component. We visualized our entire corpus using this  
646 ordination technique and did not observe any outlier responses that obscured the remaining data;  
647 therefore, no CRs were removed (see Supplemental Figure 2). We found six significant axes using  
648 this technique (1000 randomizations;  $p < 0.03$ ). Combined, these six axes explain 36.8% of the total  
649 variance. The first axis explained 9.4% of the data, while the second explained 7.6%. We found DCA  
650 and PCoA provided similar results and will therefore only describe DCA results due to the usefulness  
651 of the first axis in calculating half-changes between responses.

652 *Ordination techniques allow easy examination of corpuses of short texts*. Using the ordination  
653 graph from DCA (Figure 3A), we can easily identify CRs that are very similar or different without  
654 reading the responses. CRs 14, 19 and 418, marked in Figure 3A, are very close to each other,  
655 indicating much similarity in word usage. These CRs read: “CO<sub>2</sub> H<sub>2</sub>O” “CO<sub>2</sub> and H<sub>2</sub>O” and  
656 “Transferred into CO<sub>2</sub> and H<sub>2</sub>O,” respectively. (Underlined words are removed.) In contrast, data  
657 points that are on the two extreme sides of the graph share no words in common. Response 160 says  
658 “Probably the energy stored in the weight was used up by cells due to the decrease in calorie intake  
659 during the diet.” Responses 9 and 10 both say, “Carbon dioxide and water,” while response 40 reads  
660 “Expelled through gas like carbon dioxide.” During an initial examination of the data, it could be  
661 useful to quickly identify CRs that are very similar or very different, especially with very large data  
662 sets that would require large amounts of time to examine individually.

663 *Categorical data can be overlayed to reveal relationships among CRs*. Categorical data  
664 (Thinking, Timing and Type) associated with the CRs can be overlaid on the ordination graphs  
665 without affecting the placement of the data points, potentially illustrating patterns within the data set  
666 (Figure 3B-D). Centroids are the average coordinate value for the categorical group and are  
667 represented in the graphs by large plus signs. One way to examine differences between groups is to  
668 calculate distances between group centroids. We found the largest change in position for centroids

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669 based on Thinking groups, with the total distance between the centroids being 134.2 units.  
670 Developing thinking is left-most on the x-axis at 149.3, Mixed thinking is in the middle at 241.0 and  
671 Scientific thinking is right-most at 283.5. While centroids represent the average of the group,  
672 PERMANOVAs test the relatedness of groups of data points in all dimensions using the matrix used  
673 to create the ordination graph. Within Thinking, the differences in relative distance are significant  
674 (Figure 3B; PERMANOVA;  $p=0.0002$ ;  $n = 88$ ). For Timing (Figure 3C), there is slight separation of  
675 the data with post-tutorial responses as a group being more to the right of the graph. There is less  
676 distance between the two group centroids of 45 units (Pre: 186.8; Post: 231.8) in comparison to  
677 Thinking (134.2 units of separation). Using PERMANOVA, these Timing groups are also  
678 significantly different ( $p=0.0002$ ;  $n = 205$ ). Finally, there appears to be minimal difference based on  
679 the Institutional Type (Figure 3D). The centroids are at most separated by only 8.4 units on the x-axis  
680 (TYC: 206.4; PUI: 214.8; RICU: 207.9) and there is not an apparent distinct clustering of the CRs.  
681 PERMANOVA reveals low statistical support for differences based on Type ( $p = 0.084$ ,  $n = 137$ ).  
682 While we did observe separation among groupings for Timing and Thinking, we also note the spread  
683 of responses within these individual groups is similar, which is consistent with the very similar  
684 number of half changes observed using ecological measures (Table 3).

## 685 4 Discussion

686 The aim of this paper was to explore the novel application of established ecological diversity  
687 measures and methods for analyzing short, explanatory texts. CR assessment offers insight into  
688 student thinking or performance through student language, but quantitative evaluation of the  
689 language diversity in CRs is limited. For this data set, we previously identified and explored patterns  
690 of ideas present in student explanations (Shiroda et al., 2021) but were dissatisfied with the available  
691 methods to quantify and represent holistic differences in language between responses and/or groups.  
692 This limitation and previous work by Jarvis (2013) comparing ecological and lexical approaches to  
693 diversity, motivated us to examine ED approaches for text analysis. Herein, ED metrics and  
694 ordination allowed us to examine student language in a different way than other methods. We were  
695 able to quantify holistic differences in language that we had observed when comparing student  
696 responses based on Thinking, Timing and Type. The purpose of the current work is meant to be  
697 confirmatory in nature, in that we have already explored this CR corpus in previous work and had  
698 expected results based on this previous qualitative work. Namely, we expected the greatest difference  
699 in language to be among Thinking, some difference based on Timing, and little difference based on  
700 Type. Using these predictions, we could examine whether the outcomes from the ED metrics and  
701 ordination techniques corresponded to construct-relevant differences in student CRs.

702 Overall, we applied seven ED measures to this data set. Richness or alpha diversity, while  
703 helpful in other calculations, does not reveal anything uniquely useful, as this can be easily calculated  
704 with other forms of text analysis. Similarly, evenness was not particularly useful in itself given how  
705 short most responses were, as students are unlikely to heavily repeat a given word in only one to  
706 three sentences. However, this information is important for interpretation of the other metrics and  
707 could be more useful in longer texts than ones used here. Shannon and Simpson diversity metrics are  
708 similar to existing lexical diversity measures in that they examine diversity of individual responses.  
709 One advantage of these ecological measures in comparison to those in lexical diversity is that they  
710 have no established lower limit on length. In spite of this, Shannon and Simpson are still influenced  
711 by evenness and richness. While this may not be problematic for all CR corpora, our data set had  
712 differences in richness based on Thinking and Timing, making the Shannon and Simpson measures  
713 more difficult to interpret for those categories of CRs.

714 We found comparing pairs of responses using Whittaker's  $\beta$ , Bray-Curtis Dissimilarity and  
715 Species Turnover to be the most interesting expansion of current text analysis approaches for our

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716 applications. These three measures each quantify differences between responses in slightly different  
717 ways. Additionally, each identified similar patterns in the categorical data, which correspond well to  
718 our previous, qualitative analysis of the corpus. Namely, that grouping responses by Thinking  
719 category has the largest effect on all three measures and suggesting that differences in student texts  
720 exist between sub-groups. Additionally, all three measures found that Developing CRs are very  
721 similar to the entire corpus. For each measure, Developing and Scientific responses are consistently  
722 most different from each other; however, Mixed responses are more similar to Developing responses  
723 with Whittaker's  $\beta$ , but more similar to Scientific responses when measured by Bray-Curtis  
724 Dissimilarity and Species Turnover. This result could be due to the difference in Richness (alpha)  
725 based on Thinking. Bray-Curtis Dissimilarity and Species Turnover also more closely agreed with  
726 our prediction that Mixed Thinking CRs would be more similar to Scientific CRs than Developing  
727 ones. We also identified a general pattern in the corpus that Scientific responses are more similar to  
728 themselves than the corpus overall. This is the only category within Type, Thinking or Timing that  
729 consistently had a unique value. This supports observations from rubric development and human  
730 coding during qualitative analysis, in that there are generally fewer ways to write correctly about a  
731 scientific idea than ways to write about incorrect or other, non-scientific ideas (Sripathi et al., 2019;  
732 Shiroda et al., 2021). We are excited these quantitative measures support these qualitative  
733 observations and consider these metrics promising for critically testing student language. As  
734 Whittaker's  $\beta$  shows a different pattern than Bray-Curtis Dissimilarity and Species Turnover, we  
735 considered which measures best suit our purposes. Bray-Curtis Dissimilarity and Species Turnover  
736 are less sensitive to differences in richness, which we prioritize because this difference is already  
737 apparent in the richness measure itself. Additionally, Whittaker's  $\beta$  is generally considered to be a  
738 very simple representation of diversity, which also contributes to our preference for Bray-Curtis  
739 Dissimilarity and Species Turnover.

740 Ordination offers a unique visualization of the CR corpus and greatly assists our comparison  
741 of language among different groupings of the CR corpus. While we can and did qualitatively  
742 examine the responses previously during human thematic coding (Sripathi et al., 2019; Shiroda et al.,  
743 2021), these processes take time. We imagine these techniques could be helpful as an exploratory  
744 phase of CR analysis, similar to LSA, to look for unique responses or determine if there are potential  
745 language differences among groups. Here, we used ordination in a confirmatory fashion. We  
746 expected Thinking to most affect student language because that is how the rubric and coding were  
747 designed. Similarly, we were expecting there to be differences based on Timing since changes in  
748 Thinking are associated with Timing (Uhl et al, 2021). In contrast, Shiroda et al (2021) found fewer  
749 apparent differences based on the institutional Type. These expectations are further supported by text  
750 analysis through having a decreasing number of predictive words. Indeed, ordination analysis  
751 reflected these expectations (Figure 3B-D), both in the more distinct clustering of responses using the  
752 categorical data and in the distance between group centroids. These overall clustering patterns could  
753 be observed in both DCA (Figure 3B-D) and in PCoA (Supplemental Figure 2B-D). While observing  
754 these patterns and calculating the half changes in the DCA are useful, PERMANOVA tests are a  
755 promising method to quantitatively compare groups of responses. Using this test, we confirm the  
756 largest difference in student text is among the groups within Thinking and between Timing, while  
757 there is limited support for differences in text among the Institutional Types groups. This allows us to  
758 conclude that student word choice differs for sub-groups in both Thinking and Timing, while word  
759 choice for CRs to this question is not related to Institutional Type. Differences between Thinking are  
760 heavily supported by the rubric, but the lack of differences in language among the institutional Types  
761 was only qualitatively supported in Shiroda et al (2021). In contrast, these PERMANOVA tests  
762 provide direct statistical rigor to the observations that are not possible with other analyses. These  
763 methods could be particularly useful in comparing differential language between groups to better  
764 understand the different ways students convey understanding. For example, when originally working

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765 with this data set, we were attempting to examine performance differences for a computerized text  
766 classification model with this data set in comparison to one that was used to create the model  
767 (Shiroda et al., 2021). Using these ordination techniques, one would be able to quickly and visually  
768 compare the original and new data sets to determine if student language was different between the  
769 sets. We have since successfully applied ordination techniques to understand other computer scoring  
770 model performance (Shiroda et al., under review). In comparison, similar text analysis approaches  
771 such as LSA may be helpful in exploratory analyses to find prevalent themes in responses but would  
772 be less helpful for this goal as they do not reveal differences in specific words and instead condense  
773 the meaning of the language. As such our novel application of ecological diversity measures may be  
774 used in complementary fashion with other text analysis methods depending on the research study.

775 We performed quantitative text analysis to support our expectations for the differences in CRs  
776 among the categorical data. Indeed, we found that these differences in ED measures correspond to  
777 differences in words identified by text analysis and which can be further linked to differences  
778 observed in human-assigned ideas (i.e. student thinking). This helps validate the ED metrics by  
779 identifying words and phrases which differ significantly in their usage between sub-groups.  
780 However, the ED methods and text analysis provide different pieces of information. While ED  
781 methods help compare individual CRs to each other, text analysis helps us understand differences in  
782 the actual text identified using the ED methods. For example, the words that are differentially used in  
783 responses categorized by coders as Scientific ideas include *H<sub>2</sub>O*, *water*, *releas-*, *cellular*, *respir-* and  
784 *form*. Most of these words are closely linked to the Scientific ideas identified in the coding rubric  
785 categories of Correct Products and Exhalation. The words *CO<sub>2</sub>*, *carbon*, *respir-*, *convert*, and *dioxid-*  
786 were more common in both Mixed and Scientific responses, indicating considerable overlap in how  
787 students describe how carbon leaves the system, but not *water* which was only frequently used in  
788 Scientific thinking. This information would not be clear using only the ecological methods we  
789 describe here. We therefore suggest that ecological methods be used in conjunction with text analysis  
790 to examine CR corpora.

791 In summary, we found that ED measures can be usefully applied to text analysis of students'  
792 short text explanations. In particular, methods that analyze between response variation (Whittaker's  
793  $\beta$ , Bray-Curtis Dissimilarity, Species Turnover, and ordination) were most useful for our interests in  
794 understanding CRs based on categorical data. For other research interests, Simpson, or Shannon  
795 diversity measures may be more informative. Similarly, richness and evenness do not seem to  
796 provide much additional insight to text diversity with this data set but are needed to better interpret  
797 the other ED measures and could be more informative for longer texts.  
798

### 799 *Future Directions and Considerations for Additional Applications*

800 These techniques help reveal differences in diversity within student language and different  
801 categories of the corpus; however, further analysis is needed to understand these results. With the  
802 exception of the first axis of DCA, it is difficult to interpret ordinations for specific differences in the  
803 text, as each axis represents multiple factors in the data. Similarly, while the different metrics (E, S,  
804 D, H',  $\beta$ , Bray-Curtis Dissimilarity and species turnover) quantify diversity and provide markers for  
805 the amount of variety in a group of responses, the metrics do not specify the nature of the differences.  
806 Determining these differences in language within the text is better achieved by text analysis, along  
807 with traditional qualitative techniques, such as coding of the responses. Therefore, we recommend  
808 that ED and ordination analysis be done to supplement text analysis and qualitative methods. For  
809 example, we performed text analysis as a proxy to differences in word choice, but examining the  
810 predictive words reveals an important difference in language. *Water* is only increased in Scientific  
811 CRs while *sweat* and *urine* are increased in Mixed thinking. This indicates that students with Mixed  
812 thinking are still having trouble articulating how water leaves the body in relation to weight loss and  
813 could serve as a target for improving student explanations. If we had only applied the ecological

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814 methods, we would know that there is a difference but not have an actionable conclusion that could  
815 promote teaching and learning.

816 We consider these analyses broadly applicable to any corpus of short texts. Our group has  
817 already successfully applied these analyses to multiple CR corpora to examine the progression of  
818 student language across physiology contexts (Shiroda et al., *in review*) and explore the effect of  
819 overlapping language on the success of machine learning models for automated assessment (Shiroda  
820 et al., *in review*). As with any ecological study, we began this study by considering the nature of our  
821 data set and recommend this as a critical first step before applying these methods to new data sets.  
822 We note that in applying these diversity methods to our data set, we made purposeful decisions about  
823 text processing, many of which led to meaningful interpretation of the results. However, we do not  
824 consider these decisions absolute for all applications and acknowledge that other data sets and/or  
825 outcomes will most likely justify different text processing decisions. For example, we chose to stem  
826 words for the diversity metrics, but not remove any other words. We chose these settings as it most  
827 closely matches the text analysis protocols that were used in the previous work. While we found the  
828 text processing method did not affect the overall patterns we found, this may not be true for other  
829 data sets (Supplementary Table 1). We selected this method as the settings are most similar to  
830 previous work, allowing this work to be more directly compared to previous work. For some CRs,  
831 the distinction between stemming and lemmatization may be important. For example, stemming is  
832 not exact in removing tense. It will remove words that maintain the same root but do not collapse the  
833 form of words that change fully such as “to be”. Since our question was in past tense, there was not a  
834 large number of differences in tense; however, for other data sets ensuring tense is collapsed may be  
835 more important to reveal patterns. Lemmatization does make these changes, but also collapses  
836 comparative words. For example, great, greater, and greatest are collapsed. Depending on the  
837 context, maintaining the levels of comparison could differentiate student thinking and be important to  
838 maintain. We strongly suggest that text processing decisions should be purposeful and tailored to the  
839 corpus.

840 Ordination requires separate, equally purposeful decisions to function correctly. We removed  
841 less meaningful words (e.g., articles, conjunctions, propositions), as common, unmeaningful words  
842 can skew the overall pattern of the data set. However, it is important to keep the CR context in mind  
843 when choosing text processing strategies. For example, if students are explaining the process of  
844 diffusion as part of a science course, the words ‘in’ and ‘out’ would be critical to student meaning in  
845 that context and should not be removed. We advise others using these techniques to examine their  
846 data to determine whether certain prepositions or words may be important. While text processing  
847 steps will likely differ, DCA and PCoA are likely to be most useful to examine language diversity in  
848 most CR data sets. A key advantage of these two approaches is that these methods can handle data  
849 sets with high percentages of zeros, which is likely to occur in most lexical datasets (i.e., short,  
850 content-rich texts). However, other ordination methods should be considered during the initial phases  
851 of data analysis to make sure the approach is appropriate for the data set and these other ordination  
852 methods explored further. For example, if a set of CRs is highly redundant, this could result in a  
853 lower percentage of zeros, opening the possibility of using ordination methods that our data  
854 excluded. We recommend that researchers who wish to apply these methods, but do not have an  
855 ecology background, seek out helpful texts including Peck (2010), Palmer (2019), and a website  
856 maintained by Oklahoma State University: <http://ordination.okstate.edu/key.htm>. We view the  
857 versatility and the ability to make purposeful choices for each data as a strength of the methodology.

858 While this study was confirmatory and the current paper is intended to describe the approach,  
859 we believe these techniques can also be used in an exploratory fashion. We were originally motivated  
860 to perform this work because we were excited by the potential to expand quantitative approaches to  
861 language diversity in CRs (or short blocks of text). The data visualization, various metrics, and  
862 statistical computations of our ED methods offer a rich and wide range of results that bring statistical

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863 and quantitative methods to a field that typically relies on qualitative methods. Overall, these ED  
864 techniques provide quantitative methods that will allow researchers to examine short texts in a novel  
865 way in comparison to current text analysis methods. Within STEM education research, these  
866 techniques can assist in the examination of differences in student writing and ideas over time, effects  
867 of a pedagogical intervention, differences in explanations across contexts for cross-cutting concepts,  
868 and many other forms of categorical data.

## 869 **5 Conflict of Interest**

870 The authors have no conflict of interest to disclose.

## 871 **6 Author Contributions**

872 First author performed data analysis and primarily drafted the manuscript. Second author assisted in  
873 data analysis and in drafting the manuscript. Third author provided feedback on the data analysis and  
874 manuscript. All three authors were involved in project design, execution, and editing of the  
875 manuscript.

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1042

## Quantitative Examination of Short Texts !

1044 **Table 1: Coding Rubric and Description.** Rubric ideas are marked with superscript to denote if  
 1045 ideas are normative (N) or non-normative (NN). These ideas are used to categorize CRs into  
 1046 Thinking categories. Developing Thinking responses contain one or more non-normative ideas and  
 1047 no normative ones. Scientific responses contain one or more normative ideas and no non-normative  
 1048 ideas. Mixed responses contain at least one normative and at least one non-normative idea. All  
 1049 categories can occur in the same response with the exception of Molecular Mechanism and General  
 1050 Metabolism. Molecular Mechanism is coded instead of both. Example responses are provided with  
 1051 the important words or phrases for that idea underlined. Spelling is corrected for clarity.  
 1052

Rubric Idea	Brief description	Example responses !
Correct Products <sup>N</sup>	Responses in this category include the idea that the products of cellular respiration, primarily carbon dioxide in any form are the result of mass loss.	The mass went to <u>water and CO<sub>2</sub></u> .
Exhalation <sup>N</sup>	Responses in this category include the idea that excess mass is exhaled or exits the body.	As glucose was burned off the mass was also <u>shed in the form of CO<sub>2</sub> and H<sub>2</sub>O</u> (sweat)
Molecular Mechanism <sup>N</sup>	Responses in this category include the idea that mass loss occurs due to correct molecular processes (e.g., cellular metabolism, beta oxidation), or describe these processes in specific detail.	That mass was broken down into energy that was used through <u>cellular respiration</u> .
General Metabolism <sup>NN</sup>	Responses in this category include the idea that mass loss occurs due to some kind of molecular conversion, even if it is only partially correct.	<u>Fats are converted into glucose, glucose is then broken down into energy and CO<sub>2</sub></u> , which then get expelled when you breathe.
Matter to Energy <sup>NN</sup>	Responses in this category include the idea that mass loss occurs through vague conversions from matter to energy.	Because the friend is not taking in as much as they had before, <u>the body turned the mass into energy</u> to do work.
Excretion <sup>NN</sup>	Responses in this category state that the mass is excreted out of the body. Responses must specifically indicate the physiological process of excretion by explicitly using the term “excreted” or similar or indicating physiological waste (i.e. sweat, feces or urine) in their responses.	I think the friend must have <u>gone to the bathroom and either pooped or peed it out</u> .
How to Lose Weight <sup>NN</sup>	Responses in this category include ideas about societal discussions of weight loss, such as “calories in” greater than “calories out” or exercise.	It was lost due to <u>a lower caloric intake</u> .

1053  
 1054 **Table 2: Words removed for ordination analysis.** These words were not removed to examine the  
 1055 diversity measures.

1056

Articles	a	an	the "				
Conjunctions	as	and	but	like	or "		
Prepositions "	aboard	about	above	across	after	against	along
	amid	among	around	at	before	behind	below
	beneath	beside	besides	between	beyond	by	concerning
	considering	despite	down	during	except	excluding	
	following	for	from	in	inside	into	minus
	near	of	off	on	onto	opposite	outside
	over	past	per	plus	regarding	round	since
	than	through	to	toward	towards	under	underneath "
	unlike	until	up	upon	versus	via	with "
	within	without "					

1057 "

1058 **Table 3. Ecological diversity metrics.** Calculated using stemming with spelling errors corrected.

1059 The values represent averages calculated from the individual responses (Richness, Evenness,

1060 Shannon and Simpson) or every possible pairing (Whittaker, Bray-Curtis, Turnover). "

Measure	All	Type			Timing		Thinking		
		TYC	PUI	RICU	Pre	Post	Dev	Mix	Sci
Richness (S, $\alpha$ )	18.1	17.2	17.9	19	19.2	17	18.1	21.7	11.9
Evenness (E)	0.984	0.984	0.984	0.983	0.982	0.985	0.901	0.937	0.992
Shannon Diversity (H')	2.65	2.63	2.6	2.71	2.7	2.59	2.64	2.88	2.27
Simpson's Diversity (D)	0.906	0.907	0.896	0.917	0.919	0.903	0.901	0.932	0.873
Whittaker's $\beta$ Diversity	37.4	39.3	37.7	35.5	35.2	39.9	37.4	31	57.3
Bray-Curtis Dissimilarity	80.4	80.6	81.6	78.5	81	78.5	80.2	75	75
Species Turnover	2.3	2.4	2.4	2.2	2.4	2.2	2.3	2	2

1061

1062 

## 11 Figures

1063 **Figure 1: Schematics of ecological diversity terms.** (A) For ecological diversity, three samples  
 1064 (open circles) are shown with differing numbers of individuals, representing a different species (filled  
 1065 shapes). Alpha values are given for each sample, and beta values are given for each pairing and the  
 1066 overall data set. Example calculations are provided for beta between Sample A and B and the data set  
 1067 overall. (B) For language applications, responses are compared instead of samples, while words are  
 1068 treated as individuals. Repeated words are equivalent to being the same species. While only single  
 1069 sentences are shown here, our data set contains many CRs that contain more than one sentence that  
 1070 are still treated as single samples. Alpha values are given for each response, and beta values are given  
 1071 for each pairing and the overall data set. Example calculations are provided for beta between  
 1072 Response A and B and the data set overall.

1073

1074 **Figure 2: Sample matrices.** (A) For ecological data matrices, samples are rows, while species are  
 1075 columns. Values in individual cells are the frequency of the given species in the sample. (B) In this

## Quantitative Examination of Short Texts

1076 example, each response is a row, while each word is a column. Values in cells are the frequency of a  
1077 word within the response.

1078  
1079 **Figure 3: Detrended Correspondence Analysis (DCA).** DCA was performed without any data  
1080 transformation. The graphs represent 416 responses after the removal of responses 35 and 78. (A)  
1081 The ordination was graphed with select responses numbered for discussion in the Results. Grouping  
1082 variables including (B) Thinking (C) Timing and (D) Type were overlaid to compare between  
1083 groups. Centroids of a given grouping variable are represented by plus signs. Ellipses are the 95%  
1084 multivariate t-distribution confidence of each categorical group.

Figure 1.TIFF

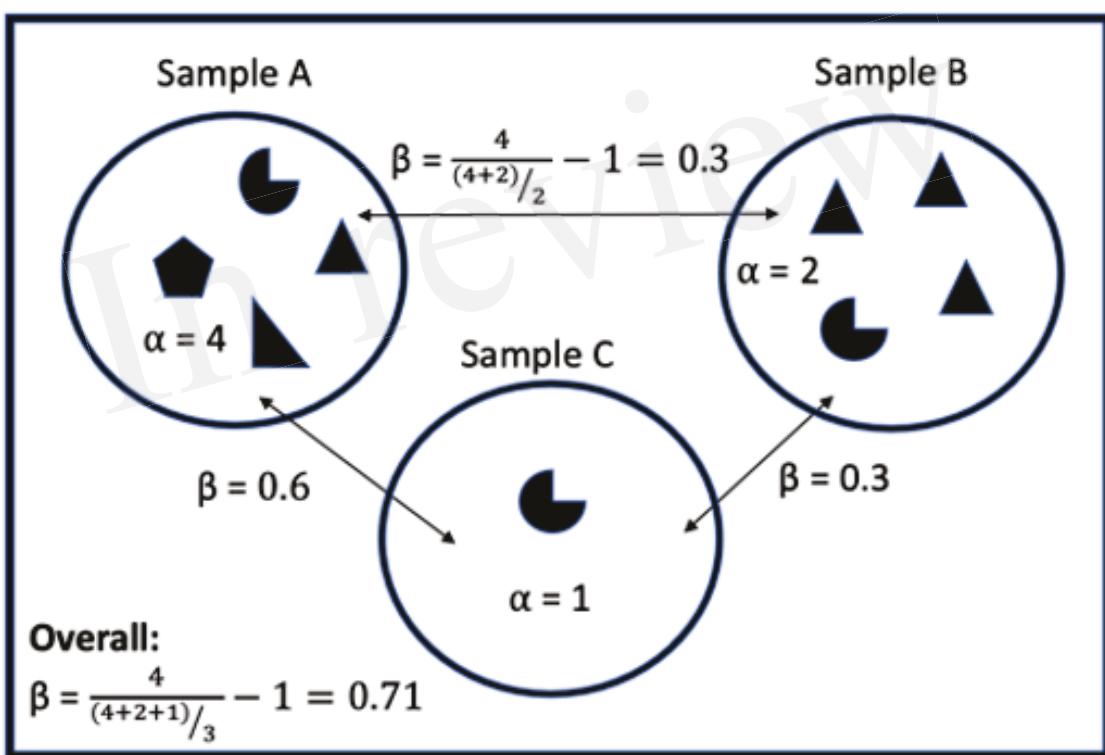


Figure 2.TIFF

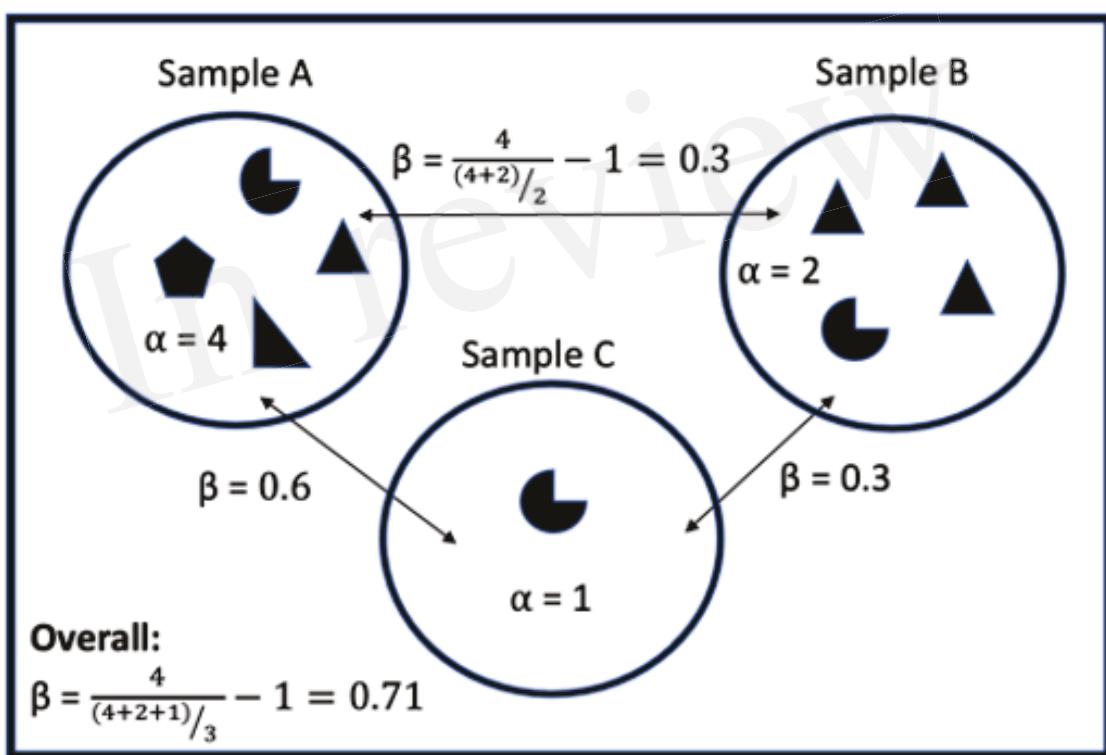


Figure 3.TIFF

Preview

Ecological	Species 1	Species 2	...	Species <i>n</i>
Sample 1	3	0	...	1
Sample 2	1	4	...	2
...	...	...	...	...
Sample <i>n</i>	0	1	...	0

Figure 4.TIFF

Language	Word 1	Word 2	...	Word <i>n</i>
Sample 1	3	0	...	1
Sample 2	1	4	...	2
...	...	...	...	...
Sample <i>n</i>	0	1	...	0

Figure 5.TIFF

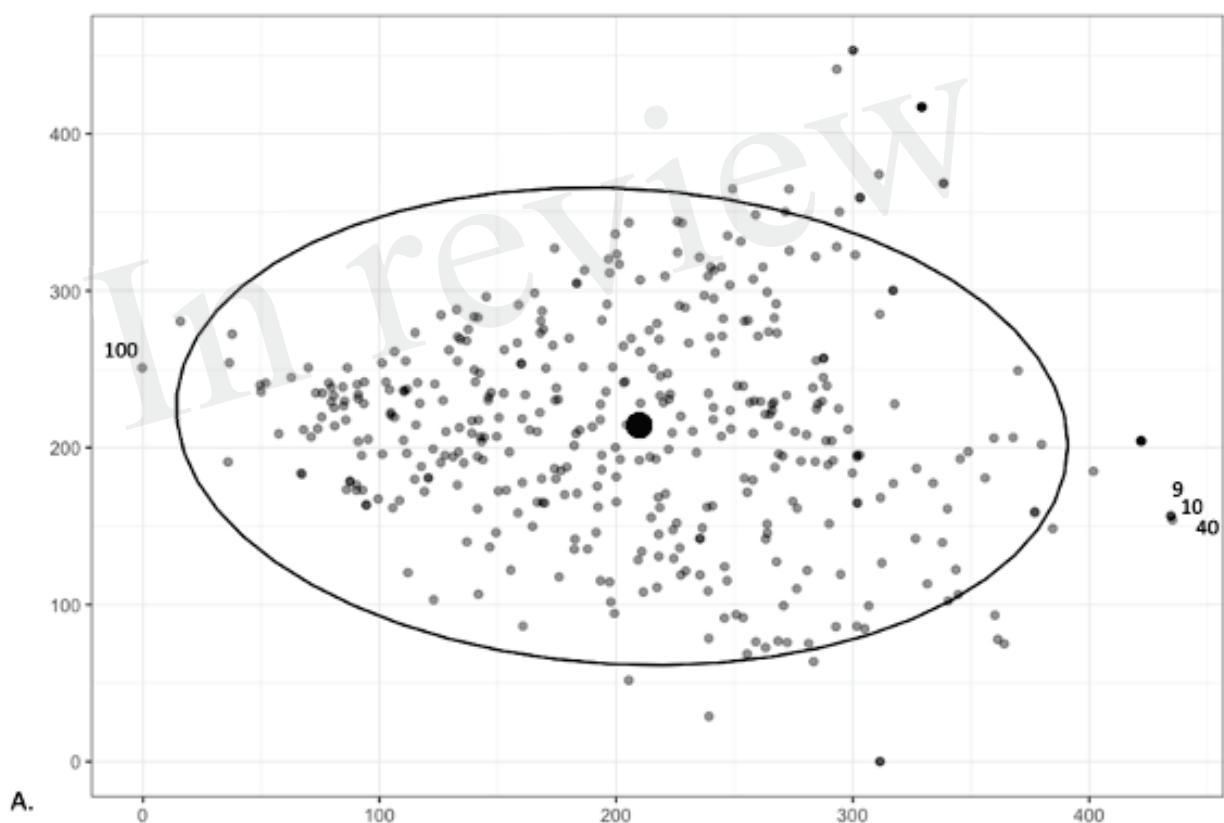


Figure 6.TIFF

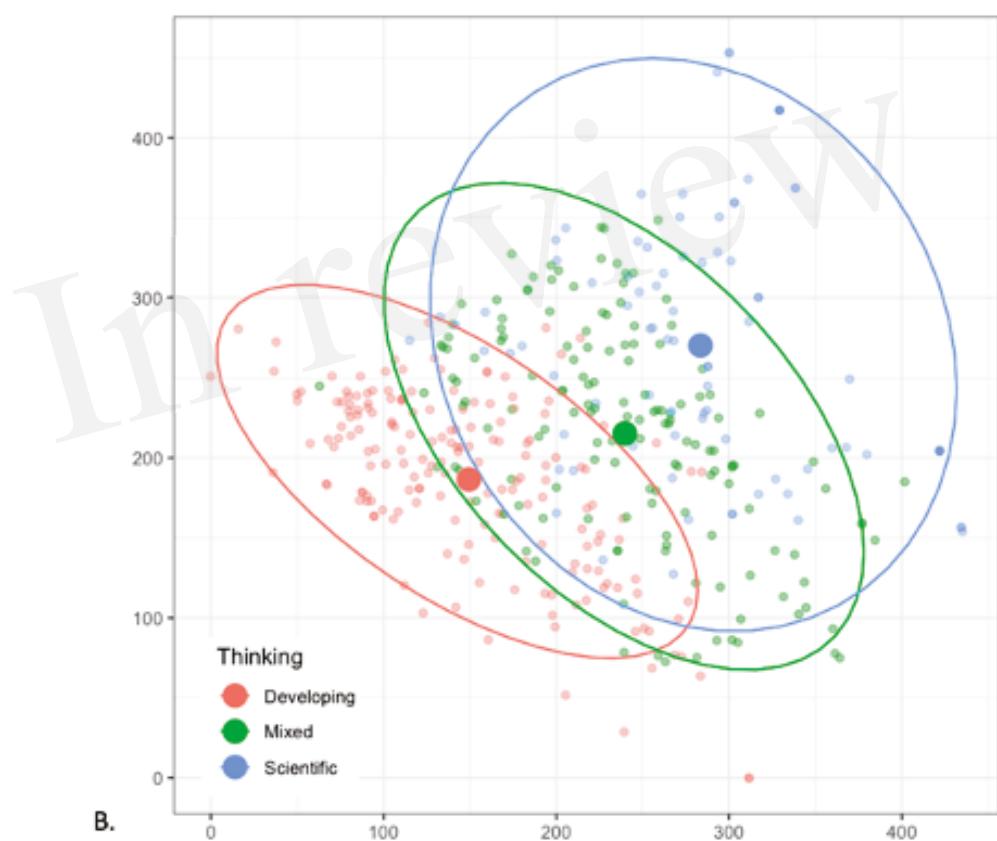


Figure 7.TIFF

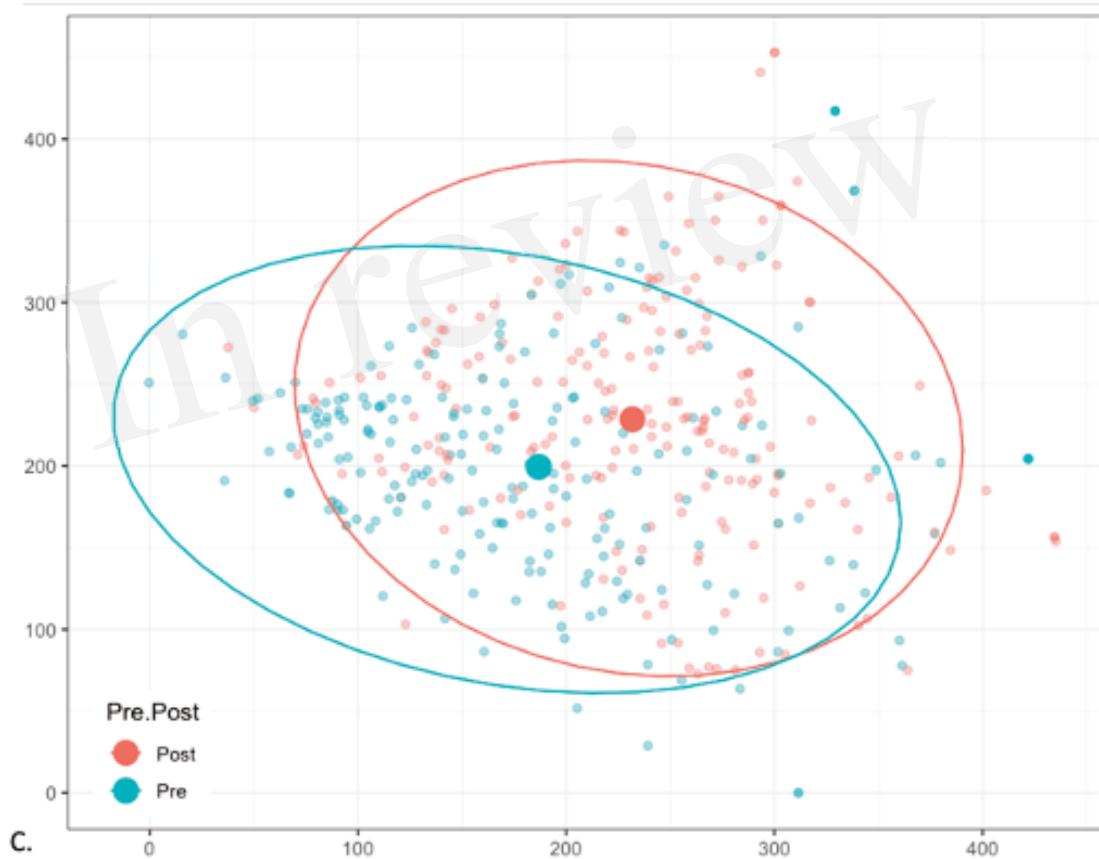


Figure 8.TIFF

