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# Disorder of excitons and trions in monolayer MoSe<sub>2</sub>

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## ABSTRACT

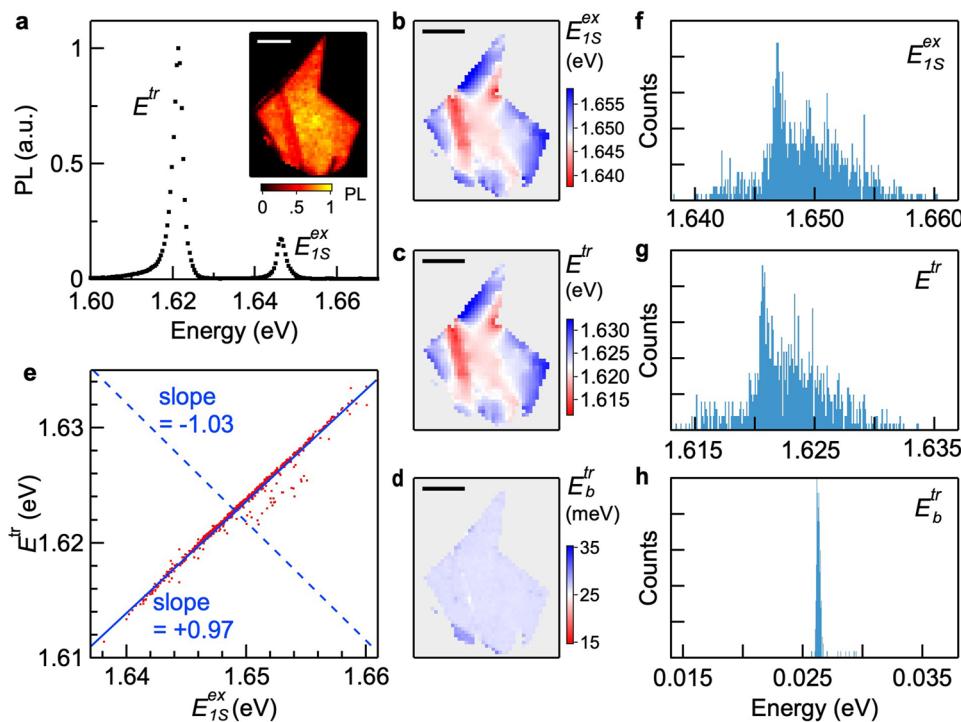
The optical spectra of transition metal dichalcogenide monolayers are dominated by excitons and trions. Here, we establish the dependence of these optical transitions on the disorder from hyperspectral imaging of h-BN encapsulated monolayer MoSe<sub>2</sub>. While both exciton and trion energies vary spatially, these two quantities are almost perfectly correlated, with spatial variation in the trion binding energy of only  $\sim 0.18$  meV. In contrast, variation in the energy splitting between the two lowest energy exciton states is one order of magnitude larger at  $\sim 1.7$  meV. Statistical analysis and theoretical modeling reveal that disorder results from dielectric and bandgap fluctuations, not electrostatic fluctuations. Our results shed light on disorder in high quality TMDC monolayers, its impact on optical transitions, and the many-body nature of excitons and trions.

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Transition metal dichalcogenide (TMDC) monolayers have emerged as the most versatile models for the exploration of many-body semiconductor physics in two-dimensions (2D). The interplay of 2D character and poorly screened Coulomb potential leads to strong many-body effects that dominate the optical properties of TMDCs. Strongly bound excitons, with binding energies in the hundreds of meV, and strongly bound trions, with binding energies in the tens of meV, have been observed in TMDCs.<sup>1–4</sup> These tightly bound excitonic complexes are attractive models for the understanding of many-body interactions in 2D and for optoelectronic applications. However, most 2D materials are strongly affected by disorder<sup>5,6</sup> whose sources include material defects,<sup>7</sup> electrostatic potential fluctuations from variations in local charge distributions,<sup>8,9</sup> dielectric constant variations,<sup>10</sup> and strain-induced bandgap changes.<sup>11,12</sup> Interestingly, as we discuss in this Communication, even state-of-the-art TMDC monolayers with hexagonal boron nitride (h-BN) encapsulation are not immune to disorder. The response of many-body exciton and trion states to disorder can provide valuable insights into both the nature of the disorder and the nature of the excitonic complexes. Here, we carry out hyperspectral imaging of excitons and trions in h-BN encapsulated

monolayer MoSe<sub>2</sub>. We find that both exciton and trion energies are sensitive to variations in the local environment, but these two energies are almost perfectly correlated, in contrast to the behavior of the energy gap between the two lowest exciton states. Statistical analysis of the spatial energy variations, combined with theoretical modeling of exciton and trion states in the presence of disorder, reveals that the sources of the disorder are dielectric constant and electronic bandgap variations of  $\Delta\epsilon \sim 0.08$  and  $\Delta E_g \sim 2\text{--}3$  meV, respectively.

In experiments, we use the highest quality monolayers exfoliated from flux grown MoSe<sub>2</sub> single crystals with low defect density ( $\sim 10^{11}$  cm<sup>-2</sup>), as quantified by scanning tunneling microscope (STM) imaging detailed recently,<sup>13</sup> and large areas ( $> 160$   $\mu\text{m}^2$ ). Each MoSe<sub>2</sub> monolayer is encapsulated in h-BN. The steady-state photoluminescence (PL) spectra [Fig. 1(a)] show two narrow peaks assigned to the lowest energy 1s exciton and the lowest energy trion,<sup>3,4</sup> with mean energies  $E_{1s}^{ex} = 1.6465 \pm 0.0001$  eV and  $E^{tr} = 1.6214 \pm 0.0001$  eV, respectively. The difference  $E_{1s}^{ex} - E^{tr}$  is often referred to as the trion binding energy  $E_b^{tr}$ . We use MoSe<sub>2</sub> monolayers exfoliated from the highest quality single crystal, with quantified defect density of  $8 \pm 5 \times 10^{10}$  cm<sup>-2</sup> from scanning



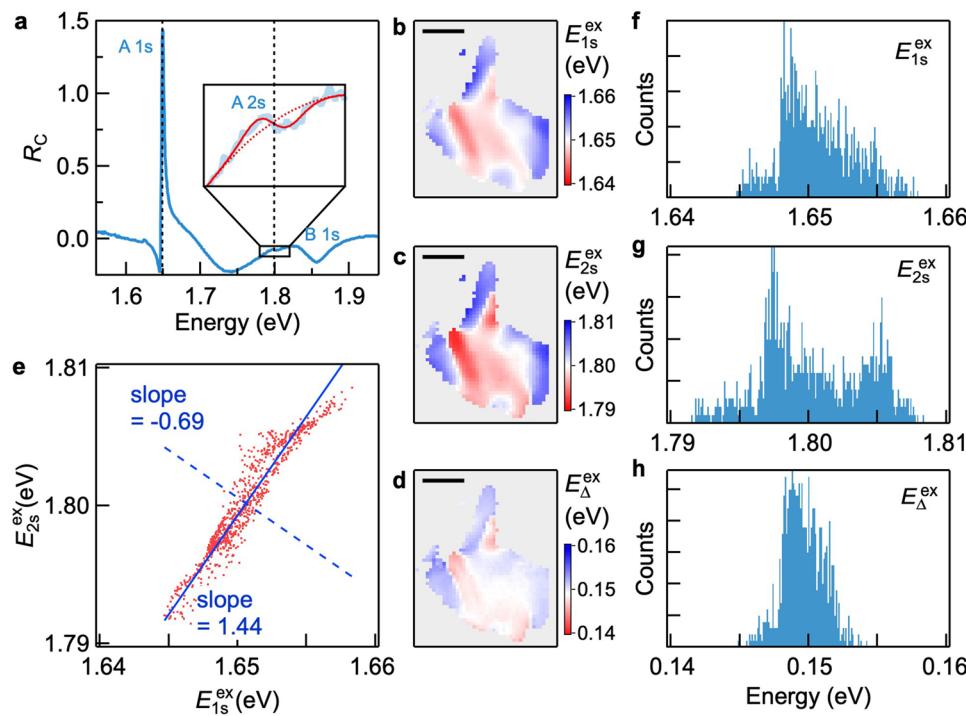
**FIG. 1.** Insensitivity of the trion binding energy to disorder in monolayer MoSe<sub>2</sub>. (a) Representative PL spectrum of monolayer MoSe<sub>2</sub> encapsulated in h-BN. Inset: total PL intensity image. Scale bar: 5  $\mu\text{m}$  (b)–(d), Spatially resolved exciton peak energy  $E_{1s}^{\text{ex}}$  (b), trion peak energy  $E^{\text{tr}}$  (c), and trion binding energy  $E_b^{\text{tr}} = E_{1s}^{\text{ex}} - E^{\text{tr}}$  (d) extracted from the PL map. The ranges of color scales are 20 meV. Scale bar: 5  $\mu\text{m}$ . (e) Correlation between trion and exciton peak energies with data points (red dots) extracted from PL mapping. The solid and dashed blue lines indicate the directions of the eigenvectors of the covariance matrix and have slopes of +0.97 and -1.03, respectively. (f)–(h) Histograms of  $E_{1s}^{\text{ex}}$  (f),  $E^{\text{tr}}$  (g) and  $E_b^{\text{tr}}$  (h). The standard deviations in the data are  $\sigma_{1s}^{\text{ex}} = 3.6 \pm 0.2 \text{ meV}$  (f),  $\sigma^{\text{tr}} = 3.5 \pm 0.2 \text{ meV}$  (g) and  $\sigma_b^{\text{tr}} = 0.186 \pm 0.001 \text{ meV}$  (h), respectively. All data shown are taken at a temperature of 4 K.

tunneling microscopy (STM), with calibrated PL quantum yield of 70%, and with full-width-at-half-maximum (FWHM) of both exciton and trion PL peaks approaching  $\sim 1$  meV, as detailed recently,<sup>13</sup> in agreement with previous reports.<sup>7,14</sup> We determine the effects of disorder<sup>7–12,15–18</sup> by hyperspectral PL imaging with a spatial resolution of  $\sim 1 \mu\text{m}$ . A continuous wave laser at  $h\nu = 2.33 \text{ eV}$  excites the sample in a diffraction-limited spot of FWHM  $\sim 0.43 \mu\text{m}$ , at  $4.66 \mu\text{W}/\mu\text{m}^2$ , corresponding to a calibrated total exciton and trion density of  $\sim 1 \times 10^{10}/\text{cm}^2$ .<sup>13</sup> The high sample quality gives rise to relatively homogeneous spatial distributions in total PL intensity [Fig. 1(a), inset] and the trion-to-exciton intensity ratio  $I_{\text{tr}}/I_{\text{ex}}$  [Fig. S1(a)]. Note that we find no correlation between  $I_{\text{tr}}$  and  $I_{\text{ex}}$  [Fig. S1(b)], suggesting the absence of measurable electron density fluctuation,<sup>8</sup> which would give rise to anti-correlation in  $I_{\text{tr}}$  and  $I_{\text{ex}}$ .

We now focus on  $E_{1s}^{\text{ex}}$  and  $E^{\text{tr}}$ , extracted for each spot from intensity-weighted averaging of the PL spectra [Fig. 1(a)]. While  $E_{1s}^{\text{ex}}$  and  $E^{\text{tr}}$  fluctuate over the whole sample area [Figs. 1(b) and 1(c)]. The difference between the two shows a surprisingly uniform spatial distribution with a mean value of  $E_b^{\text{tr}} = 26.220(1) \pm 0.0005 \text{ meV}$  [Fig. 1(d)]. This suggests that spatial fluctuations in  $E_{1s}^{\text{ex}}$  and  $E^{\text{tr}}$  are highly correlated. Figure 1(e) shows a scatter plot of  $E^{\text{tr}}$  vs  $E_{1s}^{\text{ex}}$ . The solid and dashed lines indicate the directions of the eigenvectors of the covariance matrix of  $E_{1s}^{\text{ex}}$  and  $E^{\text{tr}}$  with slopes of +0.97 and -1.03, respectively. Note that slopes of  $\pm 1$  would indicate perfect correlation and slopes of 0 and  $\infty$  would indicate no correlation. We plot histograms of  $E_{1s}^{\text{ex}}$ ,  $E^{\text{tr}}$ , and  $E_b^{\text{tr}}$  in Figs. 1(f)–1(h), corresponding to standard deviations of  $\sigma_{1s}^{\text{ex}} = 3.6 \pm 0.2 \text{ meV}$ ,  $\sigma^{\text{tr}} = 3.5 \pm 0.2 \text{ meV}$ , and  $\sigma_b^{\text{tr}} = 0.186 \pm 0.001 \text{ meV}$ , respectively. Because of the nearly

perfect correlation between  $E_{1s}^{\text{ex}}$  and  $E^{\text{tr}}$ ,  $\sigma_b^{\text{tr}}$  is only  $\sim 5\%$  of  $\sigma_{1s}^{\text{ex}}$  and  $\sigma^{\text{tr}}$ . The insensitivity of  $E_b^{\text{tr}}$  to disorder is seen in a broad temperature range until  $T \sim 60 \text{ K}$ , above which the trion PL peak disappears, likely attributed to dissociation of the many-body trion complex by phonon scattering (Figs. S2 and S3).

In stark contrast to the nearly constant  $E_b^{\text{tr}}$ , the energy splitting between the exciton levels is more broadly distributed. We quantify the spatial distributions in 1s and 2s exciton energies from reflectance contrast ( $R_c$ ) spectra on the same sample as in Fig. 1. Figure 2(a) is a representative  $R_c$  spectrum showing the A-exciton 1s (1.649 eV) and 2s (1.799 eV, inset) transitions, and the B-exciton 1s transition (1.847 eV), with energies in agreement with previous reports.<sup>10,19</sup> The  $E_{1s}^{\text{ex}}$  and  $E_{2s}^{\text{ex}}$  energy maps for the A-1s exciton in Figs. 2(b) and 2(c) show characteristic spatial variations attributed to the disorder. The energy gap,  $E_{\Delta}^{\text{ex}} = E_{2s}^{\text{ex}} - E_{1s}^{\text{ex}}$ , also shows spatial variation of the same order [Fig. 2(d)]. A scatter plot of  $E_{2s}^{\text{ex}}$  vs  $E_{1s}^{\text{ex}}$  is shown in Fig. 2(e), along with solid and dashed blue lines showing the directions of the eigenvectors of their covariance matrix. The slopes, +1.44 and -0.69, indicate a much weaker correlation than that between  $E_{1s}^{\text{ex}}$  and  $E^{\text{tr}}$ . Figures 2(f)–2(h) show histograms of  $E_{1s}^{\text{ex}}$  and  $E_{2s}^{\text{ex}}$ , and  $E_{\Delta}^{\text{ex}}$  with standard deviations  $\sigma_{1s}^{\text{ex}} = 3.1 \pm 0.2 \text{ meV}$ ,  $\sigma_{2s}^{\text{ex}} = 4.4 \pm 0.4 \text{ meV}$ , and  $\sigma_{\Delta}^{\text{ex}} = 1.7 \pm 0.1 \text{ meV}$ , respectively. The weak correlation between  $E_{1s}^{\text{ex}}$  and  $E_{2s}^{\text{ex}}$  results in  $\sigma_{1s}^{\text{ex}}$  being 40%–60% of  $\sigma_{2s}^{\text{ex}}$  and  $\sigma_{1s}^{\text{ex}}$ . Note that a comparison of Fig. 2(f) from reflectance and Fig. 1(f) from PL gives a small Stokes shift of  $-1.5 \pm 0.1 \text{ meV}$ , consistent with the low defect density of our sample. Note also that the spin-orbit splitting in the valence band, as reflected in the difference between A and B exciton energies, is an intrinsic property of the monolayer and is robust against spatial variations, Fig. S4.



**FIG. 2.** Spatial fluctuation of the exciton energy level splitting in monolayer MoSe<sub>2</sub>. (a) A 1s (1.649 eV), A 2s (1.799 eV) and B 1s resonances. Inset: Fit (red line) to  $R_c$  around the A 2s resonance (light blue line). (b)–(d) Spatially resolved exciton peak energies  $E_{1s}^{\text{ex}}$  (b),  $E_{2s}^{\text{ex}}$  (c) and  $E_{\Delta}^{\text{ex}} = E_{2s}^{\text{ex}} - E_{1s}^{\text{ex}}$ , (d) extracted from  $R_c$  spectral image. All three color scales span 20 meV. Scale bar: 5  $\mu\text{m}$ . (e) Correlation between  $E_{2s}^{\text{ex}}$  and  $E_{1s}^{\text{ex}}$  exciton energies (red dots). The solid and dashed blue lines indicate the directions of the eigenvectors of the covariance matrix with slopes of +1.44 and -0.69, respectively. (f)–(h) Histograms of the exciton energies  $E_{1s}^{\text{ex}}$  (f),  $E_{2s}^{\text{ex}}$  (g) and the energy difference  $E_{\Delta}^{\text{ex}}$  (h). The respective standard deviations are  $3.08 \pm 0.05$ ,  $4.37 \pm 0.05$  and  $1.73 \pm 0.05$  meV. The mean value of 2s-1s energy difference  $E_{\Delta}^{\text{ex}}$  is  $149.46 \pm 0.05$  meV. All data shown are taken at a temperature of 4 K.

The covariance matrices  $K^a(E_{1s}^{\text{ex}}, E_{2s}^{\text{ex}})$  and  $K^b(E_{1s}^{\text{ex}}, E^{\text{tr}})$  can be used to understand the nature of the disorder. These matrices are obtained from the data (in units of meV<sup>2</sup>),

$$K^a(E_{1s}^{\text{ex}}, E_{2s}^{\text{ex}}) = \begin{bmatrix} 9.4763 & 12.7781 \\ 12.7781 & 19.0697 \end{bmatrix}, \quad (1)$$

$$K^b(E_{1s}^{\text{ex}}, E^{\text{tr}}) = \begin{bmatrix} 12.8235 & 12.4329 \\ 12.4329 & 12.0843 \end{bmatrix}.$$

The determinants of both covariance matrices are non-zero, *implying that more than one disorder mechanism is responsible for the observed spatial variations in the exciton and trion energies*. We consider the effects of two different types of spatial disorder on  $E_{\Delta}^{\text{ex}}$  and  $E_b^{\text{tr}}$ : (i) electronic bandgap variations due to strain<sup>11,12</sup> and (ii) disorder in the dielectric constant of the media surrounding the 2D monolayer.<sup>10</sup> In the [supplementary material](#), we discuss potential disorder and explain why it is inconsistent with our experimental observations.

Recent many body models have shown that the PL peaks observed in the measured optical spectra correspond to a superposition of exciton and trion states,<sup>20</sup> (also called exciton-polaron states<sup>21–23</sup>), rather than to pure exciton or pure trion states. Furthermore, the trions states involved in this superposition are four-body neutral states<sup>20</sup> and not three-body charged states, as is commonly assumed. However, given the small electron density in our samples ( $\leq 10^{11} \text{ cm}^{-2}$ ) as quantitatively determined by exciton/trion intensities and STM imaging,<sup>13</sup> one can safely assume, in light of the model

of Rana *et al.*,<sup>20</sup> that the observed lowest energy exciton-trion superposition state in our PL spectrum is essentially a four-body bound trion state ( $E_{1s1s}^{\text{tr}}$ ) and the higher energy superposition states in PL and  $R_c$  spectra are essentially two-body bound exciton states ( $E_{1s}^{\text{ex}}$  and  $E_{2s}^{\text{ex}}$ ). If  $\vec{R}$  is the center of mass coordinate of the exciton (or trion), the local shifts in the exciton and trion energies can be written as

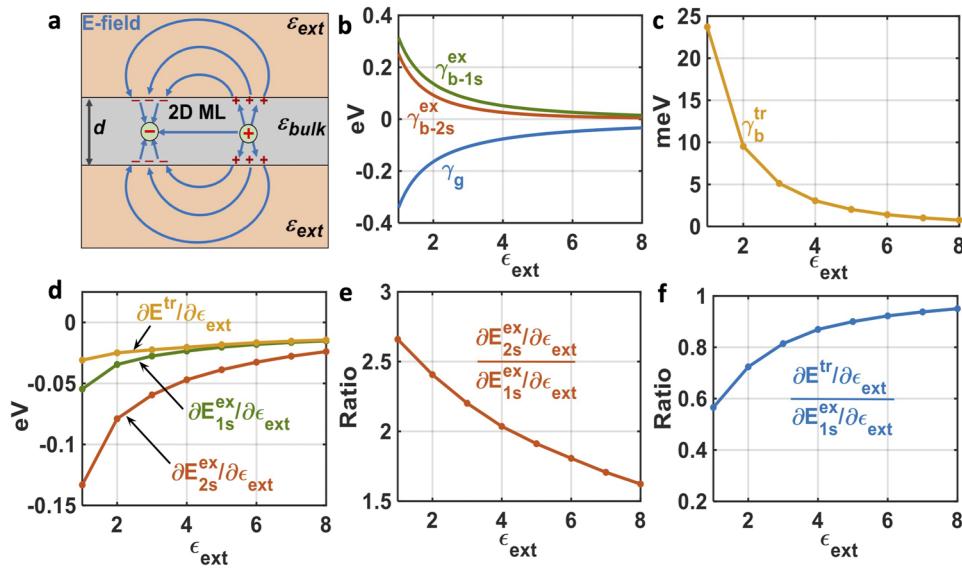
$$\Delta E_{ns}^{\text{ex}}(\vec{R}) = \Delta E_g^{\text{S,T}}(\vec{R}) + (\gamma_g + \gamma_{b-ns}^{\text{ex}}) \Delta \epsilon_{\text{ext}}(\vec{R}), \quad (2)$$

$$\Delta E^{\text{tr}}(\vec{R}) = \Delta E_g^{\text{S,T}}(\vec{R}) + (\gamma_g + \gamma_{b-1s}^{\text{ex}} + \gamma_b^{\text{tr}}) \Delta \epsilon_{\text{ext}}(\vec{R}).$$

Here,  $\Delta E_g^{\text{S,T}}$  is the variation in the bandgap attributed to strain, the coefficient  $\gamma_g = \partial E_g / \partial \epsilon_{\text{ext}}$  describes the change in the bandgap due to dielectric disorder, the coefficients  $\gamma_{b-ns}^{\text{ex}} = -\partial E_{b-ns}^{\text{ex}} / \partial \epsilon_{\text{ext}}$  and  $\gamma_b^{\text{tr}} = -\partial E_b^{\text{tr}} / \partial \epsilon_{\text{ext}}$  describe the changes in the exciton and trion *binding* energies, respectively, due to dielectric disorder, and  $\Delta \epsilon_{\text{ext}}(\vec{R})$  represents the variation in the (relative) dielectric constant of the media surrounding the monolayer.<sup>10</sup> Note that  $\epsilon_{\text{ext}}$  is the average of the dielectric constants of the media on the top and bottom sides of the monolayer. The value of  $\gamma_g$  can be obtained as the change in the energy of a hole due to dielectric polarization charges [Fig. 3(a)] in a thin film of thickness  $d$ , of bulk dielectric constant  $\epsilon_{\text{bulk}}$ , and surrounded by a medium of dielectric constant  $\epsilon_{\text{ext}}$ , when  $\epsilon_{\text{ext}}$  changes by a small amount,<sup>20</sup>

$$\gamma_g = \frac{\partial}{\partial \epsilon_{\text{ext}}} \int \frac{d^2 \vec{q}}{(2\pi)^2} \frac{e}{2\epsilon_0 q} \left[ \frac{1}{\epsilon_{2D}(q)} - \frac{1}{\epsilon_{\text{bulk}}} \right], \quad (3)$$

where the dielectric constant  $\epsilon_{2D}(q)$  is given by<sup>20</sup>



$$\varepsilon(q) = \varepsilon_{bulk} \frac{(1 + \varepsilon_{bulk}/\varepsilon_{ext}) + (1 - \varepsilon_{bulk}/\varepsilon_{ext})e^{-qd}}{(1 + \varepsilon_{bulk}/\varepsilon_{ext}) - (1 - \varepsilon_{bulk}/\varepsilon_{ext})e^{-qd}}. \quad (4)$$

The values of  $\gamma_{b-ns}^{ex}$  and  $\gamma_b^{tr}$  can be computed using methods discussed previously.<sup>20</sup> The results are shown in Figs. 3(b) and 3(c). Consistent with a previous report,<sup>10</sup> our calculations show that effects due to bandgap renormalization and exciton binding energy shift almost cancel each other for the 1s exciton state such that  $|\partial E_{2s}^{ex}/\partial \varepsilon_{ext}|$  for the 2s exciton state is almost exactly a factor of two larger than  $|\partial E_{1s}^{ex}/\partial \varepsilon_{ext}|$  when  $\varepsilon_{ext} \sim 4$  (the dielectric constant of h-BN) [Figs. 3(d) and 3(e)]. We also find that the trion energy closely tracks the 1s exciton energy such that  $|\partial E^{tr}/\partial \varepsilon_{ext}|$  is  $\sim 0.87|\partial E_{1s}^{ex}/\partial \varepsilon_{ext}|$  when  $\varepsilon_{ext} \sim 4$  [Figs. 3(d) and 3(f)]. Assuming that  $\Delta E_g^{S,T}(\vec{R})$  and  $\Delta \varepsilon_{ext}(\vec{R})$  are statistically independent, the following quantities can be obtained directly from the covariance matrices of our data given in Eq. (1),

$$\frac{\partial E_{2s}^{ex}/\partial \varepsilon_{ext}}{\partial E_{1s}^{ex}/\partial \varepsilon_{ext}} = \frac{K_{12}^a(E_{1s}^{ex}, E_{2s}^{ex}) - K_{22}^a(E_{1s}^{ex}, E_{2s}^{ex})}{K_{11}^a(E_{1s}^{ex}, E_{2s}^{ex}) - K_{12}^a(E_{1s}^{ex}, E_{2s}^{ex})} = 1.91, \quad (5)$$

$$\frac{\partial E^{tr}/\partial \varepsilon_{ext}}{\partial E_{1s}^{ex}/\partial \varepsilon_{ext}} = \frac{K_{12}^b(E_{1s}^{ex}, E^{tr}) - K_{22}^b(E_{1s}^{ex}, E^{tr})}{K_{11}^b(E_{1s}^{ex}, E^{tr}) - K_{12}^b(E_{1s}^{ex}, E^{tr})} = 0.89. \quad (6)$$

The experimentally determined values of 1.91 and 0.89 for the ratios above are in remarkably agreement with the respective theoretical values of 2.03 and 0.87 (for  $\varepsilon_{ext} \sim 4$ ). This agreement shows that the model given in Eq. (2) captures the essential physics. In the [supplementary material](#), we show that  $\partial E_{2s}^{ex}/\partial E_{1s}^{ex}$  calculated in the case of potential disorder is given by the ratio of the polarizabilities of the 2s and 1s exciton states and equals  $\sim 102$ , which is  $\sim 53$  times larger than the measured value of 1.91. We, therefore, conclude that potential disorder is not the main contributor to the variations in exciton and trion energies in our samples.

**FIG. 3.** Theoretical model. (a) Dielectric polarization charge, which renormalizes the bandgap of a TMD monolayer, is depicted for the case  $\varepsilon_{bulk} > \varepsilon_{ext}$ . (b) and (c) The coefficients  $\gamma_g = \partial E_g/\partial \varepsilon_{ext}$ ,  $\gamma_{b-1s}^{ex} = -\partial E_{b-1s}^{ex}/\partial \varepsilon_{ext}$ , and  $\gamma_{b-2s}^{ex} = -\partial E_{b-2s}^{ex}/\partial \varepsilon_{ext}$  (b) and  $\gamma_b^{tr} = -\partial E_b^{tr}/\partial \varepsilon_{ext}$  (c) that describe bandgap renormalization, and the sensitivities of the binding energies of the 2s and the 1s exciton levels and the trion level, respectively, are plotted as functions of  $\varepsilon_{ext}$ . (d) The sensitivities of the energies of the 2s and the 1s exciton levels and the trion level, including bandgap renormalization, are plotted as a function of  $\varepsilon_{ext}$ . (e) and (f), The relative sensitivities of the energies of the 2s and 1s exciton levels (e), and of the trion and 1s exciton levels (f), with respect to changes in  $\varepsilon_{ext}$ .

Based on Eq. (2), one can also use the covariance matrices to obtain root mean square values  $\sqrt{\langle (\Delta E_g^{S,T})^2 \rangle}$  and  $\sqrt{\langle (\Delta \varepsilon_{ext})^2 \rangle}$  from the following relations:

$$\sqrt{\langle (\Delta \varepsilon_{ext})^2 \rangle} = \frac{1}{|\partial E_{1s}^{ex}/\partial \varepsilon_{ext}|} \sqrt{\frac{(K_{11}^{a/b} - K_{12}^{a/b})^2}{K_{11}^{a/b} + K_{22}^{a/b} - 2K_{12}^{a/b}}}, \quad (7)$$

$$\sqrt{\langle (\Delta E_g^{S,T})^2 \rangle} = \sqrt{\frac{K_{11}^{a/b} K_{22}^{a/b} - (K_{12}^{a/b})^2}{K_{11}^{a/b} + K_{22}^{a/b} - 2K_{12}^{a/b}}}.$$

Using the theoretical value  $\sim 23.5$  meV of  $|\partial E_{1s}^{ex}/\partial \varepsilon_{ext}|$  [Fig. 3(d)], we find that  $\sqrt{\langle (\Delta \varepsilon_{ext})^2 \rangle}$  equals 0.0813 if we use the covariance matrix  $K^a(E_{1s}^{ex}, E_{2s}^{ex})$  and 0.0810 if we use the covariance matrix  $K^b(E_{1s}^{ex}, E_{2s}^{ex})$ . This remarkable agreement between the values of  $\sqrt{\langle (\Delta \varepsilon_{ext})^2 \rangle}$  obtained using two different experimental techniques (PL and reflection spectroscopies) that looked at two different energy level differences (between 2s and 1s exciton levels in the case of reflection spectroscopy and between 1s exciton and trion levels in the case of PL) further supports the validity of our theoretical model. The values of  $\sqrt{\langle (\Delta E_g^{S,T})^2 \rangle}$  come out to be 2.4 and 2.9 meV if we use the covariance matrices  $K^a(E_{1s}^{ex}, E_{2s}^{ex})$  and  $K^b(E_{1s}^{ex}, E^{tr})$ , respectively. These  $\sqrt{\langle (\Delta \varepsilon_{ext})^2 \rangle}$  values are in satisfactory agreement given the very different experimental measurements.

We point out that the use of the state-of-the-art sample of the lowest defect density to date<sup>13</sup> is key to the first quantitative comparison between experiment and theory on exciton and trion disorder in a TMDC monolayer. This comparison identifies

excitonic disorder as resulting from dielectric fluctuation and strain-related bandgap changes, not electrostatic variation. While dielectric fluctuation may come from impurity charges and adsorbates,<sup>10</sup> strain may have intrinsic origin due to atomic scale relaxation at interface,<sup>24</sup> and extrinsic sources from the transfer stacking process<sup>25</sup> or roughness of the substrate.<sup>5</sup> Further minimizing disorder may necessitate the development of automated transfer stacking processes in ultra-clean environments. We note that previous spectroscopic efforts in exploring the disorder problem have focused on distinguishing homogeneous from heterogeneous linewidth of exciton transitions from coherent spectroscopies.<sup>26–28</sup> In a four-wave mixing experiment on exciton-trion coherence, Jakubczyk *et al.* also reported a nearly constant trion binding energy despite the presence of more extensive spatial disorder from the use of more defective samples without encapsulation; these authors noted the interesting observation without providing an interpretation.<sup>28</sup>

In conclusion, we have compared the behaviors of excitons and trions in the presence of disorder in monolayer MoSe<sub>2</sub> encapsulated in h-BN. Hyperspectral imaging revealed that the 2s-1s exciton energy splitting varies by  $\sigma_b^{ex} = 1.7 \pm 0.1$  meV due to disorder. In contrast, the trion binding energy is robust with spatial variation of only  $\sigma_b^{tr} = 0.186 \pm 0.001$  meV, which is one order of magnitude lower than  $\sigma_b^{ex}$ . Theoretical analysis based on the many-body exciton-trion quantum superposition model<sup>20</sup> provides a quantitative explanation of the experimental results and suggests dielectric and strain origins, not an electrostatic one, for exciton and trion disorder.

See the [supplementary material](#) for methods, additional data, and analysis (Figures S1–S5).

## ACKNOWLEDGMENTS

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## AUTHOR DECLARATIONS

### Conflict of Interest

The authors have no conflicts to disclose.

### Author Contributions

**Jue Wang:** Conceptualization (equal); Data curation (equal); Formal analysis (equal); Investigation (equal); Methodology (equal); Validation (equal); Visualization (equal); Writing – original draft (equal). **Christina Manolatou:** Data curation (equal); Formal analysis (equal); Investigation (equal); Methodology (equal); Software (equal). **Yusong Bai:** Data curation (equal); Methodology (equal). **James Hone:** Methodology (equal). **Farhan Rana:** Conceptualization (equal); Formal analysis (equal); Investigation (equal);

Resources (equal); Software (equal); Writing – review & editing (equal). **X.-Y. Zhu:** Conceptualization (equal); Formal analysis (equal); Funding acquisition (lead); Project administration (lead); Supervision (lead); Writing – original draft (lead).

## DATA AVAILABILITY

The data that support the findings of this study are available within the article and its [supplementary material](#).

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