

1 **Reactive-transport modeling of neodymium and its radiogenic isotope in deep-sea sediments:**  
2 **the roles of authigenesis, marine silicate weathering and reverse weathering**

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## 12 Abstract

13 Dissolved Rare Earth Elements (REE) and radiogenic neodymium (Nd) isotope composition ( $\epsilon_{\text{Nd}}$ ) of  
14 seawater are widely used geochemical tools in studying marine processes, but their modern ocean budgets  
15 are poorly understood. Recent discoveries of large benthic fluxes of REE with unique  $\epsilon_{\text{Nd}}$  signatures from  
16 marine sediments, particularly in the deep-sea, have led to a “bottom-up” hypothesis, which suggests that  
17 early diagenesis below the sediment-water interface (SWI) controls the ocean's REE and  $\epsilon_{\text{Nd}}$  budgets. To  
18 investigate such sedimentary processes, we created a reactive-transport model for the biogeochemical  
19 cycling of Nd and  $\epsilon_{\text{Nd}}$  in marine sediments. Here, we attempt to quantify the roles of authigenesis, marine  
20 silicate weathering and reverse weathering in the diagenetic cycling of Nd and  $\epsilon_{\text{Nd}}$  at a deep-sea (3000 m)  
21 site on the Oregon margin.

22 Our model predicts that, at this site, Nd carried by Fe/Mn oxides into sediments eventually  
23 transforms to authigenic Nd-phosphate, during which ~9% of the incoming solid Nd flux is released as a  
24 dissolved benthic flux back to the overlying bottom water. We also find that the classic reversible  
25 scavenging formulation applied to Nd co-cycling with Fe/Mn oxides is inconsistent with the data. Rather, a  
26 co-precipitation formulation, assuming Nd is structurally incorporated into Fe/Mn oxides, successfully  
27 simulates the data. The model also shows that authigenesis alone cannot explain the pore water and  
28 authigenic  $\epsilon_{\text{Nd}}$ , which are both more radiogenic than bottom water at this site. However, the weathering of  
29 volcanic silicates sourced from the local subduction zone can successfully explain  $\epsilon_{\text{Nd}}$ . We suggest that,  
30 because reverse weathering by authigenic clay formation maintains the under-saturation of primary silicates  
31 in pore water, marine silicate weathering can proceed. The processes we model likely affect the sedimentary  
32 cycling of many other trace elements and isotopes, with much broader implications for the understanding of  
33 ocean biogeochemistry.

## 34 Keywords:

35 Reactive-transport model, Rare Earth Elements, Radiogenic neodymium isotope, Authigenesis, Marine  
36 silicate weathering, Reverse weathering

## 37 1. Introduction

38 The seawater Rare Earth Elements (REE) are widely used geochemical tools for tracing ocean  
39 processes, such as circulation and the particulate-dissolved interaction known as Boundary Exchange  
40 (Elderfield and Greaves, 1982; Lacan and Jeandel, 2005; Piepraga et al., 1979). Among the 14 REE,  
41 neodymium (Nd) has received the most attention because its radiogenic isotope composition, expressed as  
42  $\varepsilon_{\text{Nd}} = [({}^{143}\text{Nd}/{}^{144}\text{Nd})_{\text{sample}}/({}^{143}\text{Nd}/{}^{144}\text{Nd})_{\text{CHUR}} - 1] \times 10^4$  where CHUR is the Chondritic Uniform Reservoir, gives  
43 additional constraints on the oceanic cycles of the REE (Goldstein and Hemming, 2003).

44 The applications of marine REE proxies have been hampered by our limited understanding of their  
45 modern oceanic budgets. Studies of marine Nd cycle have long identified a “missing source” problem: the  
46 known riverine and atmospheric inputs are too small to balance the global budgets, and some ~90% of the  
47 required sources needed to maintain the ocean inventory appears to be “missing” (Arsouze et al., 2009;  
48 Bertram and Elderfield, 1993; Tachikawa et al., 2003; Goldstein and Jacobsen, 1988).

49 Recently, the discovery of large benthic fluxes from marine sediment, with  $\varepsilon_{\text{Nd}}$  values that also  
50 satisfy the isotope budget, provides a promising candidate for this “missing source”, leading to the “bottom-  
51 up” hypothesis of the marine REE cycles (Abbott et al., 2015a; Du et al., 2020; Haley et al., 2017). In this  
52 hypothesis, the sedimentary flux is the dominant source of ocean REE, and seawater  $\varepsilon_{\text{Nd}}$  signatures are  
53 acquired at the sediment-water interface (SWI) rather than at the river/atmosphere-ocean interface.  
54 Anomalous behavior of  $\varepsilon_{\text{Nd}}$  at the SWI has been documented (Grenier et al., 2013; Lacan and Jeandel, 2005;  
55 Lambelet et al., 2018), suggesting that processes involved in Boundary Exchange are indeed critical to trace  
56 element and isotopic budgets. It is thus important to understand the mechanisms of early diagenesis within  
57 sediments that derive these benthic fluxes, and how these processes contribute to the broader concepts of  
58 Boundary Exchange (Jeandel, 2016).

59 If correct, the “bottom-up” hypothesis would significantly change our interpretations of marine REE  
60 proxies; for example, the use of  $\varepsilon_{\text{Nd}}$  to trace paleo-circulation (Abbott et al., 2022; Du et al., 2020, 2018).  
61 However, studies of pore water REE concentrations and  $\varepsilon_{\text{Nd}}$  are scarce and mostly observational, with the  
62 mechanisms regulating the flux obscured by the complexity of sedimentary processes.

63 Here we report a reactive-transport model of the early diagenesis of Nd and  $\varepsilon_{\text{Nd}}$  in marine sediments  
64 with the intent of establishing the “bottom-up” hypothesis in mechanistic and quantitative terms. We focus

65 on deep-sea sediments where the benthic flux is the largest yet measured, potentially dominating the global  
66 budget (Abbott et al., 2015b; Du et al., 2020). We also present a test application of the model to a deep-sea  
67 site on the Oregon Margin, to date the only region for which a comprehensive pore water dataset exists  
68 (Abbott et al., 2019, 2016, 2015b, 2015a). We test three processes hypothesized to be critical in the  
69 diagenetic Nd cycle: (1) authigenesis of Fe-Mn oxides and phosphates (Schijf and Byrne, 2021; Takahashi et  
70 al., 2015; Bi et al., 2021; Abbott et al., 2016); (2) weathering of lithogenic sediments, for example silicate  
71 minerals (Abbott et al., 2022; Blaser et al., 2019; Du et al., 2020; Jeandel and Oelkers, 2015; Lacan and  
72 Jeandel, 2005), and (3) reverse weathering through conversion of biogenic silica to authigenic clay (Aller,  
73 2014; Mackin and Aller, 1984). These processes are likely important for the sedimentary cycle of many  
74 trace elements and isotopes (TEIs), and our general modelling approach as well as the specific results for  
75 this site thus have implications for the global budgets of these TEIs. Our model also helps illuminate how  
76 authigenic phases acquire  $\varepsilon_{\text{Nd}}$  diagenetically, thus providing key insights for the use of authigenic  $\varepsilon_{\text{Nd}}$  in  
77 paleoceanography.

## 78 2. Study region

79 Paired REE and  $\varepsilon_{\text{Nd}}$  measurements in pore water and sediment, as well as ancillary data needed by the  
80 model, have only been made by Abbott et al., (2019, 2016, 2015b, 2015a) at three sites on the Oregon  
81 margin, Northeast Pacific (Fig. 1). We choose to model site HH3000 at 3000 m water depth, because it has  
82 one of the highest benthic Nd fluxes yet measured ( $\sim 30 \text{ pmol/cm}^2/\text{yr}$ ). The water column here has a uniform  
83  $\varepsilon_{\text{Nd}}$  of  $-2.4 \varepsilon$ , but pore water  $\varepsilon_{\text{Nd}}$  ( $-1.8 \varepsilon$ ) is more radiogenic, the first evidence that diagenetic processes can  
84 decouple bottom and pore water  $\varepsilon_{\text{Nd}}$ .

85 The site underlies oxic bottom water ( $\sim 100 \mu\text{M}$ ) and has a low organic carbon rain rate ( $200 \mu\text{g/cm}^2/\text{yr}$ )  
86 (Lyle et al., 1992). These conditions lead to a weakly reducing shallow sediment package, with dissolved  
87 Mn ( $\sim 50 \mu\text{M}$ ) higher than Fe ( $< 10 \mu\text{M}$ ) in pore water (Abbott et al., 2016). Sediments are composed mainly  
88 of terrigenous materials ( $\sim 90 \text{ wt\%}$ ) with moderate organic carbon (OC) ( $\sim 1.8 \text{ wt\%}$ ), significant biogenic  
89 opal ( $\sim 6 \text{ wt\%}$ ), but negligible carbonate ( $\sim 0.05 \text{ wt\%}$ ). The accumulation rate is  $\sim 13 \text{ cm/kyr}$  (Abbott et al.,  
90 2016; Lyle et al., 1992). Terrigenous sediments are delivered by small coastal rivers that drain across the  
91 Oregon Coastal Range and Cascade Arc. The mineral assemblage consists of quartz, plagioclase, chlorite

92 and muscovite/illite, with minor clinopyroxene, amphibole and volcanic glass (Abbott et al., 2019),  
93 reflecting their sources in the igneous and low-grade metamorphic rocks of the continental arc  
94 (VanLaningham et al., 2008).

### 95 3. Diagenetic modelling

96 Ours is a classic 1D reactive-transport model describing the distributions of dissolved species in pore  
97 water and solid species in sediments (Boudreau, 1997). Physical transport includes molecular diffusion,  
98 burial and bio-irrigation for dissolved species, and bioturbation and burial for solid species. The model  
99 includes the classic sequence of organic matter decomposition, and uses the continuum formulation of the  
100 reactivity of organic matter. The model also includes secondary redox reactions, dissolution of biogenic  
101 opal,  $\text{CaCO}_3$  and precipitation of  $\text{FeS}/\text{FeS}_2$ . We also model pH for speciation calculations. Complete model  
102 details are given in the Supplementary Methods; here we only present those that relate to Nd and  $\varepsilon_{\text{Nd}}$ .

103 We model  $^{144}\text{Nd}$  and radiogenic  $^{143}\text{Nd}$  as two separate tracers. The convention for reporting radiogenic  
104  $\varepsilon_{\text{Nd}}$  is to remove the natural and instrumental stable isotope fractionation by normalizing the  $^{143}\text{Nd}/^{144}\text{Nd}$   
105 ratio to a fixed  $^{146}\text{Nd}/^{144}\text{Nd}$  ratio of 0.7219. A model of  $\varepsilon_{\text{Nd}}$  thus has no need to consider stable isotope  
106 fractionation. Modeled Nd concentration is the sum of these two isotopes divided by the summed natural  
107 abundance (0.35971). Nd speciation for both isotopes is computed following Schijf and Byrne (2021),  
108 considering complexation with dissolved ligands  $\text{CO}_3^{2-}$ ,  $\text{HCO}_3^-$ ,  $\text{Cl}^-$ ,  $\text{SO}_4^{2-}$  and  $\text{H}_3\text{SiO}_4^-$ . We do not consider  
109 organic ligands since they have not been characterized in sediment pore water.

#### 110 3.1. Authigenic Fe/Mn oxides

111 To date, interaction of Nd with solid phases in ocean models has been formulated as *equilibrium*  
112 reversible scavenging (Siddall et al., 2008). Using  $\text{MnO}_2$  as an example (same for  $\text{FeOOH}$ ):

$$113 \quad {}^i\text{Nd}_{\text{MnO}_2} = {}^i\text{Nd}_d \times K_{\text{ads-MnO}_2} \times \text{MnO}_2, \quad (1)$$

114 where

115  ${}^i\text{Nd}_d$  is the *total* dissolved Nd concentration ( $i=143$  or  $144$ );

116  ${}^i\text{Nd}_{\text{MnO}_2}$  is the adsorbed Nd concentrations;

117  $K_{ads-\text{MnO}_2}$  is the adsorption constant specific to  $\text{MnO}_2$ .

118 We also consider an alternative *kinetic* co-precipitation formulation:

$$119 \quad R^i \text{Nd}_{\text{Mn-pre}} = R \text{Mn}_{\text{oxi}} \times D_{\text{Nd/Mn}} \times {}^i \text{Nd}_{\text{d/Mn}}, \quad (2)$$

$$120 \quad R^i \text{Nd}_{\text{Mn-dis}} = R \text{MnO}_{2\text{red}} \times {}^i \text{Nd}_{\text{MnO}_2}/\text{MnO}_2, \quad (3)$$

121 where

122  $R^i \text{Nd}_{\text{Mn-pre}}$  is the co-precipitation rate of Nd when dissolved Mn ( $\text{Mn}_d$ ) is oxidized at a rate of  $R \text{Mn}_{\text{oxi}}$ ;

123  $D_{\text{Nd/Mn}}$  is the partition coefficient controlling the enrichment of Nd relative to Mn in  $\text{MnO}_2$ ;

124  $R^i \text{Nd}_{\text{Mn-dis}}$  is the release rate of solid Nd ( ${}^i \text{Nd}_{\text{MnO}_2}$ ) in  $\text{MnO}_2$  during reduction ( $R \text{MnO}_{2\text{red}}$ ).

125 In this formulation, newly formed oxides have the same  $\varepsilon_{\text{Nd}}$  as the pore water precipitating them, and  
126 during dissolution the release of dissolved Nd isotopes are proportional to the release of dissolved Mn  
127 according to the solid concentration ratio of Nd isotopes to Mn in  $\text{MnO}_2$  (*i.e.*, dissolution is congruent).

### 128 3.2. Authigenic phosphate

129 We consider the precipitation-dissolution of rhabdophane ( $\text{NdPO}_4$ ) using the classic linear Transient  
130 State Theory (TST) (Steefel et al., 2014):

$$131 \quad R^i \text{Nd}_{\text{PO}_4} = k_{\text{NdPO}_4} \times a^i_{\text{NdPO}_4} \times ({}^i \text{Nd}^{3+} \times [\text{PO}_4^{3-}] / K_{sp\text{NdPO}_4} / a^i_{\text{NdPO}_4} - 1), \quad (4)$$

132 where

133  $k_{\text{NdPO}_4}$  is the precipitation rate constant;

134  $a^i_{\text{NdPO}_4}$  is the activity of the isotopic  $\text{NdPO}_4$  species ( $i=143,144$ ), which we assume to form an ideal solid-  
135 solution so that the activity is equal to the mole fraction;

136  $[{}^i \text{Nd}^{3+}]$  is the *free* Nd concentration of an isotope;

137  $[\text{PO}_4^{3-}]$  is the concentration of  $\text{PO}_4^{3-}$  ion;

138  $K_{sp\text{NdPO}_4}$  is the *apparent* solubility.

139 Positive  $R^iNd_{PO_4}$  favors precipitation while negative values imply dissolution. This formulation

140 ensures that newly formed NdPO<sub>4</sub> has the same  $\epsilon_{Nd}$  as the pore water.

141 **3.3. Marine silicate weathering**

142 We model the dissolution of four silicate phases: basalt glass, clinopyroxene, plagioclase and chlorite.

143 The general TST law of silicate dissolution is (Heřmanská et al., 2022):

144  $R_{silicate} = k_{silicate} \times S_{silicate} \times M_{silicate} \times \text{silicate} \times (1 - \Omega_{silicate}),$  (5)

145 Which is used for clinopyroxene and chlorite, but modified for basalt and plagioclase to include the Al-

146 inhibition term (Heřmanská et al., 2022):

147  $R_{basalt} = k_{basalt} \times S_{basalt} \times M_{basalt} \times \text{basalt} \times (a^3 H^+ / a_{Al^3+})^{1/3} \times (1 - \Omega_{basalt}),$  (6)

148  $R_{plag} = k_{plag} \times S_{plag} \times M_{plag} \times \text{plag} \times (a^3 H^+ / a_{Al^3+})^{0.35} \times (1 - \Omega_{plag}),$  (7)

149 where

150  $k$  is the surface area normalized Si release rate;

151  $S$  is the specific surface area;

152  $M$  is the mineral molecular weight;

153 *Silicate/Basalt/Plag* is the mineral concentration in solid sediment;

154  $\Omega$  is the saturation state in pore water, and dissolution is allowed only when  $\Omega < 1$ ;

155  $a$  refers to aqueous activity.

156 The release of Nd isotopes are assumed congruent to Si:

157  $R^{143}Nd_{silicate} = R_{silicate} \times r_{Nd/Si} \times 0.35971 \times {}^{143}Nd / {}^{144}Nd_{silicate} / ({}^{143}Nd / {}^{144}Nd_{silicate} + 1),$  (8)

158  $R^{144}Nd_{silicate} = R_{silicate} \times r_{Nd/Si} \times 0.35971 / ({}^{143}Nd / {}^{144}Nd_{silicate} + 1),$  (9)

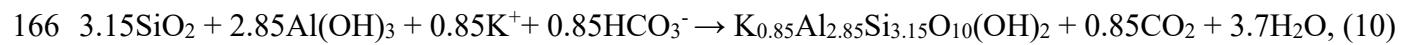
159 where

160  $r_{Nd/Si}$  is the molar Nd/Si ratio in silicates;

161  $^{143}\text{Nd}/^{144}\text{Nd}_{\text{silicate}}$  is the Nd isotopic ratio of silicates.

162 **3.4. Reverse weathering**

163 In the model, reverse weathering includes two reactions: (1) opal dissolution, releasing dissolved Si  
164 to pore water, and; (2) authigenic illite formation, previously identified in marine sediments (Mackin and  
165 Aller, 1986), that consumes cations and alkalinity from pore water while releasing CO<sub>2</sub>. The net reaction is:



167 Opal dissolution also releases Al according to a molar Al/Si ratio of 0.0025 in diatom frustules (Van  
168 Cappellen et al., 2002), and marine silicate weathering provides additional Al sources.

169 The dissolution rate of opal is (Van Cappellen et al., 2002):

170  $R_{\text{opal}} = k_{\text{opal}} \times \text{opal} \times (1 - \Omega_{\text{opal}})$ , (11)

171 where

172  $k_{\text{opal}}$  is the opal dissolution rate constant and,

173  $\Omega_{\text{opal}}$  is the opal saturation state.

174 The rate of authigenic illite precipitation is computed using the TST rate law Eq. (5) when  $\Omega_{\text{illite}} > 1$ .

175 **3.5. Model simulations**

176 We perform two types of simulations: baseline simulations and simulations that further add silicate  
177 weathering and reverse weathering. The baseline simulations include the sediment biogeochemical reactions  
178 and the authigenic Fe/Mn oxides and phosphate phases, and we test both the reversible scavenging and co-  
179 precipitation formulations. In the silicate weathering and reverse weathering simulations, silicate phases are  
180 added to the sediments to study their behavior. We test the model sensitivity to the dissolution rates of  
181 silicates, and the precipitation rates of authigenic clay during reverse weathering.

182 The model domain is the top 50 cm of the sediment, representing ~3500 years of sedimentation. This  
183 depth domain is discretized into 200 intervals, with finer grid spacing close to SWI to capture the large  
184 biogeochemical gradients there, resulting in 6600 coupled and stiff differential equations in the baseline  
185 simulations. Boundary conditions and the model solution are described in the Supplementary Methods.

186 4. Results

187 4.1. Sediment biogeochemistry

188 The model reproduces the classic redox sequence at site HH3000 (Fig. 2). The depth-integrated OC  
189 remineralization rate is 0.5 mmol/m<sup>2</sup>/d, typical of this margin at similar water depth (McManus et al., 2012).  
190 The remineralization pathway is dominated by aerobic respiration (37.6%) and sulfate reduction (52.6%)  
191 (Fig. 2a). Despite its importance, sulfate reduction is still far from complete, with only ~0.5 mM of SO<sub>4</sub>  
192 consumed in the top 50 cm (Fig. 2f) and little formation of Fe sulfides (~0.12 wt%, Fig. 2e). Denitrification  
193 (8.0%) and MnO<sub>2</sub> reduction (1.6%) also contribute to carbon remineralization, but there is little FeOOH  
194 reduction (0.25%) and methanogenesis is negligible (Fig. 2a). Organic carbon respiration slightly decreases  
195 pH from ~7.7 in the bottom water to ~7.3 in the deep pore water (Fig. 2i). Pore water total silica  
196 concentration is relatively high (~620 μM, Fig. 2g) because of high opal content.

197 In the model, the surface bioturbated layer is ~ 6 cm thick. To fit the OC profile (Fig. 2d), the initial age  
198 of OC in the continuum reactivity model is 60 yr, higher than that of fresh phytoplankton but within the  
199 range observed in deep-sea studies (Arndt et al., 2013). To fit the dissolved phosphate profile (Fig. 2h), the  
200 required P/C ratio is 1/170, lower than the classic Redfield ratio (1/106). Together, the lower reactivity and  
201 P/C imply the presence of refractory terrestrial OC at this site (Hastings et al., 2012).

202 Assuming sediments below 6 cm represent the lithogenic background, the excesses of MnO<sub>2</sub>,  
203 presumably authigenic, are ~0.45 wt% near the surface (Fig. 2d) (Abbott et al., 2016). Modeled surface  
204 sediment MnO<sub>2</sub> (~0.05 wt%) has to be lower than this value to fit the pore water Mn profile (Fig. 2c),  
205 suggesting that the surface enrichment might be a transient feature, or that other interfaces or microbial  
206 processes are involved but not modeled. Estimated authigenic (0.5 wt%) and modeled (0.2 wt%) FeOOH are  
207 similar (Fig. 2d). The authigenic enrichment of Fe is thus much lower than Mn, given the higher lithogenic  
208 background for Fe (~5 wt%) versus Mn (~0.07 wt%). Model results are consistent with elemental mapping  
209 using energy dispersive X-ray spectroscopy (EDS), which shows that Fe is located mainly in silicates, while  
210 Mn is enriched in amorphous nanoparticles that are likely authigenic (Abbott et al., 2019). Modeled Mn  
211 cycling is more intense than Fe cycling, at rates one order of magnitude higher for Mn than Fe (Fig. 2d). The  
212 modeled benthic Mn flux is 0.14 μmol/m<sup>2</sup>/d, in the range of measurements at similar depths at this margin

213 (McManus et al., 2012). The modeled benthic Fe flux is  $-0.005 \mu\text{mol/m}^2/\text{d}$ , also consistent with  
214 measurements (McManus et al., 1997).

## 215 5. Discussion

### 216 5.1. Authigenesis

217 Authigenesis has typically been considered the main process affecting the early diagenesis of REE  
218 (Haley et al., 2004; German and Elderfield, 1989), which in turn has justified the assumption that pore water  
219 and authigenic Nd are simply derived from bottom water Nd at the SWI (Goldstein and Hemming, 2003).  
220 Here we investigate to what degree authigenesis alone can explain the observations of the diagenetic Nd  
221 cycle.

#### 222 5.1.1. Authigenic Fe/Mn oxides and co-precipitation

223 Our co-precipitation formulation is controlled by the partition coefficients ( $D$ ). We use the results of  
224 the GEOTRACES Pacific GP16 cruise (Haley et al., 2021; Lam et al., 2018) to derive these parameter  
225 values.  $D_{Nd/Mn}$  is calculated as  $(Nd_{auth}/MnO_2)/(Nd_d/Mn_d)$ .  $Nd_{auth}$  is the measured particulate Nd corrected for  
226 lithogenic background, using a lithogenic Nd/Al mass ratio of  $3.375 \times 10^{-4}$  and measured particulate Al. Data  
227 for authigenic  $MnO_2$ ,  $FeOOH$ , dissolved Nd and Mn are from the cited studies (Haley et al., 2021; Lam et  
228 al., 2018). We find  $D_{Nd/Mn}=0.025$  and  $D_{Nd/Fe}=0.005$  in the deep-sea ( $>2500$  m). Using these values, the fluxes  
229 of Nd carried by  $MnO_2$  and  $FeOOH$  into sediments at the study site are  $612$  and  $40 \text{ pmol/cm}^2/\text{yr}$ ,  
230 respectively, based on the  $MnO_2$  and  $FeOOH$  fluxes in the model (Supplementary Information).

231 For co-precipitation, the modeled pore water and authigenic Nd agree well with measurements (Fig.  
232 3).  $MnO_2$  reduction (by POC,  $Fe^{2+}$  and  $H_2S$ ) is predicted to be the major source of pore water Nd (Fig. 3d),  
233 while Mn oxidation (by  $O_2$ ) is a small sink. The depth-integrated  $MnO_2$  reduction source ( $647 \text{ pmol}$   
234  $Nd/\text{cm}^2/\text{yr}$ ) far outweighs the Mn oxidation sink ( $35 \text{ pmol Nd/cm}^2/\text{yr}$ ). In comparison,  $FeOOH$  reduction (by  
235 POC and  $H_2S$ ) is a much smaller source of pore water Nd (Fig. 3d), while Fe oxidation (by  $O_2$  and  $MnO_2$ ) is  
236 a relatively larger sink. The depth-integrated  $FeOOH$  reduction source ( $120 \text{ pmol Nd/cm}^2/\text{yr}$ ) slightly  
237 exceeds the Fe oxidation sink ( $80 \text{ pmol Nd/cm}^2/\text{yr}$ ).

238 **5.1.2. Authigenic Fe/Mn oxides and reversible scavenging**

239 The reversible scavenging formulation is controlled by the adsorption constants ( $K_{ads}$ ). We use

240 values of  $K_{ads-MnO_2}=5\times 10^7$  (M<sup>-1</sup>) and  $K_{ads-FeOOH}=0.8\times 10^7$  (M<sup>-1</sup>), to deliver the same amount of Nd to the

241 sediment via Fe/Mn oxides as in the co-precipitation simulation (Supplementary Methods).

242 These model results cannot explain the pore water Nd profile (Fig. 4). Modeled peak Nd

243 concentration is far deeper than measured (Fig. 4c). Model sensitivity tests show that by varying  $K_{ads}$  the

244 magnitude of the peak Nd concentration would change, but it would not affect the depth of the peak

245 (Supplementary Fig. 1). This is because, in the presence of MnO<sub>2</sub> and FeOOH, Nd remains in the adsorbed

246 form, and is converted to dissolved Nd only when the concentrations of oxides greatly decrease (Fig. 4b). In

247 contrast, in the co-precipitation formulation Nd is released to pore water as soon as oxide reduction begins

248 (Fig. 3d). The failure of reversible scavenging is perhaps not surprising given that *reversible* adsorption is a

249 first step toward *irreversible* structural incorporation (co-precipitation), and laboratory experiments have

250 identified the gradual structural incorporation of adsorbed trace metals into Mn oxides (Atkins et al., 2016).

251 Most existing ocean models rely on reversible scavenging to explain increasing seawater REE (and

252 other TEIs) concentrations with increasing water depth in the open ocean (Arsouze et al., 2009; Siddall et

253 al., 2008), on the premise that the concentrations of particulate scavengers decrease with depth. However, no

254 ocean REE model has included Fe/Mn oxides, despite the fact that they are amongst the most important

255 scavengers, especially in the deep ocean (Schijf et al., 2015). If Fe/Mn oxide concentrations in seawater

256 increase with depth, as recent GEOTRACES results have shown (Lam et al., 2018), reversible scavenging

257 onto Fe/Mn oxides would predict a decrease, rather than an increase, of seawater REE concentrations with

258 depth. Our results do not necessarily indicate that adsorption is unimportant, but rather that the reversible

259 scavenging formulation in present ocean models may be unsuitable to describe this process, or that kinetic

260 rather than equilibrium process may better describe particulate-dissolved interaction in seawater. We suggest

261 that future studies need to include Fe/Mn oxides to robustly evaluate the appropriateness of reversible

262 scavenging.

263 5.1.3. Authigenic phosphate

264 Solid REE concentrations in Pacific sediments are most strongly correlated to phosphate, more so than  
265 Fe/Mn oxides and other elements (Bi et al., 2021). Also, bio-apatite becomes strongly enriched in REE post-  
266 deposition (Toyoda and Tokonami, 1990). Diagenetic Nd formed on foraminiferal tests is associated with  
267 oxides, *but also phosphorous* (Roberts et al., 2012). Transformation of labile Fe/Mn oxide-associated REE  
268 to stable phosphate phases has been identified in pelagic sediments, suggesting phosphate is likely the  
269 ultimate sink of REE (Takahashi et al., 2015). Whether REE form their own phosphate minerals, are  
270 incorporated into authigenic Ca-phosphates, or are taken up by biogenic phosphate, is unclear. In the model,  
271 we choose rhabdophane, a common REE mineral forming in low-temperature environment (Gausse et al.,  
272 2016; Liu and Byrne, 1997; Pearce et al., 2013), as the authigenic phosphate ( $\text{NdPO}_4$ ), largely because  
273 relevant thermodynamic data exist.

274 Literature values of  $\log(K_{sp}^0_{\text{NdPO}_4})$  at standard state and zero ionic strength are in the range of  $-26 \sim -24$   
275 (Gausse et al., 2016). The corresponding *apparent*  $\log(K_{sp\text{NdPO}_4})$  in seawater medium at *in situ* temperature  
276 ( $2^\circ\text{C}$ ) and atmospheric pressure is estimated to be  $-20 \sim -18$  using the activity coefficients of Pierrot and  
277 Millero (2017), but we lack the thermodynamic data to compute the constant at *in situ* pressure. Model  
278 sensitivity tests show that the higher end of solubility estimates fits the pore water Nd profile better  
279 (Supplementary Fig. 2), which could be because either greater pressure leads to higher solubility than  
280 reported values at the standard state, or because  $\text{NdPO}_4$  formed in sediments is less crystalline than the  
281 versions used in some solubility experiments (Gausse et al., 2016). The saturation concentration of *total* Nd  
282 with respect to  $\text{NdPO}_4$  is

$$283 Nd_{saturation} = K_{sp\text{NdPO}_4} / ([\text{PO}_4^{3-}] \times f_{\text{Nd}^{3+}}), \quad (12)$$

284 where  $f_{\text{Nd}^{3+}}$  is the fraction of the *free*  $\text{Nd}^{3+}$  ion.

285 Given  $k_{\text{NdPO}_4} = 100 \text{ pmol/cm}^3/\text{yr}$ , the modeled pore water Nd fits observations very well (Fig. 3g). Pore  
286 water becomes oversaturated below  $\sim 1 \text{ cm}$ . Close to the SWI, solid  $\text{NdPO}_4$  that is formed in the over-  
287 saturation zone beneath is brought up to the under-saturation zone by bioturbation, and its dissolution is a  
288 greater source of pore water Nd than  $\text{MnO}_2$  reduction (Fig. 3d, e). Overall, phosphate precipitation is the

289 dominant sink of pore water Nd, far surpassing that of Fe/Mn oxidation (Fig. 3d–e). As modeled oxides  
290 disappear below 30 cm, the model predicts pore water Nd concentration that are nearly at *equilibrium* with  
291 NdPO<sub>4</sub> (Fig. 3g). The modeled total (MnO<sub>2</sub>, FeOOH and phosphate related) authigenic Nd concentration (~9  
292 ppm) also matches estimates based on an *operationally* defined acid-reductive leaching (Abbott et al., 2016).  
293 Though leaching studies of authigenic Nd have traditionally focused on the role of Fe/Mn oxides, it is well-  
294 known that the acetic acid used in these studies can also extract authigenic and biogenic phosphates  
295 (Ruttenberg, 1992).

#### 296 5.1.4. Authigenesis and benthic flux

297 The benthic Nd flux in the model is affected by molecular diffusion and bio-irrigation (i.e.,  
298 convective exchange between pore water and bottom water due to the activity of benthic organisms)  
299 (Supplementary Methods). Using the co-precipitation formulation and including authigenic phosphate, the  
300 modeled diffusive flux is 39 pmol/cm<sup>2</sup>/yr, agreeing well with the estimate (24~41 pmol/cm<sup>2</sup>/yr) based on the  
301 measured pore water profile (Abbott et al., 2015b). The model uses the bio-irrigation parameterization of  
302 Meile and Van Cappellen (2003), derived from the globally measured O<sub>2</sub> flux. The resulting bio-irrigation  
303 Nd flux is 20 pmol/cm<sup>2</sup>/yr. This value is an upper limit because the impact of bio-irrigation on other  
304 dissolved species is likely weaker than on O<sub>2</sub> (Meile et al., 2005). Taken together the total benthic flux is 59  
305 pmol/cm<sup>2</sup>/yr.

306 The authigenic minerals influence the benthic Nd flux in different ways. Both MnO<sub>2</sub> and NdPO<sub>4</sub> are  
307 sources of pore water Nd at the SWI, and thus support the benthic flux. However, when integrated over the  
308 sediment column, MnO<sub>2</sub> is a net source of pore water Nd while NdPO<sub>4</sub> is a net sink (Fig. 3d–f). In contrast,  
309 FeOOH is a sink of pore water Nd at the SWI and thus decreases the benthic flux (Fig. 3d–f), despite the  
310 fact that FeOOH is a net source of pore water Nd integrated over the sediment column.

311 In summary, in the baseline simulation including only authigenesis, the early diagenetic Nd cycle at the  
312 study site can be described as near total (~91%) conversion of Nd carried by incoming MnO<sub>2</sub>, and to a lesser  
313 degree FeOOH, to authigenic NdPO<sub>4</sub>, with a small fraction (~9%) returning to bottom water via diffusion  
314 and irrigation. Since, in this model, all Nd sources ultimately come from incoming water column-derived  
315 Fe/Mn oxides, modeled pore water and authigenic  $\epsilon_{Nd}$  are the same as bottom water (Fig. 3i).

### 316 5.2. Silicate weathering

317 The observed relatively small  $\varepsilon_{\text{Nd}}$  difference ( $+0.6 \varepsilon$ ) between pore water and bottom water is an  
318 indication that bottom water  $\varepsilon_{\text{Nd}}$  is strongly influenced by pore water  $\varepsilon_{\text{Nd}}$  because of a large benthic flux  
319 (Abbott et al., 2016). To explain this difference additional processes must be invoked. Much larger  
320 differences between pore water/authigenic and bottom water  $\varepsilon_{\text{Nd}}$  exist elsewhere, linked to smaller benthic  
321 flux or reactive lithogenic sediments (Abbott et al., 2016; Blaser et al., 2019; Du et al., 2016; Wilson et al.,  
322 2013). Moreover, variations in authigenic  $\varepsilon_{\text{Nd}}$  on glacial-interglacial timescales is only on the order of  $1\sim2 \varepsilon$ ,  
323 sometimes correlated to changes of lithogenic sediment  $\varepsilon_{\text{Nd}}$  (Du et al., 2020 and references therein). It is thus  
324 important to understand  $\varepsilon_{\text{Nd}}$  differences on this order of magnitude for robust circulation reconstruction.

#### 325 5.2.1. The reactive spectrum of silicate minerals

326 Our next model iteration investigates the impact of marine silicate weathering on the diagenetic cycle of  
327  $\varepsilon_{\text{Nd}}$ , focusing on mineral reactivity. We model four phases: basaltic glass, clinopyroxene, chlorite and  
328 plagioclase (albite): all present in the study region (Abbott et al., 2019; VanLaningham et al., 2008).  
329 Volcanic glass, often derived from ash deposition that reaches far into the ocean interior, is ubiquitous in  
330 Pacific sediments (Du et al., 2020; Straub and Schmincke, 1998). Clinopyroxene is a mafic mineral that is  
331 commonly found in sediments near volcanic arcs. Chlorite often exists as a clay mineral, as the metamorphic  
332 alteration product of igneous minerals (Griffin et al., 1968). Plagioclase is not necessarily volcanic but it  
333 is the most abundant primary silicate mineral, after quartz, in marine sediments (Li and Schoonmaker,  
334 2014). Collectively they represent a large range of silicate reactivity in terms of abundance, dissolution rate  
335 and solubility.

336 We add these phases separately to the baseline model, with deposition fluxes that are proportional to the  
337 total incoming sediment: 2 wt% of basalt glass and clinopyroxene, 10 wt% of chlorite and 20 wt% of  
338 plagioclase respectively, based on published abundance data in the study region (Abbott et al., 2019;  
339 VanLaningham et al., 2008; Zemmel and Cook, 1973). Interrogation of the GEOROC database  
340 (Supplementary Methods), either using data from the Cascade Arc or other convergent margins, suggests  
341 that the average Nd/Si molar ratios of basalt glass, clinopyroxene and plagioclase are  $1.9 \times 10^{-5}$ ,  $1.8 \times 10^{-5}$  and  
342  $1.9 \times 10^{-6}$  respectively (Supplementary Fig. 3), consistent with the partition coefficients of Nd in silicates

343 (Taylor and McLennan, 1988). For chlorite, we use the average Nd/Si ratio ( $1.6 \times 10^{-5}$ ) of clay minerals from  
344 rivers draining volcanic terrains, as compiled by Bayon et al., (2015). In comparison, the average Nd/Si ratio  
345 of volcanic rocks from the Cascade Arc is  $1.7 \times 10^{-5}$ , similar to that of basalt glass, clinopyroxene and clay,  
346 but 1-order of magnitude higher than plagioclase. The average  $\epsilon_{\text{Nd}}$  of Cascade volcanic rocks is  $+6.2 \epsilon$  which  
347 we use for all four silicates. Dissolution parameters for these phases are reported in Supplementary Table 6.

348 We further assume that during silicate weathering the Nd/Si dissolution rate ratio is the same as the  
349 Nd/Si ratio in silicates (*i.e.*, congruent dissolution). In the laboratory dissolution experiment of Pearce et al.,  
350 (2013), the ratio of *gross* Nd/Si release, estimated using  $\epsilon_{\text{Nd}}$ , from three basalt samples at the end of 121  
351 days is  $\sim 2.5 \times 10^{-5}$ . This value is similar to the Nd/Si ratio in their basalt samples ( $\sim 2.1 \times 10^{-5}$ ), supporting our  
352 assumption. No other experimental studies of Nd and  $\epsilon_{\text{Nd}}$  during silicate dissolution exists to our knowledge,  
353 thus whether this assumption is true for other silicates is presently not tested.

354 Field-derived weathering rates are often lower than laboratory-derived values, a conundrum that has  
355 been attributed to inadequate dissolution rate laws, the loss of reactive surface sites due to occlusion, fluid  
356 transport limitation and the influence of secondary phases on saturation state (e.g., Maher et al., 2006). For  
357 example, Maher et al., (2006) suggested that the plagioclase dissolution rate in deep-sea sediments is  $10^5$   
358 times lower than in the laboratory for the linear TST rate law at their study site. To investigate our model  
359 sensitivity, we vary the silicate dissolution rates by 6 orders of magnitude, from the laboratory-derived rates  
360 to values 1 to 5 orders of magnitude lower.

361 At higher dissolution rates, silicates are quickly consumed, while at lower rates greater amounts of  
362 minerals are preserved (Fig. 5). The modeled pore water Nd concentration, however, do not respond linearly  
363 to changes of dissolution rate (Fig. 5–6). In the upper sediment (<10 cm), dissolved Nd still largely agrees  
364 with the observed concentrations (Fig. 6), as silicate Nd release at even the highest dissolution rates are  
365 slower than Nd release from  $\text{MnO}_2/\text{NdPO}_4$  (Fig. 3). In the deeper sediment, modeled dissolved Nd exceeds  
366 the measured values at intermediate dissolution rates, but neither with the highest nor lowest rates: the  
367 former because the silicates are spent and the latter because dissolution is slow at all depths. Modeled  
368 dissolved Si is subject to a similar influence (Fig. 5).

369 Model sensitivity also depends on mineral abundance, Nd/Si ratio and solubility (Fig. 5–6). Modeled Nd,  
370 Si concentrations and  $\epsilon_{\text{Nd}}$  are not sensitive to dissolution of basaltic glass nor clinopyroxene because their  
371 Nd and Si reservoirs are small due to low abundance at the study site (Fig. 5a–h, 6a–h). In contrast, modeled  
372 Si concentration are very sensitive to plagioclase dissolution (Fig. 5i–l) because it is more abundant and thus  
373 has greater potential to affect pore water chemistry, such as pH. This in turn drives large changes of Nd  
374 speciation and dissolved Nd concentration (Fig. 6i). The influence on  $\epsilon_{\text{Nd}}$  is however limited too because  
375 low Nd/Si in plagioclase leads to a small Nd reservoir. In comparison, despite a relatively high abundance  
376 and large Nd reservoir, modeled  $\epsilon_{\text{Nd}}$  is not much more sensitive to chlorite dissolution rates because of its  
377 relatively low solubility (Fig. 5m–p, 6m–p).

### 378 5.2.2. Best-fit silicate weathering models

379 Considering the fit to observed pore water  $\epsilon_{\text{Nd}}$ , Nd and Si concentrations, the best-fit models include  
380 the weathering of volcanic phases such as basaltic glass and clinopyroxene, at dissolution rates within 2  
381 orders of magnitude of laboratory-derived rates (Fig. 5a–h, 6a–h), and with their presence at <2 wt%. This  
382 relatively high reactivity may be explained by their “freshness,” because of direct volcanic ash deposition, or  
383 fast physical erosion of volcanic rocks in the Costal Range and Cascade Arc, coupled to short transport  
384 times in coastal rivers and efficient dispersal of fluvial sediments on the Oregon margin (Wheatcroft and  
385 Sommerfield, 2005). In contrast, to explain pore water  $\epsilon_{\text{Nd}}$  requires that nearly all plagioclase dissolves,  
386 inconsistent with its observed abundance at ~20 wt%. The model using chlorite cannot fit Nd concentration  
387 and  $\epsilon_{\text{Nd}}$  simultaneously, and its abundance at ~10 wt% also suggest it is likely not reactive. The inferred low  
388 reactivity of plagioclase and chlorite implies that at site HH3000 these minerals are probably not of volcanic  
389 origin (*i.e.*, sedimentary or metamorphic), and have experienced loss of reactivity before reaching the  
390 seafloor.

391 Adding silicate weathering increases *diffusive* benthic Nd fluxes from 39 pmol/cm<sup>2</sup>/yr in the baseline  
392 model to 41~42 pmol/cm<sup>2</sup>/yr in the best-fit models (the range is given for basalt weathering using  
393 dissolution rates that are 10<sup>-1</sup>~10<sup>0</sup> times of laboratory-derived rate). Thus, the impact of silicate weathering  
394 on the elemental Nd benthic flux is likely non-measurable at site HH3000. In contrast, the  $\epsilon_{\text{Nd}}$  of the flux  
395 increases from -2.4  $\epsilon$  to -1.7~ -1.3  $\epsilon$ , a significant difference given the analytical uncertainty (2 $\sigma$ =0.27  $\epsilon$ ).

396 Modeled pore water  $\epsilon_{Nd}$  is more radiogenic than bottom water ( $-2.4 \epsilon$ ), and importantly, the trend of pore  
397 water  $\epsilon_{Nd}$  deviating toward bottom water  $\epsilon_{Nd}$  at  $\sim 5$  cm is reproduced (Fig. 6c, 6g). This depth is where  $MnO_2$   
398 reduction rate is at a maximum, and thus is the peak release for seawater derived Nd (Fig. 3d).

399 Modeled authigenic  $\epsilon_{Nd}$  is similar to pore water, but has a smoother profile (Fig. 6d, 6h), as  
400 authigenic phases integrate over longer timescales and are subject to bioturbation. However, modeled  
401 authigenic  $\epsilon_{Nd}$  is still not as radiogenic as the *operationally* defined leachate  $\epsilon_{Nd}$  (Abbott et al., 2016),  
402 suggesting that the leach likely extracts some non-authigenic components that are refractory under *in situ*  
403 sediment conditions but reactive in laboratory leaching (Abbott et al., 2022, 2016; Du et al., 2016). If the  
404 lower pH and wash off of major cations during leaching increases the dissolution rates and under-saturation  
405 of silicate minerals like plagioclase and chlorite, enough silicate Nd could be released, just as our model  
406 demonstrates (Fig. 6p). At site HH3000, a combination of  $\sim 8.5$  ppm *truly* authigenic Nd ( $-1.8 \epsilon$ ) with  $\sim 0.5$   
407 ppm Nd extracted from silicates ( $+6.2 \epsilon$ ), can explain the leachate Nd ( $\sim 9$  ppm and  $\sim -1.2 \epsilon$ ).

#### 408 5.3. Reverse weathering

409 Authigenic clay formation during reverse weathering can affect the saturation state of primary  
410 silicates by influencing pore water Al concentration (Maher et al., 2006), thus *indirectly* controlling the  
411 diagenetic Nd cycle. In the “best-fit” silicate weathering models discussed above, we included reverse  
412 weathering using an authigenic illite precipitation rate of  $10^{-19}$  mol/m<sup>2</sup>/s, as suggested by a previous study  
413 (Maher et al., 2006), but  $\sim 6$  orders of magnitude lower than laboratory-derived rates (Marty et al., 2015).

414 We ran further sensitivity tests of the influence of reverse weathering by varying the authigenic illite  
415 precipitation rate (Fig. 7):  $10^{-19}$  mol/m<sup>2</sup>/s in the “normal clay” model;  $10^{-16}$  in the “fast clay”;  $10^{-22}$  in the  
416 “slow clay”, and 0 in the “no clay” (no reverse weathering) models. At the study site illite is also a *detrital*  
417 mineral through riverine input (VanLaningham et al., 2008). Therefore, in the model, we add a *detrital* illite  
418 flux that represents 2 wt% of the total sediment. We model the *total* illite concentration, with the *authigenic*  
419 fraction as the excess above the detrital input. In these tests we include basalt weathering as discussed  
420 previously, at a dissolution rate  $10^{-1}$  times the laboratory-derived value.

421 Close to the SWI ( $<0.2$  cm), modeled Al and Si concentrations are positively correlated because of  
422 co-release by basalt and opal dissolution, but they become anti-correlated at depth because of authigenic

423 illite formation, except in the “no clay” model wherein the positive correlation persists (Fig. 7e–f, 8). At  
424 depth, the Al concentration converges to equilibrium values with respect to illite solubility in the “fast clay”  
425 model, but reaches an asymptote to values that are congruent to Si with respect to opal in the “no clay”  
426 model. Pore water Al in the upper sediment increases from ~1 nM in the “fast clay” model to ~1000 nM in  
427 the “no clay” model (Fig. 7e), reducing basalt under-saturation, until over-saturation (Fig. 7g). Authigenic  
428 illite concentration is <1 wt% in all models.

429 Pore water Al was not measured at HH3000. We compare the modeled Al-Si relationship with  
430 published seawater and pore water data to evaluate if model results are reasonable (Fig. 8). Al-Si trends in  
431 the “fast clay” and “normal clay” models follow that of deep ocean water (GEOTRACES Intermediate Data  
432 Product Group, 2021) and East China Sea pore water (Mackin and Aller, 1984). Al-Si trends in the “normal  
433 clay” and “slow clay” models bracket pore water data from the North Atlantic, Southern Ocean and Amazon  
434 shelf (Mackin and Aller, 1986, 1986; Stoffyn-Egli, 1982; Van Beueskom et al., 1997). The Al speciation in  
435 the model considers only hydrolysis, but if other ligands are present, which is likely in reality, then the same  
436 *free*  $\text{Al}^{3+}$  concentration in the model would lead to greater *total* Al concentrations. Thus the modeled total Al  
437 concentration is likely a lower limit. Overall, we consider the “normal clay” model the best option given its  
438 consistency with literature data and the uncertainty in Al speciation. As long as the precipitation rate is  
439 higher than in the “slow clay” model, reverse weathering will drive basalt weathering, and modeled pore  
440 water  $\varepsilon_{\text{Nd}}$  will agree with observations (Fig. 7l).

441 Finally, whether Nd is *directly* incorporated into authigenic clay is unknown. If it is, and assuming  
442 the same Nd/Si ratio as primary silicates, the authigenic illite sink for Nd (<3 pmol/cm<sup>3</sup>/yr) (Fig. 7a) would  
443 be much smaller than the phosphate sink (~200 pmol/cm<sup>3</sup>/yr) (Fig. 3d), and thus negligible.

## 444 6. Implications and perspectives

445 The modeled diagenetic Nd cycle at the study site is summarized in Fig. 9. Our aim was to  
446 investigate the roles of commonly suggested sedimentary processes, rather than comprehensively consider  
447 all potential processes. That the model successfully simulated observations indicates co-cycling with Fe/Mn,  
448 authigenic phosphate formation, silicate weathering and reverse weathering are indeed among the most

449 important at the study site. Future studies should aim to examine other potential processes, such as the role  
450 of organic ligands and colloids in pore water.

451 Our study paves the way for modeling diagenetic Nd cycling at other sites and regions where the  
452 relative contributions of the studied processes may differ. For instance, site HH200 on the Oregon shelf (200  
453 m) has a much larger pore water to bottom water  $\varepsilon_{\text{Nd}}$  difference (+1.6  $\varepsilon$ ) than the study site HH3000 (+0.6  $\varepsilon$ ),  
454 corresponding to a greater abundance of volcanic phases like glass and clinopyroxene in sediments (Abbott  
455 et al., 2019). One would thus expect silicate weathering to be more important than at the deep-sea site  
456 HH3000.

457 Our study also has global implications. With authigenesis alone, a benthic flux only produces  
458 regenerated Nd (Fig. 9), with significant impact on the oceanic budget of Nd concentration but not  $\varepsilon_{\text{Nd}}$ . In  
459 contrast, silicate weathering produces a new external source of Nd (Fig. 9), which may have a small impact  
460 on the Nd concentration but a significant one on  $\varepsilon_{\text{Nd}}$ , particularly when the  $\varepsilon_{\text{Nd}}$  difference between seawater  
461 and reactive silicate phases is large. This contrast in element versus isotopic sensitivity mirrors seawater  
462 observations and implies that diagenetic transformation at the SWI is likely a key component of Boundary  
463 Exchange (Jeandel, 2016). The apparent conservative behavior of seawater  $\varepsilon_{\text{Nd}}$ , in the presence of non-  
464 conservative Nd concentration due to benthic flux, can be preserved in the first case but not in the second.  
465 The reality is likely somewhere in-between (Du et al., 2020). We suggest the differing response of Nd  
466 concentration versus  $\varepsilon_{\text{Nd}}$  to the benthic flux is key to resolving the “Nd paradox” (Goldstein and Hemming,  
467 2003).

468 Our results may also explain why, globally, benthic Nd fluxes do not correlate to redox parameters  
469 such as bottom water oxygen and OC rain rate (Du et al., 2018). For example, strong redox cycling on the  
470 continental shelf does not convert to high benthic Nd flux (Abbott et al., 2015b; Deng et al., 2022) as it does  
471 for Fe and Mn (McManus et al., 2012, 1997). We suggest that the non-redox-sensitive Nd sink (phosphate)  
472 may play a more important role than the redox-sensitive source (Fe/Mn oxides). If phosphate  
473 precipitation/dissolution is fast enough, pore water Nd concentrations will be largely controlled by  
474 phosphate solubility, and only weakly dependent on redox cycling.

475 Our model illustrates the *indispensable* role of pore water TEI data in constraining diagenetic  
476 processes and fluxes across the SWI. In our best-fit models, with 2 wt% basalt/clinopyroxene supply to  
477 sediments, only <0.4 wt% remains at the surface, and none below 10 cm. Such small fractions are virtually  
478 undetectable by solid phase analysis methods, let alone when the solid phases have disappeared completely  
479 and leave only an imprint on pore water. Thus, it is likely *not* possible to study such processes using solid  
480 phase analysis alone: pore water TEIs may be our only source of evidence.

481 The processes investigated here also affect the diagenesis of other TEIs (Little et al., 2020; Jeandel,  
482 2016). Presently, the application of diagenetic modeling to TEIs is limited by the scarcity of comprehensive  
483 pore water data and measurements of the fluxes of all solid components into sediments. As fluxes at the SWI  
484 are increasingly seen to be a key part of the global ocean budgets of TEIs (Homoky et al., 2016), it is  
485 important for further pore water and sediment trap TEI studies, as extensions of the GEOTRACES water  
486 column surveys.

## 487 7. Conclusions

488 We created the first reactive-transport model for Nd and  $\epsilon_{\text{Nd}}$  in marine sediments, and quantified the  
489 roles of authigenesis, silicate weathering and reverse weathering in the early diagenetic Nd cycle at the  
490 deep-sea site HH3000 on the Oregon margin.

491 The model correctly captured the biogeochemical processes at the site and successfully simulated the  
492 observed pore water Nd profile using the co-precipitation formulation of Nd co-cycling with Fe/Mn and  
493 authigenic phosphate formation. In the simulation, we found that  $\text{MnO}_2$  reduction is the main source of Nd  
494 in pore water, phosphate formation is the main sink, and Fe cycling plays a minor role. Benthic Nd flux is  
495 mainly driven by  $\text{MnO}_2$  reduction and phosphate dissolution close to the SWI. In contrast, the model cannot  
496 reproduce the pore water Nd profile via the reversible scavenging formulation of Nd co-cycling with Fe/Mn.

497 We further included silicate weathering and reverse weathering to simulate pore water  $\epsilon_{\text{Nd}}$ . We  
498 studied the model's sensitivity to the dissolution of basaltic glass, clinopyroxene, plagioclase and chlorite,  
499 representing a wide range of mineral reactivity, abundance and solubility. The model correctly simulated  
500 pore water  $\epsilon_{\text{Nd}}$  (and other data) if it includes the weathering of basaltic glass or clinopyroxene with relatively

501 high dissolution rates, supporting the hypothesis that weathering of volcanic sediments is responsible for the  
502 relatively more radiogenic  $\epsilon_{\text{Nd}}$  of pore water and authigenic phases in the Pacific. Furthermore, we show that  
503 reverse weathering is necessary to maintain relatively low pore water Al concentrations, thus enabling the  
504 undersaturation of primary silicates and indirectly contributing to the diagenetic Nd cycle.

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## 513 Data availability

514 Model output from this study can be found at: <https://doi.org/10.5281/zenodo.6998239>.

## 515 Figure legends

516  
517 Fig 1. Map of the study region. Site HH3000 is marked by the white dot with black border. The two thin  
518 black lines on the seafloor indicate the 200 m and 3000 m depth contours. The white dashed lines indicate  
519 the plate tectonic boundaries. The red triangles on land indicate volcanoes in the Cascades. The blue lines on  
520 land indicate rivers.

521

522 Fig. 2. Modeled sediment biogeochemistry. (a) POC oxidation rates. (b) Mn and Fe cycling rates. (c–h)  
523 Solid and dissolved species (lines) compared with measured values (colored dots with red borders). (i) Pore  
524 water pH (free proton scale). The prefix “T” in names indicates total concentrations summed over all species  
525 (e.g., TH<sub>3</sub>PO<sub>4</sub> = H<sub>3</sub>PO<sub>4</sub> + H<sub>2</sub>PO<sub>4</sub><sup>–</sup> + HPO<sub>4</sub><sup>2–</sup> + PO<sub>4</sub><sup>3–</sup>).

526

527 Fig. 3. Baseline simulation using the co-precipitation formulation for Fe/Mn oxides and including NdPO<sub>4</sub>.  
528 (a–c) Fe, Mn and phosphate cycling. (d) Nd uptake/release due to individual reactions. Positive means Nd  
529 release to pore water and negative uptake. (e) Net Nd release/uptake driven by Fe, Mn and phosphate  
530 cycling. (f) pore water Nd sources and sinks summed over individual reactions, and the net source. (g)  
531 Concentrations of the *total* dissolved Nd and the *free* Nd<sup>3+</sup> ion, and the *total* Nd concentrations at saturation  
532 with respect to NdPO<sub>4</sub>. (h) Authigenic Nd concentrations. (i) Pore water and authigenic ε<sub>Nd</sub>. In the plots  
533 colored dots with red borders indicate direct measurements, except in (h–i) where authigenic Nd and ε<sub>Nd</sub> are  
534 estimated using an *operationally* defined acid-reductive leach.

535

536 Fig. 4. Model results using the reversible scavenging formulation of Fe/Mn oxides. (a) Fe/Mn oxide  
537 concentrations. (b) Nd adsorbed on to the oxides. (c) Pore water Nd concentrations compared with the  
538 results of the co-precipitation formulation and with measurements (in red dots). Sensitivity tests involving  
539 different adsorption constants are reported in Supplementary Fig. 1.

540

541 Fig. 5. Model sensitivity to silicate dissolution rate. (a) Nd release rate by basalt dissolution. (b) Basalt  
542 concentration. (c) Dissolved silica. Red dots indicate measurements. (d) Basalt saturation index. Red dashed  
543 line indicates saturation. The color legend in (a) indicates the orders of magnitude of dissolution rate  
544 reduction in the sensitivity tests. “1e0” means dissolution rate is the same as the laboratory-derived value.  
545 “1e1” means a dissolution rate that is 1-order of magnitude lower etc. (e–h) are the same as (a–d) but for  
546 clinopyroxene. (i–l) are for plagioclase, and (m–p) are for chlorite.

547

548 Fig. 6. Sensitivity of the Nd cycle to silicate weathering. (a–d) Pore water Nd, authigenic Nd, pore water ε<sub>Nd</sub>,  
549 and authigenic ε<sub>Nd</sub> respectively in the basalt weathering sensitivity tests. The color legend in (a) indicates the  
550 orders of magnitude of dissolution rate reduction in the sensitivity tests as in Fig. 5. Red dots indicate direct  
551 measurements, except that authigenic Nd and ε<sub>Nd</sub> are estimated using an *operationally* defined acid-

552 reductive leach. In (c–d) the  $2\sigma$  analytical errors of  $\varepsilon_{\text{Nd}}$  are shown. (e–h), (i–l) and (m–p) are the results of  
553 model tests with weathering of clinopyroxene, plagioclase and chlorite respectively.

554

555 Fig. 7. The impact of reverse weathering on silicate weathering and the Nd cycle. (a) Illite precipitation rate.  
556 (b) Basalt dissolution rate. (c) Opal dissolution rate. (d) pH. (e) Al concentration. (f) Dissolved Si. (g) Basalt  
557 saturation index. Dash red line indicates saturation. (h) Illite saturation index. (i) Basalt concentration. (j)  
558 Authigenic illite concentration. (k) Pore water Nd. (l) Pore water  $\varepsilon_{\text{Nd}}$ . The color legend in (a) indicates the  
559 sensitivity tests using different authigenic clay precipitation rates. Red dots indicate measured values.

560

561 Fig. 8. Modeled pore water Al-Si relationship at the study site compared with literature results. Seawater  
562 data are from the GEOTRACES IDP2021 (GEOTRACES Intermediate Data Product Group, 2021) and only  
563 the deep ocean data are shown (>1000 m depth). Pore water data are from the North Atlantic, Southern  
564 Ocean, East China Sea and Amazon shelf (Mackin and Aller, 1986, 1986; Stoffyn-Egli, 1982; Van  
565 Beueskom et al., 1997). Al and Si concentrations are in units of mol/kg on the log scale.

566

567 Fig. 9. Summary of the early diagenetic cycle of Nd and  $\varepsilon_{\text{Nd}}$  at HH3000. Black italic numbers are Nd fluxes  
568 and depth-integrated transformation rates in pmol/cm<sup>2</sup>/yr. The benthic fluxes are written in the form of  
569 “diffusive + bio-irrigation” fluxes. Purple numbers are  $\varepsilon_{\text{Nd}}$ . The summary is based on (1) the baseline model  
570 using the co-precipitation formulation of Fe/Mn oxides and including authigenic phosphate, (2) the silicate-  
571 weathering model using the dissolution of basalt glass at a rate 1 order of magnitude lower than laboratory-  
572 derived rate, and (3) the “normal clay” model of reverse weathering. Reverse weathering is shown in dashed  
573 lines as it influences the Nd cycle indirectly by driving the marine silicate weathering. The flux of refractory  
574 silicate Nd is not modeled but calculated using the sedimentation rate and refractory silicate Nd  
575 concentration, which is estimated as the difference between the measured bulk and modeled authigenic Nd  
576 concentration. Similarly, the  $\varepsilon_{\text{Nd}}$  of refractory silicate is computed using the measured bulk  $\varepsilon_{\text{Nd}}$  and modeled  
577 authigenic  $\varepsilon_{\text{Nd}}$  based on isotopic mass balance. The refractory silicates are not reactive on the short timescale

578 of early diagenesis but may become reactive on the longer timescales of later diagenesis. Bulk sediment data  
579 are from Abbott et al., (2016).

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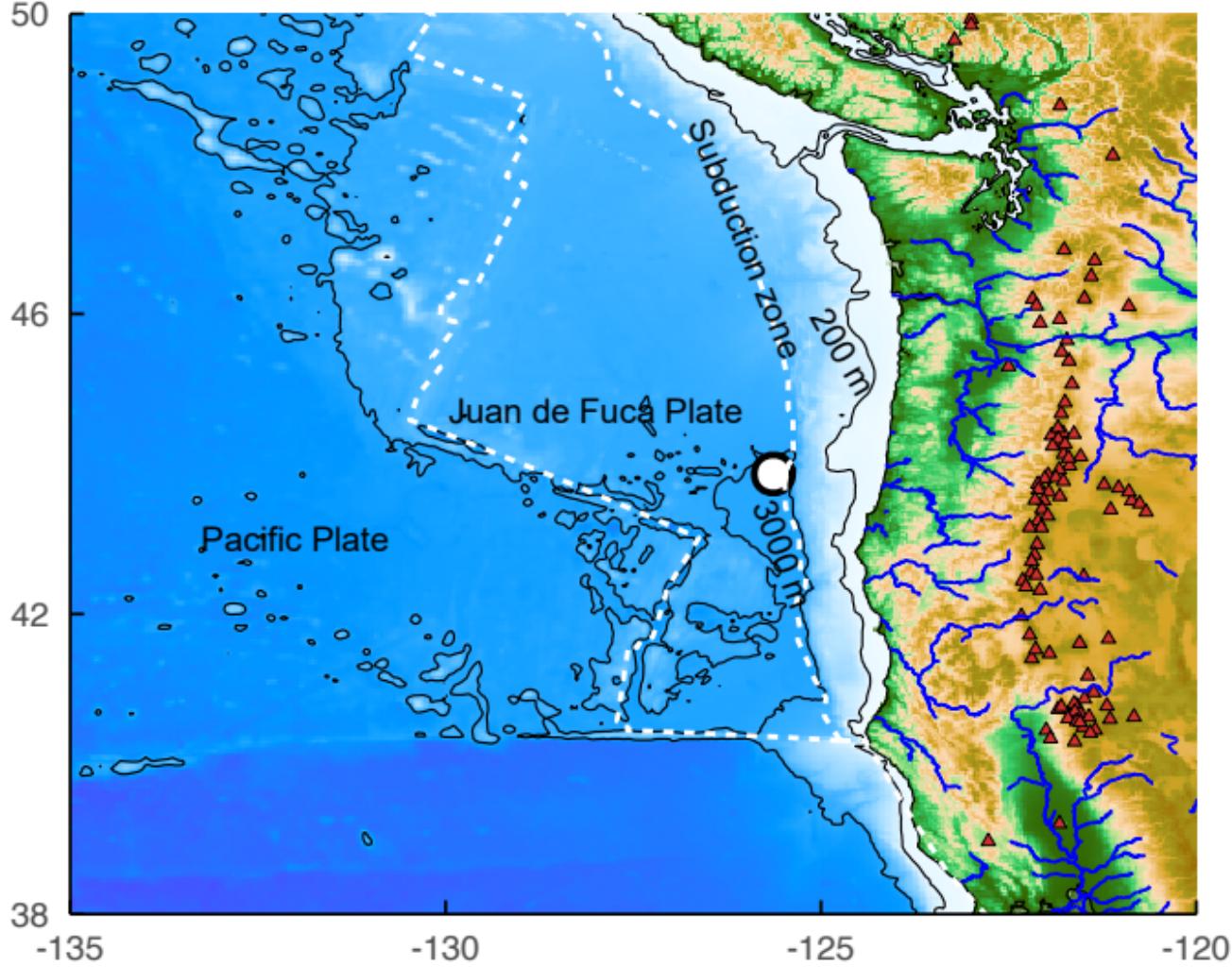
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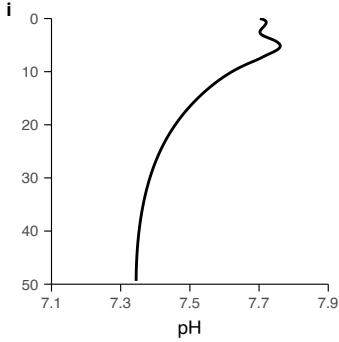
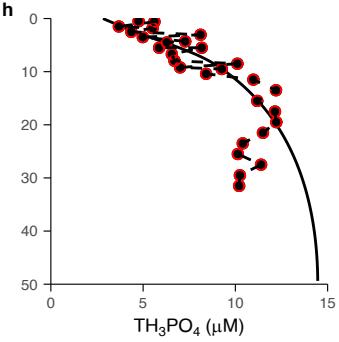
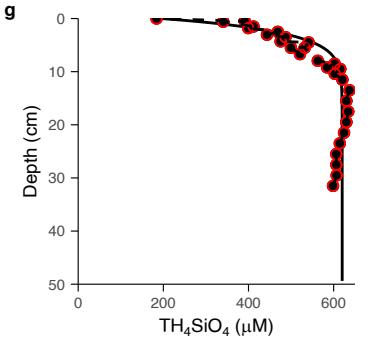
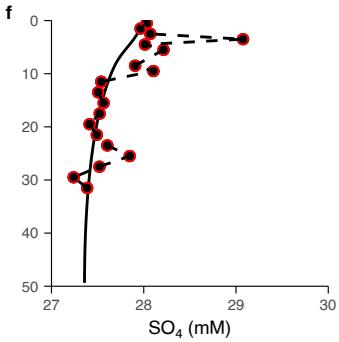
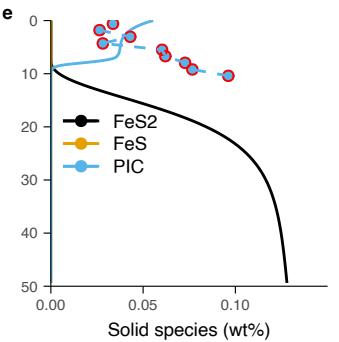
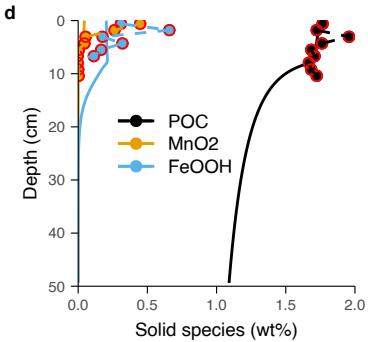
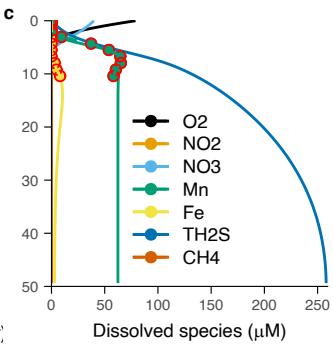
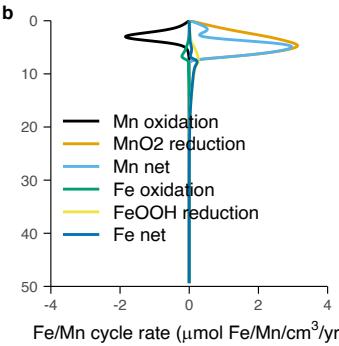
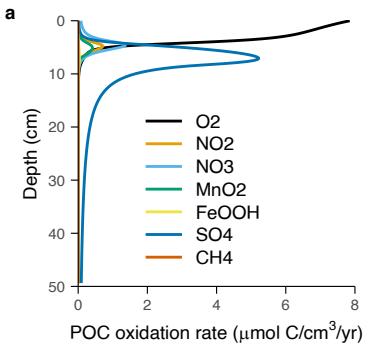
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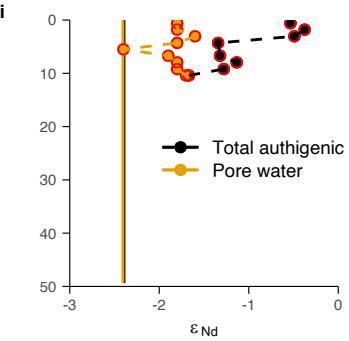
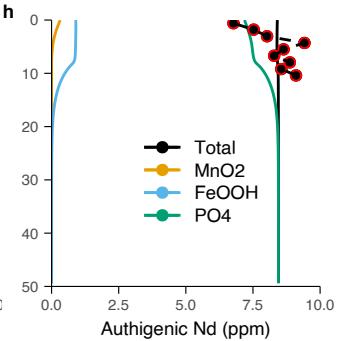
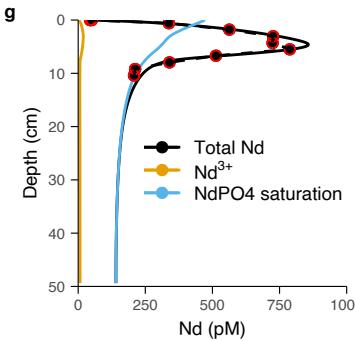
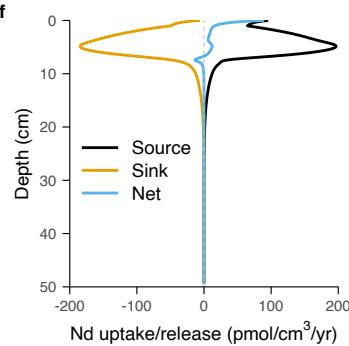
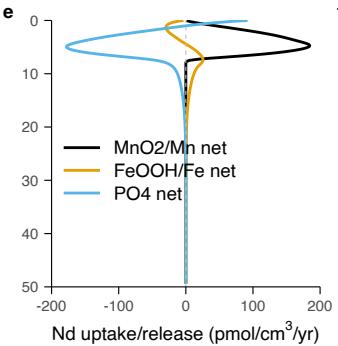
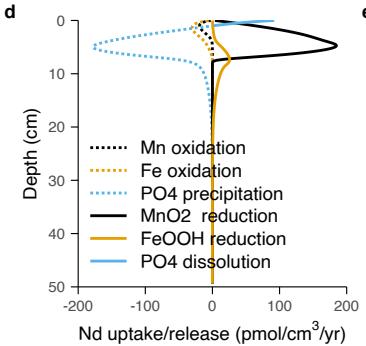
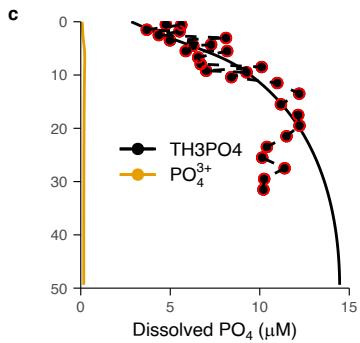
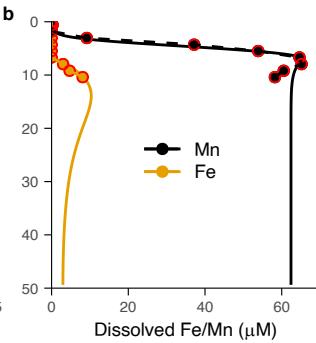
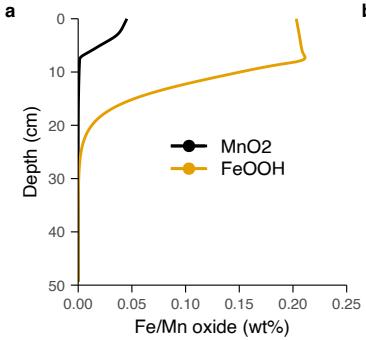
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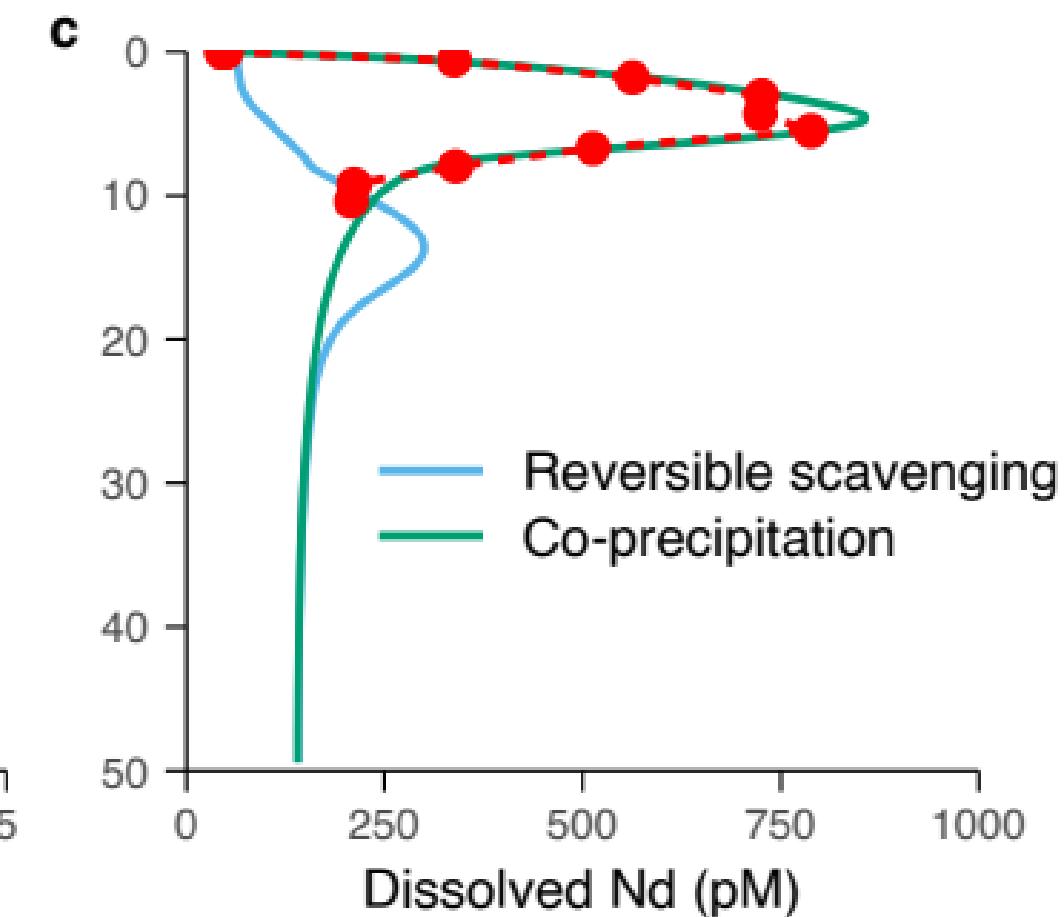
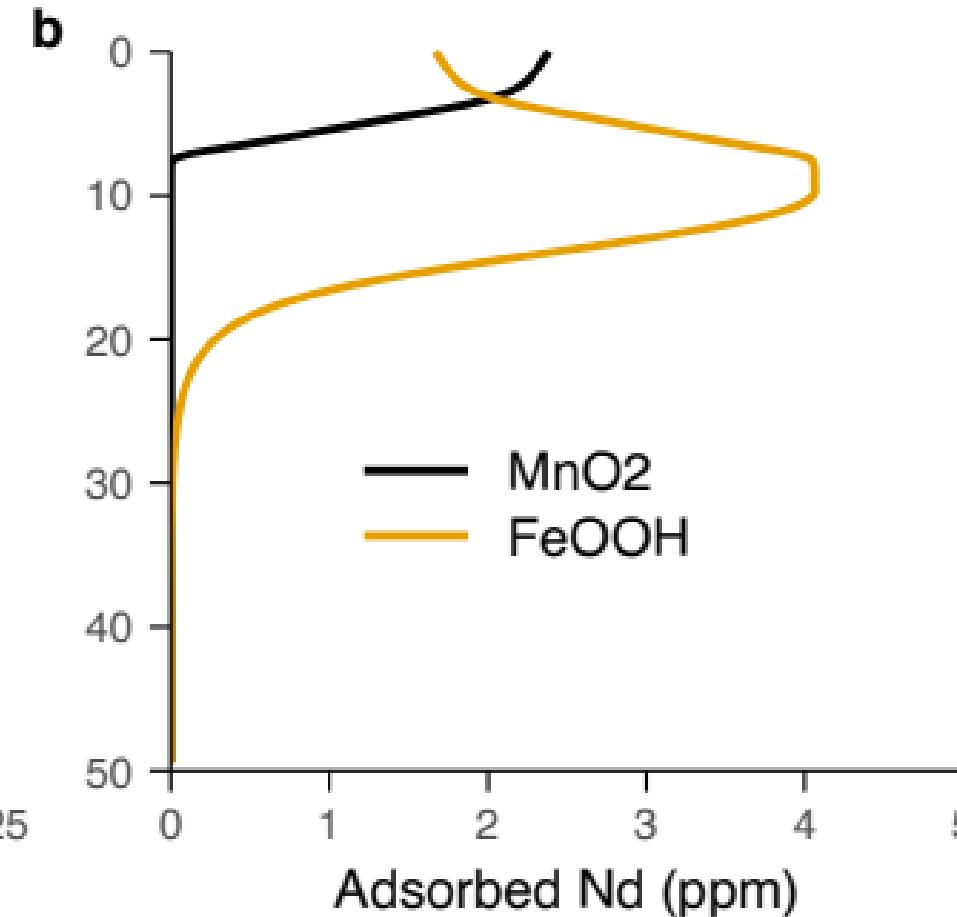
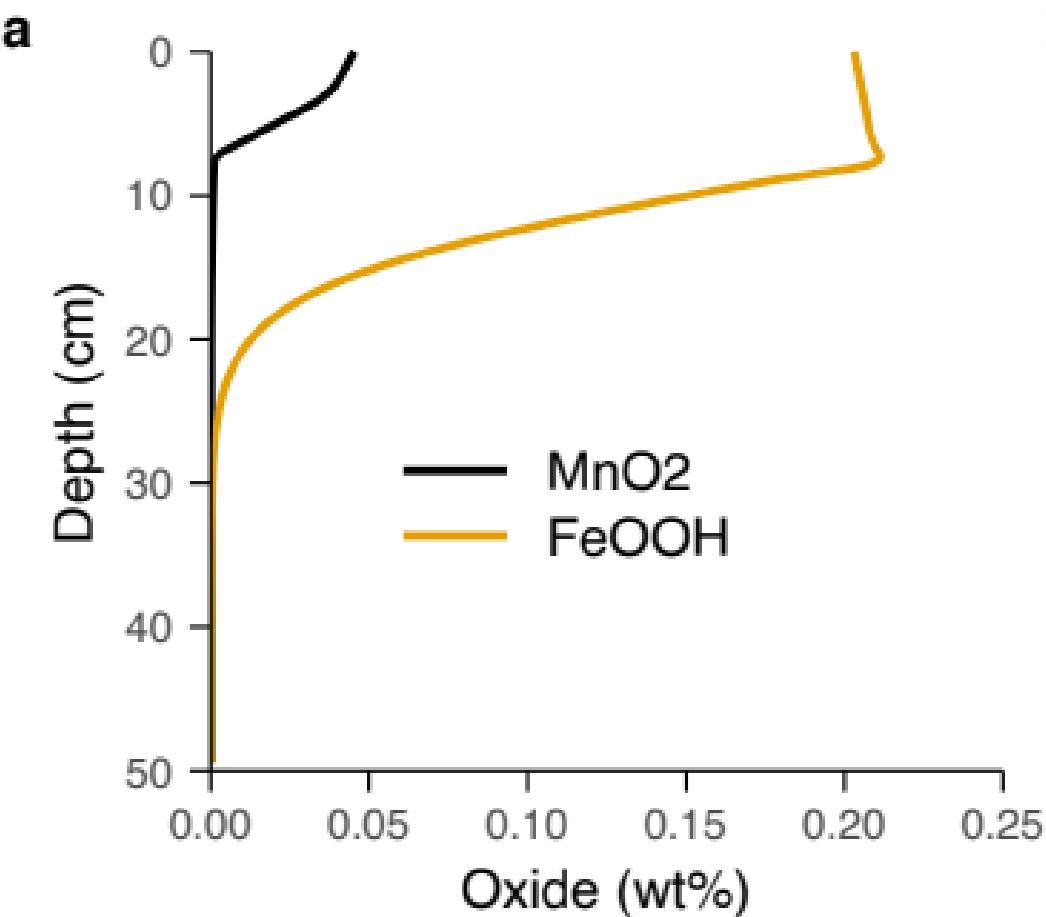
789 Zemmel, I., Cook, H.E., 1973. Appendix IV; X-ray mineralogy of sediments from the Northeast Pacific and  
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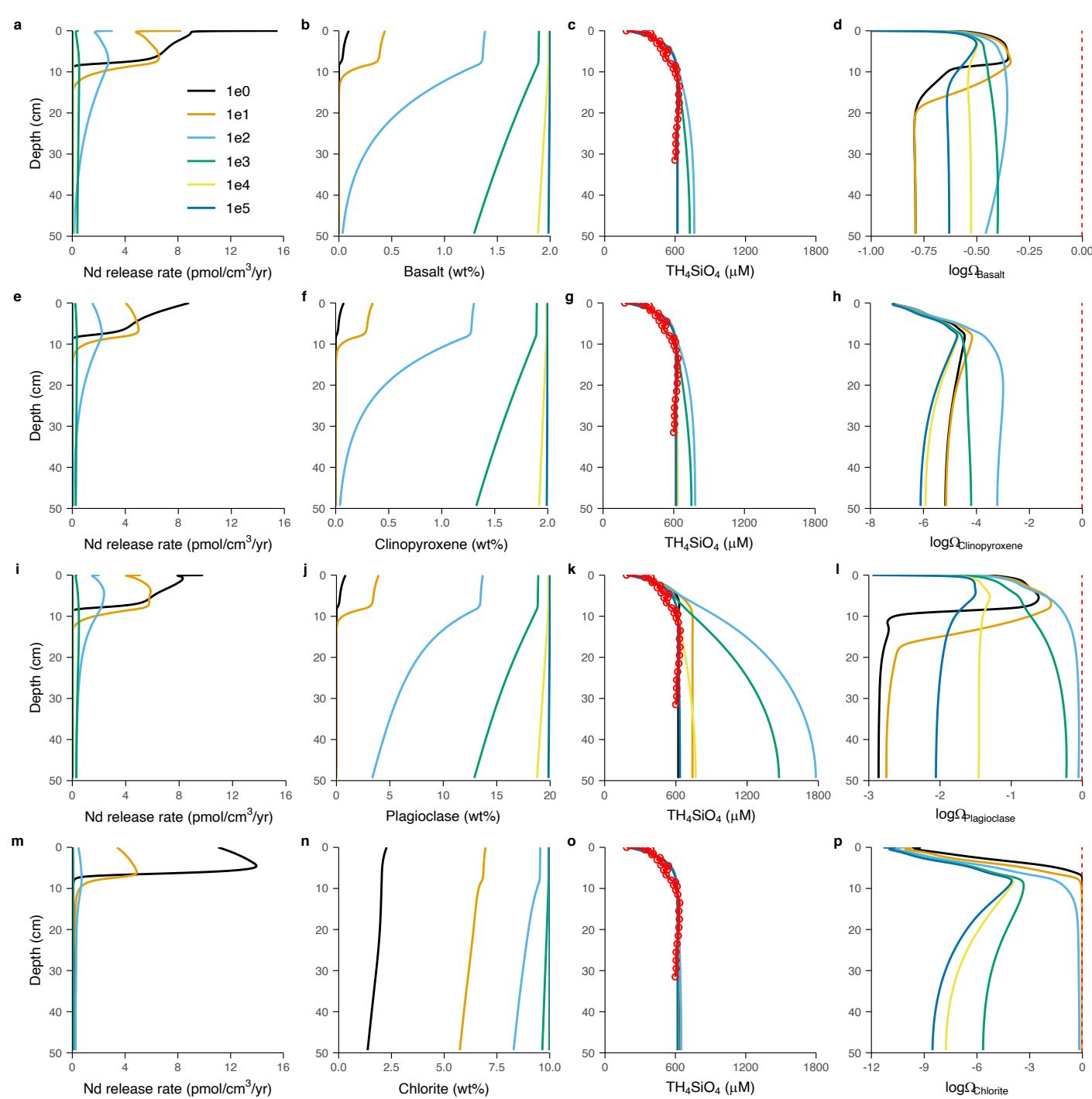
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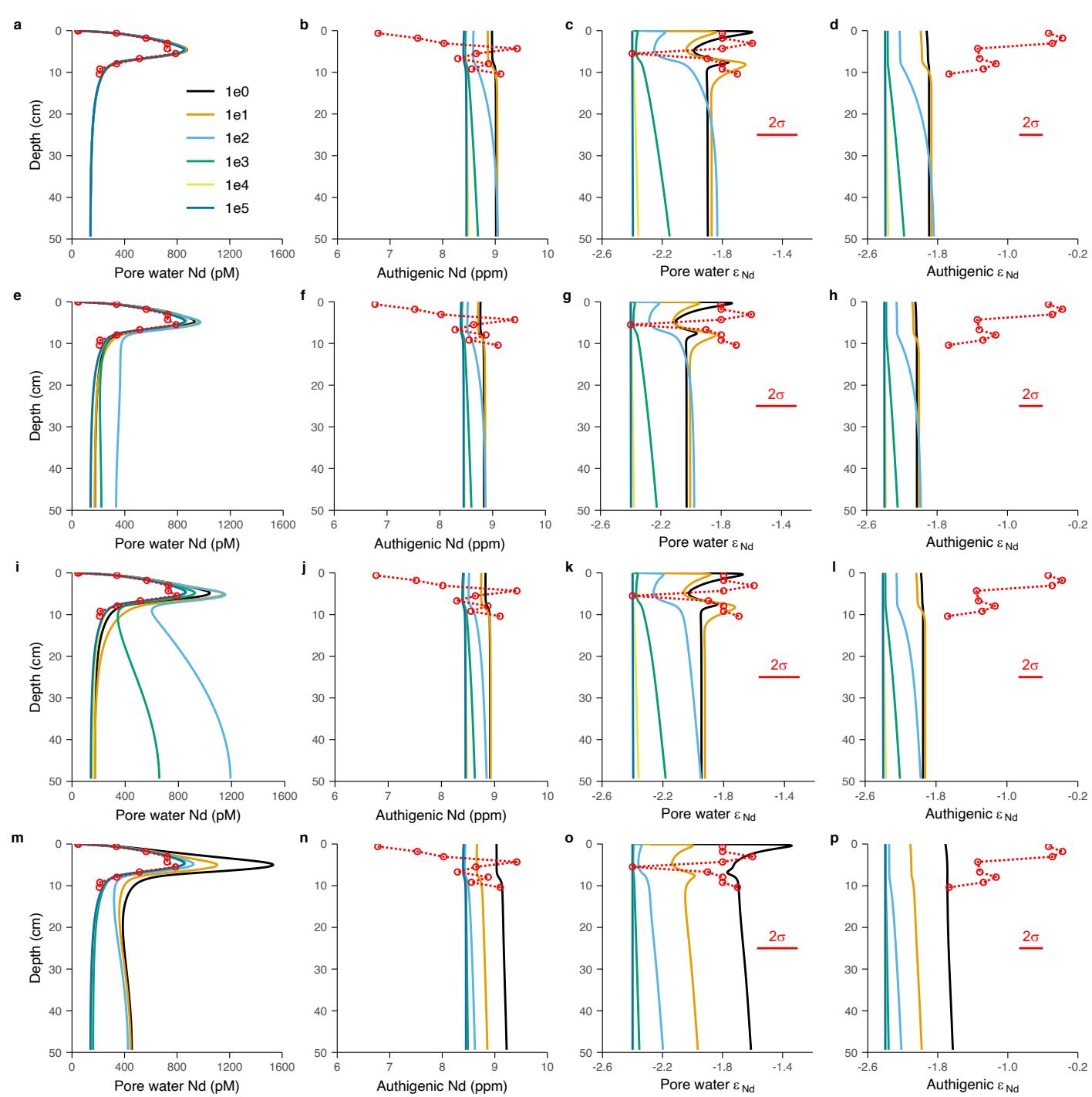


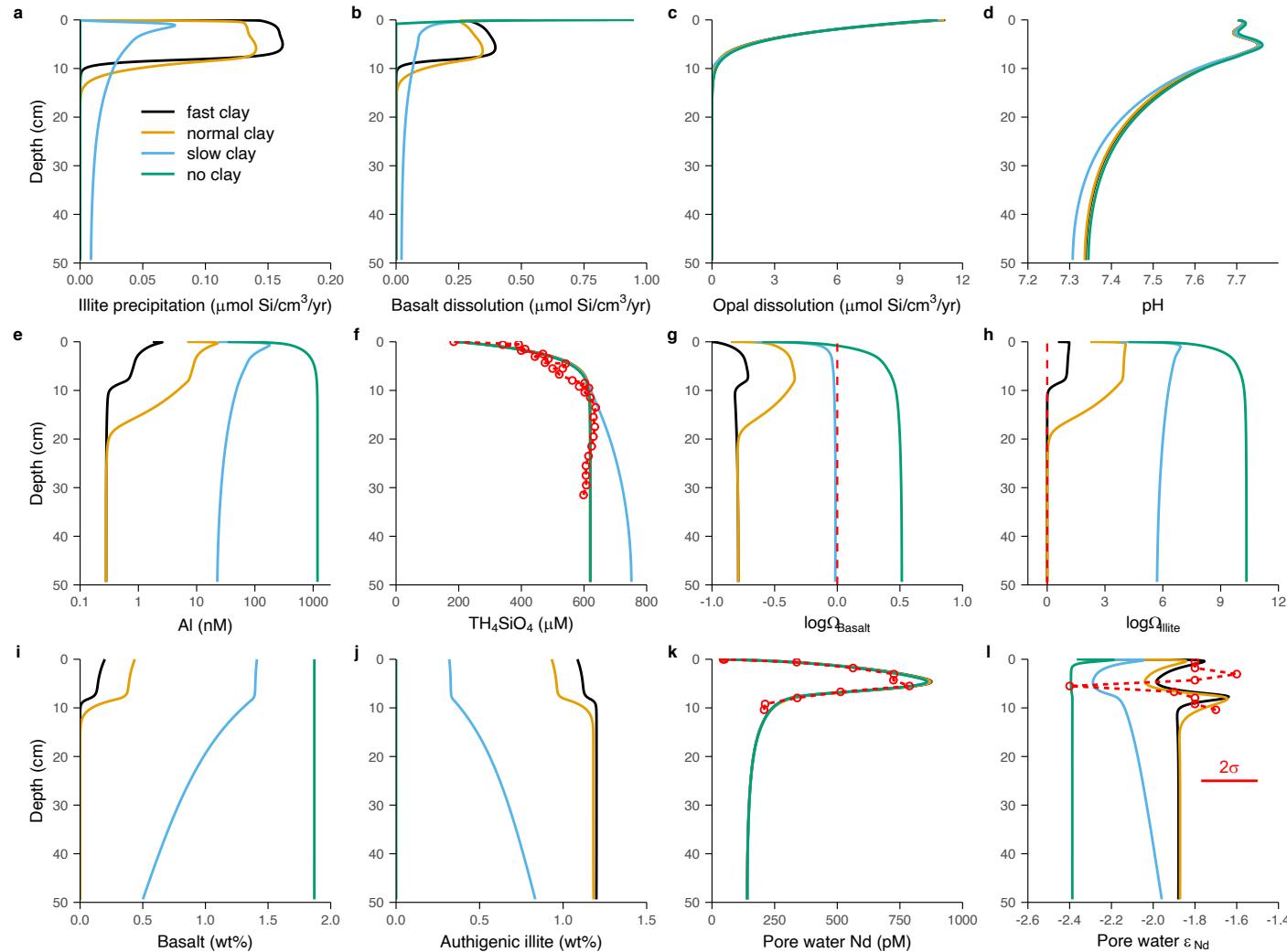


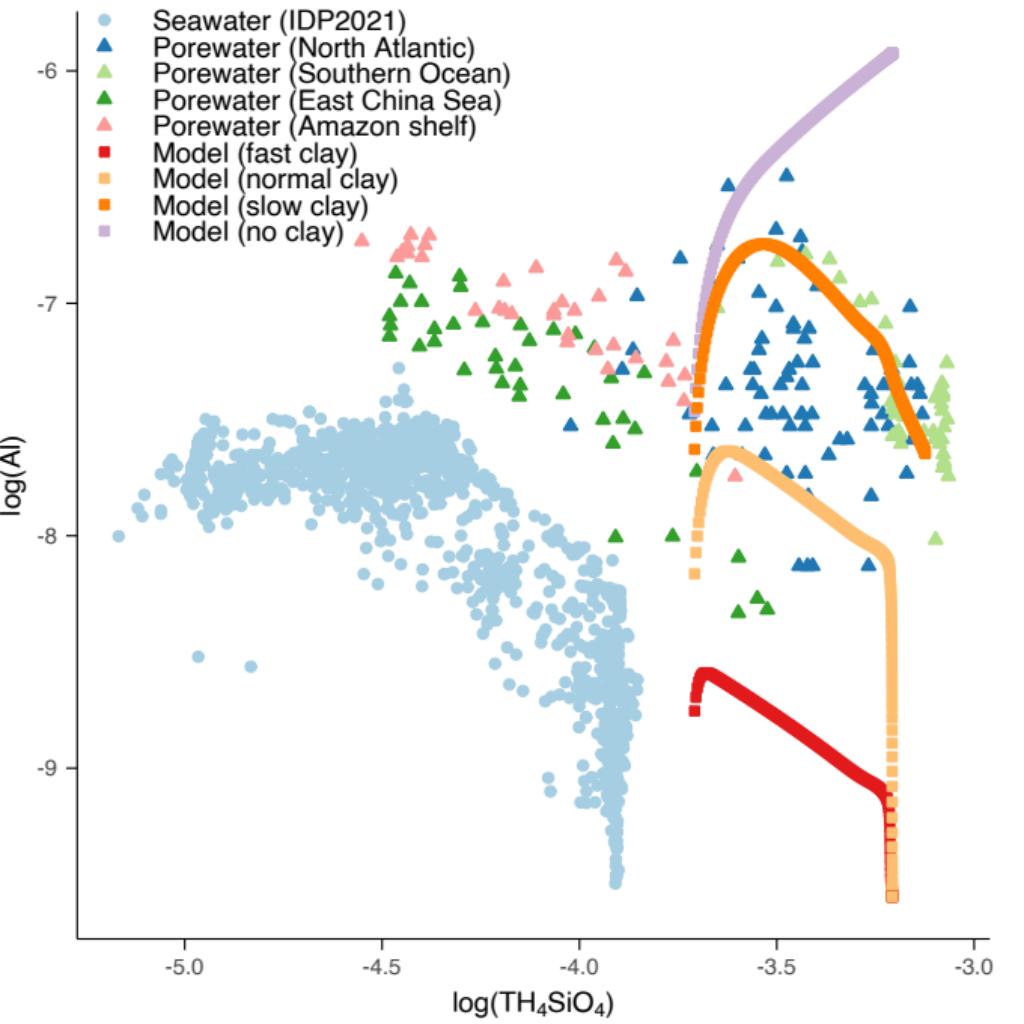


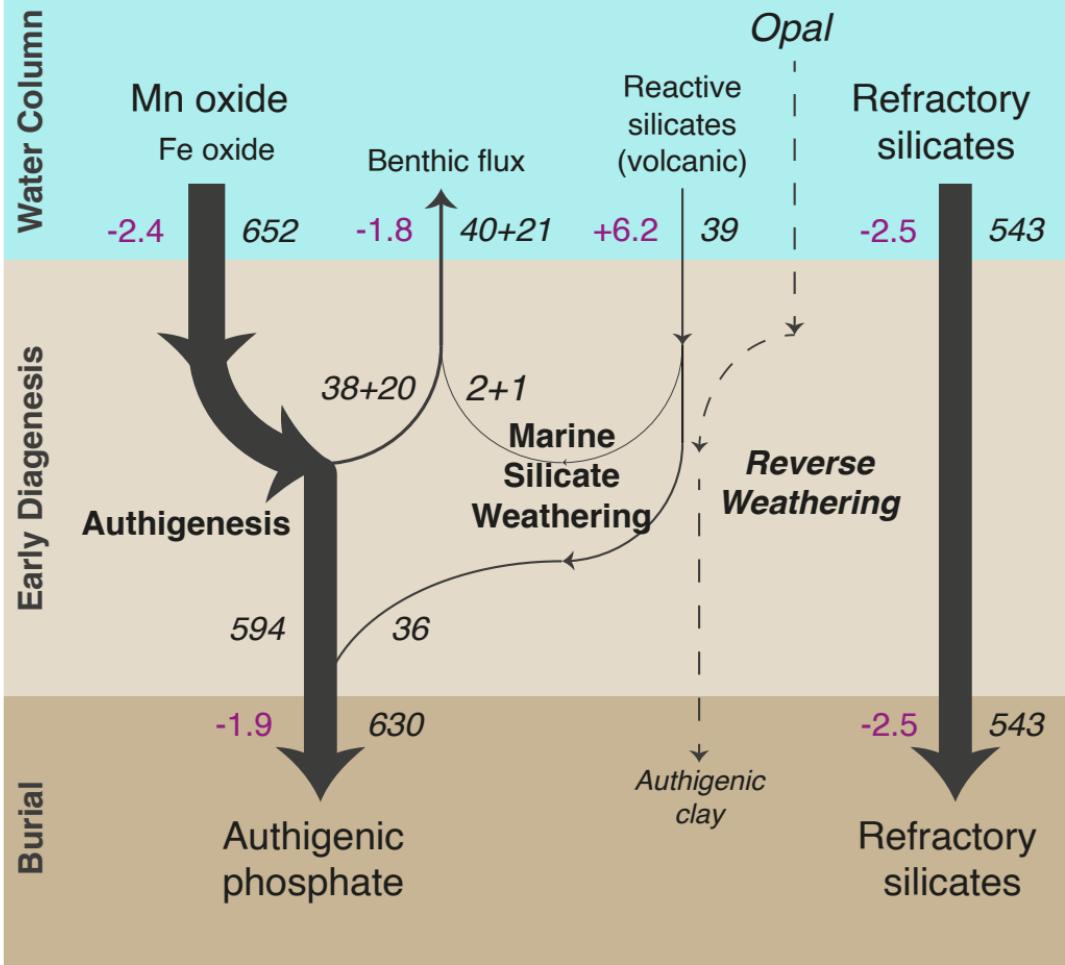












## Supplementary Information

## Reactive-transport modeling of neodymium and its radiogenic isotope in deep-sea sediments: the roles of authigenesis, marine silicate weathering and reverse weathering

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## Supplementary Methods

### 1. Diagenetic equations

The concentrations of dissolved ( $C_d$ , in mmol/cm<sup>3</sup> pore water) and solid ( $C_s$ , in mmol/cm<sup>3</sup> dry sediment) species are modeled using the classic 1-D reactive transport model of early diagenesis (Boudreau, 1997):

$$\varphi \frac{\partial C_d}{\partial z} = \frac{\partial}{\partial z} \left( \varphi D_d \frac{\partial C_d}{\partial z} \right) - \frac{\partial}{\partial z} (\varphi u_d C_d) + \varphi \alpha (C_{BW} - C_d) + \varphi \sum R, \quad (1)$$

$$(1 - \varphi) \frac{\partial C_s}{\partial z} = \frac{\partial}{\partial z} \left( (1 - \varphi) D_s \frac{\partial C_s}{\partial z} \right) - \frac{\partial}{\partial z} ((1 - \varphi) u_s C_s) + (1 - \varphi) \sum R, \quad (2)$$

where  $\varphi$  is porosity,  $z$  is sediment depth,  $C_{BW}$  is the bottom water concentration and  $R$  is the reaction rate. Physical transport includes molecular diffusion corrected for tortuosity ( $D_d$ ), burial ( $u_d$ ) and bio-irrigation ( $\alpha$ ) for dissolved species, and bioturbation ( $D_s$ ) and burial ( $u_s$ ) for solid species.

### 2. Physical transport

The physical transport in the model follows well-established principals in early diagenesis assuming steady state compaction (Berner, 1980; Boudreau, 1997; Dale et al., 2015; Meysman et al., 2003). The parameterizations of the transport terms are reported in Supplementary Table 1 and the parameters are reported in Supplementary Table 2.

### 3. Biogeochemical reaction network

The biogeochemical reaction network in the model follows the classic studies of early diagenesis including the organic carbon remineralization sequence, secondary redox reactions and minerals such as opal, calcite and Fe sulfides (Berner, 1980; Boudreau, 1997; Dale et al., 2015; Meysman et al., 2003; Wang and Van Cappellen, 1996). The reactions are reported in Supplementary Table 3, the rate expressions are reported in Supplementary Table 4, and the reaction parameters are reported in Supplementary Table 5. Silicate weathering and reverse weathering reactions are reported in Supplementary Table 6.

In the model we use the continuum model of POC reactivity (Boudreau et al., 2008; Boudreau and Ruddick, 1991):

$$k_{POC} = \frac{\nu}{a_0 + a}, \quad (3)$$

40 Here  $k_{POC}$  is the POC remineralization rate,  $\nu$  controls the shape of the gamma distribution  
 41 for POC mineralization,  $a_0$  is the initial age of POC, and  $a$  is duration of remineralization.  
 42 We model the deposition age of sediment (Meile and Van Cappellen, 2005) to represent  $a$  in  
 43 Eq. (3):

$$44 \frac{\partial Age}{\partial z} = \frac{1}{1-\varphi} \frac{\partial}{\partial z} \left( (1-\varphi) D_s \frac{\partial Age}{\partial z} \right) - \frac{1}{1-\varphi} \frac{\partial}{\partial z} \left( (1-\varphi) u_s Age \right) + 1, \quad (4)$$

#### 45 4. Adsorption

46 The adsorption of Nd is described in the main text. In the model,  $\text{NH}_4$  adsorption is  
 47 modeled as (Mackin and Aller, 1984):

$$48 NH_{4ads} = K NH_{4ads} \times NH_4, \quad (5)$$

49 Dissolved Fe and Mn can be adsorbed onto  $\text{FeOOH}$  and  $\text{MnO}_2$  (Katsev et al., 2007):

$$50 Fe_{ads-MnO_2} = K Fe_{ads-MnO_2} \times Fe \times MnO_2, \quad (6)$$

$$51 Fe_{ads-FeOOH} = K Fe_{ads-FeOOH} \times Fe \times FeOOH, \quad (7)$$

$$52 Mn_{ads-MnO_2} = K Mn_{ads-MnO_2} \times Mn \times MnO_2, \quad (8)$$

$$53 Mn_{ads-FeOOH} = K Mn_{ads-FeOOH} \times Mn \times FeOOH, \quad (9)$$

#### 54 5. Aqueous speciation

55 Speciation reactions and constants are reported in Supplementary Table 7 and 8. To  
 56 calculate mineral saturation state the model computes pore water pH and the speciation of  
 57 dissolved Nd, Fe(II) and Al. We follow the Direct Substitution Approach to pH modeling  
 58 (Hofmann et al., 2008):

$$59 \frac{\partial H}{\partial t} = \left( \frac{\partial TA}{\partial t} - \frac{\partial TCO_2}{\partial t} \frac{\partial TA}{\partial TCO_2} - \frac{\partial TH_2S}{\partial t} \frac{\partial TA}{\partial TH_2S} - \frac{\partial TB(OH)_3}{\partial t} \frac{\partial TA}{\partial TB(OH)_3} \right) / \frac{\partial TA}{\partial H}, \quad (10)$$

60 Proton (H) concentration is modeled dynamically following the impacts of transport  
 61 and reactions on *total* alkalinity ( $TA = \text{HCO}_3^- + 2\text{CO}_3^{2-} + \text{HS}^- + \text{B(OH)}_4^- + \text{OH}^- - \text{H}^+$ ), total carbon  
 62 ( $TCO_2 = \text{CO}_2 + \text{HCO}_3^- + \text{CO}_3^{2-}$ ), total sulfide ( $TH_2S = \text{H}_2\text{S} + \text{HS}^-$ ), total boron  
 63 ( $TB(OH)_3 = \text{B(OH)}_3 + \text{B(OH)}_4^-$ ) and their individual species. Given modeled pH and assuming  
 64 local equilibrium, the acid-base equilibria are computed, also including the dissociation of  
 65  $\text{H}_4\text{SiO}_4$  and  $\text{H}_3\text{PO}_4$ , which contribute little to TA but needed for metal speciation. *Apparent*  
 66 equilibrium constants for seawater are computed at *in situ* temperature (2°C) and pressure

67 (300 bar) using “seacarb” package (Gattuso et al., 2016) following the best practice  
68 recommendation of Dickson et al. (2007).

69 For Fe(II), complexation with  $\text{HS}^-$ ,  $\text{CO}_3^{2-}$ ,  $\text{HCO}_3^-$ ,  $\text{Cl}^-$ ,  $\text{SO}_4^{2-}$  are included (Pierrot and  
70 Millero, 2017; Rickard, 2006). For Al we consider stepwise hydrolysis (Brown and Ekberg,  
71 2016). *Apparent* equilibrium constants for complex formation and mineral saturation suitable  
72 for a seawater medium are either measured, or computed using the constants at zero ionic  
73 strength and the activity coefficients from the Pitzer equation based Miami Ion Interaction  
74 model of seawater (Pierrot and Millero, 2017). The constants at *in situ* temperature are  
75 computed whenever possible, otherwise those at the standard state (25°C) are used. The  
76 pressure effects are generally unknown and thus unaccounted for.

77 For example, the *apparent* solubility of Nd rhabdophane is computed as

$$78 \quad K_{\text{sp}}^0_{\text{NdPO}_4} = \frac{K_{\text{sp}}^0_{\text{NdPO}_4}}{\gamma_{\text{Nd}^{3+}} \gamma_{\text{PO}_4^{3-}}} \quad (11)$$

79 where  $K_{\text{sp}}^0_{\text{NdPO}_4}$  is the solubility at zero ionic strength and *in situ* temperature (Gausse et al.,  
80 2016), and  $\gamma$  are the activity coefficients in seawater at *in situ* temperature (Pierrot and  
81 Millero, 2017).

82 In the model, pore water concentrations of  $\text{Cl}^-$ ,  $\text{F}^-$ ,  $\text{Na}^+$ ,  $\text{Mg}^{2+}$ ,  $\text{K}^+$  are taken to be the same  
83 as seawater (salinity=35) as they generally remain constant in surface sediments, while other  
84 ligands and species are modeled explicitly. We do not consider organic ligands since they  
85 have not been characterized in sediment pore water.

## 86 6. Boundary conditions

87 Boundary conditions of modeled species are reported in Supplementary Table 9. In  
88 the model, the flux of Nd is linked to Fe/Mn oxides. In the reversible scavenging formulation,  
89 the flux of Nd entering sediments and adsorbed onto  $\text{MnO}_2$  (same for  $\text{FeOOH}$ ) is:

$$90 \quad FNd_{\text{MnO}_2-\text{ads}} = FMnO_2 \times K_{\text{ads-MnO}_2} \times {}^iNd_{\text{BW}}, \quad (12)$$

91 In the co-precipitation formulation, the flux of Nd entering sediments and co-  
92 precipitated with Mn is

$$93 \quad FNd_{\text{MnO}_2-\text{copre}} = FMnO_2 \times D_{\text{Nd/Mn}} \times \frac{{}^iNd_{\text{BW}}}{Mn_{\text{BW}}}, \quad (13)$$

94 Subscript “BW” refers to bottom water and  $FMnO_2$  is the flux of  $MnO_2$ . Both  
95 formulations assume that incoming oxides inherit  $\varepsilon_{Nd}$  from the bottom water.

96 Finally, using the modeled pore water Nd concentration, we compute the total benthic  
97 Nd flux as the sum of diffusive flux, burial flux and bio-irrigation flux:

98 
$$F_{Nd} = -\phi D_{Nd} \frac{\partial Nd}{\partial z} \Big|_{z=0} + \phi u_d Nd \Big|_{z=0} + \int_{0 \text{ cm}}^{50 \text{ cm}} \phi \alpha (Nd - Nd_{BW}) dz, \quad (14)$$

99 We compute the benthic flux of both  $^{143}\text{Nd}$  and  $^{144}\text{Nd}$ , and the  $\varepsilon_{Nd}$  is computed using the ratio  
100 of their fluxes accordingly.

## 101 7. Numerical solution

102 The model code is written in the Julia Language, a programming language for high-  
103 performance scientific computing (Bezanson et al., 2017). Diagenetic equations are  
104 discretized using the Method-of-Line approach (Boudreau, 1996), resulting in 6600 coupled  
105 and stiff ordinary differential equations in the baseline simulation. We solve the sparse  
106 system of equations using the CVODE\_BDF GMRES solver from the SUNDIALS package  
107 (Hindmarsh et al., 2005) included in the Julia package “DifferentialEquations.jl”  
108 (Rackauckas and Nie, 2017). The model is run dynamically toward steady state.

## 109 8. Data source

110 Geochemical datasets used in this study are derived from the GEOROC database:

111 Cascade Arc compilation: <https://doi.org/10.25625/PVFZCE>IDBJFS>.

112 Clinopyroxene compilation: <https://doi.org/10.25625/SGFTFN/QDDJRA>.

113 Plagioclase compilation: <https://doi.org/10.25625/SGFTFN/C8I6RT>.

## Supplementary Tables

**Supplementary Table 1. Parameterization of physical transport**

| Variables                      | Parameterization   |
|--------------------------------|--|
| Porosity                       | $\varphi(z) = (\varphi_0 - \varphi_L)\exp(-z/z_\varphi) + \varphi_L$ |
| Pore water burial velocity     | $u_d(z) = \frac{\varphi_L}{\varphi(z)} u_s^L$                        |
| Solid sediment burial velocity | $u_s(z) = \frac{1-\varphi_L}{1-\varphi(z)} u_s^L$                    |
| Final sediment burial velocity | $u_s^L = \frac{F_{sed}}{\rho_s(1-\varphi_L)}$                        |
| Bioturbation                   | $D_s(z) = D_s^0 \operatorname{erfc}(\frac{z-z_s}{2})$                |
| Bio-irrigation                 | $\alpha(z) = \alpha^0 \exp(-\frac{z}{z_{\text{irr}}})$               |
| Molecular diffusion            | $D_d(z) = \frac{D_m}{1-\ln(\varphi^2(z))}$                           |

**Supplementary Table 2. Parameters of physical transport**

| Parameter        | Explanation                  | Values   | Sources                         |
|------------------|------------------------------|--|---------------------------------|
| $\varphi_0$      | Porosity at 0 cm             | 0.8  | This study                      |
| $\varphi_L$      | Porosity at 50 cm            | 0.7  | This study                      |
| $z_\varphi$      | Porosity attenuation scale   | 5 cm   | This study                      |
| $F_{sed}$        | Total sediment flux          | $1.01 \times 10^{-2} \text{ g/cm}^2/\text{yr}$ | (Lyle et al., 1992)             |
| $\rho_s$         | Dry sediment density         | 2.6 g/cm <sup>3</sup>                          | This study                      |
| $D_s^0$          | Bioturbation at 0 cm         | 1.9 cm <sup>2</sup> /yr                        | (Middelburg et al., 1997)       |
| $z_s$            | Mixed layer depth scale      | 6 cm   | (Boudreau, 1994)                |
| $\alpha^0$       | Bio-irrigation at 0 cm       | 28.4 yr <sup>-1</sup>                          | (Meile and Van Cappellen, 2003) |
| $z_{\text{irr}}$ | Irrigation attenuation scale | 2 cm   | This study                      |
| $D_m$            | Molecular diffusivity        | Calculated for each species                    | (Boudreau, 1997)                |

**Supplementary Table 3. Biogeochemical reaction network**

| Reaction                          | Explanation                    | Chemical equation  |
|-----------------------------------|--------------------------------|--|
| RO2POC <sup>1</sup>               | Aerobic respiration of POC     | $(CH_2O)(NH_3)[rNC](H_3PO_4)[rPC] + O_2 + (rNC-rPC)*H\{+\} = CO_2 + rNC*NH_4\{+\} + rPC*H_2PO_4\{-\} + H_2O$                               |
| RNO2POC                           | Denitrification using NO2      | $(CH_2O)(NH_3)[rNC](H_3PO_4)[rPC] + 4/3*NO_2\{-\} + (4/3+rNC - rPC)*H\{+\} = CO_2 + rNC*NH_4\{+\} + rPC*H_2PO_4\{-\} + 2/3*N_2 + 5/3*H_2O$ |
| RNO3POC                           | Denitrification using NO3      | $(CH_2O)(NH_3)[rNC](H_3PO_4)[rPC] + 2*NO_3\{-\} + (rNC - rPC)*H\{+\} = CO_2 + rNC*NH_4\{+\} + rPC*H_2PO_4\{-\} + 2*NO_2\{-\} + H_2O$       |
| RMnO2POC                          | Mn reduction by POC            | $(CH_2O)(NH_3)[rNC](H_3PO_4)[rPC] + 2*MnO_2 + (4 + rNC - rPC)*H\{+\} = CO_2 + rNC*NH_4\{+\} + rPC*H_2PO_4\{-\} + 2*Mn\{2+\} + 3*H_2O$      |
| RFeOOHPOC                         | Fe reduction by POC            | $(CH_2O)(NH_3)[rNC](H_3PO_4)[rPC] + 4*FeOOH + (8+rNC - rPC)*H\{+\} = CO_2 + rNC*NH_4\{+\} + rPC*H_2PO_4\{-\} + 4*Fe\{2+\} + 7*H_2O$        |
| RSO4POC                           | SO4 reduction by POC           | $(CH_2O)(NH_3)[rNC](H_3PO_4)[rPC] + 1/2*SO_4\{2-\} + (1+rNC - rPC)*H\{+\} = CO_2 + rNC*NH_4\{+\} + rPC*H_2PO_4\{-\} + 1/2*H_2S + H_2O$     |
| RCH4POC                           | Methanogenesis                 | $(CH_2O)(NH_3)[rNC](H_3PO_4)[rPC] + (rNC - rPC)*H\{+\} = 1/2*CO_2 + 1/2*CH_4 + rNC*NH_4\{+\} + rPC*H_2PO_4\{-\}$                           |
| RO2NO2                            | Oxidation of NO2 by O2         | $1/2*O_2 + NO_2\{-\} = NO_3\{-\}$  |
| RO2NH4                            | Oxidation of NH4 by O2         | $3/2*O_2 + NH_4\{+\} = NO_2\{-\} + 2*H\{+\} + H_2O$  |
| RO2Mn                             | Oxidation of Mn2+ by O2        | $1/2*O_2 + Mn\{2+\} + H_2O = MnO_2 + 2*H\{+\}$   |
| RO2Mn <sub>ads</sub> <sup>2</sup> | Oxidation of adsorbed Mn by O2 | $1/2*O_2 + Mn_{ads} + H_2O = MnO_2 + 2*H\{+\}$   |
| RO2Fe                             | Oxidation of Fe2+ by O2        | $1/4*O_2 + Fe\{2+\} + 3/2*H_2O = FeOOH + 2*H\{+\}$   |
| RO2Fe <sub>ads</sub> <sup>3</sup> | Oxidation of adsorbed Fe by O2 | $1/4*O_2 + Fe_{ads} + 3/2*H_2O = FeOOH + 2*H\{+\}$   |
| RO2H2S                            | Oxidation of H2S by O2         | $2*O_2 + H_2S = SO_4\{2-\} + 2*H\{+\}$   |
| RO2FeS                            | Oxidation of FeS by O2         | $9/4*O_2 + FeS + 3/2*H_2O = FeOOH + SO_4\{2-\} + 2*H\{+\}$   |
| RO2CH4                            | Oxidation of CH4 by O2         | $2*O_2 + CH_4 = CO_2 + 2*H_2O$   |
| RNO2NH4                           | Anammox                        | $NO_2\{-\} + NH_4\{+\} = N_2 + 2*H_2O$   |
| RSO4CH4                           | Anaerobic oxidation of methane | $SO_4\{2-\} + CH_4 + 2*H\{+\} = CO_2 + H_2S + 2*H_2O$  |
| RMnO2Fe                           | Oxidation of Fe2+ by MnO2      | $1/2*MnO_2 + Fe\{2+\} + H_2O = 1/2*Mn\{2+\} + FeOOH + H\{+\}$  |
| RMnO2H2S                          | Oxidation of H2S by MnO2       | $MnO_2 + H_2S + 2*H\{+\} = Mn\{2+\} + S + 2*H_2O$  |
| RFeOOHH2S                         | Oxidation of H2S by FeOOH      | $2*FeOOH + H_2S + 4*H\{+\} = 2*Fe\{2+\} + S + 4*H_2O$  |
| RFeSH2S                           | Precipitation of pyrite        | $FeS + H_2S = FeS_2 + H_2$   |
| RFeS <sub>dis</sub>               | FeS dissolution                | $FeS + H\{+\} = Fe\{2+\} + HS\{-\}$  |
| RFeS <sub>pre</sub>               | FeS precipitation              | $Fe\{2+\} + HS\{-\} = FeS + H\{+\}$  |
| RCaCO3 <sub>dis</sub>             | Calcite dissolution            | $CaCO_3 = Ca\{2+\} + CO_3\{2-\}$   |
| RBSi <sub>dis</sub> <sup>4</sup>  | Biogenic opal dissolution      | $SiO_2(Al)[rAlSi] + 2*H_2O = H_4SiO_4 + rAlSi*Al\{3+\}$  |

<sup>1</sup>The chemical formula of POC is  $(CH_2O)(NH_3)[rNC](H_3PO_4)[rPC]$ , where  $rNC$  is the N:C ratio and  $rPC$  is the P:C ratio.

<sup>2</sup> $Mn_{ads}$  is the sum of Mn adsorbed on MnO2 and FeOOH.

<sup>3</sup> $Fe_{ads}$  is the sum of Fe adsorbed on MnO2 and FeOOH.

<sup>4</sup>Biogenic opal contains Al at an Al:Si molar ratio of  $rAlSi$ .

**Supplementary Table 4. Biogeochemical reaction rates**

| Reaction                           | Rate expression  |
|------------------------------------|--|
| RO2POC                             | $O_2/(K_02+O_2)^*v/(a_0+A_{ge})*POC$   |
| RNO2POC                            | $NO_2/(KNO_2+NO_2)^*K_02/(K_02+O_2)^* v/(a_0+A_{ge})*POC$  |
| RNO3POC                            | $NO_3/(KNO_3+NO_3)^*KNO_2/(KNO_2+NO_2)^*K_02/(K_02+O_2)^* v/(a_0+A_{ge})*POC$  |
| RMnO2POC                           | $MnO_2/(KMnO_2+MnO_2)^*KNO_3/(KNO_3+NO_3)^*KNO_2/(KNO_2+NO_2)^*K_02/(K_02+O_2)^* v/(a_0+A_{ge})*POC$   |
| RFeOOHPOC                          | $FeOOH/(KFeOOH+FeOOH)^*KMnO_2/(KMnO_2+MnO_2)^*KNO_3/(KNO_3+NO_3)^*KNO_2/(KNO_2+NO_2)^*K_02/(K_02+O_2)^* v/(a_0+A_{ge})*POC$                      |
| RSO4POC                            | $SO_4/(KSO_4+SO_4)^*KFeOOH/(KFeOOH+FeOOH)^*KMnO_2/(KMnO_2+MnO_2)^*KNO_3/(KNO_3+NO_3)^*KNO_2/(KNO_2+NO_2)^*K_02/(K_02+O_2)^* v/(a_0+A_{ge})*POC$  |
| RCH4POC                            | $KSO_4/(KSO_4+SO_4)^*KFeOOH/(KFeOOH+FeOOH)^*KMnO_2/(KMnO_2+MnO_2)^*KNO_3/(KNO_3+NO_3)^*KNO_2/(KNO_2+NO_2)^*K_02/(K_02+O_2)^* v/(a_0+A_{ge})*POC$ |
| RO2NO2                             | $kO_2NO_2^*O_2^*NO_2$  |
| RO2NH4                             | $kO_2NH_4^*O_2^*NH_4$  |
| RO2Mn                              | $kO_2Mn^*O_2^*Mn$  |
| RO2Mn <sub>ads</sub> <sup>1</sup>  | $kO_2Mn_{ads}^*O_2^*Mn_{ads}^*dstopw$  |
| RO2Fe                              | $kO_2Fe^*O_2^*Fe$  |
| RO2Fe <sub>ads</sub> <sup>1</sup>  | $kO_2Fe_{ads}^*O_2^*Fe_{ads}^*dstopw$  |
| RO2H2S                             | $kO_2H_2S^*O_2^*TH_2S$   |
| RO2FeS                             | $kO_2FeS^*O_2^*FeS$  |
| RO2CH4                             | $kO_2CH_4^*O_2^*CH_4$  |
| RNO2NH4                            | $kNO_2NH_4^*NO_2^*NH_4$  |
| RSO4CH4                            | $kAOM^*CH_4^*SO_4/(SO_4+KAOM)$   |
| RMnO2Fe                            | $kMnO_2Fe^*MnO_2^*Fe$  |
| RMnO2H2S                           | $kMnO_2H_2S^*MnO_2^*TH_2S$   |
| RFeOOHH2S                          | $kFeOOHH_2S^*FeOOH^*TH_2S$   |
| RFeSH2S                            | $kFeSH_2S^*FeS^*TH_2S$   |
| RFeS <sub>dis</sub> <sup>2</sup>   | $kFeS_{dis}^*FeS^*(1-Fe_{free}^*HS/(H^*KspFeS)), \text{ if } Fe_{free}^*HS/(H^*KspFeS) < 1$  |
| RFeS <sub>pre</sub> <sup>2</sup>   | $kFeS_{pre}^*Fe^*TH_2S^*(Fe_{free}^*HS/(H^*KspFeS)-1), \text{ if } Fe_{free}^*HS/(H^*KspFeS) > 1$  |
| RCaCO3 <sub>dis</sub> <sup>3</sup> | $kCaCO_3dis0^*CaCO_3 + kCaCO_3dis1^*CaCO_3^*(1-Ca^*CO_3/KspCaCO_3_{dis})^nCaCO_3dis, \text{ if } Ca^*CO_3/KspCaCO_3 < 1$                         |
| RBSi <sub>dis</sub>                | $kBSi_{dis}^*BSi^*(1-TH_4SiO_4/TH_4SiO_4_{sat}), \text{ if } TH_4SiO_4/TH_4SiO_4_{sat} < 1$  |

<sup>1</sup> Rate is converted to unit in per volume of pore water by multiplying  $dstopw = (1 - \varphi)/\varphi$

<sup>2</sup>  $Fe_{free}$  is the free  $Fe^{2+}$  concentration computed using the speciation model.

<sup>3</sup> Calcite dissolution rate is the sum of the close to saturation rate ( $kCaCO_3dis0$ ) and the far from saturation rate ( $kCaCO_3dis1$ ) (Naviaux et al., 2019).

**Supplementary Table 5. Biogeochemical reaction parameters**

| Parameter           | Value      | Unit <sup>1</sup>   | Explanation   | Sources  |
|---------------------|------------|---|---|--|
| $\nu$               | 0.125      | dimensionless   | Shape of the gamma distribution of POC reactivity             | (Boudreau et al., 2008)                              |
| $a_0$               | 60         | yr  | Initial age of POC  | This study   |
| $r_{NC}$            | 16/117     | mol/mol   | N:C ratio of POC  | (Anderson and Sarmiento, 1994)                       |
| $r_{PC}$            | 1/170      | mol/mol   | P:C ratio of POC  | This study   |
| $K_{O_2}$           | 1.00E-06   | mmol cm <sup>-3</sup> pw                                  | Half saturation constant of O <sub>2</sub> in POC oxidation   | (Dale et al., 2015)                                  |
| $K_{NO_2}$          | 1.00E-05   | mmol cm <sup>-3</sup> pw                                  | Half saturation constant of NO <sub>2</sub> in POC oxidation  | (Dale et al., 2015)                                  |
| $K_{NO_3}$          | 1.00E-05   | mmol cm <sup>-3</sup> pw                                  | Half saturation constant of NO <sub>3</sub> in POC oxidation  | (Dale et al., 2015)                                  |
| $K_{MnO_2}$         | 0.03       | mmol cm <sup>-3</sup> ds                                  | Half saturation constant of MnO <sub>2</sub> in POC oxidation | (Dale et al., 2015)                                  |
| $K_{FeOOH}$         | 8.8        | mmol cm <sup>-3</sup> ds                                  | Half saturation constant of FeOOH in POC oxidation            | This study   |
| $K_{SO_4}$          | 2.60E-06   | mmol cm <sup>-3</sup> pw                                  | Half saturation constant of SO <sub>4</sub> in POC oxidation  | (Contreras et al., 2013)                             |
| $k_{O_2NO_2}$       | 1.00E+07   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup> yr <sup>-1</sup> | Rate of NO <sub>2</sub> oxidation by O <sub>2</sub>           | (Dale et al., 2015)                                  |
| $k_{O_2NH_4}$       | 1.00E+07   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup> yr <sup>-1</sup> | Rate of NH <sub>4</sub> oxidation by O <sub>2</sub>           | (Dale et al., 2015)                                  |
| $k_{O_2Mn}$         | 0.00E+00   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup> yr <sup>-1</sup> | Rate of Mn <sup>2+</sup> oxidation by O <sub>2</sub>          | (Meysman et al., 2003; Wang and Van Cappellen, 1996) |
| $k_{O_2Mn\_ads}$    | 1.00E+06   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup> yr <sup>-1</sup> | Rate of adsorbed Mn oxidation by O <sub>2</sub>               | (Meysman et al., 2003; Wang and Van Cappellen, 1996) |
| $k_{O_2Fe}$         | 1.00E+07   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup> yr <sup>-1</sup> | Rate of Fe <sup>2+</sup> oxidation by O <sub>2</sub>          | (Meysman et al., 2003; Wang and Van Cappellen, 1996) |
| $k_{O_2Fe\_ads}$    | 1.00E+06   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup> yr <sup>-1</sup> | Rate of adsorbed Fe oxidation by O <sub>2</sub>               | (Meysman et al., 2003; Wang and Van Cappellen, 1996) |
| $k_{O_2H_2S}$       | 1.00E+05   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup> yr <sup>-1</sup> | Rate of H <sub>2</sub> S oxidation by O <sub>2</sub>          | (Meysman et al., 2003; Wang and Van Cappellen, 1996) |
| $k_{O_2FeS}$        | 1.00E+05   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup> yr <sup>-1</sup> | Rate of FeS oxidation by O <sub>2</sub>                       | (Meysman et al., 2003; Wang and Van Cappellen, 1996) |
| $k_{O_2CH_4}$       | 1.00E+10   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup> yr <sup>-1</sup> | Rate of CH <sub>4</sub> oxidation by O <sub>2</sub>           | (Meysman et al., 2003; Wang and Van Cappellen, 1996) |
| $k_{NO_2NH_4}$      | 1.00E+08   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup> yr <sup>-1</sup> | Rate of anammox   | (Dale et al., 2015)                                  |
| $k_{AOM}$           | 4.00E-02   | yr <sup>-1</sup>  | Rate of anaerobic oxidation of methane (AOM)                  | (Contreras et al., 2013)                             |
| $K_{AOM}$           | 1.00E-03   | mmol cm <sup>-3</sup> pw                                  | Half saturation constant of SO <sub>4</sub> in AOM            | (Contreras et al., 2013)                             |
| $k_{MnO_2Fe}$       | 1.00E+06   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup> yr <sup>-1</sup> | Rate of Fe <sup>2+</sup> oxidation by MnO <sub>2</sub>        | (Meysman et al., 2003; Wang and Van Cappellen, 1996) |
| $k_{MnO_2H_2S}$     | 1.00E+04   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup> yr <sup>-1</sup> | Rate of H <sub>2</sub> S oxidation by MnO <sub>2</sub>        | (Meysman et al., 2003; Wang and Van Cappellen, 1996) |
| $k_{FeOOHH_2S}$     | 1.00E+01   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup> yr <sup>-1</sup> | Rate of H <sub>2</sub> S oxidation by FeOOH                   | This study   |
| $k_{FeSH_2S}$       | 1.00E+07   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup> yr <sup>-1</sup> | Rate of pyrite precipitation                                  | (Meysman et al., 2003; Wang and Van Cappellen, 1996) |
| $K_{spFeS}$         | 1.3465E-03 | mmol cm <sup>-3</sup> pw                                  | Solubility of FeS   | (Rickard, 2006)                                      |
| $k_{FeSdis}$        | 1.00E-03   | yr <sup>-1</sup>  | Rate of FeS dissolution                                       | (Meysman et al., 2003; Wang and Van Cappellen, 1996) |
| $k_{FeSpre}$        | 2.00E+03   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup> yr <sup>-1</sup> | Rate of FeS precipitation                                     | This study   |
| $k_{CaCO_3dis0}$    | 5.54E-02   | yr <sup>-1</sup>  | Close to saturation dissolution rate constant of calcite      | (Naviaux et al., 2019)                               |
| $k_{CaCO_3dis1}$    | 1.75E+02   | yr <sup>-1</sup>  | Far from saturation dissolution rate constant of calcite      | (Naviaux et al., 2019)                               |
| $n_{CaCO_3dis}$     | 5          | dimensionless   | Order of far from saturation dissolution rate of calcite      | (Naviaux et al., 2019)                               |
| $K_{spCaCO_3}$      | 7.8636E-07 | (mmol cm <sup>-3</sup> pw) <sup>2</sup>                   | Solubility of calcite   | (Gattuso et al., 2016)                               |
| $k_{BSi\_dis}$      | 0.025      | yr <sup>-1</sup>  | Dissolution rate of biogenic opal                             | (Van Cappellen et al., 2002)                         |
| $TH_{4SiO_4\_sat}$  | 6.20E-04   | mmol cm <sup>-3</sup> pw                                  | Saturation concentration of opal dissolution                  | This study   |
| $r_{AlSi}$          | 0.0025     | mol/mol   | Al/Si ratio in opal   | (Van Cappellen et al., 2002)                         |
| $K_{NH_4ads}$       | 4.16       | cm <sup>3</sup> (pw) cm <sup>-3</sup> (ds)                | Adsorption constant of NH <sub>4</sub>                        | (Mackin and Aller, 1984)                             |
| $K_{Mn_{ads}MnO_2}$ | 1.00E+04   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup>                  | Adsorption constant of dissolved Mn on MnO <sub>2</sub>       | (Van Cappellen et al., 2002)                         |
| $K_{Mn_{ads}FeOOH}$ | 1.00E+02   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup>                  | Adsorption constant of dissolved Mn on FeOOH                  | (Van Cappellen et al., 2002)                         |
| $K_{Fe_{ads}MnO_2}$ | 1.00E+04   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup>                  | Adsorption constant of dissolved Fe on MnO <sub>2</sub>       | (Van Cappellen et al., 2002)                         |
| $K_{Fe_{ads}FeOOH}$ | 1.00E+04   | (mmol cm <sup>-3</sup> pw) <sup>-1</sup>                  | Adsorption constant of dissolved Fe on FeOOH                  | (Van Cappellen et al., 2002)                         |

<sup>1</sup>Units of volume are either referring to pore water (pw) or dry sediments (ds).

**Supplementary Table 6. Silicate weathering and reverse weathering reactions.**

| Reaction   | Solubility<br>logK | Rate<br>Logk<br>(mol/m <sup>2</sup> /s) | Surface<br>area<br>(m <sup>2</sup> /g) <sup>1</sup> | Reference & Comment  |
|--|--------------------|---|---|--|
| <b>Basalt</b><br>$\text{SiAl}_{0.36}\text{O}_2(\text{OH})_{1.08} + 0.92\text{H}_2\text{O} + 1.08\text{H}^+ = \text{H}_4\text{SiO}_4 + 0.36\text{Al}^{3+}$  | 0.64               | -8.05                                   | 7   | (1) Solubility is computed as the stoichiometrically weighted sum of amorphous Si gel and gibbsite dissolution (Gislason and Oelkers, 2003) at <i>in situ</i> temperature and pressure using SUPCRTBL (Zimmer et al., 2016). It is then converted to apparent solubility in seawater using the activity coefficient at <i>in situ</i> temperature and salinity from the Miami Pitzer Model (Pierrot and Millero, 2017). (2) Dissolution rate at near neutral condition is from (Heřmanská et al., 2022). |
| <b>Clinopyroxene (Di<sub>45</sub>Hed<sub>25</sub>En<sub>19</sub>Fs<sub>11</sub>)</b><br>$\text{Ca}_{0.7}\text{Mg}_{0.84}\text{Fe}_{0.46}\text{Si}_2\text{O}_6 + 4\text{H}^+ + 2\text{H}_2\text{O} = 0.7\text{Ca}^{2+} + 0.84\text{Mg}^{2+} + 0.46\text{Fe}^{2+} + 2\text{H}_4\text{SiO}_4$ | 23.63              | -11.65                                  | 7   | (1) Solubility at <i>in situ</i> temperature is from (Stefánsson, 2001), then converted to apparent solubility in seawater using the activity coefficient at <i>in situ</i> temperature and salinity (Pierrot and Millero, 2017). (2) Dissolution rate at near neutral condition is from (Heřmanská et al., 2022).   |
| <b>Plagioclase (An<sub>29</sub>Ab<sub>71</sub>)</b><br>$\text{Ca}_{0.29}\text{Na}_{0.71}\text{Al}_{1.29}\text{Si}_{2.71}\text{O}_8 + 5.16\text{H}^+ + 2.84\text{H}_2\text{O} = 0.29\text{Ca}^{2+} + 0.71\text{Na}^+ + 1.29\text{Al}^{3+} + 2.71\text{H}_4\text{SiO}_4$                     | 14.04              | -8.41                                   | 7   | (1) Solubility at <i>in situ</i> temperature is from (Stefánsson, 2001), then converted to apparent solubility in seawater using the activity coefficient at <i>in situ</i> temperature and salinity (Pierrot and Millero, 2017). (2) Dissolution rate at near neutral condition is from (Heřmanská et al., 2022).   |
| <b>Chlorite</b><br>$\text{Mg}_3\text{Fe}_2\text{Al}_2\text{Si}_3\text{O}_{10}(\text{OH})_8 + 16\text{H}^+ = 2\text{Fe}^{2+} + 3\text{H}_4\text{SiO}_4 + 2\text{Al}^{3+} + 6\text{H}_2\text{O} + 3\text{Mg}^{2+}$   | 72.92              | -13.15                                  | 7   | (1) Solubility at <i>in situ</i> temperature is from the LLNL database (Delany and Lundein, 1991), then converted to apparent solubility in seawater using the activity coefficient at <i>in situ</i> temperature and salinity (Pierrot and Millero, 2017). (2) Dissolution rate at near neutral condition is from (Smith and Carroll, 2016).  |
| <b>Illite</b><br>$\text{K}_{0.85}\text{Al}_{2.85}\text{Si}_{3.15}\text{O}_{10}(\text{OH})_2 + 9.4\text{H}^+ + 0.6\text{H}_2\text{O} = 0.85\text{K}^+ + 2.85\text{Al}^{3+} + 3.15\text{H}_4\text{SiO}_4$  | 18.64              | -19.00                                  | 55  | (1) Solubility at <i>in situ</i> temperature is from the Thermochimie database (Marty et al., 2015), then converted to apparent solubility in seawater using the activity coefficient at <i>in situ</i> temperature and salinity (Pierrot and Millero, 2017). (2) Precipitation rate is tested in the main text.   |

<sup>1</sup>Surface areas for primary silicates and authigenic clay are assumed to be 7 and 55 m<sup>2</sup>/g respectively following previous studies of marine sediments (Maher et al., 2006).

**Supplementary Table 7. Metal speciation**

| Equation   | logK <sup>1</sup> | Sources                     |
|--|-------------------|-----------------------------|
| Fe{2+} + OH{-} = Fe(OH){+}                       | 3.68              | (Pierrot and Millero, 2017) |
| Fe{2+} + 2*OH{-} = Fe(OH)[2]                     | 5.68              | (Pierrot and Millero, 2017) |
| Fe{2+} + HCO3{-} = FeHCO3{+}                     | 0.58              | (Pierrot and Millero, 2017) |
| Fe{2+} + CO3{2-} = FeCO3 <sup>0</sup>            | 2.98              | (Pierrot and Millero, 2017) |
| Fe{2+} + 2*CO3{2-} = Fe(CO3)[2]{2-}              | 4.62              | (Pierrot and Millero, 2017) |
| Fe{2+} + SO4{2-} = FeSO4 <sup>0</sup>            | 0.82              | (Pierrot and Millero, 2017) |
| Fe{2+} + Cl{-} = FeCl{+}                         | -0.26             | (Pierrot and Millero, 2017) |
| Fe{2+} + HS{-} = FeS <sup>0</sup> + H{+}         | -2.82             | (Rickard, 2006)             |
| Al{3+} + H2O = Al(OH){2+} + H{+}                 | -5.63             | (Brown and Ekberg, 2016)    |
| Al{3+} + 2*H2O = Al(OH)[2]{+} + 2*H{+}           | -12.74            | (Brown and Ekberg, 2016)    |
| Al{3+} + 3*H2O = Al(OH)[3] <sup>0</sup> + 3*H{+} | -18.23            | (Brown and Ekberg, 2016)    |
| Al{3+} + 4*H2O = Al(OH)[4]{-} + 4*H{+}           | -25.85            | (Brown and Ekberg, 2016)    |
| Nd{3+} + CO3{2-} = NdCO3{+}                      | 5.46              | (Schijf and Byrne, 2021)    |
| Nd{3+} + 2*CO3{2-} = Nd(CO3)[2]{-}               | 9.56              | (Schijf and Byrne, 2021)    |
| Nd{3+} + HCO3{-} = NdHCO3{2+}                    | 0.87              | (Schijf and Byrne, 2021)    |
| Nd{3+} + Cl{-} = NdCl{2+}                        | -0.46             | (Schijf and Byrne, 2021)    |
| Nd{3+} + SO4{2-} = NdSO4{+}                      | 1.75              | (Schijf and Byrne, 2021)    |
| Nd{3+} + H2O = NdOH{2+} + H{+}                   | -9.02             | (Schijf and Byrne, 2021)    |
| Nd{3+} + H3SiO4{-} = NdH3SiO4{2+}                | 5.20              | (Schijf and Byrne, 2021)    |
| Nd{3+} + 2*H3SiO4{-} = Nd(H3SiO4)[2]{+}          | 10.80             | (Schijf and Byrne, 2021)    |

<sup>1</sup>Apparent stability constants, either measured at ionic strength of 0.7, or corrected to salinity of 35 using the activity coefficients from (Pierrot and Millero, 2017). We made further corrections to *in situ* temperature (2°C) and pressure (300 bar) whenever possible, otherwise we use the values at the standard state (25°C and 1 bar).

**Supplementary Table 8. Acid dissociation**

| <b>Equation</b>   | <b>logK<sup>1</sup></b> |
|---|-------------------------|
| $\text{H}_4\text{SiO}_4 = \text{H}_3\text{SiO}_4\{-\} + \text{H}\{+\}$                    | -9.72                   |
| $\text{H}_3\text{PO}_4 = \text{H}_2\text{PO}_4\{-\} + \text{H}\{+\}$                      | -1.59                   |
| $\text{H}_2\text{PO}_4\{-\} = \text{HPO}_4\{2-\} + \text{H}\{+\}$                         | -6.11                   |
| $\text{HPO}_4\{2-\} = \text{PO}_4\{3-\} + \text{H}\{+\}$                                  | -9.26                   |
| $\text{CO}_2 + \text{H}_2\text{O} = \text{HCO}_3\{-\} + \text{H}\{+\}$                    | -6.01                   |
| $\text{HCO}_3\{-\} = \text{CO}_3\{2-\} + \text{H}\{+\}$                                   | -9.32                   |
| $\text{H}_2\text{S} = \text{HS}\{-\} + \text{H}\{+\}$                                     | -6.11                   |
| $\text{B}(\text{OH})_3 + \text{H}_2\text{O} + \text{B}(\text{OH})_4\{-\} + \text{H}\{+\}$ | -8.78                   |
| $\text{H}_2\text{O} = \text{OH}\{-\} + \text{H}\{+\}$                                     | -14.13                  |

<sup>1</sup>Computed at *in situ* temperature (2°C), pressure (300 bar) and salinity (35) (Gattuso et al., 2016).

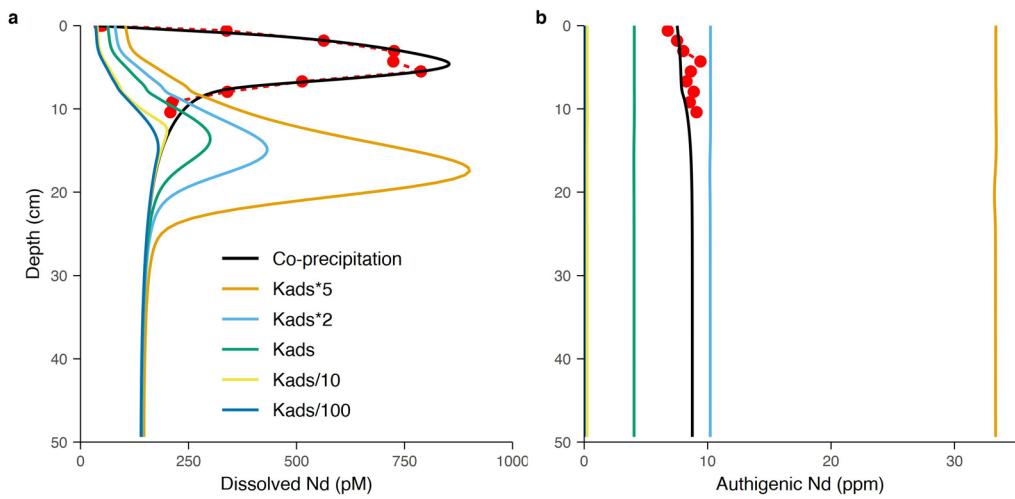
**Supplementary Table 9. Boundary conditions<sup>1</sup>**

| Variable | Type          | Value    | Unit                                   |
|----------|---------------|----------|--|
| POC      | Incoming flux | 2.7E-3   | mmol cm <sup>-2</sup> yr <sup>-1</sup> |
| MnO2     | Incoming flux | 3.5E-4   | mmol cm <sup>-2</sup> yr <sup>-1</sup> |
| FeOOH    | Incoming flux | 1.1E-4   | mmol cm <sup>-2</sup> yr <sup>-1</sup> |
| FeS      | Incoming flux | 0        | mmol cm <sup>-2</sup> yr <sup>-1</sup> |
| FeS2     | Incoming flux | 0        | mmol cm <sup>-2</sup> yr <sup>-1</sup> |
| CaCO3    | Incoming flux | 1.01E-2  | mmol cm <sup>-2</sup> yr <sup>-1</sup> |
| BSi      | Incoming flux | 3.23E-2  | mmol cm <sup>-2</sup> yr <sup>-1</sup> |
| Ca       | Bottom water  | 1.03E-02 | mmol cm <sup>-3</sup>                  |
| SO4      | Bottom water  | 2.80E-02 | mmol cm <sup>-3</sup>                  |
| TH3BO3   | Bottom water  | 8.71E-05 | mmol cm <sup>-3</sup>                  |
| Mn       | Bottom water  | 5.00E-10 | mmol cm <sup>-3</sup>                  |
| Fe       | Bottom water  | 5.00E-10 | mmol cm <sup>-3</sup>                  |
| Al       | Bottom water  | 5.00E-10 | mmol cm <sup>-3</sup>                  |
| CH4      | Bottom water  | 0        | mmol cm <sup>-3</sup>                  |
| O2       | Bottom water  | 8.00E-05 | mmol cm <sup>-3</sup>                  |
| NO3      | Bottom water  | 4.00E-05 | mmol cm <sup>-3</sup>                  |
| NO2      | Bottom water  | 5.00E-08 | mmol cm <sup>-3</sup>                  |
| NH4      | Bottom water  | 0.00E+00 | mmol cm <sup>-3</sup>                  |
| TH3PO4   | Bottom water  | 2.80E-06 | mmol cm <sup>-3</sup>                  |
| TH4SiO4  | Bottom water  | 1.90E-04 | mmol cm <sup>-3</sup>                  |
| pH       | Bottom water  | 7.7      | free H scale                           |
| TCO2     | Bottom water  | 2.38E-03 | mmol cm <sup>-3</sup>                  |
| TH2S     | Bottom water  | 0.00E+00 | mmol cm <sup>-3</sup>                  |
| Age      |               | 0        | yr                                     |

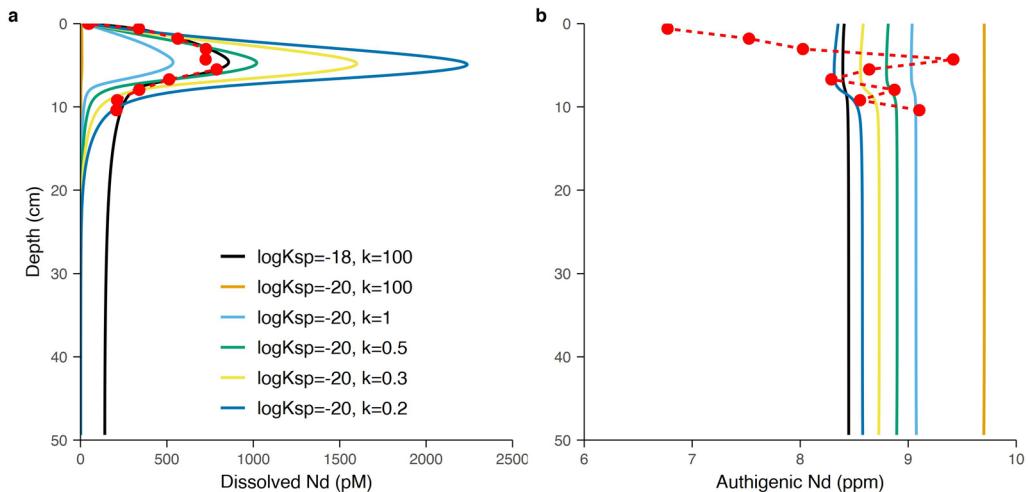
<sup>1</sup>Boundary conditions at the sediment-water interface. For solid materials, we specify the incoming flux. For dissolved species, we specify the bottom water concentration. Boundary conditions at L=50 cm are no-flux conditions for all species, except for Age, which

is  $\frac{\partial \text{Age}}{\partial z}|_{z=L} = 1/u_s^L$ .

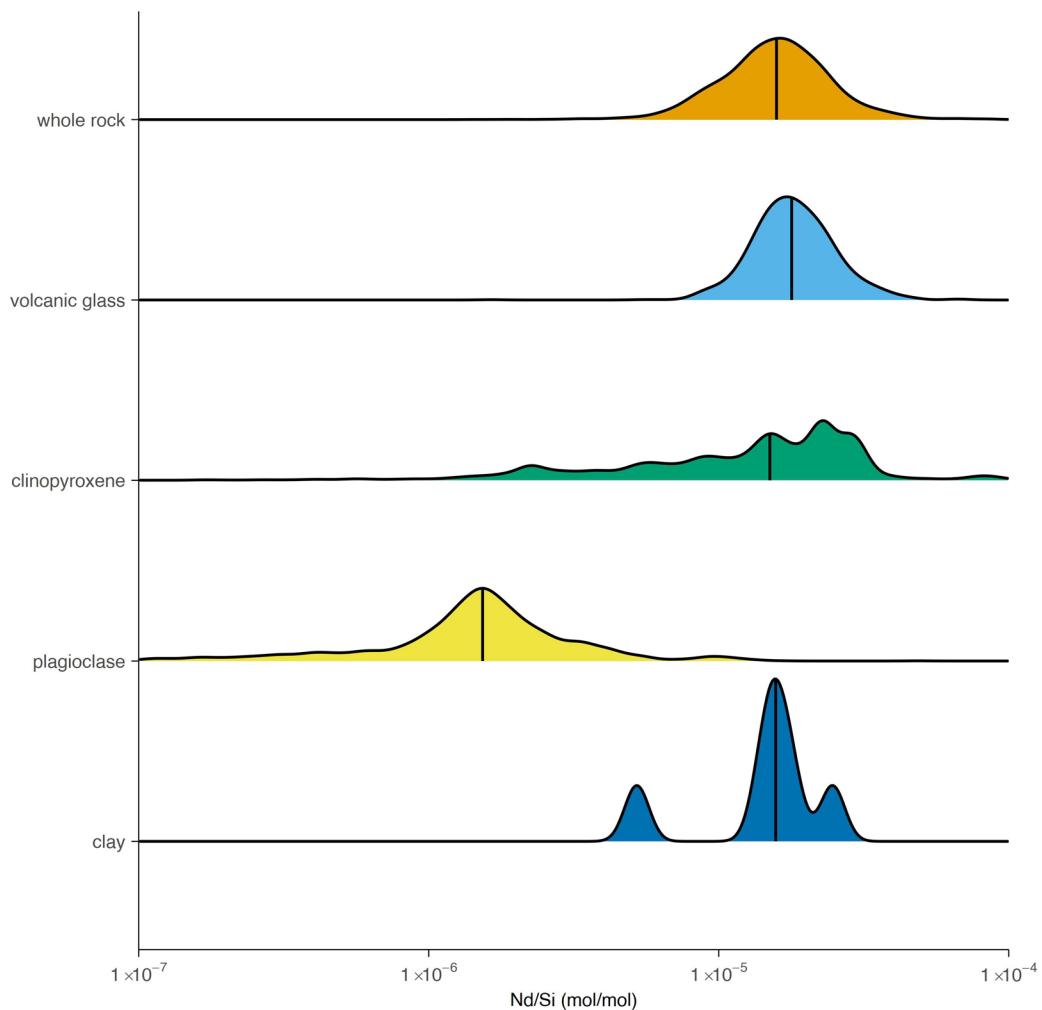
## Supplementary Figures



**Supplementary Fig. 1. Model sensitivity to adsorption constants in the reversible scavenging formulation of Nd cycling with Fe/Mn oxides.** The adsorption constants for both  $\text{MnO}_2$  and  $\text{FeOOH}$  are varied from 5 times (“Kads\*5”) to 1/100 (“Kads/100”) of the values (“Kads”) used in the main text in Fig. 4. The results are compared with the co-precipitation formulation and the observations (red dots). The results show that the reversible scavenging formulation cannot capture the depth of the peak dissolved Nd concentration in pore water (**a**). With lower adsorption constants, less Nd is carried by oxides into the sediments, leading to lower pore water (**a**) and authigenic Nd concentrations (**b**).



**Supplementary Fig. 2. Model sensitivity to the solubility and precipitation rate of NdPO<sub>4</sub>.** The parameters chosen in the main text in Fig. 3 are logK<sub>sp</sub> = -18 and k = 100 pmol/cm<sup>3</sup>/yr. In the sensitivity tests we reduce the solubility to logK<sub>sp</sub> = -20 while decreasing the precipitation rate from 100 to 0.2 pmol/cm<sup>3</sup>/yr. With lower solubility, the peak concentration can be captured if reducing the precipitation rate (**a**). However, the resulting peak shapes are narrower than the data suggest. The increase of Nd concentration with depth is delayed close to the sediment water interface, while the decrease of Nd concentration beneath the peak is more abrupt. The best constraint on the parameters would be Nd concentration beneath 20 cm, which would directly reflect the equilibrium concentration with respect to NdPO<sub>4</sub>, but is unfortunately unavailable. Overall, the fit to the data is worse than using higher solubility (logK<sub>sp</sub> = -18). Modeled authigenic Nd concentration is not as sensitive considering the data scatter (**b**).



**Supplementary Fig. 3. The molar Nd/Si ratio in silicate phases.** Data are plotted as probability density graphs (arbitrary y-scale), and the vertical lines indicate median values. Data of whole rock, volcanic glass, clinopyroxene and plagioclase come from the GEOROC database. The whole rock data include all volcanic rock samples from the Cascade Arc. The volcanic glass data are also from the Cascade Arc. The clinopyroxene and plagioclase data are from other convergent margins in the database since no data from the Cascade Arc is found. Clay data are from the global river sediment REE compilation of Bayon et al., (2015), and include the clay data from rivers draining volcanic terrains.

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