

### Rheology of Marine Sponges Reveals Anisotropic Mechanics and Tuned Dynamics

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Sponges are animals that inhabit many aquatic environments while filtering small particles and ejecting metabolic wastes. They are composed of cells in a bulk extracellular matrix, often with an embedded scaffolding of stiff, siliceous spicules. We hypothesize that the mechanical response of this heterogeneous tissue to hydrodynamic flow influences cell proliferation in a manner that generates the body of a sponge. Toward a more complete picture of the emergence of sponge morphology, we dissected a set of species and subjected disks of living tissue to physiological shear and uniaxial deformations on a rheometer. Various species exhibited rheological properties such as anisotropic elasticity, shear softening and compression stiffening, negative normal stress, and non-monotonic dissipation as a function of both shear strain and frequency. Erect sponges possessed aligned, spicule-reinforced fibers which endowed three times greater stiffness axially compared with orthogonally. By contrast, tissue taken from shorter sponges was more isotropic but time-dependent, suggesting higher flow sensitivity in these compared with erect forms. We explore ecological and physiological implications of our results and speculate about flow-induced mechanical signaling in sponge cells.

Keywords: rheology, marine sponges, tissue mechanics, anisotropic elasticity, auxeticity, nonlinear viscoelasticity

## 1 2 3 I. INTRODUCTION 4 5

6 Sponges, animals that branched near the root of the metazoan tree [1, 2], are a successful  
7 and unique phylum despite perceived simplicity since they have no muscles nor nerves [3, 4].  
8 The extracellular part of their bodies is a highly efficient fluid transport system made of  
9 diverse collagen-like proteins (spongins) and stiff organomineral inclusions called spicules  
10 [5]. Inner chambers of sponge tissue are lined with flagellated collar cells whose waving  
11 flagella draw ambient water in through small surface pores (ostia) on the sponge body. The  
12 water travels through narrowing canals, is filtered of dissolved nutrients, and then leaves  
13 through widening canals until exiting from larger, apical holes (oscula). Famously, sponges  
14 vary vastly in size and shape, appearing in almost all aquatic niches and flow regimes as  
15 globs, cups, vases, carpets, fans, barrels, spheres, fingers, and tall trees. How they grow and  
16 sustain bodies presumably optimized for transport of matter in these various niches is not  
17 fully understood, thus physical characterization of their tissue is necessary.  
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20 Like snowflakes, no two sponges are exactly alike, and this dizzying diversity likely arises  
21 from interactions among an individual's tissue mechanical properties, the hydrodynamics  
22 of its environment, and mechanical signaling of its cells. Early spongiologists knew that  
23 sponges of smaller diameter piping generate larger pump pressures which send filtered water  
24 further [6]. This lowers the probability of water recirculation but increases the frictional  
25 cost of transport through the sponge [7]. G.P. Bidder in particular<sup>1</sup> documented that thin-  
26 tissued, deep-sea glass varieties of sponge ~~would~~ have lower internal pressure than their  
27 denser, shallow-water cousins [6, 7]. The tissue elasticity of these dense sponges counteracts  
28 ambient pressure and flow-induced stresses in mechanical equilibrium. However, no explicit  
29 measure of these elastic properties across sponge groups has yet been made.  
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32 An ecological study of the encrusting sponge *H. panicea*, placed its tissue stiffness (elas-  
33 ticity) between 200 and 600 kPa, and proportional to wave-induced stresses up to 10 kPa [8].  
34 Steady, flow-induced forces like drag and lift<sup>2</sup> impart highly morphology-dependent stresses  
35 on the bodies of sessile aquatic animals. However, sponges of different body forms are often  
36 found next to each other (Fig. S3), such that there isn't a simple form vs. ambient flow  
37 relationship in these animals. Tissue mechanical properties then, must also be tuned by  
38 evolution and development in specific sponges. Other invertebrates with fixed body forms  
39 and static mechanical properties such as mussels, urchins, and limpets, have a strict upper  
40 limit to their mechanical properties. Sponges, on the other hand, have a much more  
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3 limit on their size in fast and accelerating (i.e. time-dependent) flows [9]. It is less clear  
4 what mechanical constraints apply to sponges, given their asymmetrical body plan and lack  
5 of internal organs, or whether there are aspects of sponge tissue that enable mechanical  
6 responsiveness to environmental flow.  
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10 Monactine sponge spicules are known to have extreme resistance to buckling failure under  
11 compression [10], but it is not understood how their arrangement within a cellular and fibrous  
12 protein network contributes to the mechanical whole of sponge tissue. Gelatin hydrogels  
13 embedded with spicules have stiffnesses proportional to the volume fraction of these stiff  
14 inclusions, as well as strain-softening dynamics [11], but did not contain sponge cells capable  
15 of creating internal strain or otherwise affecting tissue rheology.  
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18 We thus take a holistic approach by performing rheology on living tissue from several  
19 common sponge species. We applied small to moderate strains over a frequency range salient  
20 to the properties of environmental flows and stresses. The mechanical and dynamical (i.e.  
21 time-dependent) properties of sponge tissue measured in this way correlate to their growth  
22 morphologies and skeletal structures. We speculate that the stiff skeleton and its coupling  
23 to living sponge cells, generates mechanical cues that in turn influence cell proliferation, just  
24 as extracellular matrix mechanics modulate many cell physiological processes in mammalian  
25 tissues [12, 13]. The sponge rheologies presented showcase tissue mechanical diversity, and  
26 in some species, rich nonlinear viscoelasticity at relatively small strains compared with *in*  
27 *vitro* and mammalian systems.  
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## 41 II. MATERIALS & METHODS

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#### 43 A. Animal Care & Sample Preparation

44 Sponges were procured from Gulf Specimen Marine Laboratories (Panacea, FL) and  
45 acclimated slowly by drip to a large, 1-m depth (ESM 4) laboratory saltwater aquarium  
46 ( $T = 20$  degrees C, salinity 36 g/kg). We chose individuals with open oscula and bright  
47 tissue for preparing samples, as these characteristics indicate good health. All sponges were  
48 used within a span of several weeks and any exposure to air was minimized. We used a  
49 kitchen sponge (Medium Duty, Scotch-Brite) to determine whether living sponge rheology  
50 was distinct from that of a synthetic porous material. For branching and erect species of  
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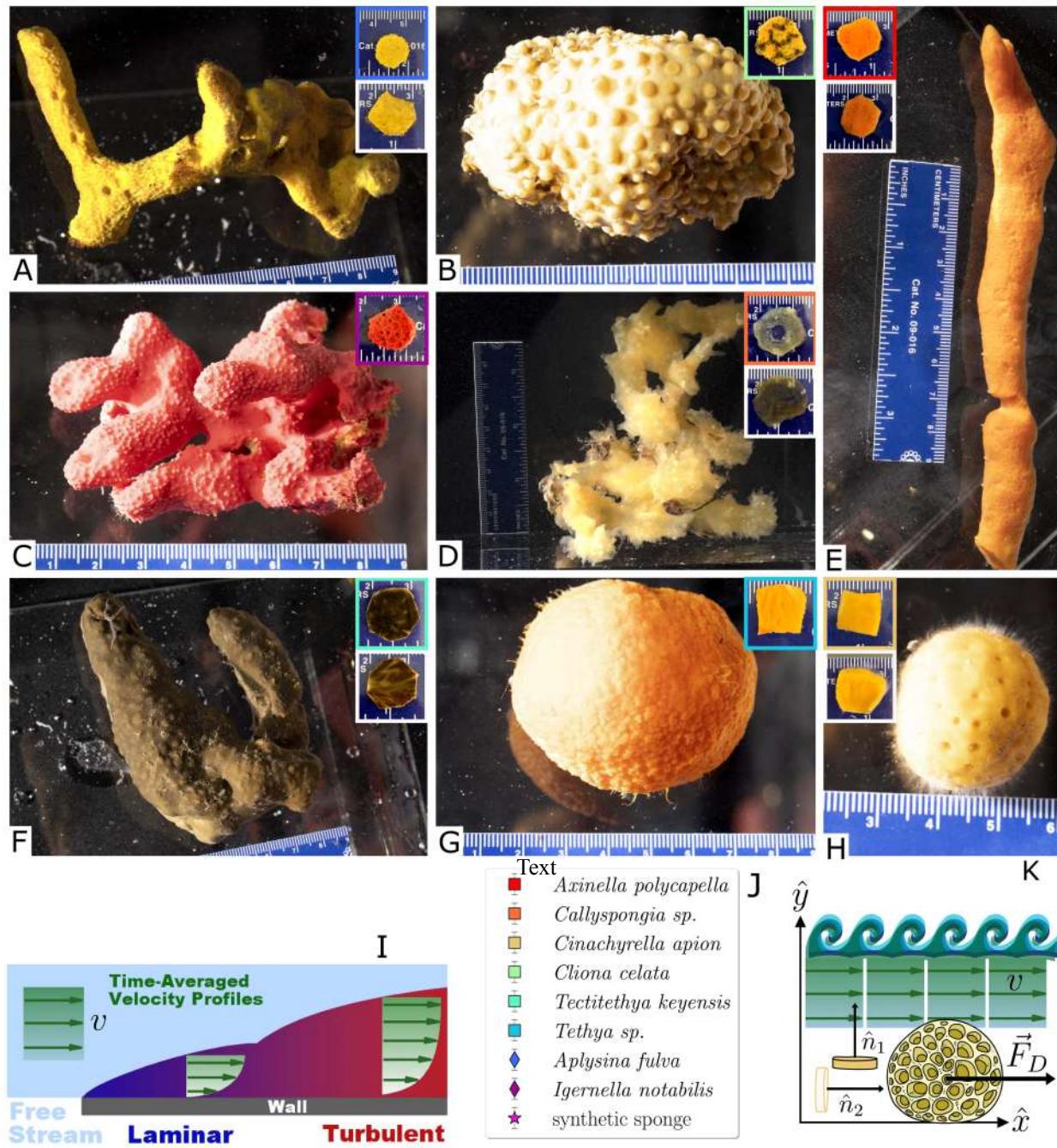


FIG. 1. Sponges studied. A) *A. fulva* B) *C. celata* (gamma growth form [14]) C) *I. notabilis* D) *Callyspongia* sp. E) *A. polycapella* F) *T. keyensis* G) *Tethya* sp. H) *C. apion*. Images of representative sample disks for rheology are inset. I) Diagram (courtesy of Symscape) of ambient flows: steady flow  $v$  (left) and boundary layer flow (right). J) Key of sponges: squares have spicules, diamonds do not. K) Schematic of sampling geometry in relation to  $v$  and subsequent drag  $\vec{F}_D$  on an example sponge.  $\hat{z}$  points into the page.

Usually you can't put citations in figure legends. It is also not clear what "courtesy of Symscape" means. Can you just redraw a simpler version of this in Illustrator to avoid the slight cheesiness of re-using a random internet gif? Also, the stuff in the caption for panel I doesn't really match what's in the image.

sponge, tissue cuts parallel to their substrate attachment area were made with a razor blade, resulting in disks of thickness 2–4 mm with axial vectors  $\hat{n}_1$  parallel to  $\hat{y}$  and perpendicular to ambient flow  $v$  as depicted in Fig. 1K. We also made cuts perpendicular to the substrate, so that these disks' axial vectors  $\hat{n}_2$ , were oriented along  $\hat{x}$ . In species where consistent samples could not be obtained in the above fashion due to tissue being too heterogeneous (*C. celata*), compressible (*I. notabilis*), or brittle (pith of *Tethya sp.*), a biopsy device was used to punch 12–14 mm diameter cylindrical cores which were then sliced into disks of thickness 2–4 mm. Disks from different cores were thus distinctly oriented at random with respect to ambient flow  $v$ , so we denote their axial vectors  $\hat{n}_{\square}$ ,  $\hat{n}_{\square}$ , and  $\hat{n}_{\square}$ .

Sponges can be difficult to identify to species, and our experimental animals were obtained from a commercial supply source. All species sampled here were demosponges, and species identifications are provided to the best of our ability in working with this supply resource. In this instance, photographs of the individuals used and their spicules are included, and are the best information we have about exact species identity. Ultimately, the magnitude and quality of the differences between individuals and species are the most salient part of the present work.

## B. Rheology

We mounted disks of live sponge tissue between parallel plates (12 mm diameter) on a rheometer (MCR 502 WESP, Anton Paar GmbH). A small amount of cyanoacrylate adhesive (Gorilla Super Glue Gel 7700104) was applied to both sides of the sample to maintain contact between it and the rheometer plates during deformation. We initialized contact with the plates by exerting a uniaxial stress  $\sigma_N \sim 10$  kPa, and the sample was then immediately rewetted with 1 mL of artificial seawater (Fig. 2A). We did not observe the living tissue react or degrade with the glue application, and the resulting film formed could be peeled off intact after the experiments. Therefore, the use of this adhesive does not seem to have altered any internal properties of the sponge tissue.

After relaxation of the loading stress, we applied sinusoidal shear strain

$$\gamma(t) = \gamma_0 \sin(\omega t) \quad (1)$$

where  $\gamma_0$  is the strain amplitude and  $\omega$  is the angular frequency (speed) of oscillation (Fig. 2B). For small  $\gamma_0$ , such that stress outputs are proportional to strain inputs, the shear

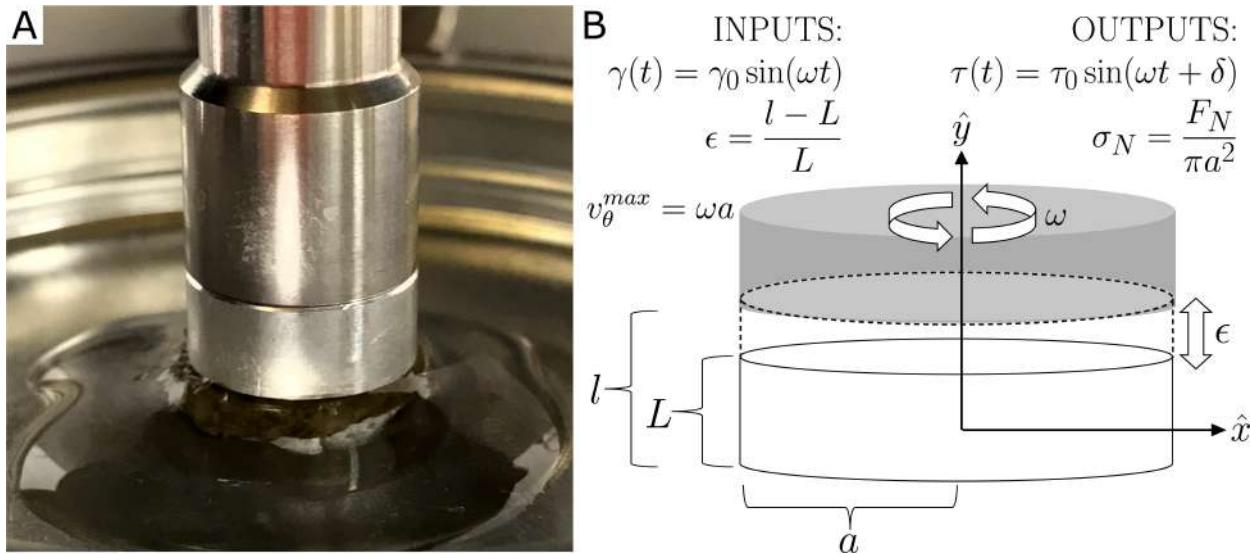


FIG. 2. Rheometry schematic. A) sample in the rheometer. B) parallel-plate geometry (radius  $a = 0.6$  cm), used to impose oscillatory shear  $\gamma(t)$  and uniaxial strain  $\epsilon$ .

stress in the sample  $\tau(t)$  is a single sinusoid shifted by an amount  $\delta$

$$\tau(t) = \tau_0 \sin(\omega t + \delta) \quad (2)$$

where  $\tau_0$  is the shear stress amplitude. The dynamic storage and loss moduli,  $G'(\omega)$  and  $G''(\omega)$ , quantify elastically stored and viscously dissipated energy due to oscillatory shear and describe a sample's viscoelastic response in the linear regime. We measured  $G'(\omega)$ ,  $G''(\omega)$ , and their ratio  $\tan \delta = G''/G'$  at twelve logarithmically spaced frequencies between  $0.1\pi$  and  $10\pi$  s $^{-1}$  at  $\gamma_0 = 0.05\%$ . Ambient, free-stream flow  $v$  (Fig. 1I) in marine intertidal and subtidal environments where sponges are common typically ranges from 0.1 to 100 cm s $^{-1}$  [8, 9]. Since the maximum speed  $v_\theta$  of a disk-shaped sample subject to torsion is  $v_\theta^{max} = \omega a$  [15] where  $a$  is the disk radius, we chose these frequencies  $\omega$  as they correspond to environmentally-relevant flow speeds between 0.2 and 20 cm s $^{-1}$ .

We interpreted the linear viscoelasticity of sponge tissue, as characterized by our frequency sweep data, using rheological circuit models. We considered the classical Maxwell, Kelvin-Voigt, and Zener models, as well as a model with a fractional-order derivative element known as a spring-pot [16]. This fractional calculus-based model was formulated to capture precisely, and without overfitting, the power-law viscoelasticity commonly seen in biological materials [16]. Fits were performed with the Julia (v1.5.3) package RHEOS, developed for robust optimization of linear viscoelastic data [17].

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3 After a frequency sweep, we subjected samples to steady uniaxial strain or large-  
4 amplitude oscillatory shear (LAOS). We conducted LAOS on a subset of species by in-  
5 creasing shear strain,  $\gamma_0$ , in twelve logarithmic increments from 0.1 to 10% at  $\omega = 4\pi \text{ s}^{-1}$ . To  
6 check for any pre-conditioning effects, we repeated this LAOS protocol after ten minutes of  
7 rest. We were unable to probe above  $\gamma_0 = 10\%$  in *A. polycapella* and *C. celata* and  $\gamma_0 = 20\%$   
8 in *Callyspongia* sp., since the glue typically separated from the rheometer plates prior to any  
9 visible sample failure. Sponges in nature are not regularly observed to deform in ambient  
10 flow, so we considered  $\gamma_0 = 20\%$  a reasonable value to qualitatively capture strains that are  
11 not readily perceptible, and above which, strains are unlikely to be physiological.  
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14 Within the nonlinear viscoelastic regime probed by LAOS experiments, higher harmonics  
15 of the driving (fundamental) frequency are excited in a material's mechanical response. In  
16 other words, the stress output in the sample  $\tau(t)$  is no longer a single sinusoid shifted in  
17 time from the input strain  $\gamma(t)$  but can be represented as a Fourier series taken over odd-  
18 integer harmonics  $n$  due to the odd symmetry of shearing :

$$\tau(t) = \gamma_0 \sum_{n:odd} \left( G'_n(\omega, \gamma_0) \sin n\omega t + G''_n(\omega, \gamma_0) \cos n\omega t \right) \quad (3)$$

29 Here,  
30 where  $G'_n(\omega, \gamma_0)$  and  $G''_n(\omega, \gamma_0)$  become  
31 a set of trigonometric Fourier coefficients. Material  
32 measures may also be extracted from parametric plots of  $\tau(t)$  vs.  $\gamma(t)$ , or elastic Lissajous-  
33 Bowditch (L-B) curves [18]. For amplitudes  $\gamma_0$  within the linear regime, L-B curves are  
34 ellipses and  $G'(\omega)$  and  $G''(\omega)$  are proportional to the semi-major and semi-minor axes [19].  
35 In the nonlinear regime, L-B curves become bent shapes whose axes are no longer constant  
36 with respect to  $\gamma(t)$ . This distortion of L-B curves is a geometrical signal that the linear  
37 moduli  $G'(\omega)$  and  $G''(\omega)$  are insufficient to describe a sample's viscoelastic nonlinearities  
38 [18].  
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41 Here, we analyze the nonlinear  $\tau(t)$  signal in sponges with the minimum strain  $G'_M(\gamma_0)$   
42 and maximum strain  $G'_L(\gamma_0)$  elastic moduli because together they describe an L-B curve's  
43 overall concavity and moreover, are analytically related to  $G'_n(\omega, \gamma_0)$  (Eqn. S5) [18, 19, 20].  
44 We compare  $G'_M(\gamma_0)$  and  $G'_L(\gamma_0)$  to each other at every  $\gamma_0$  (using the intracycle stiffening  
45 index  $S$  [18]) and also consider each as a function of  $\gamma_0$ . We calculated these measures of  
46 elastic nonlinearity by fast Fourier transform (FFT) methods on the time-resolved strain  
47  $\gamma(t)$  and stress  $\tau(t)$  signals at each amplitude as described in Sec. V B.  
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50 Finally, on distinct samples not already subjected to LAOS, we applied steady uniaxial  
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$$\epsilon = \frac{l - L}{L} \quad (4)$$

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where  $l$  is the deformed height of the sample controlled by changes in the rheometer gap, initially at height  $L$ . Compression or extension was applied in seven linearly spaced steps between 0% and  $\pm 12\%$  ( $\epsilon < 0$  in compression and  $\epsilon > 0$  in extension). We calculated the uniaxial stress in a sample of radius  $a = 0.6$  as

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$$\sigma_N = \frac{F_N}{\pi a^2} \quad (5)$$

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where  $F_N$  is the rheometer reported normal force exerted on the top plate. We superposed an oscillatory shear of  $\gamma_0 = 0.05\%$  and  $\omega = \pi \text{ s}^{-1}$  to measure the shear storage modulus  $G'$  as a function of uniaxial strain  $\epsilon$ . Since  $\epsilon$  was constant within a step, we waited until  $\sigma_N$  and  $G'$  relaxed to apply the next 2% gap change, averaging the last four time points of both to compute values for each  $\epsilon$ . We calculated uniaxial moduli for distinctly oriented samples  $\hat{n}_1$  and  $\hat{n}_2$  in each species as the slope of linear fits to plots of uniaxial stress vs. uniaxial strain, and denoted them  $E_1$  and  $E_2$ . Comparing these as well as  $G'$  measured at  $\epsilon = 0$  for each orientation,  $(G'_0)_1$  and  $(G'_0)_2$ , allowed us to make general statements about mechanical symmetries in living sponges.35  
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### C. Dissection Microscopy

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After rheology, samples were removed from the rheometer, put back into artificial seawater, and allowed to rest. We blotted each of excess water, determined its wet mass  $m_w$ , and in between four layers of paper towel applied firm pressure ( $\sigma_N \sim 1 \text{ MPa}$ ), until water could no longer be drawn into fresh, layered paper towel. This method may not remove water bound tightly to protein, but provides an adequate estimate of the mass fraction of bulk water in the tissue  $\phi_w = \frac{m_w - m_d}{m_w}$  where  $m_d$  is the squeeze-dried mass of the disk.61  
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To characterize sponge skeletal architecture, we submerged individuals of each species in DI water, causing cells to osmotically burst, and agitated gently in several washes of additional DI water to remove remaining cellular debris. Some of the species left behind stiff, fibrous skeletons after washing, while others fully disintegrated in this treatment. Intact skeletons were dried in air before being sampled into disks of distinct orientations  $\hat{n}_1$  and  $\hat{n}_2$  as in Sec. II A. We imaged these with a USB microscope (Dino-Lite AM4113T) and a

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3 stereomicroscope (Nikon SMZ800). We used the ImageJ (v1.53e) plugin FibrilTool to check  
4 for structural anisotropy in the skeletons at this mesoscopic scale (0.001–10 cm). FibrilTool  
5 uses a local nematic order tensor as a measure of average fiber orientation, and thus quantifies  
6 fibrillar anisotropy within a region of interest (ROI) [21]. We drew three ROIs in each image  
7 to determine whether fiber orientation depended on its position within an image or overall  
8 tissue disk orientation.  
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11 To quantify spicule content in the sponges, we first made 5 mm-diameter tissue cores  
12 with a biopsy device. Thin (~2 mm) core slices were placed in individual wells of a 24-well  
13 culture plate with 1 mL of 6% bleach to dissolve all organic material including the protein  
14 skeleton while preserving any siliceous spicules (Fig. S6). After dissolution of tissue, the  
15 supernatant was removed with care to leave settled spicules undisturbed. We then washed  
16 the spicules three times with 1 mL of DI water, allowing them to settle before removing the  
17 wash fluid and rinsing a final time with 95% ethanol. A few drops of well-mixed solution  
18 were drawn into clean, large-bore pipettes and held vertically for about 30 seconds to allow  
19 sedimentation. A single drop (~0.05 mL) of this sedimented aliquot was then placed on a  
20 slide and examined by light microscopy. We used the multipoint tool in ImageJ to count  
21 all whole spicules in a field of view to estimate the number density of spicules in different  
22 species.  
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### 37 III. RESULTS

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#### 40 A. Mechanics

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43 These eight species (Fig. 1) span six orders within the largest sponge class (Demospon-  
44 giae) and display an array of growth forms [22, 23]. In five of them, *A. fulva*, *Callyspongia*  
45 *sp.*, *A. polycapella*, *T. keyensis*, and *C. apion* (Fig. 1A,D,E,F,H), we obtained samples per-  
46 pendicular  $\hat{n}_1$ , and parallel  $\hat{n}_2$ , to the assumed substrate and ambient, free-stream flow  $v$   
47 (Fig. 1I). Due to various features of their biology, the other three species (Fig. 1B,C,G)  
48 required a slightly different sampling strategy as follows. *C. celata* tissue was dense with  
49 embedded tracts of sand (Fig. S4C), which resulted in randomly oriented samples  $\hat{n}_{\blacksquare}$ ,  $\hat{n}_{\blacksquare}$ ,  
50 and so on. *I. notabilis* was comparatively homogeneous but soft and collapsible upon at-  
51 tempted slicing (Fig. S4D), so we used any mechanically stable and geometrically suitable  
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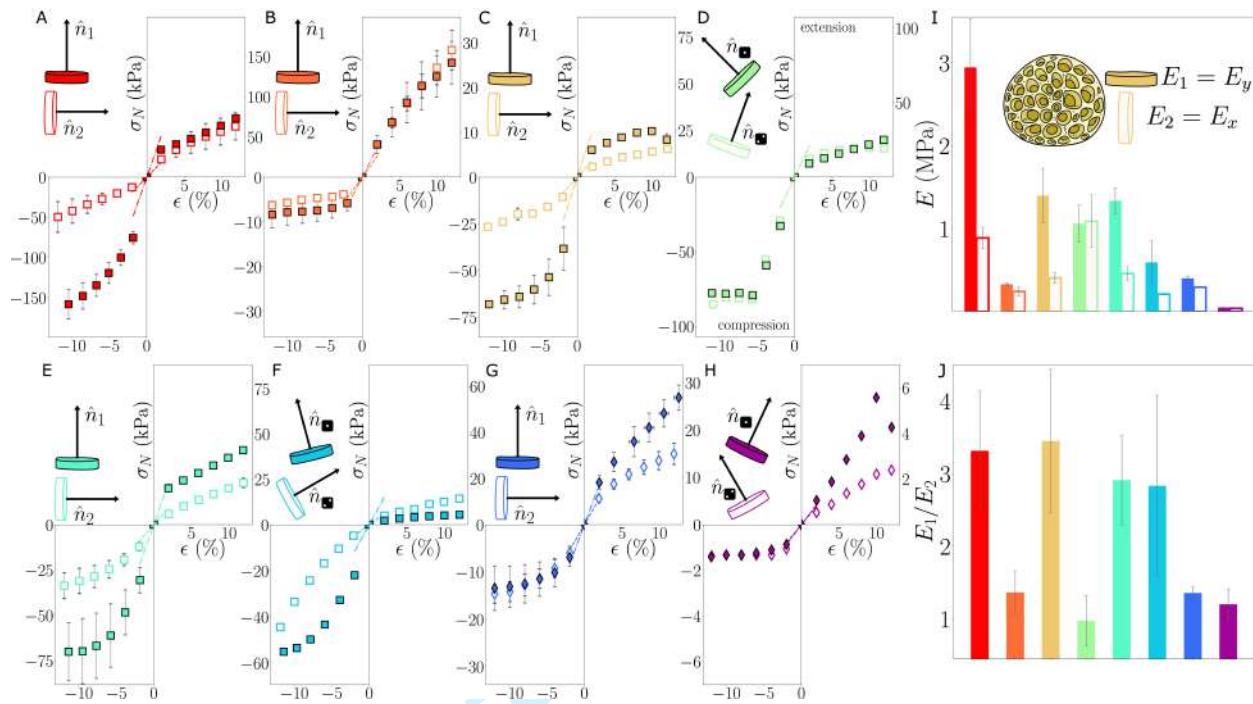


FIG. 3. Uniaxial stress-strain curves for distinct sample orientations  $\hat{n}_1$  and  $\hat{n}_2$  (filled and unfilled markers) in each sponge. Error bars are s.e. of  $N$  samples in A)-C), E), and G) while D), F), and H) have no error bars since in these species we compared pairwise, randomly oriented samples. I) Uniaxial modulus  $E$  in MPa J) Ratio of  $E$  measured along each direction,  $E_1/E_2$ .

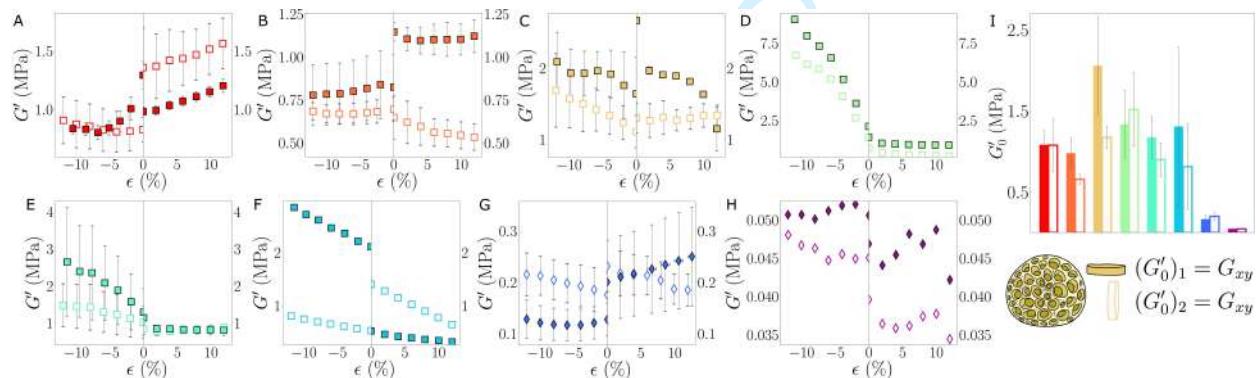


FIG. 4. Linear shear storage modulus  $G'$  vs. uniaxial strain  $\epsilon$ . I)  $G'$  at  $\epsilon = 0$ ,  $G'_0$ .

samples (Fig. 1C inset) while making note of distinct orientations. *Tethya* sp. had a stiff cortex that overloaded the rheometer's normal force transducer ( $F_N > 50$  N), barring us from rheology on the outer part of this sponge (Fig. S4A). Its pith was softer but brittle with long and flexible spicules, resulting in randomly oriented samples for *Tethya* sp.

Sampling geometries and uniaxial stress-strain curves in each species of sponge are shown

in Fig. 3A-H. We took slopes within the linear regime of each as an effective, uniaxial modulus  $E = \sigma_N/\epsilon$  (Fig. 3I). *A. polycapella*, *C. apion*, *T. keyensis*, and *Tethya sp.* uniaxial mechanics were highly dependent on sample orientation. Their tissue more strongly resisted compression along the  $\hat{n}_1$ , than along the  $\hat{n}_2$  direction. *C. celata* curves on the other hand, were independent of sample orientation but highly nonlinear, sharply plateauing in  $\sigma_N$  at  $\epsilon = -6\%$ . The ratio of uniaxial moduli measured along each direction,  $E_1/E_2$ , confirms the former sponges were about three times stiffer along  $\hat{n}_1$  compared with  $\hat{n}_2$  (Fig. 3J). By contrast,  $E$ 's for *Callyspongia sp.*, *A. fulva*, and *I. notabilis*, ~~were much less different along different directions ( $E_1/E_2 = 1.3$ )~~, a result suggesting the tissue of these three sponges contains at least one plane of isotropy. The  $E_1/E_2$  ratio in *C. celata* was equal to one, and therefore we conclude *C. celata* was the closest to isotropic of the sponges tested.

The shear storage modulus  $G'$  (measured at  $\omega = \pi \text{ s}^{-1}$  and  $\gamma_0 = 0.05\%$ ) as a function of uniaxial strain  $\epsilon$  is shown in Fig. 4. It increased with compression in *C. apion*, *C. celata*, *T. keyensis*, and *Tethya sp.*. Instead, in *A. polycapella*, *Callyspongia sp.*, *A. fulva*, and *I. notabilis*,  $G'$  stiffened modestly in compression, and only after initially softening. Reconstituted networks of collagen and fibrin have also been shown to compression soften, while whole tissues made of these biopolymers plus cells, compression stiffen [24]. We found that sponge tissue with living cells ~~does both~~ depending on the species. This suggests that the presence of deformable but volume-conserving cells [25], is not the biggest contributor to compression stiffening in sponges.

In Fig. 5, we compare sponge multiaxial mechanics with that of mammalian tissues.  $G'$  as a function of compressive stress  $|\sigma_N|$  in brain [26], liver [27], and adipose [28], is approximately linear,  $G'(\sigma_N) = m|\sigma_N| + G'_0$  with slopes  $m \leq 1$  [29]. The sponges compression stiffen linearly as well, but ~~had~~  $m \gg 1$ , with  $m$  highest in *C. celata* at about 60 (zoomed inset). *C. celata* also displayed a sharp discontinuity at  $\epsilon = -6\%$ , where  $m$  goes to infinity and  $G'$  increases to 9 MPa, more than four times its initial value at  $\epsilon = 0\%$ . By ~~complete~~ contrast, *A. polycapella*, *Callyspongia sp.*, and the spicule-less sponges, change their  $G'$  relatively little with  $|\sigma_N|$ , indicating low multiaxial responsivity.

In Fig. 5B, we normalize the change in  $G'$  by  $G'_0$ , and see that under the ~~significantly~~ smaller strains we applied ( $\epsilon = -12\%$  vs.  $\epsilon = -40\%$  in brain [26], for example), sponges overall accessed a larger scaled range of  $G'$  for every scaled increment of  $|\sigma_N|$ , ~~than did any of the mammalian tissues~~. The slope produced by this approximately linear scaling also

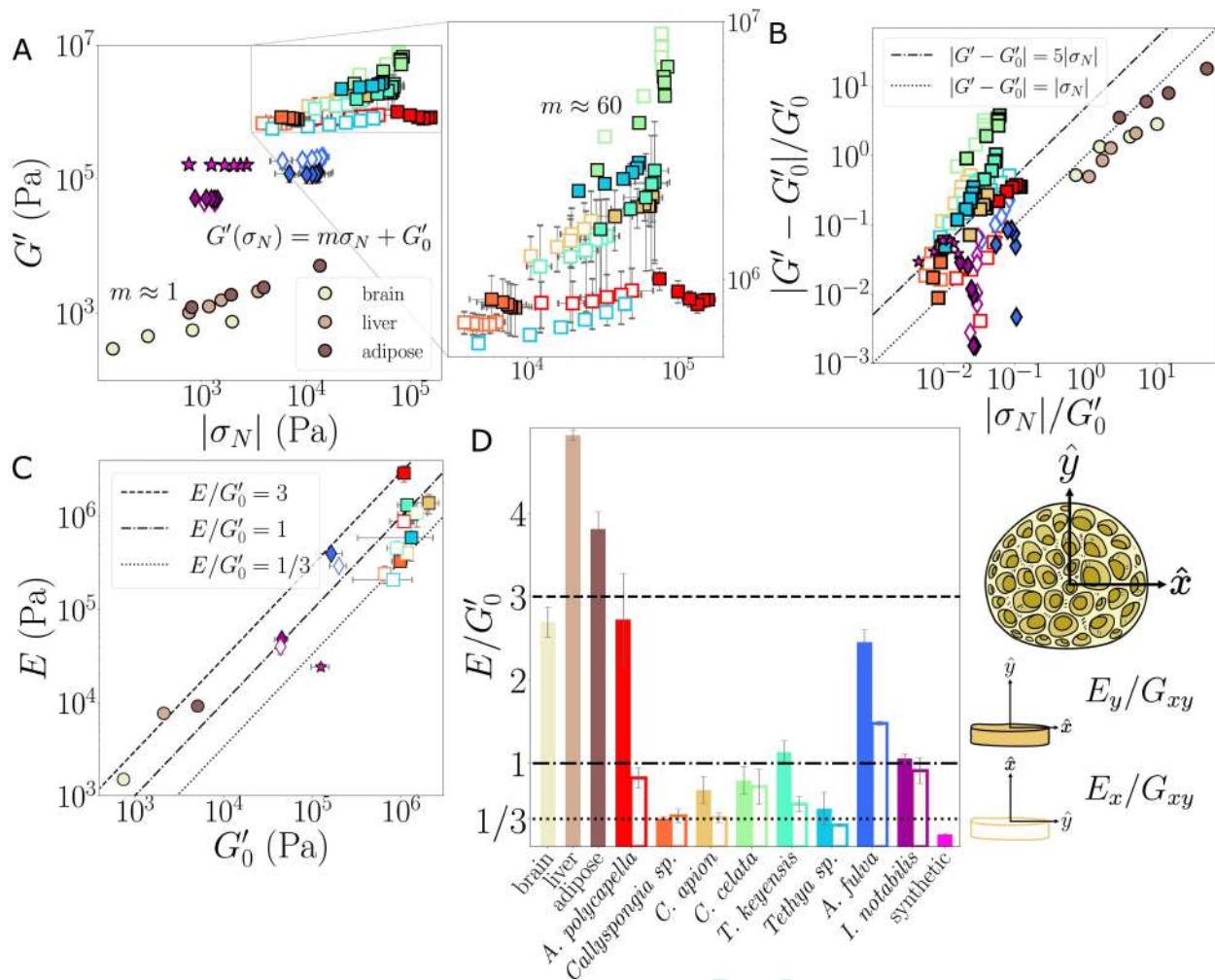


FIG. 5. A)  $G'$  vs. the magnitude of compressive stress  $|\sigma_N|$  in the sponges and mammalian brain, liver, and adipose tissue [26, 27, 28]. B) Change in magnitude of  $G'$  vs. corresponding change in  $|\sigma_N|$ , both normalized by  $G'_0$ . C)  $E$  vs.  $G'_0$  along each direction in the sponges and in the mammalian tissues. D)  $E/G'_0$  bar plot; the diagram adjacent depicts which uniaxial and shear moduli were measured in the rheometer based on the sampling geometry.

gives an estimate of the persistence length (bending rigidity [30, 31]) of the biopolymers underlying these living tissues. We found the mammalian tissues at a scaling of about one (dotted line), and the sponges varied from one ~~through~~ <sup>to</sup> five (a value typically used *in silico* and found in semi-flexible biopolymer gels ([31], dashed-dotted line) and upwards. This indicates a ~~comparatively large~~ range of bending rigidities in the sponges that make up the tissue of these species, given that larger slopes translate to smaller bending rigidities [31]. Overall, most of the sponges had larger slopes than one, and therefore spiculated sponges

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Is this sentence implying that spongins are stiffer locally, but also of higher molecular weight than mammalian collagens, leading to lower per-polymer bending rigidity? If so, say that directly, it is unclear here and potentially interesting.

are more flexible than mammalian collagens but locally quite stiff. Taken together, these results suggest that spiculated spongins may be semi-flexible polymers.

We compare  $E$  with  $G'_0$  in the sponges and mammalian tissues in Fig. 5C. Material constants in sponges would be most accurately determined from constitutive models that include dissipation both from fluid flow within the pore space [32] and viscoelastic flow (Sec. III B) of the solid constituents, the spiculated spongins. Here, the diversity in the measured linear elastic constants  $E$  and  $G'_0$  is sufficient for comparative biology among this set of sponges, and ~~vs.~~ <sup>to</sup> brain, liver, and adipose tissue. Interestingly,  $E$  was larger than  $G'_0$  in all of the mammalian tissues, while the opposite was true in most of the sponges (Fig. 5D). These data recapitulate that mammalian tissues are incompressible (like rubber, with Poisson's ratio  $\nu = 1/2$  [27]), while the sponges approach what is expected for extremely compressible materials,  $\nu = -1$  [33]. Negative values of  $\nu$  imply auxeticity, or the tendency to contract instead of bulge transversely when compressed, and 'spongy' materials like re-entrant polymer foams and many honeycomb structures are auxetic [34]. Through the usual constraints associated with the stress and strain tensors of linear elasticity (Sec. V A), we found  $\nu$  ~~take on~~ <sup>to occupy</sup> negative values in all of the sponges (Tab. S1), suggesting auxeticity is possible in Poriferan body tissue.

## B. Linear Viscoelasticity

The linear viscoelastic response of sponge tissue as a function of driving frequency  $\omega$  is shown in Fig. 6. The storage modulus  $G'(\omega)$  was an order of magnitude larger than the loss modulus  $G''(\omega)$  and spanned two orders of magnitude ( $10^4 - 10^6$  Pa) in these sponge species. Sponges with spicules (squares) were an order of magnitude stiffer than those without (diamonds).  $G'(\omega)$  followed a very weak power-law in all specimens, including the synthetic cellulose sponge, but interestingly,  $G''(\omega)$  also followed a frequency power-law for the synthetic sponge only, and was non-monotonic and disparate among living sponges (Fig. 6B).

The ratio of dissipated to stored energy in the tissue when sheared,  $\tan \delta$ , highlights these disparities (Fig. 6C). In *C. apion*, *C. celata*, *Tectitethya* sp., and *Tethya* sp.,  $\tan \delta$  decreases at low  $\omega$ , followed by a slow increase in some, or a plateau in others. *A. polycapella*, *Callyspongia* sp., and *I. notabilis* behave similarly, but  $\tan \delta$  takes values roughly four-fold

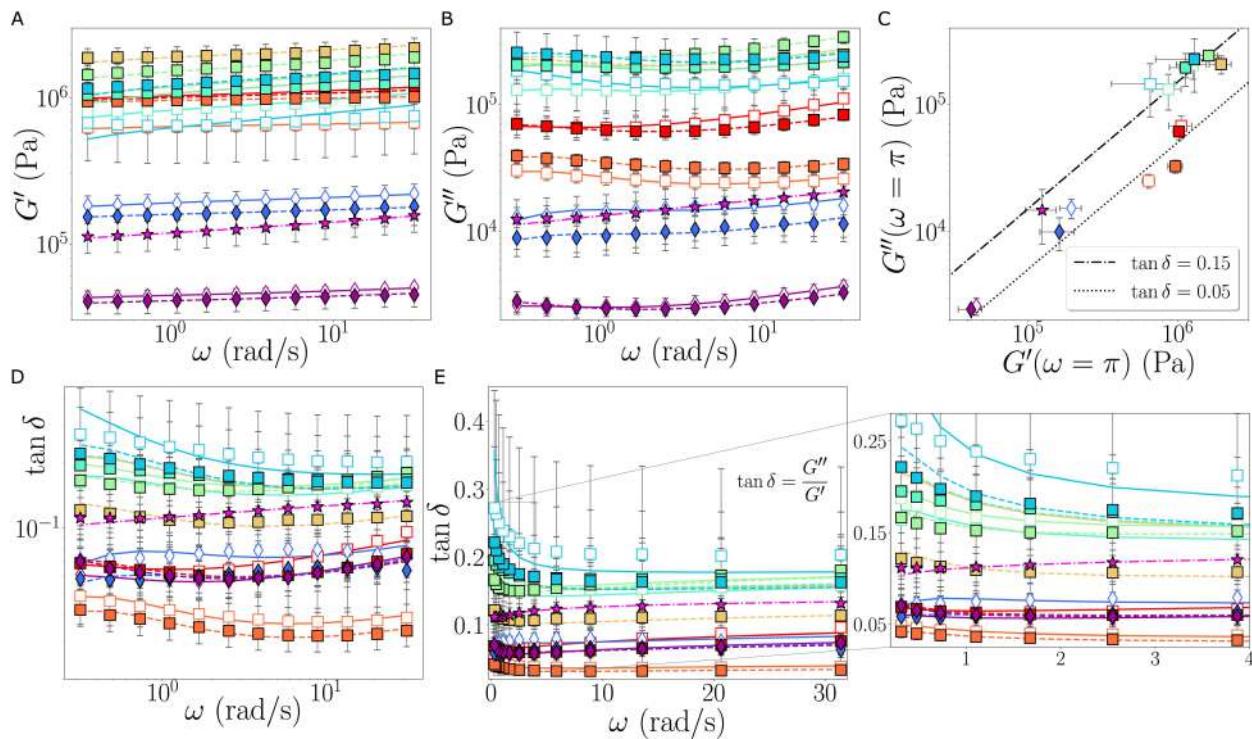


FIG. 6. Sponge tissue frequency sweeps at  $\gamma_0 = 0.05\%$ . A)  $G'(\omega)$  B)  $G''(\omega)$  C)  $G''$  vs.  $G'$  at  $\omega = \pi$  s $^{-1}$  D)  $\tan \delta$  vs.  $\omega$ , replotted on linear axes in E). Curves are fits of the fractional solid model [16] and error bars are mean  $\pm$  s.e. of  $N$  samples.

smaller (Fig. 6D). In other words, the first group of sponges dissipate four times as much energy when sheared compared to the second group, and many of the sponges had dissipation minima at specific frequencies (Fig. 6E).

None of the classical viscoelastic circuit models that we fit provided adequate descriptions of  $G'(\omega)$  and  $G''(\omega)$  (Fig. S8). We also fit a model including a fractional element that reproduces the power-law behavior associated with a continuous distribution of relaxation times in biological materials [16]. This model reproduced the power-law storage behavior and the non-monotonicity of dissipation in the live sponges with high accuracy.

### C. Nonlinear Viscoelasticity

For increasing amplitude of oscillatory shear strain  $\gamma_0$  (LAOS), sponge tissue responded nonlinearly by softening as indicated by decrease of  $G'_M(\gamma_0)$  and  $G'_L(\gamma_0)$  (Fig. 7A-C), defined in Sec. II B. We let the onset of softening  $\gamma_a$  (dotted vertical lines) be where  $G'_M$  first

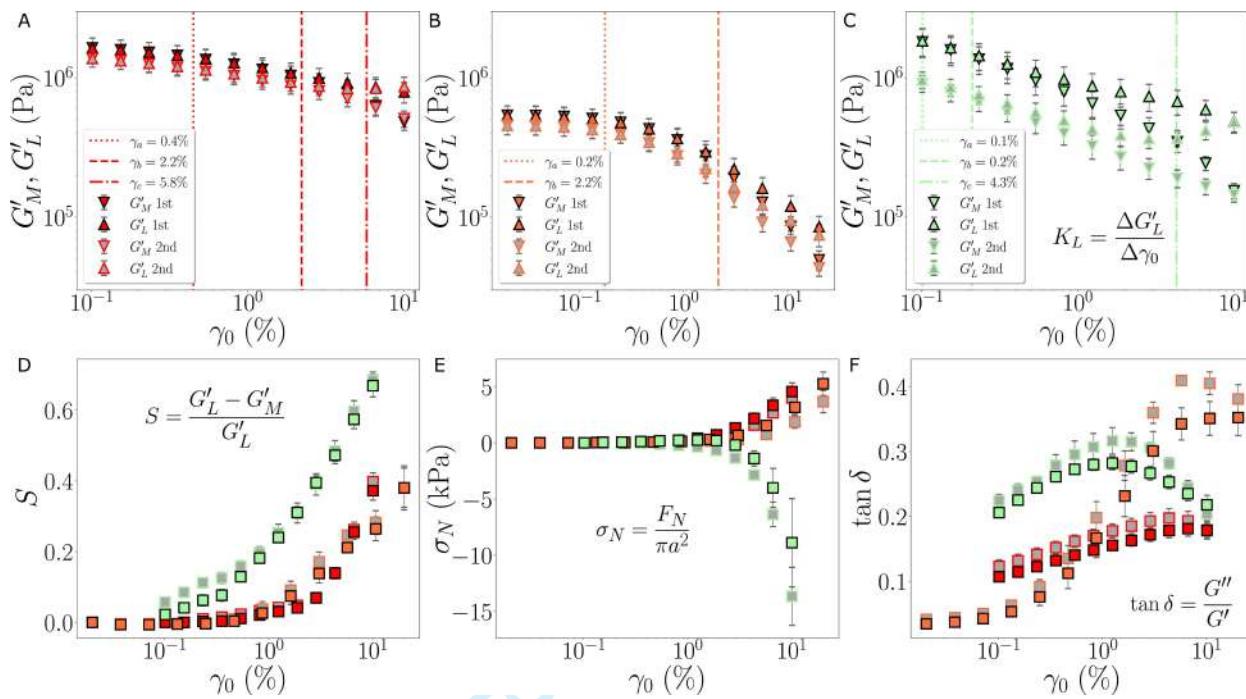


FIG. 7. Sponge tissue amplitude sweeps at  $\omega = 4\pi \text{ s}^{-1}$ .  $G'_M$  (downward triangles) and  $G'_L$  (upward triangles) vs.  $\gamma_0$  in A) *A. polycapella* B) *Callyspongia sp.* and C) *C. celata*. Data for the second round are in gray. D)  $S$  E)  $\sigma_N$  F)  $\tan \delta$  vs.  $\gamma_0$

decreased more than 10% from its previous value. *C. celata* began softening at a smaller  $\gamma_a$  and also softened more than *A. polycapella* and *Callyspongia sp.* over the course of one LAOS test. By the final amplitude,  $G'_M$  had decreased by roughly 90% in *C. celata* (Tab. S2).

Intriguingly, *A. polycapella* and *C. celata* tissue had additional shear nonlinearities arise after pre-conditioning of the first LAOS test. During the second LAOS test, the large strain elastic modulus  $G'_L(\gamma_0)$  (gray upward triangles) in these two species increases after another strain  $\gamma_c$  (dashed-dotted vertical lines). This was most pronounced in *C. celata* (Fig. 7C). It softened so much in the first LAOS but still returns exactly to its state at the end of the first LAOS, indicating strong shear softening followed by equally strong stiffening. In other words,  $G'_L(\gamma_0)$  has an inflection point during the second LAOS in these species. *Callyspongia sp.* does not, despite it being sheared to twice the value of  $\gamma_0 = 20\%$ . We made  $\gamma_c$  be where the point at which the numerical derivative  $K_L = \Delta G'_L / \Delta \gamma_0$  changed sign to confirm there was no inflection point in  $G'_L(\gamma_0)$  for *Callyspongia sp.* during the second round of LAOS (Tab. S3).

The time-resolved trajectory of the shear stress  $\tau(t)$  ((ii) Fig. S2) in response to oscillating shear strain  $\gamma(t)$  ((i) Fig. S2) reveals further richness in the larger strain viscoelasticity of

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3 sponge tissue.  $\tau(t)$  increases nonlinearly during a single cycle from  $\gamma = 0$  to  $\gamma = \pm\gamma_0$  as  
4 indicated by concave-up parametric plots of  $\tau(t)$  vs.  $\gamma(t)$  (L-B curves Fig. S2(iv)). We  
5 evaluated this stiffening at each  $\gamma_0$  with the index  $S = \frac{G'_L - G'_M}{G'_L}$  and ~~made~~<sup>set</sup> its onset  $\gamma_b$  be  
6 to the point at which  
7 where  $S \geq 0.1$  [18].  $S = 0$  signifies no stiffening within a cycle and elliptical L-B curves with  
8 well-defined semi-major and semi-minor axes (L-B curve lower insets). The more positive is  
9  $S$ , the greater  $G'_L$  compared with  $G'_M$ , the more upwardly concave the L-B curve, and the  
10 greater the stiffening (L-B curve upper insets) at ~~that~~<sup>the given</sup>  $\gamma_0$ . This stiffening nonlinearity occurs  
11 during a single oscillation from  $\gamma = 0$  to  $\gamma = \pm\gamma_0$  for  $\gamma_0 > \gamma_b$ .  
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The onset of stiffening  $\gamma_b$  (dashed vertical lines) followed the same trend as  $\gamma_a$ . It was about ten times smaller in *C. celata* compared with *A. polycapella* and *Callyspongia* sp. (Tab. S2). In other words  $\gamma_{a,b}^{Cliona} < \gamma_{a,b}^{Callyspongia} < \gamma_{a,b}^{Axinella}$  was true.  $S$  increased monotonically with increasing  $\gamma_0$  in all species and by  $\gamma_0 = 10\%$  *C. celata* had the largest and *Callyspongia* sp. the smallest  $S$  (Fig. 7D). *C. celata* shear stiffened more (more positive  $S$ ) and after smaller strains than *A. polycapella* and *Callyspongia* sp. when  $\gamma(t)$  is increased over the trajectory of a single cycle but also softens more (more negative  $K_L$ ) and at smaller strains (Tab. S2).

*C. celata* was also distinct from *A. polycapella* and *Callyspongia* sp. by the sign of its induced normal stress and ratio of dissipation to storage as functions of  $\gamma_0$  (Fig. 7E,F). Due to perpendicular expansion upon shearing, positive normal stress is induced in many materials [35]. Semi-flexible biopolymer networks instead pull downward when sheared, exhibiting negative normal stress [35]. Surprisingly, sponge tissue did both: *A. polycapella* and *Callyspongia* sp. pushed upward on the top plate with a positive normal stress of roughly 5 kPa while *C. celata* pulled downward with negative normal stress twice as large by  $\gamma_0 = 10\%$ . Finally,  $\tan \delta$  increases with  $\gamma_0$  in all three species initially, but *C. celata* reaches a clear maximum dissipation (Fig. 7F). *A. polycapella* and *Callyspongia* sp. begin the LAOS experiment about half as dissipative as *C. celata*, and after increasing initially, dissipation then only marginally decreases for *A. polycapella* and *Callyspongia* sp. over this physiological range of  $\gamma_0$ .

## D. Morphological & Skeletal Characteristics

As described in Sec. II C, we imaged mesoscopic features in the washed fibrous skeletons of less dense sponges (Fig. 8). *A. fulva* grows as rope-like branches that hang downward. It has no spicules but a relatively stiff spongin skeleton of irregular polygons with large mesh sizes of a few millimeters. We could not distinguish  $\hat{n}_1$  from  $\hat{n}_2$  in *A. fulva* samples at this scale. *I. notabilis*, the other sponge without spicules in our dataset, has a similar skeleton (Fig. S5B) and a lobe-like, branching growth form. *Callyspongia sp.* has hollow tissue (Fig. 8H), making it ultimately vase-like, but when viewed on a smaller scale by stereomicroscope (Fig. S5F,G) its tissue looks like that of *A. fulva* and *I. notabilis*.

By contrast, *A. polycapella* is conspicuously solid and axially arranged. This sponge forms erect, tree-like structures (Fig. S3), with one central column, or trunk. Fig. 8E (F) shows an  $\hat{n}_1$  ( $\hat{n}_2$ ) disk of *A. polycapella*. The red lines signifying local nematic order and thus average fiber orientation show a condensed region of axial fibers, a trait well-documented in erect sponges [36, 37], as well as radial and tangential fibers. *Tethya sp.* and *T. keyensis* growth forms are radially symmetric but the nematic tensors drawn with FibrilTool also reveal three principal fiber directions as in *A. polycapella* (Fig. S4A,B). Materials such as wood [38], bone [39], and brick [40], also have three principal directions and are thus orthotropic. A point within an orthotropic material has three mutually perpendicular planes of reflection symmetry [39] and material properties are different along each principal direction. This was most obvious in *A. polycapella*, whose tissue does bear a striking resemblance to a tree trunk (Fig. S5D), but we also found structural and mechanical signatures of orthotropy in *T. keyensis* and *Tethya sp.*

In terms of the bulk density measured by the mass fraction of water  $\phi_w$  in <sup>the</sup> ~~their~~ tissue, *C. apion*, *C. celata*, *T. keyensis*, and *Tethya sp.* were significantly denser ( $\phi_w \leq 0.5$ ) than *A. polycapella*, *Callyspongia sp.*, *A. fulva*, and *I. notabilis* ( $\phi_w \geq 0.7$ ) (Fig. 9A). Multiplying the mass fraction of solids  $\phi_s = 1 - \phi_w$  by the total density of the sponge tissue disk  $m_w/V$ , gives an estimate of the concentration of spongins  $c$ . On a log-log plot of  $G'_0$  vs.  $c$  in mg/mL, we find an approximate scaling of  $G'_0 \sim c^{11/5}$  to fit the sponge data (Fig. 9B). This agrees with previous results for the dependence of the network shear modulus on semi-flexible polymer concentration [41], providing further evidence for general semi-flexibility of spiculated spongins.

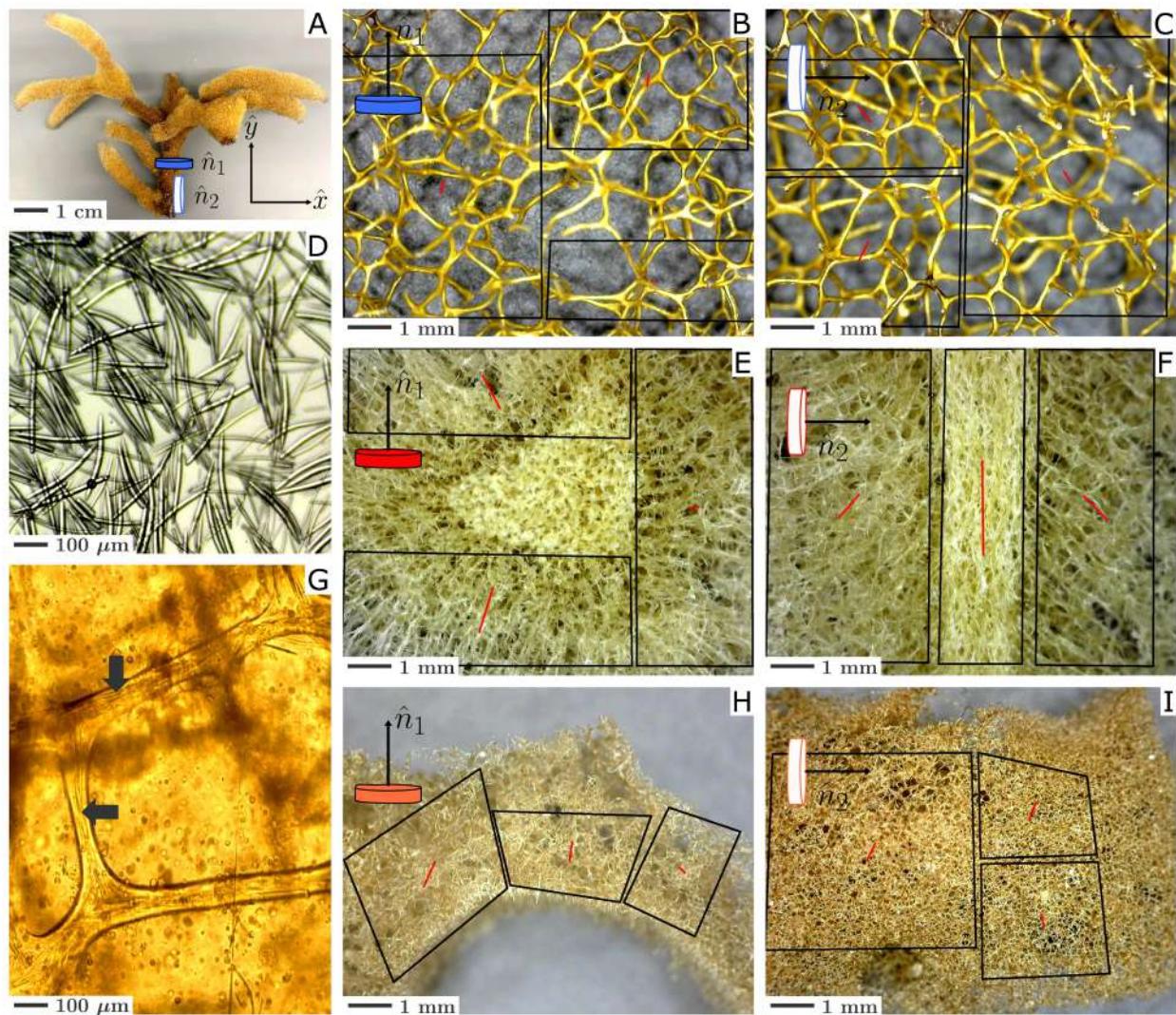


FIG. 8. Sponge structure and morphology. A) dried *A. fulva* spongin fiber skeleton sampled into B)  $\hat{n}_1$  and C)  $\hat{n}_2$  disks. Red lines inside black boxes correspond to average fiber orientation measured using FibrilTool [21]. D) *A. polycapella* spicule preparation. E)  $\hat{n}_1$  F)  $\hat{n}_2$  *A. polycapella*. G) *Callyspongia* sp. skeleton, arrows show spicules confined inside spongin fibers. H)  $\hat{n}_1$  I)  $\hat{n}_2$  *Callyspongia* sp.

The major component of the spicule population in these species were monactine (Fig. S7). *Tethya* sp. (Fig. S7D) also contained spiky spherical spicules (spherasters) in its cortex only. We did not count these since they were much more numerous than the monactine strongyloxeas found in both the cortex and pith. *A. polycapella* oxeas (Fig. 8D), *Callyspongia* sp. oxeas (Fig. 8G), and *C. celata* tylostyles (Fig. S7B) were similar in size and shape: monactine and about 100  $\mu\text{m}$  long and 10  $\mu\text{m}$  thick, though arranged differently with respect

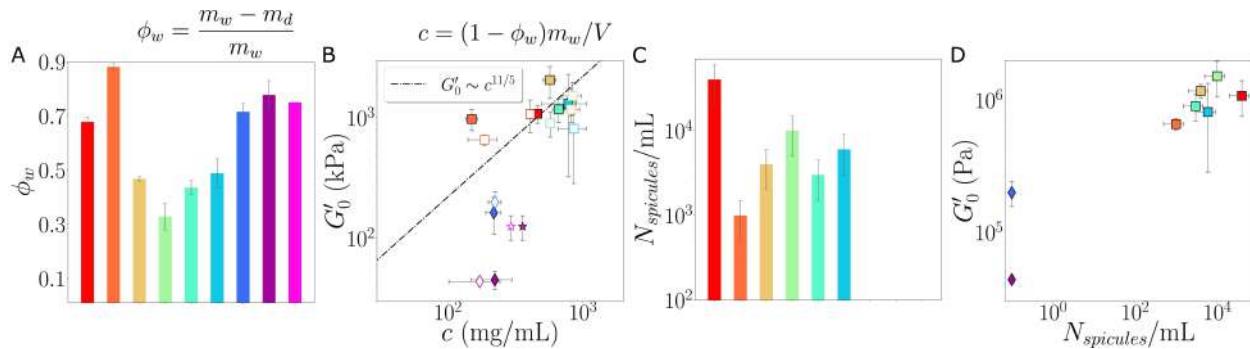


FIG. 9. A) mean mass fraction of water  $\phi_w \pm \text{s.e.}$  of  $N$  disks B)  $G'_0$  vs. the concentration of spongins  $c$  estimated from  $\phi_w$ . C) estimated number of spicules per mL of tissue  $\pm 50\%$ . D)  $G'_0$  vs. the number density of spicules.

to the softer part of the tissue. The three fiber directions in *A. polycapella* are spicule-reinforced [42] while spicules in *Callyspongia sp.* are constrained entirely within the fibers of its spongin network [43]. *C. celata* spicules are arranged and oriented densely and randomly [22], along with a surprising amount of sand (Fig. S6F). We observed *A. polycapella*, *C. apion*, *C. celata*, *T. keyensis*, and *Tethya sp.* tissue dissolve slowly and vigorously in bleach (Vid. S1) and produce strong light scattering in culture wells (Fig. S6). These observations and our estimates of spicule number density (Fig. 9C-D) confirm heavier spiculation in these sponges compared with *Callyspongia sp.* and the two species without spicules.

#### IV. DISCUSSION

We explored the mechanics and dynamics of a set of sponge species using rheology and microscopy. Our results on the detailed and surprisingly diverse tissue mechanics of these sponges informs our understanding of the great diversity of body forms both within and between species in this phylum.

We first consider the species in our dataset with the most pronounced axial skeleton and erect growth form, *A. polycapella*. An axial skeleton is not unique to *A. polycapella* but present across many sponge clades and thought to be a morphological mechanism that generates rigidity [36, 37, 44]. Despite possession of this trait, *A. polycapella* had a smaller stiffness, i.e. shear rigidity  $G'_0$ , than *C. celata*. The sand that *C. celata* incorporated in addition to its spicules must be increasing its  $G'_0$ . Since the presence of spicules at all

increased  $G'_0$  by a factor of ten, stiffness is proportional to the total volume fraction of stiff inclusions, including sand grains. We speculate that the cortex of *Tethya sp.* overloaded the normal force transducer because spheraster-form spicules led to jamming in the physical sense, where in a system with sterically repulsive interactions, density and geometry combine to prohibit translational motions [45]. The dense, sandy inclusions in *C. celata* may have caused jamming in some regions of its tissue. So, while axial skeletons do not appear to cause anomalously high  $G'_0$ , or stiffness, in our dataset, the presence of an axial skeleton evidently does produce orthotropic elasticity. Orthotropic elasticity is when the material stiffness at a particular point in a body differs along three mutually orthogonal axes.

This form of anisotropic stiffness likely contributes to the ability of erect sponges to withstand pressure drag experienced in free stream, steady flow  $v$  (Fig. 1I). The magnitude of this drag force is

$$F_D = \frac{C_D \mathcal{S}}{2} \rho v^2 \quad (6)$$

where  $C_D$  is the drag coefficient,  $\mathcal{S}$  is the area exposed to flow, and  $\rho$  is the fluid density [46]. We consider *A. polycapella* as an upright, solid cylinder of radius  $a$  and length  $\ell$  (Fig. 1E) and therefore  $\mathcal{S} = 2a\ell$ .  $C_D$  depends on the Reynolds number  $Re = \rho v \ell / \eta$  where  $\eta$  is the fluid viscosity. Using the range of  $v$  from Sec. II B and values of  $\rho$  and  $\eta$  for seawater at 20 degrees C, we find  $10^2 \lesssim Re \lesssim 10^5$  over which  $C_D \approx 1$  for a cylinder [46]. The maximum flow-induced shear stress may be estimated as  $\tau_0 = F_D / \pi a^2$  and thus written as a function of  $v$  using Eqn. 6

$$\tau_0 = \frac{C_D \ell}{\pi a} \rho v^2 \quad (7)$$

This equation states that the more slender a cylindrical sponge is through  $\ell/a$  the larger is  $\tau_0$ . The Loop Current [47], which runs through places where *A. polycapella* is common along the Gulf of Mexico, around Florida, and up into northern Atlantic waters [48], can reach  $v = 80$  cm/s and would impart  $\tau_0 \approx 4.2$  kPa. As *A. polycapella* and other tree-like sponges grow taller, orthotropic tissue that is stiffest along  $\hat{y}$  is necessary to withstand large  $\tau_0$ . Wood, another orthotropic material [38] that is stiffest along its central axis, is also subjected to a single principal force: wind-induced drag [46]. Sponges with axial skeletons are therefore mechanically analogous to trees by this reasoning, and using them for reef dendrochronology should be possible in principle. The tangential fibers of *A. polycapella* (Fig. 8F) correspond to surfaces of earlier accretive growth, as they do in a tree's trunk.

Eqn. 7 also shows that as  $\ell$  increases during growth, sponges could keep the load on themselves constant by keeping the ratio  $\ell/a$  constant, which would fix the value of the tissue stiffness  $G'_0 = \tau_0/\gamma_0$  in each branch and across the whole animal. This line of reasoning suggests global rigidity [49], as mediated by  $\ell/a$ , is the tissue network parameter optimized by sponges with axial skeletons [50]. This model in turn predicts that sponges should branch in a self-similar or fractal way, with fractal dimension increasing in areas of higher flow speed in order to share a larger load on the tissue  $\tau_0$  between more branches. In other words, the cost of construction of new branches is fixed throughout the whole height of the animal. Tree-like sponges do branch in a self-similar way [50, 51], with higher fractal dimension measured in individuals from sites of higher flow  $v$ , but relevant optimization functionals have not been explored like they have in more familiar transport networks [52].

In contrast, our results suggest that *T. keyensis* and *Tethya sp.* tissue is orthotropic but these sponges are not obviously tree-like since they do not form branches. They are erect, though, and thus exposed to one principal force: pressure drag which acts perpendicular to  $\hat{y}$ . Indeed, dissecting them revealed thicker skeletal fibers parallel to  $\hat{y}$  than along  $\hat{x}$  or  $\hat{z}$  (Fig. S4A,B). Given the above, it is likely that axial and radial sponge skeletons are both orthotropic. The former grows cylindrically while the latter spherically, but sometimes within a single individual, both types exist (Fig. 9 in [53]), lending support to the idea that each is a manifestation of orthotropy. As long as a sponge is slender enough ( $\ell \gtrsim a$ ) such that flow separates around it [54], its tissue must be stiffest along  $\hat{y}$  to withstand this. For low-aspect-ratio sponges ( $\ell < a$ ), Eqn. 7 no longer holds as such shapes are subject to different forces.

In addition to pressure drag, there will be other flow-induced forces on low-aspect-ratio sponges like ‘skin’ or viscous drag, lift, and accelerating flows. The calculation of these is subtle and presented in [9, 54], so we do not include it here. However, the key point is that both kinds of drag, lift, and accelerating flows can all become important in different dynamic flow conditions, and thus the direction of the net force on a low-aspect-ratio sessile animal is not generally perpendicular to  $\hat{y}$  or even fixed. It then makes sense for an amorphous, massively encrusting sponge like *C. celata* to have isotropic tissue, since it contends with applied forces that are time-dependent, and from multiple directions. *Callyspongia sp.*, *A. fulva*, and *I. notabilis* tissue was also more isotropic, but these sponges form hollow cavities, making them vase-like and mechanically transversely isotropic, i.e. the  $xz$ -plane is one of

isotropy and is transverse to the  $y$ -axis of symmetry, the long axis of the vase [39]. In other words, the body cavity, or spongocoel, is an axis of mechanical symmetry that is typically perpendicular to the substrate plane in vase-like sponges. Sponges of different growth forms are therefore well-adapted to the same environments through unique tissue mechanical strategies. Moreover, it has been shown that high-aspect-ratio forms like erect cylinders, encounter primarily fine particles whereas low-aspect-ratio forms encounter larger particles [54]. This sedimentation gradient would enable sponges of different growth forms to specialize in differently-sized food particles.

In many ways, *C. celata* had the richest rheology of the sponges we tested. Its tissue appeared to undergo a compression-induced phase transition as indicated by the discontinuity in  $G'$  vs.  $|\sigma_N|$ . Recently, simulations have shown that networks of semi-flexible polymers embedded with stiff inclusions can undergo a phase transition as the inclusions rearrange non-uniformly (non-affinely) under bulk compression [55]. Our multiaxial mechanical data was qualitatively very similar to these simulations. The slope change at  $\epsilon = -6\%$  in *C. celata* and others may be seen as the signal of imminent jamming. Rearrangement of stiff inclusions during compression induces local tension within intrinsically semi-flexible biopolymers [56], leading to macroscopic increase of rigidity [55]. Semi-flexible polymers are those which are flexible on scales larger than their persistence length [30], but locally quite stiff, and nonetheless subject to thermal fluctuations. Many ubiquitous biopolymers are semi-flexible [57]. Our mechanical data, taken together with the biochemical similarity of spongins to fibrillar and non-fibrillar mammalian collagens [58, 59], and the fact that the average spongin fibril size (10 nm [5]) is comparable to intermediate filament sizes [57], points to spongin semi-flexibility. In other words, spiculated spongin bundles likely contribute significant stretching, but also bending energies towards the total energy of deformation of sponge tissue.

The strong compression stiffening in sponges compared with mammalian tissues likely comes from shape constraints as described above, but also volume constraints from cells acting as deformable inclusions [25]. Sponge microenvironments can be dense and crowded, especially in high-microbial-abundance species where symbiotic bacteria in the tissue are  $\sim 100$  times more numerous than in low-microbial-abundance species [60]. The effects of cell confinement and in turn nuclear deformation during cell motility have only just begun to be explored in mammalian systems [24, 61]. Because of the purported absence of cytoskeletal

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3 intermediate filaments like nuclear lamins in sponges, global compression of tissue may cause  
4 contact percolation of sponge cells and subsequent nuclear deformation (Fig. 57A in [5]) and  
5 mechanical signaling. For this to be plausible, sponge cells must be able to respond to strains  
6  $\lesssim 10\%$ , considering flow-induced forces would have to be transmitted from the surrounding  
7 tissue.  
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11 The observed auxeticity of sponge tissue provides a possible mechanism for amplification  
12 of strain in biological systems [34]. While we made indirect measurements of Poisson's ratios  
13  $\nu_{ij}$  in this set of sponges (Tab. S1), direct observation of contraction upon compression of  
14 a randomly picked marine sponge (Vid. S3) confirms  $\nu$  generally takes negative values in  
15 these animals. To our knowledge, there are no examples of bulk collageneous mammalian  
16 tissues which are auxetic. Auxetic re-entrant polymer foams (Fig. 2 in [62]) ~~certainly~~ bear  
17 a resemblance to the fiber skeletons of *Callyspongia sp.*, *A. fulva*, and *I. notabilis*. Since  
18 sponges are generally subject to stresses 1–10 kPa and strains rarely above 10%, their cells  
19 may be able to respond to these comparatively small mechanical shifts by living within  
20 auxetic tissues which amplify applied strain by avoiding changes of dimension. Some models  
21 of auxetic response show that the walls of the voids within the material collapse inward in  
22 controlled fashion [33]. Local strain at these points is presumably very high, and a potential  
23 source of a cellular mechanobiological response.  
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26 Our results on the nonlinear viscoelasticity in sponges point at general responsiveness of  
27 sponge tissue to comparatively small, flow-induced strains. *C. celata* begins shear softening  
28 at  $\gamma_a \approx 0.1\%$ , an onset at least ten times smaller than in collagen gels [20]. In fact, for *in*  
29 *vitro* collagen, the extent of shear softening is weak enough that it is seldom reported on  
30 [20], but living sponge tissue softened significantly. The strong softening in *C. celata* might  
31 allow structural remodeling in the face of increasing  $\gamma_0$ . *C. celata* and *A. polycapella* shear  
32 stiffen at  $\gamma_c \approx 5\%$ , an onset four times smaller than in collagen gels ( $\gamma_c \approx 20\%$  [20]) and  
33 they only do so after pre-conditioning with one round of LAOS. During the second round,  
34  $G'_L(\gamma_0)$  decreases as before, until  $\gamma_c$  where it begins to increase as described in Sec. IIIC.  
35 We discuss this important subtlety below.  
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38 Cyclically loading a large class of disordered systems can allow mechanical memory of  
39 steady-state driving amplitudes [63, 64]. Sponge tissue is a ~~great~~ candidate for mechanical  
40 memory formation. It is deformable but stable, made of heterogeneous network structures  
41 that rearrange under applied strain [65]. We interpret the shear stiffening only after a second  
42 round of LAOS as a mechanical memory effect. We discuss this in Sec. IIIC.  
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round of LAOS in *A. polycapella* and *C. celata* as a return to a previous rheological steady-state: the final applied strain  $\gamma_0$  and stress response  $\tau_0$  (encoded by  $G'_M(\gamma_0)$  and  $G'_L(\gamma_0)$ ) from the first round. This effect is also apparent in the L-B curves for these two species (Fig. S2 rows A and C, col iv) and is more obvious in *C. celata*. Considering this species' more granular, disordered nature, it would make sense for its tissue to recall 'training' strains with higher fidelity compared with *A. polycapella*. Furthermore, the general non-monotonicity of dissipation ( $\tan \delta$ ) as functions of both  $\omega$  and  $\gamma_0$  in living sponge tissue implies tunability and responsivity [63]. *C. celata* must also be more tunable than any of the other sponges tested, given it had such a clear maximum dissipation at a small  $\gamma_0$ . Since memory formation is intrinsically tied to non-equilibrium dynamics [63], this suggests *C. celata* tissue is more irreversibly driven by flow than *A. polycapella*.

We speculate on the absence of a strain-stiffening nonlinearity ( $\gamma_c$ ) in *Callyspongia* sp. by considering how its spicules are constrained within the softer fibers of its tissue. As this sponge is sheared, its spicules presumably slide past each other or perhaps only weakly interact but still inside large spongin fibers (Fig. 8G). Past  $\gamma_a$ , the spicules may rupture out of these fibers, causing the more dramatic softening between  $\gamma_a < \gamma_0 < \gamma_b$  (Fig. 7B). This sponge was also the least dense of any we tested, such that there may be too much open space in its tissue for spicules to abut and create internal strain. We assume that  $\gamma_b$  ( $\gamma_{intra}$  in [20]), corresponds to the strain at which nonlinear elastic stiffening [56] of the spiculated spongin part of the tissue becomes relevant. That *A. polycapella* and *Callyspongia* sp. had similar values of  $\gamma_b \approx 4\%$  and the same sign of induced normal stress under shear (positive) but  $\gamma_b \approx 0.5\%$  in *C. celata*, which had an opposing sign of induced normal stress (negative), suggests major physical differences and diversity in spiculated sponges.

In any case, *C. celata* must have a strong interaction between its softer fibrous network and stiffer spiculated skeleton, and we suggest this sponge and those like it are in the same class of disordered systems as colloidal gels, which have recently been demonstrated to have an ability to embed mechanical memories perpendicular to a driving shear [65]. The large magnitude of the induced negative normal stress in *C. celata* may even be connected to the 'recording' of a high-fidelity memory through compression. It is curious that ~~as a deformation,~~ compression appears more lossy than shear. Overall, increased sensitivity and tunability in disordered tissue, low-aspect-ratio growth form sponges like *C. celata*, could be a trade-off with the stability that mechanical order provides in more durable, higher-aspect-

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3 ratio sponges like *A. polycapella* and *Callyspongia* sp.  
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