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2 ***Vo-Norvana: Versatile Framework for Efficient Segmentation of Large Point***

3 **Cloud Datasets**

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5 **Abstract**

6 Dense 3D point clouds collected from rapidly evolving data acquisition techniques such as light detection
7 and ranging (lidar) and structure from motion (SfM) multi-view stereo (MVS) photogrammetry contain
8 detailed geometric information of a scene suitable for a wide variety of applications. Amongst the many
9 processes within a typical point cloud processing workflow, segmentation is often a crucial step to group
10 points with similar attributes to support more advanced modeling and analysis. Segmenting large point
11 cloud datasets (i.e., hundreds of millions to billions of points) can be extremely time consuming and
12 tedious to execute with current tools, which primarily rely on significant manual effort. While many
13 automated methods have been proposed, the practicality, scalability, and versatility of these approaches
14 remain a bottleneck stifling processing of large datasets. To overcome these challenges, this paper
15 introduces a novel, generalized segmentation framework called *Vo-Norvana*, which incorporates a new
16 voxelization technique, a normal variation analysis considering the positioning uncertainty of the point
17 cloud, and a custom region growing process for clustering. The proposed framework was tested with
18 several large-volume datasets collected in diverse scene types using several data acquisition platforms
19 including terrestrial lidar, mobile lidar, airborne lidar, and drone-based SfM-MVS photogrammetry. In
20 evaluating the accuracy of models generated from *Vo-Norvana* against manual segmentation, the average
21 error of the position, orientation, and dimensions are 2.7 mm, 0.083°, and 0.9 mm, respectively. Over 0.2

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22 million points per second and 36 thousand voxels per second can be achieved when segmenting an
23 airborne lidar dataset containing over 639 million points to about 1 million segments.

24 **Keywords:** point cloud, lidar, SfM, segmentation, voxelization, feature extraction

25

26 **Introduction**

27 Three-dimensional (3D) point clouds are a common form to digitally represent 3D objects or
28 scenes. Techniques such as light detection and ranging (lidar) and structure from motion (SfM) multi-
29 view stereo (MVS) photogrammetry have been adopted to collect 3D point clouds for numerous
30 applications (Olsen et al., 2013) supporting a wide range of disciplines. Lidar systems can be generally
31 categorized based on the acquisition platform into terrestrial laser scanning (TLS), mobile laser scanning
32 (MLS), and airborne laser scanning (ALS). Point clouds contain the precise 3D location of each data
33 record and sometimes include other basic information such as color, intensity (strength of return signal
34 from lidar sensors), and so on. Additional processes including feature extraction, classification, and
35 modeling are often required to extract higher-level information for a variety of applications. Point cloud
36 segmentation is the process of grouping points based on common attributes such that instead of handling
37 each individual data record, subsequent process can operate with each segment as the basic unit rather.
38 Increasing spatial resolution and area of coverage in mapping efforts can raise data volumes
39 exponentially, which poses a substantial challenge for both manual and automated segmentation
40 approaches.

41 Herein, we propose a novel, generalized, and efficient point cloud segmentation framework to
42 cope with a variety of scenes (e.g., urban, rural, industrial sites, etc.) and systems (e.g., TLS, MLS, ALS,
43 SfM/MVS photogrammetry, etc.). This paper describes the three primary steps of this automated
44 framework: data organization with a voxelization technique that can preserve geometric details, Normal
45 Variation Analysis (*Norvana*), and point clustering. *Vo-Norvana* offers several advances over existing
46 segmentation algorithms, including the ability to (1) cope with a variety of shapes in different sizes and

47 produce high quality modelling results, (2) consider of positional uncertainty of the data both locally and
48 globally, reducing improper segmentation results from noise when combining scans or flightlines from
49 different locations, (3) achieve a much higher computational performance on large datasets (both in terms
50 of number of points and spatial extent), and (4) be versatile in processing data from a variety of systems
51 and scenes with minimal fine-tuning of parameters. These contributions are explored and demonstrated
52 through extensive testing of several representative datasets where the approached showed high accuracy
53 modelling results (within a few mm of manual modelling procedures), computational efficiency (over 0.2
54 million points per second and 36 thousand voxels per second for a large dataset of 639 million points).

55 **Related Work**

56 This section summarizes related research in point cloud segmentation. It will commence with a
57 brief background on segmentation followed by a description of common approaches to implement
58 segmentation including planar feature detection techniques, scan-to-bim processes, voxelization, data
59 structuring, and artificial intelligence.

60 *Segmentation background*

61 At its basic level, segmentation is a process to group points based on one or more common
62 attributes (e.g., intensity, color, normal, etc.). This process can divide millions of discrete points into
63 clusters such that instead of handling each individual point, subsequent processes can be efficiently
64 performed with each segment as the basic operating element, significantly reducing the data volume. For
65 example, generating thousands of geometric models directly from the original point cloud can be very
66 challenging given the ambiguity and complexity within a scene. In contrast, with a segmented point
67 cloud, the modeling or fitting technique only needs to fit one or a few primitives to the points within each
68 segment, resulting in more robust and efficient processing. Segmentation results can also be used as input
69 for object-based classification due to richer information provided within each segment compared with
70 individual points (e.g., Poux et al., 2020, Che et al., 2021a). Because manual processing of point cloud
71 data can be extremely tedious and time-consuming, much research has focused on different aspects of
72 automating point cloud segmentation in addition to point cloud processing more broadly.

73 We recently conducted a thorough literature review on the subject of object recognition, feature
74 extraction, segmentation, and classification for MLS data (Che et al., 2019). Considering prior work
75 documented by other researchers and other detailed reviews of the state of the art (e.g., Grilli et al., 2017,
76 Xia et al., 2020), there has been a reasonably comprehensive coverage of existing segmentation methods
77 for both TLS and MLS. Thus, for the remainder of this section, we will focus on segmentation approaches
78 that apply to ALS and SfM/MVS point clouds, as well as provide a summary of more recent or highly
79 relevant research associated with TLS and MLS to this work.

80 Compared with TLS and MLS, ALS data usually covers a much larger area and has a relatively
81 more consistent point density but generally suffers from limited coverage on vertical faces of objects
82 (e.g., buildings, trees, etc.) as well as lower resolution overall. Some of these issues can be reduced
83 through optimized flight planning such as lower flight altitude, higher overlap, and orientation of the
84 flight path (Vo et al., 2021). Given the large data volume and covered area, most ALS algorithms focus
85 on specific applications such as land cover classification, 3D reconstruction, or 3D urban modeling
86 (Wang, 2013; Wang et al., 2018).

87 *Planar features*

88 Within an urban environment, the vast majority of anthropogenic objects captured by ALS (e.g.,
89 roofs) consist of planar surfaces. Xia et al. (2020) thoroughly reviewed the state-of-the-art in extracting
90 geometric primitives such as planes from 3D point clouds. Since that review was published, several new
91 algorithms have been proposed (e.g., Poz et al., 2020, Wang et al., 2020, Zhu et al., 2021, Zhang et al.,
92 2021). Towards the objective of fitting a plane, one or multiple techniques are employed for segmentation
93 including the Hough transform, principal component analysis (PCA), random sample consensus
94 (RANSAC), and/or region growing. In application to ALS data, most of these approaches have been
95 focused on extracting roofs. Zhao et al. (2021) compared these techniques for roof segmentation and
96 found that most approaches proved effective for their test datasets. Nevertheless, these approaches
97 focused on only extracting planar surfaces such as rooftops, which can result in many artefacts of under-
98 and over-segmentation for other geometric shapes (e.g., spheres).

99 A generalized segmentation algorithm capable of working with many different types of surfaces
100 is necessary for reliable execution of subsequent processes such as classification (Vosselman, 2013).
101 Other methods eliminate small planar segments by classifying point clouds into smooth and rough surface
102 segments (e.g., Ni et al., 2017) in an effort to improve the segmentation. Point cloud segmentation
103 algorithms for forest scenes are focused on individual tree segmentation (e.g., Wang et al., 2019, Yang et
104 al., 2020).

105 In principle, most of the aforementioned methods should also be adaptable to point clouds
106 generated with lidar or SfM/MVS data obtained from an uncrewed aerial system (UAS) platform because
107 it has a similar scan acquisition geometry. However, to-date very few methods have been rigorously
108 tested and demonstrated on UAS-lidar or SfM/MVS data likely due to differences in applications and
109 variant noise levels from these systems.

110 *Scan-to-BIM segmentation*

111 Some approaches have been developed specifically for ground-based lidar point clouds, primarily
112 for handling planar surfaces to extract features from building façades, indoor environments, bridges, and
113 other anthropogenic objects. These features are then used in applications such as 3D model
114 reconstruction, building information modeling (BIM), quality control inspection, progress tracking,
115 cultural heritage, and so forth (Wang & Kim, 2019). As an example, Maalek et al. (2018) proposed a
116 technique utilizing PCA that segments the point cloud into planar and linear features for the purpose of
117 tracking progress on a construction site. Bassier et al. (2017) proposed an approach based on region
118 growing and conditional random fields for the reconstruction of BIM models.

119 *Voxelization*

120 The voxelization process often organizes the point cloud into 3D grids or cubes containing a
121 number of points whereas supervoxels can be derived by refining the boundary considering the
122 homogeneity in terms of predefined attributes. The majority of generic segmentation approaches have
123 been developed based on voxelization (e.g., Vo et al., 2015) and super-voxelization (e.g., Mahmoudabadi
124 et al. 2013, Lin et al., 2017, Dong et al., 2018, Huang et al., 2019). For example, Xu et al., (2021)

125 performed a comprehensive review on voxelization and super-voxelization methods and applications.
126 These voxels or supervoxels themselves inherently provide an over-segmented result, requiring an
127 additional step to cluster the supervoxels. It is worth noting that the supervoxelization is particularly
128 effective for buildings and scenes containing large planar surfaces. Unfortunately, investigation of its
129 performance for other curved surfaces has been limited.

130 *Scan Pattern Grid*

131 Recently, we proposed an efficient segmentation approach, namely *Norvana* (Che & Olsen,
132 2018). *Norvana* operated specifically on TLS data to take advantage of the scan pattern grid, which
133 enabled all points within a scan to be stored into a compact 2D grid representation without any
134 information loss. We then extended this conceptual idea to MLS data and developed *Mo-Norvana* (Che &
135 Olsen, 2019), by introducing a robust trajectory reconstruction method that regenerates the scan pattern
136 from an unorganized MLS point cloud. Both approaches proved to be very efficient, scalable, and capable
137 of tackling a variety of shapes and objects.

138 *Artificial Intelligence*

139 Lately, due to the rapid development of computer vision, deep learning, and artificial intelligence
140 (AI) technology combined with the growing availability of computing resources and public datasets,
141 numerous studies have used AI for 3D point cloud processing. Rather than segmenting the point cloud
142 into groups (i.e., instance segmentation) based on the surface characteristics, the computer vision and AI
143 communities tend to be more concerned with classifying or labeling each individual point directly (called
144 semantic segmentation) (Poux & Billen, 2019, Xie et al., 2020). Before deep learning became a widely
145 popular technique in semantic segmentation for 3D point clouds, some work utilized machine learning
146 methods. For example, Weinmann et al. (2015) analyzed different techniques in each step of a machine
147 learning framework for semantic segmentation including neighborhood selection, feature extraction,
148 feature selection, and supervised classifier. Recently, Bello et al. (2020) conducted a critical review on the
149 use of deep learning in processing point clouds. In addition to this work, several relevant state-of-the-art

150 review papers have been published that focus on specific applications such as autonomous driving (e.g.,
151 Li et al., 2021) and 3D heritage (Matrone et al., 2020).

152 Although it is undeniable that the deep learning technique is powerful and has tremendous
153 potential in the context of point cloud processing, it is worth noting that most of the datasets used to
154 develop and test these deep learning frameworks are often substantially sparser with significantly less
155 geometric details than the dense point clouds acquired with survey-grade systems (Hackel et al., 2017).
156 Additionally, most deep learning approaches require extensive compilations of high-quality training
157 datasets to tackle a variety of systems and scenes, which is difficult given that the publicly available 3D
158 training dataset cover very limited scenarios. Unfortunately, labeling 3D point cloud manually to generate
159 training datasets can be tedious, time consuming, and often subjective. This immense effort required is
160 rarely reported quantitatively, resulting in difficulties in predicting the cost of establishing an effective
161 benchmark dataset. Hence, given this reliance on substantial training datasets, deep learning approaches
162 face challenges of scalability and versatility for processing typical lidar datasets collected for the complex
163 built environment.

164 **Summary of Limitations**

165 Although the aforementioned studies present reasonable segmentation results to different degrees,
166 three important limitations in the state-of-the-art can be summarized as follows:

167 (1) The overwhelming majority of approaches focus on extracting planar patches or surfaces.
168 Consequently, such assumptions substantially impact their performance on other basic shapes or more
169 complex objects common within the built environment. In particular, this limitation significantly hinders
170 the application to outdoor scenes, which consist of both geometric primitives and irregular shapes.

171 (2) Most existing approaches were only tested on a single dataset or several small datasets on the
172 order of hundreds of thousands to a few million points. Many have also only been tested for a relatively
173 small area where basic down-sampling can substantially reduce the data volume without significant loss
174 of information. In practice, typical point cloud datasets often obtain hundreds of millions to billions of
175 points and cover large areas. The efficiency of the majority of these methods do not scale linearly with

176 point size and sufficient information is not often reported to understand how they scale to larger datasets.
177 Processing time typically increases exponentially with larger volumes of data resulting from the higher
178 computational complexity, often involving many iterations and global optimizations.

179 (3) Very few studies test their segmentation methods on a variety of datasets from different
180 platforms; most are geared towards to a specific system and application. Because deploying multiple lidar
181 and/or drone systems on a single project is becoming more and more common to maximize coverage and
182 completeness as well as improve efficiency throughout the area of interest, it is crucial to have a method
183 available that can simultaneously handle data from different sources. Lastly, a general-purpose
184 segmentation approach can also improve data reuse and increase the value of the point cloud data as it
185 supports many downstream analyses and applications. For instance, to be able to reconstruct 3D as-built
186 models from high resolution point clouds to create digital twins, an automated and scalable segmentation
187 is required to reduce the data complexity and simplify the modeling process by dividing the unorganized
188 data into more manageable and meaningful groups.

189 **Objectives**

190 To overcome these limitations, we propose a novel, generalized segmentation framework, namely
191 *Vo-Norvana*, that: (1) copes with a variety of regular and irregular shapes and objects; (2) reliably
192 processes and efficiently scales to handle expansive, unorganized point cloud data containing hundreds of
193 millions of points; (3) considers the level of uncertainty of the point cloud data to improve the
194 segmentation, and (4) robustly handles data collected from different scenes and systems. We will
195 illustrate the workflow in the methodology section and then present a series of experiments to
196 demonstrate the effectiveness of the proposed approach both qualitatively and quantitatively.

197 To clarify the novelty of the proposed approach, especially compared against our prior work
198 including *Norvana* (Che & Olsen, 2018) and *Mo-Norvana* (Che & Olsen, 2019), we will explain key
199 differences and innovations. First, *Vo-Norvana* structures the unorganized point cloud data via a new
200 voxelization approach whereas *Norvana* and *Mo-Norvana* exploit the scan pattern grid, requiring specific
201 sensor parameters and/or organized input data. Consequently, the proposed *Vo-Norvana* algorithm is able

202 to cope with a much broader range of 3D point cloud data from any platform (both individually and
203 merged together) while the previous approaches can only handle specific data collected from TLS and
204 MLS systems, respectively. Additionally, without being limited to work solely within a scan pattern grid,
205 the proposed approach supports analysis at a custom scale that can be different from the acquisition
206 resolution. Lastly, it is also worth pointing out that although all these three methods share a similar
207 concept in the normal variation analysis, the implementation of the *Vo-Norvana* is fundamentally
208 different in how it handles the data to compute the normals as well as its ability to consider the data
209 uncertainty, enabling rougher surfaces to be effectively extracted.

210 **Methodology**

211 The *Vo-Norvana* segmentation takes full-resolution georeferenced or registered point clouds as
212 input without requiring any prior cleaning or subsampling. The segmentation consists of three primary
213 steps (Figure 1), including: data organization (Section 2.1), normal variation analysis (Section 2.2), and
214 point clustering (Section 2.3). Firstly, the input point cloud data is partitioned into 3D tiles with overlap
215 along the boundary followed by a new voxelization approach that can reduce the data volume while
216 preserving more geometric details compared with traditional voxelization methods. Secondly, in each 3D
217 tile, each point will be analyzed with its neighbors to classify it as a *smooth*, *rough*, or *invalid* surface
218 point. Then, based on the classification result, a custom region growing algorithm groups each class of
219 points. Finally, the point classification and clustering results are mapped back to the original input
220 datasets to ensure the integrity of the data and generate the full segmented point cloud.

221 **Data Organization**

222 Many voxelization approaches suffer from excessive memory consumption due to numerous empty
223 voxels. Consequentially, methods directly exploiting voxelization for organizing a point cloud must balance
224 the voxel size with the spatial extent of the point cloud. For example, for a 100 by 100 m area with a vertical
225 extent of 50 m, an analysis at a scale (i.e., voxel size) of 0.05 m requires 4 billion voxels to be constructed.
226 This large quantity of voxels is difficult to manage and significantly hinders processing including the point

227 cloud segmentation as each voxel has to be analyzed. Sometimes multiple iterations are required, further
228 compounding the processing time. Additionally, using the aggregated information from voxels (e.g., single
229 point at the center or centroid of a voxel) instead of the actual points can result in loss of geometric details.
230 For instance, some methods resample the point cloud with the center coordinates of each voxel occupied
231 by one or more points, while others use the average, median, or centroid coordinates of all the points within
232 each voxel. Although these methods can simplify the analysis and reduce the computation complexity, they
233 result in difficulty in precisely representing the geometry of an object. Hence, we propose a dynamic
234 voxelization process to organize and structure the point cloud while preserving more geometric details.

235 *3D Tiling*

236 First, in the tiling process, we align the point cloud with the principal axis computed from principal
237 component analysis (PCA) to reduce the total number of voxels required (Figure 2). In many cases, a
238 rotation of the point cloud data about the Z-axis only would suffice for reducing the memory consumption.
239 Secondly, we partition the point cloud data via coarse 3D tiles such that the more intense computations can
240 take place in each tile to achieve high efficiency and low memory consumption. Then, to avoid boundary
241 artifacts and ensure subsequent processing is seamless across adjacent tiles, we buffer each side of a 3D tile
242 to provide overlap. The buffer size should be determined by considering the size of the searching window
243 utilized in the subsequent processes to ensure a seamless analysis throughout the workflow. In the presented
244 implementation of the proposed segmentation method, the minimum width of the buffer is 2 voxels on each
245 side, and the dimension of each 3D tile is initialized as 200 times of the voxel size, S_v , such that each 3D
246 tile contains ~8.5 million (204 x 204 x 204) voxels in total. This allows the processing to balance between
247 multiple factors including the extent of the data, typical size of a segment, the computing capacity (e.g.,
248 RAM, number of threads) and so on. It is also worth noting that the proposed framework includes the
249 process of merging all the analysis results at the point clustering stage to cope with the large segments
250 covered in multiple tiles.

251 *Voxelization*

252 Recently, we introduced a related voxelization approach to down-sample point cloud data and
253 demonstrated its effectiveness for ground filtering (Che et al., 2021b). Herein, we significantly improved
254 this new voxelization approach to organize the point cloud data to enable more efficient data processing,
255 especially in terms of memory consumption.

256 Because each 3D tile can be processed independently, only the memory associated with the voxels
257 within the specific tile under analysis need to be allocated at a time. Thus, we can dynamically voxelize the
258 point cloud within each 3D tile while still linking the information and analysis results associated with each
259 point back to the original point cloud throughout the entire process. In other words, the 3D tiles and voxels
260 only serve as a structure to organize the point cloud, but do not actually down-sample the data for the final
261 results as is commonly performed with most voxelization techniques. To further improve the efficiency,
262 we record the indices of the 3D tile and voxel for each point such that the points can be directly mapped to
263 the proper voxel and 3D tile with limited computational expense in case multiple iterations or processing
264 steps are needed. To preserve the geometric details, we mark the point that is closest to the center of the
265 corresponding voxel as *core* point candidates to represent the 3D coordinates of that specific voxel (Figure
266 3). Notice that we utilize the voxel center rather than the barycenter or median coordinates because the
267 point clouds can have highly variable point density, especially for lidar data. As a result, other approaches
268 can bias the sampling result and result in challenges associated with modelling multiple scans and/or data
269 sources. Next, to further normalize the point density, at each *core* point candidate, we search its neighbors
270 with a diameter of half of the voxel scale and determine if it is indeed the *core* point with the shortest
271 distance to the corresponding voxel center. If so, this *core* point candidate is marked as a *core* point while
272 all the other points in the voxel are classified as *accessory* points.

273 After labeling the point cloud as *core* and *accessory* points, we can directly simplify the data
274 robustly with a consistent point density by sampling the *core* points for the initial analysis before linking
275 the results back to the full point cloud for the full segmentation. Compared with most other voxelization
276 techniques, the proposed approach can preserve more geometric details because it samples from the original
277 points rather than re-sampling using voxels or aggregating points. For example, given the point cloud in

278 Figure 3, simply using the voxel centers for re-sampling (occupied voxels) would completely fail to
279 represent the zigzag pattern. If the re-sampling is conducted by taking the average or median coordinates
280 of all points in each voxel, the sharp corners would likely be undesirably smoothed. Moreover, to ensure
281 the robustness of the computation, a minimum number of points is often required. In other cases, a larger
282 voxel size S_v is needed, which would compromise details. Fortunately, the proposed voxelization
283 framework keeps the original point cloud and only the *core* points are distributed with consistent spacing.
284 Thus, further analysis for point cloud segmentation can be applied to the *core* points only with reduced
285 computational complexity, followed by projecting the analysis and segmentation results from the *core*
286 points to the *accessory* points to ensure the completeness.

287 **Norvana**

288 Our prior work of segmentation methods developed exclusively for terrestrial laser scanning (TLS)
289 and mobile laser scanning (MLS) data both organize the point cloud data into a 2D scan pattern grid,
290 followed by a normal variation analysis (*Norvana*), which exploits this data structure (Che & Olsen, 2018;
291 Che & Olsen, 2019). In contrast, in this work our objective is to develop a general segmentation approach
292 that can handle any type of point cloud. Hence, we generalize this technique by extending the same concept
293 into 3D space as well as introduce several significant improvements to allow more flexibility in handling
294 handle different types and qualities of point clouds. For example, while the 2D scan pattern grid embeds a
295 lot of constraints in terms of both geometry and topology in neighbor searching, additional geometric
296 constraints need to be added when generating a local triangular mesh in the proposed generalized *Norvana*
297 stage. In addition, we now consider the data uncertainty including both local (e.g., ranging precision) and
298 global (e.g., registration accuracy) errors during the *Norvana* process. Furthermore, although the previous
299 versions of *Norvana* were able to identify smooth surfaces, they were sensitive to vegetation and other
300 rough surfaces. To overcome this limitation, we implemented a multi-step feature classification to
301 categorize the point cloud into *smooth*, *rough*, or *invalid* surfaces as well as unclassified points such that
302 they are handled differently in the segmentation.

303 With the voxels serving as indices of the point cloud, a variety of neighbor searching strategies can
304 be employed efficiently. Given a point or coordinates, we define its neighbor as the points lying within its
305 corresponding and adjacent voxels. As a result, a total of 26 voxels needs to be jointly examined for
306 neighbor searching. The normal vector at each point can be estimated by computing the eigenvector
307 corresponding to the smallest eigenvalue derived from this point and its neighboring *core* points utilizing
308 singular value decomposition (SVD). Notice that the normal estimation can take place at a different scale
309 than the selected voxel size. The *core* points will be labeled as unclassified if the normal estimation does
310 not yield a valid result (e.g., no close neighbors). Otherwise, the normal variation analysis is performed to
311 each *core* point with its neighboring *core* points searched from its adjacent neighbor voxels. When the
312 number of the *core* neighbor points for a *core* point is less than the given threshold ($T_{N_Neighbors}$), this *core*
313 point is directly classified as an *invalid* surface point because it cannot form a reliable local surface for
314 further analysis. Otherwise, the 3D coordinates of a *core* point and its neighbors are projected to a local
315 coordinate system to align with the normal vector where the *core* point under analysis is defined as the
316 origin, the normal vector is defined as z'-axis, and the x' and y'-axis are set arbitrarily.

317 One limitation of the segmentation analyzing the normal variations is its sensitivity to the positional
318 errors and surface roughness (Che & Olsen, 2018). To cope with the positional uncertainty within point
319 clouds, we adjust the positions of the neighboring *core* points towards the *core* point under analysis in z'
320 direction (Figure 4). Note that this adjustment is only performed temporarily for this local normal
321 computation, and the actual coordinates of the point remain unchanged. We consider two types of
322 uncertainty and simplified them by utilizing two constant parameters, σ_{local} and σ_{global} . If the neighboring
323 *core* point is from the same source (e.g., scan, flight line, sensor), we utilize σ_{local} , which can be set as a
324 function of the ranging accuracy according to the specifications of the system (mm- to cm-level). When
325 combining data from different sources, in addition to σ_{local} , we further consider the errors from data
326 processing (e.g., registration, georeferencing) by defining the global uncertainty σ_{global} (mm- to cm-level),
327 which is often available in a data processing report. In some cases, the system specifications and/or data

328 reports are not available, the parameters can be estimated by measuring deviations of the point cloud in
329 localized areas until a reasonable sample is obtained. To further consider the uncertainty at the *core* point
330 in the following local analysis, the maximum allowable adjustment of its neighbor *core* points is set as two
331 times of the σ_{local} or σ_{global} .

332 Because we assumed that the point cloud only captures the surface of an object, we remove the
333 neighbor *core* points that are closer than $0.25S_v$ on the x'-y' plane to avoid creating a complex triangular
334 mesh locally. Next, we sort the neighbor points by their projected horizontal angle (θ) within the x'-y' plane
335 and generate a triangular mesh around the *core* point under analysis. To avoid sharp triangles and improve
336 the robustness of the segmentation, when the angle θ exceeds a threshold T_θ (maximum tolerant angle), the
337 *core* point under analysis is marked as an *invalid* surface. Otherwise, the normals of each triangle can be
338 computed, and the normal gradients at the *core* point under analysis in different directions are computed
339 with each pair of triangles in the local mesh. We further compare the largest normal gradient against a
340 threshold of $T_{\Delta\text{Norm}}$ (maximum tolerated normal gradient) to label the *core* point under analysis as a *smooth*
341 ($\leq T_{\Delta\text{Norm}}$) or *rough* surface point ($> T_{\Delta\text{Norm}}$).

342 **Point Clustering**

343 Several algorithms have been proposed to cluster points based on common attributes. For example,
344 connected components is a common approach to efficiently group linked voxels with limited constraints
345 due to the straightforward and fast neighbor searching process (Olsen et al., 2015) from the organization
346 provided by the voxelization. Meanwhile, region growing is another common point clustering method very
347 similar to connected components; however, it typically requires more constraints (e.g., difference in
348 normals), providing more flexibility (Che & Olsen, 2018). In our proposed method, we extract *smooth*,
349 *rough*, and *invalid* surfaces in order by utilizing some of the core concepts of the connected components
350 approach to segment the point cloud but with different constraints and criteria (Table 1) similar to a region
351 growing process. For each class of surfaces, the *core* points are first clustered and then mapped to their

352 nearby *core* and *accessory* points. Such a process enables high efficiency via the voxel-based neighbor
353 searching while each surface class can still be segmented based on their general geometric characteristics.

354 Specifically, we initiate the *core* point clustering by grouping the *smooth* surface *core* points. To
355 determine whether a cluster from a core point can grow to a connected one, we first compute the difference
356 of normals at these two core points (ΔNorm in Figure 5). There are cases in which points lying on different
357 surfaces have similar normal vectors. As a result, only checking the normal gradient can result in under-
358 segmentation issues where multiple surfaces can be grouped into the same segment. To cope with this
359 situation, we temporarily adjust the position the one *core* point (point B in Figure 5) under analysis along
360 the direction of the normal vector of the other point (point A in Figure 5) following the same process
361 described in Section 2.3. Next, the normal vector as well as the adjusted coordinates of point B (point B' in
362 Figure 5) can be used to define a plane. On this plane, we assume point A and point B' both lie on an arc
363 where the normal vector at B' can be computed. This yields another estimation of normal difference
364 between these two *core* points ($\Delta\text{Norm}'$). The same analysis is then applied with point B swapped for point
365 A to obtain another estimation of normal difference. Ultimately, this analysis essentially combines the
366 estimation of both curvature and the normal gradient, strengthening the robustness by providing a total of
367 three estimations of the normal gradient between points A and B. To grow from one *smooth* surface *core*
368 point to the other, all three estimations need to be equal to or less than the threshold $T_{\Delta\text{Norm}}$.

369 After clustering all of the *smooth* surface *core* points, we dismiss smaller segments if the number
370 of *core* points within a segment contains are less than a user-given parameter, T_{N_cores} . Then, for each point
371 that does not belong to a *smooth* surface segment, we first adjust and estimate the normal difference with
372 all of its neighboring *core* points, which are segmented using the same approach as the *core* points. Among
373 all the neighboring *core* points meeting the criteria of growing, we populate the point under analysis using
374 the segment ID of the one with the shortest projected distance along the normal vector. This mapping
375 approach not only groups the accessory points lying on a *smooth* surface to the nearest surface segment but
376 also groups points lying on a sharp edge of multiple surfaces.

377 To further cluster the *rough* and *invalid* surfaces, we group the *smooth* and *rough* surface *core*
378 points that have not been assigned to a segment first. The same procedure as segmenting *smooth* surfaces
379 is followed but with different criteria to determine whether a point belongs to a *rough* surface. Because a
380 *rough* surface has a larger deviation in the surface normal direction (Points D, E, and F in Figure 5), the
381 metrics that we use for *smooth* surface would over-segment the point cloud in many cases. Hence, we
382 simply compute and compare the normal difference between two points against the threshold $T_{\Delta\text{Norm}}$ to
383 preserve the *rough* surface. This result is refined by examining the number of *core* members $T_{N_{\text{Cores}}}$ which
384 can be given based on the voxel size S_v and the minimum dimension of the objects of interest in the scene.
385 Finally, all of the *core* points that have not yet been tagged with a segment ID are grouped into *invalid*
386 surface segments. The same procedures are followed where the criterion is the 3D distance, which has
387 already been embedded in the voxel-based neighbor searching, similar to connected components. The points
388 tagged to a segment that fails to meet the threshold of $T_{N_{\text{Cores}}}$ will be assigned as *unclassified* noise.

389 Lastly, some *core* points lying along the surface edges as well as some of the accessory points may
390 not yet be segmented. To map the *core* point segmentation results to these unlabeled points, we use the
391 similar criteria to determine whether an unlabeled point belongs to a segment or not. Note that because the
392 estimated normal of a point located on the edge between surfaces can be unreliable, for *smooth* surface
393 segments, we only take one estimation of the normal gradient with the known normal vector of the
394 segmented *core* point. If more than one segment meets the criteria at an unlabeled point, this point will be
395 labeled as the same with the closest labeled *core* point. The projected distance is used for *smooth* and *rough*
396 surface segments whereas the 3D distance is used for *invalid* surfaces.

397 **Experiment**

398 **Overview**

399 We tested the proposed *Vo-Norvana* segmentation both quantitatively and qualitatively with five
400 distinct datasets (Figure 6, Table 2) from different systems to examine the effectiveness and versatility of
401 the proposed method. Notably, Table 2 relates key information related to each dataset (e.g., dimensions

402 and point count) and parameters used in processing (e.g., voxel size) to several metrics for evaluating
403 processing efficiency. The first dataset consists of a single TLS scan (Leica ScanStation P40) acquired in
404 an indoor setting and captures basic geometric shapes for quantitatively evaluating and comparing the
405 quality of the segmentation results for modeling purposes. The remaining datasets are significantly larger
406 in terms of both data size and extent to evaluate the scalability and robustness of the method, including a
407 TLS dataset containing 8 scans, a MLS dataset collected by a Leica Pegasus:Two system, an ALS dataset
408 containing 20 flightlines, and a point cloud data from an uncrewed airborne system (UAS) using SfM
409 MVS photogrammetry. Note that the adjusted extent is the dimension of the data after the data is rotated
410 to align to its principal axis (Figure 2) while a voxel containing at least one data point are defined as a
411 valid voxel. All data are stored in an unorganized format, namely LASzip (i.e., LAZ), compressed from
412 the ASPRS LAS format (Isenburg, 2013; ASPRS, 2019). Additional details about each dataset and the
413 selected parameters will be discussed in the following sections. The metrics of quantifying the efficiency
414 of the proposed method (Table 2) are discussed in details in the Computational Performance section.

415 **Computational Performance**

416 The proposed algorithm was implemented using C++ with OpenMP parallel programming within
417 the Visual Studio 2019 platform. All tests were performed on a desktop computer configured with Intel
418 Xeon W-2145 CPU @ 3.70 GHz (8 cores, 16 threads) and 128 GB RAM. The processing times reported
419 in Table 2 for each dataset includes all steps (e.g., data preparation, normal estimation, voxelization,
420 segmentation, etc.) except for data I/O. To holistically evaluate the computational performance of *Vo-*
421 *Norvana*, in addition to the overall processing time, we calculate the point, voxel, and segment-based
422 performance. The point-based performance is computed using the total number of points to represent the
423 data volume, in general. Because the voxelization process simplifies the data, the spatial extent of the
424 dataset and voxel size should also be considered when analyzing processing times. We calculated the
425 voxel-based performance using the total number of valid voxels so that empty voxels were excluded.
426 Because the highest resolution voxel size is ultimately a function of the point density and scale of the
427 features to be extracted, the voxel-based performance turned out to be somewhat consistent across the

428 different datasets. It is worth noting that although a larger voxel size can increase performance, the lower
429 resolution can substantially limit the use of the data. One reason behind the lower voxel-based efficiency
430 for the TLS dataset is that it has a relatively large extent in the Z direction compared with the MLS, ALS,
431 and UAS-SfM datasets. This imbalance potentially reduces the spatial coherence when loading data into
432 the cache. Lastly, the number of segments represents the overall complexity of the scene given the voxel
433 size; hence, we calculated the segment-based performance (i.e., number of segments per second) to
434 highlight the variety of the testing data in terms of the scene complexity.

435 In summary, based on the results presented in Table 2, *Vo-Norvana* is highly efficient in
436 processing unorganized point cloud data with a wide range of complexities. In addition, the extraordinary
437 scalability of our approach is demonstrated by successful testing of datasets containing hundreds of
438 millions of points.

439 Accuracy Assessment

440 Many researchers simply report the accuracy of a segmentation method using a point-based
441 assessment using common statistical metrics such as recall, precision, F-1 score, accuracy, and so on.
442 Unfortunately, such metrics treat each point with the same weight; as a result, they can be substantially
443 biased by the segment size when a dataset is large where larger segments dominate and the finer details of
444 relatively simple segments are ignored. Thus, we assessed and analyzed the accuracy of *Vo-Norvana* by
445 evaluating fitted geometric models derived from the segmented point clouds. The reference models we
446 used are derived from the manual and *Norvana* segmentations from our prior work of the same
447 benchmark dataset (Che et al. 2018), which consists of one plane, two spheres, two cylinders and two
448 cones.

449 A voxel size of 0.01 m was used to be consistent with the analysis scale used in our prior work
450 developing *Norvana*. In *Vo-Norvana*, a local error σ_{local} of 3 mm was given based on the scanner
451 specifications. Unlike *Norvana*, *Vo-Norvana* does not have a designated step to remove mixed pixels
452 given that the scanner location is unknown due to the unorganized data format. However, we found
453 increasing the minimum and lowering the maximum neighbor angles T_0 can somewhat mitigate errors

454 caused by mixed pixels. For the comparison, the intermediate results of segmenting the *core* points as
455 well as those from the full segmentation (Figure 7) are both evaluated to demonstrate the ability of *Vo-*
456 *Norvana* to preserve geometric details with the benefits of mapping the results back to the full point cloud
457 rather than work with a down-sampled version as is common in many other works.

458 In addition to the manual and *Norvana* segmentation, we also performed segmentation via
459 *RANSAC* and *QTPS* (Zhu et al., 2021) for comparison. For both methods, we fine-tuned the settings to
460 match the parameters used in *Norvana* and *Vo-Norvana*. *RANSAC* was set to specifically detect planes,
461 cylinders, and cones from the input point cloud. It is also worth noting that we only used the *RANSAC*
462 segmentation/fitting results but not the shape recognition information because of the poor recognition that
463 occurred, especially between planes, spheres, and cylinders. The *RANSAC* segmentation produced 53
464 segments while *QTPS* segments the point cloud into 102 segments (Figure 7). Because *QTPS* was
465 developed primarily for ALS data targeting planar surfaces, it significantly over-segmented the curved
466 surfaces such that a meaningful comprehensive quantitative analysis could not be conducted for the
467 objects of interest.

468 The modeling process was then performed using the Leica Cyclone software with the *RANSAC*
469 option disabled to ensure the fitting was fully based on least squares. The error statistics are first reported
470 to validate the fitting quality of each model and method (Table 3). The mean, standard deviation, and
471 absolute mean errors among all the four approaches are mostly on par; however, the absolute maximum
472 errors for the *Vo-Norvana* results are slightly larger than, but still comparable with, the manual, *RANSAC*
473 and *Norvana* segmentation. As most of the absolute maximum errors are near the voxel size (0.01 m)
474 used in the voxelization, such differences can be largely explained by the specified scale of analysis.
475 Next, we compared the number of points in the segments for modeling which shows that the *Vo-Norvana*
476 segmentation is more similar to the manual process because both operate data in a 3D space, whereas
477 *Norvana* organizes data into a 2D scan pattern. Additionally, because *Vo-Norvana* considers the point
478 uncertainty in the process, it is less sensitive to noise compared with *Norvana* in our prior work.

479 As another approach to further assess the accuracy of the modeling results using the different
480 segmentation approaches, we compared the position, orientation, and shape of the models (Table 4). As
481 the comparison shows, the accuracy of the position and shape is mostly at the millimeter, if not sub-
482 millimeter, level while the errors in orientation are generally lower than 0.1°. These errors vary with the
483 objects because of their shapes, sizes, materials and so forth. While in this simple case, the *RANSAC*
484 segmentation yields slightly better results overall mostly due to the extra input of the target primitives,
485 *RANSAC* was unsuccessful at obtaining satisfactory results with drastic over- and under-segmentation as
486 well as requiring a very long processing time on the other datasets tested. Also note that the accuracy of
487 the *core*-only segmentation is worse than the full *Vo-Norvana* result, which demonstrates that mapping
488 the segmentation results from the voxels to all of the points helps improve the accuracy in modeling
489 applications. Nevertheless, the *core*-only segmentation result can still be sufficient for many applications
490 to provide higher computational efficiency and lower data volume, if desired.

491 **Versatility Tests**

492 We further performed *Vo-Norvana* segmentation to process four large datasets acquired by TLS,
493 MLS, ALS, and UAS-SfM to evaluate the versatility and scalability of the algorithm. These datasets
494 cover a wide range of data collection methods, scene types, and objects. We also attempted to test several
495 existing methods (e.g., *RANSAC*, *QTPS*) for comparison. Unfortunately, these approaches struggled in
496 processing the large datasets (both point counts and spatial extent) and suffered substantial over and
497 under-segmentation given the complexity of these scenes. Hence a meaningful comparison is not
498 possible.

499 *3.4.1 TLS Testing*

500 The TLS test dataset was collected near Weatherford Hall located on the Oregon State University
501 campus in Corvallis, Oregon, United States. The angular resolution of each scan is 0.02° and the
502 maximum range is 120 m. Given that this dataset contains multiple scans registered together, the reported
503 registration RMS error statistic of 6 mm is used to estimate σ_{global} . The voxel size was set as 0.05 m based
504 on our prior work while the minimum segment size was set to 50 voxels to minimize segmentation of

505 small objects. All other parameters (i.e., σ_{local} , $T_{\Delta\text{Norm}}$, $T_{\text{N_Neighbors}}$, T_0) were kept the same as the
506 benchmark test to demonstrate that the method is not highly sensitive to parameter selection (Table 2).
507 Not that this same dataset was also tested and documented in detail in our prior work (Che & Olsen,
508 2018) for comparison.

509 *Vo-Norvana* categorizes the input point cloud into four classes: *smooth* surface, *rough* surface,
510 *invalid* surface, and *unclassified* noise. For the TLS dataset (Figure 8), man-made objects such as road,
511 sidewalk, and buildings are mostly classified as *smooth* surface while the tree trunks and grass
512 categorized as *rough* surfaces. Tree branches and leaves, as well as other linear or other irregular shapes
513 are mostly tagged as *invalid* surfaces, whereas the *unclassified* noise primarily consists of small clusters.

514 Close-up views of different objects further highlight the effectiveness of the proposed approach
515 (Figure 9). For example, the architectural features (e.g., divided blocks, columns, windows, etc.) were
516 correctly segmented for the building façade (Figure 9 (A) and (B)). Note that the façade below the
517 balcony at the bottom of the building is a curved surface. Similarly, the curb face is effectively segmented
518 as a single segment (Figure 9 (B)). Additionally, several moving objects were captured during the scans
519 (e.g., vehicles, bikes, pedestrians, etc.), resulting in numerous unwanted points in the data. *Vo-Norvana*
520 effectively segmented these points into clusters such that they can be easily removed given that these
521 objects were grouped into segments mostly classified as invalid surfaces. For the trees, which vary in
522 species and sizes throughout the scene (Figure 9 (A) and (C)), the tree trunks and crowns were separated
523 into different segments because they were categorized into different classes, as discussed in the prior
524 section.

525 *MLS Testing*

526 Next, we evaluated the proposed method on an MLS dataset collected along a 1.3 km stretch of
527 road through a sub-urban area in Philomath, Oregon, United States with an average speed of 6.7 m/s and
528 an angular resolution of 0.07°. Compared to the TLS data consisting of multiple scans to cover an area,
529 MLS data typically has a lower point density, depending on the range and driving speed. Moreover, in
530 addition to the ranging and angle measurement errors of the lidar sensor itself, because the GNSS

531 receivers and Inertial Measurement Unit (IMU) provide direct georeferencing, the accuracy of MLS point
532 cloud is typically lower than TLS. As a result, we set the σ_{local} to 0.01 m based on empirical evaluation of
533 the data quality of several datasets with this specific system. The parameters $T_{\text{N_Neighbors}}$ and T_{θ} were set
534 to 3 and 150°, respectively, due to the lower point density and rare occurrence of mixed pixels in MLS
535 data.

536 The segmented results (Figure 10) show that most ground points were grouped into a single
537 segment including the road, sidewalks, and driveways except for areas further from the scanner with a
538 local point density lower than the analysis scale (e.g., black points in Figure 10 (A, B)). Similar to the
539 TLS data, the sidewalk and roadway were segmented together because they are smoothly connected via
540 the curb ramps and driveways. Although most of the curbs were separated from the roadway and
541 sidewalk, some were over-segmented into smaller sections rather than as a long stretch as in the TLS
542 testing (Figure 10 (A, C, D, E)). The primary reason is that the point density in such areas is relatively
543 low, and hence the normal estimation is less accurate. In addition to horizontal features, the vertical
544 features were accurately segmented. For example, not only were the utility poles clearly distinguished
545 from the ground, but different components (e.g., pole, ground wire, guy wire, crossarm, transformer, etc.)
546 were also be separated into their own segments (Figure 10 (A, B, C, D)), potentially supporting detailed
547 modeling and further analysis. Some utility poles appear to be over-segmented (e.g., Figure 10 (D))
548 because the secondary wires occlude the MLS system at certain angles, dividing the pole into multiple
549 sections. If the point density is sufficient on the wires and powerlines, *Vo-Norvana* can be used to extract
550 and segment these linear features, which are classified as *invalid* surface points (Figure 10 (C, D)). Signs
551 of varying sizes located at different heights were accurately segmented with the poles and boards properly
552 separated. (Figure 10 (A, B, E)). In a few cases, the sign boards were spilt into two parts at the pole
553 because only the back of the sign was captured by the MLS system.

554 *ALS Testing*

555 Very few segmentation methods are tested on both ground-based and airborne lidar datasets.
556 Hence, to validate the versatility and scalability of the *Vo-Norvana* segmentation, we tested it with a

557 massive, publicly available dataset (Laefer et al., 2017) collected in Dublin, Ireland, in 2015 (Figure 11)
558 encompassing an area of approximately 9 sq. km. More specifically, we selected all 20 flight lines on the
559 Northeast and Southwest direction from the entire dataset, comprising nearly 640 million points. A
560 typical ALS data processing workflow would partition the data into 2D tiles to make this immense data
561 volume more manageable early in and throughout the processing. While this approach is effective for
562 some processing tasks, tiling requires adding overlaps between tiles as well as additional treatments to
563 link segments across multiple tiles to ensure the consistency of the segmentation results, particularly near
564 the boundary of each tile. Since the *Vo-Norvana* segmentation establishes 3D tiles during voxelization as
565 only a temporary measure, we input the individual flight lines as separate files and processed the entire
566 test dataset directly without having to process as individual tiles. This strategy allowed us to account for
567 offsets between flightlines in the segmentation analysis compared to the typical processing approach of
568 merging data from all flightlines before tiling. The voxel size S_v was determined to be 0.35 m based on
569 the typical point density while the local error σ_{local} and global error σ_{global} were both 0.03 m according to
570 the data report (Laefer et al., 2017). We also set the minimum segment size to ensure each segment
571 occupied at least 10 voxels. The other parameters $T_{\Delta\text{Norm}}$, $T_{\text{N}_\text{Neighbors}}$ and T_θ were kept the same with
572 prior tests to be consistent. Given the vast size and complexity of this dataset, herein we will showcase
573 select smaller regions across the dataset to demonstrate the effectiveness of the proposed approach. To
574 provide some reference of the actual scene, we added the corresponding satellite images along with the
575 screenshot of the segmented point cloud.

576 First of all, the ground surface (mostly paved road or sidewalk surfaces) was segmented into a
577 couple of very large segments, demonstrating that *Vo-Norvana* can serve effectively as a ground filtering
578 approach for ALS data in an urban scene (Figures 12-14). In this case, the ground (e.g., road surface,
579 sidewalk, etc.) did not turn out to be one segment because there are railroad tracks passing through the
580 scene and splitting the road surface into two parts. Then along the river, the water surface was clustered
581 given the fact that it appeared as a *smooth* or *rough* surface in the lidar data (Figures 12 and 14). In

582 addition, the vehicles captured in the scene were not separated into individual objects (Figure 14) because
583 *Vo-Norvana* segmented the body of a car into multiple parts based on the distinct changes in geometry.

584 A variety of roof structures and types are presented in this area including flat, hip, valley, dormer,
585 dome, and others (Figure 12, 13, 15, and 16). Most of the roofs consist of planar surfaces and each face
586 was extracted as a segment. Admittedly, these simplistic roofs are relatively easy to tackle with any
587 segmentation approach where basic plane fitting can readily distinguish each face of the roof. However,
588 in contrast, the courts and church (the left and center of Figure 12) both feature a dome roof, which can be
589 very challenging to most existing methods. With *Vo-Norvana*, they were correctly segmented into a single
590 cluster while the tips were separated from the dome. Another example shows that *Vo-Norvana* also
591 managed to divide an octagonal roof to each planar face with other roof in different types and sizes
592 (Figure 16). It is also worth noting that most facets of the arched roof of the train station (Figure 15) were
593 segmented correctly with the exception of a few facets representing glass skylights that are adversely
594 impacted by the increased lidar ranging uncertainty. Nevertheless, despite these minor issues, *Vo-*
595 *Norvana* robustly copes with a variety of complex geometric surfaces throughout the scene.

596 The *Vo-Norvana* segmentation is proven to be capable of handling objects and features in a
597 variety of shapes and dimensions. The ALS dataset captures several other types of assets such as
598 streetlamps, traffic lights, and poles. Because the spatial resolution is much lower than typical TLS and
599 MLS data, the points lying on these objects were classified as *invalid* surfaces but were still segmented
600 properly (Figure 14). Similarly, the guard rails on the bridge were also clustered into a segment. In
601 addition to the infrastructure, tree crowns can be also of interest in the ALS point cloud, and *Vo-Norvana*
602 can be used to reliably distinguish individual trees within the point cloud. The points representing the tree
603 crowns were classified as *invalid* surface points, and each was typically clustered into a single large
604 segment; however, sometimes they were subdivided into a few smaller segments that can be grouped with
605 further process (Figures 12 and 13).

606 *UAS-SfM Testing*

607 Lastly, we rigorously tested *Vo-Norvana* segmentation on a UAS-SfM point cloud, which tends
608 to be noisier compared with the TLS data. These data were collected from a historic paper mill next to the
609 Willamette Falls in Oregon City, Oregon, United States (Bresky, 2016) using a DJI Phantom 4 RTK UAS
610 with approximately 10 ground control points observed with GNSS and processed against a base station.
611 The post-processing was performed in Agisoft Metashape, providing a typical point spacing in the dense
612 point cloud of approximately 0.05 m. It is worth noting that even though multiple flightlines with
613 significant overlap were planned and flown to cover the area of interest, unlike the airborne lidar, the
614 point cloud itself cannot be divided into individual flightlines given that the SfM process requires data
615 from overlapping flightlines be combined to reconstruct the point cloud via bundle adjustment. As a
616 result, we considered the UAS-SfM point cloud as a single, merged point cloud and did not apply σ_{global}
617 while setting σ_{local} to 0.01 m based on the residuals at ground control points. The other parameters were again
618 kept as consistent as possible with the other tests. *Vo-Norvana* yielded a quick but robust segmentation of
619 various features in the scene (Figure 17). For example, the hydroelectric dam (Figure 17 (A)) was
620 captured in the point cloud and segmented into different parts. In the paper mill, several storage tanks
621 with spherical or cylindrical shapes of different sizes were cleanly extracted (Figure 17 (B, C)). The
622 performance of the proposed segmentation of the roofs was robust (Figure 17 (D)) and similar to the
623 result of ALS testing discussed in the prior section.

624 **Summary**

625 In the experiment, we tested a total of five different point cloud datasets including a TLS
626 benchmark dataset, an outdoor TLS dataset collected in the university campus, an MLS dataset captured
627 in a suburban area, an ALS dataset covering an entire city in a high resolution, and a UAS-SfM point
628 cloud acquired from an industrial site. We first evaluated the computational performance of the *Vo-*
629 *Norvana* segmentation considering the number of points, data extent, and scene complexity (e.g., number
630 of segments). By exploiting parallel programming (8 cores, 16 threads), the largest dataset (ALS)
631 containing nearly 640 million points can be segmented within 50 minutes without any pre-processing.
632 Then, we assessed the accuracy of *Vo-Norvana* quantitatively by comparing its modeling results to two

633 existing automated methods as well as manually derived results. The average differences of the position,
634 orientation, and dimension between the models generated from *Vo-Norvana* and manual segmentation are
635 0.0027 m, 0.0830°, and 0.0009 m, respectively, which indicates minimal difference between the methods.
636 Finally, we demonstrated the versatility of the proposed framework on TLS, MLS, ALS, and UAS-SfM
637 datasets. The results show that *Vo-Norvana* segmented these point clouds effectively and efficiently with
638 relatively consistent parameter settings. Because each parameter has a clear physical meaning, it is
639 straightforward for users to give proper values based on the data quality, target objects, level of detail
640 desired, and other factors. The high computational performance also enables efficient parameter fine-
641 tuning when needed.

642 Conclusion

643 This paper introduces a novel point cloud segmentation framework, *Vo-Norvana*, based on a
644 specialized voxelization technique that can preserve geometric details to a large degree. *Vo-Norvana*
645 consists of three primary steps, data organization, Normal Variation Analysis (*Norvana*), and point
646 clustering and provides segment IDs and classes to unorganized point cloud automatically. *Vo-Norvana*
647 was tested on a diverse range of datasets and scenes including terrestrial lidar, mobile lidar, airborne lidar,
648 and UAS-SfM. The data volume ranges from about 1.3 million points in a laboratory setting to nearly 640
649 million points at a city-wide scale. The segmentation results were evaluated and discussed both
650 qualitatively and quantitatively. Key highlights observed with the proposed approach are as follows:

- 651 1. Unlike most existing methods, *Vo-Norvana* is not limited to pre-defined geometric primitives
652 such that it can cope with a variety of shapes in different sizes to complete the segmentation
653 for general purposes. The automated modelling results derived from the segmented point
654 cloud can satisfy most applications.
- 655 2. *Vo-Norvana* also can consider the positional uncertainty of the data both locally and globally,
656 reducing improper segmentation results from noise when combining scans or flightlines from
657 different locations.

658 3. By being designed to effectively take advantage of parallel programming, *Vo-Norvana*
659 consistently achieves a computational performance on the order of hundreds of thousands of
660 points or tens of thousands of voxels per second on a desktop computer. This efficiency holds
661 even when processing hundreds of millions of points that cover an entire city at a time,
662 demonstrating the outstanding scalability of the *Vo-Norvana* framework.

663 4. The versatility of the proposed approach was proven through extensive tests on point cloud
664 data collected from different scenes (e.g., architecture, sub-urban, urban, industry) using a
665 wide range of systems (e.g., ground and aerial-based, lidar and SfM-based) with relatively
666 consistent parameter settings which does not require extensive fine-tuning.

667 Although not directly demonstrated in this manuscript due to scope, the point cloud segmentation
668 results can be improved by combining multiple iterations of *Vo-Norvana* with different parameter settings
669 to perform a multi-scale analysis considering the objects of interest and adapting to the variable point
670 density within the scene. Such results can directly benefit semantic segmentation by feeding rich
671 information extracted from each segment determined at several different scales. We are currently utilizing
672 *Vo-Norvana* to enable efficient feature extraction, classification, modelling, and other applications, as
673 well as performing additional quantitative assessments of accuracy. For example, in our recent work, we
674 applied the proposed segmentation approach as a pre-processing tool to separate walls, floors, ceilings,
675 furniture, and other objects for supporting the Scan-to-BIM process including the 2D floor plan
676 generation and 3D modelling (Baru et al., 2022). In the future, we plan to leverage the *Vo-Norvana*
677 framework in developing novel machine learning and deep learning approaches due to its efficiency and
678 scalability.

679 **Data Availability Statement**

680 Some data, models, or code that support the findings of this study are available from the
681 corresponding author upon reasonable request (benchmark, TLS, and UAS-SfM datasets). Some data,
682 models, or code used during the study were provided by a third party (MLS dataset). Direct requests for

683 these materials may be made to the provider as indicated in the Acknowledgements. Some data, models,
684 or code generated or used during the study are available in a repository online in accordance with funder
685 data retention policies (ALS dataset, available at https://geo.nyu.edu/catalog/nyu_2451_38684).

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696 **Conflict of Interest**

697 The authors Dr. Che and Dr. Olsen have financial interests in EZDataMD LLC, a company which
698 commercializes the technology related to this research. The conduct, outcomes, or reporting of this
699 research could benefit EZDataMD LLC and could potentially benefit the authors.

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Table 1. Summary of the proposed point clustering approach for different types of surfaces.

Surface Class	Neighbor Searching	Member <i>Core</i> Points	Clustering Criteria / Thresholds	Segment Criteria
<i>Smooth</i>	<i>Core</i> points from 26 neighboring voxels	<i>Smooth</i>	Normal gradient (3 estimations) $T_{\Delta\text{Norm}}$	Number of <i>core</i> members T_{N_Cores}
<i>Rough</i>		<i>Unclustered Smooth</i> + <i>Rough</i>	Normal gradient (1 estimation) $T_{\Delta\text{Norm}}$	
<i>Invalid</i>		<i>All remaining</i>	3D distance	

817 *Table 2. Key information (e.g., dimensions, errors), parameters, and processing efficiency for the*
 818 *datasets used in the experimentation. The efficiency is reported in four metrics: processing time,*
 819 *point-based, voxel-based, and segment-based performance.*

Key Information and Parameters	Benchmark	TLS	MLS	ALS	UAS-SfM
Number of scans/flight lines	1	8	1	20	1
Number of points	1,205,600	391,764,131	75,657,595	639,309,547	79,541,367
Number of valid voxels	96,655	18,688,805	23,933,223	105,012,969	17,596,719
Adjusted X extent (m)	3.0	289	1,367	2,818	344
Adjusted Y extent (m)	4.0	290	486	3,095	704
Adjusted Z extent (m)	3.0	44	153	518	60
Voxel size S_v (m)	0.010	0.050	0.050	0.350	0.100
Local error σ_{local} (m)	0.003	0.003	0.010	0.030	0.010
Global error σ_{global} (m)	-	0.006	-	0.030	-
Min segment size T_{N_cores}	100	50	50	10	10
Max normal gradient $T_{\Delta\text{Norm}}$ (degree)	15	15	15	15	15
Min neighbor $T_{N_Neighbors}$	8	8	3	3	3
Max neighbor angle T_θ (degree)	90	90	150	150	150
Number of segments	56	16,435	28,490	979,668	18,762
Processing time (s)	3	1,030	633	2,929	347
Point-based performance (million points per second)	0.402	0.380	0.120	0.218	0.229
Voxel-based performance (million valid voxels per second)	0.032	0.018	0.038	0.036	0.051
Segment-based performance (segments per second)	19	16	45	334	156

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822 *Table 3. Summary of the quality of the model fitting statistics from the Manual, RANSAC,*
 823 *Norvana, Vo-Norvana (Core) and Vo-Norvana (Full). Note that the Manual and Norvana results*
 824 *were reported in Che & Olsen (2018) while RANSAC modeling was conducted in*
 825 *CloudCompare.*

Object	Approach	Error Statistics (m)				# of Points
		Mean	Std. Dev.	Abs. Mean	Abs. Max.	
Plane	<i>Manual</i>	0.0000	0.0013	0.0011	0.0047	132,983
	<i>RANSAC</i>	0.0000	0.0014	0.0011	0.0069	133,485
	<i>Norvana</i>	0.0000	0.0013	0.0010	0.0044	126,435
	<i>Vo-Norvana (Core)</i>	0.0000	0.0014	0.0011	0.0092	6,989
	<i>Vo-Norvana (Full)</i>	0.0000	0.0014	0.0011	0.0102	132,836
Sphere1	<i>Manual</i>	0.0000	0.0022	0.0018	0.0091	119,872
	<i>RANSAC</i>	0.0000	0.0023	0.0019	0.0089	123,019
	<i>Norvana</i>	0.0000	0.0022	0.0018	0.0091	117,257
	<i>Vo-Norvana (Core)</i>	0.0000	0.0025	0.0021	0.0080	9,696
	<i>Vo-Norvana (Full)</i>	0.0000	0.0023	0.0019	0.0092	122,153
Sphere2	<i>Manual</i>	0.0000	0.0010	0.0008	0.0048	40,109
	<i>RANSAC</i>	0.0000	0.0011	0.0008	0.0091	42,132
	<i>Norvana</i>	0.0000	0.0010	0.0007	0.0060	39,200
	<i>Vo-Norvana (Core)</i>	0.0000	0.0013	0.0010	0.0056	3,660
	<i>Vo-Norvana (Full)</i>	0.0000	0.0010	0.0008	0.0055	41,897
Cylinder1	<i>Manual</i>	0.0000	0.0002	0.0002	0.0018	4,661
	<i>RANSAC</i>	0.0000	0.0003	0.0002	0.0017	4,625
	<i>Norvana</i>	0.0000	0.0004	0.0003	0.0014	3,595
	<i>Vo-Norvana (Core)</i>	0.0000	0.0003	0.0003	0.0015	265
	<i>Vo-Norvana (Full)</i>	0.0000	0.0003	0.0002	0.0016	4,614
Cylinder2	<i>Manual</i>	0.0000	0.0004	0.0003	0.0017	11,890
	<i>RANSAC</i>	0.0000	0.0005	0.0004	0.0027	12,285
	<i>Norvana</i>	0.0000	0.0004	0.0003	0.0017	5,668
	<i>Vo-Norvana (Core)</i>	0.0000	0.0012	0.0006	0.0131	1,145
	<i>Vo-Norvana (Full)</i>	0.0000	0.0010	0.0005	0.0173	12,719
Cone1	<i>Manual</i>	0.0000	0.0006	0.0004	0.0028	34,298
	<i>RANSAC</i>	0.0000	0.0006	0.0005	0.0048	35,144
	<i>Norvana</i>	0.0000	0.0005	0.0004	0.0025	30,881
	<i>Vo-Norvana (Core)</i>	0.0000	0.0007	0.0006	0.0044	2,192
	<i>Vo-Norvana (Full)</i>	0.0000	0.0006	0.0005	0.0053	35,161
Cone2	<i>Manual</i>	0.0000	0.0006	0.0005	0.0026	15,428
	<i>RANSAC</i>	0.0000	0.0007	0.0005	0.0062	16,108
	<i>Norvana</i>	0.0000	0.0005	0.0004	0.0062	13,329
	<i>Vo-Norvana (Core)</i>	0.0000	0.0008	0.0006	0.0045	1,062
	<i>Vo-Norvana (Full)</i>	0.0000	0.0006	0.0005	0.0059	15,445

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828 *Table 4. Comparison of the modeling results using the RANSAC, Norvana, Vo-Norvana (Core) and Vo-*
 829 *Norvana (Full) compared with the manually extracted results.*

Object	Approach	Difference against manual modeling results		
		Position (m)	Orientation (°)	Shape (m)
Plane	<i>RANSAC</i>	0.0027	0.0090	-
	<i>Norvana</i>	0.0031	0.0069	-
	<i>Vo-Norvana (Core)</i>	0.0101	0.0148	-
	<i>Vo-Norvana (Full)</i>	0.0036	0.0123	-
Sphere1	<i>RANSAC</i>	0.0002	-	0.0003
	<i>Norvana</i>	0.0001	-	0.0000
	<i>Vo-Norvana (Core)</i>	0.0014	-	0.0015
	<i>Vo-Norvana (Full)</i>	0.0001	-	0.0001
Sphere2	<i>RANSAC</i>	0.0002	-	0.0002
	<i>Norvana</i>	0.0004	-	0.0008
	<i>Vo-Norvana (Core)</i>	0.0006		-0.0006
	<i>Vo-Norvana (Full)</i>	0.0001	-	-0.0001
Cylinder1	<i>RANSAC</i>	0.0003	0.1365	-0.0005
	<i>Norvana</i>	0.0015	0.7468	-0.0006
	<i>Vo-Norvana (Core)</i>	0.0019	0.1146	-0.0006
	<i>Vo-Norvana (Full)</i>	0.0022	0.0845	-0.0004
Cylinder2	<i>RANSAC</i>	0.0005	0.0044	0.0000
	<i>Norvana</i>	0.0039	0.0152	0.0021
	<i>Vo-Norvana (Core)</i>	0.0023	0.0179	0.0009
	<i>Vo-Norvana (Full)</i>	0.0023	0.0227	0.0009
Cone1	<i>RANSAC</i>	0.0093	0.1308	0.0010
	<i>Norvana</i>	0.0105	0.1776	-0.0031
	<i>Vo-Norvana (Core)</i>	0.0246	0.3797	0.0025
	<i>Vo-Norvana (Full)</i>	0.0061	0.0889	0.0011
Cone2	<i>RANSAC</i>	0.0060	0.2528	0.0042
	<i>Norvana</i>	0.0090	0.1509	0.0000
	<i>Vo-Norvana (Core)</i>	0.0078	0.4410	0.0025
	<i>Vo-Norvana (Full)</i>	0.0045	0.2066	0.0030

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831 **Figure 1.** Workflow of *Vo-Norvana* framework for point cloud segmentation.

832 **Figure 2.** Example of the proposed PCA alignment and 3D tiling approach to optimize the partitioning of
833 mobile lidar data

834 **Figure 3.** Simplified 2D schematic of the proposed voxelization and subsampling approach.

835 **Figure 4.** Schematic illustrating proposed core point Norvana where point #0 (yellow) is the point under
836 analysis while the others are its 8 neighboring core points. The two graphs in the center show the
837 side view and top view of the points in the projected coordinate system of point #0. In the side
838 view, parameter σ (i.e., σ_{local} or σ_{global}) depending whether the neighboring point and point #0 are
839 from the same source or not) represents the positioning uncertainty of a point with respect to
840 point #0. From the top view, point #8 is removed from the analysis to reduce the sensitivity of the
841 proposed analysis to the noise. The graph on the right shows the process of generating a mesh
842 where the angle θ at point #0 for each triangle cannot be larger than T_θ .

843 **Figure 5.** Growing process for smooth surface and rough surface where point A and B are both classified
844 as smooth surface core points while point D, E, F are classified as rough surface points. In the
845 process of growing from point A to B, two of the three estimations of the normal difference
846 between these two points are shown in the figure where point B' is the adjusted position for point
847 B with the given parameter σ (i.e., σ_{local} or σ_{global}) while the third estimation is obtained in a
848 similar way with $\Delta\text{Norm}'$ by adjusting point A along the normal of point B. When clustering
849 points on smooth and rough surfaces, the estimations of normal differences are compared against
850 the user parameter $T_{\Delta\text{Norm}}$.

851 **Figure 6.** Overview of the lidar datasets used in the experiment, including the Benchmark, TLS, MLS,
852 ALS, and UAS SfM/MVS data.

853 **Figure 7.** Segmentation results from the benchmark data with RANSAC, QTPS, core points only and full
854 dataset with *Vo-Norvana* where each randomly assigned color represents a unique segment and
855 unclassified points are colored in black.

856 **Figure 8.** Feature classification and segmentation result for TLS data where each distinct color
857 (randomized) represents a unique segment. Unclassified points are colored in black. Subplots
858 show smooth, rough, invalid and unclassified points.

859 **Figure 9.** Close-up views of the segmentation result on the TLS dataset where each color represents a
860 unique distinct segment. Unclassified points are colored in black. Close-ups are shown for the
861 building façade (A) to highlight the ability to segment complex architectural details, a busy street
862 (B) with noise from pedestrians and vehicles to highlight the usefulness for noise removal, and
863 segmentation of individual tree canopies (C).

864 **Figure 10.** Segmentation result of the MLS testing dataset where each color represents a unique distinct
865 segment. Unclassified points are colored in black. Close-ups show the detailed segmentation of a
866 variety of urban objects including buildings (A and C), poles (A, B, C, and D), powerlines (C and
867 D), signs (A, B, and E), curbs (C, D, and E), and the road surface (A, B, C, D, and E).

868 **Figure 11.** Segmentation results for the ALS test dataset where each distinct color represents a unique
869 segment. Unclassified points are colored in black. Locations of closeup views for details shown in
870 Figure 12 - 16 are identified.

871 **Figure 12.** Close-up view of the segmented point cloud and reference satellite images near Four Courts
872 (left) and Adam & Eve's Church and St. Audoen's Church (right) where multiple types of roofs
873 are successfully segmented. Numbers show common points between the photograph and point
874 cloud for reference.

875 **Figure 13.** Close-up view of the segmented point cloud and reference satellite image near
876 Communications Workers' Union consisting of trees, road, and buildings (roof).

877 **Figure 14.** Close-up view of the segmented point cloud and reference street view images at Talbot
878 Memorial Bridge where the pole-like objects in different sizes are segmented into individual
879 objects. The objects highlighted include street lamps (a, b, e) and traffic lights (c, d).

880 **Figure 15.** Close-up view of the segmented point cloud and reference satellite image at Pearse Station
881 and St Andrew's Roman Catholic Church where a variety of complex buildings present in the
882 scene.

883 **Figure 16.** Close-up view of the segmented point cloud and reference satellite image at Technological
884 University Dublin and Seetec jobpath Bishops Square where the roofs consist of a variety of
885 shapes.

886 **Figure 17.** Segmentation result of the UAS-SfM testing data where each distinct color represents a unique
887 segment. Unclassified points are colored in black. The close-up views include: (A) a
888 hydroelectric dam (the photograph is from the source UAS imagery dataset); (B) cylindrical and
889 spherical storage tanks in different sizes; (C) a cylindrical storage tank; (D) various types of
890 building roofs. Numbers show common points between the photograph and point cloud for
891 reference.

892