

1 **Solute and Precipitate Effects on Ce-containing Mg Alloy Dynamic Recrystallization Kinetics**

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30 Abstract

31 Composition variations in precipitate and solute content of ZK60 Mg alloys, with Zn variations and Ce
32 substitutions, impact dynamic recrystallization (DRX) behavior, microstructure, and mechanical
33 properties. A constitutive model was developed based on hot compression testing at various strain rates
34 and temperatures, quantifying the relationship between temperature, strain rate and imposed strain. Ce
35 additions are shown to impede DRX kinetics more than Zn. Texture weakening is observed in post-DRX
36 microstructures and varies based on composition.

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61 MANUSCRIPT BODY

62 ZK60 alloys are known to have high mechanical strength relative to other Mg alloys. Low melting point
63 precipitates, such as Mg_3Zn_7 in Mg-Zn-Zr alloys, can cause incipient melting during thermomechanical
64 processing if temperatures are too high. The substitution of rare earth elements, such as Ce, for Zr
65 allows for the formation of higher melting point precipitates, improving elevated temperature
66 properties and higher temperature processing windows. Ce additions are also known to enhance
67 corrosion resistance, improve creep resistance, and ultimately accelerate dynamic recrystallization (DRX)
68 [1]. Conventional Mg alloys exhibit improved formability at higher temperatures when non-basal slip
69 systems are activated, further facilitating dislocation slip. In this way, DRX during processing is a
70 powerful way to improve grain structure and resultant mechanical properties.

71 Internal stored energy accumulates during slip deformation, while DRX reduces stored energy.
72 Continuous DRX (CDRX) at rotated lattice regions in the area of grain boundaries is the dominant DRX
73 mechanism in Mg alloys. The CDRX mechanism is known to occur via subgrain rotation during
74 compressive deformation in the temperature range of 250-500°C [2]. There is limited knowledge about
75 the formation of preferred crystallographic orientations in Mg alloys due to other possible deformation
76 mechanisms, such as discontinuous DRX (DDRX) and twin DRX [3]. DDRX occurs by prior grain boundary
77 protrusion toward surrounding, high dislocation density grains, while twin DRX occurs at twin
78 intersections or fragments. In alloys with rare earth elements, particle-stimulated nucleation (PSN) in
79 the vicinity of second phase particles has also been shown to occur [4]. Texture weakening in Mg alloys has
80 been associated with PSN, as well as other phenomena including particle pinning, solute drag, and
81 heterogeneous deformation promoting shear band formation [4]. Alloying with rare earth elements,
82 such as Ce, can increase both strength and ductility, while reducing crystallographic texture.

83 Creating constitutive models of the DRX process in various Mg alloys can help guide processing to
84 efficiently create products with desirable microstructures. Fu et al. studied DRX mechanisms in Mg-Zn-
85 Mn alloys microalloyed with Sm, La, and/or Ca and determined that DDRX and PSN mechanisms
86 weakened the basal texture [5]. The occurrence of CDRX was observed by Xu et al. in a Mg-13Gd-4Y-
87 2Zn-0.5Zr (wt%) alloy during compression-torsion deformation at 450°C. It was also determined that
88 strain rate affects dominant DRX mechanisms [6]. Mg alloy properties are highly dependent on the
89 relationship between specific rare earth elements and the dominant DRX mechanisms.

90 Calculation of hot flow stress and DRX can give insight into ideal processing conditions. Flow stress is a
91 parameter that characterizes mechanical properties during hot deformation and is dependent on
92 deformation temperature, strain rate, and strain [7]. In modeling strain hardening and DRX during hot
93 deformation, it is essential to investigate both process parameters and deformation mechanisms. There
94 are multiple avenues to model flow stress for hot deformation that have been developed over the years.
95 Hollomon developed a mechanical equation at small plastic strains [8]. Subsequently, Mecking and
96 Kocks considered microstructural evolution and mechanical properties and determined that structural
97 parameters such as dislocation density can describe DRX flow curves [9]. For Mg alloys, it is
98 characteristic for flow stress to increase with strain due to work hardening, then decrease after it
99 reaches the peak as DRX occurs at a critical strain [7]. This study focuses on analyzing DRX and strain
100 hardening and calculating the critical stress for DRX to occur.

101 The alloy used for this study is a modified ZK60 (Mg-Zn-Zr) composition, with deliberate variations in Zn
102 levels and a replacement of Ce for Zr in various amounts. It is an extrusion alloy that experiences

103 precipitation hardening and exhibits a finer microstructures after solidification, hot working, or
104 annealing processes. The composition matrix is separated into 3 levels of Zn, varying the hypothesized
105 solute volume, and 3 levels of Ce, varying the hypothesized precipitate volume (electronic
106 supplementary table S1). The variations in Zn and Ce within these alloys result in changes to second
107 phase insoluble particle type, volume fraction, and distribution. ZK60 is ideally suited for this study,
108 because it is a commercial alloy with insoluble Mg-Zr precipitates that influence DRX kinetics and
109 texture. The samples for this study were machined into small cylindrical compression specimens with a
110 diameter of 10 mm and a height of 15 mm, with the cylinder height longitudinal to the extrusion
111 direction.

112 Electron backscatter diffraction (EBSD) was completed on all alloys and processing conditions. After
113 compression testing, each sample was mounted, ground, and polished to 0.05 μm colloidal silica and
114 etched after each polishing step in a solution of 4.2g picric acid, 70 mL ethanol, 10 mL glacier acetic acid,
115 and 10 mL deionized water, for 10 s [12]. The polished surface for these samples was longitudinal to the
116 compression direction. EBSD mapping analysis was performed with a 20 kV electron beam, 18 mm
117 working distance, and 2 μm step size. Each inverse pole figure (IPF) map was processed with Neighbor
118 Pattern Averaging & Indexing (NPAR) in the Orientation Imaging Microscopy (OIM) software.

119 Uniaxial compression tests on small cylindrical samples of each of the five alloys was conducted on a
120 Gleeble 3500 thermal-mechanical simulator. All samples were compressed to a final true strain of 0.8
121 and were deformed at approximate engineering strain rates of 0.001, 0.01 and 0.1 s^{-1} at either 350 or
122 400°C. One set of thermocouples was welded on the surface at half height of each sample and used to
123 monitor temperature throughout the test. The samples were lubricated at the surface of each anvil with
124 layers of Ni paste and grafoil. Each sample was heated at 5°C/s under force control to the deformation
125 temperature (350 or 400°C), held in displacement control for 30 s to ensure the temperature
126 throughout the sample was homogenous, deformed to approximately 0.8 true strain and quenched with
127 compressed air (electronic supplementary figure S1). Load-displacement data was obtained from the
128 compression tests and converted to true stress-true strain using standard conversion equations. This
129 data gives way to analysis of flow behavior and microstructural characterization.

130 True stress-strain curves for all five alloys tested at all processing conditions are presented in electronic
131 supplementary figure S2. In general, the flow stress increases to a maximum, then decreases to a steady
132 state when DRX is present. This maximum flow stress is the peak flow stress used through DRX modeling
133 and calculations. At higher strain rates, flow stress increases to a high peak stress, then exhibits
134 moderate work softening. At medium strain rates, flow stress increases to a moderate peak stress, with
135 negligible work softening. At low strain rates, there is a small peak stress and strain, and negligible work
136 softening. This is characteristic of DRX behavior for Mg alloys [7]. A flow stress curve is normally
137 separated by a work-hardening stage, transition stage, softening stage and steady stage. A greater true
138 stress is required for DRX in alloys processed at lower temperatures.

139 The onset of DRX can also be identified phenomenologically from the inflection point in the strain
140 hardening rate versus flow curve [9]. The critical stress identified from strain hardening rate graphs
141 identifies the onset of DRX and occurs lower than the peak stress. A third order polynomial, equation 1,
142 is fit to each true stress-strain curve up to the peak stress. A third order polynomial effectively fits data
143 with prolonged and multiple peaks.

$$\theta = A\sigma^3 + B\sigma^2 + C\sigma + D$$

144 (1)

145 where $\theta = \frac{d\sigma}{d\epsilon}$ and constants A, B, C and D allow for calculations of certain DRX conditions. When this
146 equation is differentiated,

$$147 \frac{d\theta}{d\sigma} = 3A\sigma^2 + 2B\sigma + C$$

148 (2)

149 The minimum point of this derivative equation correlates to the critical stress.

150 The validity of these equations in comparison to models of expected DRX behavior is confirmed by
151 Najafizadeh et al. in analysis of 304H stainless steel [10]. Calculation of critical stress according to the
152 derivative goes as follows:

$$153 \frac{d^2\theta}{d\sigma^2} = 0 \rightarrow 6A\sigma_c + 2B = 0 \rightarrow \sigma_c = \frac{-B}{3A}$$

154 (3)

155

156 Each θ/σ polynomial relation and associated σ_c are tabulated and utilized to determine the Zener-
157 Hollomon parameter (electronic supplementary table S2). The activation energy can also be determined
158 by equations for the Zener-Hollomon parameter, Z [11]:

$$159 \dot{\epsilon} = A_1\sigma^{n_1} = A_2 \exp(\beta\sigma) = A(\sinh(\alpha\sigma))^n \exp\left(-\frac{Q}{RT}\right)$$

160 (4)

$$161 Z = \dot{\epsilon} \exp\left[\frac{Q_{def}}{RT}\right] = A(\sinh(\alpha\sigma))^n$$

162 (5)

$$163 Q_{def} = R \left[\frac{\partial \ln \dot{\epsilon}}{\partial \ln(\sinh(\alpha\sigma))} \right]_T * \left[\frac{\partial \ln \sinh(\alpha\sigma)}{\partial \left(\frac{1}{T}\right)} \right]_{\dot{\epsilon}}$$

164 (6)

165 where Q_{def} is the deformation activation energy, R is the gas constant (8.314 J/mol K), σ is flow stress, T
166 is the deformation temperature, n, A_1 , β , A_2 , and α are material constants. A graph of peak stress (σ_p)
167 for each alloy versus temperature displays that increases in Zn content increases σ_p that occurs before
168 DRX (electronic supplementary figure S3). The effect of strain rate on σ_p was also analyzed and increases
169 in strain rate require increased σ_p during DRX. This increase is relatively linear, due to the direct
170 relationship between σ_p and strain rate. The value of n_1 is obtained from the linear regression of $\ln \dot{\epsilon} - \sigma_p$
171 using equation 4 [11] (electronic supplementary figure S4). The values of β are determined by the slope
172 of the linear regression of $\ln \dot{\epsilon} - \ln \sigma_p$. The values of n_1 , β , and α values ($\alpha = \beta/n_1$) are determined
173 (electronic supplementary table S3). From these values, it is essential to calculate activation energy, Q,
174 for DRX. The linear slope of $\ln \dot{\epsilon}$ vs. $\ln[\sinh(\alpha\sigma)]$, varied by temperature is the left side of equation 5. The
175 linear slope of $\ln[\sinh(\alpha\sigma)]$ vs. $1/T$ at different strain rates is the right side of equation 6. The Q value for
176 each $\dot{\epsilon}$ and T is calculated to further determine Z values, as presented in electronic supplementary table
177 S2 and shown graphically in electronic supplementary figure S4. Q increases with Zn content, and
178 similarly but to a lesser degree with Ce content. The average Q for the LZ-0.4Ce alloy is 81.9% less than
179 the average Q for the HZ-0.3Ce alloy. The average Q for HZ-0Ce is 69.5% less than the average Q for HZ-
180 0.3Ce.

181 Z values are calculated based on $\dot{\epsilon}$, Q, R and T of each, as set up in equation 5, and are shown in
182 electronic supplementary table S3. This Zener-Hollomon parameter describes the effect of both strain
183 rate and temperature on flow stress. For Mg alloys there is a linear relationship between flow stress and

184 the Zener-Hollomon parameter [11]. The linear relationship for each of alloy is determined (electronic
185 supplementary figure S5) and utilized to determine a constitutive equation describing DRX kinetics. The
186 stress exponent (n) and constant A are determined from the linear regression of each dataset (electronic
187 supplementary table S3). The constitutive equation can be modeled using tabulated values in the
188 format:

$$\sigma_p = \frac{1}{\alpha} \left(\left(\frac{Z}{A} \right)^{\frac{1}{n}} + \left(\frac{Z}{A} \right)^{\frac{2}{n}} + 1 \right)^{\frac{1}{2}}$$

189 (7)

190 An additional relation between Z and σ_p based on the linear regression of the two is determined for each
191 alloy, accounting for the stress exponent, n, and constant A (electronic supplementary table S4). Similar
192 modeling methods has been deemed accurate for thermomechanically processed Mg alloys, specifically
193 a T-4 treated ZK60 Mg alloy by Yu. et.al [11]. The model shows more variation for samples processed at
194 high strain rates and lower temperatures, meaning that DRX processes are less predictable under these
195 conditions and should be avoided in industrial processing. Samples with higher Zn content, as well as
196 higher Ce content, have slower DRX and require more energy for the process to begin.

197 Texture weakening is observed after DRX (electronic supplementary figure S6). The red colored grains
198 are basal grains, whereas the blue/green grains are non-basal grains. The basal texture weakens and the
199 non-basal texture is preferential, with the exception of some basal areas throughout the sample. There
200 are some long, elongated and un-recrystallized grains in certain areas where DRX did not occur. Many of
201 these grains were near-basal oriented, potentially due to less slip in these regions. Zener pinning and
202 solute drag have an effect on how significantly DRX occurs throughout the microstructure, and increased
203 amounts of Zn and Ce cause less homogenous post-DRX texture, due to areas with previously
204 inhomogeneous solute distribution. This observance is particularly prevalent in the HZ-0.3Ce and HZ-0.1
205 Ce alloys. An increase in strain in these compression tests, especially at lower temperatures, causes
206 increased inhomogeneous texture.

207 The DRX kinetics during compression testing at elevated temperatures and resultant microstructural
208 properties in a set of designed Mg-Zn-Ce alloys were investigated in this study to give further insight into
209 the effect of varying solute and precipitate content. The following conclusions were determined.

- 210 1. Ce additions impede DRX kinetics to a greater extent than Zn additions, per wt.% increase. Ce
211 additions dramatically increase precipitate fraction and Zener pinning, while Zn additions
212 primarily increase solute drag. Zener pinning, by this reasoning, has a greater impact on
213 retarding DRX kinetics than solute drag. The activation energy, Q, is lowest for the HZ-0Ce alloy,
214 but is the highest for the HZ-0.3Ce alloy because of this.
- 215 2. The determined constitutive equations for the DRX process reflect the activation energy and
216 effective Zener-pinning effect in each alloy and can be used to determine industrially relevant
217 processing parameters, given different processing conditions.
- 218 3. The σ_p , determined via flow curves, and σ_c , determined through calculations, are an accurate
219 representation of DRX initiation. Q and σ_p are directly correlated, and σ_p is greater for alloys
220 with greater Ce additions and Zn content. Greater dependence on Ce additions is observed than
221 for Zn additions.

222 4. Texture weakening and randomization is prevalent in the microstructure after DRX. A less
223 homogenous basal texture is observed with increases in Zn, higher strain rates and lower
224 temperatures.
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