

Improved ionization potential of calcium using frequency-comb-based Rydberg spectroscopy

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We report frequency-comb-based measurements of Ca Rydberg energy levels. Counterpropagating laser beams at 390 and 423 nm excite Ca atoms from the $4s^2 \ ^1S_0$ ground state to $4s n \ ^1S_0$ Rydberg levels with n ranging from 40 to 110. Near-resonant two-photon two-color excitation of atoms in a thermal beam makes it possible to eliminate the first-order Doppler shift. The resulting line shapes are symmetric and Gaussian. We verify laser metrology and absolute accuracy by reproducing measurements of well-known transitions in Cs, close to the fundamental wavelengths of our frequency-doubled Ti:sapphire lasers. From the measured transition energies we derive the ionization potential of Ca, $E_{IP} = 1478\,154\,283.42 \pm 0.08$ (statistical) ± 0.07 (systematic) MHz, improving the previous determinations by a factor of 11.

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I. INTRODUCTION

Spectroscopy of Rydberg atoms finds applications in a number of areas. These include quantum information [1–3], detection of rare isotopes [4], atomic structure calculations [5,6], rf field detection [7,8], and many-body dynamical studies [9–11]. These applications, as well as many others, exploit the Rydberg atoms’ extreme sensitivity to electric and magnetic fields.

In a low-density field-free environment, the energy-level structure of unperturbed Rydberg atoms is straightforward. The Ritz formula [12] predicts energy levels

$$E_n = E_{IP} - \frac{R}{[n - \delta(n)]^2}, \quad (1)$$

where E_n is the energy of the level with a principle quantum number of n , E_{IP} is the ionization potential of the atom, R is the Rydberg constant with a finite mass correction for the atom, and $\delta(n)$ is the quantum defect. The pure power series expansion of $\delta(n)$ is

$$\delta(n) = \delta_0 + \frac{\delta_1}{(n - \delta_0)^2} + \frac{\delta_2}{(n - \delta_0)^4} + \dots, \quad (2)$$

where the quantum defect parameters $\delta_0, \delta_1, \delta_2$ can be calculated using multichannel quantum defect theory or fit using experimental data [13].

In calcium atoms, the quantum defects for S , P , and D singlet and triplet states are known with high accuracy in the range of $n = 22$ –55 [13]. This work was extended to the range of $n = 20$ –150 for singlet P and F states [14]. The quantum defects for singlet S states has also been confirmed within the range of $n = 40$ –120 [15].

A recent publication reported calcium Rydberg energy-level measurements in a magneto-optical trap (MOT) [15]. A near-resonant laser at 423 nm together with a near-UV laser

excited the calcium MOT atoms to Rydberg states. The laser frequencies were determined using a calibrated wavelength meter, similar to other studies [16–20]. On resonance, the two-photon excitation opened a loss channel in the MOT and the steady-state MOT fluorescence decreased. Measuring the MOT fluorescence as a function of laser frequency produced an asymmetric line shape, due to Rydberg-Rydberg atom interactions in the MOT [5]. In that study, no line-shape analysis was given, even though atom-atom interactions can shift the line center [21]. Systematic uncertainties in determining the line center were 10 MHz. The study used Eq. (1) to produce a value of E_{IP} with an uncertainty of 1.2 MHz, consistent with previous less accurate work [14]. The accuracy of such a conclusion is based on assumptions about the nature of the experimental and statistical uncertainties and neglects systematic errors such as line shape, ac Stark shift, and density shifts.

In this paper we present measurements of calcium Rydberg energy levels and a determination of the Ca ionization potential. We describe our Doppler-free atomic spectroscopy and laser metrology together with a detailed error analysis. We report an ionization potential of $E_{IP} = 1478\,154\,283.42 \pm 0.11$ MHz (statistical and systematic uncertainties combined), improving previous measurements by a factor of 11.

II. EXPERIMENT

A schematic diagram of our experimental setup is shown in Fig. 1. An atomic beam is created by heating calcium to 500 °C. The beam is collimated using an aligned microcapillary array, similar to previous work [22,23]. Calcium atoms are excited to Rydberg states using counterpropagating lasers, one with a wavelength of 423 nm and a second laser at wavelengths between 390 and 391 nm. The 423-nm laser is detuned from the Ca $4s^2 \ ^1S_0$ – $4s4p \ ^1P_1$ transition by typically -4000 MHz, as shown in Fig. 2(a).

We use frequency-doubled Ti:sapphire lasers to generate laser radiation at 423 nm and near 390 nm. The two laser beams are overlapped on a dichroic mirror and coupled into

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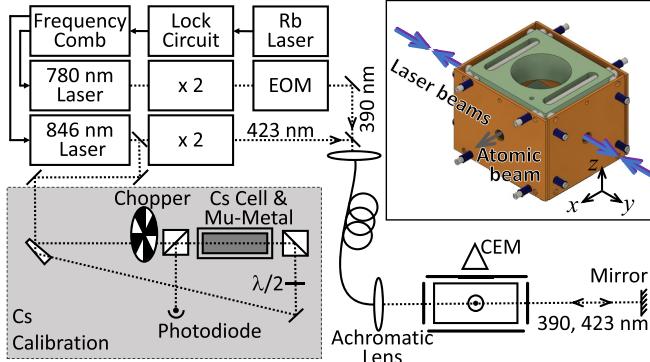


FIG. 1. Schematic diagram of the experiment setup. Continuous-wave Ti:sapphire lasers at 780 and 846 nm are offset locked to a GPS-disciplined Ti:sapphire frequency comb. The lasers are frequency doubled to 390 and 423 nm and coupled to a single-mode polarization-maintaining optical fiber. The collimated laser beams cross a collimated Ca atomic beam to excite atoms to $4s n s \ ^1 S_0$ levels. The shaded region at the lower left shows the Cs saturated absorption setup used to verify our laser metrology. Here CEM denotes channel electron multiplier. The inset shows a CAD rendering of the interaction region. The box is made entirely from copper, held together using alumina spacers and metal springs. Not shown is the mesh across the bottom of the top plate, allowing ions to pass through to the time-of-flight tube and ion detector. The 390- and 423-nm laser beams both copropagate and counterpropagate across the atomic beam.

a large-area single-mode optical fiber. The output of the fiber is collimated using an achromatic lens. After crossing the atomic beam, the lasers are retroreflected back into the optical fiber to ensure nearly perfect counterpropagating alignment, as shown in Fig. 1. The 390-nm laser beam is pulsed using an electro-optic modulator (EOM). The optical pulse width is approximately 6.5 μ s FWHM.

Three pairs of copper plates connected by shielded alumina rods and spacers are used to eliminate the dc Stark shift (see

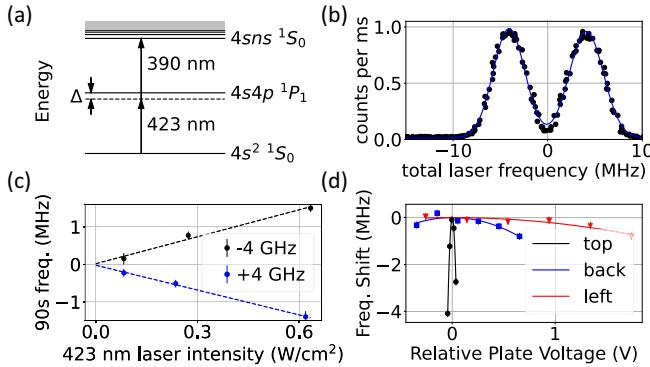


FIG. 2. Experimental details. (a) Partial energy-level diagram for Ca showing the intermediate state detuning Δ . (b) Typical 90s Rydberg spectrum. Two Doppler-shifted peaks appear while scanning the 423-nm laser as discussed in the text. (c) The ac Stark shifts vs 423-nm laser power, extrapolated to zero power. The extrapolations with $\Delta/2\pi = \pm 4000$ MHz agree with each other. (d) The dc Stark shift minimization.

inset to Fig. 1), similar to many other studies, for example, [24]. We ionize the Rydberg atoms by applying a capacitively coupled, 1- μ s duration, -100-V pulse onto the top copper plate. The pulse rises 18.5 μ s after the peak of the 390-nm laser pulse. The pulse directs ions towards the time-of-flight tube and channel electron multiplier detector. The excitation-ionization cycle repeats at a rate of 10 kHz. We scan the 423-nm laser over a frequency range of ± 13 MHz. At each laser frequency setting, we count the number of detected ions during a 4-s time interval [see Fig. 2(b)].

The excitation lasers are not exactly the same wavelength. The first-order Doppler shift is not automatically eliminated. Both laser beams counterpropagate across the atomic beam in both directions. Because the laser propagation direction is not exactly perpendicular to the atomic beam, two Doppler-reduced peaks are observed. They are symmetrically shifted above and below the Doppler-free frequency. The first-order Doppler shift is a function of the laser \vec{k} vector and the atomic velocity \vec{v} ,

$$\Delta f = \frac{1}{2\pi} \sum \vec{k} \cdot \vec{v}. \quad (3)$$

The thermal velocity of the calcium atoms is $v = (k_B T/m)^{1/2} = 400$ m/s. The angle between \vec{k} and \vec{v} is $\theta = 87^\circ$. The resulting Doppler shifts are

$$\Delta f = \pm(400 \text{ m/s}) \cos(\theta) \left(\frac{1}{390 \text{ nm}} - \frac{1}{423 \text{ nm}} \right) \\ = \pm 3.5 \text{ MHz}, \quad (4)$$

where the \pm comes from the relative directions of the 390- and 423-nm laser beams. We fit the ion count rate vs laser frequency to a two-Gaussian line-shape function. Averaging the center frequency of the two Gaussian functions gives the Doppler-free transition frequency. Typical data for the 90s state are shown in Fig. 2(b).

The apparent transition frequency depends on the excitation laser power, as shown in Fig. 2(c). Our laser intensities range up to 600 and 1100 mW/cm² for the 423- and 390-nm lasers, respectively. The Rabi frequency for the $4s^2 \ ^1 S_0$ - $4s4p \ ^1 P_1$ transition is $\Omega_{423} = \gamma(I/2I_{\text{sat}})^{1/2} = 2\pi \times 78$ MHz, where $\gamma = 2\pi \times 35$ MHz for the 423-nm transition and $I_{\text{sat}} = 60$ mW/cm². Based on scaling the results of Ref. [25], we estimate the Rabi frequency for the $4s4p \ ^1 P_1$ - $4s90s \ ^1 S_0$ transition to be $\Omega_{390} = 2\pi \times 12$ kHz. The two-photon Rabi frequency is $\Omega_{423}\Omega_{390}/\Delta = 2\pi \times 0.2$ kHz.

We use a frequency comb to determine the frequencies of our lasers, as described in previous publications [26–28]. One mode of the frequency comb is offset locked to a Rb-stabilized diode laser. The GHz comb repetition rate is not stabilized but varies typically 1 Hz in a 1-s measurement interval. Other lasers in the experiment are offset locked to their nearest comb modes, and the beat notes between the lasers and their nearest comb modes are measured. The laser frequency is calculated using

$$f_{\text{laser}} = f_{\text{Rb}} \pm f_{\text{Rbb}} + N f_{\text{rep}} \pm f_{\text{beat}}, \quad (5)$$

where the f_{Rb} is the $^{87}\text{Rb } D_2 F = 2 \rightarrow F' = (2, 3)$ crossover transition frequency of the Rb laser [29], f_{Rbb} is the beat note between the Rb-stabilized diode laser and the nearest

TABLE I. Statistical uncertainties in laser metrology and atomic spectroscopy. All values are given in terms of their contribution to the total Rydberg frequency measurement.

Parameter	Error contribution (MHz)
dc Stark shift	0.130
ac Stark shift	0.100
comb f_0	0.200
f_{rep}	0.012
423-nm (846-nm) laser lock to comb	0.060
390-nm (780-nm) laser lock to comb	0.060
Rb laser lock to comb	0.120
total	0.300

frequency comb mode, f_{beat} is the beat note between the 846- or 780-nm laser and the nearest frequency comb mode, and N is an integer.

Excitation of the Rydberg level uses the second harmonics of the 846- and 780-nm lasers, both of which are locked to the frequency comb. Using Eq. (5), the Rydberg transition frequency is calculated to be

$$f_{\text{Ryd}} = 2[2(f_{\text{Rb}} \pm f_{\text{Rbb}}) - N_2 f_{\text{rep}} \pm f_{846b} \pm f_{780b}], \quad (6)$$

where f_{846b} and f_{780b} are the beat notes between the two infrared lasers and the frequency comb and N_2 is an integer. The ambiguity in the beat note signs is removed by measuring the change in the unlocked beat note when we change the laser frequency.

III. ERROR ANALYSIS

The errors can be divided into two classes: atomic spectroscopy and laser metrology. Table I lists a summary of our error analysis. We minimize the dc Stark shift by applying small voltages to the copper plates surrounding the excitation region. The apparent transition frequency shifts quadratically in applied voltage, as shown in Fig. 2(d). We fit the frequency-vs-voltage measurements to a parabola and acquire data at voltages minimizing the Stark shift. The statistical uncertainty in the transition frequency due to the dc Stark shift is typically 0.13 MHz.

To eliminate the ac Stark shift, we measure the Rydberg transition frequency for a range of 423-nm laser power and for two values of the intermediate state detuning. We extrapolate the measured transition frequencies to zero laser power, as shown in Fig. 2(c). The uncertainty in the extrapolated value is typically 0.1 MHz at the Rydberg transition frequency.

Because the ground and Rydberg states have no angular momentum, the Zeeman shift vanishes. We address the Doppler shift in Sec. II. In our measurements, the angle between the atomic beam and the laser beams is $\theta = 87^\circ$. The line shapes are symmetric with widths that indicate the frequency noise in our excitation lasers.

The frequency of the Rydberg transition [Eq. (6)] depends on the $^{87}\text{Rb } D_2 F = 2 \rightarrow F' = (2, 3)$ crossover transition, the lock point of our reference laser relative to that frequency, and several beat note frequencies in the 20–1000 MHz range.

While the Rb transition is well known, our frequency lock relative to that transition could be shifted due to offsets in

the locking electronics. To verify the accuracy of the frequency comb, including the reference laser offset relative to the Rb transition, we measure the well-known Cs $D_2 F = 4 \rightarrow F' = (4, 5)$ crossover transition [30]. Typical data are shown in Fig. 2(d). Uncertainties in determining this offset are estimated by measuring all six lines in the Cs D_2 hyperfine array relative to their known values and also by repeated measurements of the Cs $D_2 F = 4 \rightarrow F' = (4, 5)$ crossover transition. We conservatively estimate the statistical uncertainty in the lock point to be 0.05 MHz at 852 nm. It is quadrupled [see Eq. (6)] and included in Table I as comb f_0 .

The beat note frequencies are measured using rf spectrum analyzers. The analyzers are referenced to a 10-MHz Rb oscillator. The Rb oscillator is referenced to the GPS satellite system, phase locked using the 1-pulse/s output from a GPS receiver on the roof of our building. The frequency error in this system is negligible for our measurements.

In our measurements, the 846-nm laser is scanned. The 846-nm laser is tightly offset locked to the frequency comb. The f_{846b} beat note spectrum is averaged for 4 s per measurement point. The peak of the averaged beat note spectrum is used for f_{846b} . The repeatability in determining the beat note is approximately 30 kHz. The f_{780b} and f_{Rbb} beat note spectra are also averaged for 4 s and read out the same way. However, because these laser frequencies do not change during the measurement process, the 4-s measurements are averaged together during one scan over the Rydberg transition. The statistical uncertainty in determining these beat notes is also approximately 30 kHz. This uncertainty is doubled for the 846- and 780-nm lasers and quadrupled for the Rb laser in Table I.

The frequency comb repetition rate $f_{\text{rep}} = 0.988$ GHz is measured using a GPS-referenced frequency counter. The counting interval is 0.5 s, read out eight times during the 4-s measurement time. The standard deviation of these measurements is typically 0.5 Hz. Assuming a normal distribution, the uncertainty in the mean is typically 0.2 Hz. The integer N_2 in Eq. (6) is roughly 30 000, making the uncertainty in f_{rep} equal to 6 kHz in a 4-s measurement time. This statistical uncertainty is doubled in Table I.

All cell-based frequency measurements must allow for shifts due to possible impurities in the cell. In the work of Refs. [31–33] it was shown that the Cs $6s(F = 4)-8s(F' = 4)$ transition shifts linearly with He pressure. They showed that the dominant impurity in aging Cs cells is atmospheric He diffusing through the glass wall. They also showed that the transition linewidth can be used as a surrogate for cell impurity measurements when the laser linewidth is well characterized. We have measured this transition in our Cs reference cell. Our zero-power extrapolated FWHM is 1.06 MHz. For this measurement, special efforts were made to minimize the noise in the frequency comb. In our $6s-8s$ measurements, transit time broadening accounts for approximately 40 kHz of the observed linewidth. Using the data from Fig. 3 of Ref. [33] and assuming zero contribution from the laser linewidth, a transition FWHM of 1.02 MHz corresponds to a shift of 18 kHz. While the pressure shift of the $D_2 F = 4 \rightarrow F' = (4, 5)$ crossover transition is not known, we can use this 18 kHz as an estimate of the systematic uncertainty in the f_{Rb} determination in Eq. (6).

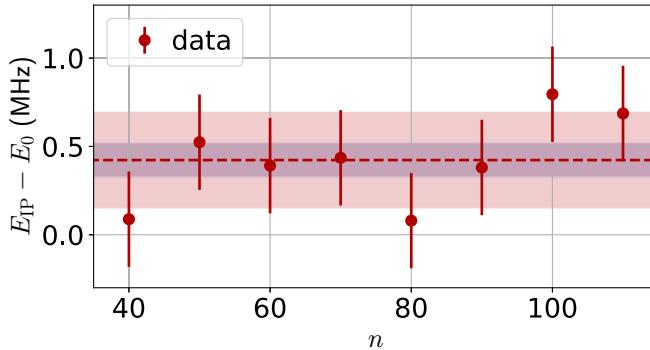


FIG. 3. Plot of E_{IP} vs principal quantum number n . The error bars for the present work are from Table I. The shaded red area indicates the standard deviation in the calculated E_{IP} values. The gray shaded area indicates the uncertainty in the mean. For this plot, $E_0 = 1478154283.00$ MHz.

IV. RESULTS AND DISCUSSION

Our measured frequencies for the Ca $4s^2 \ ^1S_0 - 4sns \ ^1S_0$ transitions with $n = 40-110$ are listed in Table II and plotted in Fig. 3. For each Rydberg level measurement, we calculate the ionization energy using the Ritz formula of Eq. (1), with the quantum defect expression in Eq. (2). The quantum defect values $\delta_0 = 2.337\ 930\ 16(300)$ and $\delta_1 = -0.114(3)$ and the Rydberg constant $R_{Ca} = 109\ 735.809\ 284\ \text{cm}^{-1}$ are from Ref. [13]. The standard deviation in the ionization energy calculations is 0.24 MHz, in close agreement with the estimated statistical uncertainties in Table I. Assuming that these ionization energy uncertainties are statistical and uncorrelated, the estimated error in the mean is $\sigma_\mu = \sigma/N^{1/2} = 0.24/8^{1/2} = 0.08$ MHz. We add the estimated systematic uncertainty of 4×0.018 MHz = 0.072 MHz, the estimated uncertainty due to pressure shifts in the Cs cell, in quadrature for a final estimated uncertainty of 0.11 MHz in E_{IP} .

Our results can be compared to a recent publication by Zelener *et al.* [15]. Their work differs from ours in that they used the steady-state number of atoms in a magneto-optical trap as their “detector” and measured their laser frequency using a laser wavelength meter. They also used a modest intermediate state detuning of -47.8 MHz compared to our value of -4000 MHz. Their typical transition linewidth was asymmetric with a full width of approximately 10 MHz. Coherent Rydberg excitation at low values of the intermediate state detuning are broadened by the intermediate-state

TABLE II. The $4s^2 \ ^1S_0 - 1sns \ ^1S_0$ Rydberg transition energies and calculated ionization potential energies. Values of E_{IP} are calculated using Eqs. (1) and (2) and quantum defect results from Ref. [13].

n	Measured E_n (MHz)	E_I (MHz)
40	1475834972.82	1478154283.09
50	1476706104.14	1478154283.52
60	1477164846.49	1478154283.39
70	1477435698.36	1478154283.44
80	1477608838.11	1478154283.08
90	1477726183.13	1478154283.38
100	1477809364.80	1478154283.80
110	1477870463.33	1478154283.69
average		1478154283.42
standard deviation		0.24
uncertainty in mean		0.08
systematic uncertainty		0.07

decoherence. Excitation line shapes can become asymmetric due to the Autler-Townes splitting [25] and atom-atom interactions [5,21]. In Ref. [15] the authors chose the minimum in the steady-state MOT fluorescence as the line center, estimating their uncertainty in the line center to be 10 MHz. They measured transitions to several $4sns \ ^1S_0$ levels with n ranging from 40 to 120. Rather than using the quantum defect values from Ref. [13], they fit their data to Eq. (1) to extract E_{IP} , δ_0 , and δ_1 . Their quantum defect values were consistent with Ref. [13], although with larger error estimates. The ionization potential from Ref. [15], $E_{IP} = 49\ 305.919\ 66(4)\ \text{cm}^{-1} = 1\ 478\ 154\ 284.9(1.2)$ MHz, assumes uncorrelated measurement errors and that all errors are statistical in nature. Their lower accuracy value is in good agreement with our results.

The greatest contribution to uncertainties in our measurements are from the frequency comb. Our lasers are tightly locked to the comb. Technical noise in the comb broadens the laser frequencies at the 1-MHz level. Reducing this noise would enable higher-precision measurements of all other systematics in the experiment.

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