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Theory of Magnetoelectric Effect for Three Layer Piezo-Magnetostrictive Asymmetric Composites

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Abstract: Here we discuss a model for the quasi-static magnetoelectric (ME) interaction in three layer composites consisting of a single piezoelectric (PE) layer and two magnetostrictive (MS) layers with positive and negative magnetostriction. Two types of layer arrangements are considered. *Type 1*:A sandwich structure with the PE layer between the two MS layers and *Type 2*: the two MS layers form the adjacent layers. Expressions for the ME response are obtained using the system of equations of elasto- and electrostatics for the PE and MS phases. The contributions from longitudinal and bending vibrations to the net ME response are considered. The theory is applied for trilayers consisting of lead zirconate titanate (PZT), nickel for negative magnetostriction and Metglas for positive magnetostriction. Estimates of the dependence of the strength of the ME response on the thickness of the three layers are provided. It is shown that the asymmetric three-layer structures of both types leads to an increase in the strength of ME interactions by almost an order of magnitude compared to a two-layer piezoelectric-magnetostrictive structure. The model predicts a much stronger ME response in *Type 2* structures than in *Type 1*. The theory discussed here is of importance for designing composites for applications such as magnetic field sensors, gyrators and energy harvesters.

Keywords: multiferroic composites, magnetostriction, piezoelectricity, magnetoelectric effect, gyrator, magnetoelectric harvester.

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1. Introduction

Piezo-magnetostrictive (PE-MS) composites are unique materials for electronics due to the mechanical coupling between the magnetostrictive and piezoelectric phases leading to magnetoelectric (ME) interaction. This interaction manifests as an electric voltage when the composite is subjected to a magnetic field (direct effect), or, conversely, a change in the magnetization of the sample occurs when it is placed in an electric field (inverse or converse ME effect). Due to the ME interaction, there is an interrelation between the electrical and magnetic properties of materials. Due to this relationship, ME composites can be used to fabricate new electronic devices that cannot be created using traditional materials [1-3]. Early works investigated various types of composites consisting of a variety of

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ferromagnetic and ferroelectric phases in form of bulk composites as well as thick film or thin film layered structures and nanocomposites in the form of nanopillars in a host matrix, core-shell particles and core-shell nanofibers [4-11]. In spite of these early efforts, the question of increasing the efficiency of the field conversion in ME materials remains fundamental at present. The efficiency is very important especially in the low-frequency region, where the strength of the ME coupling is practically independent of frequency. Although the ME effect in the electromechanical resonance region is much stronger than at low-frequency, the frequency width of the electromechanical resonance line is rather narrow. Therefore, in applications such as energy harvesters operating at the resonance frequency will not be efficient. In contrast to single phase multiferroics, where the ME interaction mechanism is a change in the electron spin-orbit interaction upon application of an external electric field [12], the ME response mechanism in PE-MS composites is the mechanical interaction between the piezoelectric and magnetostrictive subsystems [13]. When a magnetic field is applied mechanical deformations occur due to magnetostriction, which is transferred to the piezoelectric and resulting in a change in polarization. The most common ferromagnetic materials for creating the composites are permendur, nickel, Terfenol-D, and amorphous Metglas alloy. When they are placed in a magnetic field in the plane of the sample, longitudinal deformations of the tension-compression type are transferred to the PE layer and also bending deformations in the case of asymmetric structures.

In bilayers the contribution from bending deformation to ME coupling is significant [14,15]. A bimorph asymmetric structure consisting of two layers of PZT with opposite directions of polarization and located between two magnetic layers which were an amorphous Metglas alloy with positive magnetostriction and a nickel layer with negative magnetostriction was studied in the work of Ref. [16]. The magnitude of the ME interaction in such a structure turned out to be an order of magnitude higher than in a two-layer Ni-PZT structure with similar parameters and comparable sizes. In the works of Refs. [16– 18], experimental studies of the ME coupling in the Terfenol-D/PZT/Ni structure at various nickel thicknesses are presented. In these works, it was shown that the efficiency of ME conversion in the region of the flexural vibration mode significantly exceeds the value of ME interaction in two-layer structures. The theory of the ME effect caused by bending deformations in a three-layer structure with two adjacent magnetic layers and a piezoelectric layer was presented in Ref.[19]. In this work, the contribution to the ME interaction only from bending vibrations was considered. However, in a two-layer structure, the contributions to the ME effect from longitudinal and bending vibrations have different signs, and their contributions to the resulting ME effect are dependent on the layer thickness.

In this report, two types of asymmetric three-layer structures are considered. *Type-1* in which the piezoelectric (PE) layer is located between two magnetostrictive (MS) layers with positive and negative magnetostriction and *Type-2* in which the PE layer is on top of two adjacent MS layers. The contributions to the ME effect from longitudinal and bending vibrations are taken into account. The purpose of this work was to model the influence of the two MS layers with positive and negative magnetostrictions on the strength of the ME interactions in each type and to determine the dependence of ME interaction strengths on the thicknesses of the MS layers. A widely used parameter characterizing the value of ME interactions is the ME voltage coefficient (MEVC) that is defined as the ratio of the induced electric field in the PE layer, (V_{ac}/t^p), to the applied AC magnetic field h_{ac} i.e., MEVC = $V_{ac}/(t^p h_{ac})$. We also considered the dependence of ME sensitivity coefficient, MESC= V_{ac}/h_{ac} on the thickness of MS layers for the two types three-layer structures. The model is applied to the case of composites with PZT and Ni, with negative magnetostriction, Metglas and Permendur with positive magnetostriction.

2. Model 93

Figure 1 shows the two types of trilayers consisting of PZT and MS layers with positive and negative magnetostriction considered for modeling.

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Fig. 1 Schematic drawing of (a) Type 1 and (b) Type 2 asymmetric trilayers, with PZT layer of thickness t^p and magnetostrictive (MS) layers with positive (MS+) and negative (MS-) magnetostriction and thicknesses t^{m1} and t^{m2} respectively. The dashed line represents the neutral plane.

When a sample is placed in a magnetic field, compressive strains occur in a layer with negative magnetostriction (nickel or nickel ferrite, for example), and tensile strains occur in a layer with positive magnetostriction (Permendur, Terfenol-D, Metglas alloy). By means of a mechanical coupling through the interface, these deformations are transferred to the PZT layer, as a result of which longitudinal tensile or compressive deformations occur in it. In addition, since the mechanical stresses resulting from the deformations are not axial, a bending moment is also present which leads to bending deformations. As a result, when a sample is placed in a magnetic field, two types of deformations occur simultaneously in a piezoelectric material - longitudinal deformations and bending deformations. Both types of these deformations contribute to the magnitude of the ME interaction.

3. Longitudinal deformations

When considering the ME interactions, we restrict ourselves to the quasi-static case, i.e., the case when the length and width of the sample are much smaller than the length. In this case, the change in strains and stresses along the length and width of the sample can be neglected and, in this case, elasto-and electrostatic equations have following forms:

$$S_i^p = \frac{1}{v^p} (T_i^p - v T_j^p) + d_{31}^p E_3, \tag{1}$$

$$S_i^{m1} = \frac{1}{Y^{m1}} (T_i^{m1} - \nu T_j^{m1}) + q_{1i}^{m1} H_1, \tag{2}$$

$$S_i^{m2} = \frac{1}{V^{m2}} (T_i^{m2} - \nu T_j^{m2}) + q_{1i}^{m2} H_1, \tag{3}$$

$$D_3^p = \varepsilon_{33}^p E_3^p + d_{31}^p (T_1^p + T_2^p) , \qquad (4)$$

where the indices i and j take the values 1 and 2, and $i \neq j$. Here S_i^p , S_i^{m1} , S_i^{m2} are strain tensor components of piezoelectric, magnetostrictive layers MS+ and MS-, respectively, Y^p , Y^{m1} , Y^{m2} are their Young's moduli, ν is Poisson's ratio, E_3 , D_3^p are components of the vector of the electric field and electric induction, T_i^p , T_i^{m1} , T_i^{m2} are the stress tensor components of PZT and MS+ and MS-, d_{31}^p , q_{1i}^m are piezoelectric and piezomagnetic coefficients, ε_{33}^p is the component of the permittivity. In contrast to Ref. [20], we do not assume that the width of the sample is much less than its length, so in this work we also take into account the contribution to the ME interaction from the stress T_2 , which is a more accurate modelling.

For simplicity of calculations, we will assume that the sample's thickness is much smaller than its length and width. We also are supposed that the bond on interface is ideal, and we don't take into account the effects, arisen on the interface. In this case we can assume that longitudinal strains are uniform throughout the layer volume, i.e., the following equality hold:

$$S_i^{m1} = S_i^{m2} = S_i^p = S_i. (5)$$

Under this assumption the longitudinal deformations for both types of structures, Type-1 and -2, will be the same and contributions to ME interactions for both type of structures will be the same. For following calculations, we will be using the modified procedure in Ref. [20]. The equilibrium condition of the sample, namely the equality to zero the *X* and *Y* projections of the force, gives for this case the following equations:

$$t^p T_i^p + t^{m1} T_i^{m1} + t^{m2} T_i^{m2} = 0, (6)$$

where the index *i* takes the values 1,2. After that, expressing the components of the stress tensor from Eq. (1), Eq. (2) and Eq. (3) and substituting the obtained expressions into Eq. (6), we obtain the following equation relating the deformations with the applied magnetic and induced electric fields:

$$(S_i + \nu S_j) = \frac{1}{\tilde{\gamma}t} \left\{ Y^p t^p (1 + \nu) d_{31}^p E_{3,long} + \begin{bmatrix} Y^{m1} t^{m1} (q_{1i}^{m1} + \nu q_{1j}^{m1}) + \\ + Y^{m2} t^{m2} (q_{1i}^{m2} + \nu q_{1j}^{m2}) \end{bmatrix} H_1 \right\}.$$
(7)

Here $\bar{Y} = (Y^p t^p + Y^{m1} t^{m1} + Y^{m2} t^{m2})/t$ is the average Young's modulus, and $t = t^p + t^{m1} + t^{m2}$ is the total thickness of the sample. After simple transformations, we get

$$(S_1 + S_2) = \frac{1}{\tilde{r}t} \left\{ 2Y^p t^p d_{31}^p E_{3,long} + \begin{bmatrix} Y^{m1} t^{m1} (q_{11}^{m1} + q_{12}^{m1}) + \\ +Y^{m2} t^{m2} (q_{11}^{m2} + \nu q_{12}^{m2}) \end{bmatrix} H_1 \right\}.$$
(8)

Substituting this expression into Eq. (4) and take into account the open-circuit condition we obtained for the electric field induced in the piezoelectric layer due to longitudinal deformations the following expression:

$$E_{3,long} = \frac{Y^p d_{31}^p}{\varepsilon_{33} \bar{r} t} \frac{[Y^{m1} t^{m1} (q_{11}^{m1} + q_{12}^{m1}) + Y^{m2} t^{m2} (q_{11}^{m2} + q_{12}^{m2})]}{[1 - \nu - 2k_p^2 (1 - Y^p t^p / \bar{Y} t)]} H_1, \tag{9}$$

where $k_p^2 = Y^p (d_{31}^p)^2 / \varepsilon_{33}$ denotes the square of the electromechanical coupling coefficient. Using the definition of the MEVC in the form $\alpha_{E,long} = E_{3,long}/H_1$, we obtain the expression for the contribution to MEVC from longitudinal deformations in the form:

$$\alpha_{E,long} = \frac{Y^p d_{31}^p}{\varepsilon_{33} \bar{Y} t} \cdot \frac{[Y^{m1} t^{m1} (q_{11}^{m1} + q_{12}^{m1}) + Y^{m2} t^{m2} (q_{11}^{m2} + q_{12}^{m2})]}{[1 - \nu - 2k_p^2 (1 - Y^p t^p / \bar{Y} t)]}$$
(10)

Along with the MEVC, which is the main ME parameter to characterizes the magnetic field-to-electric field conversion efficiency we can also use the other parameter, to characterize the electric response to the magnetic field. This parameter, namely the ME sensitivity coefficient is equal to the ratio of the magnitude of the induced electric voltage $U_{long} = E_{3long}t^p$ to the magnitude of the alternating magnetic field, i.e., $\beta_{U,long} = U_{long}/H_1$. Using Eq. (6) we get the following expression for the ME sensitivity coefficient (MESC):

$$\beta_{U,long} = \frac{Y^p d_{31}^p t^p}{\varepsilon_{33} \tilde{Y} t} \cdot \frac{\left[Y^{m1} t^{m1} (q_{11}^{m1} + q_{12}^{m1}) + Y^{m2} t^{m2} (q_{11}^{m2} + q_{12}^{m2})\right]}{\left[1 - v - 2k_p^2 (1 - Y^p t^p / \tilde{Y} t)\right]},\tag{11}$$

Equations (10) and (11) make it possible to analyze the dependence of the MEVC and MESC due to longitudinal deformation on the physical parameters of the magnetostrictive and piezoelectric phases and their layer thicknesses.

3. Bending deformations

When an asymmetric structure is placed in a magnetic field, a bending moment M_y arises, leading to bending along axis X(1) and a bending moment M_X , leading to bending of the structure along axis Y(2). The deformations S_1 and S_2 arising in this case are proportional to the bending moments M_y and M_x respectively and they are inversely proportional to the stiffness of the structure at bending along length L and width W.

When considering the bending deformations, we will assume that the bonding between the layers is ideal and, according to the Bernoulli hypothesis [21] the following relation holds for the deformations of the piezoelectric and the two magnetic layers:

$$S_i = (z - z_0)/\rho_i, (12)$$

where z_0 is the neutral line coordinate and ρ_i is the radius of curvature of the neutral line along i axe. The bending moment M_i , occurs in MS layers by applying magnetic field H_1 and is related to the radius of curvature by the relation:

$$1/\rho_i = M_i/D_i,\tag{13}$$

where $D_i = (Y^{m1}J_{i,z0}^{m1} + Y^{m2}J_{i,z0}^{m2} + Y^pJ_{i,z0}^p)$ is the cylindrical stiffness of the structure. Here $J_{i,z0}^{m1}$, $J_{i,z0}^{m2}$ and $J_{i,z0}^{p}$ are the moment of inertia of the layered sections about the neutral axis Z_0 . The position of the neutral line is determined from the condition that the X-projection of the force is equal to zero.

The bending moment, the position of the neutral axis and, as a result, the moment of inertia of the layers about the neutral axis for Type-1 and Type-2 will be different. It will result in longitudinal deformations opposite in direction and the contributions to MEVC due to bending deformations from for the two composites will be different.

3.1 Type-1 Structure

For this type of asymmetric composite, the position of the neutral line, the bending moment and the moments of inertia are given by the following expressions:

$$z_0 = 0.5 \begin{bmatrix} Y^{m1}(t^{m1})^2 + Y^p(t^p)^2 + Y^{m2}(t^{m1})^2 + 2Y^pt^{m1}t^p + \\ +2Y^{m2}(t^{m1} + t^p)t^{m2} \end{bmatrix} / \bar{Y}t,$$
 (14)

$$M_{j} = W_{i} \left[q_{1i}^{m1} Y^{m1} t^{m1} \left(\frac{t^{m1}}{2} - z_{0} \right) + q_{1i}^{m2} Y^{m2} t^{m2} \left(t^{m1} + t^{p} + \frac{t^{m2}}{2} - z_{0} \right) \right] H_{1}$$

$$(15)$$

$$J_{i,z_0}^{m_1} = \frac{1}{12} W_i(t^{m_1})^3 + W_i t^{m_1} (0.5t^{m_1} - z_0)^2,$$
 (16)

$$J_{i,z_0}^p = \frac{1}{12} W_i(t^p)^3 + W_i t^p (t^{m_1} + 0.5t^p - z_0)^2, \tag{17}$$

$$J_{i,z_0}^{m2} = \frac{1}{12} W_i(t^{m2})^3 + W_i t^{m2} (t^{m1} + t^p + 0.5t^{m2} - z_0)^2,$$
 (18)

where $W_i = W$ for i = 1 and $W_i = L$ for i = 2, W is the width of the sample.

As can see from Eq. (15) – (18), bending moment M_j and stiffness D_i linear depend on W_i , because but their relationship $\frac{M_j}{W_i}$ does not depend on W or L. For further calculations, we introduce the following notation $D = D_i/W_i$ is a cylindrical stiffness of the structure and $m_x = \frac{M_x}{L}$, $m_y = \frac{M_y}{L}$.

The neutral line position depends on the relation between thicknesses of the PE layer, first and second MS layers and can lie either in the PE layer or in the MS layers. If the neutral line is in the PE layer, then in this case the part of the PE that lies above the neutral line undergoes tension (compression), and the other part undergoes compression (tension). As a result, the resulting electric fields in different parts of the PE layers will have opposite directions, because of which the total electric field will decrease. If the neutral layer is in a MS layer, then the bending moments arising under the action of the magnetic field in the parts located on opposite sides of the neutral line will have opposite directions, and the net bending moment decreases. The maximum ME response will be in the case when the neutral line is located at the interface between the MS layer and the PE layer, i.e., when the neutral line coordinate $z_0 = t^{m1}$ or $z_0 = (t^{m1} + t^p)$. Using Eq. (11) one can calculate the thicknesses of the layers for maximum MEVC. Under the action of a bending moment, the structure bends, and the resulting deformations induce an electric field is induced in the PE layer. Using equations (9) and (10), as well as the open circuit condition, for the electric field inducing by bending deformations, we obtain the following expression:

$$E_{3,bend}^{p} = Y^{p} \frac{d_{31}^{p} (m_{x} + m_{y})}{\varepsilon_{33}^{p} D^{(1)} (1 - k_{p}^{2})} (z - z_{0}).$$
(19)

In contrast to the case of longitudinal deformations in which the induced electric field is uniform over the thickness of the sample, bending deformation induced electric field is nonuniform over the thickness of the piezoelectric. The value of MEVC $\alpha_{E,bend}$, associated with the bending is determined as follows:

$$\alpha_{E,bend} = \langle E_{3,bend} \rangle / H_1, \tag{20}$$

where $\langle E_{3,bend} \rangle$ is the average value of the induced electric field strength, which for the given structure is given by:

$$\langle E_{3,bend} \rangle = \frac{1}{t^p} \int_{t^{m_1}}^{t^{m_1} + t^p} E_{3,bend} dz$$
 (21)

Substituting Eq. (16) into Eq. (18) and integrating, we obtain the expression for the average value of the induced electric field strength. Then, using Eq. (17) for the contributions to MEVC and MESC by bending deformations for the first type structure we get the following expressions:

$$\alpha_{E,bend}^{(1)} = \\ = Y^{p} \frac{d_{31}^{p} \left[(q_{11}^{m1} + q_{12}^{m1}) Y^{m1} t^{m1} \left(\frac{t^{m1}}{2} - z_{0} \right) + (q_{11}^{m2} + q_{12}^{m2}) Y^{m2} t^{m2} \left(t^{m1} + t^{p} + \frac{t^{m2}}{2} - z_{0} \right) \right]}{\varepsilon_{33}^{p} D^{(1)} (1 - k_{p}^{2})} \cdot (22)$$

$$\left(\left(t^{m1} + \frac{t^{p}}{2} \right) - z_{0} \right),$$

$$\beta_{E,bend}^{(1)} =$$

$$= Y^{p} \frac{d_{31}^{p} t^{p} \left[(q_{11}^{m1} + q_{12}^{m1}) Y^{m1} t^{m1} \left(\frac{t^{m1}}{2} - z_{0} \right) + (q_{11}^{m2} + q_{12}^{m2}) Y^{m2} t^{m2} \left(t^{m1} + t^{p} + \frac{t^{m2}}{2} - z_{0} \right) \right]}{\varepsilon_{33}^{p} D^{(1)} (1 - k_{p}^{2})} \cdot ((t^{m1} + \frac{t^{p}}{2}) - z_{0}).$$

$$(23)$$

The values of the moments of inertia $J_{z_0}^{m1}$, $J_{z_0}^p$ and $J_{z_0}^{m2}$ are proportional to the width of the sample W, so the denominators in expressions (22) and (23) do not depend on the width of the sample and the ME conversion efficiency is determined only by the physical parameters of the three layers and their thicknesses. Equations (22), (23) can be used to estimate the dependence of the MEVC and the MESC on the physical and geometrical parameters of the Type-1 three-layer structure.

3.2 Type-2 Structure

For the second type of structure, the position of the neutral line, the bending moment are given by the following expressions:

$$z_0 = 0.5 \left[\frac{Y^{m1}(t^{m1})^2 + Y^p(t^p)^2 + Y^{m2}(t^{m1})^2 + 2Y^{m2}t^{m1}t^{m2}}{+2Y^p(t^{m1} + t^{m2})t^p} + \right] / \bar{Y}t,$$
 (24)

$$m_{j} = \left[q_{1i}^{m1} Y^{m1} t^{m1} \left(\frac{t^{m1}}{2} - z_{0} \right) + q_{1i}^{m2} Y^{m2} t^{m2} \left(t^{m1} + \frac{t^{m2}}{2} - z_{0} \right) \right] H_{1}$$
 (25)

$$J_{i,z_0}^{m_1} = \frac{1}{12} W_i(t^{m_1})^3 + W_i t^{m_1} (0.5t^{m_1} - z_0)^2,$$
 (26)

$$J_{i,z_0}^{m2} = \frac{1}{12} W_i(t^{m2})^3 + W_i t^{m2} (t^{m1} + 0.5t^{m2} - z_0)^2,$$
 (27)

$$J_{i,z_0}^p = \frac{1}{12} W_i(t^p)^3 + W_i t^p (t^{m1} + t^{m2} + 0.5t^p - z_0)^2, \tag{28}$$

Using these equations and following the same procedure as for Type-1 composite, we obtain the following expressions for the coefficients characterizing the ME interaction:

$$\alpha_{E,bend}^{(2)} = \\ = Y^{p} \frac{d_{31}^{p} \left[(q_{11}^{m1} + q_{12}^{m1}) Y^{m1} t^{m1} \left(\frac{t^{m1}}{2} - z_{0} \right) + (q_{11}^{m2} + q_{12}^{m2}) Y^{m2} t^{m2} \left(t^{m1} + \frac{t^{m2}}{2} - z_{0} \right) \right]}{\varepsilon_{33}^{p} D^{(2)} (1 - k_{p}^{2})} \cdot \left(\left(t^{m1} + t^{m2} + \frac{t^{p}}{2} \right) - z_{0} \right),$$

$$(29)$$

$$\beta_{E,bend}^{(2)} = \\ = Y^{p} \frac{d_{31}^{p} t^{p} \left[(q_{11}^{m1} + q_{12}^{m1}) Y^{m1} t^{m1} \left(\frac{t^{m1}}{2} - z_{0} \right) + (q_{11}^{m2} + q_{12}^{m2}) Y^{m2} t^{m2} \left(t^{m1} + \frac{t^{m2}}{2} - z_{0} \right) \right]}{\varepsilon_{33}^{p} D^{(2)} (1 - k_{p}^{2})} \cdot (30)$$

$$((t^{m1} + t^{m2} + \frac{t^{p}}{2}) - z_{0}).$$

4. Results and Discussions

The net MEVC $\alpha_{E,net}$ and the MESC $\beta_{U,net}$ are the sums of the contributions from longitudinal and bending deformations and are given by:

$$\alpha_{E,net} = \alpha_{E,long} + \alpha_{E,bend}, \tag{31}$$

$$\beta_{U,net} = \beta_{U,long} + \beta_{U,bend}, \tag{32}$$

Both longitudinal and bending contributions are proportional to the product of the piezoelectric coefficient d_{31}^p , the piezomagnetic coefficient q_{11}^m and the Young's modulus of the

piezoelectric Y^p and are inversely proportional to the permittivity ε_{33}^p . For the quasi-static case the contributions do not depend on the width and length of the sample, but will depend on the thickness of the piezoelectric and both magnetic layers.

For longitudinal deformations in a magnetic field, MS(-) layer experiences compression, and a layer with MS(+) experiences tension. As a result, depending on the thickness ratio of the MS layers, the PE layer can experience either compression or tension, depending on the position of the neutral layer, one part can experience tension and the other compression. For small thicknesses of the layer with positive magnetostriction, the compression force is greater than the tension force, as a result of which the contribution from longitudinal deformations to the magnitude of the ME effect is positive and decreases with increasing thickness of the second layer until the following equality occurs

$$Y^{m1}t^{m1}(q_{11}^{m1} + q_{12}^{m1}) + Y^{m2}t^{m2}(q_{11}^{m2} + q_{12}^{m2}) = 0. (33)$$

For these thicknesses of MS layers, the contribution to MEVC from longitudinal deformations is zero. With a further increase in the thickness of the second MS layer, the value of MEVC_{long} changes sign and begins to increase, and at thicknesses $t^{m2} \gg t^{m1}$, t^p tends to the limit value equal to

$$\lim_{t^{m2} \to \infty} (\alpha_{E,long}) = Y^p d_{31}^p (q_{11}^{m2} + q_{12}^{m2}) / \varepsilon_{33} . \tag{34}$$

For the Type-1 structure, the contribution to the magnitude of the ME interaction from bending deformations for small thicknesses of the second MS layer has the opposite sign to longitudinal deformation. As the thickness of the second layer increases, its contribution begins to grow and reaches a maximum when the neutral layer lies at the interface between the layers with negative and positive magnetostriction, i.e., when

$$t^{m1} = 0.5[Y^{m1}(t^{m1})^2 + Y^p(t^p)^2 + Y^{m2}(t^{m1})^2 + 2Y^pt^{m1}t^p + 2Y^{m2}(t^{m1} + t^p)t^{m2}]/\bar{Y}t .$$
(35)

With a further increase, the value of the ME coefficient begins to decrease since the neutral layer moves into the piezoelectric, and as a result a part of the PE experiences tension, and another part compression, which leads to a decrease in the magnitude of the ME interaction. In the case when the neutral layer lies in the middle of the piezoelectric layer, i.e., for a given structure, when the relation $z_0 = t^{m1} + 0.5t^p$ is satisfied, then in this case, according to equation (19), the contribution from bending vibrations to the magnitude of the ME interaction will be equal to zero. With a further increase, the value of MEVC due to bending begins to increase. But the analysis of the contribution with a further increase in the thickness of the second magnetostrictive layer is of no interest since such structures are not realized in practice.

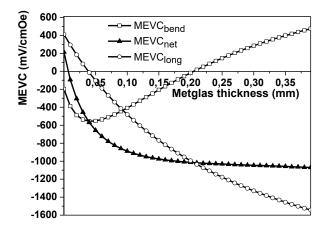
Next, we apply the theory to representative three-layer composites with Ni, , Permendur (an alloy of Fe, Co, and V), or Metglas for the ferromagnetic layer and PZT for the piezoelectric layer. Nickel has a negative longitudinal magnetostriction whereas it is positive for Permendur and Metglas. The piezomagnetic coefficients for the ferromagnets and the piezoelectric coefficient for PZT are listed in Table 1.

Table 1. Parameters of materials of composite structures

	Young's modulus Y,	Piezomodules d ₃₁ , pC/N; and	Permittivity ε
Material			
	GPa	q11, q12 ppm/Oe	
PZT	66.7	$d_{31} = -175$	1750
Ni	215	q ₁₁ =- 0.07, q ₁₂ =+0.02	-
Pe	207	$q_{11} = +0.02, q_{12} = -0.003$	-
Metglas	110	$q_{11} = +0.3, q_{12} = -0.03$	

The value of the piezoelectric module d_{31} was used from [22] and the values of the piezomagnetic modules $q=d\lambda/dH$ were get using the data for magnetostriction curves [23-25] at the bias magnetic field near 50 Oe.

Figures 2 and 3 show the MEVC and MESC dependences, respectively, for Type-1 composite for nickel with negative magnetostriction, PZT, and Metglas with positive magnetostriction. In Figure 2 MEVS is shown as a function of Metglas thickness for a fixed PZT and Ni thicknesses of t^p =0.2 mm and t^{m1} =0.2 mm respectively. As can be seen from Figure 2, the net MEVC has a broad maximum in the region located beyond the region where (MEVC)_{bend} has a maximum. For the trilayer composite the MEVC is a factor of five higher than for Ni/PZT bilayer. With a further increase in the thickness of the second MS layer, MEVC decreases due to the decrease in the contribution from bending caused by the increase in the stiffness of the structure.



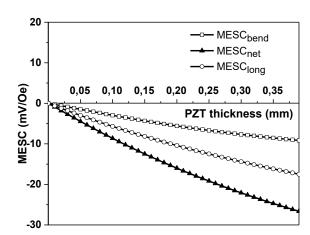


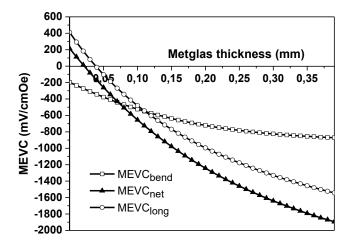
Figure 2. Estimated dependence of MEVC in a Ni - PZT – Metglas first type three-layered structures on the Metglas layer thickness. The PZT layer thickness $t^p = 0.2 \ mm$, the Ni thickness $t^{m1} = 0.2 \ mm$.

Figure 3. Estimated dependence of MESC in a Ni - PZT – Metglas first type three-layered structures on the PZT layer thickness. The Ni layer thickness $t^{m1} = 0.2 \ mm$, the Metglas thickness $t^{m2} = 0.2 \ mm$.

Figure 3 shows the estimated variation in MESC with the thickness of PZT layer. The Ni thickness and Metglas are assumed to be 0.2 mm. These thicknesses were chosen because they correspond to the region where the MEVC has a maximum. The MESC is zero at $t^p = 0$. The MESC caused by longitudinal deformations increases with the increase of PZT layer thickness and predicted to attain saturation at $t^p \gg t^{m1}$, t^{m1} . This saturation value of MESC equals:

$$(\beta_{U,long})_{t^{p}\to\infty} = d_{31}^{p} [Y^{m1}t^{m1}(q_{11}^{m1} + q_{12}^{m1}) + Y^{m2}t^{m2}(q_{11}^{m2} + q_{12}^{m2})]/\varepsilon_{33}$$
(33)

The MESC due to bending deformations increases with the increase in t^p , then it reaches a maximum value and then slowly decreases with a further increase in the thickness of the piezoelectric layer. The net MESC first increases with increase in t^p , then there is a small plateau in its value but this plateau is observed at large thickness of PZT which seldom is used in practice.



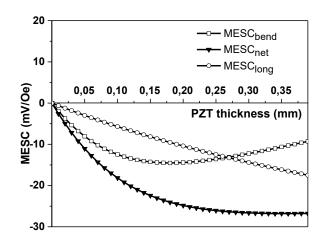


Figure 4. Estimated dependence of MEVC in a Ni - Metglas - PZT second type three-layered structures on the Metglas layer thickness. The PZT layer thickness $t^p = 0.2 \ mm$, the Ni thickness $t^{m1} = 0.2 \ mm$.

Figure 5. Estimated dependence of MESC in a Ni - Metglas - PZT second type three-layered structures on the PZT layer thickness. The Ni layer thickness $t^{m1} = 0.2 \, mm$, the Metglas thickness $t^{m2} = 0.2 \, mm$.

Theoretical estimates of MEVC and MESC for the Type-2 three-layered structures of Ni-Metglas- PZT are shown in Figures 4 and 5, respectively. As can see from Fig. 4 MEVC due to longitudinal deformations is the same as for the Type-1. This fact is a consequence of the assumption that the longitudinal deformations of the piezoelectric and two magnetostrictive layers are the same. The contribution to MEVC from bending for Type-2 structure, however, is different from Type-1 structures. The (MEVC)_{bend} value for Type-2 has high rate of increase with the thickness of the Metglas until the position of the neutral line lies into the Metglas layer. With further increase in Metglas thickness the rate of change in the (MEVC)_{bend} begins to decrease and reaches a plateau. The (MESC)_{bend} value for in Fig.5 at first increased with increase in PZT thickness, then it has plateau and then begins to decrease.

Figure 6 shows estimates of MEVC as a function of Metglas thickness for both types of trilayers with Ni and PZT. Both structures are expected to have higher maximum MEVC than bilayer of Ni-PZT. The maximum value for Type-1 structure is a factor of higher than the value for Ni-PZT bilayer whereas the maximum value for MEVC is an order of magnitude than for the Ni-PZT bilayer.

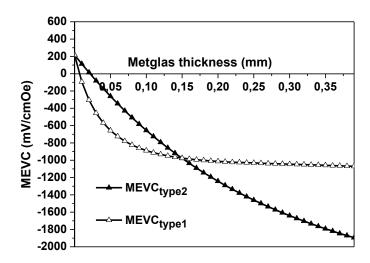
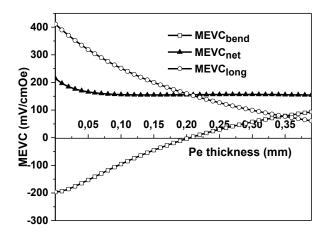


Figure 6. Estimated dependence of MEVC in a Ni - PZT - Metglas - (type-1) and Ni - Metglas - PZT (type-2) three-layered structures on the Metglas layer thickness. The PZT layer thickness $t^p = 0.2 \, mm$, the Ni thickness $t^{m1} = 0.2 \, mm$.

Similar theoretical values of ME response and sensitivity are shown in Figure 7 and 8 for Type-1 trilayer with Ni-PZT-Permendur (for positive magnetostriction). The difference between Permendur and Metglas layers is that Pe has a factor of two higher Young's modulus value than Metglas, but Permendur has fifteen-time smaller piezomagnetic coefficient value than Metglas. Thus, (MEVC) $_{long} \sim 0$ for Permendur layer thickness which is eight time higher than Metglas thickness.



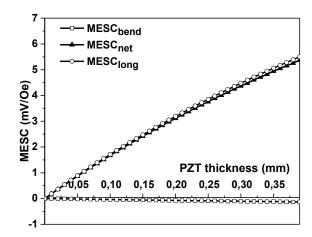


Figure 7. Estimated dependence of MEVC in a Ni - PZT – Permendur first type three-layered structures on the Permendur layer thickness. The PZT layer thickness $t^p = 0.2 \ mm$, the Ni thickness $t^{m1} = 0.2 \ mm$.

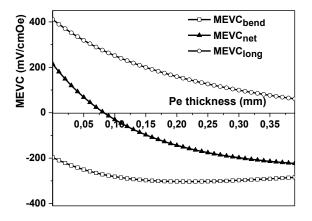
Figure 8. Estimated dependence of MESC in a Ni - PZT – Permendur first type three-layered structures on the PZT layer thickness. The Ni layer thickness $t^{m1} = 0.2 \ mm$, the Permendur thickness $t^{m2} = 0.15 \ mm$.

Figures 9 and 10 show the theoretical estimates of the dependencies of the MEVC and MESC for Type-2, Ni – Permendur-PZT, trilayer. As can see from Fig. 7 and Fig.9 the MEVC for three-layered Ni – PZT – Pe structures has the same value as for bilayer Ni – PZT structures, thus using the three-layered Ni – PZT – Pe structures are impractical.



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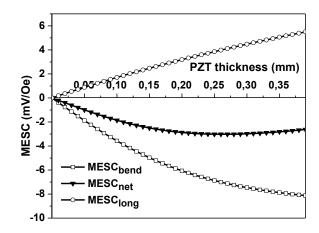


Figure 9. Estimated dependence of MEVC in a Ni - Permendur - PZT second type three-layered structures on the Permendur layer thickness. The PZT layer thickness $t^p = 0.2 \, mm$, the Ni thickness $t^{m1} = 0.2 \, mm$.

300

200

100

0

-100

-200

-300

MEVC (mV/cmOe)

Figure 10. Estimated dependence of MESC in a Ni - Permendur - PZT second type three-layered structures on the PZT layer thickness. The Ni layer thickness $t^{m1} = 0.2 \ mm$, the Permendur thickness $t^{m2} = 0.15 \ mm$.

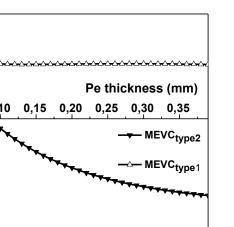


Figure 11. Estimated dependence of MEVC in a Ni - PZT - Pe - first type and Ni - Pe - PZT second type three-layered structures on the Permendur layer thickness. The PZT layer thickness $t^p = 0.2 \, mm$, the Ni thickness $t^{m1} = 0.2 \, mm$.

On the Fig. 11 shown the dependencies of the net MEVC as a function of Pe thickness for both the first and second types of structures. As can see from Fig.11 both Ni - PZT - PZT

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Pe structures have the same value as for bilayer Ni – PZT structures, thus using the three-layered Ni – PZT – Pe structures are impractical.

4. Conclusions

The best ME coupling have the asymmetric three-layered Ni – Metglas – PZT structures. The ME coupling in these structures is in several time more than bilayer Ni – PZT structures. This fact connected with them, that both materials Ni and Metglas have been the maximum piezomagnetic coefficient in the region bias magnetic field near 50 Oe. The three-layered Ni – Pe – PZT structures demonstrated the same ME coupling as bilayer Ni – PZT structures at bias magnetic field near 50 Oe. This is explained by that Pe has maximum piezomagnetic coefficient at bias magnetic field near 600 Oe, but at this magnetic field the Ni piezomagnetic coefficient become is very decreases, thus using three - layered Ni-PZT-Pe structures are impractical.

The use of three-layer structures makes it possible to control the ME characteristics over a wide range.

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