

Article

Atomic Mechanisms of Crystallization in Nano-Sized Metallic Glasses

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Abstract: Understanding crystallization mechanisms in nano-sized metallic glasses (MGs) is important to the manufacturing and application of these new nanomaterials that possess a unique combination of structural and functional properties. Due to the two-dimensional projections and limited spatial and/or temporal resolutions in experiments, significant questions (e.g., whether nucleation takes place on the free surface or in a near-surface layer) regarding this subject remain under debate. Here, we address these outstanding questions using molecular dynamics simulations of crystallization in MG nanorods together with atomistic visualization and data analysis. We show that nucleation in the nano-sized MGs predominantly takes place on the surface by converting the high-energy liquid surface to a lower-energy crystal surface (the most close-packed atomic plane). This is true for all the nanorods with different diameters studied. On the other hand, the apparent growth mode (inward/radial, lateral or longitudinal) and the resulting grain structure are more dependent on the nanorod diameter. For a relatively big diameter of the nanorod, the overall growth rate does not differ much among the three directions and the resulting grains are approximately semispherical. For small diameters, grains appear to grow more in longitudinal direction and some grains may form relatively long single-crystal segments along the length of the nanorod. The reasons for the difference are discussed. The study provides direct atomistic insights into the crystallization mechanisms in nano-sized MGs, which can facilitate the manufacturing and application of these new advanced materials.



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1. Introduction

Metallic glasses (MGs) are highly non-conventional metallic alloys that possess an overall disordered (glassy) atomic structure, without any crystal grains or crystal-related defects. The unique structure endows MGs with a host of properties far surpassing those of their crystalline counterparts (conventional alloys), such as exceptionally high strength, hardness, wear- and corrosion-resistance, near-net-shape castability and thermoplastic processability [1–16]. One of the recent developments in this field is the creation of nano-sized MGs in the form of nanowires or nanorods [17–20]. This brings about possibilities to utilize the advantageous properties of MGs in nanoscale electromechanical or biomedical devices.

MGs are metastable materials and always possess a tendency to crystallize. In order to retain their glassy structure and associated properties, crystallization needs to be avoided during manufacturing process (or, heat-involving applications) of nano-sized MGs, particularly at elevated temperatures as employed in nanomoulding/nanoimprinting. Therefore, understanding how crystallization takes place in nano-sized MGs is of practical importance as well as fundamental scientific interest. From a different perspective, nano-sized MGs could be used as a precursor for producing nano-sized alloys with a poly- or single-crystalline structure, which also requires a good understanding of crystallization of nano-sized MGs.

One seemingly reasonable conjecture has been that the free surface of a nano-sized MG acts as the heterogeneous nucleation site for crystal formation, based on the well-known fact that the surface atoms are in a higher energy state than the interior atoms. However, if a crystal nucleus does form at the MG surface, the crystal atoms exposed on the surface will also possess higher energy than the atoms in the crystal interior, and hence it is not immediately clear why energetics should favor the crystal nucleation on the surface of a nano-sized MG. Recently, it has been proposed [21] that, instead of heterogeneous nucleation on the free surface, crystal nucleation may occur in a homogeneous fashion within a near-surface layer (~1 nm from the free surface) due to the faster dynamics therein—compared with the further inside of the nano-sized MG.

In situ heating experiments on a TEM (transmission electron microscope) [22] have been used to study crystallization of MG nanorods and have revealed clear effects of the sample size (diameter) on the apparent onset of crystallization. However, due to the 2D-projection nature of the TEM technique (as well as most other experimental techniques), it is not possible to determine the exact positions of the observed crystallites with respect to the 3D surface in the experiments (the information on the free surface above or below the central projected cross-sectional plane is overlapped with the information in the interior of the sample). Furthermore, the still limited spatial and time resolutions on most existing characterization instruments do not allow the capture of the full process of nucleation (i.e., subcritical-to-supercritical transition of a nucleus) or even early stage of crystal growth. As a result, the fundamental questions of where exactly nucleation takes place in a nano-sized MG and why, and how a supercritical nucleus grows three-dimensionally after nucleation, remain to be answered.

In this work, we use molecular dynamics (MD) simulations to investigate the crystal nucleation and growth in nano-sized MG samples. MD simulations, combined with posterior structural and potential energy analysis and atomistic visualization, provide access to great atomic-level details that are much needed to better understand crystallization of nano-sized MGs. The simulation results directly help address the aforementioned key questions regarding crystallization in nano-sized MGs.

2. Methodology

The open-source LAMMPS (Large-scale Atomic/Molecular Massively Parallel Simulator) code [23] developed and distributed by the Sandia National Laboratory is used for all the MD simulations in this study. The material used here is elemental tantalum (Ta), which is chosen because of its relatively good glass-forming ability, high thermal stability in the solid glass regime, and yet strong tendency to crystallize in the supercooled liquid regime [24–29]. The EAM (Embedded Atom Method) potential [28] for Ta developed on the basis of both experimental and quantum mechanical reference data is employed in our MD simulations.

A fairly large rectangular Ta MG sample with dimensions of $\sim 28 \text{ nm} \times 28 \text{ nm} \times 40 \text{ nm}$, containing 1,536,000 atoms, is first prepared by cooling the molten Ta from 2400 K to 300 K (cooling rate used: 5 K/ps), under all-periodic boundary conditions and NPT (controlled particle number N , pressure P , and temperature T) ensemble. The purpose of this step is to obtain a single large enough MG sample from which nanorods of different diameters can be simply carved out (without having to go through individual melt-cooling processes). This step takes $\sim 29 \text{ h}$ using 28 cores (Intel Xeon E7-4830 v4) on a single node of a high performance computing (HPC) system. The rectangular sample is then cut into nanorods with different diameters (x and y dimensions), namely, 10, 15, 20, and 25 nm, keeping the original height (z -dimension). The boundary conditions for the x and y dimensions are changed to “shrink-wrapped”, which sets the cylindrical surface to be a free surface. Each nanorod sample is then relaxed for 50 ps at 300 K and subsequently heated up at a rate of 1 K/ps towards 2500 K to induce crystallization. The potential energy, along with spatial coordinates, of each atom is exported for a series of temperatures during each simulation. Post-simulation structural and potential energy analyses are conducted using

the Ovito (Open Visualization Tool) program [30]. More specifically, for structural analysis, atoms are divided into three categories: 1. BCC (body centered cubic, the preferred crystal structure by Ta) atoms, i.e., atoms with a BCC local environment; 2. BCC shell atoms, i.e., the first nearest neighbors of the BCC atoms; and 3. The disordered matrix atoms, i.e., those that are neither BCC atoms nor BCC shell atoms. The BCC atoms are identified through the polyhedral template matching function inside OVITO with a root mean square deviation cutoff of 0.12. The BCC shell atoms are identified as the neighbors surrounding the BCC atoms that are within the nearest neighbor distance as determined from the valley between the first and the second coordination peaks on the pair distribution function.

3. Results and Discussion

Figure 1 shows the spatial distribution of the BCC (blue colored) and the BCC shell (gray colored) atoms in the 25 nm diameter MG nanorod at different temperatures during the simulated heating process. Note that the matrix (supercooled liquid) atoms are intentionally omitted in the figure. It is evident from Figure 1 that the sample is undergoing crystallization. Both the top view (orthogonal projection, upper row in Figure 1) and the side view (perspective projection, lower row in Figure 1) clearly show that although BCC clusters are forming throughout the 3D material, nucleation, i.e., successful transition from a subcritical to supercritical nucleus, is virtually all occurring on the free surface. The subcritical nuclei (BCC clusters) dynamically form and re-dissolve into the supercooled liquid matrix, both in the interior and on the free surface. The supercritical nuclei formed on the free surface grow in three directions: inward/radial, lateral or longitudinal, at approximately equal rates, leading to a nearly semispherical shape of crystal grains (Figure 1d,e,i,j).

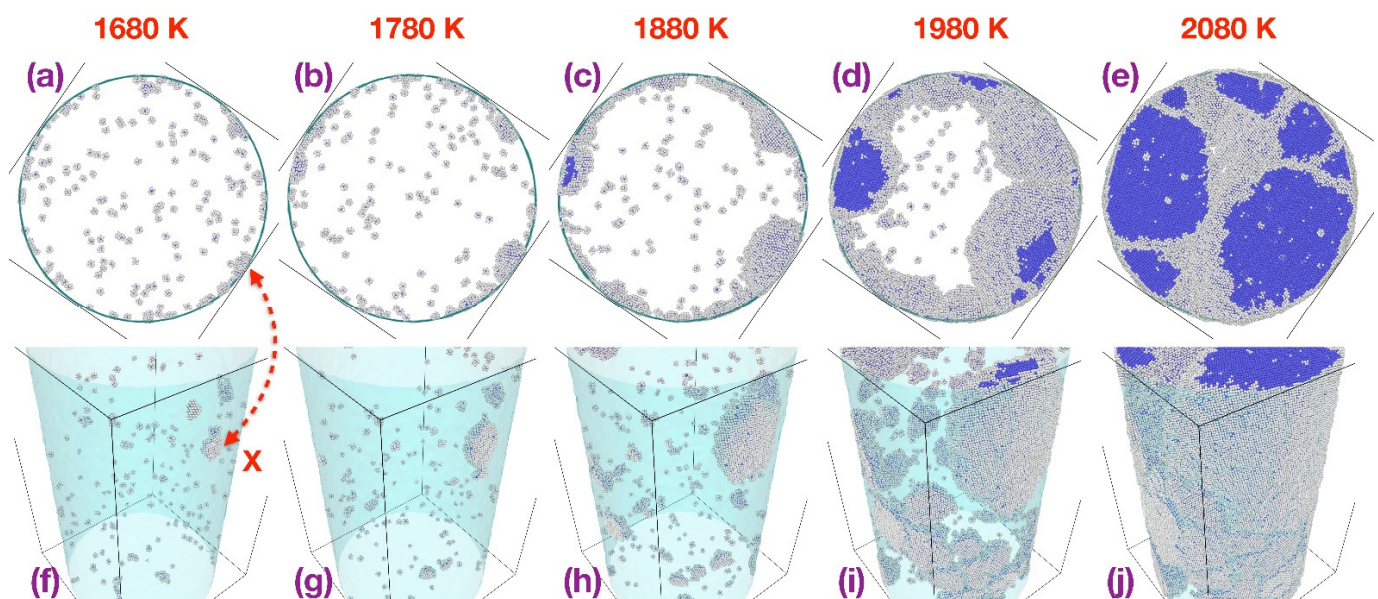


Figure 1. Spatial distribution of BCC (blue colored) and BCC shell (gray colored) atoms in the 25 nm diameter MG nanorod at different temperatures during the simulated heating process. The matrix (supercooled liquid) atoms are made invisible. Upper row (a–e): top view (orthogonal projection). Lower row (f–j): side view (perspective projection).

To give more details, Figure 2 provides a close-up view of the crystal grain marked as “X” in Figure 1a,f. During the nucleation process and early growth stage (as represented by Figure 2a,b), the grain exposes a single {1 1 0} plane on the free surface. It is well-known that {1 1 0} planes are the most close-packed in a BCC crystal structure, and when exposed on the surface, provide the lowest crystal surface energy. The {1 1 0} planes are indeed found to be used as the crystal surface by all the supercritical nuclei, including Grain X and others. As

shown in Figure 2b, the newly formed supercritical nucleus of Grain X on the free surface is essentially a stack of a few $\{1\ 1\ 0\}$ planes, with a shape more like a platelet than a semisphere. This indicates an initial faster growth in the lateral and longitudinal directions than the inward/radial direction. As it enters the later growth stage (Figure 2c), however, a single $\{1\ 1\ 0\}$ plane can no longer serve as the crystal surface due to the curvature of the sample surface, and steps of $\{1\ 1\ 0\}$ planes emerge on the crystal surface. Since steps represent a higher energy state than a perfect single $\{1\ 1\ 0\}$ plane, this slows down the growth of the crystal grain on the surface, and the inward/radial growth catches up, driving the overall shape of the grain towards a near-semisphere.

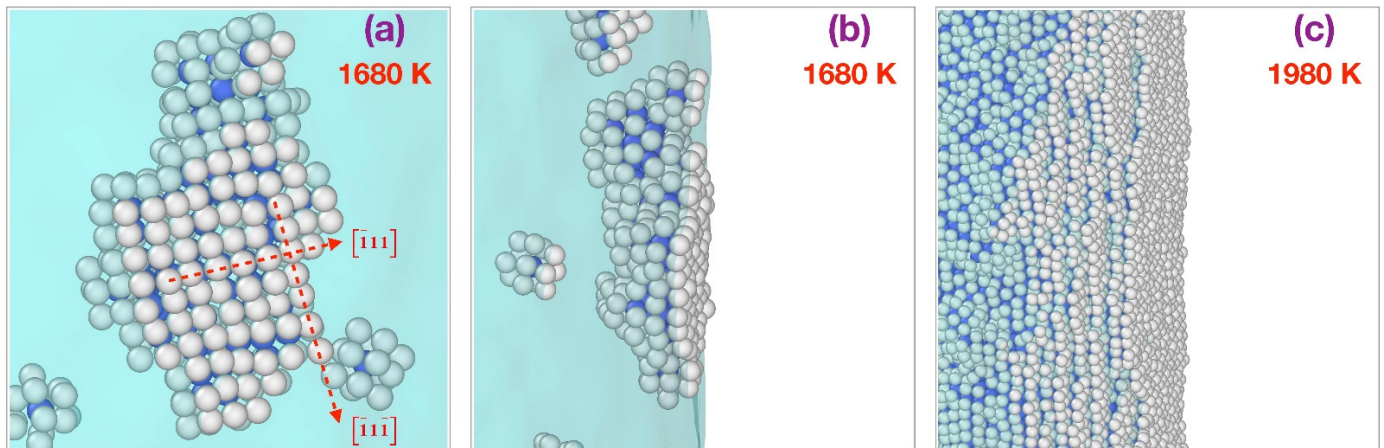


Figure 2. Close-up view (perspective projection) of the crystal grain marked as “X” in Figure 1a,f at 1680 K (a,b) and 1980 K (c). Blue: BCC atoms; Gray: BCC shell atoms.

To understand why nucleation predominantly occurs on the surface, we perform potential energy analysis for atoms within a 3D volume surrounding the Grain X. This includes BCC atoms, BCC shell atoms and matrix (supercooled liquid) atoms. Figure 3a–c present the front view (from outside the surface) of these atoms at 1540, 1640 and 1740 K, respectively, using the same color scheme (blue: BCC; gray: non-BCC) as in Figures 1 and 2 to indicate the structural environment of each atom. It can be seen that the Grain X (marked with the dashed circle) is nucleated around 1640 K and is growing at 1740 K. Figure 3d–f show the corresponding potential energy (E_p) distribution among the atoms, represented by a “hot” color scheme (black-red-yellow-white, in the order of increasing E_p). By comparing Figure 3e with Figure 3d and referring to the corresponding structural change in Figure 3a,b, one can notice that the BCC-shell atoms exposed on the surface due to nucleation of the Grain X create a darker, lower energy zone in the middle of the (supercooled) liquid surface. This lower energy zone on the surface expands as the grain grows, as shown by Figure 3b,c,e,f.

To be more quantitative, we further divide the atoms in Figure 3 into five categories: 1. BCC atoms, 2. BCC shell atoms on the surface, 3. BCC shell atoms in the sample interior, 4. liquid atoms on the surface, and 5. liquid atoms in the sample interior. We then calculate the average potential energy ($\bar{E}_p$) for each category at 1740 K (where there are an adequate number of atoms in each category). The resulting $\bar{E}_p$ value is: -7.80 , -6.77 , -7.69 , -6.54 , -7.68 eV/atom, for the five categories named above, respectively. The BCC atoms possess the lowest $\bar{E}_p$ among the five, as expected from their crystalline environment. These atoms correspond to the shaded zone, “Crystal (X)”, in Figure 4—the traditional sketch used to explain heterogeneous nucleation. The $\bar{E}_p$ of the liquid interior atoms (corresponding to the “Liquid (L)” zone in Figure 4) is higher than that of the BCC atoms by 0.12 eV/atom. The BCC shell atoms on the surface, corresponding to the zone shared by X and S in Figure 4, possess an energy higher than the BCC atoms by 1.03 eV/atom. The BCC shell atoms in the sample interior, corresponding to the zone shared by X and L in Figure 4, possess an

energy higher than the BCC atoms by 0.11 eV/atom, but lower than the BCC shell atoms on the surface by 0.92 eV/atom. If considering this fact only, one might anticipate that a BCC nucleus would prefer to build its shell entirely in the sample interior. However, it is important to notice that the $\bar{E}_p$ of the BCC shell atoms in the sample interior is only 0.01 eV/atom lower than that of the liquid interior atoms, while the $\bar{E}_p$ of the BCC shell atoms on the surface is 0.23 eV/atom lower than that of the liquid surface atoms (L - S shared zone in Figure 4). This means that the BCC shell in the sample interior is more vulnerable to the attack (i.e., redissolution) by the liquid interior than the BCC shell on the surface is to the attack by the liquid surface atoms. This explains why nucleation predominantly takes place on the nanorod surface.

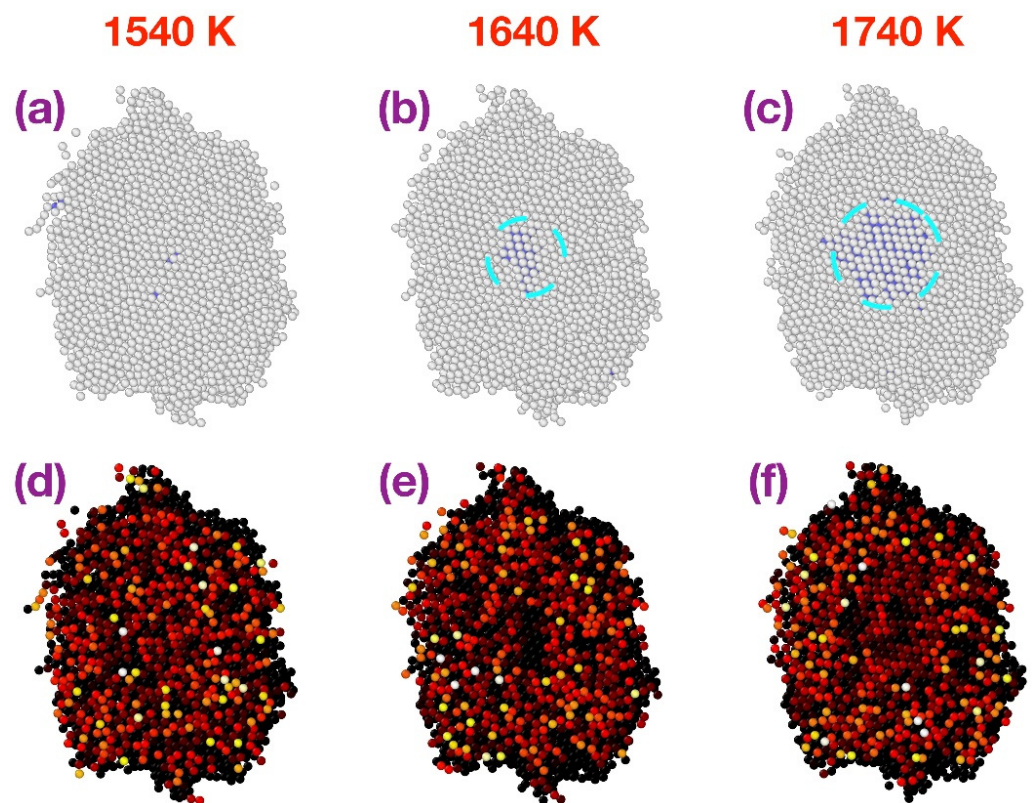


Figure 3. Front view (from outside the surface) of atoms surrounding Grain X (defined in Figure 1) at 1540, 1640 and 1740 K during nucleation and early growth of Grain X. Upper row (a–c): local structure (blue—BCC, gray—non-BCC). Lower row (d–f): atomic potential energy (E_p) represented by a “hot” color scheme (black-red-yellow-white, in the order of increasing E_p).

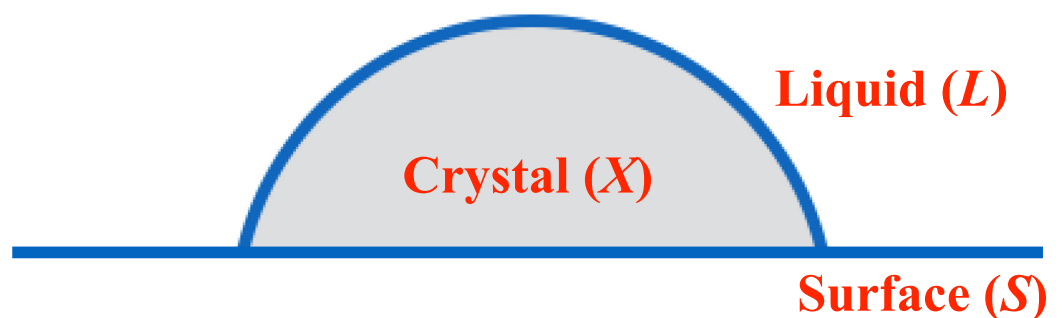


Figure 4. Schematics showing different regions surrounding a crystal grain nucleated from the surface.

As the early nucleated grains grow in three dimensions, more supercritical nuclei are forming on the nanorod surface. The transformation of the surface of the 25 nm diameter nanorod from the (supercooled) liquid surface to the crystal surface is completed by 2160 K. Shortly after that, all the interior liquid atoms are transformed to either BCC or BCC shell atoms by 2220 K due to continued grain growth. The resulting polycrystalline structure is presented in Figure 5 where colors are used to indicate the different orientations of the grains. The grains are mostly close to semispherical (or, equiaxed but halved along the radial direction).

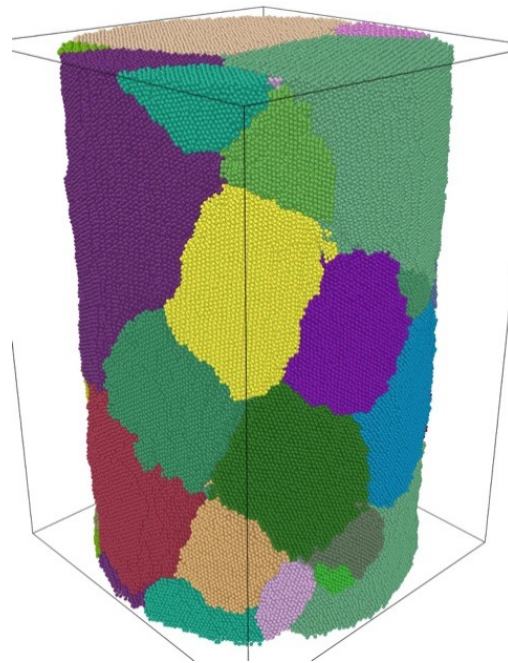


Figure 5. The grain structure (2180 K) resulting from the crystallization of the 25 nm diameter MG nanorod. Colors indicate different grain orientations.

The main features of nucleation and growth described above for the 25 nm diameter nanorod are largely applicable to the 20, 15 and 10 nm diameter nanorods. In particular, the nucleation in all these samples predominantly takes place on the free surface. Figure 6 presents the top and the side views of all BCC clusters (subcritical or supercritical) in the 10 nm diameter nanorod at different temperatures, which again shows the heterogeneous nucleation on the surface and the three-dimensional growth at the early stage.

However, some new features of crystal growth appear with decreasing nanorod diameter. Grain Y, which is marked in Figure 6e, initially grows three dimensionally but later fragments into three smaller grains with a reduced dimension (width) in the lateral direction, as can be seen from Figure 6h. The subsequent growth of these fragments leads to the three longitudinally extending grains at the front and middle of Figure 7 which appear to have been growing preferentially in the longitudinal direction. The fragmentation of the Grain Y has two reasons: (a). the cylindrical surface with the small diameter exerts bending strain on the original single $\{1\ 1\ 0\}$ surface plane of the supercritical nucleus, and (b). formation and joining of affiliated BCC clusters at the frontline of growth with somewhat different orientations (see Figure 6g). Fragmentation, however, does not occur to all the grains.

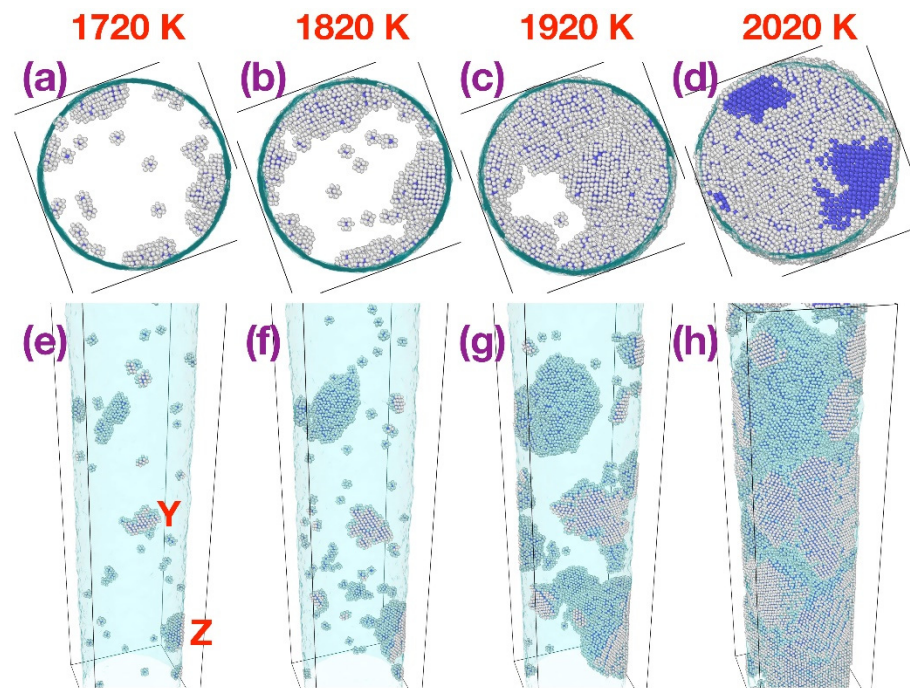


Figure 6. Spatial distribution of BCC (blue colored) and BCC shell (gray colored) atoms in the 10 nm diameter MG nanorod at different temperatures during the simulated heating process. The matrix (supercooled liquid) atoms are made invisible. Upper row (a–d): top view (orthogonal projection). Lower row (e–h): side view (perspective projection). The two grains labelled as “Y” and “Z” are discussed in the text.

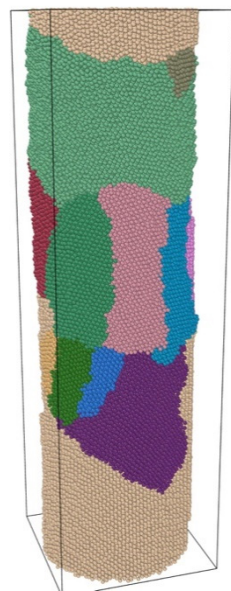


Figure 7. The grain structure (2100 K) resulting from the crystallization of the 10 nm diameter MG nanorod. Colors indicate different grain orientations.

Another new feature of growth is demonstrated by the Grain Z which is marked in Figure 6e. This grain manages to fill the entire cross section (by ~2020 K) before being interrupted laterally by other grains, and the subsequent growth of this grain becomes solely longitudinal. This produces a single-crystal segment along the length of the nanorod, as can be seen at the bottom of Figure 7 (another segment, colored green near the top, is also a single crystal grain). Two factors, both related to the small diameter of the nanorod,

are considered to have contributed to this behavior. The first one is the shorter dimension over which a supercritical nucleus needs to grow in the radial direction in order to fill the cross section. The second one is the smaller number of supercritical nuclei (grains) being formed on the surface due to the reduced surface area, which can be seen from Figure 8 where the number of supercritical nuclei (grains) is plotted as a function of time (and temperature) for the four different nanorod diameters studied. While the 25 nm and 20 nm diameter nanorods produce similar numbers of supercritical nuclei, the 15 nm and 10 nm diameter nanorods clearly show the decreasing number of supercritical nuclei as the nanorod diameter goes down. The smaller number of supercritical nuclei provides Grain Z with more time to grow and fill the cross section without interruption. The reduced nucleation probability/frequency due to reduced surface area in very small diameter nanorods has previously been inferred in an experimental work [22] although it is not possible to precisely determine the number of supercritical nuclei in experiments because of limitations of experimental techniques as discussed in Introduction.

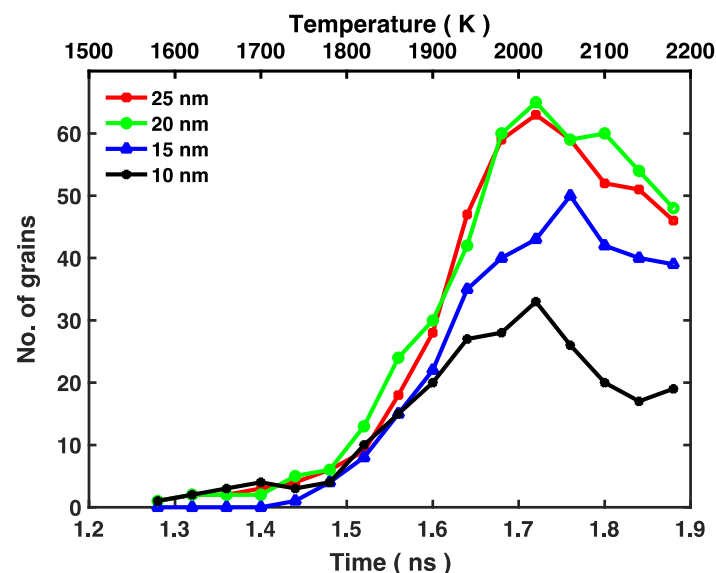


Figure 8. Number of supercritical nuclei (grains) as a function of time (and temperature) for the nanorods of different diameters (the drop past the peaks is due to coarsening/merging of the grains with continuously increasing temperature).

Finally, we point out that the above reported results should be largely valid over a range of nanorod diameters. In the meantime, it can also be inferred that, when the nanorod diameter increases beyond a certain value (possibly a few hundred nanometers), homogeneous nucleation of crystals from the interior of the supercooled liquid may start to take a role before the supercritical nuclei formed on the free surface could transform the entire sample to a crystalline structure. MD simulation of the crystallization of the bigger diameter nanorods, however, would be much more computationally expensive.

4. Conclusions

We have performed molecular dynamics simulations of crystallization in metallic glass nanorods with varied diameters, and post-simulation atomistic visualization and data analysis. Our results clearly show that crystal nucleation predominantly takes place on the free surface for all the nanorods studied. Structural analysis reveals that the crystal grains all expose the most close-packed plane (family) to the surface. Statistical analysis reveals a larger potential energy difference between the crystal shell on the surface and the (supercooled) liquid surface, than between the crystal shell inside the liquid and the liquid bulk. This shows that the crystal shell on the surface is more resistant than the crystal shell in the interior to redissolution by surrounding liquid atoms, thereby explaining

the predominance of surface nucleation. After nucleation, supercritical nuclei grow three dimensionally along the radial/inward, lateral, and longitudinal directions in a nanorod with a relatively big diameter, producing nearly semispherical grains. In a small diameter nanorod, some grains fragment into longitudinally extending sub-grains, while some others grow and fill the entire cross section of the nanorod and subsequently develop into a single-crystal segment along the length of the nanorod. The study uncovers many atomic scale details of crystallization in nano-sized MGs that are currently missing due to limitations in existing experimental techniques. The findings also provide a useful scientific reference for the manufacturing and application of nano-sized metallic glasses as advanced structural and functional materials, or, as a precursor for producing nano-sized crystalline metallic alloys.

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Conflicts of Interest: The authors declare no conflict of interest.

References

- Greer, A.L. Metallic glasses. *Science* **1995**, *267*, 1947–1953. [\[CrossRef\]](#) [\[PubMed\]](#)
- Johnson, W.L. Bulk glass-forming metallic alloys: Science and technology. *MRS Bull.* **1999**, *24*, 42–56. [\[CrossRef\]](#)
- Inoue, A. Stabilization of metallic supercooled liquid and bulk amorphous alloys. *Acta Mater.* **2000**, *48*, 279–306. [\[CrossRef\]](#)
- Schroers, J. BULK Metallic Glasses. *Phys. Today* **2013**, *66*, 32–37. [\[CrossRef\]](#)
- Löffler, J.F. Bulk metallic glasses. *Intermetallics* **2003**, *11*, 529–540. [\[CrossRef\]](#)
- Schroers, J.; Johnson, W.L. Ductile bulk metallic glass. *Phys. Rev. Lett.* **2004**, *93*, 255506. [\[CrossRef\]](#)
- Choi-Yim, H.; Johnson, W.L. Bulk metallic glass matrix composites. *Appl. Phys. Lett.* **1997**, *71*, 3808–3810. [\[CrossRef\]](#)
- Choi-Yim, H.; Xu, D.; Johnson, W.L. Ni-based bulk metallic glass formation in the Ni–Nb–Sn and Ni–Nb–Sn–X (X=B,Fe,Cu) alloy systems. *Appl. Phys. Lett.* **2003**, *82*, 1030–1032. [\[CrossRef\]](#)
- Saini, J.S.; Miska, J.P.; Lei, F.; AuYeung, N.; Xu, D. Hafnium based metallic glasses with high density and high glass-forming ability. *J. Alloy. Compd.* **2021**, *882*, 160896. [\[CrossRef\]](#)
- Saini, J.S.; Palian, C.; Lei, F.; Dyal, A.; Auyeung, N.; McQuade, R.; Gupta, S.K.; Cann, D.P.; Xu, D. Rare-earth and precious-metal free Cu-based metallic glasses with superior glass-forming ability and processability. *Appl. Phys. Lett.* **2020**, *116*, 011901. [\[CrossRef\]](#)
- Ponnambalam, V.; Poon, S.J.; Shiflet, G.J. Fe-based bulk metallic glasses with diameter thickness larger than one centimeter. *J. Mater. Res.* **2004**, *19*, 1320–1323. [\[CrossRef\]](#)
- Xu, D.; Lohwongwatana, B.; Duan, G.; Johnson, W.L.; Garland, C. Bulk metallic glass formation in binary Cu-rich alloy series—Cu_{100-x}Zr_x (x=34, 36, 38.2, 40 at.%) and mechanical properties of bulk Cu₆₄Zr₃₆ glass. *Acta Mater.* **2004**, *52*, 2621–2624. [\[CrossRef\]](#)
- Xu, D.; Duan, G.; Johnson, W.L.; Garland, C. Formation and properties of new Ni-based amorphous alloys with critical casting thickness up to 5 mm. *Acta Mater.* **2004**, *52*, 3493–3497. [\[CrossRef\]](#)
- Xu, D.; Duan, G.; Johnson, W.L. Unusual Glass-Forming Ability of Bulk Amorphous Alloys Based on Ordinary Metal Copper. *Phys. Rev. Lett.* **2004**, *92*, 245504. [\[CrossRef\]](#)
- Xu, D. *Development of Novel Binary and Multi-Component Bulk Metallic Glasses*; California Institute of Technology: Pasadena, CA, USA, 2005.
- Park, E.S.; Kim, D.H. Phase separation and enhancement of plasticity in Cu–Zr–Al–Y bulk metallic glasses. *Acta Mater.* **2006**, *54*, 2597–2604. [\[CrossRef\]](#)
- Liu, Y.; Liu, J.; Sohn, S.; Li, Y.; Cha, J.J.; Schroers, J. Metallic glass nanostructures of tunable shape and composition. *Nat. Commun.* **2015**, *6*, 7043. [\[CrossRef\]](#)
- Zhou, C.; Datye, A.; Chen, Z.; Simon, G.H.; Wang, X.; Schroers, J.; Schwarz, U.D. Atomic imprinting in the absence of an intrinsic length scale. *APL Mater.* **2020**, *8*, 111104. [\[CrossRef\]](#)
- Kumar, G.; Tang, H.X.; Schroers, J. Nanomoulding with amorphous metals. *Nature* **2009**, *457*, 868–872. [\[CrossRef\]](#)
- Schroers, J. The superplastic forming of bulk metallic glasses. *JOM* **2005**, *57*, 35–39. [\[CrossRef\]](#)

21. Zhang, P.; Maldonis, J.J.; Liu, Z.; Schroers, J.; Voyles, P.M. Spatially heterogeneous dynamics in a metallic glass forming liquid imaged by electron correlation microscopy. *Nat. Commun.* **2018**, *9*, 1129. [[CrossRef](#)]
22. Sohn, S.; Jung, Y.; Xie, Y.; Osuji, C.; Schroers, J.; Cha, J.J. Nanoscale size effects in crystallization of metallic glass nanorods. *Nat. Commun.* **2015**, *6*, 8157. [[CrossRef](#)] [[PubMed](#)]
23. Plimpton, S. Fast Parallel Algorithms for Short-Range Molecular Dynamics. *J. Comput. Phys.* **1995**, *117*, 1–19. [[CrossRef](#)]
24. Chen, F.; Xu, D. 3D surface condensation of large atomic shear strain in nanoscale metallic glasses under low uniaxial stress. *J. Phys. Condens. Matter* **2019**, *31*, 025401. [[CrossRef](#)] [[PubMed](#)]
25. Xu, D.; Chen, F. Continuously variable atomic structure in monatomic metallic glasses through active icosahedral dynamics below glass transition temperature. *J. Appl. Phys.* **2018**, *124*, 125101. [[CrossRef](#)]
26. Xu, D.; Wang, Z.; Chang, T.-Y.; Chen, F. Inverted core-shell potential energy landscape of icosahedral clusters in deeply undercooled metallic liquids and glasses and its effect on the glass forming ability of bcc and fcc metals. *J. Phys. Condens. Matter* **2020**, *32*, 405402. [[CrossRef](#)]
27. Chang, T.-Y.; Wang, Z.; Xu, D. Formation energetics/dynamics of icosahedral clusters in supercooled metallic liquids in the dynamic equilibrium regime: Gibbs free energy, entropy, enthalpy, and connection to coordination shells. *J. Mater. Res.* **2023**. [[CrossRef](#)]
28. Zhong, L.; Wang, J.; Sheng, H.; Zhang, Z.; Mao, S.X. Formation of monatomic metallic glasses through ultrafast liquid quenching. *Nature* **2014**, *512*, 177–180. [[CrossRef](#)]
29. Stella, K.; Bürstel, D.; Hasselbrink, E.; Diesing, D. Thin tantalum films on crystalline silicon—A metallic glass. *Phys. Status Solidi Rapid Res. Lett.* **2011**, *5*, 68–70. [[CrossRef](#)]
30. Stukowski, A. Visualization and analysis of atomistic simulation data with OVITO—The Open Visualization Tool. *Model. Simul. Mater. Sci. Eng.* **2010**, *18*, 015012. [[CrossRef](#)]

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