

Ramsey Spectroscopy of the $2S_{1=2}$ Hyperfine Interval in Atomic Hydrogen

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The $2S_{1=2}$ hyperfine interval in atomic hydrogen was measured using Ramsey spectroscopy with a thermal beam cooled to cryogenic temperatures. The measured value is $177\,556\,838.87(85)$ Hz, which represents the most precise determination of this interval to date. The $1S_{1=2}$ hyperfine interval $\delta 1S_{1=2}$ and the $2S_{1=2}$ hyperfine interval $\delta 2S_{1=2}$ can be combined to give the quantity $D_{21} \approx \delta 2S_{1=2} - \delta 1S_{1=2}$, which mostly eliminates uncertainty due to nuclear structure effects and is well described by bound-state quantum electrodynamics. Using the value of $\delta 2S_{1=2}$ from this work gives a value of $D_{21}^{\text{expt}} \approx 48\,959.2\delta 6.8$ Hz, which is in agreement with the theoretical value of $D_{21}^{\text{Theory}} \approx 48\,954.1\delta 2.3$ Hz.

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The simple structure of the hydrogen atom allows for precise calculations that can be compared with experiment. Not only has hydrogen been used to determine fundamental constants, such as the proton charge radius and the Rydberg constant [1], but it has also been used as a theoretical testing ground for quantum mechanics and quantum electrodynamics (QED) for over a century. Using hydrogen masers, the ground-state hyperfine interval in atomic hydrogen has been measured extremely precisely, with a relative uncertainty of roughly 10^{-12} [2–5]. Calculations of this transition with QED corrections are available [6–8]. Unfortunately, a comparison of the experimentally determined value with theory is limited by an insufficient understanding of proton structure effects [9]. However, a linear combination of the $1S_{1=2}$ and $2S_{1=2}$ hyperfine intervals given by

$$D_{21} \approx \delta 2S_{1=2} - \delta 1S_{1=2} \quad \delta 1\text{p}$$

largely eliminates the theoretical uncertainty in nuclear structure and is a stringent test of fourth-order bound-state QED [6–8,10–14]. In 2002, the theoretical value of D_{21} was calculated including fourth-order QED corrections [6,7]. The value was updated slightly in 2006 after reevaluating the self-energy correction and adding a numerically small logarithmic recoil correction [8]. A high-precision numerical calculation of the self-energy was then performed in 2008, resulting in $D_{21}^{\text{Theory}} \approx 48\,954.1\delta 2.3$ Hz [15], which is the most up-to-date published value.

In addition to bound-state QED tests, several authors have noted that measurements of D_{21} can be used to provide constraints on light bosons with weak coupling to standard model particles [16–18]. Such hypothetical particles could manifest themselves by producing an additional spin-dependent interaction between the proton and electron, which would cause a deviation between the experimental and theoretical values of D_{21} .

Because of the very high precision of the ground-state hyperfine measurements, the experimentally determined values of D_{21} in atomic hydrogen are limited by the uncertainty in measurements of the $2S_{1=2}$ hyperfine interval. While direct measurements of this magnetic-dipole radio-frequency (rf) transition have been performed in the past [19,20], substantial improvements in precision optical spectroscopy have also allowed for measurements through the $1S_{1=2} - 2S_{1=2}$ two-photon optical transition [21,22]. The most recent optical measurement was $\delta 2S_{1=2} \approx 177\,556\,834.3\delta 6.7$ Hz, resulting in $D_{21}^{\text{expt}} \approx 48\,923\delta 54$ Hz, which is in good agreement with theory.

Here, we present a rf measurement of the $2S_{1=2}$ hyperfine interval using Ramsey's method of separated oscillatory fields. The last measurement using Ramsey's method was performed by Heberle et al. in 1956 [19]. In addition to the general advances in experimental equipment and techniques since that time, we notably have the ability to selectively populate the $2S_{1=2}^{F=0}$ state using the $1S_{1=2} - 2S_{1=2}$ two-photon transition before spectroscopy (as in [23,24]). This simplifies the rf measurement and allows for the adjustment of the mean velocity of our atomic beam through the control of our cryogenic nozzle. These advances have allowed for a reduction in the uncertainty of D_{21}^{expt} by a factor of ≈ 8 as compared to the previous best optical measurement [22] and by a factor of ≈ 60 as compared to the previous measurement using rf Ramsey spectroscopy [19].

The experimental apparatus to generate cryogenic $2S_{1=2}^{F=0}$ or $2S_{1=2}^{F=1}$ hydrogen atoms has been previously described in [24]. Additionally, the velocity distribution of the atomic beam was characterized in [25]. After preparation of atoms in the $2S_{1=2}^{F=0}$ state, the atoms enter the rf spectroscopy chamber. The rf spectroscopy region consists of two copper loops separated by a distance of 28 cm. Each loop is

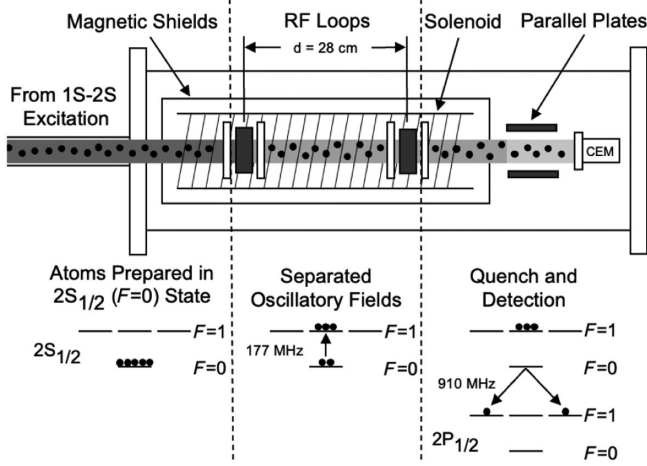


FIG. 1. Schematic of the experimental apparatus. Atoms initially prepared in the $2S_{1/2}^{F=0}$ state enter a magnetically shielded region where Ramsey spectroscopy is performed. A solenoid allows for a bias magnetic field to be applied. Any remaining population in the $2S_{1/2}^{F=0}$ state is selectively quenched to the $2P_{1/2}^{F=1}$ state using an electric-dipole transition. The excited-state population is detected using a CEM.

driven by a rf source to generate an oscillating magnetic field at ≈ 177 MHz to drive population from the $2S_{1/2}^{F=0} \delta m_F = 0$ state to the $2S_{1/2}^{F=1} \delta m_F = 0$ state. The rf sources use direct-digital-synthesis (DDS) and are referenced through an optical fiber link to a small ensemble of cesium beam clocks at the National Institute of Standards and Technology (NIST) WWV radio station, which is in turn referenced to UTC(NIST). Any remaining population in the $2S_{1/2}^{F=0}$ state is selectively quenched to the $2P_{1/2}^{F=1}$ state using an oscillating electric field at ≈ 910 MHz produced by a parallel-plate capacitor. Atoms in the $2S_{1/2}^{F=1}$ state are then detected using a channel-electron multiplier (CEM) in pulse-counting mode to give the final spectroscopic signal. The spectroscopy region is housed within a magnetic shield with a solenoid to produce a small bias magnetic field. Additionally, on both sides of each copper loop is an aluminum ring. These sets of aluminum rings serve to mitigate any net magnetic flux through the solenoid. Without these rings, the combination of rf loops and the solenoid resembles a transformer that could produce an unwanted rf voltage along the length of the solenoid. The entire rf spectroscopy region is coated in colloidal graphite to reduce stray dc electric fields. A schematic of the rf spectroscopy system is shown in Fig. 1.

In Fig. 2, we show a typical Ramsey fringe obtained from our spectrometer. We have overlaid experimental data with a simulation obtained by integrating the Bloch equations given the time-dependent magnetic fields seen by the atoms as they traverse the spectrometer. For the simulation, we used the metastable atom velocity distribution measured previously in our apparatus [25]. As can be seen from the figure, the agreement with our simulation is

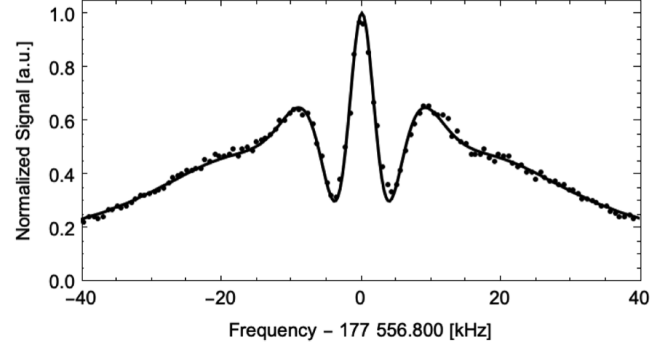


FIG. 2. Example line shape from an average of six scans of the $2S_{1/2}^{F=0} \delta m_F = 0 \rightarrow 2S_{1/2}^{F=1} \delta m_F = 0$ resonance obtained using Ramsey spectroscopy with room temperature hydrogen beam with a numerical simulation overlaid. The FWHM of the central peak is approximately 4 kHz.

excellent, which we believe is a testament to the relatively straightforward experimental apparatus.

A total of 17 measurement runs were performed over the course of two months in 2022. We usually obtained one measurement run in a given day where each run consisted of ≈ 300 individual scans of the resonance. Measurement runs were conducted at varied times of day and typically required 6 h of cumulative data collection. Each scan of the resonance included 32 frequencies about the central feature of the Ramsey fringe. For each scan, frequency points were taken in a new random order to eliminate potential systematic effects related to drifting atomic beam flux. The resonance was fit with a function F , defined by

$$F = B + A \text{sinc}^2 \frac{f - f_0}{\Gamma}; \quad \delta 2p$$

where A and f_0 represent the amplitude and line center frequency, respectively, and Γ is proportional to the width of the line shape. The offset B was included in the fit function because the Ramsey fringe minimum is not zero, in contrast to a sinc^2 function. While the use of a sinc^2 function is an approximation to the true central feature of the Ramsey fringe, we prefer to fit our data with simple analytic functions since it eliminates possible errors stemming from an incorrect numerical model, which necessarily has some assumptions. We also performed our data analysis using a Gaussian fit function and found that it altered our final result by only 0.08 Hz, which shows that our analysis was not, within reason, sensitive to the specific fit function.

A typical challenge to Ramsey spectroscopy is to ensure that there is no phase difference between the two rf spectroscopy regions. The frequency shift due to a phase difference $\Delta\phi$ is inversely proportional to the time atoms spend between the two loops and is approximately

$$f_{\Delta\phi} \approx \frac{v\Delta\phi}{2\pi d}; \quad \delta 3p$$

where v and d are the velocity of the atoms and distance between the rf loops, respectively. Since this systematic shift is proportional to the beam velocity, it can be considered a residual first-order Doppler shift. A common but challenging method to characterize and eliminate $\Delta\phi$ is to exchange the order of the two rf regions in the beamline as in [26]. However, since we have the ability to adjust the velocity of the hydrogen beam, we can perform a linear extrapolation of the measured line center as a function of velocity to extract the true line center. Thus, we do not need to eliminate $\Delta\phi$, but only require that it is stable during a given measurement run.

During a measurement run, we randomly alternate between measurements with the atomic beam nozzle at 6 and 30 K, leaving all other experimentally controlled parameters identical. To eliminate any long-term drifts in the phase between the rf loops, scans are binned, where a single bin includes 20–25 scans of the resonance at a given temperature. Additionally, the relative phase between the two rf loops is monitored using a setup similar to that in [26]. Directional couplers and rf mixers produce voltages proportional to the phase difference between the two incident and reflected signals, which are continuously monitored. We observe no significant drift in either phase over the course of any data collection day. Although the temperature of the cryogenic nozzle is constantly monitored, deviations between the temperature reading of the nozzle and the actual temperature of the hydrogen beam are possible, therefore we perform extrapolations of the line center as a function of the measured transit-time broadened linewidth for each bin, which is proportional to the beam velocity. The rf loop voltage was varied before every run to ensure that power broadening was negligible, and mean velocities determined from the obtained linewidths were consistent with the measured nozzle temperature.

An example extrapolation and the extracted line centers from 17 data runs are shown in Fig. 3. While it may seem intuitive that such extrapolations are linear, the situation is somewhat more complicated since we measure a thermal velocity distribution and not a single velocity class. By simulating our line shapes using thermal velocity distributions, we find that the extrapolations have a small error, which is proportional to $\Delta\phi$, with a maximum magnitude of 0.2 Hz. As an experimental check, we changed $\Delta\phi$ using DDS control for different measurement runs and observed no discrepancies in the extrapolated value. We include a 0.2 Hz uncertainty to account for this slight nonlinearity in the extrapolation.

The shift to the splitting of the $2S_{1=2}^{F=0} \tilde{0}m_F \frac{1}{4} 0P - 2S_{1=2}^{F=1} \tilde{0}m_F \frac{1}{4} 0P$ transition in the presence of a static magnetic field is quadratic and has the value $22.184 \text{ kHz} = G^2$ [19]. In order to characterize any residual field along the direction of the atomic beam remaining after magnetic shielding, we applied a bias field at various field strengths and measured the line center as shown in Fig. 4. We find a

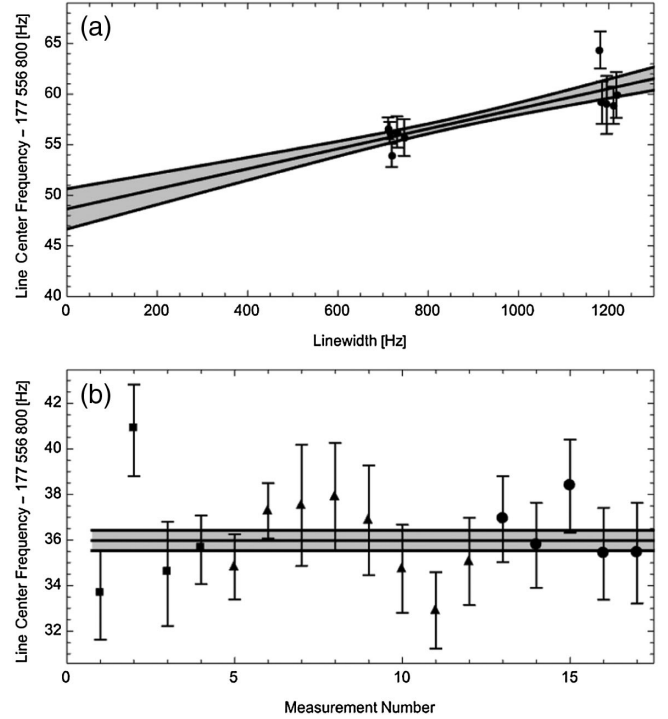


FIG. 3. (a) Example phase shift extrapolation between temperatures of 6 and 30 K as a function of the extracted linewidth. The shaded gray region corresponds to the 1 standard deviation confidence interval. (b) Extrapolated zero-phase line centers after bias magnetic field correction. Squares, triangles, and circles represent data taken at 8, 16, and 24 mG applied magnetic field, respectively. The shaded gray region represents 1 standard deviation from the statistical mean. The reduced χ^2 for the 17 datasets is 1.05.

residual field of $0.14(13) \text{ mG}$, which agrees well with the simulated performance of our magnetic shield along with measurements of Earth's field near the apparatus.

The maximum magnetic field applied during the measurement runs shown in Fig. 3(b) is 24 mG. Taking into account the residual field and its uncertainty, we apply a correction of $-13.26\delta 28P \text{ Hz}$ for data runs taken at this bias magnetic field. The uncertainty in the bias field correction is smaller for data runs taken at 8 and 16 mG magnetic fields; however, we conservatively add an uncertainty of 0.28 Hz to the total measurement due to the presence of residual magnetic fields.

While transition rates to the $2S_{1=2}^{F=1} \tilde{0}m_F \frac{1}{4} 1P$ states should be small due to the polarization of the magnetic fields produced by the rf loops, the splitting of those states is a substantial $1.4 \text{ MHz} = G$. However, a shift in the measured resonance will only occur if the $2S_{1=2}^{F=1} \tilde{0}m_F \frac{1}{4} 1P$ states are excited unequally, which would require some degree of circular rf polarization. Such circular polarization is unlikely given the rf loop design. Nevertheless, to quantify this effect, we measured the transition with the atomic beam at room temperature and with a bias field of 1.5 mG. This places any spurious resonance directly on the side of the main peak.

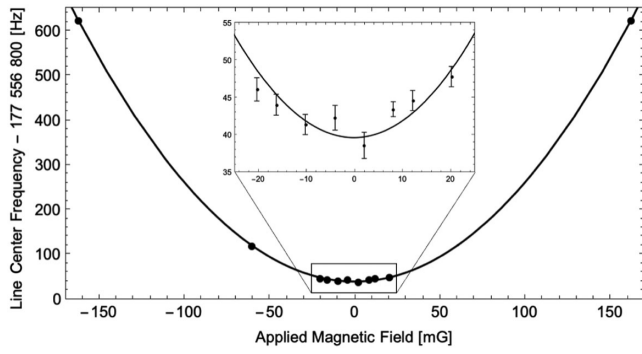


FIG. 4. Relative shift of the resonance as a function of applied magnetic field from solenoid. In the main figure, error bars are not included because they are too small to be visible.

Upon reversal of the field, we observed no shift in the resonance up to our measurement precision of 4 Hz for this test. With this we are able to limit the relative imbalance of transitions to the $2S_{1=2}^{F=1} \delta m_F \pm 1$ states to 0.003 that of the main resonance. With the magnetic fields and beam temperatures used in the data shown in Fig. 3(b), the $2S_{1=2}^{F=1} \delta m_F \pm 1$ transitions are far off resonance and would pull the line by a maximum of 10^{-5} Hz.

As atoms traverse the regions near each of the rf loops, a small electric field is expected to be present due to the oscillating current at 177 MHz in the copper loops. This can produce a rf Stark shift through coupling of the $2S_{1=2}$ state to the $2P_{1=2}$ and $2P_{3=2}$ states. Since the shift in the line center as a function of the rf drive power is linear, we performed an extrapolation of the extracted line center as a function of the rf drive power to characterize this effect. For this test, the rf drive power was varied by a factor of 16, which was the maximum variation possible to produce sufficient signal-to-noise ratios while ensuring that saturation effects were negligible. We find that the shift due to the rf Stark effect is -2.85 ± 0.63 Hz. This shift is reasonable given the residual level of electric field expected within the rf loops. There is also the possibility of a rf Stark shift from leakage of the 910 MHz field used to quench the $2S_{1=2}^{F=0}$ population. This field is well shielded from the interaction region and we measured > 55 dB of attenuation outside of the quench region, which we estimate produces a < 0.007 Hz shift to the measurement.

The dc Stark shift is quadratic and has the value $\Delta f_{dc} \approx -\delta 880 E^2 \pm 230 E^2$ Hz $\delta \text{cm} = V \pm^2$ [19]. In order to mitigate this effect, the entire rf system was enclosed in a Faraday cage and coated with colloidal graphite. Previously, we have characterized the strength of dc electric fields using the same method to prepare the Faraday cage and found fields to be ≤ 6.5 mV/cm [24]. Therefore, we assume a stray field of 6.5 mV/cm in the radial direction and apply a shift of 0.037(37) Hz.

The collisional shift of the $2S_{1=2}$ hyperfine interval is on the order of 10 Hz/mbar [22]. All of the data collection

TABLE I. Systematic corrections to the phase-extrapolated and magnetic field corrected $2S_{1=2}$ hyperfine interval.

	$f\delta 2S_{1=2} \text{p}$ (Hz)	σ (Hz)
Phase and bias field corrected	177 556 835.98	0.45
rf Stark effect (177 MHz)	2.85	0.63
rf Stark effect (910 MHz)	0	0.007
Residual magnetic fields	0	0.28
Extrapolation nonlinearity	0	0.2
dc Stark effect	0.037	0.037
Spurious transitions	0	10^{-5}
Collisional shift	0	10^{-7}
Second-order Doppler shift	0.001	0.001
Final measured value	177 556 838.87	0.85

was taken with background hydrogen pressure on the order of 10^{-8} mbar or lower, which we estimate is the dominant source of collisions. This leads to a negligible shift.

From the phase-extrapolated data after the bias magnetic field corrections, we obtain a value for the $2S_{1=2}$ hyperfine interval of $f\delta 2S_{1=2} \text{p} \approx 177 556 835.98 \pm 0.45$ Hz. After correction due to other systematic effects, the value is $f\delta 2S_{1=2} \text{p} \approx 177 556 838.87 \pm 0.85$ Hz. All systematic corrections are summarized in Table I. Combining the measured value of the $2S_{1=2}$ hyperfine interval from this work and the experimentally determined value of the $1S_{1=2}$ hyperfine interval gives

$$D_{21} \approx 48 959.2 \pm 0.8 \text{ Hz}; \quad \delta 4 \text{p}$$

which is in good agreement with the theoretical value as shown in Fig. 5.

Experimental values of D_{21} are also available for deuterium [27,28] and the $^3\text{He}^b$ ion [29,30]. Previously, constraints on light pseudovector bosons were similar in all three species [16]. However, with the results presented here, the constraints from hydrogen have been significantly improved. Therefore, we believe a new measurement of

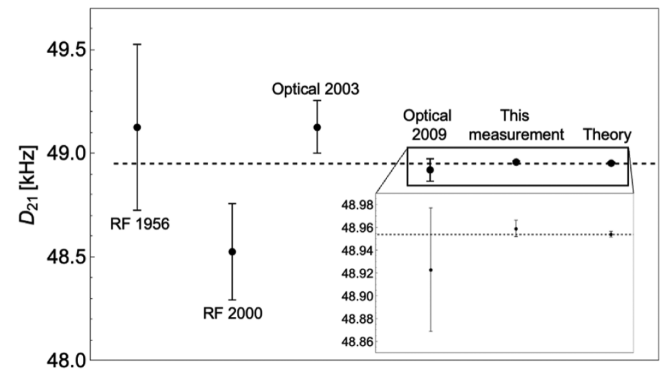


FIG. 5. Experimental (rf 1956 [19], rf 2000 [20], optical 2003 [21], and optical 2009 [22]) and theoretical [15] values of D_{21} . The dashed line represents the theoretical value.

D_{21} in deuterium using rf Ramsey spectroscopy is well motivated. While the theory value is currently 2.8 times more precise than our experimental measurement, further improvements could likely be achieved by increasing the distance between the rf loops in our Ramsey spectrometer. With this, an investigation into the remaining sources of theoretical uncertainty in the fourth-order QED corrections may be warranted [6,7].

In conclusion, we present a new measurement of the hydrogen $2S_{1=2}$ hyperfine interval. We have reduced the experimental uncertainty of this interval by a factor of ≈ 8 and find a value in good agreement with theory [6,8], which provides a stringent test of bound-state QED. We note that added confidence in the bound-state QED corrections may be relevant for upcoming measurements of the ground-state hyperfine splitting in muonic hydrogen, which aim to obtain precise information about the magnetic structure of the proton [31].

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