



Full Length Article

Alignment of the CLAS12 central hybrid tracker with a Kalman Filter

S.J. Paul⁴², A. Peck⁴², M. Arratia^{42,38,*}, Y. Gotra³⁸, V. Ziegler³⁸, R. De Vita¹⁴, F. Bossù⁴⁷, M. Defurne⁴⁷, H. Atac³⁷, C. Ayerbe Gayoso⁴⁵, L. Baashen⁹, N.A. Baltzell³⁸, L. Barion¹², M. Bashkanov⁴⁴, M. Battaglieri¹⁴, I. Bedlinskiy²⁷, B. Benkel³⁹, F. Benmokhtar⁶, A. Bianconi^{40,19}, L. Biondo^{14,15,16}, A.S. Biselli⁷, M. Bondi¹⁷, S. Boiarinov³⁸, K.-Th. Brinkmann³², W.J. Briscoe¹⁰, W.K. Brooks³⁹, D. Bulumulla³¹, V.D. Burkert³⁸, R. Capobianco⁵, D.S. Carman³⁸, J.C. Carvajal⁹, P. Chatagnon²⁰, V. Chesnokov³⁵, T. Chetry^{9,26,30}, G. Ciullo^{12,8}, P.L. Cole²⁴, G. Costantini^{40,19}, A. D'Angelo^{17,34}, N. Dashyan⁴⁶, A. Deur³⁸, S. Diehl^{32,5}, C. Djalali³⁰, R. Dupre²⁰, A. El Alaoui³⁹, L. El Fassi²⁶, L. Elouadrhiri³⁸, A. Filippi¹⁸, K. Gates⁴³, G. Gavalian³⁸, Y. Ghandilyan⁴⁶, G.P. Gilfoyle³³, A.A. Golubenkov³⁵, G. Gosta^{40,19}, R.W. Gothe³⁶, K. Griffioen⁴⁵, M. Guidal²⁰, H. Hakobyan³⁹, M. Hattawy³¹, F. Hauenstein³⁸, T.B. Hayward^{5,45}, D. Heddle^{4,38}, A. Hobart²⁰, M. Holtrop²⁸, Y. Ilieva³⁶, D.G. Ireland⁴³, E.L. Isupov³⁵, H.S. Jo²³, R. Johnston²⁵, K. Joo⁵, D. Keller⁴⁷, M. Khachatryan³¹, A. Khanal⁹, A. Kim⁵, W. Kim²³, V. Klimenko⁵, A. Kripko³², L. Lanza¹⁷, M. Leali^{40,19}, P. Lenisa^{12,8}, X. Li²⁵, I.J.D. MacGregor⁴³, D. Marchand²⁰, L. Marsicano¹⁴, V. Mascagna^{40,19}, B. McKinnon⁴³, C. McLauchlin³⁶, S. Migliorati^{40,19}, T. Mineeva³⁹, M. Mirazita¹³, V. Mokeev³⁸, C. Munoz Camacho²⁰, P. Nadel-Turonski³⁸, P. Naidoo⁴³, K. Neupane³⁶, D. Nguyen³⁸, S. Niccolai²⁰, M. Nicol⁴⁴, G. Niculescu²², M. Osipenko¹⁴, P. Pandey³¹, M. Paolone^{29,37}, R. Paremuzyan^{38,28}, N. Pilleux²⁰, O. Pogorelko²⁷, M. Pokhrel³¹, J. Poudel³¹, J.W. Price¹, Y. Prok³¹, T. Reed⁹, M. Ripani¹⁴, J. Ritman^{11,21}, F. Sabatié³, S. Schadmand¹¹, A. Schmidt^{10,25}, E.V. Shirokov³⁵, U. Shrestha^{5,30}, P. Simmerling⁵, D. Sokhan^{3,43}, N. Sparveris³⁷, M. Spreafico^{41,14}, I.I. Strakovsky¹⁰, S. Strauch³⁶, J.A. Tan²³, R. Tyson⁴³, M. Ungaro³⁸, S. Vallarino¹², L. Venturelli^{40,19}, H. Voskanyan⁴⁶, E. Voutier²⁰, D.P. Watts⁴⁴, X. Wei³⁸, R. Wishart⁴³, M.H. Wood², N. Zachariou⁴⁴

¹ California State University, Dominguez Hills, Carson, CA 90747, USA² Canisius College, Buffalo, NY, USA³ IRFU, CEA, Université Paris-Saclay, F-91191 Gif-sur-Yvette, France⁴ Christopher Newport University, Newport News, VA 23606, USA⁵ University of Connecticut, Storrs, CT 06269, USA⁶ Duquesne University, Pittsburgh, PA 15282, USA⁷ Fairfield University, Fairfield, CT 06824, USA⁸ Università di Ferrara, 44121 Ferrara, Italy⁹ Florida International University, Miami, FL 33199, USA¹⁰ The George Washington University, Washington, DC 20052, USA¹¹ GSI Helmholtzzentrum für Schwerionenforschung GmbH, D-64291 Darmstadt, Germany¹² INFN, Sezione di Ferrara, 44100 Ferrara, Italy¹³ INFN, Laboratori Nazionali di Frascati, 00044 Frascati, Italy¹⁴ INFN, Sezione di Genova, 16146 Genova, Italy¹⁵ INFN, Sezione di Catania, 95123 Catania, Italy¹⁶ Università degli Studi di Messina, 98166 Messina, Italy¹⁷ INFN, Sezione di Roma Tor Vergata, 00133 Rome, Italy¹⁸ INFN, Sezione di Torino, 10125 Torino, Italy¹⁹ INFN, Sezione di Pavia, 27100 Pavia, Italy²⁰ Université Paris-Saclay, CNRS/IN2P3, IJCLab, 91405 Orsay, France²¹ Institute für Kernphysik (Juelich), Juelich, Germany

* Corresponding author at: University of California Riverside, 900 University Avenue, Riverside, CA 92521, USA.

E-mail address: miguel.arratia@ucr.edu (M. Arratia).

- ²² James Madison University, Harrisonburg, VA 22807, USA
²³ Kyungpook National University, Daegu 41566, Republic of Korea
²⁴ Lamar University, 4400 MLK Blvd, PO Box 10046, Beaumont, TX 77710, USA
²⁵ Massachusetts Institute of Technology, Cambridge, MA, 02139-4307, USA
²⁶ Mississippi State University, Mississippi State, MS 39762-5167, USA
²⁷ National Research Centre Kurchatov Institute - ITEP, Moscow, 117259, Russia
²⁸ University of New Hampshire, Durham, NH 03824-3568, USA
²⁹ New Mexico State University, PO Box 30001, Las Cruces, NM 88003, USA
³⁰ Ohio University, Athens, OH 45701, USA
³¹ Old Dominion University, Norfolk, VA, 23529, USA
³² II Physikalisches Institut der Universitaet Giessen, 35392 Giessen, Germany
³³ University of Richmond, Richmond, VA 23173, USA
³⁴ Università di Roma Tor Vergata, 00133 Rome, Italy
³⁵ Skobeltsyn Institute of Nuclear Physics, Lomonosov Moscow State University, 119234 Moscow, Russia
³⁶ University of South Carolina, Columbia, SC 29208, USA
³⁷ Temple University, Philadelphia, PA 19122, USA
³⁸ Thomas Jefferson National Accelerator Facility (Jefferson Lab), Newport News, VA 23606, USA
³⁹ Universidad Técnica Federico Santa María, Casilla 110-V Valparaíso, Chile
⁴⁰ Università degli Studi di Brescia, 25123 Brescia, Italy
⁴¹ Università di Genova, Dipartimento di Fisica, 16146 Genova, Italy
⁴² University of California Riverside, 900 University Avenue, Riverside, CA 92521, USA
⁴³ University of Glasgow, Glasgow G12 8QQ, United Kingdom
⁴⁴ University of York, York YO10 5DD, United Kingdom
⁴⁵ College of William and Mary, Williamsburg, VA 23187-8795, USA
⁴⁶ Yerevan Physics Institute, 375036 Yerevan, Armenia
⁴⁷ IIRFU, CEA, Université Paris-Saclay, F-91191 Gif-sur-Yvette, France

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ABSTRACT

Several factors can contribute to the difficulty of aligning the sensors of tracking detectors, including a large number of modules, multiple types of detector technologies, and non-linear strip patterns on the sensors. The latter two of these three factors apply to the CLAS12 CVT, which is a hybrid detector consisting of planar silicon sensors with non-parallel strips, and cylindrical micromegas sensors with longitudinal and arc-shaped strips located within a 5 T superconducting solenoid. To align this detector, we used the Kalman Alignment Algorithm, which accounts for correlations between the alignment parameters without requiring the time-consuming inversion of large matrices. This is the first time that this algorithm has been adapted for use with hybrid technologies, non-parallel strips, and curved sensors. We present the results for the first alignment of the CLAS12 CVT using straight tracks from cosmic rays and from a target with the magnetic field turned off. After running this procedure, we achieved alignment at the level of 10 μm , and the widths of the residual spectra were greatly reduced. These results attest to the flexibility of this algorithm and its applicability to future use in the CLAS12 CVT and other hybrid or curved trackers, such as those proposed for the future Electron-Ion Collider.

1. Introduction

Aligning a tracking detector is a non-trivial task, which can involve large numbers of degrees of freedom. Various algorithms have been developed for this task, such as HIP [1] and MillePede [2]. The Kalman Alignment Algorithm (KAA) [3,4], which is based on the Kalman-filter algorithm, was first implemented to align the CMS silicon tracker [5], and we used it to align the CEBAF Large Acceptance Spectrometer (CLAS12) Central Vertex Tracker (CVT) [6–8] in Hall B at Jefferson Lab.

These algorithms take the fitted tracks, reconstructed from misaligned detector data, and a model of the dependence of the residuals of the track fit to the alignment and track parameters. Here, the residuals are the differences between the measurements along the track and the values interpolated from the track fit. The goal of these algorithms is then to find the values of the alignment parameters that minimize the sum of squares of the residuals (*i.e.* the track fit χ^2).

When choosing an alignment algorithm, two important factors are the computational speed and biases in the results. One drawback to the MillePede algorithm is that it requires the inversion of a large matrix, typically of rank $N_{\text{align}} \times N_{\text{align}}$, where N_{align} is the number of alignment parameters.¹ In the first version of MillePede, this inversion could potentially be time-consuming, however, in MillePede II, sparse-matrix libraries have been utilized to reduce the runtime of this inversion

significantly [2]. The Hits and Impact Points (HIP) algorithm is similar to MillePede, except that it forces the analogous matrix to be block-diagonal (and thus much faster to invert) at the cost of ignoring the dependence of the residuals on the track parameters (which MillePede and the KAA take into account). Because this dependence is ignored, the correlations between alignment parameters for one module and those of another module are not accounted for and can introduce biases in the results. The KAA overcomes both of these problems. Like MillePede, it corrects for the biases caused by the track-parameter dependence of the residuals, but the KAA does so in a manner that avoids the inversion of large matrices.

The results obtained with the HIP, KAA, and MillePede algorithms for the CMS inner tracker were compared to one another in Ref. [5]. The tracking-residual distributions obtained with the three algorithms were all centered within a few μm of zero and had comparable RMS values to one another (about 300 μm).

One important difference between CMS and the CLAS12 CVT is that the strips in the sensors in CMS are straight and parallel,² whereas the CLAS12 CVT has both sensors that are curved and non-parallel strips within the same sensor. These two features cause the tracking residuals to depend non-linearly on the alignment parameters. The HIP, KAA, and MillePede algorithms all approximate the relationship between these residuals and the alignment parameters as linear, causing such algorithms to converge at non-optimal values for the alignment parameters.

² The strips in one sensor of CMS are not necessarily parallel to those in another sensor, since there is a stereo angle between nearby sensors.

¹ In the case of the CLAS12 CVT, $N_{\text{align}} = 612$.

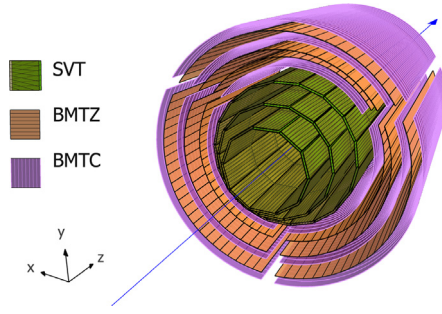


Fig. 1. Rendering of the CLAS12 CVT, which consists of three double layers of SVT (inner, leaf-green) and six layers of BMT, with Z layers in orange and C layers in purple. The blue line represents the beamline. The lines within the sensors indicate every 32nd strip.

One solution to this issue is to run multiple iterations of an alignment algorithm, and refit the tracks between iterations with the alignment parameters obtained from the previous iteration. Such an approach was used, for example, in the alignment of the LHCb VELO (silicon Vertex LOcator) [9,10] and also for the ATLAS Inner Detector (ID) [11,12]. In this work, we used the KAA to align the CLAS12 CVT, likewise using a multi-iteration approach. The CLAS12 CVT presents two new challenges for the KAA that were not applicable when it was first implemented for CMS: the CVT is a hybrid of two different types of sensor technology, silicon and micromegas, while CMS is a fully silicon tracker, and the CVT includes curved sensors, while the sensors at CMS are flat. Thus, the alignment of the CVT using the KAA is a test of the versatility and flexibility of the algorithm for diverse detectors.

Details of the CLAS12 CVT are given in Section 2. We then describe the KAA in Section 3. Section 4 describes the datasets used for alignment. In Section 5, we describe the procedure for running the KAA for the CLAS12 CVT. We then present the results for the data in Section 6 and we conclude in Section 7.

2. The CLAS12 Central Vertex Tracker

The CLAS12 CVT, which covers the polar-angle³ range $35^\circ < \theta < 125^\circ$, is shown in Fig. 1. It consists of three regions of double-sided Silicon Vertex Tracker (SVT) modules [7] and six layers of the Barrel Micromegas Tracker (BMT) [8].

The SVT regions are arranged in concentric polygons with 10, 14, and 18 sectors in the inner, middle, and outer pairs of layers.⁴ The geometry of the SVT is summarized in Table 1. Within each pair of layers, each sector is a separate module, consisting of one sensor on each of the two layers, separated radially by 3.16 mm. The sensor consists of three daisy-chained silicon microstrip detectors and has 256 strips. Each detector is 320 μm thick, 42.00 mm wide, and 111.63 mm long. A rendering of the geometry of the SVT module is shown in Fig. 2.

At the upstream end of the sensor planes, where the strips connect to the readout, they have 156 μm pitch, but they fan out, with the angle of the strip relative to longitudinal direction of the sensor increasing linearly from 0° at the first strip to 3° at the last strip. The two sensors in each module are mounted back-to-back, so that the first strip of one sensor corresponds with the last strip of the other and vice versa. This geometry allows measurements of the longitudinal hit positions due to the 3° stereo angle between the two sensors on each module.

³ Throughout this paper, the lab-frame coordinates are defined as follows: z is along the beam direction, y is the up direction, and x is to the left when looking at the detector from upstream.

⁴ Since the pairs of layers have different numbers of modules, the sectors in one double layer do not line up with those in the other double layers, with the exception of the top and bottom sector in each double layer.

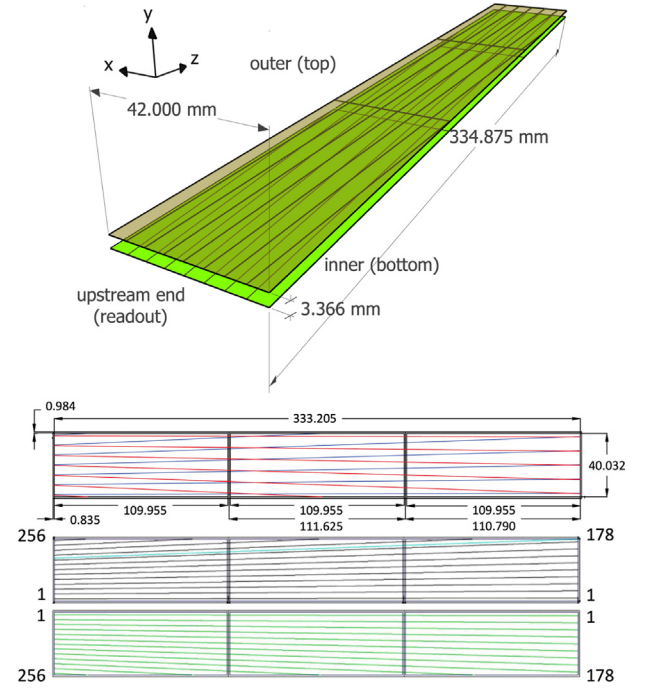


Fig. 2. Top: 3D Rendering of one of the SVT sector modules. The inner (outer) sensor of the module is shown in green (yellow). Every 32nd strip is shown for both sensors as lines on the sensors. Bottom (from Ref. [7]): Sensor strip layout. The upstream end, which has the readout, is on the left side. Strip numbers are indicated. Dimensions are in mm.

Table 1

Summary of parameters of each SVT layer. The radii given are the nominal values for the perpendicular distance between the midplane of the SVT backing structure and the beamline. The pitch varies from 156 μm at the upstream end to about 224 μm at the downstream end.

Layer	Radius (mm)	Pitch (μm)	Sectors
1	65.29	156–224	10
2	68.77	156–224	10
3	92.89	156–224	14
4	96.37	156–224	14
5	120.32	156–224	18
6	123.80	156–224	18

The thickness of the ROHACELL® closed-cell rigid foam and the backing-structure assembly of the SVT after molding was measured by Fermilab's Silicon Detector Facility (3 points along the length) with a precision of 10 μm . CMM (Coordinate-Measurement Machine) inspection of the surface flatness of the backing structure and the best-fit fiducial flatness of installed sensors from OGP® system CMM was done also by SiDet with precision of 5 μm . Structural Finite-Element Analysis on the SVT detector elements was performed using the Ansys Mechanical software package [13]. The deflection in the detector was analyzed for an individual module and for a region as a whole. The deflection was calculated based on the gravitational load on the module. On the upstream end, the module was assumed to be fixed since it is fastened to the upstream support ring of the detector. On the downstream end a simply supported condition was assumed since it is supported by the downstream ring. The maximum deflection of a module due to gravity is 14 μm due to the excellent mechanical rigidity of the silicon sensors and the carbon-fiber support. The deflection of the downstream ring is less than 7 μm . The vertical modules in the barrel minimize the deflection in the downstream ring making it a fairly rigid structure. The maximum deflection of the entire SVT is 23 μm .

The BMT is divided azimuthally into three sectors, each of which consists of six cylindrical arc layers. There are two types of sensors: Z-type (layers 2, 3, and 5), in which the strips are (nominally) parallel

Table 2

Summary of parameters of each BMT layer. The pitches of the C layers vary from strip to strip, with wider strips towards the front and back, and narrower strips near the center.

Layer	Radius (mm)	Pitch (μm)	Strip orientation
1	146.15	330–860	C
2	161.15	487	Z
3	176.15	536	Z
4	191.15	340–770	C
5	206.15	529	Z
6	221.15	330–670	C

to the beamline and measure the azimuthal position of the particle's trajectory, and C-type (layers 1, 4, and 6) in which the strips curve azimuthally around the beamline and measure the longitudinal position of the particle's trajectory (which is also used to measure the polar angle of the trajectory). Throughout this paper, we refer to the Z layers as the BMTZ and the C layers as the BMTC. The radii, pitches, and strip orientations for each layer are given in Table 2.

For the BMT, mechanical deformations will mainly affect the local radial position, which is not extremely crucial (in terms of precision) for the alignment.

3. Methodology

We used the KAA, which is described in detail in Refs. [3,4]. Here we present a summary of the main features of the algorithm and detail the specific implementation to the CLAS12 case. We note here that our method relies on straight tracks to obtain the alignment parameters and was validated with both straight and curved tracks.

A Kalman filter is an algorithm that uses an ordered sequence of measurements and produces estimates of unknown parameters that converge upon more precise values than those obtained from a single measurement. Like any other Kalman-filter algorithm, the KAA begins with an estimate of the parameters to be fitted and a matrix of the covariances among these parameters. It then loops through the measurements in the input sample and updates the values of the parameters and their covariance matrix after each measurement. In the case of the KAA, the parameters to be fitted are the alignment parameters, and the measurements are fitted tracks and the tracking residuals thereof.⁵ As more tracks are processed, the uncertainties on the alignment parameters (that is, the square roots of the diagonal elements of the covariance matrix) decrease, and the alignment parameters converge to more precise values.

In the KAA, the deviations of each sensor and module from their nominal positions are represented by the column vector \mathbf{d} . The KAA requires a preliminary estimate of \mathbf{d} and its covariance matrix \mathbf{D} , and a set of several matrices for each track. These matrices, which are summarized below, model the track residuals for each measurement in the track, their dependence on the alignment and track parameters, and the expected resolution on these residuals and are summarized below. The alignment values and its covariance matrix are updated sequentially for every track in the sample of input events.

Straight-line tracks in the CVT are represented by their direction, \hat{u} , and a point on the line, \vec{x}_{ref} . Unless otherwise noted, all coordinates are given in the lab frame. We use the following track parameters: the distance of closest approach of the track to the beamline, d_0 , the azimuthal angle of the track direction, ϕ_0 , the longitudinal position of the track's point of closest approach, z_0 , and the tangent of the track's dip angle, t_0 . Expressed in terms of these parameters, \vec{x}_{ref} and \hat{u} are:

$$\vec{x}_{\text{ref}} = (-d_0 \sin \phi_0 + x_b, d_0 \cos \phi_0 + y_b, z_0) \quad (1)$$

⁵ This is analogous to the Kalman-filter track-fitting algorithm, where the parameters of a single track are fitted, and the individual measurements are the hits and/or clusters along the track.

and

$$\hat{u} = \frac{(\cos \phi_0, \sin \phi_0, t_0)}{\sqrt{1 + t_0^2}}, \quad (2)$$

where (x_b, y_b) is the beam position.

In the CVT, each measurement corresponds to a contiguous cluster of hits in one of the SVT or BMT layers. We represented these clusters as line segments connecting the centroids⁶ of the endpoints of the strips on one end of the sensor to the centroid of the endpoints of the strips on the other end. Notice the direction of each line segment in the lab frame is not necessarily parallel to a particular strip. We defined the vector \vec{e} to be the coordinates (in the lab frame) of a point on this line segment (arbitrarily, we chose the midpoint), and $\hat{\ell}$ to be the direction of this line, i.e., the direction of the lines connecting the centroids of the endpoints of the strips on each end of the sensor.⁷ We also defined the unit vector \hat{n} as the unit normal vector to the sensor, and $\hat{s} = \hat{n} \times \hat{\ell}$, which we call the “measurement direction”, as shown in Fig. 3.

For the BMTC, each strip is an arc, therefore we analogously constructed a “centroid” arc using the centroids of two endpoints and centers of the individual strip's arcs. We then extrapolated the track to the BMTC layer, and find the line that is tangent to the arc at the same azimuthal position as the extrapolation point (right panel of Fig. 3). The vectors \vec{e} and $\hat{\ell}$ are then defined as a point on this line (we chose the tangent point) and the direction of the line respectively. The measurement direction, \hat{s} , is defined to be along the BMTC layer's cylindrical axis, and \hat{n} is normal to the sensor at the extrapolated azimuthal position.

Using these representations of the track and its clusters, we then determined the matrices needed for the KAA's input. The first two matrices are a column vector of the 1D measurements along the track, \mathbf{m} , and another column vector \mathbf{c} of the expected values for each measurement based on a track fit performed in reconstruction, which is made using the Kalman Filter algorithm [14]. The tracking-residuals column vector, \mathbf{r} , is defined as their difference, $\mathbf{m} - \mathbf{c}$.

We calculated the element of the column vectors \mathbf{c} , \mathbf{m} , and \mathbf{r} corresponding to the i th measurement along the track using the following formulas:

$$c_i = \hat{s} \cdot \left(\vec{x}_{\text{ref}} + \hat{u} \frac{\hat{e} \cdot (\vec{e} - \vec{x}_{\text{ref}})}{\hat{u} \cdot \hat{n}} \right), \quad (3)$$

$$m_i = \hat{s} \cdot \vec{e}, \quad (4)$$

and

$$r_i = m_i - c_i, \quad (5)$$

$$= \hat{s} \cdot \left(\vec{e} - \vec{x}_{\text{ref}} - \hat{u} \frac{\hat{e} \cdot (\vec{e} - \vec{x}_{\text{ref}})}{\hat{u} \cdot \hat{n}} \right) \quad (6)$$

$$= \vec{s}' \cdot (\vec{e} - \vec{x}_{\text{ref}}), \quad (7)$$

where

$$\vec{s}' = \hat{s} - \frac{\hat{s} \cdot \hat{u}}{\hat{u} \cdot \hat{n}} \hat{n}. \quad (8)$$

Eq. (7) is equivalent to the distance along the measurement direction, \hat{s} , between the centroid line of the cluster of hits on the sensor and the extrapolated position where the track intersects the sensor. A more complete derivation of Eqs. (3)–(8) is given in Appendix A.

The dependence of the residuals on the alignment parameters and on the track parameters are modeled linearly by the alignment-derivative matrix, \mathbf{A} , and the track-derivative matrix \mathbf{B} . The elements of \mathbf{A} are defined by

$$A_{ij} = \frac{\partial r_i}{\partial d_j}, \quad (9)$$

⁶ weighted by the reconstructed energy deposited in the strip

⁷ For the SVT, which has non-parallel strips, this is the weighted average of the directions of the strips in the cluster

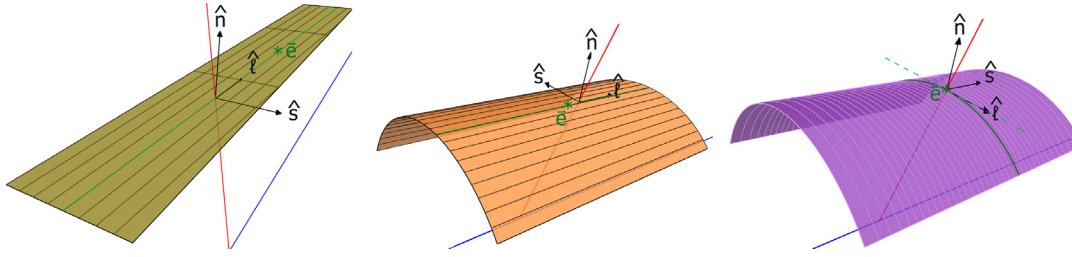


Fig. 3. Illustrations of the vectors \hat{s} , \hat{n} , and $\hat{\ell}$ for the SVT (left), BMTZ (middle), and BMTC (right). The beamline and the reference trajectory are shown in blue and red, respectively. The struck strip is shown as a solid green line or arc. For the BMTC, the tangent line to the struck strip is shown as a green dashed line. A point on the line, \vec{e} , is indicated by an asterisk (for the SVT and BMTZ, we chose the midpoint of the strip; for the BMTC, we used the tangent point).

where r_i is the residual of the i th measurement in the track and d_j is the j th alignment parameter. In this work, we assume that every module is a rigid body, and therefore consider only rotation and translation, but not deformations within any module.⁸ For three rotation variables and three translation variables per module, \mathbf{A} has dimension $n_{\text{meas}} \times 6n_{\text{mod}}$, where n_{meas} is the number of measurements (clusters) in the track, and n_{mod} is the total number of modules to be aligned.

The elements of \mathbf{B} are likewise defined as

$$B_{ij} = \frac{\partial r_i}{\partial t_j}, \quad (10)$$

where r_i is the residual of the i th measurement in the track and t_j is the j th track parameter. Since four parameters define a straight track, \mathbf{B} has dimension $n_{\text{meas}} \times 4$.

When expanding \mathbf{r} in terms of the alignment parameters \mathbf{d} and track parameters \mathbf{t} about the values for a fully aligned detector, \mathbf{d}_0 and \mathbf{t}_0 , one can model the detector response as

$$\mathbf{r} = \mathbf{A}(\mathbf{d} - \mathbf{d}_0) + \mathbf{B}(\mathbf{t} - \mathbf{t}_0) + \epsilon, \quad (11)$$

where ϵ is the random part of the residuals due to resolution effects.

The last matrix in the input, \mathbf{V} , is the covariance matrix for ϵ . Its matrix elements V_{ij} are given by

$$V_{ij} = \langle \epsilon_i \epsilon_j \rangle. \quad (12)$$

Since ϵ_i and ϵ_j for $i \neq j$ are independent of one another, this matrix is diagonal. Further, the diagonal elements are the square of the expected spatial resolutions for the corresponding measurement in the track. These are calculated in the CLAS12 reconstruction package [15]. In a single-strip cluster, resolution is the width (pitch) of a strip divided by $\sqrt{12}$, as expected for binary readout. For the SVT, where the strips get wider further downstream, the strip width is calculated at the longitudinal position of the intersection of the clusters in a stereo pair. Therefore the resulting resolution for single-strip SVT clusters is 45–65 μm . In the BMTZ, this yields a single-strip resolution of about 141–153 μm (depending on the layer). In the BMTC, the strip pitch varies with the position in z , therefore this is reflected in the expected resolutions. For single-strip clusters in the BMTC, the resolution varies from 95 to 248 μm .

For multi-strip clusters, the resolution the square root of the sum of squares of those of the individual strips, which is worse than the single-strip case. This is because there is insufficient charge-measurement resolution in a single strip to use this information to improve the resolution.

In our implementation, the elements of the alignment-derivative matrix, \mathbf{A} , are

$$A_{i,\vec{T}} = \vec{s}' \quad (13)$$

⁸ While deformations could, in principle, be included as degrees of freedom in the KAA, doing so would require major changes to the event-reconstruction software, which are well outside the scope of this paper

and

$$A_{i,\vec{R}} = -\vec{s}' \times \left(\vec{x}_{\text{ref}} + \left(\frac{\vec{n} \cdot (\vec{e} - \vec{x}_{\text{ref}})}{\hat{u} \cdot \hat{n}} \right) \hat{u} \right). \quad (14)$$

The \vec{T} and \vec{R} vectors represent the groups of indices corresponding to the translation and rotation parameters of the module which the i th measurement in the track takes place in.

The elements of the track-derivative matrix, \mathbf{B} , are

$$B_{i,d_0} = -\vec{s}' \cdot (-\sin \phi_0, \cos \phi_0, 0) \quad (15)$$

$$B_{i,\phi_0} = -\vec{s}' \cdot \left\{ \frac{\hat{n} \cdot (\vec{e} - \vec{x}_{\text{ref}})}{\hat{u} \cdot \hat{n} \sqrt{1 + t_0^2}} (-\sin \phi_0, \cos \phi_0, 0) \right. \\ \left. - d_0 (\cos \phi_0, \sin \phi_0, 0) \right\} \quad (16)$$

$$B_{i,z_0} = -s'_z \quad (17)$$

$$B_{i,t_0} = -s'_z \frac{\hat{n} \cdot (\vec{e} - \vec{x}_{\text{ref}})}{\hat{u} \cdot \hat{n}}. \quad (18)$$

Eq. (13) was obtained by taking the derivative of the formula for the residuals (Eq. (7)) with respect to \vec{e} . To obtain Eq. (14), we took the derivative of Eq. (7) with respect to an infinitesimal rotation $d\vec{R}$ of the sensor: $\hat{n} \rightarrow \hat{n} + d\vec{R} \times \hat{n}$, and likewise for \hat{s} , $\hat{\ell}$, and \vec{e} . The track is not rotated, so the vectors \hat{u} and \vec{x}_{ref} are not rotated.

Eqs. (15)–(18) were obtained by taking the derivative of Eq. (7) with respect to the track parameters d_0 , ϕ_0 , z_0 , and t_0 , using the definitions of \vec{x}_{ref} and \hat{u} in Eqs. (1) and (2).

The degrees of freedom corresponding to the matrix elements of \mathbf{A} and \mathbf{B} for all three detector subsystems are illustrated in Appendix B. There are some degrees of freedom of the alignment that are either entirely unconstrained or very poorly constrained, which are referred to as “weak modes”. Rotations of BMTC modules along the z are entirely unconstrained weak modes, as well as translations of BMTZ modules along the z direction. As such, these degrees of freedom cannot be constrained by track-based alignment. For the SVT, translations in the direction transverse to the sensors can be better constrained than translations in z and in the direction normal to the SVT sensors.

Following Refs. [3,4], KAA loops through all of the tracks, and updates the alignment parameters \mathbf{d} and their covariance matrix \mathbf{D} using Eqs. (19)–(22) below (the derivations of these equations are beyond the scope of this article, and can be found in Refs. [3,4]):

$$\mathbf{d}' = \mathbf{d} + \mathbf{D}\mathbf{A}^T \mathbf{G} (\mathbf{m} - \mathbf{c} - \mathbf{A}\mathbf{d}) \quad (19)$$

and

$$\mathbf{D}' = (\mathbf{I} - \mathbf{D}\mathbf{A}^T \mathbf{G}\mathbf{A})\mathbf{D}(\mathbf{I} - \mathbf{A}^T \mathbf{G}\mathbf{A}\mathbf{D}) \\ + \mathbf{D}\mathbf{A}^T \mathbf{G}\mathbf{V}\mathbf{G}\mathbf{A}\mathbf{D}, \quad (20)$$

where

$$\mathbf{G} = \mathbf{V}_D^{-1} - \mathbf{V}_D^{-1} \mathbf{B} (\mathbf{B}^T \mathbf{V}_D^{-1} \mathbf{B})^{-1} \mathbf{B}^T \mathbf{V}_D^{-1} \quad (21)$$

and

$$\mathbf{V}_D = \mathbf{V} + \mathbf{A}\mathbf{D}\mathbf{A}^T, \quad (22)$$

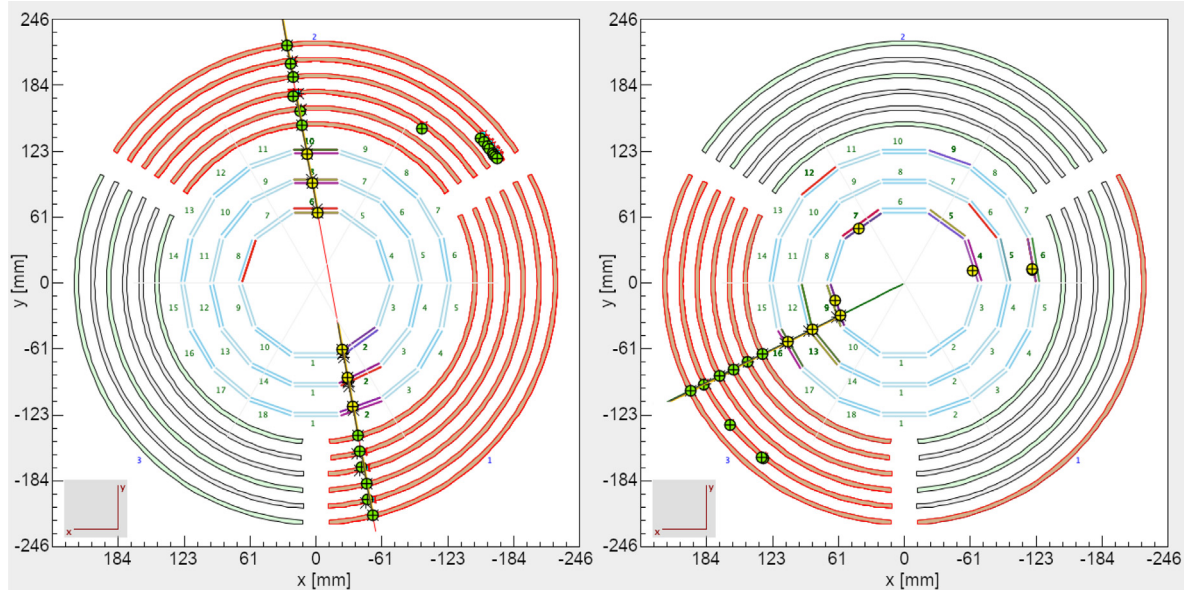


Fig. 4. Example tracks from the “cosmic” (left) and “field-off” (right) configurations, as shown in the CLAS12 Event Display. Units are mm. BMT tiles that have been hit are outlined in red. A yellow circle with a + represents a reconstructed crossing between pairs of clusters on the two sensors in the same SVT module. The green circles represent the reconstructed position of BMT clusters (for BMTC, the azimuthal position is shown at the crossing of the track and the layer). An asterisk is shown behind the circles at the position where the fitted track intersects the sensors. The colors of the SVT sensors represent the ADC values of the hits on those sensors.

and \mathbf{I} is the identity matrix of the same dimensions as \mathbf{D} . The matrix \mathbf{V}_D can be interpreted as sum of the covariance of the residuals due to measurement uncertainty and the covariance due to the alignment uncertainty. \mathbf{G} can be interpreted as a projection of the inverse of \mathbf{V}_D such that $\mathbf{GB} = \mathbf{B}^T \mathbf{G} = 0$, in order to remove bias.

For some types of detector geometries, including that of the CVT, the residuals may depend non-linearly on the alignment parameters and/or the track parameters. Such non-linearity can lead to a systematic bias in the alignment parameters obtained by the KAA. We found that multiple iterations of the KAA, alternating with reiterations of the event reconstruction with the updated alignment parameters, are necessary in order to converge on a non-biased set of alignment parameters. This differs from the use of KAA in CMS, where the exclusive use of parallel strips and planar sensors cause the residuals to depend linearly on the alignment parameters. For CMS, only a single pass of the KAA was necessary [5].

4. Datasets

We used two special calibration runs taken in spring, 2019 during an experiment with a 10.6 GeV electron beam on a 5 cm liquid-deuterium target. The first run was a “cosmic run”, which was taken by turning off the beam and the spectrometer’s magnetic field, and triggering on cosmic rays passing through the detector. The second run was in the “field-off” configuration: the electron beam was on with 5 nA, and the target was in place,⁹ but the magnetic field was turned off. Example tracks from both runs are shown in Fig. 4. The position of the target, relative to the detector system, is shown in Fig. 5.

For both configurations, the particles’ trajectories are (neglecting multiple scattering) straight lines, which have several advantages over using helical tracks. First, the straight tracks can be described with fewer parameters: four parameters rather than the five parameters for a helical track. Second, no corrections need to be applied due to a possible non-homogeneity of the magnetic field. Third, when the

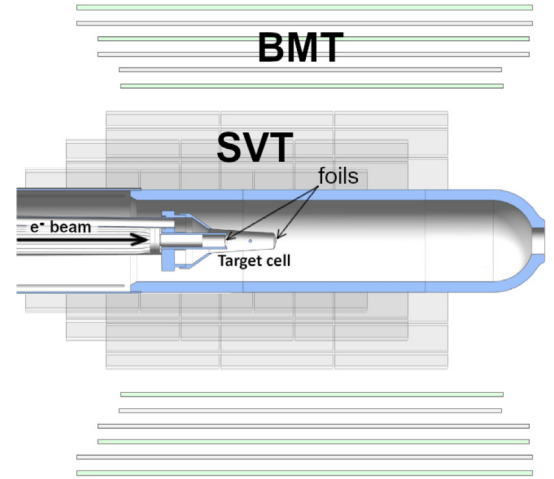


Fig. 5. Cross-sectional side-view of the CVT, showing the position of the empty cryogenic target used in the field-off runs. Most of the interactions in these runs occur in the indicated foil entrance and exit windows of the target cell, located at $z = \pm 2.5$ cm.

magnetic field is switched off, the Lorentz effect in the BMT is non-existent [8], so no corrections are needed for this effect. Finally, the formulas for the derivative matrices \mathbf{A} and \mathbf{B} (see Eqs. (9)–(18)) are simpler for straight tracks than for helices.

The two data-taking configurations each have their strengths and weaknesses when used in alignment, so combining both in our sample takes advantage of both of their strengths. Since the cosmic tracks pass through both the top half of the detector and the bottom half of the detector, they are useful for aligning the two halves together. However, the cosmic tracks are less likely to pass through the SVT modules on the sides of the detector mounted vertically (ϕ near 0° or 180°) and do not provide information about the alignment of the detector relative to the beamline. The “field-off” tracks from the target have a nearly uniform distribution in ϕ , and therefore have reasonable statistics in all of the

⁹ For this run, the target was in the “empty” configuration, *i.e.* depressurized so that almost all of the scattering took place on the target windows, and only a small part of the data sample was from scattering from the residual gas. This way, the longitudinal position of the target could be determined.

SVT sectors. Since such tracks originate from the target, they can be used later on to constrain the alignment of the detector relative to the target and the beamline.

The BMTC, in particular, cannot be aligned using only the tracks that originate from the beamline. This is because each sector of the BMTC has a global weak mode in which the three BMTC layers within the sector are shifted along the beam direction by an amount proportional to their radii. However, these weak modes can be constrained by using the cosmic tracks, which do not pass through the beamline. By including both types of events in our sample, we remove the problematic weak modes and have sufficient statistics in all of the modules of the CVT.

Since the alignment procedure required rerunning the CLAS12 event reconstruction on each data set multiple times, we developed a procedure to create a sub-sample containing only the events with tracks that would be used in the KAA. First, we ran a preliminary event reconstruction using the CLAS12 reconstruction package [15] with a pre-aligned version of the detector geometry, which was found using a detector survey followed by manual ad-hoc adjustments to individual alignment parameters. We then filtered out events that did not have tracks in the CVT. Events with more than two tracks were also removed, in order to get a cleaner sample. If the angle between the reconstructed track direction and the normal of any sensor used in reconstructing the track was more than 75° , or if the magnitude of the vector \vec{s}' (see Eq. (8)) was greater than 10, then the whole track was rejected. These cuts removed tracks that were difficult to accurately reconstruct with the detector.

To further improve the quality of our selected tracks, we required that all tracks had at least three BMTC clusters, two BMTZ clusters, and two pairs of clusters on paired sensors in the SVT. Further, we rejected tracks with very large residuals; these cuts were 7 mm for the BMTZ (which had the worst misalignments of the three subsystems before the alignment), and 2 mm for the BMTC and SVT.

5. Aligning the CLAS12 CVT

The alignment procedure was comprised of several iterations of the following steps:

- Running the CVT part of the CLAS12 reconstruction package [15] using the alignment parameters from the calibration-constants database (CCDB).
- Running the KAA. This is not part of the CLAS12 reconstruction, but rather a stand-alone software package, which takes as input from the reconstruction step a set of track measurements along with the alignment and track-derivative matrices (Eqs. (9) and (10)).
- Adjusting the values in the CCDB based on the output of the KAA.

For the track fitting part of the reconstruction, we ignored the effects of multiple scattering, which were used in the standard variation of reconstruction. We did this in order to avoid having an uneven weighting of hits in the outer layers during the fit, which would produce artificially large (small) residuals in the outer (inner) layers. Furthermore, our estimation of multiple-scattering effects is dependent on the knowledge of the momentum of the particle, which requires the magnetic field (which was turned off during both types of alignment runs).

Several cycles were necessary because the KAA operates using a linear expansion of the track residuals' dependence on the alignment parameters, as determined using the values of the alignment parameters at the time that the events were reconstructed, while the dependence in reality is non-linear, since the CLAS12 CVT contains non-parallel strips and curved sensors. Therefore, the alignment values obtained from a single iteration may have some bias, which can be improved by multiple iterations.

We used an event sample that combines the cosmic and “field-off” event samples. In order to avoid any bias from having all of the events of one of these two types at the beginning of the event sample and all of the other type at the end of the sample, we randomized the order of the events before starting the KAA.

All three subsystems were fit simultaneously, rather than fitting them individually, since this takes into account the correlations between the alignments of the different subsystems. At the beginning of each iteration, the diagonal elements of the covariance matrix \mathbf{D}_{init} were initialized to the following values:

- $\epsilon^2 = 10^{-14}$ for the elements corresponding to fixed parameters. This value is arbitrarily small, but non-zero in order to prevent \mathbf{D}_{init} from being singular. This includes translations in z for all BMTZ sensors and rotations in z for all BMTC sensors. We also chose to fix all parameters for one of the BMTZ modules (layer 5, sector 2), so that all alignment parameters would be relative to this sensor. Since global translations in z would otherwise be a weak mode, we also fixed the translations in z for one of the BMTC modules (layer 6, sector 2).
- For the non-fixed parameters, we used the following values: $\Delta T^2 = (1.5 \text{ mm})^2$ for translations and $\Delta R^2 = (0.005 \text{ rad})^2$ for rotations. The values of ΔT and ΔR were chosen to be bit larger than the maximum uncertainty of the precision of the preliminary survey.¹⁰ It should be noted that due to the convergence of Kalman filter algorithms in general, overestimating the initial uncertainties has a very limited impact on the final results.

Since there are 6 parameters per module and 84 SVT sensors and 18 BMT sensors, there are $6 \times (84 + 18) = 612$ total parameters. However, considering the fact that six parameters are fixed for global alignment, and one parameter is fixed for each BMT sensor, the remaining number of degrees of freedom is 588.

6. Results

To align the detector using the cosmic-ray and “field-off” data from the Spring 2019 run, we followed the procedure detailed in Section 5 for running the KAA with multiple iterations. The alignment procedure, including reiteration of the event reconstruction, took about half an hour on a Lambda Vector workstation, using four iterations, using 14k cosmic tracks and 8k field-off tracks from the target (after event selection). The KAA provides the alignment parameters needed to correct for errors in the reconstructed particle tracks, thus minimizing the residuals of the track reconstruction when those corrections are applied.

The distributions of residuals.¹¹ of the sampled tracks before (red, dashed) and after (black, solid) alignment are shown in Fig. 6 for the SVT (a), BMTZ (b), and BMTC (c). In each detector, the residual distributions after alignment are much narrower than those before the alignment. We then determined the full widths at half maximum (FWHMs) of these distributions, which are 116 μm for the SVT, 432 μm for the BMTZ, and 248 μm for the BMTC. Similarly, we also fit the cores of the distributions to Gaussian functions and obtained values that are about half of the values of the FWHMs¹²: 57, 230 and 180 μm for the SVT, BMTZ, and BMTC, respectively. These are comparable to the expected spatial resolutions of the SVT and BMT from Refs. [7,8],

¹⁰ The survey had an estimated precision of a few hundred μm (in the global x and y directions) to 1 mm (in global z) for the BMT internal alignment, and about 100-150 μm for internal alignment of the SVT (due to the use of fiducials for every module), and 200 μm for the global SVT-BMT relative alignment. Here, we define internal alignment of a detector subsystem as the relative alignment between modules in that subsystem.

¹¹ As defined by Eq. (7)

¹² The ratio of the FWHM to the standard deviation of a distribution depends on its shape. For reference, this ratio is ≈ 2.35 for a Gaussian distribution.

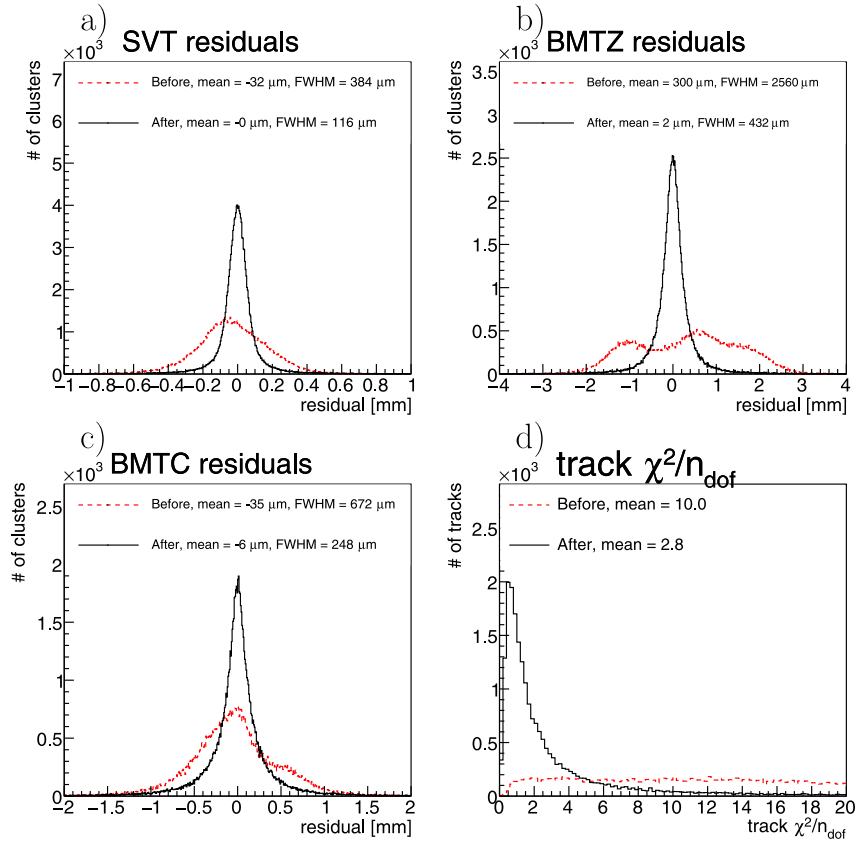


Fig. 6. Residuals distribution before (red, dashed) and after (black, solid) alignment for the SVT (a), BMTZ (b) and BMTc (c). Panel (d) shows the χ^2/n_{dof} distribution (bottom right) for each reconstructed track. Each cluster produces a single residual for a single track.

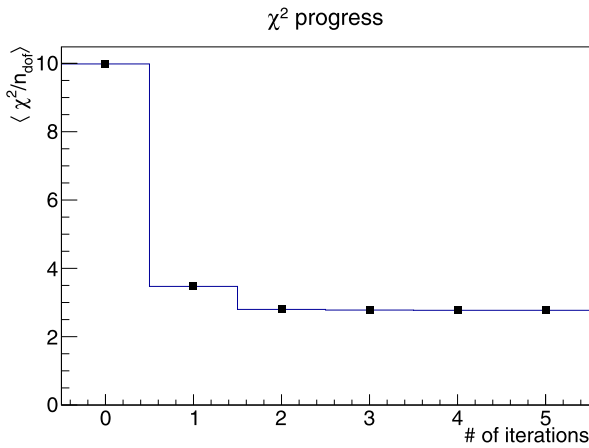


Fig. 7. Average track χ^2/n_{dof} after the indicated number of iterations of the KAA. The first point (at zero iterations) represents the average track χ^2/n_{dof} before running any alignment with the KAA.

respectively. The means of these distributions are on the order of a few μm , which is acceptable. The measured resolutions are consistent with the system design goal of momentum resolution below 5% for charged particles with momenta up to 1 GeV in stand-alone SVT reconstruction [7].

We calculated the χ^2 for each track as

$$\chi^2 = \mathbf{r}^T \mathbf{V}^{-1} \mathbf{r}, \quad (23)$$

where the number of degrees of freedom, n_{dof} , is the number of clusters in the track minus four (since there are four parameters for the track fit). The distributions of the χ^2/n_{dof} values before and after alignment

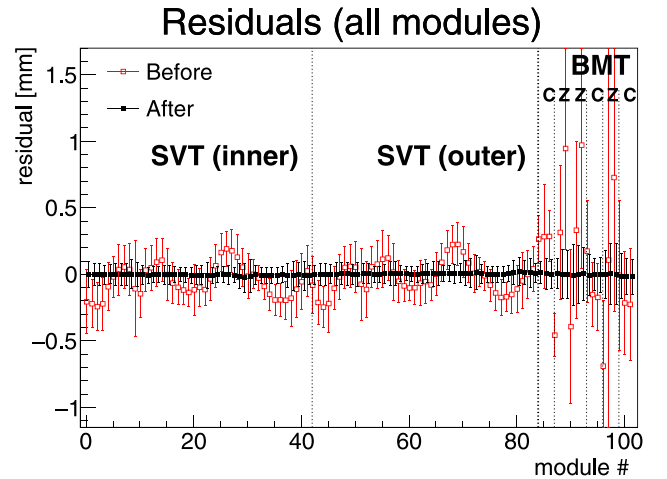


Fig. 8. Residuals for the each module, before (red, open symbols) and after (black, closed symbols) alignment. The error bars for each point represent the FWHMs of the distributions, divided by two (so that the distance from the top of the upper error bar to the bottom of the lower error bar is one FWHM). Module numbers 1–84 represent SVT sensors; numbers 85–102 represent BMT tiles. Symbols are shifted horizontally slightly for clarity.

are shown in Fig. 6(d). As shown in Fig. 7, the average χ^2/n_{dof} goes down from 10.0 to about 3.4 after the first iteration, and down to about 2.8 after the second. There is a very small improvement (<0.1) after the third iteration. After the fourth and fifth iterations, there is no significant change to the average χ^2/n_{dof} . Based on this assessment, there is no need to run the KAA for more than three iterations.

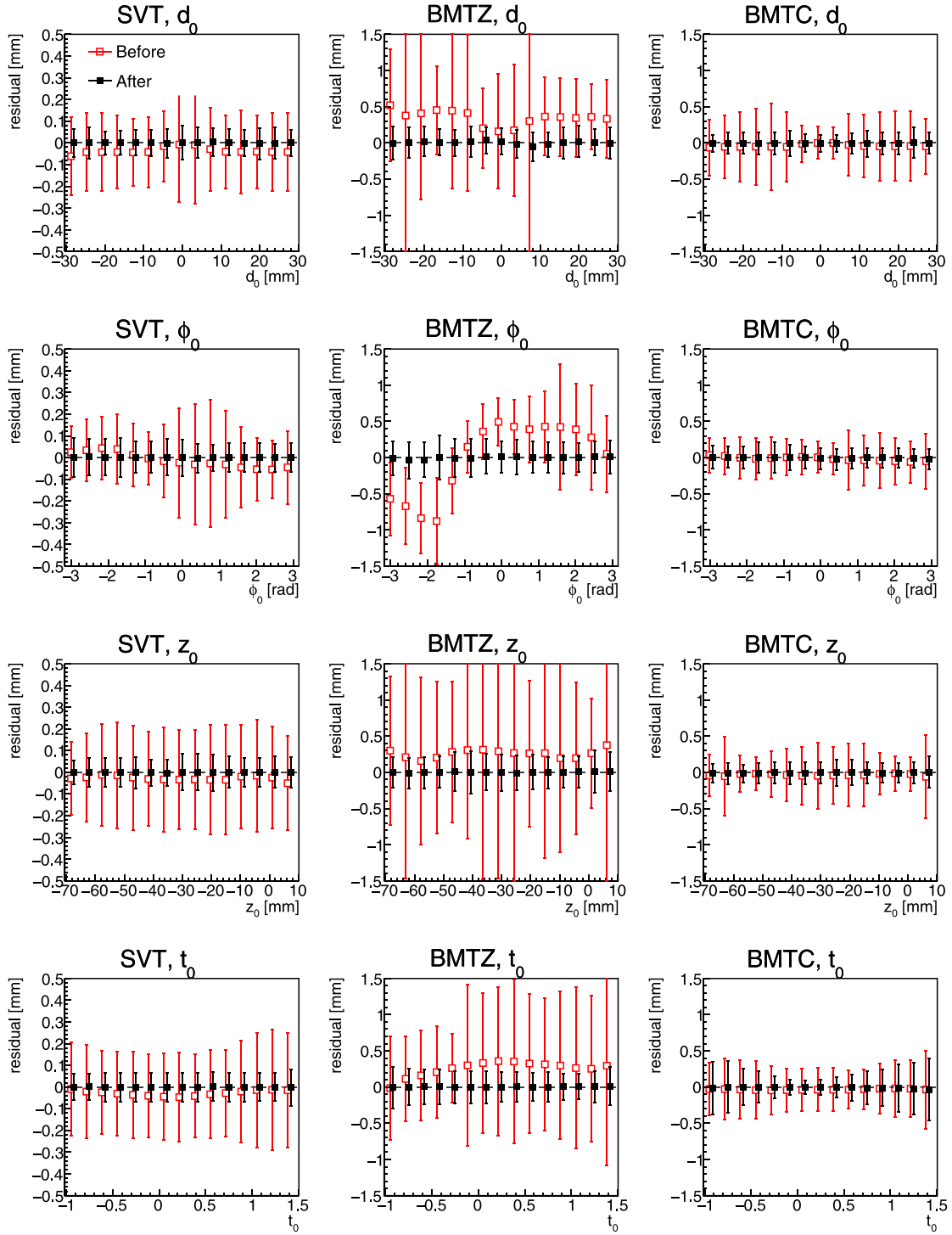


Fig. 9. Residuals before (red, open symbols) and after (black, closed symbols) alignment, as a function of the kinematic variables: from top to bottom, d_0 , ϕ_0 , z_0 and θ_0 . The error bars for each point represent the FWHMs of the distributions, divided by two (so that the distance from the top of the upper error bar to the bottom of the lower error bar is one FWHM). From left to right, the results are shown for the SVT, BMTZ, and BMTc. Symbols are shifted horizontally slightly for clarity.

Since the residual distributions in Fig. 6 are the sum over the residual distributions in all of the sensors of each given type, it does not provide information about the alignment of individual sensors. Therefore, we determined the residual distributions of every sensor module individually in order to make sure that none of them had large misalignments. We then determined the means and FWHMs of these distributions, which we show in Fig. 8. After fitting, the means of the residual distributions for all sensors are within 20 μm of zero, and the FWHMs are less than 170 (460) μm for each of the SVT (BMT) sensors.

The alignment process can become biased to show lower performance for certain track locations due to data sampling and the specific algorithm implementation. In order to show that there is no bias in the alignment, we studied the dependence of the residuals on the track parameters. Fig. 9 shows the residuals for each of the three detector types as a function of the track kinematic variables d_0 , ϕ_0 , z_0 and t_0 . The residual distributions after the alignment procedure are centered at zero, with no significant dependence on the kinematic variables.

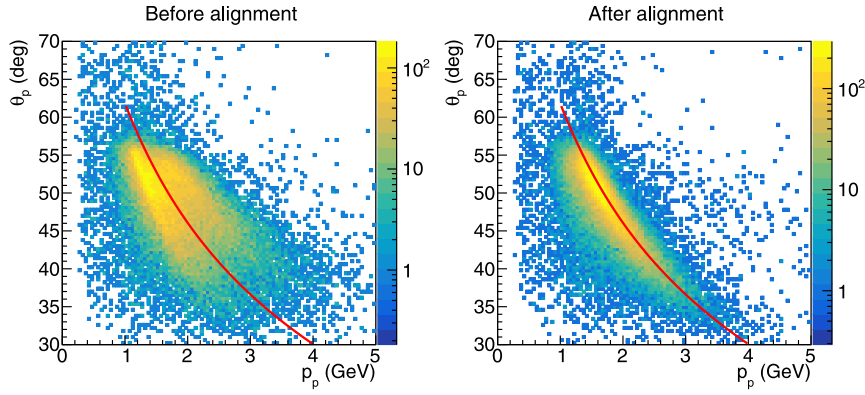


Fig. 10. Polar angle vs. momentum distributions for elastically scattered protons in the CVT, before (left) and after (right) the alignment. The curve shows the expected correlation between the two variables.

The KAA algorithm also yields the correlation among the alignment parameters. The correlations are given by the matrix \mathbf{C} , where each element is given by

$$C_{ij} = D_{ij} / \sqrt{D_{ii} D_{jj}}, \quad (24)$$

where \mathbf{D} is the covariance matrix. By construction, the diagonal elements of \mathbf{C} are equal to one. Many of the parameters are strongly correlated with one another, leading to off-diagonal elements of \mathbf{C} close to +1 (−1) when the correlations are strongly positive (negative). We show plots of the values of the elements of \mathbf{C} in Appendix C and discuss there in further detail which types of parameters are strongly or weakly correlated.

In order to see if the residual distributions depend on where the particles cross the sensors, we plot in Appendix D.1 the distributions of the residuals versus the extrapolated lab-frame coordinates of the hits in the detectors, both before and after the alignment. We also include the residuals versus the measured centroid strip number of the hits in each cluster. We found that the residual distributions after alignment appear to be centered at zero regardless of the position of the hit in the detector.

With an unaligned detector, the residuals in one sensor may be strongly correlated to those in another, whereas with a well-aligned detector, such correlations vanish. In Appendix D.2, we plot distributions of the residuals in one sensor versus those of another, for several different representative combinations of sensors. The 2D residual distributions show strong correlation for some of these combinations before alignment, but there is no significant correlation between the residuals after alignment.

To validate our results, we performed the same procedure on Monte-Carlo (MC) simulations, and present the results in Appendix E. In the simulations, the means of the residual distributions are within about 15 μm of zero, which is comparable to the data. However, the residual distributions are considerably narrower in the simulations than in the data, and as a result the χ^2/n_{dof} distribution in the simulation has a smaller mean than in the data. This could be due to a mis-modeling of the resolution effects in the detector, since the resolutions in the simulation were estimated using an idealized detector.

Finally, we validated that the alignment works not only for straight tracks, but also for curved tracks (with the solenoid field turned on), using the following test. Using a run configuration with 5 nA on liquid hydrogen at 10.2 GeV, we reconstructed events where electrons scattered elastically off a proton. These were selected by requiring one electron in the Forward Detector of CLAS12, with $W < 1.1 \text{ GeV}$,¹³ i.e. in the elastic-peak region, and at least one positive track in CVT,

which was assumed to be a proton. We show the distribution of the reconstructed polar angle θ vs the reconstructed momentum p of the protons in these reactions in Fig. 10, before (left) and after (right) the alignment procedure. The expected relation between θ_p and p_p for protons in elastic kinematics (which follows from the conservation of momentum) is:

$$p_p = \frac{2E_b m_p (E_b + m_p) \cos \theta_p}{E_b^2 \sin^2 \theta_p + 2E_b m_p + m_p^2}, \quad (25)$$

where m_p is the mass of a proton, and $E_b=10.2 \text{ GeV}$ is the beam energy; we show this as a curve overlaid on the distribution in Fig. 10. The θ vs. p distribution obtained after the alignment follows the curve much more closely than the one obtained before the alignment.

7. Conclusions

We have adapted the KAA, originally developed for CMS, to align the CLAS12 CVT—a hybrid detector consisting of both silicon and micromegas tracking technologies, with both curved and non-parallel strips.

Using a sample of cosmic-ray tracks and “field-off” data, we obtained residual distributions centered within 10 μm of zero for each of the silicon and micromegas sensors. In order to avoid significant bias from the non-linearity of the detector geometry, we had to run multiple iterations of the alignment, re-running the event reconstruction with the updated alignment parameters in between iterations.

By adapting the algorithm to the CLAS12 CVT, we demonstrated the flexibility and power of the KAA [3,4]. Future work will include extending these results to include the CLAS12 forward detectors or curved tracks as additional constraints.

The methodology and results detailed in this work could serve as reference for alignment of the CLAS12 CVT for upcoming experiments [16,17], as well as for future experiments at the Electron-Ion Collider [18].

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

The authors are unable or have chosen not to specify which data has been used.

¹³ W is defined as $\sqrt{2m_p \nu + m_p^2 - Q^2}$, where Q^2 is the square of the four-momentum transfer of the reaction, ν is the energy transfer, and m_p is the proton mass.

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Appendix A. Supplementary data

Supplementary material related to this article can be found online at <https://doi.org/10.1016/j.nima.2023.168032>.

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