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2 Revision 1

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4 Wave vector and field vector orientation dependence of Fe K pre-edge X-ray absorption features
5 in clinopyroxenes

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23

24

Abstract

25

26 Pre-edge X-ray absorption features are commonly used to derive redox states for
27 transition metal oxides in crystals and glasses. Several calibrations for Fe^{2+} and Fe^{3+} in silicate
28 glasses have utilized the general relationships among pre-edge peak intensity, energy, and redox
29 state. However, absorption variations complicate those relationships in anisotropic crystals.
30 Although absorption anisotropy at and above the energy of the rising edge adheres to the typical
31 \cos^2 relationship observed in absorption spectroscopies at other energies, the anisotropy of the
32 pre-edge is far more complicated. Prior studies focusing on pre-edge absorption anisotropy
33 demonstrate a $1-\cos 4\phi$ dependence of absorption magnitudes with rotation. Experiments
34 presented here show that absorption magnitudes of the pre-edge vary as a function of both
35 electric field vector orientation and wave vector direction. However, rotations around the field
36 vector axis or wave vector axis individually result in \cos^2 dependence of absorption magnitudes.
37 Rotations where both wave vector and field vector orientation are varied are not well-fit by either
38 model in the pre-edge. The resulting anisotropy complicates the process of measuring
39 characteristic absorption in the pre-edge, making valence state determinations challenging for
40 strongly anisotropic crystal structures such as pyroxene.

41

42

Introduction

43

44 In transition metal oxides, absorption over the pre-edge energy range of X-ray absorption
45 spectra is an important indicator of oxidation state and distortion of metal-containing polyhedra.
46 Because of its sensitivity to valence state, the pre-edge has been used by numerous authors to

47 indicate oxygen fugacity (f_{O_2}) of the crystallization or solidification environment of igneous and
48 metamorphic rocks (Bajt et al., 1994; Wilke et al., 2004; Yaxley et al., 2012). Among the
49 community of X-ray absorption spectroscopy (XAS) users, absorption anisotropy of spectra
50 collected from crystals is known to be a barrier to quantifying valence states of multivalent
51 elements (Dyar et al. 2002; Muñoz et al. 2013). Research on mineral samples has shown that in
52 anisotropic materials, calibrations for quantifying multivalent elements can be profoundly
53 affected by the orientation of the photon source relative to the polarization direction of the
54 crystals being studied.

55 The angular dependence of absorption anisotropy from energies spanning from the rising
56 edge and above is closely approximated as a $\cos^2\theta$ relationship from one absorption magnitude
57 to another. This has been demonstrated by numerous authors (Heald and Stern, 1977; Rosenberg
58 et al., 1986; Stöhr and Outka, 1987) and applied as a way of empirically interpolating absorption
59 magnitudes. In this study, the $\cos^2\theta$ relationship was determined from observations made using
60 ultraviolet-visible (UV-Vis) and infrared spectroscopies, where absorption magnitudes have
61 similar anisotropies.

62 In our earlier work, Steven et al. (2022) show that absorption anisotropy is well-modeled
63 in three dimensions with a $\cos^2\theta$ absorption indicatrix, a geometric model representing
64 absorption magnitudes for a given field vector direction. However, pre-edge anisotropy was
65 distinctly discordant from the $\cos^2\theta$ model. The discrepancy was suspected to be due to the
66 nature of the quadrupole transitions at pre-edge energies coupled with the relatively low
67 absorption intensities near the intense rising edge. For example, even a slightly overabsorbed
68 scan causes pre-edge peaks to be systematically more intense than an ideal scan, and is not
69 always fully corrected for in the normalization process. The suggestion that the discordance is

70 the result of quadrupole transitions is not new. An earlier example is a model employed by Hahn
71 et al. (1982), $\sin^2 2\phi$, which interpolates the observed data in Cu K-edge scans of a $(\text{CuCl}_4)^{2-}$
72 complex. Similarly, Uozumi et al. (1992) employed an equivalent model, $1-\cos 4\phi$, to describe
73 pre-edge anisotropy of Ti K-edge spectra of TiO_2 .

74 The objective of this research is to characterize the nature of absorption anisotropy in
75 clinopyroxene, with a focus on the pre-edge. Geologically, clinopyroxenes are an important
76 index mineral for determining conditions of the crystallization environment, namely in
77 geothermobarometry and oxybarometry. Among anisotropic minerals, clinopyroxenes exhibit
78 extreme X-ray absorption anisotropy, making them an ideal candidate for examining the angular
79 dependence of absorption anisotropy. Although the pre-edge peaks are the focus of these
80 experiments, full spectra were collected to gauge the extent of over-absorption. These
81 experiments were run on samples of end-member Fe^{2+} and Fe^{3+} clinopyroxenes, as well as a
82 mixed $\text{Fe}^{2+}/\text{Fe}^{3+}$ sample.

83 **Background**

84

85 In spectra acquired over visible wavelengths, anisotropic absorption is routinely observed
86 as pleochroism on a polarized light microscope. The amount of absorption depends on absorber
87 concentration, absorber orientation, and the orientation of vibration directions in the viewing
88 section of the crystal. In other words, given a random section of a crystal, the amount of
89 absorption is first dictated by the optical indicatrix and its orientation, then by the absorption
90 indicatrix at a given wavelength. Examples of the interplay between optical and absorption
91 indicatrices are given in Libowitzky and Rossman (1996) applied to infrared spectroscopy. The
92 orientation of vibration directions can be determined if the optical indicatrix orientation is

93 known. Vibration directions are simply the semi-major and semi-minor axes of an ellipse formed
94 by a plane section across the optical indicatrix. When linearly polarized light is oriented along a
95 vibration direction, a true absorption magnitude can be acquired. Plane sections of ellipsoid
96 calculations are ubiquitous in many corners of science, but an example derivation is in Gendzwill
97 and Stauffer (1981).

98 Because absorption magnitudes are influenced by polarization, observed magnitudes can
99 vary in an irregular fashion depending on the orientation of the crystal and the rotation axis. If
100 the rotation axis is a wave vector axis, absorption magnitudes are always $\cos^2\theta$ dependent.

101 Although refraction and crystal polarization effects are nearly nonexistent for X-ray
102 wavelengths, observed absorption anisotropy over the XAS energy range shares some
103 similarities with visible light. To an extent, absorption magnitudes can be modeled in three
104 dimensions using the concept of an absorption indicatrix, where absorption magnitudes in each
105 direction are modeled by a surface-described \cos^2 variation in all directions, as seen on the
106 surface in Figure 1 (Steven et al., 2022). However, \cos^2 dependence breaks down in the pre-edge.
107 Some authors have employed microscopic models to describe the anisotropy, while others (Hahn
108 et al. 1982; Uozumi et al., 1992) have used a macroscopic $1-\cos 4\phi$ model to describe magnitudes
109 from quadrupole transitions. Based on figures and descriptions of the collection geometries from
110 Hahn et al. (1982) and Uozumi et al. (1992), both collected scans from materials with rotational
111 symmetry, with that axis oriented vertically. The vertical axis was then rotated, designated in
112 both papers as a rotation of ϕ , to collect spectra at various ϕ settings. Those experiments were
113 collected in the geometry equivalent to the position shown in Figure 2, with crystals mounted
114 with rotational symmetry elements parallel to the ϕ -axis, and rotating the spindle axis ϕ . In this
115 study, θ is defined as the rotation axis parallel to the beam direction, and the ϕ -axis is defined as

116 a rotation axis orthogonal to the beam direction, which can be rotated by θ as depicted in Figure
117 2.

118 The 3-D models in Figure 1 only apply if the anisotropy depends on a single axis, such as
119 the electric field vector orientation. If there is wave vector dependence, observed absorption
120 magnitudes can deviate from these models. The experiments in this paper are designed to look
121 for and characterize this variation.

122

123 **Methods and Samples**

124

125 Three clinopyroxene samples were used to evaluate anisotropy of samples of that range
126 in $\text{Fe}^{3+}/\Sigma\text{Fe}$. They are 1) HMM119666, a hedenbergite composition from Broken Hill mines,
127 Yancowinna, New South Wales, Australia which has an $\text{Fe}^{3+}/\Sigma\text{Fe}$ of 0 and formula of
128 $(\text{Ca}_{0.990}\text{Na}_{0.002})(\text{Fe}^{2+}_{0.834}\text{Mg}_{0.045}\text{Mn}_{0.147})(\text{Si}_{1.989}\text{Al}_{0.004})\text{O}_6$ 2) DH208, an augite composition from
129 mantle xenoliths from Dish Hill, California, USA which has an $\text{Fe}^{3+}/\Sigma\text{Fe}$ of 0.36 and formula of
130 $(\text{Ca}_{0.810}\text{Na}_{0.107})(\text{Fe}^{2+}_{0.210}\text{Fe}^{3+}_{0.118}\text{Mg}_{0.579}\text{Mn}_{0.008}\text{Al}_{0.118})(\text{Si}_{1.751}\text{Al}_{0.249})\text{O}_6$ and 3) AMNH82544, an
131 aegirine from Langesundsfjord, Norway on loan from the American Museum of Natural History
132 which has an $\text{Fe}^{3+}/\Sigma\text{Fe}$ of 0.97 and formula of
133 $(\text{Ca}_{0.007}\text{Na}_{0.961})(\text{Fe}^{2+}_{0.026}\text{Fe}^{3+}_{0.849}\text{Mg}_{0.005}\text{Mn}_{0.037}\text{Ti}_{0.067}\text{Al}_{0.008})(\text{Si}_{2.013})\text{O}_6$.

134 Clinopyroxene single crystals were mounted on specimen pins with the spindle axis
135 parallel to a random axis, the **b**-axis, or the vector normal to (100). Crystal orientation was
136 guided by the (110) cleavages during mounting, then crystallographic axes vectors were located
137 using single-crystal X-ray diffraction (SC-XRD). The output orientation matrix from SC-XRD

138 was then related to the principle optical vectors using the methods described in Steven and
139 Gunter (2020).

140 For precise **b**-axis mounts, the diagonals of the intersections of the (110) cleavages were
141 mounted parallel to the specimen pin axis, resulting in an axis near either the **b**-axis, or the
142 normal vector to (100). While viewing into the microscope, the specimen pin was turned with the
143 X-ray goniometer fixed at the 0° spindle position until the long axis of the crystal (the **c**-axis)
144 was roughly in the plane of view for consistency. Crystals with an orientation matrix indicating
145 that the **b**-axis was within approximately 14° of the spindle axis are within range of goniometer
146 arc adjustments. Specimen pins on the X-ray goniometer were then marked to indicate the
147 location of the mounting notch and transferred to the coinciding position of an arc goniometer.

148 Optical orientations and crystal axes were then determined with spindle stage techniques
149 and EXCELIBR (Steven and Gunter, 2017). Despite the slight discrepancy resulting from the
150 transfer between goniometers, the crystallographic orientation from the SC-XRD should be near
151 the crystallographic orientation determined on the microscope (Figure 3). The Y = **b**-axis
152 orientation is then brought to the spindle axis by numerically minimizing the angle between the
153 spindle axis and the **b**-axis with the operations of the goniometer arcs represented as rotation
154 matrices. In Figure 3, open circles represent the orientation after the goniometer arcs are adjusted
155 so that Y = **b** is parallel to the spindle axis (the -x, +x cartesian axis); this required an up-arc
156 adjustment of -10.7° and lo-arc adjustment of -0.2° in this example. The beamline geometry is
157 then adjusted to match the microscope cartesian basis.

158 Fe K-edge spectra were collected at the 13-ID-E undulator-based microprobe at the
159 GeoSoilEnviro-CARS sector, Advanced Photon Source (APS), Argonne National Laboratory,
160 USA. Optical and instrument configuration of the beamline is outlined in Sutton et al. (2017). A

161 cryogenically-cooled, double-crystal Si(311) monochromator set was used for monochromatic
162 radiation. Beam to sample focusing was performed using a pair of 240 mm long, polished,
163 dynamically-bent silicon mirrors in a Kirkpatrick-Baez (KB) geometry. Beam focus is capable of
164 generating focused spot sizes of approximately $1.5 \times 2 \mu\text{m}$ full-width half maximum, and
165 incident monochromatic flux (I_0) in excess of 6×10^{12} photons/second, which is measured in a
166 helium-filled, 200 mm-long ion chamber upstream of KB mirror optics.

167 Experiments from this research measured fluorescence with a solid-state detector at 90°
168 to the X-ray source axis (Figure 2). Fluorescence spectra were collected using a Canberra SXD-7
169 7 element Si drift detector in conjunction with the high-speed digital spectrometer system
170 Quantum Xpress3. Incident X-ray energy was calibrated on the first derivative peak of Fe,
171 7110.75 eV, from an Fe metal foil standard (Kraft et al., 1996) and no energy drift was detected
172 throughout the analytical session. X-ray absorption spectra were collected for fluorescence with
173 a collection time of 1 second per step from 7012 to 7104 eV at an energy increment of 2 eV from
174 7012 to 7104 eV for the background region, 0.1 eV increment from 7104 to 7124 eV for the pre-
175 edge and edge region, 0.5 eV increment from 7124 to 7152 eV for the near edge region, and 5 eV
176 increment 7152 to 7407 eV for the EXAFS region.

177 A motorized θ -axis and ϕ -axis stage were used to perform the microscope stage and
178 spindle stage rotations to align vectors parallel to the **arrow goes above the E** E^\rightarrow field vector, though the wave vector direction k^\rightarrow is also known for
179 each crystal (Figure 2). Spectra were normalized and flattened initially in the software Larch
180 (Newville, 2013), and figures of the pre-edge are renormalized near the pre-edge to reduce the
181 effects of overabsorption outliers and focus on anisotropy. Flattened full spectra from 7012 to
182 7354 eV from this research are provided in the Online Materials¹.
183

184

185 **Fitting Data**

186

187 Above the pre-edge, anisotropy of XAS is well-characterized as a $\cos^2\theta$ or $\cos^2\phi$
188 relationship from one absorption magnitude to another, as is the case for other absorption
189 spectroscopies (Steven et al., 2022). However, pre-edge peaks are attributed to quadrupole and
190 mixed quadrupole-dipole transitions (De Groot et al., 2009). Because of the quadrupole
191 contributions, interpolating absorption anisotropy in the pre-edge requires a different model. The
192 angular-dependence of quadrupole transitions with respect to ϕ is fit by $1-\cos 4\phi$ following Hahn
193 et al. (1982) and Uozumi et al. (1992). Note that in their experiments, ϕ denotes the angle
194 between k^\rightarrow and the **a**-axis of TiO_2 , where k^\rightarrow and E^\rightarrow are kept perpendicular to the **c**-axis.
195 Essentially, those experiments were run by collecting spectra with the **c**-axis of TiO_2 oriented
196 vertically and parallel to the ϕ -axis, and after rotating ϕ at several ϕ angles. The utility of running
197 the experiment in this fashion is that the k^\rightarrow direction relative to the crystallographic basis is
198 easy to determine if there is angular dependence on k^\rightarrow . In the experiments for this study, ϕ only
199 designates the angle around the axis of the spindle, and crystal orientations are designated
200 separately. Thus, both k^\rightarrow and E^\rightarrow dependence are tested separately in ϕ and θ rotations.

201 In two dimensions, the observed $\cos^2\theta$ magnitudes of a section are fit numerically to
202 solve the parameters a , b , and ψ in the expression $a*\cos^2(\theta + \psi) + b*\sin^2(\theta + \psi) = r$, where r is
203 an absorption magnitude. For example, using a Gauss-Newton algorithm for angular-dependent
204 data of spectra collected at 7120 eV, the resulting fit has the parameters $a = 0.7506$ $b = 0.3626$ ψ
205 $= 8.22^\circ$ with an RMSE of 0.0136 for the sample in Figure 4. In scans where the \cos^2 does not fit

206 the data alone, a weighted combination of \cos^2 and $1-\cos 4\theta$ dependences are used following the
207 discussion of mixed dipole and quadrupole absorption character in Hahn et al. (1982).

208

209 **Scan types**

210

211 Three scan types are used here to test anisotropy with respect to rotating ϕ and θ . The
212 first type includes scans where ϕ is rotated at $\theta = 0^\circ$, which is denoted as the ϕ -axis, where $E^\rightarrow //$
213 ϕ . These scans are used only to test for wave vector dependence of spectra by fixing the
214 orientation of E^\rightarrow relative to the crystal's orientation. The second scan type is a rotation of ϕ at θ
215 $= -90^\circ$ (ϕ -axis, $E^\rightarrow \perp \phi$). This geometry is inspired by visible light absorption behavior, where if
216 \mathbf{b} is parallel to the ϕ -axis for a monoclinic crystal, the orthogonal direction is always a vibration
217 direction, eliminating crystal polarization effects.

218 The final scan type is a rotation of θ , which is also inspired by visible light absorption
219 behavior. This geometry is equivalent to rotating a microscope stage and observing pleochroism.
220 In θ rotations for visible light, there are two orthogonal vibration directions due to polarization
221 through the crystal. Relative to the lower polarizer, absorption magnitudes between the vibration
222 directions arise from the probability of polarization along these two paths rather than absorption
223 probability itself.

224 All three scan types were acquired on a near end-member Fe^{2+} hedenbergite sample
225 HMM119666. For the endmember Fe^{3+} aegirine samples and the mixed valence augites, only the
226 ϕ -axis, $E^\rightarrow // \phi$ and ϕ -axis, $E^\rightarrow \perp \phi$ scans were acquired. In each geometry, a spectrum is
227 collected, then the next spectrum is collected after rotating either the ϕ -axis or θ -axis by 10°

228 depending on scan type. This is repeated until a section spanning 0° to 170° or more is
229 completed.

230

231 **Results**

232

233 **Hedenbergite (Fe³⁺/ΣFe = 0.0)**

234

235 Hedenbergite samples (Fe²⁺-containing only without Fe³⁺) have three dominant pre-edge
236 peaks centered approximately at 7110.9 eV, 7111.7 eV, and 7113.2 eV. Hedenbergite sample
237 HMM119666 was run in three experimental geometries, two of which were sweeps with E^{\rightarrow}
238 oriented along various axes along (010) and one with $E^{\rightarrow} \parallel \phi$ -axis $\parallel \mathbf{b}$ -axis at different angles of
239 ϕ . In the first (010) scan, the crystal was mounted with $\mathbf{c} \parallel \phi$ with ϕ turned such that the photon
240 propagation direction $k^{\rightarrow} \parallel \mathbf{b}$ -axis at various θ settings (Figure 2). The second (010) scan
241 geometry is with the \mathbf{b} -axis $\parallel \phi$ at $\theta = -90^{\circ}$, while turning to various ϕ settings, and thus, E^{\rightarrow} was
242 also along axes in the (010) plane.

243

244 ϕ -axis, $E^{\rightarrow} \parallel \phi \parallel \mathbf{b}$ -axis

245

246 The ϕ -axis scan with $E^{\rightarrow} \parallel \phi \parallel \mathbf{b}$ -axis was run to test if or to what degree is there wave
247 vector dependence of X-ray absorption spectra of clinopyroxenes. HMM119666 was mounted
248 with the spindle axis ϕ parallel to the \mathbf{b} -axis for both consistency and to cover a wide variety of
249 orientations relative to a known symmetry axis. The scan geometry of this experiment has θ
250 fixed at zero for all spectra with the spindle axis parallel to the polarization axis E^{\rightarrow} . Spectra

251 were collected every 10 degrees from $\phi = 0^\circ$ to $\phi = 170^\circ$. With E^\rightarrow fixed along the **b**-axis, the
252 angular dependence of absorption relative to the crystal's orientation is with respect to k^\rightarrow
253 orientation in this dataset (Figure 6). As demonstrated in Figure 6, pre-edge peaks of
254 hedenbergite have strong absorption anisotropy when k^\rightarrow is varied and the orientation of E^\rightarrow is
255 fixed relative to the crystal. Spectra are fit with a $\cos^2\phi$ dependence for comparison, based on its
256 coincidence with the data.

257

258 θ -axis, $E^\rightarrow \perp \mathbf{b}$ -axis

259

260 Absorption magnitudes collected at different settings of θ were used to test whether
261 absorption anisotropy at X-ray wavelengths is analogous to UV-Vis and infrared wavelengths.
262 This geometry is equivalent to observing absorption magnitudes by rotating the microscope stage
263 of a pleochroic mineral in thin section. In this set of experiments, a single crystal of HMM19666
264 was mounted with the **c**-axis parallel to the ϕ -axis and ϕ was rotated to make k^\rightarrow parallel to the **b**-
265 axis at each θ setting. The resulting absorption magnitudes of the prominent pre-edge peaks are
266 plotted relative to θ setting in Figure 7 and fit with $\cos^2\theta$ dependence for comparison. After
267 normalizing, observed absorption anisotropy closely correspond to the $\cos^2\theta$ model for all
268 energies, and the angular dependence of the prominent peak centroids are plotted radially in
269 Figure 7.

270

271 ϕ -axis, $E^\rightarrow \perp \phi$

272

273 The geometry of scans where ϕ is rotated at $\theta = -90^\circ$ is depicted in Figure 2. In this
274 geometry, the **b**-axis of HMM119666 is mounted parallel to the ϕ -axis and resulted in the
275 absorption magnitudes shown in Figure 8. The orientations of both k^\rightarrow and E^\rightarrow are varied relative
276 to the crystallographic orientation. They result in a lobed absorption anisotropy relative to the
277 rotation axis minimum and maximum absorption occurring at 45° to one another with respect to
278 k^\rightarrow and E^\rightarrow . Only the 7113.2 eV peak can be fit with the 1-cos4 ϕ model. The other two peaks are
279 fit with a mixed model using weighted components of both 1-cos4 ϕ and cos² ϕ for comparison.

280

281 **Augite (Fe³⁺/ΣFe = 0.36)**

282

283 An intermediate Fe³⁺/ΣFe concentration of augite, DH208, was analyzed to assess pre-
284 edge peak intensities of a common composition of clinopyroxene. The pre-edge peaks of DH208
285 is subdivided into centroids centered at 7111.2 eV, 7112.9 eV, 7114.1 eV (Figure 9). Spectra of
286 augite were only collected in the geometry where ϕ is rotated with E^\rightarrow perpendicular to ϕ at a
287 fixed θ position of -90°. This corresponds to the exact position from Figure 2 and collecting
288 spectra every 10° from 0-170° ϕ . As with the pre-edge absorption of hedenbergite, augite spectra
289 also have the lobed absorption anisotropy when analyzed in this geometry. The peak centered at
290 7111.2 eV has absorption magnitudes with stronger four-fold symmetry, similar to the 7113.2 eV
291 peak of HMM119666. The 7112.9 eV and 7114.1 eV peaks are not as anisotropic as the 7111.eV
292 peak, but do exhibit nonsystematic differences in absorption intensity when normalized to 7115.5
293 eV. Peaks are fit with combined cos² ϕ and 1-cos4 ϕ models due to the large discrepancy with
294 both models when applied individually.

295

296 Aegirine ($\text{Fe}^{3+}/\Sigma\text{Fe} = 0.97$)

297

298 Aegirine samples that are completely oxidized consistently have two dominant pre-edge
299 peaks, one centered at 7112.8 eV and the other centered near 7114.1 eV. Among trivalent
300 transition metal oxides, the general interpretation of the lowest energy peak is that it arises from
301 quadrupole transitions to the empty d orbital. The next higher-energy peak has differing
302 interpretations, but is thought to occur from a mix of quadrupole transitions to $3d$ orbital and
303 non-local excitations to an adjacent $4p$ orbital (Vanko et al., 2008). In both scan geometries
304 analyzed, aegirine exhibits the greatest difference in absorption extremes of the pre-edge peaks
305 in all pyroxenes scanned when comparing Figures 6 - 11.

306

307 ϕ -axis, $E^\rightarrow // \phi$

308

309 A limited dataset was collected in the geometry in which $E^\rightarrow // \phi // \mathbf{b}$ -axis to investigate
310 whether or not the anisotropy of the Fe^{3+} end-member aegirine is similar to the Fe^{2+} hedenbergite
311 sample. Absorption magnitudes are plotted radially and fit with a $\cos^2\phi$ model in Figure 10. Even
312 with the limited dataset, absorption magnitudes also follow the $\cos^2\phi$ model as with the more-
313 complete dataset of HMM119666. At a minimum, this dataset demonstrates strong absorption
314 anisotropy, and the angular dependence of the absorption anisotropy does not have four-fold
315 symmetry, just as with HMM119666 in this geometry.

316

317 ϕ -axis, $E^\rightarrow \perp \phi$

318

319 The 7112.8 eV aegirine peak collected in the ϕ -axis, $E^{\rightarrow} \perp \phi$ geometry resembles the
320 same lobed appearance as the 7113.2 eV peak of hedenbergite and the 7111.2 eV peak of augite
321 (Figure 11). The 7114.1 eV peak is only similar to the 7114.1 eV peak of augite but is not
322 particularly well described by either the $\cos^2\phi$ or $1-\cos4\phi$ models individually. Rather, a mixed
323 model is applied to fit the datapoints following the discussion of mixed quadrupole and dipole
324 transition character among trivalent oxides in Vanko et al. (2008). The pre-edge peaks of
325 aegirine are both the most intense, and most anisotropic in terms of the variation of peak area
326 ratio differences between the 7112.8 and 7114.1 eV peaks with respect to ϕ position.

327

328 **Discussion**

329

330 Individually, wave vector dependence appears to be the same as field vector dependence,
331 in that absorption anisotropy is well-fit with the \cos^2 model. However, when varying both the
332 wave vector and field vector orientations of any pyroxene crystal, absorption magnitudes
333 delineate irregular patterns that do not always correspond with the $1-\cos4\phi$ model that worked to
334 describe anisotropy in TiO_2 from Uozumi et al. (1992). Arguably, the combination of the two
335 models describes the absorption anisotropy from Figures 8, 9, and 11 that would coincide with
336 the explanation of mixed dipole and quadrupole character from each sample. Scans analyzing the
337 same section, such as the (010) of HMM119666, exhibit different results depending on rotation
338 and mount axis. For example, with E^{\rightarrow} in the (010) plane, absorption magnitudes collected by
339 rotating ϕ (Figure 8) differs from those collected by rotating θ (Figure 7). This suggests that
340 quadrupole transitions are also strongly dependent on k^{\rightarrow} orientation unlike dipole transitions
341 (Hahn et al., 1982). The results from this study, particularly the scans from HMM119666 are

342 antithetical to the expected absorption anisotropy if pre-edge peaks resulted from dipole
343 transitions alone. With the selection rules of quadrupole transitions having dependence on E^\rightarrow
344 and k^\rightarrow orientation (Hahn et al., 1982), the exact scan geometry of the pre-edge is thus a
345 significant factor when analyzing the pre-edge of anisotropic crystals.

346 Absorption above pre-edge energies does not demonstrate significant variation with
347 respect to k^\rightarrow orientation alone (Figure 5). However, the systematic difference in absorption due
348 to differing count rates for each spectrum collected in Figure 5 emphasizes another concern. This
349 concern is the extreme sensitivity of the rising edge to thickness and absorber concentration as
350 discussed in Heald and Stern (1977). Ordinarily, corrections for variation in count rates produce
351 consistent results for multiple spectra collected on irregular crystals. However, overabsorption is
352 likely when analyzing thicker sections of irregular, high Fe crystals such as hedenbergite. As a
353 result, the peaks just above the rising edge are vary in scale, though in a systematic way.

354

355 Comparisons between visible light and X-ray absorption

356

357 Absorption anisotropy in the pre-edge is only similar to visible light anisotropy in two
358 ways. The first is that rotations around the wave vector axis result in $\cos^2\theta$ dependence of
359 absorption magnitudes. The second similarity is that the pre-edge absorption anisotropy has
360 wave vector orientation dependence. With visible light, this dependence arises from the
361 polarization paths through the crystal, whereas with X-ray wavelengths, the dependence is
362 related to differences in atomic positions along the propagation path, along with the type and
363 nature of the transitions.

364 When changing the propagation path at a fixed vibration path orientation, there are no
365 perceivable differences in absorption intensity above pre-edge energies. In contrast, pre-edge
366 peak intensities vary by as much as 33% of its maximum intensity when changing the
367 propagation path, even at a fixed E^{\rightarrow} orientation. In visible light spectroscopy, a change in
368 absorption due to propagation path orientation does occur, but is understood to be due to a
369 change in polarization state through the crystal. Because anisotropic crystals are considered to
370 split visible light into two linear vibration paths in classical mechanics, the amount of absorption
371 depends on the amount of light traveling along each path, and the amount of absorption along
372 each path. The amount of light traveling along each path depends on the initial orientation of
373 linearly polarized light relative to the orientations of the two vibration paths. In the XAS
374 experiments above, fluorescence is measured and is proportional to absorption. The disparity
375 between visible light and X-ray absorption anisotropy is strongest when examining pre-edge
376 energies and is only apparent in geometry from Figure 2 where ϕ is rotated. Rotations of ϕ with
377 the rotation axis parallel to the polarization axis at pre-edge energies result in \cos^2 angular-
378 dependence. Similarly, rotations of θ also have the \cos^2 dependence between pre-edge energies
379 and visible light. As mentioned, the disparity arises from the geometry where ϕ is rotated and E^{\rightarrow}
380 is orthogonal to the ϕ -axis and propagation direction. When modeling the effects of polarization
381 with the optical indicatrix model combined with an absorption indicatrix model of a monoclinic
382 crystal, rotations of ϕ do not result in absorption magnitudes with four-fold symmetry.

383 Under visible light, ϕ rotations with the geometry of Figure 2 will have two-fold
384 symmetry angular-dependence rather than the four-fold symmetry shown in Figures 8, 9, and 11.
385 Depending on how the crystal is mounted, lower symmetry crystals will generally display two-
386 fold angular-dependence of absorption, which is not necessarily \cos^2 dependent in this geometry.

387

388 Possible factors contributing to X-ray absorption anisotropy

389

390 At X-ray wavelengths, diffraction dominates, which has a significant effect on X-ray
391 absorption. For example, the Borrman effect is the increased X-ray transparency of a crystal
392 along Bragg reflections (Borrman, 1941).

393 Moreover, quadrupole transitions of the pre-edge have different angular dependence of
394 absorption probabilities than dipole transitions both in theory and observation. As mentioned
395 above, the fits of the pre-edge by Uozumi et al. (1992) from Ti K-edge spectra use the $1-\cos 4\phi$
396 model. This model fits some of the pre-edge peaks of pyroxenes but not all. It should also be
397 noted that ϕ only refers to the experimental geometry, so the equation is not necessarily
398 applicable to field vector orientations in the crystal's basis. Rather, it may depend on how the
399 crystal is mounted. As shown in Figures 7 and 8, collecting absorption spectra with the field
400 vector oriented along the same axes with differing wave vector directions may yield different
401 results.

402 If X-ray absorption anisotropy was dependent only on the field vector orientation relative
403 to absorbers, there should be no difference in the results shown in Figures 7 and 8, nor should
404 there be variation in the spectra from Figure 10. Further, wave vector dependence is distinct only
405 in the pre-edge of spectra. Differences of absorption anisotropy between quadrupole and dipole
406 transitions are likely the reason for the strong dependence of k^\rightarrow orientation for pre-edge
407 energies.

408

409 $1-\cos 4\phi$ dependence

410

411 The lobed anisotropy that arises only from the ϕ -axis, $E^{\rightarrow} \perp \phi$ experiments apparently
412 results from the combined wave vector and field vector dependences of the spectra. When
413 spectra are collected at different ϕ -axis settings at $\phi = 0$, however, the orientation of E^{\rightarrow} is fixed
414 and the anisotropy follows the \cos^2 model. With our limited dataset testing the wave vector
415 dependence of the pre-edge, the absorption magnitudes do not resemble the lobed appearance of
416 the other ϕ -axis scans, and instead correspond closely with the $\cos^2\phi$ fit.

417 Wave vector dependence may arise from a change in multiple scattering paths. In θ
418 rotations, multiple scattering paths are the same relative to the wave vector. Although numerous
419 authors have demonstrated absorption anisotropy of XAS, wave vector and field vector
420 dependence of pre-edge XAS anisotropy was theorized by Brouder (1990) on the basis of
421 multiple-scattering theory combined with group theory.

422 Regardless of whether the wave vector dependence is due to the nature of the quadrupole
423 transitions or a product of multiple scattering paths, the pre-edge is significantly affected by both
424 the orientation of the wave vector and field vector. In experiments where the field vector
425 orientation was fixed and wave vector varied, absorption intensity changed by as much as 33%.
426 This implies that empirical quantification of valence states of anisotropic crystals using the pre-
427 edge is far more complicated than originally thought. Reference datasets for determining redox
428 ratios in anisotropic crystals must account for both contributors to anisotropy. This involves
429 either modeling the anisotropy, or, creating a dataset that is valid for a specific orientation, both
430 in section, and vibration direction.

431

432 **Implications**

433

434 Given the significant wave vector and field vector orientation dependence of XAS on
435 pyroxenes, absorption anisotropy remains difficult to characterize. The fact that anisotropy with
436 respect to wave vector orientation is just as significant as field vector orientation implies that
437 orientation-dependent XAS studies will be most useful if they keep track of E^{\rightarrow} and k^{\rightarrow} in the
438 crystal's basis for each spectrum. The uncertainty of how absorption magnitudes are influenced
439 by orientation has major ramifications for quantifying valence states using the pre-edge only,
440 even in studies attempting to compare similar orientations. In this regard, collecting a spectrum
441 along the same orientation generally refers to the orientation of the field vector, though in XAS,
442 the wave vector axis must also be the same to eliminate the orientation variable in a valence state
443 calibration. Given the change in peak intensity by 33% in some pre-edge peaks, this can
444 dramatically influence Fe valence state predictions in clinopyroxene based on the pre-edge alone,
445 especially if the analyzed orientation does not have the exact same E^{\rightarrow} and k^{\rightarrow} orientation in the
446 crystal's basis. The clinopyroxene group minerals studied here are an extreme example of
447 absorption anisotropy due to the linear arrangement of the absorbers in their structure.

448 More optimistically, this study provides the first steps that will enable modeling for
449 valence state calibrations in pyroxenes empirically. Anisotropy from rising edge energies up
450 follow straightforward systematics once enough datapoints are collected to define characteristic
451 absorption axes (Steven et al., 2022). This allows production of a database of spectra, collected
452 at all possible orientations, to be built from oriented spectra of standards with known Fe^{3+}
453 contents. In other words, acquisition of XAS spectra from standards with known Fe^{2+} and Fe^{3+}
454 concentrations at known orientations provides the data from which spectra at any orientation can
455 now be calculated. Those data can in turn be used as training data for classification or regression

456 models utilizing machine learning algorithms. The resultant models can be used to predict Fe^{2+}
457 and Fe^{3+} in unknown samples at random orientations, either by matching spectra of unknowns to
458 those of standards, or through multivariate analyses based on the training data. Our group is
459 pursuing this approach for pyroxenes, with an ultimate goal of generating robust methodology
460 for measuring Fe^{2+} and Fe^{3+} in pyroxenes in thin section.

461

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463

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466

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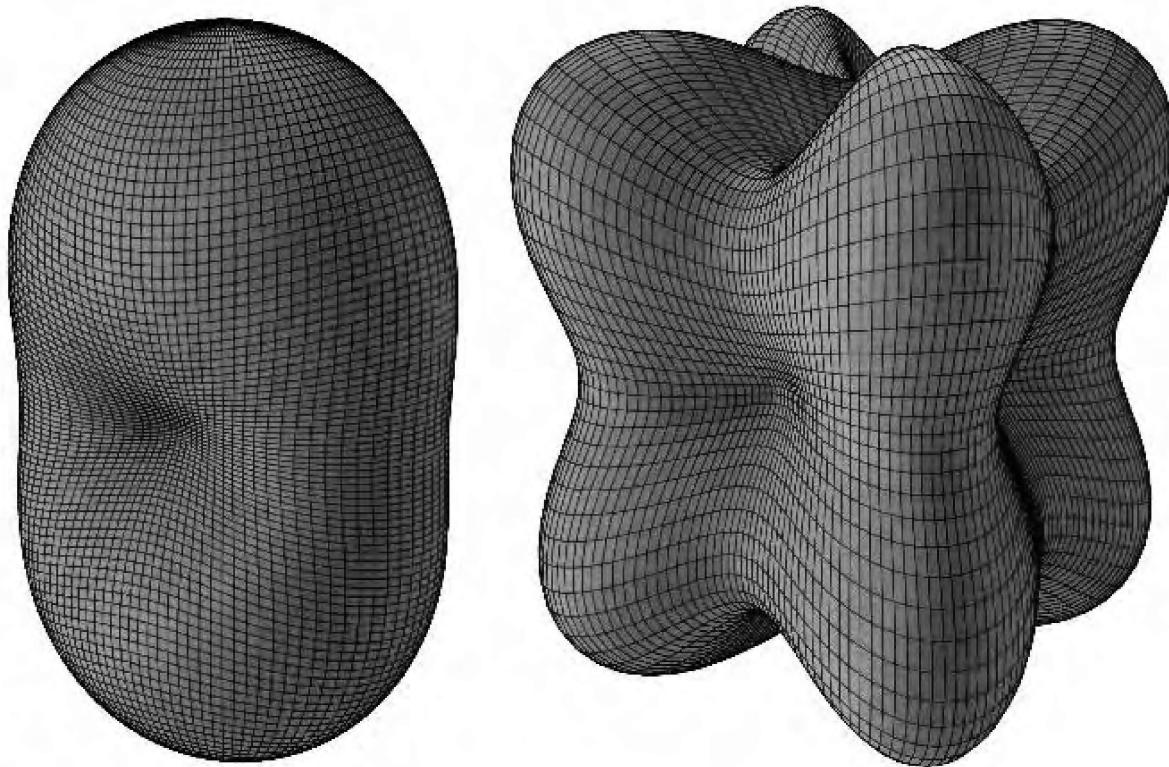
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Figures

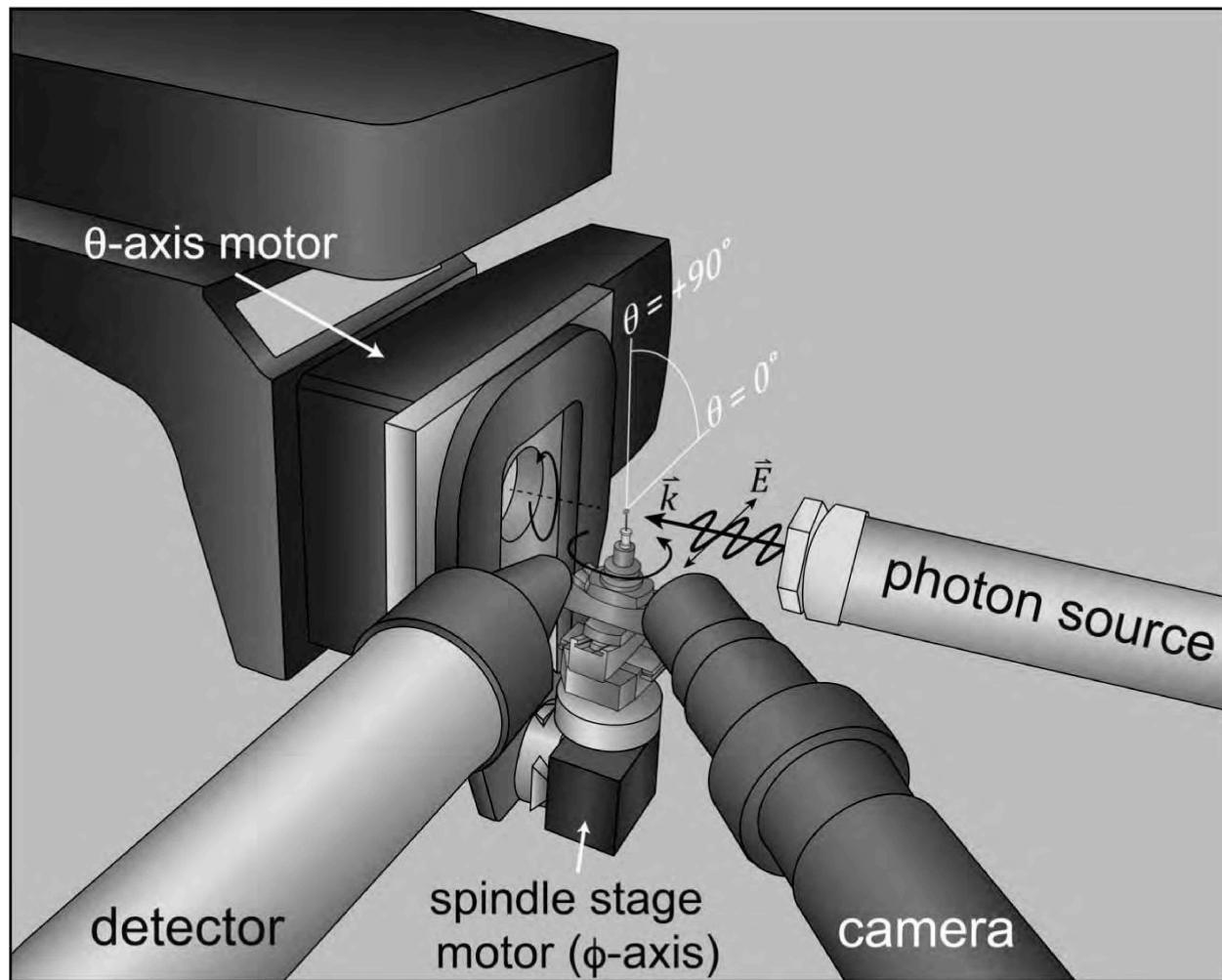
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557 **Figure 1)** Absorption indicatrices based on absorption due to only dipole transitions (left) and a
558 possible absorption indicatrix due to quadrupole transitions (right).

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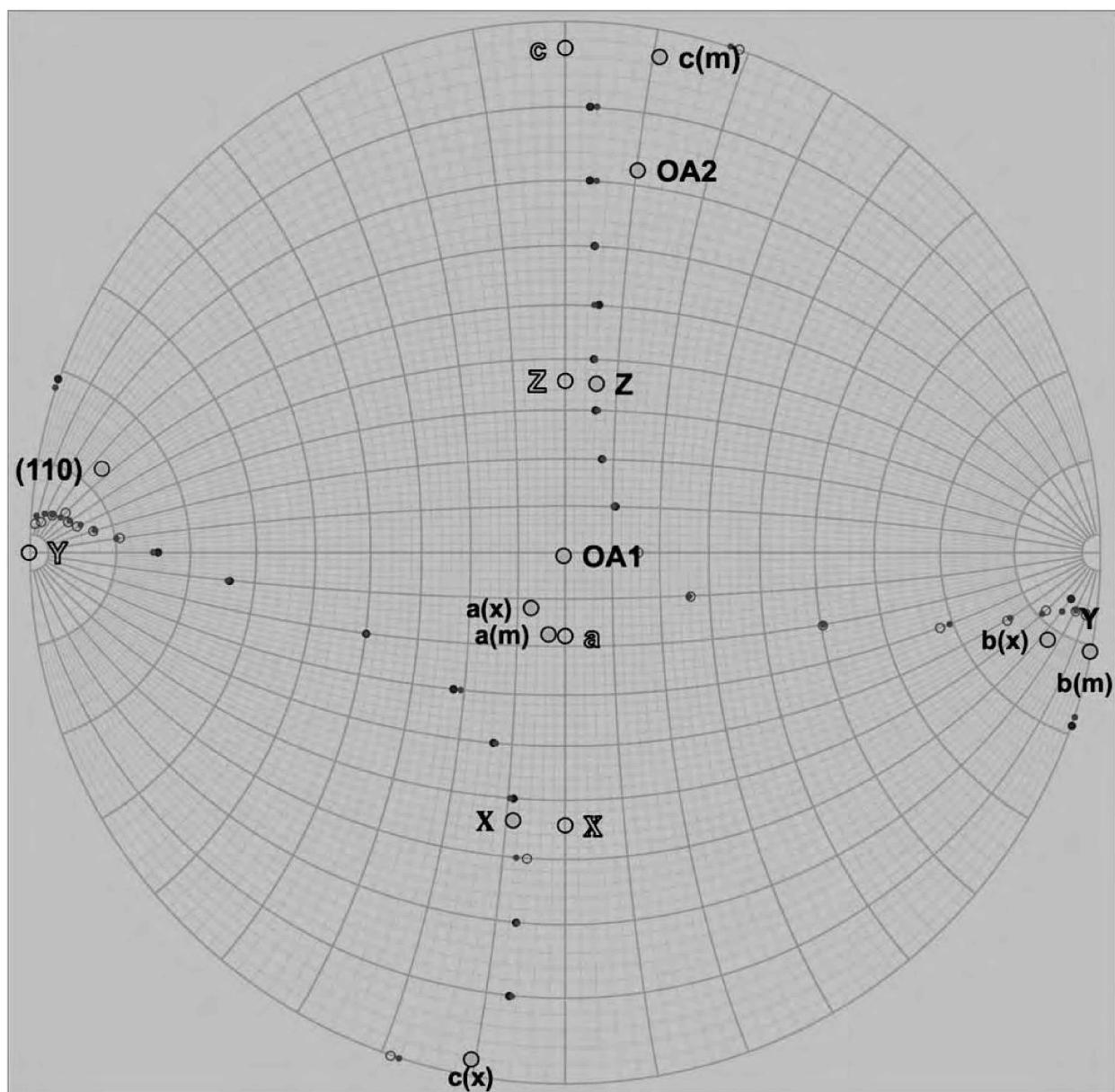


560

561 **Figure 2)** Experimental geometry for analyzing single crystals at Argonne National Laboratory.

562 A motorized spindle ϕ and stage θ rotate around their respective axes. The wave vector \vec{k} of the
563 photon source propagates along the θ -axis and the field vector \vec{E} is orthogonal to \vec{k} and in the
564 horizontal plane.

565



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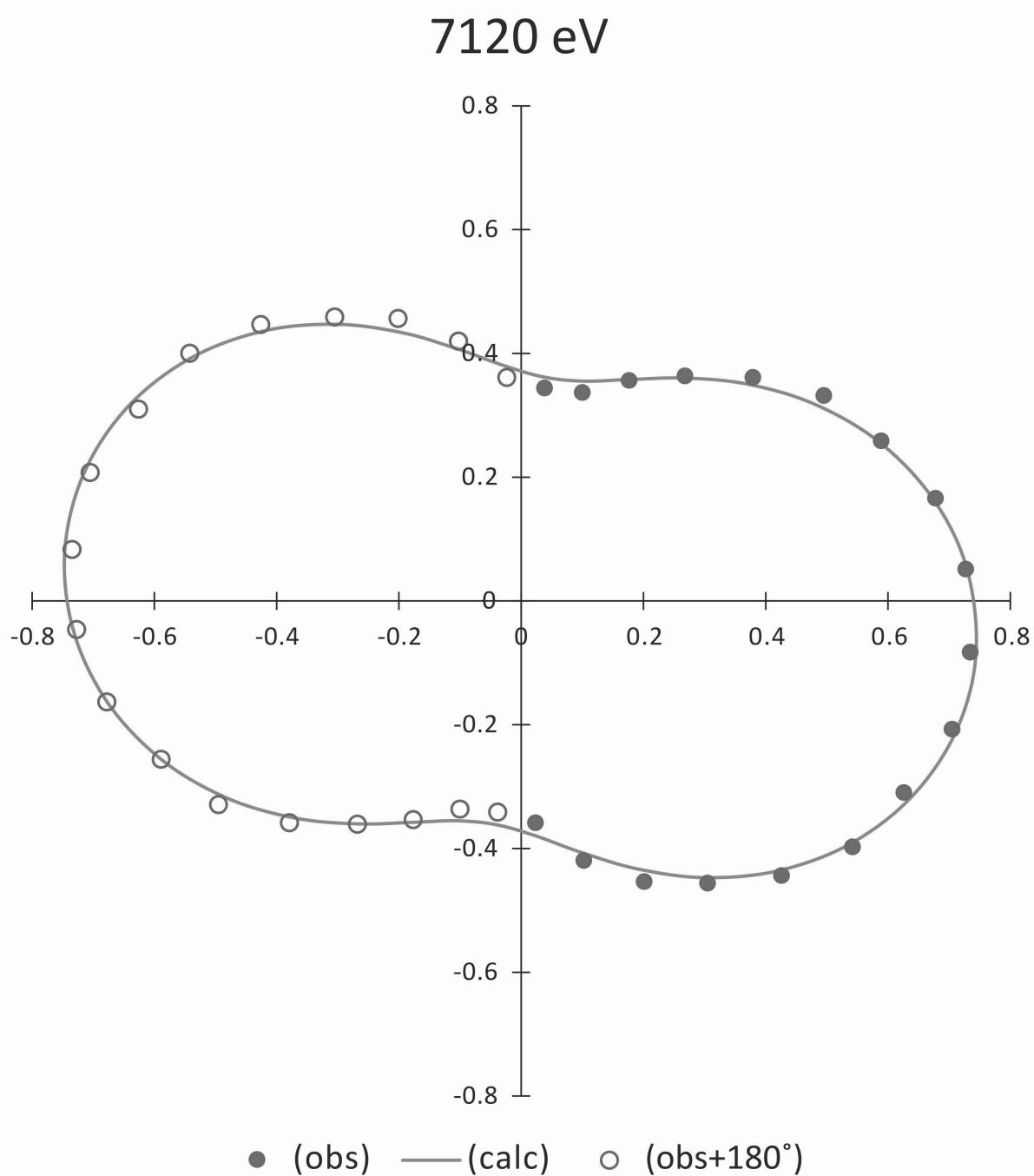
567 **Figure 3)** Stereogram of an initial determination of principle optical vectors and crystallographic
568 axes of a pyroxene. The orientation after manipulating the goniometer arcs is represented as open
569 circles.

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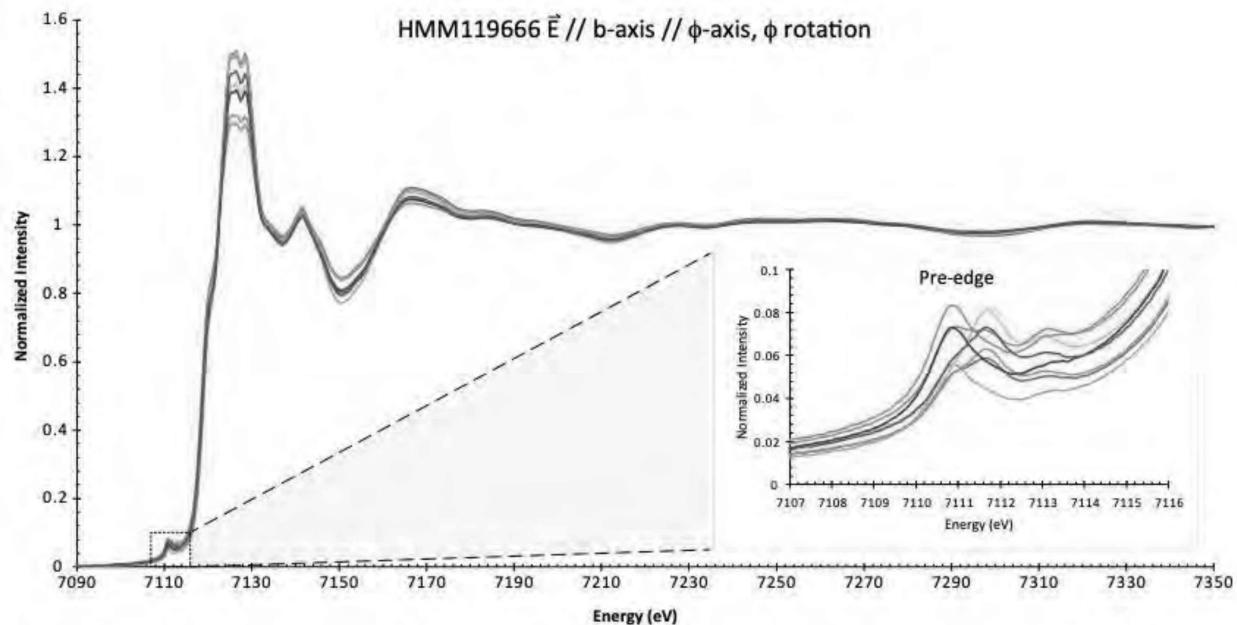
574

575 **Figure 4)** Absorption magnitudes collected at the rising edge (7120 eV) with \vec{E} oriented along
576 various axes in the (010) plane of a 34% $\text{Fe}^{3+}/\Sigma\text{Fe}$ augite. In this and following figures, the
577 magnitudes of the axes represent absorption intensity.

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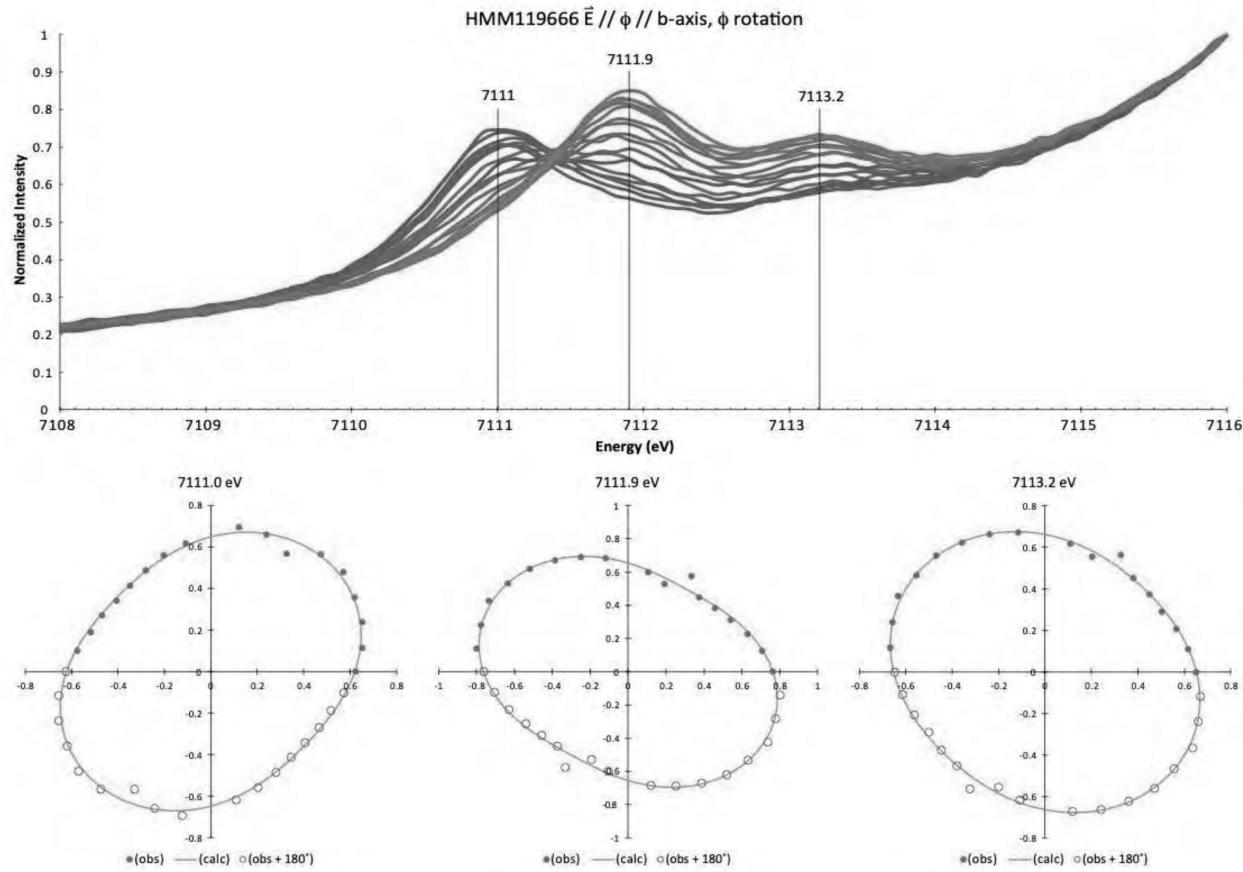
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Figure 5) Full X-ray absorption spectra collected from multiple wave vector axes with the field vector axis fixed. A plot of a magnified view of the pre-edge is inset, and a detailed examination of the anisotropy of the pre-edge peak centroids for this sample is given in Figure 6.

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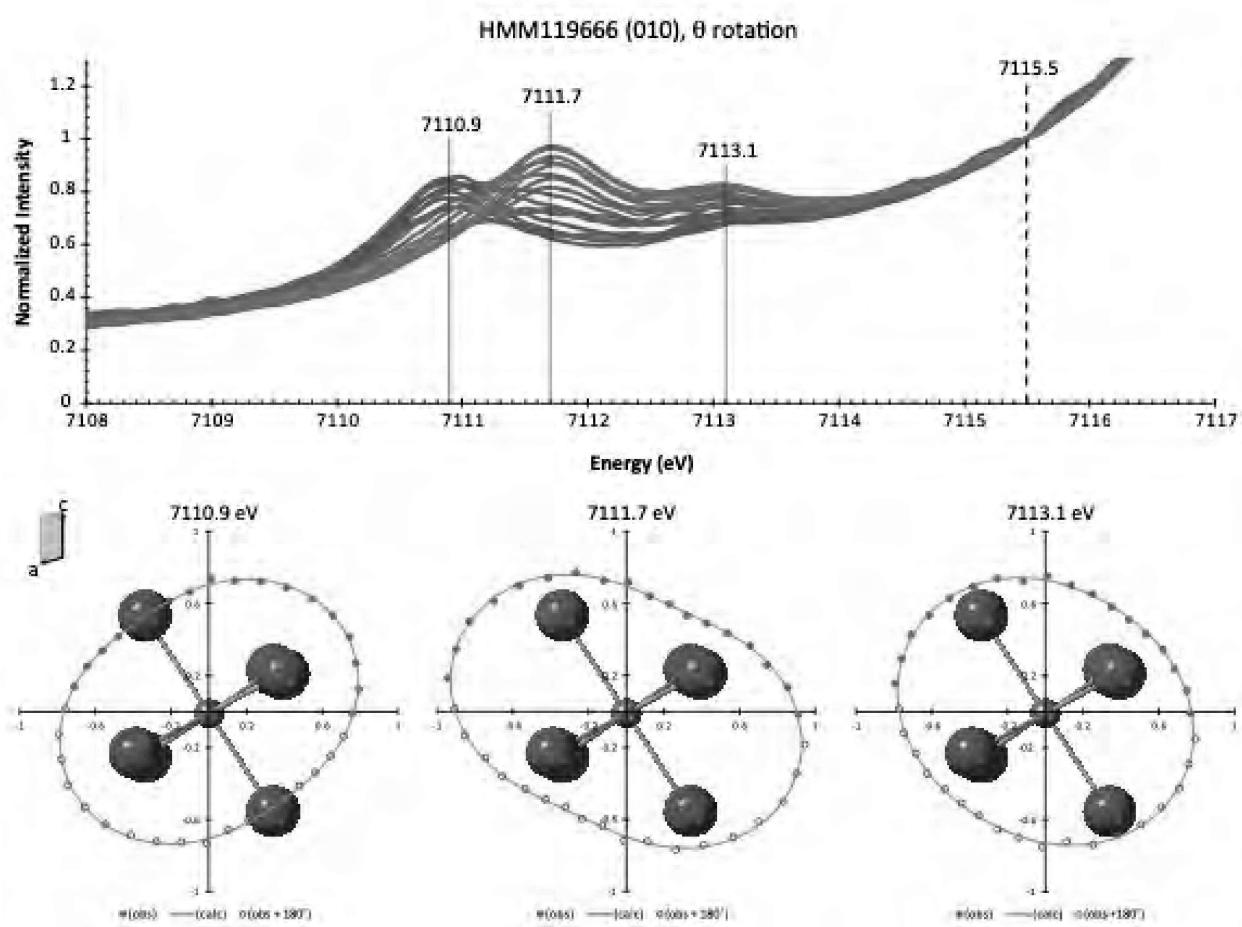


586

587 **Figure 6**) X-ray absorption spectra (top) of a 0.0 $\text{Fe}^{3+}/\Sigma\text{Fe}$ hedenbergite analyzed at a selection
588 of ϕ -axis angles with $\vec{E} // \phi // \mathbf{b}$ -axis. The resulting absorption magnitudes are plotted radially
589 with respect to \vec{k} orientation (bottom) at 7110.8, 7111.7, and 7113.1 eV. Absorption magnitudes
590 are the distances of the points from the origin in the radial plots, and are fit with $\cos^2\phi$ for
591 comparison. Axes in bottom row follow conventions used in Figure 4.

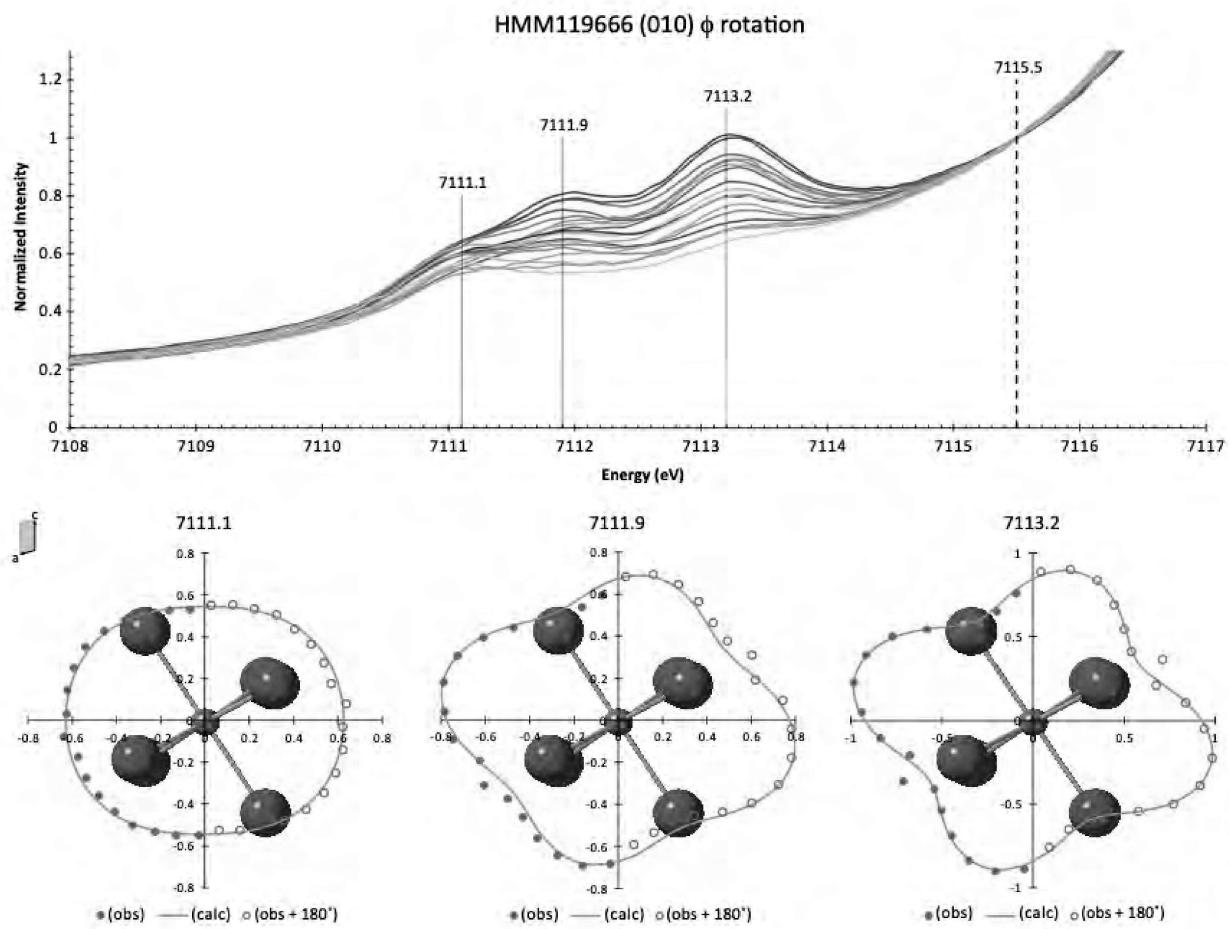
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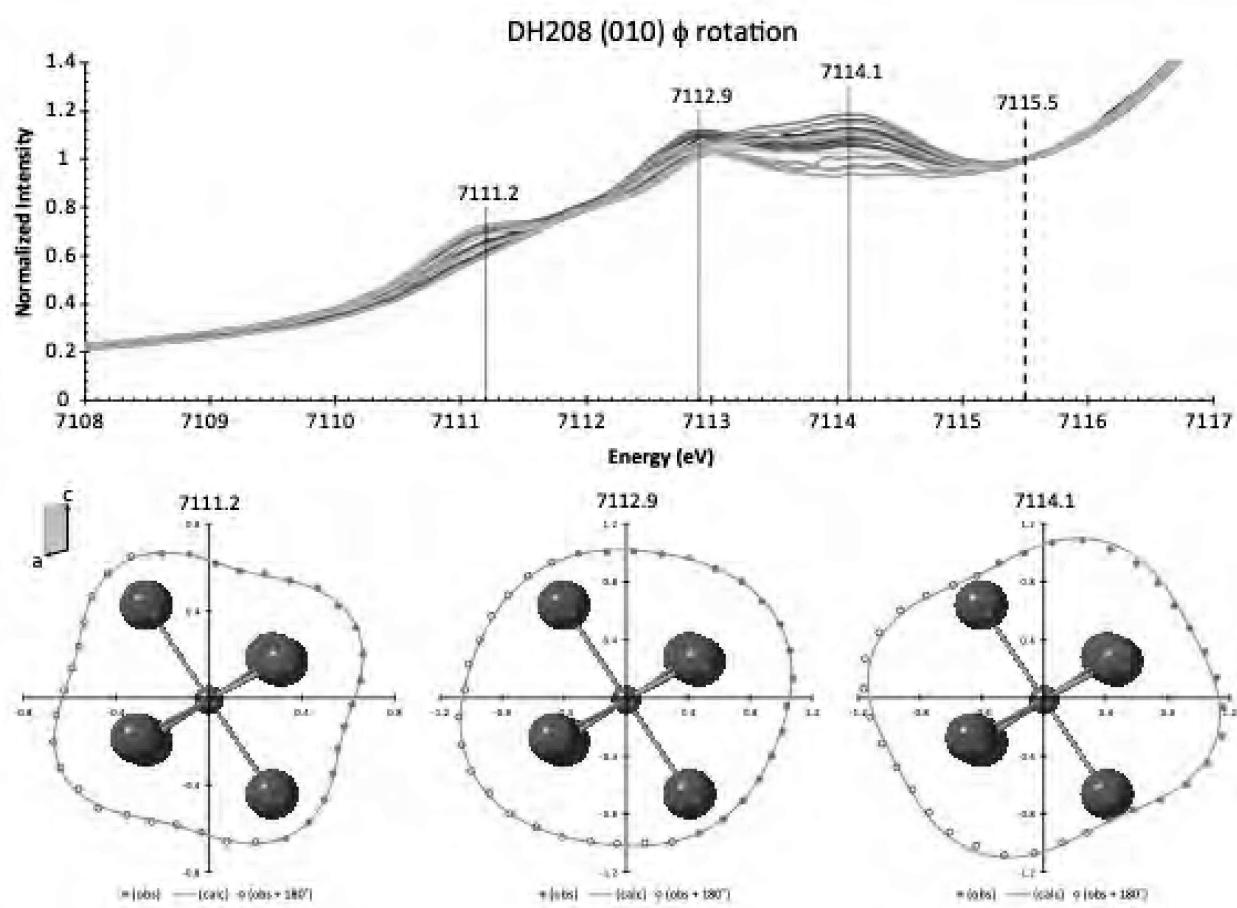
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595 **Figure 7)** X-ray absorption spectra (top) of a 0.0 $\text{Fe}^{3+}/\Sigma\text{Fe}$ hedenbergite analyzed with \vec{E}
596 oriented along various axes in (010) with the orientation of \vec{k} fixed along the b-axis. Absorption
597 magnitudes are plotted radially (bottom) with respect to the orientation of \vec{E} at 7110.9, 7111.7,
598 and 7113.1 eV. Spectra are renormalized near the pre-edge peaks at 7115.5 eV to highlight the
599 anisotropy. The orientation of the crystallographic axes and the coordinating polyhedron of the
600 M1 site is depicted relative to the orientation of the absorption magnitudes. Axes in bottom row
601 follow conventions used in Figure 4.



603 **Figure 8)** X-ray absorption spectra (top) of a 0.0 $\text{Fe}^{3+}/\Sigma\text{Fe}$ hedenbergite analyzed with \vec{E} and \vec{k}
604 oriented along various axes in (010). The crystal was mounted with the b-axis // ϕ -axis at $\theta = -$
605 90° as depicted in Figure 2 with spectra collected at various ϕ settings. Absorption magnitudes
606 are plotted radially with respect to \vec{E} orientation, and for each datapoint the orientation of \vec{k} is
607 90° away. Spectra are renormalized near the pre-edge peaks at 7115.5 eV to highlight the
608 anisotropy. The orientation of the crystallographic axes and the coordinating polyhedron of the
609 M1 site is depicted relative to the orientation of the absorption magnitudes. Axes in bottom row
610 follow conventions used in Figure 4.

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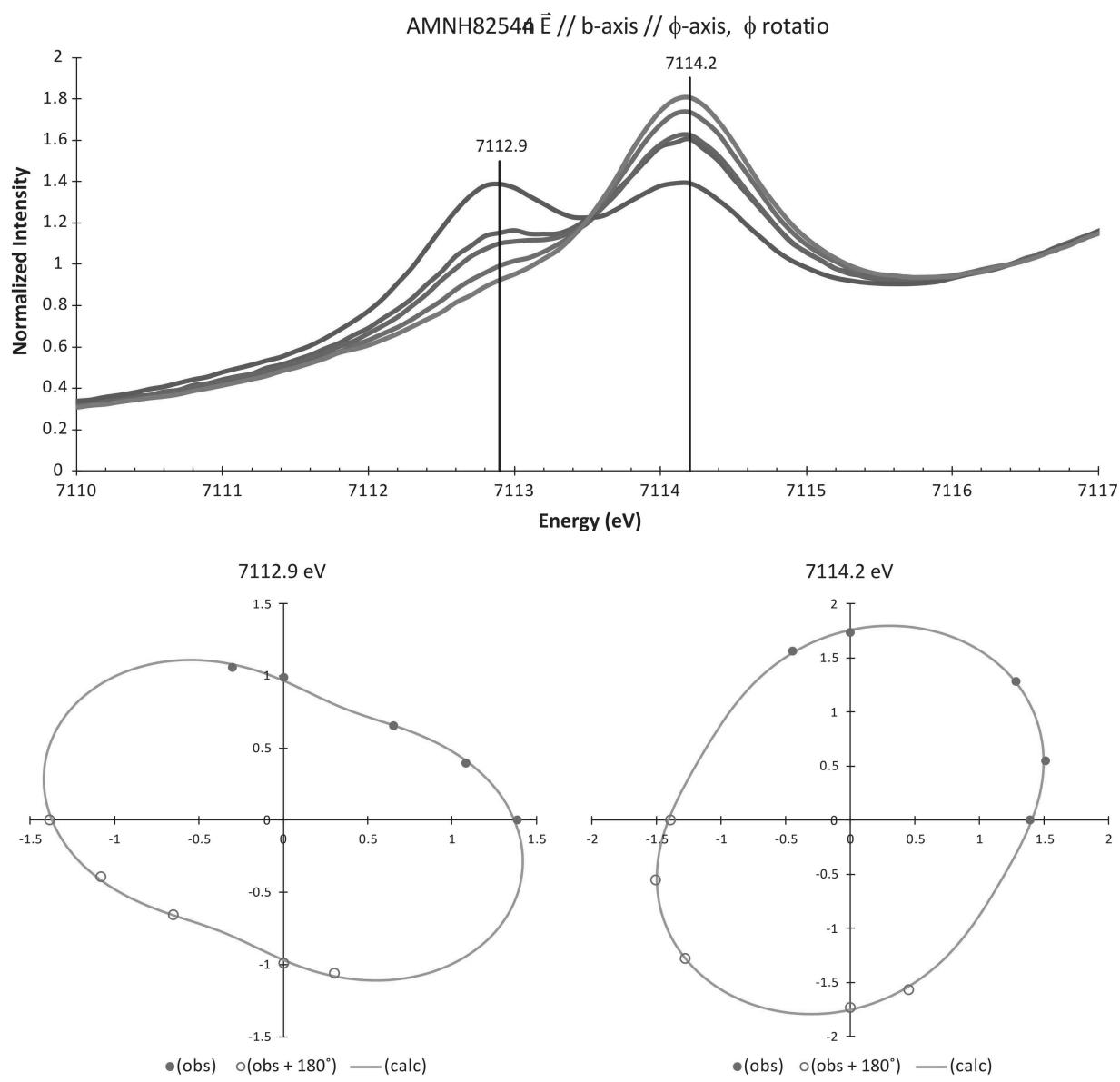


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614 **Figure 9)** X-ray absorption spectra (top) of a 0.3 $\text{Fe}^{3+}/\Sigma\text{Fe}$ augite analyzed with \vec{E} and \vec{k} oriented
615 along various axes in (010). The crystal was mounted with the b-axis // ϕ -axis at $\theta = -90^\circ$ as
616 depicted in Figure 2 with spectra collected at various ϕ settings. Absorption magnitudes are
617 plotted radially with respect to \vec{E} orientation, and for each datapoint the orientation of \vec{k} is 90°
618 away. Spectra are renormalized near the pre-edge peaks at 7115.5 eV to highlight the anisotropy.
619 The orientation of the crystallographic axes and the coordinating polyhedron of the M1 site is
620 depicted relative to the orientation of the absorption magnitudes. Axes in bottom row follow
621 conventions used in Figure 4.

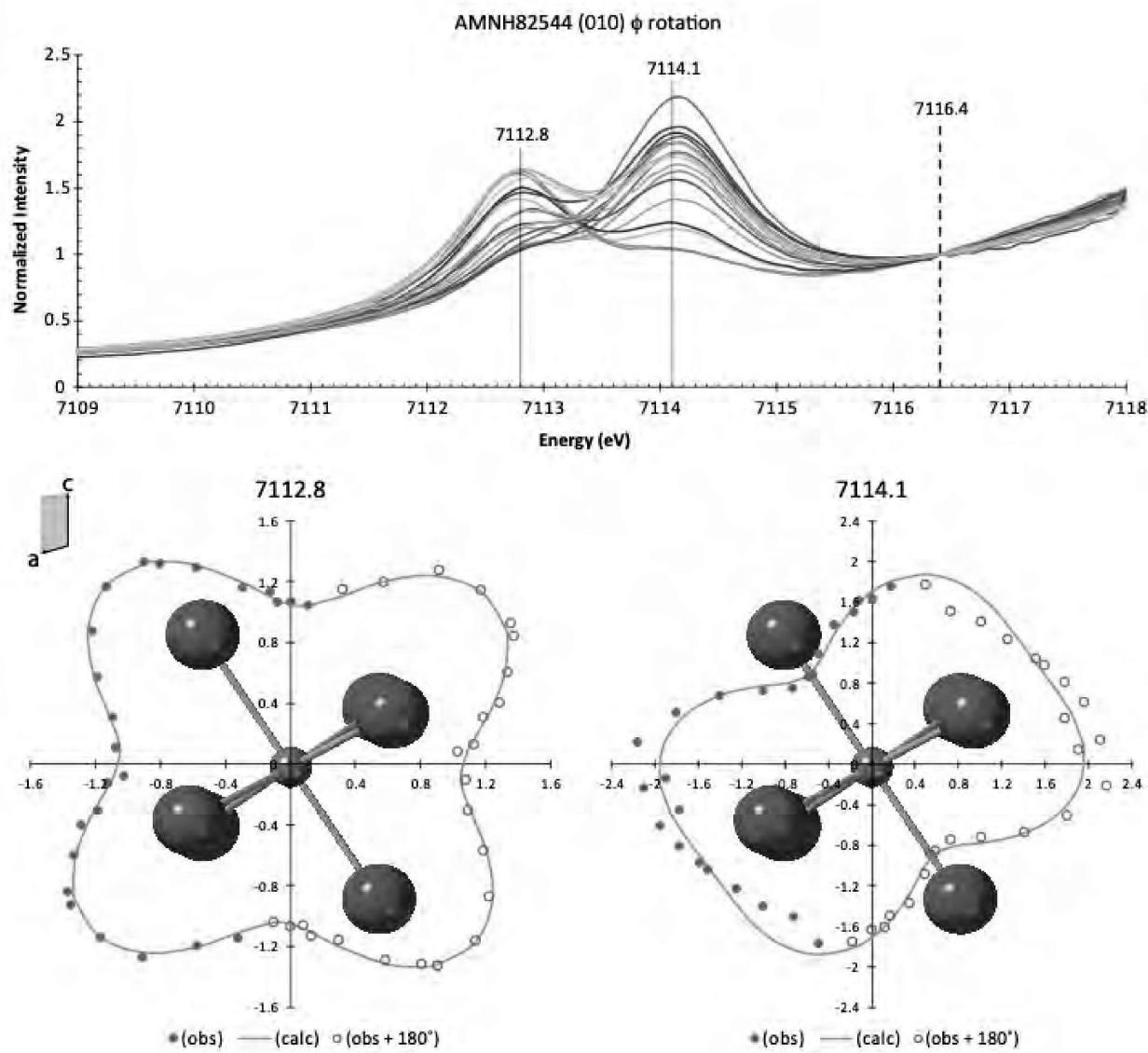
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625 **Figure 10)** X-ray absorption spectra (top) of a 1.0 $\text{Fe}^{3+}/\Sigma\text{Fe}$ aegirine analyzed at a selection of ϕ -axis angles with $\vec{E} // \phi // \mathbf{b}$ -axis. The resulting absorption magnitudes are plotted radially with
626 respect to \vec{k} orientation (bottom) at 7112.9 and 7114.2 eV. Absorption magnitudes are fit with
627 $\cos^2\phi$ for comparison. Axes in bottom row follow conventions used in Figure 4.
628



629

630 **Figure 11)** X-ray absorption spectra (top) of a 1.0 $\text{Fe}^{3+}/\Sigma\text{Fe}$ aegirine analyzed with \vec{E} and \vec{k}
631 oriented along various axes in (010). The crystal was mounted with the b-axis // ϕ -axis at $\theta = -$
632 90° as depicted in Figure 2 with spectra collected at various ϕ settings. Absorption magnitudes
633 are plotted radially with respect to \vec{E} orientation, and for each datapoint the orientation of \vec{k} is
634 90° away. Spectra are renormalized near the pre-edge peaks at 7116.4 eV to highlight the
635 anisotropy. The orientation of the crystallographic axes and the coordinating polyhedron of the
636 M1 site is depicted relative to the orientation of the absorption magnitudes. Axes in bottom row
637 follow conventions used in Figure 4.

638