

Comptonization by reconnection plasmoids in black hole coronae II: Electron-ion plasma

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ABSTRACT

We perform 2D particle-in-cell simulations of magnetic reconnection in electron-ion plasmas subject to strong Compton cooling and calculate the X-ray spectra produced by this process. The simulations are performed for trans-relativistic reconnection with magnetization $1 \leq \sigma \leq 3$ (defined as the ratio of magnetic tension to plasma rest-mass energy density), which is expected in the coronae of accretion discs around black holes. We find that magnetic dissipation proceeds with inefficient energy exchange between the heated ions and the Compton-cooled electrons. As a result, most electrons are kept at a low temperature in Compton equilibrium with radiation, and so thermal Comptonization cannot reach photon energies ~ 100 keV observed from accreting black holes. Nevertheless, magnetic reconnection efficiently generates ~ 100 keV photons because of mildly relativistic bulk motions of the plasmoid chain formed in the reconnection layer. Comptonization by the plasmoid motions dominates the radiative output and controls the peak of the radiation spectrum E_{pk} . We find $E_{\text{pk}} \sim 40$ keV for $\sigma = 1$ and $E_{\text{pk}} \sim 100$ keV for $\sigma = 3$. In addition to the X-ray peak around 100 keV, the simulations show a non-thermal MeV tail emitted by a non-thermal electron population generated near X-points of the reconnection layer. The results are consistent with the typical hard state of accreting black holes. In particular, we find that the spectrum of Cygnus X-1 is well explained by electron-ion reconnection with $\sigma \sim 3$.

Key words: acceleration of particles – black hole physics – magnetic reconnection – radiation mechanisms: non-thermal – radiative transfer – X-rays: binaries.

1 INTRODUCTION

Hard, non-thermal X-rays observed from black hole X-ray binaries (BHXBs) are traditionally attributed to thermal Comptonization of seed soft photons by a hot plasma ('corona') surrounding the black hole (BH), with typical inferred electron temperatures ~ 100 keV (Zdziarski & Gierliński 2004). X-ray spectral and temporal studies have shed light on how the geometry and location of the corona change depending on the phase of the outburst (Kara et al. 2019; Sridhar et al. 2020; Cao et al. 2022; Wang et al. 2021). Yet, the mechanism that energizes the corona against the strong inverse Compton (IC) losses is still a mystery. Recently, Beloborodov (2017) suggested that magnetic reconnection can power the Comptonization process through the bulk motions of plasmoids in the reconnection layer.¹ The plasmoids sustain relativistic speeds if the magnetic energy density $B^2/8\pi$ exceeds the plasma rest mass energy density ρc^2 , which corresponds to a magnetization parameter $\sigma \equiv B^2/4\pi \rho c^2 > 1$. The Comptonization model of Beloborodov (2017) was followed by full kinetic simulations of reconnection in e^\pm plasma with strong IC cooling (Werner, Philippov & Uzdensky 2019; Sironi & Beloborodov 2020, hereafter SB20; Sridhar et al. 2021, hereafter SSB21). The simulations (SB20, SSB21) confirmed that the pair

plasma trapped in plasmoids is efficiently cooled to a non-relativistic temperature while their bulk motions remain trans-relativistic, resembling a Maxwellian distribution with effective temperature $k_B T_{\text{bulk}} \sim 100$ keV. Furthermore, Monte Carlo simulations of X-ray spectra produced by the 'cold-chain Comptonization' approximately agreed with the observed hard state of BHXBs in particular Cygnus X-1 (Sridhar et al. 2021). Our previous numerical simulations (SB20, SSB21) focused on reconnection in strongly magnetized ($\sigma \gg 1$) e^\pm pair plasma. However, accretion disc coronae can also have ion-dominated regions with $\sigma \sim 1$ adjacent to the accretion flow (e.g. Galeev, Rosner & Vaiana 1979). Formation of disc coronae is a difficult problem studied with GRMHD simulations (e.g. Chatterjee et al. 2019; Jiang, Stone & Davis 2019; Ripperda, Bacchini & Philippov 2020; Nathaniel et al. 2022; Ripperda et al. 2022). It is not established which region dominates the observed hard X-ray emission. It is possible that magnetic reconnection in electron-ion plasma with moderate $\sigma \sim 1$ is the dominant source of hard X-rays.

This paper investigates this possibility using radiative kinetic simulations. Similar simulations of trans-relativistic reconnection in electron-ion plasmas were performed before only in the absence of radiative cooling (Melzani et al. 2014a, b; Rowan, Sironi & Narayan 2017; Ball, Sironi & Özel 2018, 2019; Werner et al. 2018; Rowan, Sironi & Narayan 2019; Kilian et al. 2020). We, for the first time, extend these studies to the radiative regime. In particular, we investigate the effect of IC losses on the particle energy distribution and evaluate the IC emission from the reconnection layer.

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¹See fig. 1 in Sridhar, Sironi & Beloborodov (2021) for a schematic illustration of the proposed 'cold-chain Comptonization' process.

Only electrons experience significant IC cooling. As a result, the reconnection layer can enter a two-temperature state with ions much hotter than the electrons. This depends on the efficiency of the electron-ion energy exchange. Exchange through Coulomb collisions is typically slow in the corona with $\sigma > 1$, however there may be collision-less mechanisms – involving e.g. ion velocity-space instabilities (Hasegawa 1969; Gary 1992; Sharma et al. 2006; Kunz, Schekochihin & Stone 2014; Riquelme, Quataert & Verscharen 2015; Sironi & Narayan 2015; Zhdankin, Uzdensky & Kunz 2021) – that could transfer the ion thermal energy to the colder electrons. This suggests a possibility for sustaining a high electron temperature T_e inside reconnection plasmoids, perhaps competitive with T_{bulk} of the plasmoid bulk motions. Then, thermal Comptonization could become important for hard X-ray production. Kinetic plasma simulations are the best way to find out, from first principles, the importance of T_e versus T_{bulk} .² The simulations will also show how the electron distribution in the reconnection layer depends on σ and what effect it has on the Comptonization spectrum.

The paper is organized as follows. In Section 2, we describe the numerical setup of our simulations. In Section 3, we present the implementation and parametrization of IC cooling, and the most important time-scales for our problem, in the context of BH coronae. In Section 4, we present our PIC results, emphasizing the dependence on magnetization and strength of IC cooling. The photon spectra derived from our PIC simulations using Monte Carlo radiative transfer calculations are presented in Section 5. We summarize our findings in Section 6.

2 PIC SIMULATION SETUP

We perform simulations of magnetic reconnection with the 3D electromagnetic particle-in-cell code TRISTAN-MP (Buneman 1993; Spitkovsky 2005); the code employs a Vay pusher (Vay 2008) for updating the particles' momenta. Overall, the simulation setup is similar to what we have employed in paper I of this series (SSB21) and in SB20. We none the less describe it here given the different composition of the plasma. We refer readers to Appendix A for the complete set of our numerical and physical input parameters.

Our simulations are performed on a 2D spatial domain – with Cartesian grid in the x – y plane – yet evolving all three components (x , y , z) of velocities and electromagnetic fields. We initialize a plasma composed of electrons (subscript ‘e’) and protons/ions (subscript ‘i’). The effect of the proton-to-electron mass ratio is examined in Appendix B for $m_i/m_e \simeq 7 - 1836$; our fiducial mass ratio is $m_i/m_e = 29$, which in the uncooled regime gives results in reasonable agreement with realistic mass ratio (see Appendix B). Electrons and ions have equal number densities, $n_{0e} = n_{0i}$, and can be described by a Maxwell–Jüttner distribution with dimension-less temperatures $\theta_e = k_B T_e / m_e c^2 \sim 10^{-4}$ and $\theta_i = k_B T_i / m_i c^2 = 10^{-4} (m_e / m_i)$, respectively, where we initialize electrons and ions with the same temperature $T_e = T_i$. The Debye length corresponding to these conditions is $\lambda_{\text{De}} = \sqrt{k_B T_e / 4\pi n_0 e^2} = 0.05$ cells. We demonstrate in Appendix C (on simulation convergence with spatial resolution) that this choice of upstream temperature does not influence our overall conclusions,

²In paper I (SSB21), we presented an experiment where only electrons were selectively cooled, with positrons remaining hot – mimicking a radiatively cooled electron-ion plasma. Our results showed that no energy is efficiently transferred from the hot positrons to the colder electrons, on time-scales shorter than the plasma advection time out of the reconnection layer.

by performing additional simulations with $\theta_e = 0.02$, or equivalently, $\lambda_{\text{De}} = 1$ cell.

For our case of cold plasma, we define the plasma magnetization of a given species σ_s ³ as:

$$\sigma_s = \frac{B_0^2}{4\pi n_{0s} m_s c^2} = \left(\frac{\omega_{\text{cs}}}{\omega_{\text{ps}}} \right)^2, \quad (1)$$

where B_0 is the asymptotic upstream magnetic field strength, $\omega_{\text{cs}} = eB_0/m_s c$ is the particle gyro-frequency, the plasma frequency ω_{ps} is defined as

$$\omega_{\text{ps}} = \sqrt{\frac{4\pi n_{0s} e^2}{m_s}}, \quad (2)$$

with the corresponding plasma skin depth given by c/ω_{ps} . The plasma we initialize is dominated in mass by the ions, therefore the overall plasma's magnetization parameter $\sigma \equiv B^2/4\pi \rho c^2$ is nearly equal to σ_i . We are interested in the regime of trans-relativistic reconnection, so we consider $\sigma_i = \sigma_e m_e / m_i = \{1, 2, 3\}$. The corresponding Alfvén speeds are $v_A/c = \sqrt{\sigma_i / (\sigma_i + 1)} = \{0.71, 0.81, 0.87\}$. The plasma- β parameter of the initialized plasma is given by $\beta_0 = \beta_i + \beta_e = 8\pi k(n_i T_i + n_e T_e) / B_0^2 \sim \theta_s / \sigma_s$. Our choices of the upstream plasma temperature and magnetization always renders the plasma $\beta_0 \ll 1$.

The fields undergoing reconnection are initialized along the $\pm \hat{x}$ direction (B_x), while the reconnected fields get oriented along the $\pm \hat{y}$ direction. This sets the plasma inflow and outflow directions to be along $\pm \hat{y}$ and $\pm \hat{x}$, respectively. We initialize the system in the so-called Harris equilibrium (Harris 1962), where the initial magnetic field profile is given by $B_x = -B_0 \tanh(2\pi y / \Delta_y)$, i.e. at $y = 0$ the field reverses its polarity over a thickness of Δ_y . Consistent with our previous work (SSB21), we also add a uniform guide field $B_g = 0.1 B_0$ along the z -axis, which does not get dissipated, and so does not add any free energy to the system.

The magnetic pressure outside the layer is balanced by particle pressure in the layer, by adding an additional population of hot particles with an overdensity of 3. We initiate reconnection by artificially cooling down the hot particles near the centre $[(x, y) = (0, 0)]$ at the initial time. We restrict the horizontal extent of the region where we trigger reconnection to a length $\Delta_x = 400 c / \omega_{\text{pe}}$. The reconnected field lines form an ‘X’-point at the centre of the domain, which eventually separates into two reconnection fronts that carry away the plasma along $\pm \hat{x}$ at \sim Alfvénic speeds. The initial thickness of the current sheet is chosen to be large enough ($\Delta_y \simeq 150 c / \omega_{\text{pe}}$) such that the tearing mode instability does not spontaneously grow before the two reconnection fronts have reached the boundaries of the domain.

We employ outflow boundary conditions along the x boundaries of the computational domain (Daughton, Scudder & Karimabadi 2006; Belyaev 2015; Cerutti et al. 2015). This ensures that the hot plasma initialized in the current sheet gets evacuated after $\sim L_x / v_A$, where L_x is the half-length of the box along x . Along the y direction, we employ two injectors that introduce fresh plasma and magnetic flux into the computational domain. These injectors move away from $y = 0$ at the speed of light, and the box dynamically expands when they reach its boundaries (see Sironi, Giannios & Petropoulou 2016, for details). With this setup, the reconnection dynamics evolves in a ‘quasi-steady state’ at time $t > L_x / v_A$ i.e. independent of the

³Throughout this paper, the subscript ‘s’ can denote either species – electrons or ions; the subscript ‘ e^{\pm} ’ is used to denote electrons and positrons in a pair plasma. E.g. when referring to results from paper I (SSB21), the magnetization $\sigma_{e^{\pm}}$ is normalized to the electron–positron mass density.

initial conditions (viz. temperature or overdensity of hot plasma in the sheet, Δ_x and Δ_y). We demonstrate this in Appendix D by showing how the reconnection rate (η_{rec} ; defined as the plasma's inflow velocity in units of the Alfvén speed) evolves with time. Akin to SSB21, we evolve the simulation up to $t_{\text{sim}} \sim 5L_x/v_A$ for all the considered magnetizations; this provides a sufficiently long time to assess the steady-state properties of the reconnection system.

We choose our computational domains with different sizes: $420 \leq L_x/(c/\omega_{pe}) \leq 6720$, or equivalently, $78 \leq L_x/(c/\omega_{pi}) \leq 1259$ (for $m_i/m_e = 29$). Large boxes are essential to retain the correct hierarchy of time and energy scales expected for BH coronae (see Section 3). We resolve the electron skin depth c/ω_{pe} with 5 grid lengths (δ) (i.e. resolution $\mathcal{R} = (c/\omega_{pe})/\delta = 5$). In Appendix C, we show for a representative case that our results are qualitatively the same with lower and higher resolutions ($\mathcal{R} = 2.5, 10$). The numerical speed of light (the Courant–Friedrichs–Lowy number) is set to 0.45 cells/time-step. We initialize the plasma with a density of $n_0 = 4$ particles per cell (2 per species), and improve particle noise in the electric current density with 32 passes of a ‘1-2-1’ low-pass digital filter (Birdsall & Langdon 1991) at each step of the PIC loop. We present a convergence test in Appendix E, where we compare our results with simulations having a higher initial particle number density, $n_0 = 64$, and a lower number of filtering passes (8).

3 INVERSE COMPTON COOLING

For each particle in our simulation with velocity \mathbf{v}_s ($= \beta_s c$) and energy $\gamma_s m_s c^2$, the IC cooling experienced by it – due to an isotropic bath of soft photons – is implemented in our code with a ‘drag force’ (Tamburini et al. 2010) given by

$$F_{\text{IC},s} = -\frac{4}{3}\sigma_{Ts}\gamma_s^2 U_{\text{rad}}\beta_s, \quad (3)$$

where $\sigma_{Ts} = 8\pi e^4/(3m_s^2 c^4)$ is the Thomson cross-section, $\gamma_s = (1 - \beta_s^2)^{-1/2}$ is the particle Lorentz factor, and U_{rad} is the radiation energy density. Since $\sigma_{Ti}/\sigma_{Te} = m_e^2/m_i^2$ and $\gamma_i/\gamma_e \sim \sigma_i/\sigma_e = m_e/m_i$, the ratio of the drag force experienced by ions and electrons is $F_{\text{IC},i}/F_{\text{IC},e} \simeq m_e^4/m_i^4 \ll 1$, even for our reduced mass ratio $m_i/m_e \sim 29$. Thus, we restrict the following discussion to electrons.

We parametrize the radiation energy density U_{rad} in the code by defining a critical Lorentz factor $\gamma_{\text{cr}} \equiv \sqrt{3e\eta_{\text{rec}}B_0/(4\sigma_{Te}U_{\text{rad}})}$, at which the Compton drag force experienced by the electrons is balanced by the force due to the electric field associated with magnetic reconnection, assuming a reconnection rate $\eta_{\text{rec}} \sim 0.1$ (Cassak, Liu & Shay 2017).⁴ We investigate the reconnection dynamics for the case of no IC cooling ($\gamma_{\text{cr}} = \infty$), and for increasing strengths of IC cooling: $20 \gtrsim \gamma_{\text{cr}} \gtrsim 7$. Given our simulations’ temporal resolution ($\Delta t = 0.09\omega_{pe}^{-1}$), the choice of $\gamma_{\text{cr}} > \sqrt{\sigma_e}$ ensures that the IC cooling time for any electron – with Lorentz factors even as high as $\gamma_e \sim \gamma_{\text{cr}}$ – is well-resolved (SB20, SSB21).

We refer readers to part I in this series of papers (SSB21) and SB20 for a detailed quantification of the plasma conditions in black hole coronae. For an e^\pm corona, we showed that the plasma magnetization is expected to be $\sigma_{e^\pm} \sim 400$. On the other hand, the coronae adjacent to the accretion disc can have moderately magnetized regions ($\sigma \sim 1$)

⁴The electric field associated with reconnection is given by $E_{\text{rec}} = \eta_{\text{rec}}(v_A/c)B_0$. When defining γ_{cr} , we take $E_{\text{rec}} \sim \eta_{\text{rec}}B_0$, which is a fair assumption for our case of trans-relativistic reconnection with $\sigma \sim 1$.

whose mass density is dominated by ions – as also seen in GRMHD simulations (Chatterjee et al. 2019; Jiang et al. 2019). It follows that $\sigma_e = \sigma_i(m_i/m_e) \gg 1$. On the other hand, the parametrization for the seed photon density U_{rad} , and so γ_{cr} , does not depend on the plasma composition, and is estimated to be $\gamma_{\text{cr}} \sim 10^4(M_{\text{BH}}/M_\odot)^{1/4}$, where M_{BH} is the mass of the black hole SSB21.

We showed in our earlier works (SB20, SSB21) that electrons accelerated at X-points typically attain Lorentz factors $\gamma_X \sim \sigma_e/8$,⁵ and that their IC cooling time-scale is much longer than the X-point acceleration time-scale. This sets the requirement of $\gamma_{\text{cr}} \gg \sigma_e/8$, which ensures that electrons accelerated at the X-points do not suffer significant IC cooling. On the other hand, the IC cooling time-scale is much shorter than the time-scale for plasma advection across the reconnection region, whose size, in BH coronae, is comparable to the gravitational radius of the black hole (Beloborodov 2017). The ratio of these two time-scales in our simulations can be cast as follows (SSB21):

$$\tau_{\text{cool}} \equiv \frac{\gamma_{\text{cr}}^2}{\eta_{\text{rec}}\sqrt{\sigma_e}} \frac{c/\omega_{pe}}{L_x} < 1. \quad (4)$$

Equation (4) is satisfied for large enough domains; we none the less explore both the strongly cooled ($\tau_{\text{cool}} < 1$) and weakly cooled ($\tau_{\text{cool}} > 1$) regimes. Values of $\tau_{\text{cool}} \ll 1$ ensure that electrons have enough time to cool down to non-relativistic temperatures before being advected out of the box. On the other hand, in the regime $\tau_{\text{cool}} \gg 1$, electrons exit the domain with a Lorentz factor $\gamma_e \sim \tau_{\text{cool}}$, and approach the asymptotic value $\gamma_e \rightarrow \sigma_e/8$ for $\tau_{\text{cool}} \gtrsim \sigma_e$. Throughout our study, we employ τ_{cool} to quantify the strength of radiative cooling experienced by the particles.

4 PIC SIMULATION RESULTS

In this section, we present the results from our PIC simulations of radiative reconnection, and discuss how the presence of ions in the plasma modifies our findings as compared to radiative reconnection in an e^\pm plasma (SB20, SSB21).

In Section 4.1, we present the general structure of the reconnection region for different values of plasma magnetization, exposed to the same level of radiative cooling (same τ_{cool}). In Section 4.2, we demonstrate how the particles’ internal and bulk motions are influenced by the plasma magnetization and the level of IC cooling. The resulting energy spectra of electrons – separated into their internal and bulk motions – are then presented in Section 4.3.

4.1 Characteristics of the reconnection region

In this section, we present the effect of different magnetizations ($1 < \sigma_i < 3$) on the structure of the radiatively cooled reconnection region, for a fixed $\tau_{\text{cool}} = 0.06$. As we show in Fig. 1, the reconnection rate exhibits a very weak dependence on the ion-to-electron mass ratio. On the other hand, η_{rec} increases from ~ 0.08 to ~ 0.12 as σ_i is increased from 1 to 3; this is consistent with MHD results of Ni et al. (2012) and PIC results of, e.g. Rowan et al. (2017) and Ball et al. (2018). For our fiducial mass ratio ($m_i/m_e = 29$), Fig. 1 also shows that reconnection proceeds with a rate that is nearly independent on the strength of radiative cooling; this conclusion holds both for

⁵This estimate assumes that half of the available magnetic energy is dissipated into particle energy (Sironi, Petropoulou & Giannios 2015), and that electrons and ions acquire the same amount of dissipated field energy.

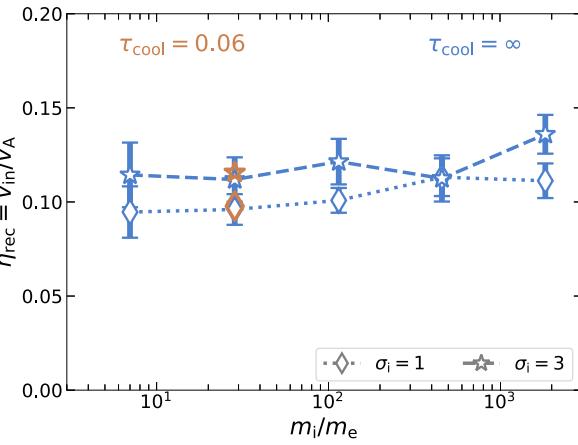


Figure 1. Reconnection rate η_{rec} , defined as the speed of the plasma inflow towards the reconnection region (v_{in}) normalized by the Alfvén speed (v_A). The dotted and dashed lines connecting the diamond and star markers, respectively, present the dependence of η_{rec} on m_i/m_e for $\sigma_i = 1$ and 3, respectively. The blue markers denote uncooled cases ($\tau_{\text{cool}} = \infty$), whereas the brown markers show the results of the strongest cooling case ($\tau_{\text{cool}} = 0.06$), for our fiducial $m_i/m_e = 29$. The inflow rate is spatially averaged over a rectangular slab located above the reconnection mid-plane (at $0.1 < x/L_x < 0.9$ and $0.05 < y/L_x < 0.15$, where $L_x/(c/\omega_{\text{pe}}) = 1680$), and is then averaged during the time interval $2 \lesssim T/(L_x/v_A) \lesssim 5$. The error bars denote the standard deviation.

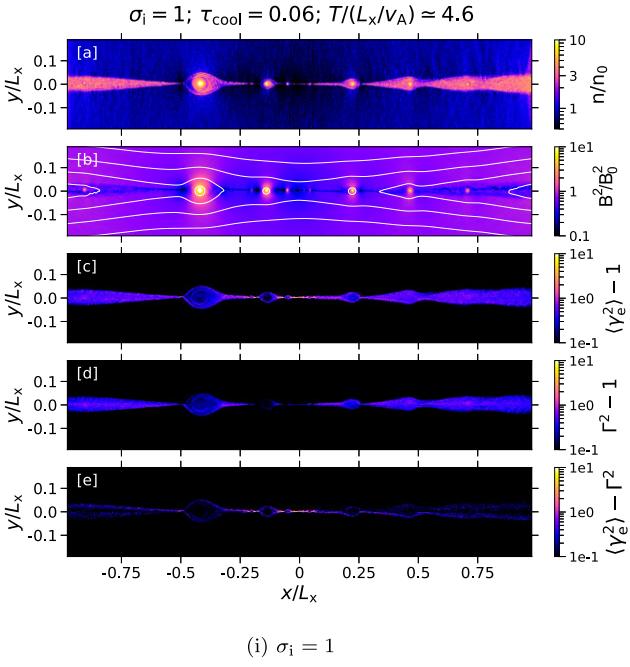
the electron-ion composition considered here, as well as for the pair plasma of our previous studies (SB20, SSB21). This can be understood from the fact that the reconnection rate is controlled by the electron inertial and thermal effects at X-points, and the electron

dynamics at X-points are not affected by cooling for our choice of $\gamma_{\text{cr}} > \sigma_{\text{e}}/8$.

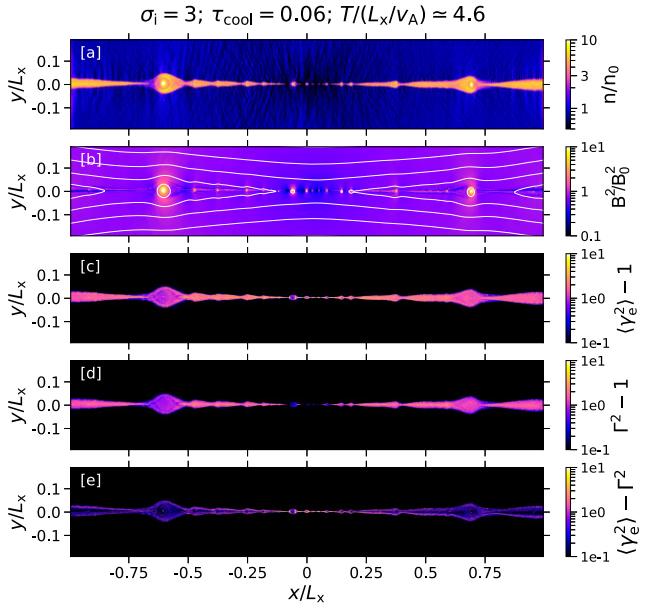
The 2D structure of strongly IC-cooled ($\tau_{\text{cool}} = 0.06$) reconnection layers for different magnetizations is presented in Fig. 2 ($\sigma_i = 1$ on the left, $\sigma_i = 3$ on the right). Regardless of the strength of IC cooling and the value of the magnetization, the reconnection region breaks into a hierarchical chain of coherent magnetic structures ('plasmoids') as a result of the tearing instability (Tajima & Shibata 1997; Loureiro, Schekochihin & Cowley 2007; Bhattacharjee et al. 2009; Uzdensky, Loureiro & Schekochihin 2010). The formed plasmoids occasionally merge with each other, leading to the formation of secondary reconnection layers at the merger site, transverse to the main layer.

The plasmoid density structure in trans-relativistic ($\sigma \sim 1$) reconnection (Fig. 2) shows some differences as compared to the ultrarelativistic ($\sigma \gg 1$) case of our earlier works (Sironi et al. 2016, SB20, SSB21). For high magnetizations, plasmoids were nearly circular, and markedly symmetric around their 'O'-point – the location of local maximum in the magnetic vector potential, corresponding to the plasmoid centre. In contrast, for $\sigma \sim 1$ they display an asymmetric 'teardrop' shape, with elongated tails. Older plasmoids (seen near the edges of the box) are more teardrop-like than newborn plasmoids (near the centre of the box). This is because large plasmoids grow by accreting smaller (so, faster) plasmoids from behind. Since for $\sigma \sim 1$ all plasmoids have comparable velocities (see below), the accreted plasmoids take some time to merge into the leading plasmoid, which gives the appearance of a long trailing tail.

The density structure in strongly cooled electron-ion simulations appears different from their pair-plasma counterparts (SSB21). Plasmoids formed in pair plasma were devoid of particles near their 'heads' (in the direction of their motion), which rather accumulate near the plasmoid 'tails'. This was caused by Compton drag acting



(i) $\sigma_i = 1$



(ii) $\sigma_i = 3$

Figure 2. Snapshot of the reconnection region at time $T \simeq 4.6 L_x/v_A$ for two magnetization models: $\sigma_i = 1$ (left-hand panel) and $\sigma_i = 3$ (right-hand panel), with otherwise the same level of cooling ($\tau_{\text{cool}} = 0.06$) and mass ratio ($m_i/m_e = 29$; see Appendix A for other runs). We only show the region $|y| \lesssim 0.2 L_x$ where reconnection occurs, where $L_x/(c/\omega_{\text{pe}}) = 1680$ and 6720 for the $\sigma_i = 1$ and 3 models, respectively. (a) Particle number density n in units of the initialized (upstream) number density n_0 . (b) B^2/B_0^2 , i.e. the magnetic energy density normalized to its upstream (initialized) value. The overplotted white contours are magnetic field lines. (c) Local average $\langle \gamma_e^2 \beta_e^2 \rangle = \langle \gamma_e^2 \rangle - 1$, which is proportional to the IC power per electron (the local average is calculated by averaging over patches of 5×5 cells). (d) $\Gamma^2 - 1$, where Γ is the bulk Lorentz factor defined in the text. (e) $\langle \gamma_e^2 \rangle - \Gamma^2$, which represents internal electron motions.

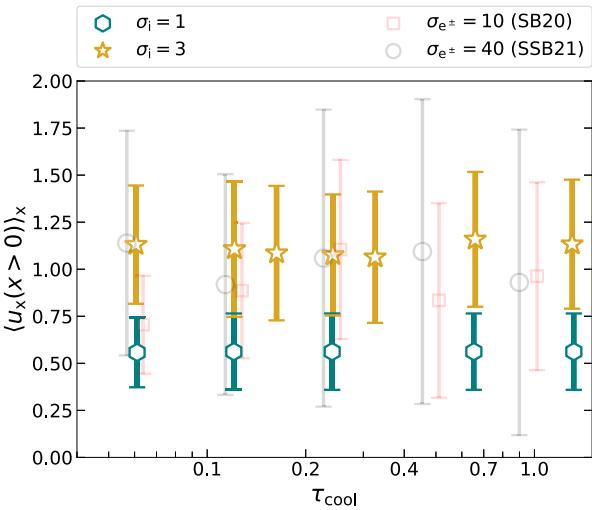


Figure 3. Bulk outflow motions in the reconnection region as a function of τ_{cool} and σ_i . The green hexagons and brown stars indicate the mean (density-weighted) bulk 4-velocity u_x for $\sigma_i = 1$ and 3, respectively, and the error bars indicate its standard deviation. The red squares and black circles denote the same quantity for an e^\pm plasma with $\sigma_{e^\pm} = 10$ (SB20) and $\sigma_{e^\pm} = 40$ (SSB21), respectively. The measurements were performed along one half of the reconnection region ($x > 0$) and the mean and standard deviation are computed during the time interval $2 \lesssim T/(L_x/v_A) \lesssim 5$.

on the electron–positron pairs. Ions, on the other hand, are not appreciably affected by Compton drag. Electrons are electrostatically coupled to ions, and so they inherit the ions’ larger inertia – ions have a larger rest mass, and they do not lose the energy gained from reconnection. Thus, in electron-ion simulations the drag effect on the plasma inside plasmoids is weaker than in otherwise equivalent e^\pm simulations.⁶

A 2D map of the magnetic energy density (in units of its initialized value) is presented in panels (b) of Fig. 2. The peak values of B^2/B_0^2 – seen at the core of plasmoids – are smaller for $\sigma_i = 1$, as compared to $\sigma_i = 3$. The magnetic field in the plasmoid cores is compressed by a factor of $B/B_0 \sim 14$ for $\sigma_i = 3$, whereas $B/B_0 \sim 8$ for $\sigma_i = 1$.

The total IC power per electron is shown in panels (c) of Fig. 2. This is represented by the quantity $\langle \gamma_e^2 \beta_e^2 \rangle = \langle \gamma_e^2 \rangle - 1$, where the average for each cell is performed in a local patch of 5×5 cells. As expected, the total IC power is larger for $\sigma_i = 3$ than for $\sigma_i = 1$, just as a consequence of the greater energy per particle. For both $\sigma_i = 1$ and 3, the IC power is fairly uniformly distributed over the reconnected plasma, with a slight excess seen around the primary X-point near the centre of the layer, in the thin layers between merging plasmoids, and at the heads and tails of plasmoids. This is similar to what was seen in radiatively cooled relativistic reconnection of an e^\pm plasma (SB20, SSB21).

The bulk motion’s contribution to the total IC power is shown in panel (d) of Fig. 2. This is represented by $\Gamma^2 - 1$, where $\Gamma = (1 - \beta^2)^{-1/2}$ is the bulk Lorentz factor of the plasma, and β is the average particle fluid velocity – weighted with the mass densities of both electrons and ions and averaged, for each cell, in the local patch of neighbouring 5×5 cells. In the frame moving with velocity β , the plasma stress–energy tensor has a vanishing energy flux, and we define this to be the plasma comoving frame (Rowan et al. 2019). We

⁶Similar results were observed in the hybrid experiment with cooled electrons and uncooled positrons that we showed in SSB21.

find that the bulk motions’ contribution to the IC power is stronger for $\sigma_i = 3$ than for $\sigma_i = 1$. This is expected, since faster bulk motions are associated with higher values of the Alfvén speed $v_A \propto \sqrt{\sigma/(1 + \sigma)}$ (more on this in Section 4.2.1 and Fig. 3).

The similarity between panels (c) and (d) in Fig. 2 for both $\sigma_i = 1$ and 3 suggests that most of the IC power comes from bulk motions. This is further supported by panels (e) (the difference between panels (c) and (d)) where we show the contribution of the electrons’ internal motion (represented by $\langle \gamma_e^2 \rangle - \Gamma^2$) to the total IC power. The figure shows that the IC power in internal motions is larger in $\sigma_i = 3$ than in $\sigma_i = 1$ simulations; this is expected since $\langle \gamma_e \rangle \propto \sigma_e \propto \sigma_i$, for the freshly accelerated electrons. While most of the electrons in the reconnection region are cooled down to non-relativistic temperatures, narrow slivers of hot electrons are seen at X-points, where the energization time-scale is faster than the IC cooling time-scale (SB20, SSB21). The outskirts of plasmoids also appear hot because the electrons accelerated at X-points of the main layer and at plasmoid merger sites enter into neighbouring plasmoids along their outer boundaries. None the less, the internal motions’ contribution to the IC power is highly subdominant relative to the one of bulk motions, in most of the layer. This conclusion, which we had derived for pair plasmas (SB20, SSB21), also holds in electron-ion plasmas.

4.2 Bulk and internal motions

In this section, we explore in more detail the effects of plasma magnetization and IC cooling strength on the bulk and internal motions of the reconnected plasma. We define the reconnection region as the area around the reconnection mid-plane $y = 0$ that contains a mixture of particles coming from above and below it, with both populations contributing at least 1 per cent to the mixture (Rowan et al. 2017). In the following sections, our discussion of the particle motions involve plasmas with different compositions (i.e. electron-ion versus e^\pm pair). Therefore, the magnetization experienced by electrons should be cast as $\sigma_e = \sigma_i m_i/m_e$ for the electron-ion case (where the overall magnetization $\sigma \sim \sigma_i$) and as $\sigma_e = 2\sigma$ for the e^\pm case (where $\sigma = \sigma_{e^\pm}$). We demonstrate below that the electron bulk motions are primarily determined by the overall σ , whereas their internal motions are governed by σ_e .

4.2.1 Bulk component

To quantify the bulk motions along the outflow direction, we calculate the bulk 4-velocity $u_x = \Gamma \beta_x$. To ensure sufficient statistics, we calculate u_x only in those cells with at least four particles, and then compute the density-weighted average in space (across the right half of the box with $x/L_x > 0$) and time (in the quasi-steady interval: $2 \lesssim T/(L_x/v_A) \lesssim 5$). This quantity, $\langle u_x(x > 0) \rangle_x$, is presented in Fig. 3 for different τ_{cool} and σ_i . The error bars illustrate the stochasticity of the reconnection layer, i.e. the dispersion away from the mean bulk motion. We quantify this by the density-weighted spatiotemporal average of the standard deviation of u_x (SSB21). Such stochastic motions can be crucial in determining the Comptonized spectrum. They can arise due to various reasons including the different speeds of plasmoids with different sizes, and the fact that a few small plasmoids can move against the mean flow, being pulled back by a large plasmoid behind them.

Fig. 3 demonstrates that for a given σ the mean bulk outflow velocity $\langle u_x \rangle$, barely depends upon τ_{cool} – akin to strongly cooled e^\pm plasmas with $\sigma = \sigma_{e^\pm} > 10$ (SSB21). For a given τ_{cool} , $\langle u_x \rangle$ varies between ~ 0.55 for $\sigma \simeq \sigma_i = 1$ and ~ 1.1 for $\sigma \simeq \sigma_i = 3$. On the

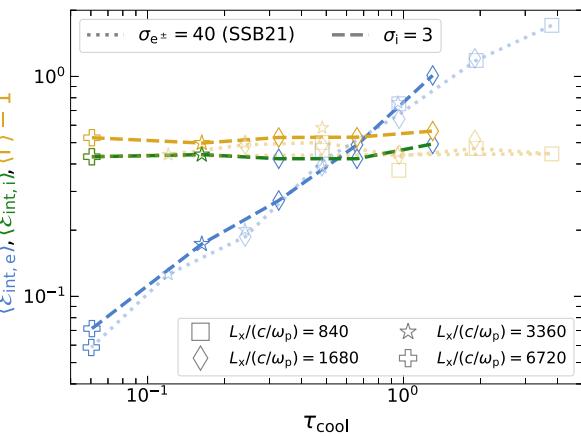


Figure 4. Average particle energy (in units of m_sc^2) separated into two components: internal (blue for electrons and green for ions) and bulk (brown), plotted against τ_{cool} . The dashed curves refer to $\sigma_i = 3$, and dotted lines to $\sigma_{e^\pm} = 40$ (SSB21). For a given magnetization and τ_{cool} , different symbols correspond to different sizes of the simulation domain (see legend), which equivalently correspond to different γ_{cr} . Where more than one simulation is available with the same σ and τ_{cool} (Table A1), the curve passes through their mean value. The measurements were performed using density-weighted averaging over the reconnection region and averaging over the quasi-steady-state time interval $2 \lesssim T/(L_x/v_A) \lesssim 5$.

other hand, $\langle u_x \rangle$ is seen to be similar between electron-ion models with $\sigma = \sigma_i = 3$, and pair plasma simulations with $\sigma = \sigma_{e^\pm} = 10$ or 40. This shows that $\langle u_x \rangle$ is σ -independent, and also independent of the plasma composition, for magnetizations $\sigma \gtrsim 3$.

A systematic increase in the stochasticity of the bulk outflow motions with increasing σ was identified in SSB21 for e^\pm plasmas. We broadly observe a similar effect here for electron-ion plasma. Considering the overall range of magnetizations, while the mean values $\langle u_x \rangle$ for $\sigma_i = 3$ and $\sigma_{e^\pm} = 40$ are nearly the same, the dispersion in the bulk outflow motions monotonically increases with magnetization, from $\sigma_i = 1$ up to $\sigma_{e^\pm} = 40$. This effect can be explained as follows. A higher dispersion is obtained for larger deviations of u_x from the mean value. The largest u_x is typically attained by the smallest plasmoids, and is given by the Alfvénic limit of $u_{x,\text{max}} \sim \sqrt{\sigma}$ (SB20, SSB21). We find that $u_{x,\text{max}}/\langle u_x \rangle \sim 1.8$ for $\sigma = \sigma_i = 1$, whereas it is ~ 5.7 for $\sigma = \sigma_{e^\pm} = 40$. This result suggests that vigorous collisions of plasmoids (i.e. colliding with appreciably different speeds) are relatively less likely to occur in the low- σ regime considered here, as compared to the higher magnetization of our earlier works (SB20, SSB21). As an additional consequence, the secondary transverse reconnection layers (along y) formed between colliding plasmoids are rarer at lower σ . Therefore, the contribution of y -directed bulk motions to the Comptonized emission gets smaller with lower σ .

4.2.2 Internal component

In this section, we set out to investigate how the energy in the bulk motion compares against the internal energy (heat) of electrons and ions, for a wide range of IC cooling strengths ($0.06 \lesssim \tau_{\text{cool}} \lesssim 3$). We specifically choose to compare the $\sigma = \sigma_i = 3$ and $\sigma = \sigma_{e^\pm} = 40$ models because they both correspond to the same electron magnetization $\sigma_e \sim 80$ (for our choice of $m_i/m_e = 29$ in electron-ion simulations). Fig. 4 shows the mean bulk energy per particle ($\langle \Gamma \rangle - 1$) and the mean internal energy per particle

($\varepsilon_{\text{int},e}$ for electrons, $\varepsilon_{\text{int},i}$ for ions, normalized to their respective rest mass energies).⁷ The mean values are obtained by first performing a density-weighted average of the respective quantity over the reconnection region, and then a time-average over the interval $2 \lesssim T/(L_x/v_A) \lesssim 5$.

Fig. 4 demonstrates that the mean bulk energy ($\langle \Gamma \rangle - 1 \sim 0.5$) is independent of τ_{cool} and σ for sufficiently relativistic plasmas, $\sigma \gtrsim 3$ (see also Fig. 3). As far as the internal energy is concerned, our results reveal a remarkable similarity in $\langle \varepsilon_{\text{int},e} \rangle$ between electron-positron models with $\sigma = \sigma_{e^\pm} = 40$ and electron-ion cases with $\sigma_i = 3$, across a wide range of τ_{cool} . This is because the electron internal motions are determined by the electron magnetization σ_e , which controls the mean energy available per electron, and is similar between the $\sigma = \sigma_{e^\pm} = 40$ ($\sigma_e = 80$) and $\sigma = \sigma_i = 3$ ($\sigma_e = 85.5$) models, for $m_i/m_e = 29$. We see that $\langle \varepsilon_{\text{int},e} \rangle > \langle \Gamma \rangle - 1$ in the ‘hot regime’ ($\tau_{\text{cool}} \gtrsim 0.5$), whereas in the ‘cold regime’ ($\tau_{\text{cool}} \ll 1$) electrons are cooled down to non-relativistic temperatures, so their total energy is dominated by bulk motions.

In our electron-ion plasma simulations with $\sigma = \sigma_i = 3$, the ion internal energy $\langle \varepsilon_{\text{int},i} \rangle$ stays at trans-relativistic values ~ 0.4 regardless of τ_{cool} . The fact that $\langle \varepsilon_{\text{int},i} \rangle$ does not depend on τ_{cool} allows one to conclude that energy is not transferred from the ions to the electrons, even when electrons are strongly cooled. In general, the electrons and ions are thermally decoupled if both collisional (Coulomb) and collision-less couplings are inefficient. Coulomb coupling is expected to be inefficient in the coronal plasma with $\sigma > 1$ (Appendix F; there, we also show that our simulations are well within the collision-less regime). Collision-less channels for ion-to-electron energy transfer could in principle occur, however we find they are not activated. As we describe in Appendix G, we have directly verified that the layer is not prone to collision-less ion velocity-space instabilities (e.g. ion-cyclotron, mirror, and firehose, see Sironi et al. 2015).

Also note in Fig. 4 that the value and trend of $\langle \varepsilon_{\text{int},i} \rangle$ as a function of τ_{cool} is identical to that of $\langle \Gamma \rangle - 1$. This is generally expected in mildly relativistic reconnection ($\sigma \sim 1$): here, not only does the internal energy of ions scale with σ_i , so also does their bulk energy, $\langle \Gamma \rangle - 1 \sim \langle \beta^2 \rangle / 2 \sim \sigma \sim \sigma_i$ (neglecting factors of the order of unity).

4.3 Particle energy spectra

Here, we present the electron and ion energy spectra for particles belonging to the reconnection region. The spectra are averaged in time over $2 \lesssim T/(L_x/c) \lesssim 5$ – representative of a quasi-steady state. Since $\tau_{\text{cool}} \propto \gamma_{\text{cr}}^2 / L_x$, we can in principle modify either γ_{cr} or the size of the computational domain L_x (or both), in order to vary τ_{cool} . For a given σ , we choose to fix γ_{cr} to a value such that $\gamma_{\text{cr}} > \sigma_e/8$ (see Section 3), and only modify L_x . The spectra are then normalized by L_x^2 for a fair comparison between simulations with different box sizes.

Fig. 5 presents the total energy spectra of electrons for different models: the magnetization increases from $\sigma_i = 1$ to 3 from top to bottom row, and the strength of IC cooling increases from $\tau_{\text{cool}} = 0.24$ to 0.06 from left to right-hand column. In addition to the total energy spectrum, each panel also shows the two chief components of the total spectrum – the bulk motion, and the high-energy tail dominated by the internal motion. For completeness, we also compare in Fig. 6 the spectra of electrons and ions, between uncooled ($\tau_{\text{cool}} = \infty$) and

⁷We refer readers to appendix C in our Paper I (SSB21) for a detailed discussion of how the internal energies are calculated.

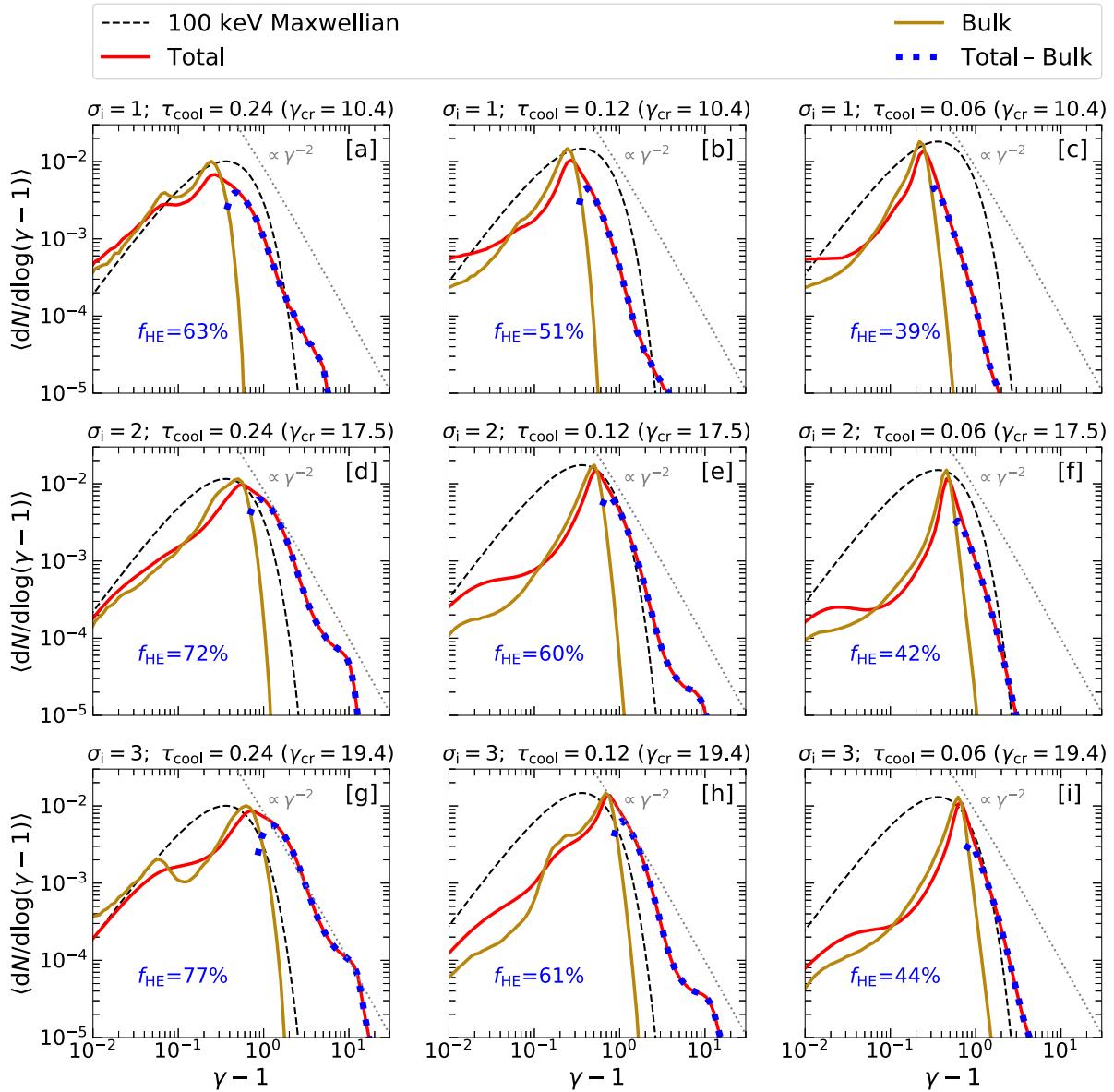


Figure 5. Electron energy spectra extracted from the reconnection region and averaged over $2 \leq T/(L_x/v_A) \leq 5$. Nine simulations are shown with magnetizations $\sigma_i = 1, 2, 3$, and different values of τ_{cool} and domain size L_x . The plasma magnetization increases from top to bottom, and the effective cooling strength (parametrized by τ_{cool}) increases from left to right (achieved by increasing L_x at fixed $\gamma_{cr} > \sigma_e/8 = \sigma_i(m_i/8m_e)$). The spectra are normalized by L_x^2 for proper comparison of models with different L_x . Each panel shows the total energy spectrum (red; $\gamma = \gamma_e$), the bulk motion spectrum (golden-brown; $\gamma = \Gamma$), and their difference (dotted blue), i.e. the part not accounted for by bulk motions; the fractional IC power contributed by this component is denoted in each panel as f_{HE} . For comparison, we also plot a Maxwellian distribution with a temperature of 100 keV (dashed black), such that the normalization of its peak matches the peak of the bulk energy spectrum. The dotted grey lines indicate the -2 slope that corresponds to equal IC power per decade in Lorentz factor.

cooled cases ($\tau_{cool} = 0.24$) for $\sigma_i = 3$. Note that the cooled model is the same as the one in Fig. 5(g).

In the absence of IC cooling, the total energy spectrum (left-hand panel of Fig. 6) of electrons in a $\sigma_i = 3$ ($\sigma_e \sim 85$) electron-ion plasma peaks at $\gamma_e - 1 \sim 10$, which resembles that of the $\sigma_{e^\pm} = 40$ ($\sigma_e = 80$) model in e^\pm plasma (SSB21). This is because the mean Lorentz factor of the electrons energized by reconnection is proportional to σ_e , and in the absence of IC cooling, electrons retain the energy they acquired from field dissipation. On the other hand, in the presence of significant IC cooling ($\tau_{cool} = 0.24$), the peak in the electron total spectrum shifts to trans-relativistic energies, $\gamma_e - 1 \sim 0.7$ for the

$\sigma_i = 3$ model. By comparison with right-hand panel of Fig. 6, we conclude that in this regime the electron energy is controlled by bulk motions. In contrast, the total energy spectra of ions are insensitive to the strength of IC cooling, and peak at $\gamma_i - 1 \sim 2$ for $\sigma_i = 3$.

Fig. 5 shows that, in the strong cooling regime ($0.24 > \tau_{cool} > 0.06$), the bulk component of the spectra peaks stably at trans-relativistic speeds, with a moderate increase with magnetization: $\Gamma - 1 \sim 0.2, 0.4$, and 0.7 , for $\sigma_i = 1, 2$, and 3 , respectively. These are the energies where the total energy spectra peak as well, indicating that in the regime of strong cooling the electron energy is dominated by the bulk motion (see also Section 4.2 and Fig. 4). This conclusion,

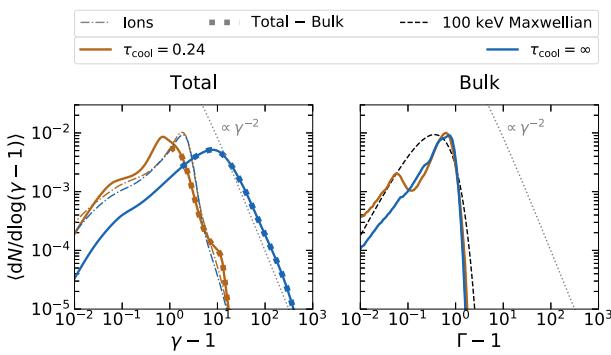


Figure 6. Total (left-hand panel) and bulk (right-hand panel) energy spectra for a model with $\sigma_i = 3$ and $m_i/m_e = 29$. In both panels, the blue curves denote the uncooled simulations ($\tau_{\text{cool}} = \infty$), whereas the brown curves denote the cooled cases ($\tau_{\text{cool}} \simeq 0.24$; same case as Fig. 5(g)). The solid curves represent electron spectra whereas the dash-dotted curves denote the ion spectra. For comparison, we also plot a Maxwellian distribution with a temperature of 100 keV (dashed black; right-hand panel) normalized so that its peak matches the peak of the bulk energy spectrum. The dotted grey lines indicate the -2 slope that corresponds to equal IC power per decade in Lorentz factor. The spectra are extracted from the reconnection region of a simulation with size $L_x/(c/\omega_{pe}) = 1680$, and time-averaged in the interval $2 \lesssim T/(L_x/v_A) \lesssim 5$.

which is especially clear for models with $\tau_{\text{cool}} = 0.06$, is in agreement with our earlier results for e^\pm plasma (SB20, SSB21).

For all the models presented in Fig. 5, we also plot a Maxwell–Jüttner distribution with $k_B T_e = 100$ keV. We showed in our earlier works (SB20, SSB21) that the spectrum of bulk motions in IC-cooled $\sigma \gg 1$ pair plasmas resembles a thermal distribution with $k_B T_e = 100$ keV. The bulk motion spectra in our electron-ion plasmas – for $1 \lesssim \sigma_i \lesssim 2$ – also have peak energies comparable to the same Maxwellian. Yet, the bulk spectra for our electron-ion cases are narrower than the Maxwellian, whereas they had comparable widths in our earlier electron–positron studies (SSB21). This can be understood from the level of stochasticity in the plasma outflow. In fact, the reconnection region is more disordered – with plasmoids moving at a wide range of speeds – for larger σ (see also Fig. 3). Such stochastic motions will manifest as a broader energy spectrum – with a wider peak – for higher magnetizations.

The higher energy tail of the spectra (i.e. blue dotted curves in Fig. 5), cannot be accounted for by the bulk motions alone, and is instead dominated by the internal motions. As shown in Fig. 2, the electrons belonging to this component are produced at interplasmoid regions (near X-points) in the main layer or at the interface of merging plasmoids (we refer to SB20 and SSB21 for more details). These electrons do radiate a considerable fraction (f_{HE}) of the total IC power, which is quoted in each panel of Fig. 5. For our considered models, f_{HE} ranges from 39 per cent (for $\sigma_i = 1$, $\tau_{\text{cool}} = 0.06$) to 77 per cent (for $\sigma_i = 3$, $\tau_{\text{cool}} = 0.24$). For a given τ_{cool} , f_{HE} increases by ~ 9 per cent from $\sigma_i = 1$ to 3 and, for a given σ_i , f_{HE} decreases by ~ 28 per cent from $\tau_{\text{cool}} = 0.24$ to 0.06. We also find that, for a given τ_{cool} , f_{HE} is generally larger in electron-ion simulations (for $\sigma_i \geq 1$) than it is in pair plasma simulations (for $\sigma_{e^\pm} \gg 1$; SSB21). This is because the high energy component of the spectrum that determines f_{HE} is defined as the difference between the total spectrum and its bulk component; the narrower shape of the bulk spectrum in our electron-ion simulations – compared to our pair plasma cases – then enhances the impact of the high energy component, thus leading to a larger f_{HE} .

The high energy component displays a ‘knee’ at $\gamma_e - 1 \sim 10$. This is populated predominantly by electrons accelerated at strong X-points near the centre of the reconnection layer. The extent over which such X-points appear is $\sim 500 c/\omega_{pe}$ regardless of L_x , which implies that the prominence of the high-energy knee decreases with increasing box size, since the fractional importance of the central X-points drops. This can be seen from all rows of Fig. 5 where the simulation box size increases from left to right. Even larger simulations will be needed to assess whether the normalization of the high-energy knee eventually settles to a fixed (i.e. box-independent) fraction of the overall particle count, or whether it keeps dropping as $\propto L_x^{-1}$.

5 MONTE CARLO RADIATIVE TRANSFER CALCULATIONS

The X-ray emission expected from the reconnection layer is calculated by performing Monte Carlo simulations of radiative transfer, using the code CompPair (Beloborodov 2021; Sridhar et al. 2021). In the Monte Carlo simulation, we inject soft seed photons sampled from a Planck distribution of temperature $k_B T_s = 10^{-3} m_e c^2$ into the mid-plane of the reconnection layer. The photons are then followed in time, as they scatter across the reconnection region, thereby producing a Comptonized, hard X-ray spectrum.

We divide the region $|x| < L_x$, $|y| < H = L_x/3$ into 60×20 patches, and for each photon scattering event, the particle momentum is drawn from the local distribution function in the patch. The transfer simulation is then evolved in time (between $T/(L_x/v_A) = 2.5$ and $T/(L_x/v_A) = 5.5$), with updating the particle distribution function every $0.5L_x/v_A$. The overall normalization of the plasma density is parametrized using the Thomson optical depth $\tau_T = H\sigma_T n_0$. We adjust the optical depth across the reconnection layer to obtain a Compton amplification factor⁸ $A \approx 10$, which gives the Comptonized spectrum with a photon index of $\Gamma \sim 1.5$ (defined as $dN/dE \propto E^{-\Gamma}$, where N is the number of photons with energy E) typical for the hard state spectra of accreting black holes. In analogy to the PIC simulation, we employ outflow boundary conditions for the Monte Carlo calculation (see Appendix H for different choices of boundary conditions).

Fig. 7 shows the spectrum of radiation escaping from the reconnection region for two models, with $\sigma_i = 1$ (dotted) and $\sigma_i = 3$ (dashed), adopting the same $\tau_{\text{cool}} = 0.06$. The emitted spectrum varies with time as reconnection proceeds, and Fig. 7 shows the emission averaged over the time interval $2.5 \lesssim T/(L_x/v_A) \lesssim 5.5$. We observe that the spectrum peaks around 40 keV for $\sigma_i = 1$ and 100 keV for $\sigma_i = 3$. This shift is primarily caused by the increase in plasmoid speeds at higher σ_i , see Fig. 3. The model with $\sigma_i = 3$ (dashed) is remarkably close to the typical hard-state of Cygnus X-1 observed in a broadband of 1–1000 keV. For comparison, we overplot in Fig. 7 the data available from BeppoSAX and CGRO/OSSE. The deviation of the data from the model at low photon energies ($\lesssim 1$ keV) is expected from interstellar absorption. The observed excess at higher energies ($\gtrsim 1$ MeV) is also well reproduced by our $\sigma_i = 3$ model. However, we caution that the particles responsible for this high-energy component belong to the high-energy knee in Fig. 5, whose prominence may become vanishingly small in the asymptotic (realistic) limit of very large domains. In this case, the high-energy photons at $\gtrsim 1$ MeV may be due to coronal regions with $\sigma_i > 3$.

⁸The factor A is the ratio of the average energy of escaping photons to the average energy of injected soft photons.

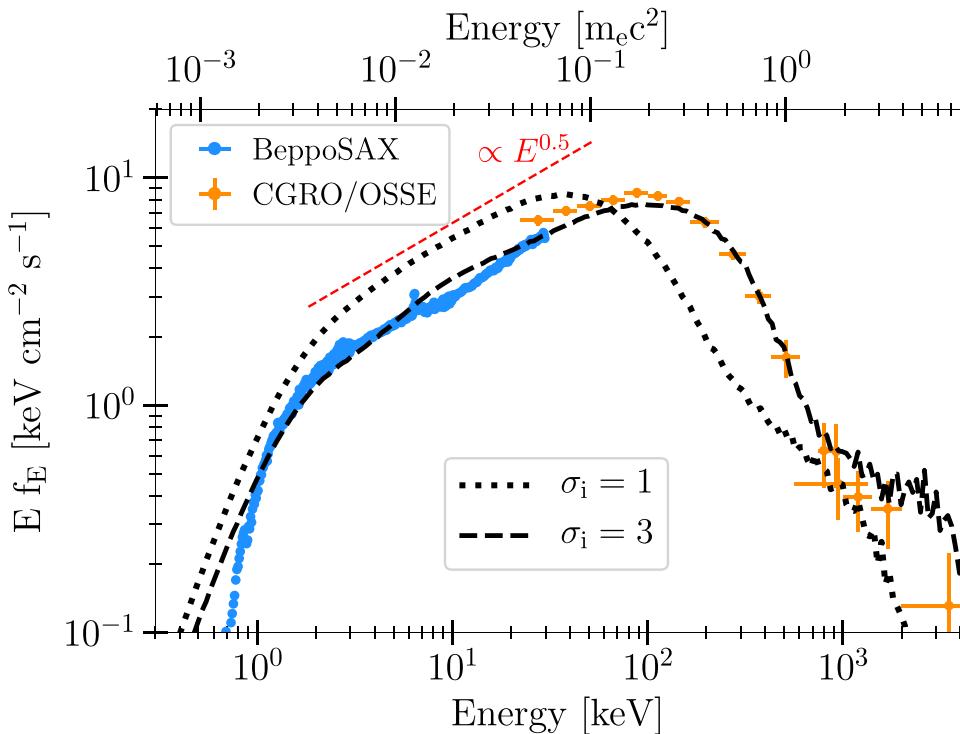


Figure 7. X-ray/γ-ray spectrum of Cygnus X-1 during its hard state, $E_F E = E^2 N(E)$. The 0.7–25 keV data (blue) are from *BeppoSAX* (Di Salvo et al. 2001; Frontera et al. 2001), and the 25–3500 keV data (orange) are from *CGRO/OSSE* (McConnell et al. 2002; see Zdziarski et al. 2017 for the spectrum in an extended range). The black dotted and dashed curves show the spectra formed by Comptonization in the reconnection layer in the models with $\sigma_i = 1$ (dotted) and $\sigma_i = 3$ (dashed), with the same strength of radiative cooling losses ($\tau_{\text{cool}} = 0.06$) and Compton amplification factor ($A = 10$). The dashed red line indicates the power-law $N(E) \propto E^{-1.5}$. All the data are normalized with respect to *OSSE*.

6 SUMMARY

The main goal of this series of papers is to explore the mechanism that gives rise to the observed hard X-ray spectra of accreting black holes. In the previous papers (SB20, SSB21), we performed 2D and 3D PIC simulations of relativistic magnetic reconnection in e^\pm plasmas subject to strong IC cooling – as appropriate to the most magnetically dominated regions of black hole coronae closer to the jet – and found that thermal Comptonization of soft seed photons by hot electrons is an unfeasible mechanism. In fact, due to the strong IC losses, electrons get cooled down to non-relativistic temperatures. None the less, we demonstrated that the hard X-ray spectra can be produced via Comptonization by the bulk motions of the Compton-cooled plasmoid chain (Beloborodov 2017). In this paper II, we have performed the first simulations of trans-relativistic magnetic reconnection ($\sigma \sim 1$) in electron-ion plasma subject to the effects of IC cooling. This is a regime that can be most relevant to the moderately magnetized regions of coronae adjacent to the accretion disc. Our main results are as follows.

(i) Regardless of the strength of IC cooling (τ_{cool}) or magnetization (σ), the reconnection layer breaks into a hierarchical chain of plasmoids. We also demonstrate that the rate at which reconnection proceeds is independent of the strength of IC cooling, and nearly independent of the ion-to-electron mass ratio, m_i/m_e .

(ii) The bulk motions of the plasmoid chain dominate the total IC power in the strong cooling regime. The mean energy in bulk motions is independent of the strength of IC cooling. On the other hand, the mean 4-velocity of bulk motions increases by a factor of two between $\sigma_i = 1$ and 3, before saturating at a value that is consistent with our

earlier results for larger magnetizations $\sigma \geq 10$ (SSB21). This shows that the typical speed of bulk motions becomes σ -independent only for $\sigma \gtrsim 3$.

(iii) For a wide range of IC cooling strengths ($0.06 \leq \tau_{\text{cool}} \leq 1.32$), the internal energy per electron for $\sigma_i = 3$ behaves remarkably similar to its $\sigma_i = 40$ counterpart in e^\pm plasma. This is because the electron magnetization is $\sigma_e \sim 80$ in both cases, and σ_e determines the electron internal energy. The electron internal energy scales linearly with τ_{cool} in the range we explored, and attains non-relativistic temperatures ~ 5 keV for strong cooling, $\tau_{\text{cool}} \sim 0.06$.

(iv) The radiatively inefficient ions retain the heat gained from reconnection, and their mean energy stays independent of τ_{cool} . Thus, the IC-cooled electrons are not re-heated by the hot ions. This renders the electrons incapable of powering thermal Comptonization, regardless of the plasma composition.

(v) The peak of the electrons' bulk energy spectra for IC-cooled trans-relativistic reconnection is generally narrower – indicating a more ordered outflow – than it is for relativistic ($\sigma \gg 1$) reconnection in e^\pm plasma. For strong cooling, the total electron spectra are dominated by their bulk component – whose peak energy increases with σ_i . For $\sigma_i = 2$ the spectral peak coincides with that of a Maxwellian distribution with a temperature of 100 keV. The high energy tail of the spectra – that are not accounted for by bulk motions – are due to electrons accelerated at X-points, on a time-scale faster than IC losses. In the limit of strong cooling, the fraction of radiated IC power contributed by these hot electrons is about 40 per cent for $1 \leq \sigma_i \leq 3$.

(vi) We find that reconnection layers in BH coronae with $\sigma_i = 3$ can Compton-upscatter soft photons to non-thermal energies and

explain the typical hard-state spectrum of accreting black holes. Such a spectrum peaks near 100 keV, and is primarily shaped by the bulk motions of plasmoids laden with cold (IC-cooled) electrons (whereas ions remain hot). The high-energy MeV tail may be produced by hot electrons quickly energized at X-points.

In the future, it may be useful to investigate how the results change for an electron–positron–ion plasma (e.g. Petropoulou et al. 2019, for the non-radiative case), in the presence of a stronger guide field, and for an asymmetric reconnection layer. Also, it has recently been shown that the physics of particle acceleration in reconnection is significantly different between 2D and 3D (Zhang et al. 2021). In 2D, electrons are accelerated near X-points up to $\gamma_X \sim \sigma_e/8$ (e.g. Sironi 2022), and then they get advected into plasmoids, where further energization proceeds slowly (e.g. Petropoulou & Sironi 2018; Hakobyan et al. 2021). Instead, in 3D most of the particles with $\gamma \gtrsim \gamma_X$ can escape from plasmoids and experience the large-scale electric field in the inflow region, resulting in fast acceleration (Zhang et al. 2021) potentially up to γ_{cr} . Further work is needed to clarify whether the amount of reconnection power dissipated in such high-energy particles can significantly change the properties of reconnection plasmoids mediated ‘cold-chain Comptonization’.

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DATA AVAILABILITY

The data underlying this article will be shared on reasonable request to the authors.

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APPENDIX A: SIMULATION PARAMETERS

We present in Table A1 the input parameters of all the simulations presented in the main text.

Table A1. List of numerical and physical input parameters.

$\sigma_i^{[1]}$	$\gamma_{\text{cr}}^{[2]}$	Domain size ^[3] $L_x/(c/\omega_{pe})$	$\tau_{\text{cool}}^{[4]}$	$m_i/m_e^{[5]}$
3	∞	1680	8	7
3	∞	1680	8	29
3	∞	1680	8	115
3	∞	1680	8	459
$\dagger 3$	∞	1680	8	1836
$\ddagger 3$	13.7	840	0.24	29
3	19.4	1680	0.24	29
3	22.5	1680	0.33	29
3	32	1680	0.66	29
3	45	1680	1.32	29
3	22.5	3360	0.16	29
3	19.4	3360	0.12	29
3	19.4	6720	0.06	29
2	17.5	1680	0.24	29
2	17.5	3360	0.12	29
2	17.5	6720	0.06	29
1	∞	1680	8	7
1	∞	1680	8	29
1	∞	1680	8	115
1	∞	1680	8	459
1	∞	1680	8	1836
1	12.1	420	0.66	29
1	17.2	420	1.32	29
1	10.4	840	0.24	29
1	10.4	1680	0.12	29
1	10.4	3360	0.06	29

Note. All simulations are performed for the same duration of $t_{\text{sim}} \sim 4.8L_x/v_A$, with the same initial particle number density, $n_0 = 4$, and spatial resolution $\mathcal{R} = (c/\omega_{pe})/\delta = 5$, unless specified otherwise. The description of each column is as follows. ^[1]Magnetization in the upstream plasma; ^[2]Critical Lorentz factor – a proxy for the intensity of incident photon field ($\gamma_{\text{cr}} = \infty$ implies no IC cooling, and smaller γ_{cr} implies greater IC cooling; see equation 3); ^[3]Half-length of the computational domain L_x , along the x -direction, in units of electron plasma skin depth; ^[4] τ_{cool} , as defined in equation (4); ^[5]Ion to electron mass ratio. \dagger indicates the model with three different available values of $\mathcal{R} = 2.5, 5$, and 10 (see Appendix C). \ddagger indicates the model with two different available values of $n_0 = 4$ and 64, different number of passes of current-density filtering (8 and 32) (see Appendix E), and different initial temperatures $\theta_e = 0.02$ and 10^{-4} (see Appendix C).

APPENDIX B: DEPENDENCE ON THE MASS RATIO

In this section, we check the influence of the mass ratio m_i/m_e on particle energization, for different σ_i , in the absence of IC cooling. As we have discussed in the main text, the overall dynamics of the reconnection layer, including the rate of reconnection, is nearly independent of m_i/m_e (see Section 4.1 and Fig. 1). In Fig. B1, we show that the mean total energy of electrons $\langle \gamma_e - 1 \rangle$ stays constant for a wide range of mass ratios, $7 \lesssim m_i/m_e \lesssim 1836$. A modest increase by a factor of ~ 3 is seen in the mean bulk energy $\langle \Gamma \rangle - 1$ while m_i/m_e decreases by a factor of ~ 260 . Furthermore, this is

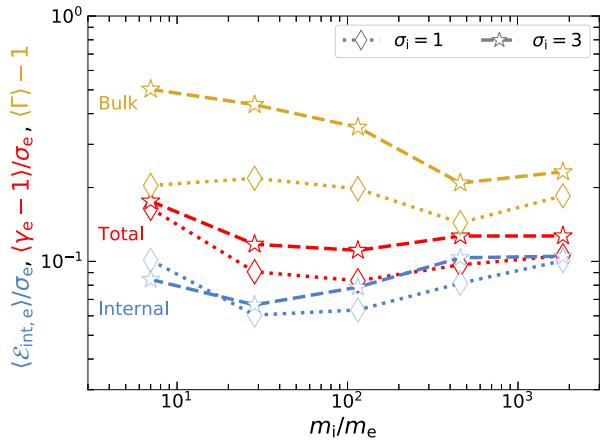


Figure B1. Mean energies of electrons (in units of $m_e c^2$) for different m_i/m_e and σ_i . The red markers indicate the total energy $\langle \gamma_e - 1 \rangle$, the blue markers indicate the internal energy $\langle \varepsilon_{\text{int},e} \rangle$, and the golden-brown markers indicate the bulk motion's contribution $\langle \Gamma \rangle - 1$. The total and internal energies are normalized by σ_e . The models with $\sigma_i = 1$ and $\sigma_i = 3$ are denoted by star and diamond markers, connected by dashed and dotted lines, respectively.

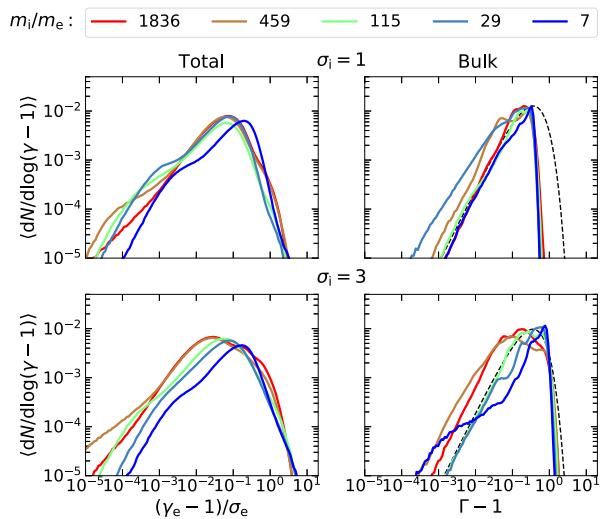


Figure B2. Total (left-hand column) and bulk (right-hand column) energy spectra of electrons for models with no external IC cooling ($\tau_{\text{cool}} = \infty$), with different magnetizations $\sigma_i = 1$ (top row) and $\sigma_i = 3$ (bottom row), and different mass ratios m_i/m_e (colour coded). For comparison, we also plot a Maxwellian distribution with a temperature of 100 keV (dashed black; right-hand panels). The spectra are time-averaged in the interval $2 \lesssim T/(L_x/v_A) \lesssim 5$, where $L_x/(c/\omega_{pe}) = 1680$ is the simulation domain size.

observable only for $\sigma_i \sim 3$, and not for $\sigma_i = 1$ (Fig. B2). For the purposes of our study, the choice of an artificially low mass ratio $m_i/m_e = 29$, as compared to its realistic value $m_i/m_e = 1836$, is not expected to impair the prospects of cold-chain Comptonization due to bulk motions. However, it is still valuable to check whether modest quantitative changes in the shape of the X-ray spectrum may come with higher, realistic mass ratios. This is left for future work.

APPENDIX C: CONVERGENCE WITH RESPECT TO SPATIAL RESOLUTION

Here, we check if the spatial resolution of the simulation domain influences the electrons' spectrum. We demonstrate with Fig. C1 that the shape of the electrons' total energy spectrum and its bulk component do not change in a systematic manner with a change in spatial resolution in the range $2.5 \leq \mathcal{R} \leq 10$. In fact, the spectra for $\mathcal{R} = 2.5$ and $\mathcal{R} = 10$ appear to overlap remarkably well. We note that the results from our simulations – performed with the default

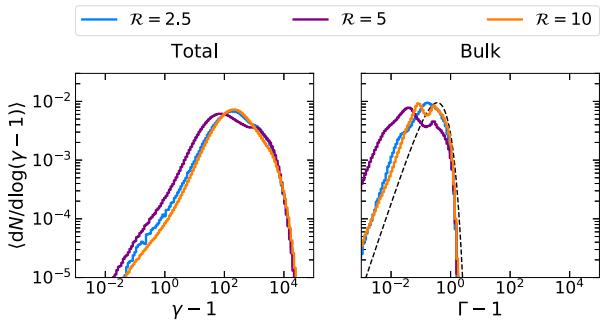


Figure C1. Total (left-hand panel) and bulk (right-hand panel) energy spectra of electrons for models with the same $\sigma_i = 3$, mass ratio $m_i/m_e = 1836$, no external IC cooling ($\tau_{\text{cool}} = \infty$), with different resolutions $\mathcal{R} = 2.5$ (blue), $\mathcal{R} = 5$ (maroon; default value in this work) and $\mathcal{R} = 10$ (orange). For comparison, we also plot a Maxwellian distribution with a temperature of 100 keV (dashed black; right-hand panels). The spectra are time-averaged in the interval $2 \leq T/(L_x/v_A) \leq 5$, where $L_x/(c/\omega_{pe}) = 1680$ is the simulation domain size.

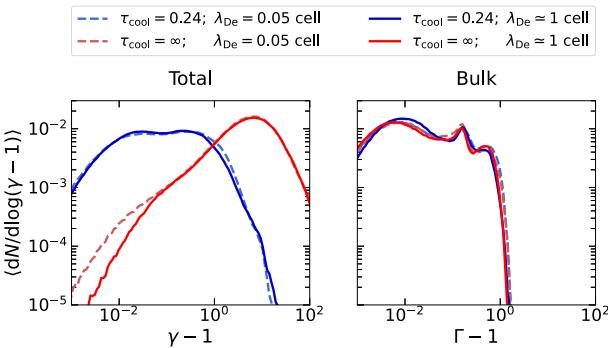


Figure C2. Total (left-hand panel) and bulk (right-hand panel) energy spectra of electrons for models with the same $\sigma_i = 3$, $m_i/m_e = 29$, spatial resolution $\mathcal{R} = 5$, but with different strengths of IC cooling, $\tau_{\text{cool}} = 0.24$ (blue curves) and $\tau_{\text{cool}} = \infty$ (red curves), and Debye lengths $\lambda_{\text{De}} = \sqrt{k_B T_e / 4 \pi n_0 e^2} = 0.05$ cells (dashed curves) and 1 cell (solid curves). The spectra are time-averaged in the interval $2 \leq T/(L_x/v_A) \leq 5$, where $L_x/(c/\omega_{pe}) = 840$ is the simulation domain size.

value of $\mathcal{R} = 5$ with outflow boundary conditions along x -direction – are robust with respect to the spatial resolution.

On the other hand, the Debye length $\lambda_{\text{De}} = \sqrt{k_B T_e / 4 \pi n_0 e^2}$ under the initial plasma conditions of our fiducial simulations is only 0.05 cells. We assess whether our results are prone to any numerical artefacts due to underresolved λ_{De} . Overall, our aim is to perform simulations in a cold plasma, meaning where the initial thermal energy is much smaller than the rest mass energy. In this case, we argue that the reconnection physics does not depend on the specific choice of initial temperature. We perform new simulations of IC-cooled reconnection, where λ_{De} is resolved. Rather than resolving λ_{De} by increasing \mathcal{R} – which is computationally very demanding (for our requirement of low τ_{cool} , and so, a large $L_x/(c/\omega_{pe})$) – we initialize a relatively hotter upstream plasma: instead of our fiducial upstream temperature of $\theta_e = k_B T_e / m_e c^2 = 10^{-4}$, we now consider a temperature of $\theta_e = 0.02$. While this is still cold enough compared to the energies particles attain as a result of reconnection (which is the regime we want to be in, as prefaced above), this choice of temperature also resolves λ_{De} with 1 cell assuming the same fiducial resolution of $\mathcal{R} = 5$. We have performed four new simulations with periodic boundary conditions along the x -direction (the boundary conditions along the y -direction remain the same as in our fiducial case) with the following parameters: $\mathcal{R} = 5$, $\sigma_i = 3$, $n_0 = 4$, 32 rounds of current filtering, and $m_i/m_e = 29$. The parameters that differentiate the four models are: (1) $\tau_{\text{cool}} = 0.24$, $\theta_e = 10^{-4}$ (as in the main text), (2) $\tau_{\text{cool}} = 0.24$, $\theta_e = 0.02$, (3) $\tau_{\text{cool}} = \infty$, $\theta_e = 10^{-4}$ (no cooling), and (4) $\tau_{\text{cool}} = \infty$, $\theta_e = 0.02$ (no cooling). Note that in Appendix D, we show that these choices of simulation parameters yield a similar η_{rec} to our fiducial simulations.

Our results are presented in Fig. C2, which shows the total energy spectrum (left-hand panel) and the bulk component (right-hand panel). One can see a close match in the spectral shape, location of the peak, its normalization, and the cut-off energy, for our current simulations with underresolved λ_{De} (dashed curves) versus the cases that resolve λ_{De} with 1 cell (solid curves). This similarity holds for both cooled (blue curves) and uncooled cases (red curves). The presence of a broad peak at $\Gamma - 1 \sim 4 \times 10^{-3}$ in the bulk spectra is due to the formation of near-static monster plasmoids at the edges of the box due to the assumed periodic boundary conditions (here, plasmoids are not advected out of the box, as in our fiducial setup, but instead they merge and keep growing over time).

APPENDIX D: ATTAINMENT OF QUASI-STEADY STATE

All the quantities of interest to this paper are calculated for times $T/(L_x/v_A) \gtrsim 2$, for this is when the reconnection layer attains a quasi-steady state, i.e. the formation of plasmoids and their advection out of the domain occur at a somewhat steady rate. This happens concurrently with the saturation of the reconnection rate ($\eta_{\text{rec}} = v_{\text{in}}/v_A$, which measures the inflow speed of upstream plasma into the reconnection layer). This is shown in Fig. D1 for various simulation conditions. We also change the initial thickness of the current sheet to delay the onset of reconnection to see if this changes the way the system evolves once reconnection is triggered. Overall, we see that the layer attains a quasi-steady state $\sim 1 L_x/v_A$ after reconnection is triggered, regardless of our chosen initial conditions.

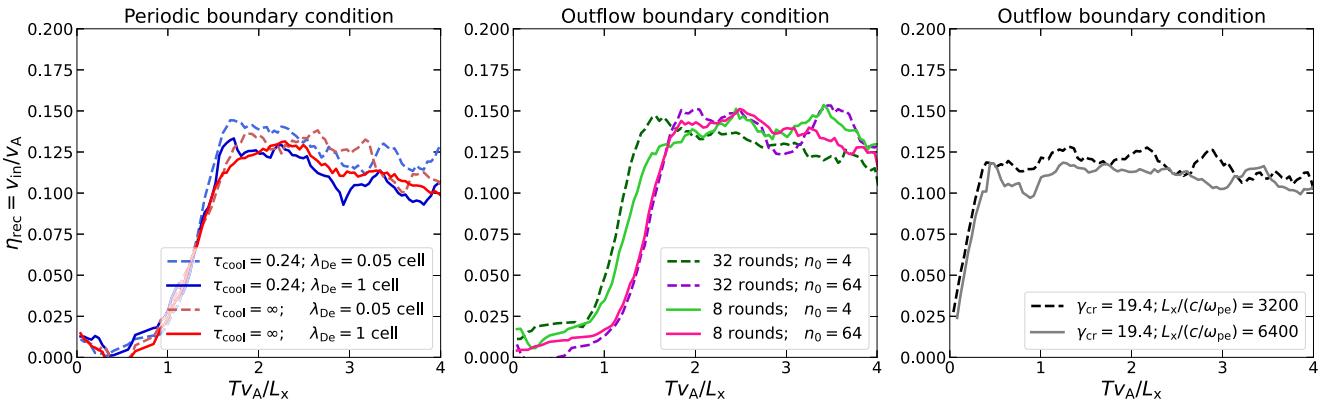


Figure D1. Reconnection rate (η_{rec}) under different simulation conditions. The fiducial set of simulation parameters are: $\mathcal{R} = 5$, $\sigma_i = 3$, $n_0 = 4$, $m_i/m_e = 29$, $L_x/(c/\omega_{\text{pe}}) = 840$, $\tau_{\text{cool}} = 24$, $\theta_e = 10^{-4}$ ($\lambda_{\text{De}} = \sqrt{k_B T_e / 4\pi n_0 e^2} = 0.05$ cells), 32 rounds of binomial current density filtering, and outflow boundary conditions along the x -direction. Each curve denotes a simulation setup that differs from the fiducial case by one or two parameters (bottom-right legend in each panel). In addition, we change the initial thickness of the current sheet Δ_y to delay the onset of reconnection by $\sim 1 L_x/v_A$, for simulations in the left and middle panels. Left-hand panel: simulations that employ periodic boundary conditions along the x -direction, for different initial temperatures (equivalent to different λ_{De}), in the presence and absence of IC cooling. Middle panel: simulations with different upstream particle number densities and rounds of binomial current filtering. Right-hand panel: simulations with different strengths of IC cooling, $\tau_{\text{cool}} = 0.06$ (grey solid curve) and $\tau_{\text{cool}} = 0.12$ (black dashed curve).

APPENDIX E: CONVERGENCE WITH RESPECT TO PARTICLE DENSITY AND ROUNDS OF CURRENT DENSITY FILTERING

Throughout our simulations, we initialize the domain with four particles per cell ($n_0 = 4$; two electrons and two ions). Here, we check if our results with outflow boundary conditions along the x -direction are robust to this choice, by comparing our default $n_0 = 4$ simulations against simulations with a higher $n_0 = 64$. Further, we check if the many rounds (32) of binomial 1-2-1 current filtering that we employ in our simulations artificially affect our results. We do this by performing new simulations with a lower number (8) of rounds of current filtering.

Fig. E1 shows the total energy spectra (left-hand panel) and the bulk component (right-hand panel). The overall conclusions of our

paper (~ 100 keV Maxwellian peak of electrons' bulk spectrum, and a corresponding ~ 100 keV cut-off energy in X-ray spectrum) are determined primarily by the shape and location of the peak of the bulk spectrum. We note that these features are not different for either 8 rounds or 32 rounds of binomial current filtering. The excess at low energies seen in the bulk spectrum at $\Gamma - 1 \sim 2 \times 10^{-3}$ for the simulation with 32 rounds of filtering is due to the stochastic formation of a monster plasmoid. We also ran simulations with a much higher particle density of $n_0 = 64$, for both 8 and 32 rounds of filtering: our original results are found to be robust.

APPENDIX F: ELECTRON-ION ENERGY EXCHANGE VIA COULOMB COLLISIONS

The coronal plasma is expected to be approximately collisionless (Goodman & Uzdensky 2008). However, the plasmas in PIC simulations differ from real astrophysical plasmas due to 'coarse-graining', i.e. multiple particles are represented in the computer by a single macroparticle. This approach – while numerically beneficial – can artificially enhance the thermal coupling between electrons and ions via Coulomb collisions (Melzani et al. 2014b). Clearly, the artificial Coulomb coupling is not significant in our simulations, since the plasma ends up with two temperatures (hot ions and cold electrons; see Fig. 4). This fact can also be seen using the following estimate for the Coulomb coupling time-scale (Spitzer 1965; Stepney 1983; Melzani et al. 2013),

$$t_{\text{ei}} = \frac{3m_i m_e c^3}{8\sqrt{2\pi} e^4} \frac{1}{\mathcal{N}} \left(\frac{k_B T_e}{m_e c^2} + \frac{k_B T_i}{m_i c^2} \right)^{3/2}, \quad (\text{F1})$$

where \mathcal{N} has units of particles per unit volume. The expression for \mathcal{N} differs between two and three dimensions, due to the different volume element in the space of impact parameters: in 3D we have $\mathcal{N} = n \ln \Lambda$, where n is the number of particles per unit volume, $\ln \Lambda = \ln(b_{\text{max}}/b_{\text{min}})$ is the Coulomb logarithm, and b_{min} and b_{max} are the minimum and maximum impact parameters for the Coulomb interaction, respectively. In 2D, instead, $\mathcal{N} = 2\pi n_{2D} \left(\frac{1}{b_{\text{min}}} - \frac{1}{b_{\text{max}}} \right) \simeq 2\pi n_{2D}/b_{\text{min}}$, where n_{2D} is the number of

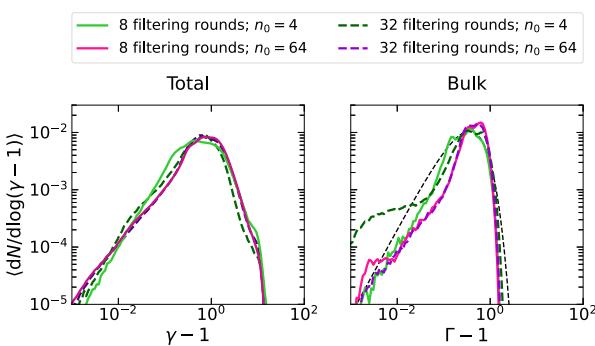


Figure E1. Total (left-hand panel) and bulk (right-hand panel) energy spectra of electrons for models with the same $\sigma_i = 3$, $m_i/m_e = 29$, $\tau_{\text{cool}} = 0.24$, but with different choices of particle number density $n_0 = 4$ (green curves; default value in this work) and $n_0 = 64$ (purple). We also show spectra from simulations with different number of binomial current density filtering: 32 rounds (dashed curves; default value in this work), and 8 rounds (solid curves). For comparison, we also plot a Maxwellian distribution with a temperature of 100 keV (dashed black; right-hand panel). The spectra are time-averaged in the interval $2 \lesssim T/(L_x/v_A) \lesssim 5$, where $L_x/(c/\omega_{\text{pe}}) = 840$ is the simulation domain size.

particles per unit area (as appropriate for a 2D simulation). The maximum impact parameter b_{\max} is the electron Debye length, $\lambda_{\text{De}} = \sqrt{k_B T_e / 4\pi n_0 e^2}$. In real astrophysical plasmas, the minimum impact parameter b_{\min} is the classical distance of closest approach. Instead, in PIC simulations it shall be taken as the characteristic size of macroparticles, which is comparable to the grid spacing δ .

For our 2D simulations, we take a 2D density of $n_{2D} \simeq n_0 = 4$ particles per cell, temperatures $k_B T_e / m_e c^2 \ll k_B T_i / m_i c^2$, and the reduced mass ratio $m_i / m_e = 29$ of our simulations. Then we obtain $t_{ei} \approx 3 \times 10^5 \omega_{pe}^{-1} (k_B T_i / 0.5 m_i c^2)^{3/2}$. Note that this is much longer than the time-scale for plasma advection out of the reconnection layer: $t_{ei} / (L_x / v_A) \approx 60$ (for the most constraining case of our largest simulation with $L_x / (c / \omega_p) = 6720$, and $\sigma_i = 3$). This confirms that Coulomb energy exchange is weak in our PIC simulations.

M marginally important Coulomb coupling is expected in real black hole coronae with high magnetizations $\sigma > 1$. It can be evaluated using the expression for t_{ei} , but now with realistic plasma parameters. The ratio of the Coulomb and advection time-scales may be written in the following form,

$$\frac{t_{ei}}{L_x / v_A} \sim \frac{m_i / m_e}{10 \tau_T \ln \Lambda} \left(\frac{v_A}{c} \right)^2 \left(\frac{k_B T_i}{m_i c^2} \right)^{3/2}, \quad \frac{T_e}{m_e} \ll \frac{T_i}{m_i}. \quad (\text{F2})$$

Coulomb logarithm $\ln \Lambda \sim 20$ is determined by the characteristic plasma density $n = \tau_T / h \sigma_T$ where $h \approx 0.1 (v_A / c) L_x$ is a fraction of the system size (a fraction of the black hole radius). Using $\tau_T \sim 1$, $(v_A / c)^2 = \sigma / (1 + \sigma)$, and $k_B T_i \sim (\sigma / 4) m_i c^2$, we obtain a rough estimate $t_{ei} / (L_x / v_A) \sim \sigma^{5/2} / (1 + \sigma)$. For a large $\sigma > 1$, $t_{ei} / (L_x / v_A)$ exceeds unity, and the ions are not expected to pass their energy to electrons via Coulomb collisions. The Coulomb coupling becomes important at lower $\sigma \sim 1$.

APPENDIX G: ION TEMPERATURE ANISOTROPY

In this section, we examine the reconnection layer for the potential occurrence of collision-less ion velocity-space instabilities that could transfer thermal energy between ions and electrons. We calculate in the reconnection region the ion temperature anisotropy parameter $\mathcal{A}_i = T_{\perp}^i / T_{\parallel}^i - 1$, where T_{\perp}^i and T_{\parallel}^i are the temperatures of the ions perpendicular and parallel to the local magnetic field, respectively. The temperature elements are obtained as follows. The stress-energy tensor and the electromagnetic tensor are Lorentz boosted to the plasma comoving frame. A rotation matrix is then computed – using Rodrigues' rotation formula – so that the local comoving magnetic field gets oriented along \hat{y} . The Lorentz boosted stress-energy tensor is then rotated with this rotation matrix. The diagonal elements of thus obtained tensor correspond to the temperatures along different axes. In this case, $T_{\parallel} = T_{yy}$ and $T_{\perp} = (T_{xx} + T_{zz})/2$.

In the presence of ion temperature anisotropy, the plasma can develop either ion-cyclotron/mirror instabilities for $\mathcal{A}_i > 0$, or fire-hose instability for $\mathcal{A}_i < 0$ (Hall 1979). Fig. G1 shows a 2D map of \mathcal{A}_i along the reconnection layer (panel b). One can see that the ions' temperatures are fairly isotropic in reconnection plasmoids that contain most of the particles (compare with the ion density in panel a). Furthermore, it is evident that the ion-cyclotron/mirror instabilities are non-operational throughout the layer (because $\mathcal{A}_i \not> 1$), precluding the possibility of ion-to-electron thermal energy transfer through this channel (e.g. Sironi et al. 2015). On the other hand, the periphery of the reconnection layer exhibits regions (with $\mathcal{A}_i < 0$) possibly prone to the firehose instability. This is understandable, as the freshly injected particles in the periphery of the layer slide along the local magnetic field lines before eventually entering the plasmoids.

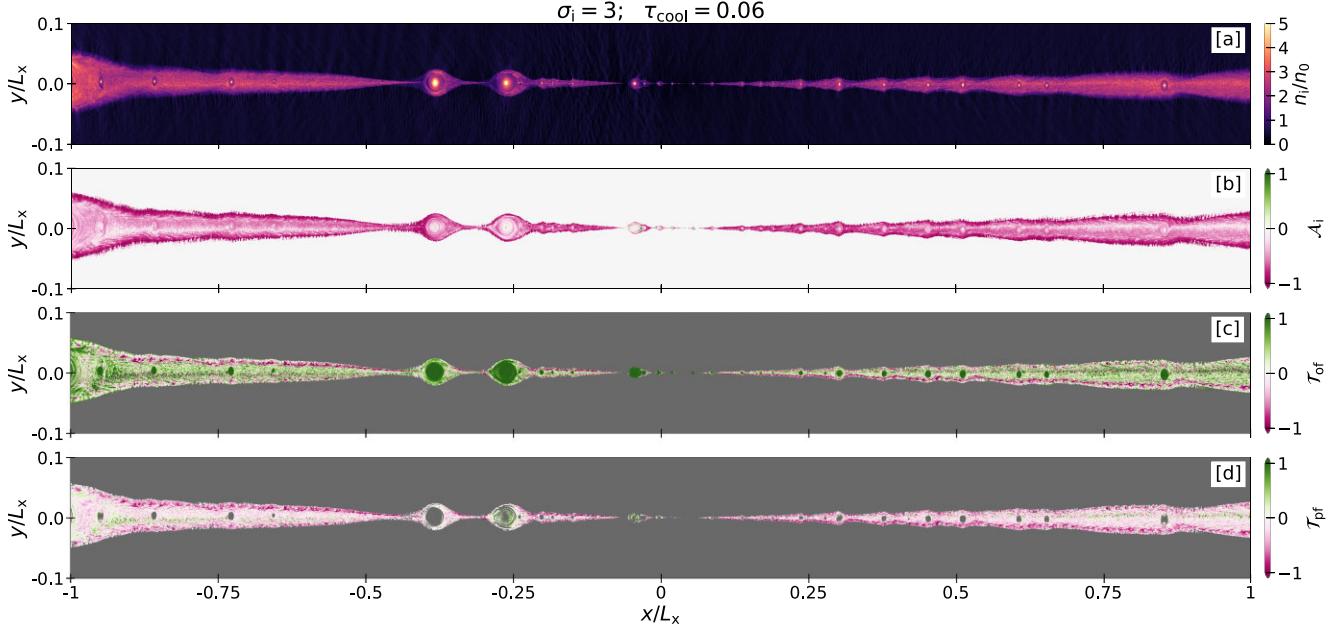


Figure G1. Snapshot of the reconnection region at time $T \simeq 5 L_x / v_A$ for the strongly cooled ($\tau_{\text{cool}} = 0.06$) run with $\sigma_i = 3$. We only show the region $|y| \leq 0.1 L_x$ where reconnection occurs, where $L_x / (c / \omega_{pe}) = 6720$. (a) Ion number density n_i in units of the initialized (upstream) number density n_0 . (b) Ion temperature anisotropy $\mathcal{A}_i = T_{\perp}^i / T_{\parallel}^i - 1$, where T_{\perp}^i and T_{\parallel}^i are the temperatures of the ions perpendicular and parallel to the local magnetic field, respectively. (c) Threshold for triggering oblique firehose instability, $\mathcal{T}_{\text{of}} = (\beta_{\parallel} + 0.11) \mathcal{A}_i + 1.4 < 0$, where $\beta_{\parallel} = 8\pi n_i k_B T_{\parallel}^i / B^2$ is the parallel ion plasma- β . (d) Threshold for triggering parallel firehose instability, $\mathcal{T}_{\text{pf}} = (\beta_{\parallel} - 0.59)^{0.53} \mathcal{A}_i + 0.47 < 0$.

The threshold condition for the firehose instability is given by (Hellinger et al. 2006),

$$\frac{T_{\perp}^i}{T_{\parallel}^i} - 1 = \frac{a}{(\beta_{\parallel} - \beta_0)^b}, \quad (G1)$$

where $\beta_{\parallel} = 8\pi n_i k_B T_{\parallel}^i / B^2$ is the parallel ion plasma- β , and a, b , and β_0 are obtained from empirical fitting (Gary et al. 1998; Samsonov et al. 2001; Hellinger et al. 2006; Bale et al. 2009). The relevant modes in the case of $\mathcal{A}_i < 0$ are the parallel firehose (Quest & Shapiro 1996) and the oblique firehose (Hellinger & Matsumoto 2000). Assuming isotropic Maxwellian electrons, the thresholds for these modes are

$$\mathcal{T}_{\text{of}} = (\beta_{\parallel} + 0.11)\mathcal{A}_i + 1.4 < 0 \quad (\text{oblique firehose}), \quad (G2)$$

$$\mathcal{T}_{\text{pf}} = (\beta_{\parallel} - 0.59)^{0.53} \mathcal{A}_i + 0.47 < 0 \quad (\text{parallel firehose}). \quad (G3)$$

We see from panel (c) of Fig. G1 that most of the reconnection region does not obey the condition $\mathcal{T}_{\text{of}} < 0$ required for the growth of the oblique firehose instability. On the other hand, $\mathcal{T}_{\text{pf}} < 0$ is satisfied along the periphery of the reconnection region – indicating that the parallel firehose instability may grow there (panel d). However, note that neither parallel nor oblique modes of firehose instabilities are seen to operate within reconnection plasmoids that contain the majority of the particles. We can therefore confirm that ion velocity–space instabilities do not play any significant role in the transfer of thermal energy from ions to electrons, as our results indicate in the main text.

APPENDIX H: BOUNDARY CONDITIONS IN RADIATIVE TRANSFER CALCULATION

Our PIC simulations employ outflow boundary conditions in the x direction of reconnection exhausts. In this Appendix, we demonstrate the effect of employing different boundary conditions for the Monte Carlo radiative transfer calculation. In our previous work (SSB21),

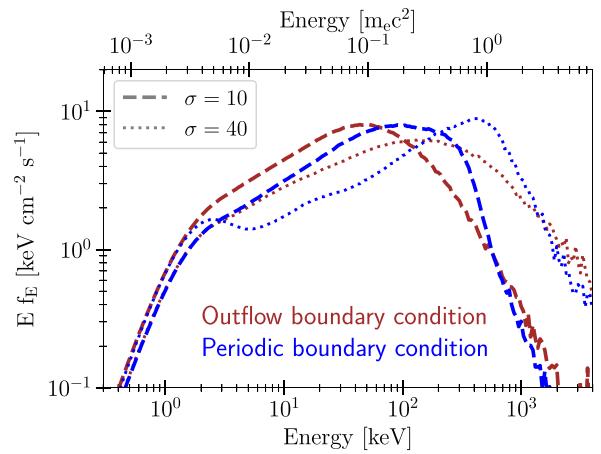


Figure H1. Dependence on the choice of boundary conditions for the Monte Carlo radiative transfer calculation. We show electron–positron models with $\sigma = 10$ (dashed) and $\sigma = 40$ (dotted), with the same strength of radiative cooling losses ($\gamma_{\text{cr}} = 16$) and Compton amplification factor ($A = 10$). The brown and blue curves are obtained by employing outflow and periodic boundary conditions, respectively.

we extracted X-ray spectra from electron–positron simulations of reconnection in strongly magnetized plasma. There, the radiative transfer code assumed periodic boundaries in the x direction. A more appropriate choice – as we have done in the main body of this paper – is to employ outflow boundaries for the Monte Carlo calculation, in analogy to the open boundaries of the PIC simulation. As shown in Fig. H1, at fixed magnetization, the X-ray spectrum peaks at higher energies in the case of periodic boundaries. This is expected, since in this case photons crossing the boundary can efficiently scatter off an oppositely directed flow, thus increasing their energy.

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