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To cite this article: K T A Assumin-Gyimah *et al* 2022 *Class. Quantum Grav.* **39** 245014

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Neutron phase contrast imaging of PbWO_4 crystals for G experiment test masses using a Talbot-Lau neutron interferometer

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Received 7 February 2022; revised 12 October 2022

Accepted for publication 9 November 2022

Published 25 November 2022



CrossMark

Abstract

The use of transparent test/source masses can benefit future measurements of Newton's gravitational constant G . Such transparent test mass materials can enable nondestructive, quantitative internal density gradient measurements using optical interferometry and allow *in-situ* optical metrology methods to be realized for the critical distance measurements often needed in a G apparatus. To confirm the sensitivity of such optical interferometry measurements to internal density gradients it is desirable to conduct a check with a totally independent technique. We present an upper bound on possible internal density gradients in lead tungstate (PbWO_4) crystals using a Talbot-Lau neutron interferometer on the Cold Neutron Imaging Facility at NIST. We placed an upper bound on a fractional atomic density gradient in two PbWO_4 test crystals of $\frac{1}{N} \frac{dN}{dx} < 0.5 \times 10^{-6} \text{ cm}^{-1}$. This value is about two orders of magnitude smaller than required for G measurements. We discuss the implications of this result and of other nondestructive methods for characterization of internal density inhomogeneities which can be applied to test masses in G experiments.

Keywords: neutron phase contrast imaging, Talbot-Lau interferometry, G experiments

(Some figures may appear in colour only in the online journal)

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1. Introduction

Despite a long history, starting with the 1798 measurement by Cavendish [1], our current knowledge of the universal gravitational constant G is rather poor compared to other fundamental constants. Gravity is the weakest force in nature and it is impossible to shield. Measuring G is a serious precision measurement challenge. The 2018 recommended value by the Committee on Data for Science and Technology (CODATA) [2] has a relative uncertainty of 22×10^{-6} . Figure 1 shows the most precise measurements conducted in the past 30 years, including both the measurements used in the 2018 CODATA evaluation and two newer measurements [3]. The scatter among the values from different experiments is far beyond what one would expect based on the quoted errors.

This implies a lack of complete understanding of either the physics behind gravitation, or the systematics used to perform these measurements, or both. General relativity, the currently accepted description of gravitation, may not be complete. A successful unification of gravitation with quantum mechanics remains elusive [4]. Typical G experiments measure small forces, torques, or accelerations with a relative uncertainty of about 10^{-5} , and it is fair to say that most people believe that the scatter in this data represents unaccounted-for systematic errors which plague the metrology of small forces. Many of these metrological issues are discussed in a recent review [5].

Given this situation, future precision G measurements will justifiably be held to a higher standard for their analysis and quantitative characterization of systematic errors. The procedures for corrections to the raw G data from apparatus calibration and systematic errors using subsidiary measurements is very specific to the particular measurement apparatus and approach. However, there are some sources of systematic uncertainties that are common to almost all precision measurements of G , for example the metrology of the source/test masses used in the experiments [6]. A research program which successfully addresses this issue can help improve G measurements.

We are working to characterize optically transparent masses for G experiments. The use of transparent source/test masses in G experiments enables nondestructive, quantitative internal density gradient measurements using optical interferometry and can help prepare the way for optical metrology methods for the critical distance measurements needed in many G measurements. The density variations of glass and single crystals are generally much smaller than those for metals [7] and hence they are likely to be a better choice for source/test masses for experiments which will need improved systematic errors. It is also desirable to use a transparent test mass with a large density.

A typical G measurement instrument involves distances on the order of 50 cm and source mass dimensions on the order of 10 cm. The masses are usually arranged in a pattern which lowers the sensitivity of the gravitational signal to small shifts δR in the location of the true center of mass from the geometrical center of the masses by about two orders of magnitude. Under these typical conditions, we conclude that in order to attain a 1 ppm uncertainty in mass metrology, the internal number density gradients of the test masses must be controlled at the level of about $\frac{1}{N} \frac{dN}{dx} = 10^{-4} \text{ cm}^{-1}$ and the absolute precision of the distance measurement to sub-micron precision. It is also valuable to use a test mass with a high density to maximize the gravitational signal strength while also bringing the masses as close as possible to each other consistent with the other experimental constraints.

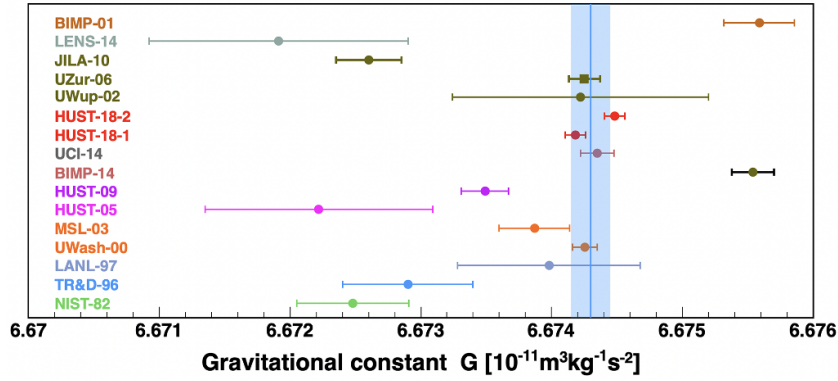


Figure 1. The most precise measurements of G over the last 30 years. The blue line and band shows the 2018 CODATA recommended value. The red data points come from two new recent measurements of G [3], since the 2018 CODATA evaluation.

We have chosen to characterize density gradients in lead tungstate (PbWO_4) to the precision required for ppm-precision G measurements. We are performing this characterization using both optical interferometry and neutron interferometry. This paper discusses the results of the neutron interferometric characterization.

2. Relevant properties of PbWO_4

Lead tungstate is a reasonable material to choose for such a characterization. It is dense, optically transparent, nonmagnetic, and machinable to the precision required to determine G and to characterize its internal density gradients by optical techniques. This material can be grown in very large optically transparent single crystals in the range of sizes needed for G experiments and has been developed in high energy physics as a high Z scintillating crystal. The high density uniformity and low impurity concentrations developed to meet the technical requirements for efficient transmission of the internal scintillation light inside these crystals also match the requirements for G test masses. Lead tungstate is transparent for the entire visible spectrum as shown in figure 2.

These crystals are non-hygroscopic and are commercially available, for example from the Shanghai Institute of Ceramics (SIC) [8]. Several tons of PbWO_4 are currently in use in nuclear and high energy physics experiments all over the world. This material is actively studied and produced in large quantities for several new detectors under construction and for R&D on future detectors to be used at the recently-approved Electron Ion Collider to be built at Brookhaven National Lab. We therefore foresee a long-term motivation for continued R&D on crystal size and quality from nuclear and high energy physics. Based on their scintillation characteristics, the SIC grows boules of PbWO_4 measuring $34 \text{ mm} \times 34 \text{ mm} \times 360 \text{ mm}$, which are then diamond cut and polished to the desired size (typically $24 \text{ mm} \times 24 \text{ mm} \times 260 \text{ mm}$) [9]. SIC has recently produced crystals of 60 mm in diameter and are capable of producing crystals with a diameter of 100 mm and length of 320 mm [10]. These larger sizes are very suitable for G experiments [11].

Since impurities in PbWO_4 affect the crystal quality, degrade the optical transmittance properties, reduce scintillation light yield, and produce radiation damage, great effort is put into

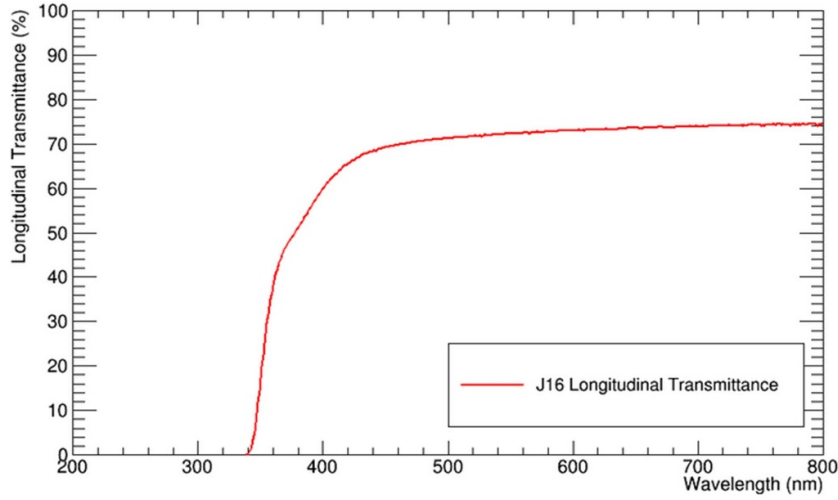


Figure 2. Transmittance of PbWO_4 as a function of wavelength of incident light.

Table 1. List of non-hygroscopic, optically-transparent, high-density crystals and their physical properties.

Material	PbWO_4	CdWO_4	LSO	LYSO	BGO
Density (g cm^{-3})	8.3	7.9	7.4	7.3	7.13
Atomic numbers	82, 74, 8	48, 74, 8	71, 32, 8	71, 39, 32, 8	83, 32, 8
Refractive index (light)	2.2	2.2–2.3	1.82	1.82	2.15
Thermal expansion	8.3 (para)	10.2	5	5	7
Coefficient(s) ($10^{-6} \text{ }^\circ\text{C}^{-1}$)	19.7 (perp)	—	—	—	—

minimizing or eliminating common impurities such as Mo^{6+} , Fe^{2+} , Na^+ , K^+ and Y^{3+} . Analysis using glow discharge mass spectroscopy indicates that most of the common impurities can be reduced to <1 ppm by weight [9]. At 32 ppm by weight Y^{3+} is the largest impurity and has a direct effect on the uniformity and scintillation properties of PbWO_4 . Therefore, the distribution of Y^{3+} is carefully controlled to ensure uniformity in detector grade crystals [9].

The mass density of PbWO_4 , $\rho = 8.26 \text{ g cm}^{-3}$, is only a factor of 2 smaller than that of tungsten, the densest material commonly used in G measurements. Its transparency opens up the possibility for G experiments to conduct laser interferometric measurements of its dimensions and location, thereby providing a way to cross-check coordinate measuring machine metrology and thereby independently confirm its absolute accuracy. In addition, the existence of such a source mass material might inspire new designs of G apparatus to take advantage of the possibility of *in-situ* optical metrology to re-optimize the apparatus design tradeoffs between systematic errors and G signal size. In addition to PbWO_4 there are several additional high density materials that are also optically transparent and could be used as source/test masses. A list of relatively high density materials and their key physical properties is listed in table 1. Although not listed in the table, silicon could be another choice for a G test mass material in view of the large volumes and very high crystal quality available and developed over decades for the semiconductor industry. Neutron and optical interferometric methods can be applied to all of these materials.

3. Use of Talbot-Lau phase contrast imaging for mass density gradient search

Slow neutrons can penetrate macroscopic amounts of matter, and their coherent interactions with matter dominate the low-energy dynamics and enable various forms of interferometric measurement methods. We sought a neutron interferometric phase-sensitive measurement method which would be as sensitive as possible to internal density gradients. A neutron passing through a medium of number density N and thickness L will accumulate a phase shift $\Phi = Nb_c\lambda L$ where b_c is the coherent neutron scattering amplitude and λ is the neutron wavelength. The quantity of interest for our study is the fractional density gradient $\frac{1}{N} \frac{dN}{dx}$. The coherent neutron scattering lengths b_c of almost all stable nuclei are known from experiment, and almost all of them possess negligible dispersion so that their values are typically known with fractional accuracy of order 10^{-2} – 10^{-3} . The neutron wavelength λ of slow neutrons can be determined with sufficient precision using a wide variety of methods including diffraction, neutron time-of-flight, etc. Uncertainties in L measurements can be quite small.

We therefore seek an interferometric technique which can measure a phase gradient $\frac{\partial \Phi}{\partial x}$. This can be done in principle using different types of phase contrast imaging techniques. Here we briefly review the operation of a specific type of shearing interferometer, a Talbot-Lau interferometer for neutron phase gradient measurement and its application to our problem. We refer readers to the description in [12] and to a recent review [13] for more details.

The Talbot-Lau interferometer sketched in figure 3 consists of three gratings G_0 , G_1 , and G_2 with their associated periods p_i . G_0 is an absorbing grating whose spacing is chosen to convert an incoherent beam of incident neutrons into multiple parallel independent line sources which are mutually incoherent but possess enough transverse phase coherence for Talbot-Lau interferometry. This allows the self-images formed at G_2 described below to be overlaid constructively and thereby enables phase contrast imaging even with the types of incoherent beams available at neutron sources.

The G_1 phase modulation grating, chosen in our case to produce π phase shifts in the transmitted neutron phase, diffracts the neutron beam and produces a near-field interference pattern (the Talbot-Lau carpet) with maxima at Talbot lengths $d_T = p_{d1}^2/8n\lambda$ where p_{d1} is the period of G_1 , and n is an odd integer (1 in our case). An absorption grating G_2 is located at one of the Talbot carpet maxima and generates a Moire pattern that can be recorded on a 2D position sensitive neutron detector. This Moire pattern has the form

$$I(x, y) = A(x, y) + B(x, y) \cos \left[\frac{2\pi z}{np_{d2}} \alpha(x, y) + \Delta(x, y) \right]$$

where x, y are the coordinates transverse to the neutron beam optical axis, which points along the direction of the separation z between gratings G_1 and G_2 . A deflection of the neutron beam direction between G_1 and G_2 , which in our case can be produced by neutron refraction from the sample, induces a corresponding lateral shift of the interference pattern. The neutron refraction angle α can be related to the gradient of the sample phase shift $\Phi(x, y)$ normal to the neutron beam direction

$$\alpha(x, y) = \frac{\lambda}{2\pi} \frac{\partial \Phi(x, y)}{\partial x}.$$

In our experiment the square cross section PbWO_4 crystals were mounted in the beam with their faces were oriented at $\pm 45^\circ$ to the neutron beam axis so that the incident neutron beam moves through the sample parallel to the diagonal. This geometry produces transverse phase gradients and therefore neutron refraction angles of equal magnitude and opposite sign on either side of the neutron beam axis. If the density of the medium is uniform, $\alpha(x, y)$ is independent of x . A fractional density gradient $\frac{1}{N} \frac{dN}{dx}$ in the PbWO_4 would generate an additional

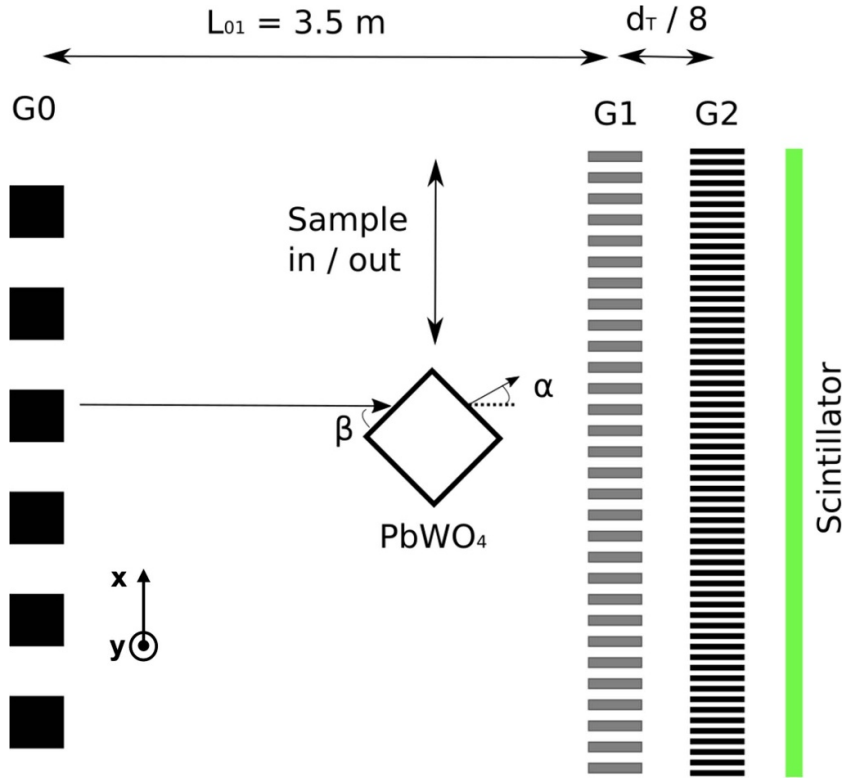


Figure 3. Sketch of the Talbot-Lau phase gradient measurement setup, not to scale, showing the gratings G_0 , G_1 , and G_2 whose functions are described in the text. The PbWO_4 crystal is placed so that each face is approximately 45° with respect to the neutron beam axis (β) which refracts the incident beam by angle α . The measurement consists of acquiring phase step images with the sample in and then translated out of the beam. The phase step images were acquired by translating G_1 through one period.

phase gradient $\frac{\partial \Phi(x,y)}{\partial x} = Nb_c \lambda L \frac{dN}{dx}$. We can therefore analyze the phase shift image to either search for or place upper bounds on the internal density gradients of interest along a direction normal to the neutron beam.

To extract the neutron phase shift information of interest from $I(x,y)$ one can measure several phase contrast maps with a grating displaced normal to the neutron beam by different values of x . This procedure generates a sinusoidal phase-stepping curve at each (x,y) pixel of the image from which a map of the total phase can be extracted [13]. The contribution to the total phase shift from $\Delta(x,y)$, which comes from imperfections, alignment offsets, etc in the gratings, can be removed by taking data with the sample absent.

4. Sample characterization

Visual inspection reveals no evidence for any nonuniform local density anomalies from internal voids or inclusions of the type which might introduce systematic errors in G measurements. The detailed shapes of the four $2.3 \text{ cm} \times 2.3 \text{ cm}$ area surfaces for each crystal were measured by the NIST Metrology Group on a coordinate measuring machine, with a maximum permissible

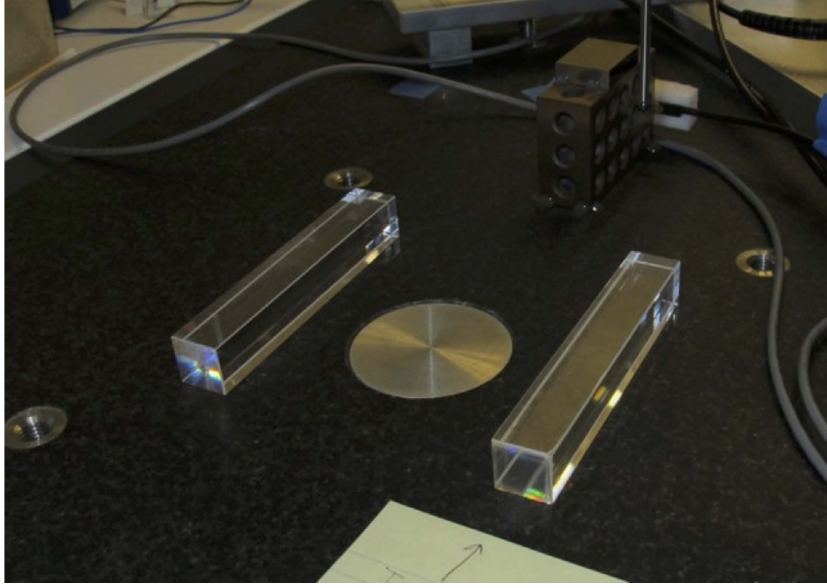


Figure 4. Two PbWO_4 crystals mounted in the NIST coordinate measuring machine. Each of the crystals shown in this photo have nominal dimensions of $2.3 \text{ cm} \times 2.3 \text{ cm} \times 12 \text{ cm}$.

error of $0.3 \mu\text{m} + L/1000 \mu\text{m}$ where L is in units of millimeters. The angles between the surface normals for the two pairs of crystal faces to be exposed to the neutron beam varied between 179.93° to 179.98° . Figure 4 shows two of the crystals resting on the coordinate measuring machine surface. Figure 5 shows an example map of the surface flatness deviations for one surface on one of the test masses.

5. Experimental details

The density gradients in two nominally identical samples of PbWO_4 crystals were measured at the NCNR Cold Neutron Imaging Facility (CNIF) [14] at the National Institute of Standards and Technology in Gaithersburg, MD. Figure 6 shows one of the PbWO_4 crystals mounted on the apparatus. The PbWO_4 crystals, both of nominal dimensions $2.3 \text{ cm} \times 2.3 \text{ cm} \times 12 \text{ cm}$, were purchased from the Shanghai Institute of Ceramics in Shanghai, China. The crystal is grown along the (001) lattice direction. PbWO_4 has a body-centered tetragonal crystallographic structure with lattice parameters $a = 0.54619 \text{ nm}$ and $c = 1.2049 \text{ nm}$ (ICDD card n.19-708).

The neutron beam from the NG-6 cold neutron guide was prepared by diffraction from a double-crystal pyrolytic graphite monochromator and had a mean neutron wavelength of 4.4 Angstroms. The Talbot-Lau interferometer consists of two vertical gratings G_0 and G_1 separated by 3.5 m, an absorption analyzer grating G_2 located at the Talbot-Lau self-image location $d_T/8$ where d_T is the Talbot length, and an imaging detector (described below) in contact with G_2 . The gratings employ Gd coatings to absorb the neutrons. Gadolinium is used for this purpose in view of its extremely high neutron absorption cross section. The initial absorption grating G_0 consists of $5 \mu\text{m}$ thick Gd lines on a $774 \mu\text{m}$ period with a duty cycle of 60%. G_1 is a phase modulation grating with $32 \mu\text{m}$ deep trenches etched in Si with a period of

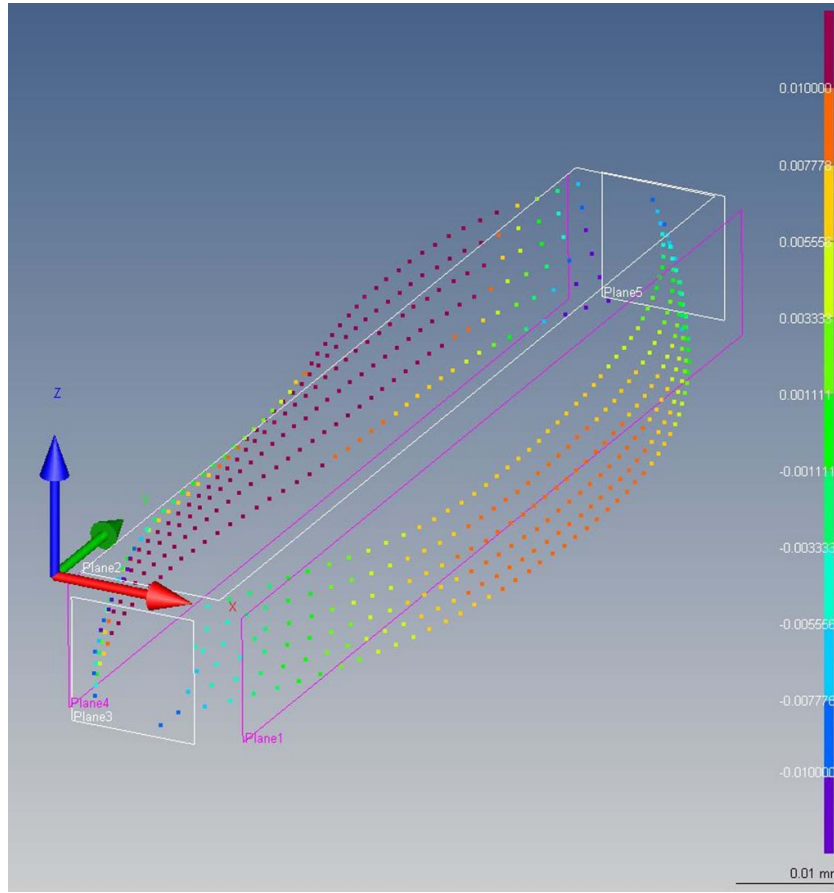


Figure 5. Example map of the surface flatness deviations for two opposing pairs of one of the crystal surfaces as measured by the NIST coordinate measuring machine. The color code on the right extends over a full range of ± 0.01 mm. The size of the measured deviations on the other surfaces of the test masses is similar.

$7.94 \mu\text{m}$ with 50% duty cycle. G_2 is an absorbing analyzer grating with $4 \mu\text{m}$ period and $3 \mu\text{m}$ high Gd lines. It is placed about 18.1 mm downstream of G_1 , which corresponds to the $1/8$ th Talbot distance $(7.94^2)/(8 \times 0.44 \text{ nm})$ in close proximity to the scintillator screen. The gratings were made at the NIST Center for Nanoscale Science and Technology nanofabrication facility and are described in the literature [15]. Gratings G_0 and G_1 are mounted on 6-axis manipulation stages to enable alignment with the neutron optical axis. The scintillator screen is $150 \mu\text{m}$ thick LiF:ZnS scintillator purchased from Applied Scintillator Technologies (now Scintacor). The camera is an Andor NEO sCMOS with $6.5 \mu\text{m}$ pixel pitch, viewing the scintillator via a Nikon 50 mm f/1.2 lens for a detector pixel pitch of about $51.35 \mu\text{m}$, geometric magnification gives an effective pixel pitch of $51.48 \mu\text{m}$.

The phase gradient images were obtained by stepping G_0 through one grating period in 21 equidistant steps in the x direction. The sample was alternately translated into and out of the neutron beam periodically. The median of 3 images was taken to rid the image of spurious background events in the zinc sulfide scintillator induced by gamma rays interacting with the camera from cosmic rays and from the ambient neutron capture gamma background in

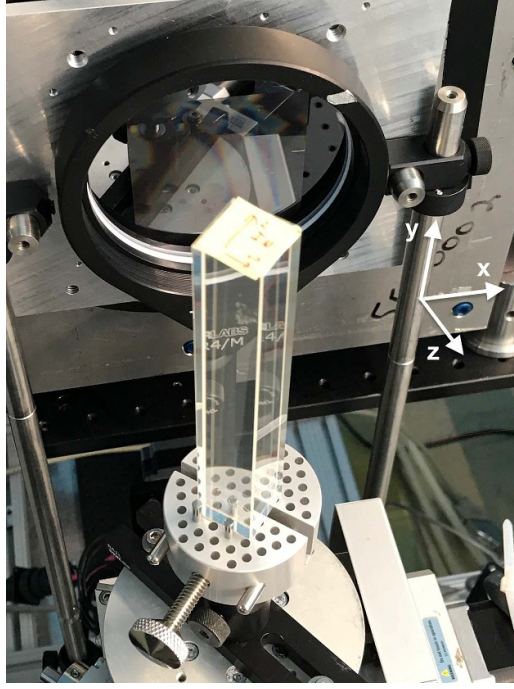


Figure 6. One of the PbWO_4 crystals mounted in the NIST CNIF beamline. G_2 is visible.

the neutron guide hall facility. After background subtraction, the amplitude and phase of the signals in each pixel of the image were fit using an analysis procedure described by [16] and implemented at CNIF in the Matlab analysis environment.

For the i th measurement sequence the phase shift is calculated as

$$\Delta\Phi_i = \Phi_i - \frac{1}{2} \left(\Phi_{\text{open}_{i-1}} + \Phi_{\text{open}_{i+1}} \right)$$

where Φ_i is the phase shift of the sample for the i th sequence, $\Phi_{\text{open}_{i-1}}$ and $\Phi_{\text{open}_{i+1}}$ are the phase shifts of the $(i-1)$ th and $(i+1)$ th sequences when the sample was out of the beam. The phase gradient for the sample is found by averaging over the individual calculated gradients.

The Talbot-Lau self image phase shift is obtained by fitting a sine curve to the measured phase stepping data using the software package GPUFIT [17]. The phase gradient of the sample is obtained from the difference of the sample to the open beam. The repeat measurements were averaged on a pixel-by-pixel basis using the propagated uncertainty. The profile was generated by taking the weighted average over 1000 rows. The resulting 1-sigma uncertainty was about 10^{-4} . This is about a factor of 2 larger than a simple estimate based on Poisson counting statistics of 5×10^{-5} based on the fluence rate, the total averaging time (45 s, 21 phase steps) and averaging area (about $0.05 \text{ mm} \times 50 \text{ mm}$) as reported in table 2. Our uncertainty is sufficient to resolve the estimated size of the self image which is

$$\theta_T = 2 \frac{Nb_c \lambda^2 d \tan(\beta)}{p_2} = 0.0715 \text{ rad.} \quad (1)$$

Table 2. List of parameters.

Parameter	Value
Pixel pitch	51.35 μm
Height of ROI (Sample 1)	5.135 cm (1000 $\times$ Pixel pitch)
Height of ROI (Sample 2)	5.109 cm (995 $\times$ Pixel pitch)
Neutron fluence	$10^6 \text{ cm}^{-2} \text{ s}^{-1}$
Number of phase steps	21
Sampling time	45 s
Density	8.30 g cm^3
Wavelength(λ)	4.4 $\text{\AA}$
1/8th Talbot distance ($d_T/8$)	1.82 cm
Grating period (p_2)	$4.0 \times 10^4 \text{ \AA}$
Inclination (β)	45°
Scattering length density (Nb_c)	$4.106 \times 10^6 \text{ \AA}^{-2}$

From figure 7 the observed θ_T is about 0.07 rad, indicating that the sample is slightly misaligned from the maximal 45° inclination (about 0.5°).

6. Analysis

Figures 7 and 8 show the averaged phase gradients for one of the PbWO_4 samples. The opposite signs for $\frac{\partial\Phi}{\partial x}$ on either side of the image are exactly as expected for the 45° -inclined square cross sectional area sample employed. These images resolve a very small but nonzero transverse gradient in $\frac{\partial\Phi}{\partial x}$ with the same magnitude and sign on both sides. For $0.4 \text{ cm} < x < 1.2 \text{ cm}$ one can calculate the slope of the phase gradient of $d/dx[\frac{\partial\Phi}{\partial x}] = 1.9 \times 10^{-3} \text{ rad cm}^{-2}$. Using the relation $\Phi = Nb_c\lambda L$, differentiating twice, and neglecting possible gradient terms in N and L quadratic in x , one picks out the term $2b_c\lambda \frac{\partial L}{\partial x} \frac{\partial N}{\partial x}$ of interest in this work.

The slope of this phase gradient therefore places an upper bound on the fractional density gradient in the PbWO_4 of $\frac{1}{N} \frac{dN}{dx} < 0.5 \times 10^{-6} \text{ cm}^{-1}$. The value on the other side of the image is similar. This value is about two orders of magnitude smaller than required for future G measurements.

7. Conclusions and future work

We have used a neutron Talbot-Lau interferometer to place an upper bound on the internal density gradient in macroscopic crystals of PbWO_4 of $\frac{1}{N} \frac{dN}{dx} < 0.5 \times 10^{-6} \text{ cm}^{-1}$. This density gradient bound is consistent with the order-of-magnitude one might expect from the level of impurities in commercially-available PbWO_4 crystals. The size of the phase gradient is also consistent with the NIST coordinate measuring machine measurements of the small deviations of the shape of the crystals away from our assumed geometry. This density gradient value is about two orders of magnitude smaller than what is needed in typical macroscopic mechanical apparatus of the type often used to measure G .

The same two PbWO_4 crystals used in this neutron interferometer study have also recently been measured using a laser interferometer [18]. The density gradient was quantified in terms of variation in the interference fringes as a laser beam scanned the crystals. The orientation of the crystal in the optical interferometer was kept similar to the orientation used in the neutron measurement. The upper bound on internal density gradients from the optical interferometer

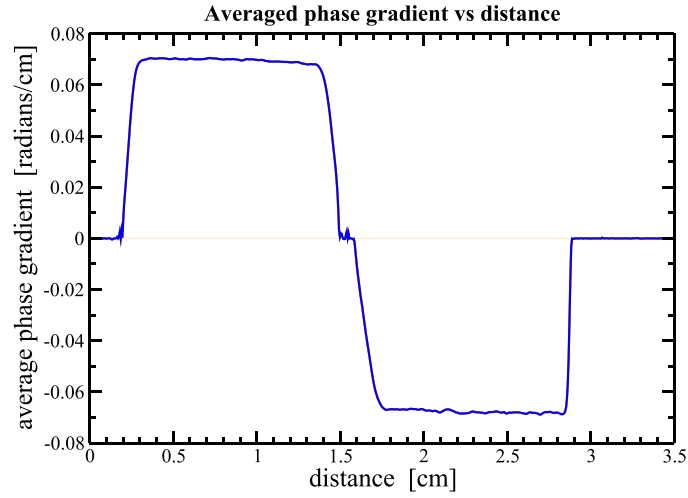


Figure 7. Phase gradient image of the PbWO_4 sample measured by the Talbot-Lau neutron interferometer.

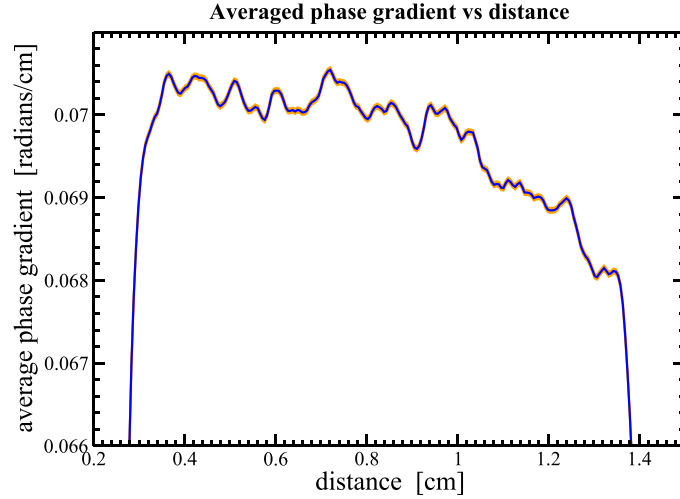


Figure 8. Closeup view of the phase gradient image of the PbWO_4 sample measured by the Talbot-Lau neutron interferometer. A small but nonzero change in the phase gradient is visible.

measurements is $\frac{1}{N} \frac{dN}{dx} < 2.1 \times 10^{-8} \text{ cm}^{-1}$. This upper bound is consistent with and more sensitive than the upper bound obtained in this neutron measurement by about a factor of 25. This result along with a detailed description of the measurement has been published [18]. We conclude that PbWO_4 is a strong candidate for use as a test mass in future G measurements.

The same measurement methods used in this work would also work for many other candidate G test mass materials. The neutron measurements of course are not restricted to optically transparent materials and could also be used to nondestructively inspect opaque dense test masses as well. If one wanted an independent confirmation of the results in this case one would need to employ another probe which could penetrate the required thickness of material.

This can be done using traditional gamma ray transmission radiography. A gamma ray radiography facility at Los Alamos can routinely penetrate several centimeters of dense material and resolve internal voids at the millimeter scale [19]. It has also recently been shown that an epithermal neutron beamline imaging facility at Los Alamos can at the same time also perform gamma imaging with a comparable spatial resolution. At a spallation neutron source such imaging beams possesses an intense gamma flash when the GeV energy proton beam strikes a high Z target to liberate neutrons by spallation, and the imaging detectors possess both neutron and gamma sensitivity. All three of these methods (neutron and optical phase contrast imaging and gamma transmission) are nondestructive and can therefore in principle be applied to the same G test mass used in the actual experimental measurements. We are therefore encouraged to think that we are close to establishing a method which can address one of the common potential systematic error sources in measurements of G .

Data availability statement

The data that support the findings of this study are available upon reasonable request from the authors.

Acknowledgments

We would like to thank D Newell and S Schlamminger of the National Institute of Standards and Technology in Gaithersburg, MD for their help in arranging the coordinate measuring machine work. K T A Assumin-Gyimah, D Dutta, and W M Snow acknowledge support from US National Science Foundation Grant PHY-1707988. W M Snow acknowledges support from US National Science Foundation Grants PHY-1614545 and PHY-1708120 and the Indiana University Center for Spacetime Symmetries. C Langlois was supported by the NSF Research Experiences for Undergraduates program.

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