

Addendum: Automated consistent truncations and stability of flux compactifications

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The expressions (2.19) and (2.20) for the scalar potentials obtained from type IIA and IIB supergravity could be improved to the following ones

$$\begin{aligned}
 V^{\text{IIA}}(\varphi^i) = & \frac{M_p^2}{2} \frac{e^{2\phi}}{\text{vol}_6} \left(-R_6 + \frac{1}{2} |H_3|_{\text{int}}^2 - e^\phi \sum_{p=4,6,8} \frac{T_{10}^{(p)}}{p+1} \right. \\
 & + \frac{e^{2\phi}}{2} \left[F_0^2 + |F_2 + F_0 B_2|_{\text{int}}^2 + \left| F_4 + C_1 \wedge H_3 + F_2 \wedge B_2 + \frac{1}{2} F_0 B_2 \wedge B_2 \right|_{\text{int}}^2 \right. \\
 & \left. \left. + \left| F_6 + C_3 \wedge H_3 + F_4 \wedge B_2 + C_1 \wedge H_3 \wedge B_2 + \frac{1}{2} F_2 \wedge B_2 \wedge B_2 + \frac{1}{6} F_0 B_2 \wedge B_2 \wedge B_2 \right|_{\text{int}}^2 \right] \right)
 \end{aligned}$$

in type IIA and

$$\begin{aligned}
 V^{\text{IIB}}(\varphi^i) = & \frac{M_p^2}{2} \frac{e^{2\phi}}{\text{vol}_6} \left(-R_6 + \frac{1}{2} |H_3|_{\text{int}}^2 - e^\phi \sum_{p=3,5,7,9} \frac{T_{10}^{(p)}}{p+1} \right. \\
 & + \frac{e^{2\phi}}{2} \left[|F_1|_{\text{int}}^2 + |F_3 - C_0 \wedge H_3 + F_1 \wedge B_2|_{\text{int}}^2 \right. \\
 & \left. \left. + \left| F_5 - C_2 \wedge H_3 + F_3 \wedge B_2 - C_0 \wedge H_3 \wedge B_2 + \frac{1}{2} F_1 \wedge B_2 \wedge B_2 \right|_{\text{int}}^2 \right] \right)
 \end{aligned}$$

in type IIB. There, one uses the definition

$$\frac{M_p^2}{2} \frac{T_{10}^{(p)_I}}{p+1} = \frac{1}{(2\pi)^3(\alpha')^2} (2^{p-5} N_{O_p}^I - N_{D_p}^I) \frac{vol B_{p-3}^I}{vol_6},$$

slightly modifying (2.17). In addition, the fluxes appearing in these scalar potentials are given by (the internal forms in) (2.2) including axion terms, and the gauge fields B_2 and C_q contain only 4d axions. These expressions for the scalar potentials match those used in the code **MSSV**, and have been successfully tested against 10d equations as discussed in section 4.

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