

1 Choice type impacts human reinforcement learning

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4 Abstract

5 In reinforcement learning (RL) experiments, participants learn to make rewarding choices
6 in response to different stimuli; RL models use outcomes to estimate stimulus-response
7 values which change incrementally. RL models consider any response type indiscrim-
8 inately, ranging from more concretely defined motor choices (pressing a key with the
9 index finger), to more general choices that can be executed in a number of ways (se-
10 lecting dinner at the restaurant). But does the learning process vary as a function of
11 the choice type? In Experiment 1, we show that it does: participants were slower and
12 less accurate in learning correct choices of a general format compared to learning more
13 concrete motor actions. Using computational modeling, we show that two mechanisms
14 contribute to this. First, there was evidence of irrelevant credit assignment: the values
15 of motor actions interfered with the values of other choice dimensions, resulting in more
16 incorrect choices when the correct response was not defined by a single motor action; sec-
17 ond, information integration for relevant general choices was slower. In Experiment 2, we
18 replicated and further extended the findings from Experiment 1 by showing that slowed
19 learning was attributable to weaker working memory use, rather than slowed RL learn-
20 ing. In both experiments we ruled out the explanation that the difference in performance
21 between two condition types was driven by difficulty/different levels of complexity. We
22 conclude that defining a more abstract choice space used by multiple learning systems
23 for credit assignment recruits executive resources, limiting how much such processes then

24 contribute to fast learning.

25

26

Introduction

27 The ability to learn rewarding choices from non-rewarding ones lies at the core of suc-
28 cessful goal-directed behavior. But what counts as a choice? When a child tries a pink
29 yogurt in the left cup and a white yogurt in the right cup, then prefers the right cup, what
30 choice should they credit this rewarding outcome to? In their next decision, should they
31 repeat their previously rewarding reach to the yogurt on the right, independently of its
32 color, or should they figure out where the white yogurt is before reaching for it? Selecting
33 the type of yogurt is a more abstract choice: it requires subsequently paying attention
34 to the other dimension (where is the white yogurt?) and applying the appropriate motor
35 program to execute the choice. Thus, making the more abstract choice additionally in-
36 volves less abstract choices, but in this case, only the abstract choice should be credited
37 for the yogurt's tastiness. Knowing the relevant dimension of choice to assign credit to
38 is essential when learning. How does choice type impact how we learn?

39 The theoretical framework of reinforcement learning (RL) is highly successful for
40 studying reward-based learning and credit assignment (Sutton et al., 2018). However,
41 RL as a computational model of cognition typically assumes a given action space defined
42 by the modeler, which provides the relevant dimensions of the choice space (i.e. either
43 the yogurt color or the cup position) - there is no ambiguity in what choices are (i.e. color
44 such as pink/white, or side such as left/right), and the nature of the choice space does not
45 matter (Rmus et al., 2021). As such, RL experiments in psychology tend to not consider
46 the type of choices (a single motor action such as pressing a key with the index finger;
47 (Collins et al., 2017; Tai et al., 2012), or the more general selection of a goal stimulus that
48 is not tied to a specific motor action (Daw et al., 2011; Foerde et al., 2011; Frank et al.,
49 2007)) as important, and researchers use the same models and generalize findings across
50 choice types. Recent research has shed some light on how participants might identify
51 relevant dimensions of the state and choice space (Farashahi et al., 2017; Niv, 2019);
52 however, this research does not address how learning occurs when the learner knows the
53 relevant choice space but multiple dimensions of choice are nonetheless available, such as
54 in our yogurt example.

55 Examining learning of responses when multiple choice dimensions may be relevant is
56 important, however, as most of our choices in everyday life are ambiguous: did I pick the

57 white yogurt or the one of the left? In some cases, these dimensions are hierarchically
58 interdependent: choices can be represented at multiple levels of abstraction (e.g. have
59 breakfast; have yogurt; have pink yogurt; have the yogurt on the right; reach for the
60 yogurt on the right side, etc.). In such cases, a choice along a relevant dimension (yogurt
61 color) requires a subsequent choice on a reward-irrelevant dimension (position/motor
62 action), which then needs to be considered for the choice's execution, but not credited
63 during learning. By contrast, in other cases, some choice dimensions may neither be
64 relevant for learning nor for executing the choice – for example, the child should learn
65 to fully ignore the color of the plate that the yogurt is on for both their choice and their
66 credit assignment.

67 Different types of choices may recruit different cognitive/neural mechanisms (Rescorla
68 et al., 1967). For example, previous animal models of decision-making suggest that
69 the orbitofrontal cortex and the anterior cingulate cortex index choice outcomes for
70 goal stimulus choices and motor action choices respectively (Luk et al., 2013). Ventral
71 striatum lesions in monkeys impaired learning to choose between rewarding stimuli, but
72 not between rewarding motor actions (Rothenhoefer et al., 2017). In humans, recent
73 behavioral evidence suggests that the credit assignment process is what differentiates
74 learning more relevant choice dimensions from less relevant (here motor) ones (McDougle
75 et al., 2016), and that there might be a hierarchical gradation of choices in terms of credit
76 assignment. In particular, while people are capable of learning the value of both abstract
77 rule choices and concrete action choices in parallel (Ballard et al., 2018; Eckstein et al.,
78 2019), they also seem to assign credit to more concrete actions by default when making
79 abstract choices that need to be realized through motor actions (Shahar et al., 2019).

80 The brain relies on multiple neuro-cognitive systems for decision-making, but whether
81 choice format impacts learning similarly across systems remains unexplored. Specifically,
82 while RL models provide a useful formalism of learning, they do not easily relate to
83 underlying processes. Indeed, RL models are known to summarize multiple processes that
84 jointly contribute to learning (Eckstein et al., 2021), such as the brain's RL mechanism,
85 but also episodic memory (Bornstein et al., 2013; Bornstein et al., 2017; Poldrack et al.,
86 2001; Vikbladh et al., 2019; Wimmer et al., 2012), or executive functions (Collins et al.,
87 2012; Rmus et al., 2021). Here we focus on working memory (WM), which has also
88 been shown to contribute to learning alongside RL (Collins et al., 2017; Collins et al.,
89 2012; 2018). If choice type matters for learning, does it matter equally for each cognitive
90 system that contributes to learning, or differently so?

91 In summary, there is a two-fold gap in our understanding of how choice format impacts
92 learning. First, when multiple choice dimensions are available but only one is relevant,

93 does the type of the relevant choice dimension impact learning, and if so, through what
94 computational mechanisms? We consider, in particular, the important case where one
95 relevant choice dimension needs to be executed through a second, irrelevant choice di-
96 mension (a motor action); and how this contrasts to learning when one dimension is
97 fully irrelevant to both choice and learning. Second, are the differences rooted in the
98 brain’s RL system, WM, or both? To address this gap, we designed a task that directly
99 compares learning to make choices along two orthogonal dimensions, with different levels
100 of generality or interdependence, when there is no ambiguity about which choices are
101 relevant to the learning problem. In our task, one choice dimension is a spatial position
102 that directly maps onto a consistent motor action, and the other is a more general choice
103 dimension, conceptualized as the selection of stimulus goals that constrain a downstream
104 selection of an overall irrelevant spatial position and corresponding motor action. In a
105 second experiment, we manipulated learning load to separately identify WM and RL con-
106 tributions to learning, and investigated with computational modeling how choice matters
107 in both systems.

108 Our results across two experiments suggest that choice type strongly impacted learn-
109 ing, resulting in slower learning when the relevant choice dimension was more general
110 and required execution along another dimension. This was in part driven by an incorrect,
111 asymmetric credit assignment to less general choices when they were irrelevant. Further-
112 more, WM (rather than RL) mechanisms seemed to drive the deficits in performance in
113 the more general choice format condition, indicating that defining a more general action
114 space, shared by multiple choice systems, recruited limited executive resources. In both
115 experiments, we ruled out the simple explanation that the performance difference was
116 driven by an effect of difficulty by 1) implementing experimental controls that minimize
117 this concern, and 2) ruling out predictions of a pure difficulty effect in analyses and
118 modeling.

119 Methods

120 Participants

121 Experiment 1

122 Our sample for Experiment 1 consisted of 82 participants (40 female, age mean (SD)
123 = 20.5(1.93), age range = 18-30) recruited from the University of California, Berkeley
124 Psychology Department’s Research Participation Program (RPP). We based our sam-

125 ple size on samples from previous similar behavioral experiments (Collins, 2018): 91
126 participants; (Collins et al., 2014):85 participants; (Collins et al., 2012):78 participants).
127 In accordance with the University of California, Berkeley Institutional Review Board
128 policy, participants provided written informed consent before taking part in the study.
129 They received course credit for their participation. To ensure that the participants in-
130 cluded in analyses were engaged with the task, we set up an exclusion criterion of 0.60
131 or greater average accuracy across all task conditions. This cutoff was determined based
132 on an elbow point in the group's overall accuracy in the task (Fig. 12). We excluded 20
133 participants based on this criterion, resulting in a total sample of 62 participants for the
134 reported analyses.

135 Experiment 2

136 For the second experiment, we recruited 75 participants (54 female, 1 preferred not to
137 answer; age mean (SD) = 20.34(2.4), Age-range=18-34) from the University of Califor-
138 nia, Berkeley RPP. One of the prerequisites for participating in Experiment 2 was that
139 participants had not previously taken part in Experiment 1. We also relied on previous
140 research to decide on the sample size, as in Experiment 1. Participants completed the
141 experiment online (De Leeuw, 2015), and received course credit for their participation.
142 Using the same exclusion criteria as the previous experiment (based on the distribution
143 of average accuracy), we excluded 18 participants, resulting in the total sample of 57
144 participants.

145 Experimental protocol

146 Experiment 1

147 Learning Blocks. Participants were instructed that they would be playing a card sort-
148 ing game, and that on each trial they would sort a card into one of three boxes. Their
149 goal was to use reward feedback to learn which box to sort each card into. The boxes
150 were labeled with 3 different colors (green, blue and red), and participants chose one of
151 the boxes by pressing one of three contiguous keyboard keys (corresponding to the box
152 position) with their index, middle and ring finger. Importantly, the color of the boxes
153 changed positions on different trials (i.e. the blue box could appear on the right side
154 on trial n, and in the middle on trial n+1). Participants received deterministic feedback
155 after each selection (+1 if they selected the correct box for the current card, 0 otherwise).

156

157 Before the experiment, participants read detailed instructions and practiced each task
158 condition. The task then consisted of 8 blocks, divided into three conditions. Each of
159 the three conditions was defined by its distinct sorting rule. In the label condition, the
160 correct box for a given card was defined deterministically by the box's color label (Fig.
161 1A). For instance, if the blue box was the correct choice for a given card, participants
162 were always supposed to select the blue box in response to that card, regardless of which
163 key mapped onto the blue box on a given trial. In the position condition, the correct
164 box was defined deterministically by the box's position (left/middle/right). For example,
165 the correct response of a given card would always be achieved by pressing the leftmost
166 key with the index finger, regardless of the box color occupying the left position (Fig.
167 1B). The sorting rule in the position control condition was identical to the sorting rule in
168 the position condition, but the boxes were not tagged with color labels. This condition
169 allowed us to assess participants' baseline performance when only one response type (e.g.
170 position, but not the label) was available. Importantly, participants were explicitly told
171 the sorting rule (position or label) at the beginning of each block, in order avoid any
172 performance variability that may arise as a function of rule inference and uncertainty.
173 Following the 8 learning blocks, participants performed two additional tasks; these are
174 not the focus of the current paper and are not analyzed here.

175 Out of 8 blocks in total, 2 were control condition blocks, 3 were position condition,
176 and 3 were label condition. Block order was pseudo-randomized: participants completed
177 a control block first and last, while the conditions of blocks 2-7 were randomly chosen
178 within subjects, but counterbalanced across subjects. In each block, participants learned
179 how to sort 6 different cards; we used a different set of images to represent cards in
180 each block. The boxes were labeled with the same 3 colors across all blocks, except
181 the position control blocks, where the boxes were not labeled. Participants experienced
182 15 repetitions of each card, resulting in 90 trials per block; trial order was pseudo-
183 randomized to ensure a uniform distribution of delays between repetitions of the same
184 card in a block. We controlled for the card-dependent position-label combinations across
185 trials. Specifically, each label occurred in each position an equal number of times (i.e.
186 the blue label occurred 5 times on the left, right and middle box for each card). We also
187 ensured that the position-label combinations were evenly distributed across the task (i.e.
188 the blue-middle combination did not occur only during the first quarter of block trials).

189 Single trial structure. On each trial, participants first saw the three boxes with their
190 color labels underneath a fixation cross at the center of the screen. After 1 second, the
191 card appeared in the center of the screen, replacing the fixation cross. Participants were

allowed to press a key only when the card appeared, with a 1-second deadline. Following their response, participants received feedback (+1 or 0) that remained on the screen for 1 second, followed by a 1 second inter-trial interval (fixation cross). This trial structure was designed to mitigate the concern that condition-based differences in performance might stem from the label condition being more difficult, by giving participants time to identify where each color label was positioned. This minimizes a potential advantage of the position condition, where participants did not need to know where colors were on a trial-by-trial basis in order to make a correct response. Giving participants time to identify where each color is positioned prior to card presentation decreases the difference between the conditions in terms of difficulty, making this confound less likely.

We designed the label and position conditions to engage choice processes with different degrees of generality. The position condition should capture the less general choice process in which the rewarding response is defined by a single motor action, and the label is irrelevant to both choice and learning. The label condition, on the other hand, captures a more general choice process in which the rewarding response (i.e. choice of the correct label) can be made by identifying one of three positions and executing any of the three motor actions, depending on where the correct box label is positioned on the given trial, such that the other dimension (position) remains irrelevant for learning but becomes relevant for choice.

Experiment 2

The task design for Experiment 2 was the same as the task design for Experiment 1, with one important exception - we varied the number of cards per block between 2 and 5, for both position and label conditions. This manipulation has previously been shown to enable computational modeling to disentangle working memory and reinforcement learning processes (Collins et al., 2012). The order of blocks was counterbalanced across participants; they completed either label or position blocks first, with the order of set sizes randomized for the first completed condition, and then repeated for the second. In addition, we removed the control condition, given that we previously observed no difference between position and control. Participants completed 4 blocks of position and label each, where each block within each condition had a different set size.

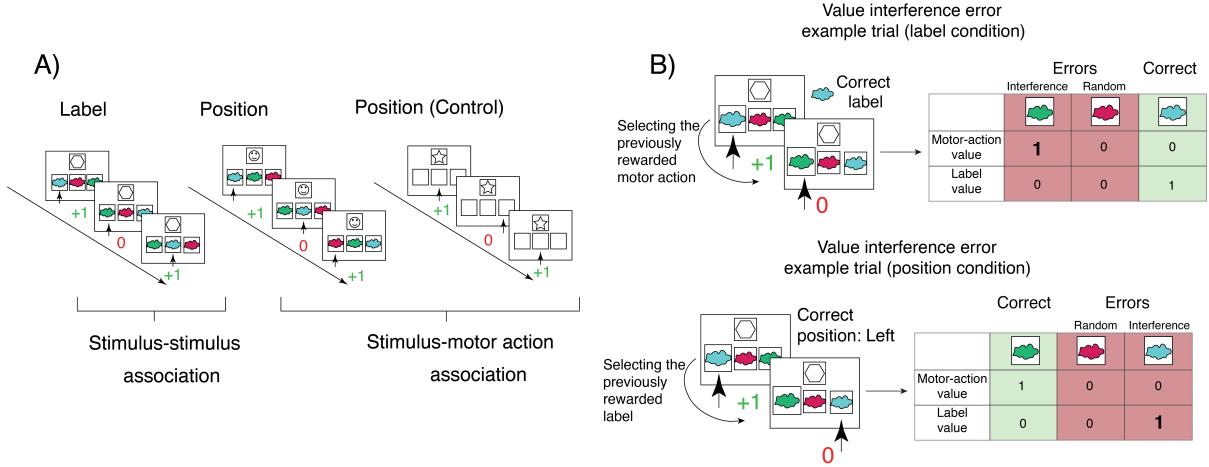


Figure 1: Experiment design. A) Participants played a card-sorting game with 3 different conditions: Label (learning which box color is correct for each card - more general choice), Position (learning which motor action/position is correct for each card - less general choice), Control (identical sorting rules as position condition, but without labeled boxes). B) We assumed that participants track card-dependent reward history for both positions and labels, and that both of these contribute to the choice selection process, sometimes resulting in interference errors. Note that the card-dependent reward history is cumulative (tracked across all past trials during which the given card was presented, rather than only one-trial back), but for simplicity of illustration we only show 1-back trial in the panel B.

222 Analyses

223 Model-independent analyses

224 In addition to general diagnostics and standard statistical analyses (see results), we
 225 sought to analyze participants' choices and response times (RT) as a function of how
 226 often each motor action and each label had been rewarded for each card. Specifically,
 227 we computed card-dependent cumulative reward history (CRH) for both positions P and
 228 labels L on each trial for a card C , in each condition:

$$\begin{aligned}
CRH_k^P(C, P) &= \sum_{k=1}^t (r_k * 1(Card_k = C, Choice_k = P)) \\
CRH_k^L(C, L) &= \sum_{k=1}^t (r_k * 1(Card_k = C, Choice_k = L)),
\end{aligned} \tag{1}$$

229 where r_k is the outcome at trial k in the block, and 1 is the indicator function that
230 takes a value of 1 if the card and position/label match C and P/L, and 0 otherwise.
231 We used this metric to analyze how the integration of two value sources shaped choices
232 when choice format was less/more general. In particular, in the example of the position
233 condition, the position CRH for a card and its associated correct position indicated the
234 past number of correct choices, while the CRH for other positions was 0. By contrast, in
235 the same position condition, the label CRH for a card reflected how often each label had
236 been rewarded due to this label being in the correct position. All label CRH values in the
237 position condition were expected to be close to each other because label positions were
238 counterbalanced, but slight differences due to past choice randomness could be predictive
239 of biases in future choice. The opposite was true in the label condition.

240 To analyze how the value integration for each type of choice shaped decisions, we
241 focused on the error trials and computed the proportion of errors driven by the other
242 irrelevant choice dimension. We reasoned that if participants were randomly lapsing, any
243 of the two possible errors should be equally likely. However, if participants experienced
244 value interference, they should be more likely to select the error with the higher CRH
245 in the irrelevant dimension. In the label condition, such an interference error would
246 look like selecting the position/motor action that was rewarded on the previous trial,
247 even though the correct label had switched positions since (Fig. 1B). In the position
248 condition, an interference error would occur when participants selected the previously
249 rewarded label that had switched positions, instead of the label currently corresponding
250 to the position/motor action that is always correct for the given card (Fig. 1B).

251 We ran a trial-by-trial analysis using a mixed-effects general linear model to char-
252 acterize choices. We used trial-by-trial reward history difference $RHD = CRH(chosen) -$
253 $mean(CRH(unchosen))$ between chosen and unchosen boxes, for both positions and la-
254 bels, and tested whether this discrepancy modulated accuracy and RTs. If participants
255 implemented an optimal decision strategy, their accuracy and RTs should increase and
256 decrease respectively with an increased RHD in the relevant choice dimension (i.e. label
257 RHD in label condition, position RHD in position condition). Alternatively, contribution
258 by the irrelevant dimension RHD (i.e. position RHD in label condition or vice versa)

259 would serve as evidence of value interference. Our mixed-effects models had the following
260 general structure:

261

$$\begin{aligned} \text{Performance} = & 1 + \beta_1 pRHD + \beta_2 lRHD + \beta_3 t + \beta_4 block + \\ & (1 + \beta_1 pRHD + \beta_2 lRHD + \beta_3 t + \beta_4 block | Subject), \end{aligned} \quad (2)$$

262 where $pRHD$ is RHD based on position reward history, and $lRHD$ is RHD based on label
263 reward history. Performance can refer to either accuracy (coded as correct/incorrect) or
264 response times.

265 In the analysis of Experiment 2 data, we also ran mixed-effects models including
266 predictors that indexed WM mechanisms (set size and delay between presentations of
267 the current stimulus and the most recently rewarded stimulus, which respectively cor-
268 respond to indexing capacity and susceptibility to decay properties of WM), and RL
269 effects (dimension-relevant, card-dependent reward history, calculated from the cumula-
270 tive number of earned points for each card, indexing reward-based learning):

$$\begin{aligned} \text{Performance} = & 1 + \beta_{RL} RL + \beta_{WM} WM + \beta_t t + \beta_b block + \\ & (1 + \beta_{RL} RL + \beta_{WM} WM + \beta_t t + \beta_b block | Subject), \end{aligned} \quad (3)$$

271 where RL corresponds to RL factors such as reward history, and WM corresponds to
272 WM factors such as decay and set size. Note that this is a general structure to demon-
273 strate how we structured the mixed-effects model, but set size and decay were entered
274 as separate predictors.

275 In other words, we explored the effects of interest on a group level, as well as how the
276 estimates of these effects vary across individual participants. We included a predictor
277 for trial number in this model, to ensure that reduction in RTs is not simply conflated
278 with practice effects/task progression. In addition, we added block number as one of the
279 regressors, in order to capture overall improvement in performance across the task.

280 Computational modeling

281 Reinforcement Learning-Working Memory (RL-WM): In order to computationally quan-
282 tify the differences in learning processes between the motor choice/general choice condi-
283 tions, we used a set of hybrid reinforcement learning (RL) and working memory (WM)

284 models. Our baseline assumption was that in the RL process, participants track and
 285 update two independent sets of stimulus-action value tables, corresponding to the two
 286 possible choice spaces: a card-position value table, and a card-label value table. We
 287 also assumed that the choice policy may reflect a mixture of both the relevant and the
 288 irrelevant value tables, potentially leading to interference errors when the value of ir-
 289 relevant choice dimension (position/label) contributes to the choice process (Fig. 2A).
 290 In addition to the RL module, a WM module allows us to capture the contribution of
 291 WM to performance. The WM memory module learns fast, but is sensitive to short
 292 term forgetting and cognitive load, and is thus particularly identifiable in the second
 293 experiment where the set size varies between 2 and 5 (Collins, 2018; Collins et al., 2012;
 294 2018). WM also potentially tracks associations between cards and two choice types, and
 295 like RL, its policy may reflect a mixture of both relevant and irrelevant associations. We
 296 investigated a range of models to pinpoint the computational mechanisms of divergence
 297 between the learning processes in the two conditions, by varying the extent to which the
 298 models allowed for condition-dependent specificity/model-parameters.

299

300 RL learning rule

301 The RL module assumes incremental learning through a simple delta rule (Sutton et al.,
 302 2018). Specifically, on each trial t , the values of labels $Q_L(c, l)$ and positions $Q_P(c, p)$ for
 303 the trial's card c and chosen labels and positions l and p are updated in proportion to
 304 the reward prediction error:

$$\begin{aligned}
 Q_{t+1}^P(c, p) &= Q_t^P(c, p) + \alpha * (r - Q_t^P(c, p)) \\
 Q_{t+1}^L(c, l) &= Q_t^L(c, l) + \alpha * (r - Q_t^L(c, l)),
 \end{aligned} \tag{4}$$

305 where α is the learning rate, and $r = 0/1$ is the outcome for incorrect and correct
 306 trials. Q -tables are initialized at 1/3 (3 = total number of positions/labels) at the start
 307 of each block to reflect initial reward expectation in the absence of information about
 308 new cards.

309 WM learning rule

310 Unlike RL, WM processes can encode and retain the previous trial's information perfectly,
 311 thus enabling one-shot learning. Note that other cognitive processes (such as episodic

312 memory) could also support one-shot learning and contribute to learning behavior in this
 313 experiment; however, here, we focus on RL and WM processes only, as our protocol does
 314 not allow us to disentangle other contributions (Yoo et al., 2022). Following previous
 315 work (Collins, 2018; Collins et al., 2014; Collins et al., 2012), we model the one-shot
 316 learning in WM by storing the immediate outcome as the stimulus-response weight:

$$\begin{aligned} W_{t+1}^P(c_t, p_t) &= r_t \\ W_{t+1}^L(c_t, l_t) &= r_t, \end{aligned} \quad (5)$$

317 Prior work in similar tasks (Frank et al., 2007; Gershman, 2015; Katahira, 2018; Niv et
 318 al., 2012) has shown an asymmetry in learning based on positive/negative feedback, such
 319 that individuals are less likely to integrate negative feedback while learning rewarding
 320 responses. Thus, we included a learning bias parameter ($0 \leq LB \leq 1$), which scales the
 321 learning rate α by LB when participants observe the negative feedback. We applied LB
 322 to both RL and WM (for both position and label dimensions, showing only an example
 323 for position here):

$$\begin{aligned} Q_{t+1}^P(c, p) &= Q_t^P(c, p) + LB * \alpha * (0 - Q_t^P(c, p)) \\ W_{t+1}^P(c, p) &= W_t^P(c, p) + LB * (0 - W_t^P(c, p)), \end{aligned} \quad (6)$$

324 To capture the phenomenon that maintenance of information in WM is short-term
 325 and subject to interference, the weights stored in WM are susceptible to decay (ϕ) at
 326 each trial, which pulls all position and label weights to their initial values (W^{P_0}, W^{L_0})
 327 following the application of the WM forgetting rule (5):

$$\begin{aligned} W_{t+1}^P &= W_t^P + \phi * (W^{P_0} - W_t^P) \\ W_{t+1}^L &= W_t^L + \phi * (W^{L_0} - W_t^L), \end{aligned} \quad (7)$$

328 While information stored in WM decays over time, reflecting the well-documented
 329 short time-scale of WM maintenance, RL is assumed to be a more robust system that
 330 is less susceptible to forgetting. Therefore, it is theoretically less justified to include a
 331 decay mechanism for Q-values. Nevertheless, for completeness, we fit the version of the
 332 model with a separate decay process in the RL module as well, and confirmed that it
 333 does not improve the model fit. Thus, in further implementations of the RL-WM model
 334 we limited decay implementation to the WM module only.

335 Policy

336 We used the softmax function to transform WM weights and RL Q-values into choice
 337 probabilities to produce position choice policies P_{RL}^P and P_{WM}^P :

$$\begin{aligned} P_{RL}^P(p|c) &= \frac{\exp(\beta * Q_t^P(c, p))}{\sum_{i=1}^3 \exp(\beta * Q_t^P(c, p_i))} \\ P_{WM}^P(p|c) &= \frac{\exp(\beta * W_t^P(c, p))}{\sum_{i=1}^3 \exp(\beta * W_t^P(c, p_i))}, \end{aligned} \quad (8)$$

338 We applied the same softmax transformation to the label Q- and W-tables to obtain
 339 the label and choice policies P_{RL}^L and P_{WM}^L . This policy permits the selection of choices
 340 with higher Q-values/weights with higher probability. The softmax β is the inverse
 341 temperature parameter, which controls how deterministic the choice process is. For each
 342 module, the overall choice policy is a mixture of both policies, determined by mixture
 343 parameters, ρ :

$$\begin{aligned} P_{RL}(p_i|pos.block) &= \rho_P * P_{RL}^P(p_i) + (1 - \rho_P) * P_{RL}^L(label(p_i)) \\ P_{WM}(p_i|pos.block) &= \rho_P * P_{WM}^P(p_i) + (1 - \rho_P) * P_{WM}^L(label(p_i)), \end{aligned} \quad (9)$$

344 We apply the same mixture process with mixture weight ρ_L for the label dimension
 345 blocks:

$$\begin{aligned} P_{RL}(l_i|lab.block) &= \rho_L * P_{RL}^L(l_i) + (1 - \rho_L) * P_{RL}^P(position(l_i)) \\ P_{WM}(l_i|lab.block) &= \rho_L * P_{WM}^L(l_i) + (1 - \rho_L) * P_{WM}^P(position(l_i)), \end{aligned} \quad (10)$$

346 The RL-WM model posits that choice comes from a weighted mixture of RL and
 347 WM, where one's reliance on WM is determined by the WM weight (ω) parameter:

$$\begin{aligned} P(p|c) &= \omega * P_{WM}(p|c) + (1 - \omega) * P_{RL}(p|c) \\ P(l|c) &= \omega * P_{WM}(l|c) + (1 - \omega) * P_{RL}(l|c), \end{aligned} \quad (11)$$

348 where ω reflects the likelihood of an item being stored in working memory and is
 349 proportional to the ratio of capacity parameter (K) and block set size (or number of
 350 stimuli; ns), scaled by the baseline propensity to rely on WM (ω_0 ; Fig 2):

$$\omega = \min(1, \frac{K}{ns}) * \omega_0 \quad (12)$$

351 We further modified the policy to parameterize additional processes. For instance,
 352 individuals often make value-independent, random lapses in choice while doing the task.
 353 To capture this property of behavior, we derived a secondary policy by adding a random
 354 noise parameter in choice selection (Nassar et al., 2016):

$$P' = (1 - \epsilon) * P + \epsilon * \frac{1}{n_A}, \quad (13)$$

355 where n_A is the total number of possible actions, $1/n_A$ is the uniform random policy,
 356 and ϵ is the noise parameter capturing the degree of random lapses.

357 We fit the different configurations of the full RL-WM model to the data from Ex-
 358 periment 2, where we varied set size, which permitted us to modulate WM involvement.
 359 Note that previous research with experiments including multiple set sizes has shown that
 360 single process models (such as RL with decay or interference) are insufficient to capture
 361 set-size effects; indeed, these processes can be decomposed into both pure cognitive load
 362 and increased forgetting with longer delays between stimuli across set sizes. Thus, in
 363 Experiment 2, we do not consider RL-only models.

364 In the absence of a set-size manipulation, it is not possible to separately identify the
 365 WM module from the RL module. Thus, in the first experiment, where set size is fixed,
 366 we only consider the RL module as approximating the joint contributions of both, and
 367 do not include a WM module. Because the RL module summarizes both RL and WM
 368 contributions, we add to it a short-term forgetting feature of the RL-WM's WM module:
 369 specifically, we implemented decay in Q-values for all cards and all choices at each trial:

$$\begin{aligned} Q_{t+1}^P &= Q_t^P + \phi * (Q_0 - Q_t^P) \\ Q_{t+1}^L &= Q_t^L + \phi * (Q_0 - Q_t^L), \end{aligned} \quad (14)$$

370 whereas in the RL-WM model the forgetting parameter is limited to the WM module
 371 only. The list of baseline parameters for RL-WM model (Experiment 2) includes: learning
 372 rate (α), inverse temperature (β), lapse (ϵ), learning bias (LB), decay (ϕ), capacity (K),
 373 WM weight (ω), and value mixture (ρ). The baseline RL model (Experiment 1) include
 374 learning rate (α), inverse temperature (β), lapse (ϵ), learning bias (LB), decay (ϕ) and
 375 value mixture (ρ). We explored different model variants by making different parameters
 376 fixed/varied across conditions. In the RL-WM (Experiment 2) model, the parameters

377 did not vary as a function of set size (i.e. same label/position parameter values for all
 378 set sizes).

379 Model fitting and comparison

380 Fitting Procedure. In both Experiment 1 and Experiment 2 modeling, we used maxi-
 381 mum likelihood estimation to fit participants' individual parameters to their full sequence
 382 of choices. All parameters were bound between 0 and 1, with the exception of the β pa-
 383 rameter, which was fixed to 100 (found to improve parameter identifiability here and in
 384 previous similar tasks (Master et al., 2020)), and the capacity parameter (K) of Exper-
 385 iment 2 models, which could take on one of the discrete values between 2-5. To find
 386 the best fitting parameters, we used 20 random starting points with MATLAB's fmincon
 387 optimization function (Wilson et al., 2019).

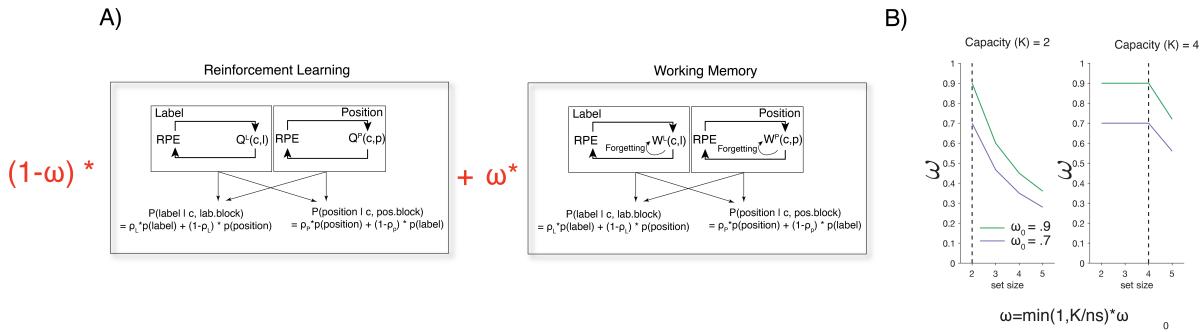


Figure 2: A) In Experiment 1 we used RL model variants, which assume incremental, feedback-driven learning. In Experiment 2, we combined RL and WM modules, under the assumption that learning is a weighted interaction between RL and WM systems. B) The extent to which participants relied on WM was determined by the WM weight parameter (ω), proportional to participants' WM capacity (K), and inversely proportional to set size.

388 Model validation. To validate whether our models could indeed capture the behavioral
 389 properties we set out to model, we simulated performance from the best parameter
 390 estimates for each subject 100 times per subject. We then compared whether the model
 391 predictions from the simulated data captured the patterns we observed in the actual data
 392 set.

393 These simulations also allowed us to ensure that our fitting procedure could ade-
 394 quately recover parameters in our experimental context, by fitting the model to the

395 simulated data and evaluating the match between the true simulation parameters and
396 recovered parameters fit on simulated data.

397 Model comparison. Exploring the full model space would lead to a combinatorial explo-
398 sion of models, given the possible variations along all parameters. Thus, to explore the
399 model space, we took a systematic approach by starting with the most complex model
400 (all parameters varied across conditions), and gradually decreasing model complexity,
401 while also monitoring the goodness of model fit. Specifically, we reduced the model
402 complexity only if we found that removing a parameter improved the model fit. We
403 chose this approach in order to conduct model comparison systematically, testing out
404 plausible parameter configurations with varying complexity. We compared the models
405 using Akaike Information Criterion (AIC) (Wagenmakers et al., 2004), which evaluates
406 model fit using likelihood values and applies a complexity penalty based on the number
407 of parameters. To ensure that our models were identifiable with AIC, we computed a
408 confusion matrix (Wilson et al., 2019) by creating synthetic data sets from each model,
409 fitting each model to the simulated data sets, and performing AIC-based comparison
410 where the ground truth was known. This confirmed that AIC was adequately penalizing
411 for model complexity in our situation.

412 Results

413 Experiment 1: Behavioral results

414 We first asked whether participants learned differently across experimental conditions.
415 Learning curves show that participants learned well in all conditions, as their accuracy
416 increased with more exposure to each card (Fig. 3A). A repeated measures one-way
417 ANOVA confirmed that there was a main effect of condition (label/position/control)
418 on performance ($F(2, 61) = 97.7, p < .001, \eta^2 = .62$). We next tested which specific
419 conditions contributed to this significant difference, and found a marginal difference
420 between control and position conditions; however, this difference did not reach statistical
421 significance (paired t-test: $t(61) = 1.61, p = .11$, Cohen's $d = .20$). This result suggests
422 that the additional choice feature (the labels) in the position condition did not have
423 a strong impact on the choice process. Performance in the label condition, however,
424 was significantly lower than that in the position and the control conditions (paired t-
425 test: position: $t(61) = 11.1, p < .001$, Cohen's $d = 1.42$; control: $t(61) = 12.9, p < .001$,
426 Cohen's $d = 1.65$).

427 We next examined why label condition performance was worse. We hypothesized
428 that choice was not simply noisier in the label condition, but instead that choice might
429 be contaminated by the reward history of irrelevant motor choices. To test this hy-
430 pothesis, we computed the cumulative card-dependent label/position reward history (see
431 methods), and quantified the proportion of error trials in which participants incorrectly
432 chose a box with high reward history of an incorrect feature (Fig. 1B). In the position
433 condition, participants did not make more interference errors than expected at chance
434 level (0.5 for two possible errors) (Fig. 3B; $t(61) = .13$, $p = .89$, *Cohen's d* = .01). This
435 confirms that the presence of labels in the position condition did not impact choice com-
436 pared to the control condition. By contrast, in the label condition, the proportion of
437 interference errors was significantly higher than chance (Fig. 3B; $t(61) = 2.54$, $p = .01$,
438 *Cohen's d* = .32). Furthermore, the proportion of interference errors in the label condition
439 was significantly greater than interference errors in the position condition ($t(61) = 2.13$,
440 $p = .03$, *Cohen's d* = .27). This result suggests an asymmetry in interference between
441 different choice spaces, in that the values of less general/motor action choices seem to
442 contaminate the more general choice process (but not the other way around). To rule out
443 the possibility that the effect we observed was driven by the block/condition order (i.e.
444 transfer of incorrect strategy from the previous block), we ran a mixed-effects general
445 linear model predicting accuracy with previous vs. current block conditions. The result
446 of this analysis showed that participants' performance was affected by the current block
447 condition ($p < .001$), but not the previous block condition ($p = 0.45$), thus ruling out or-
448 der effects as a possible explanation of our results. In addition, our results were replicated
449 in the second experiment (as reported later), where we removed the control condition
450 altogether, and counterbalanced the remaining condition blocks such that participants
451 could either experience position or label condition blocks first. This further supports the
452 conclusion that the observed results are unlikely to be explained by the order effects.

453 Next, we performed a trial-by-trial analysis to examine the effect of card/label values
454 on correct trials' reaction times (RT). For each condition, we used a mixed-effects linear
455 model to predict $\log(RT)$ from the reward history difference (RHD) between chosen
456 and unchosen choices (see methods), where choice referred to label in one predictor
457 and position in the other. The rationale behind this analysis is that if participants
458 are engaging in the appropriate decision strategy, then RTs should decrease with the
459 higher RHD in the condition-relevant dimension (label or position), because a higher
460 RHD means greater evidence in favor of the correct response. On the other hand, in the
461 event of interference, we expected participants' RTs to be modulated by the RHD of the
462 incorrect dimension (e.g. position RHD in label condition). We controlled for the trial

463 number in the model.

464 As predicted, in models for each condition (position condition model $f^2 = .27$; label
 465 condition model $f^2 = .154$), participants' RTs decreased with increased respective RHD
 466 (Fig. 3C; label condition: $\beta_{label} = -.04$, $p < .001$; position condition: $\beta_{position} = -.06$,
 467 $p < .001$). Label RHD did not affect the RTs in the position condition ($\beta_{label} = -.004$,
 468 $p = 0.55$). Hence, the mixed-effects model aligned with interference errors, confirming
 469 that participants' choices were not affected by the presence of an additional feature (the
 470 labels) in the position condition. On the other hand, the position RHD surprisingly
 471 increased RTs in the label condition ($\beta_{position} = .034$, $p = .001$), suggesting that the
 472 interference of motor action values with label values may have resulted in the delay of
 473 choices (Fig. 3C). We compared the subject-level β estimates of the effect of incorrect
 474 dimension RHD on RTs in position and label conditions, and found that the incorrect
 475 RHD effect was significantly greater in the label condition (paired t-test: $t(61) = 3.87$, $p <$
 476 $.001$, *Cohen's d* = .49), confirming the asymmetry between conditions that was revealed
 477 in previous analyses.

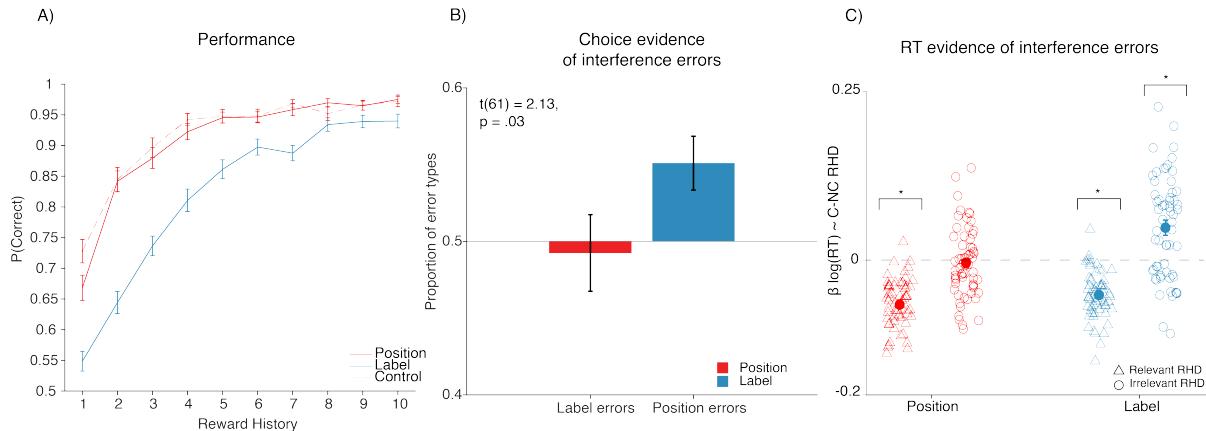


Figure 3: Experiment 1 Model-independent results. A) Proportion of correct choices as a function of number of previous rewards obtained for a given stimulus. Participants performed worse in the label condition, compared to the position and control conditions. Performance in the position and control conditions did not differ statistically. B) Asymmetric value interference: The values of motor actions interfered with values of correct labels in the label condition, thus resulting in the interference errors, but not the other way around. C) Mixed-effects regression model shows that the interference of motor action reward history/values may have resulted in the longer RTs in the label condition.
 * indicates statistical significance at $p < .05$

478 Experiment 1: Modeling results

479 We used computational modeling to tease apart the mechanisms driving condition effects.
480 We fit several variants of reinforcement learning (RL) models, and focus here on 4 models
481 that represent the main different theoretical predictions (Fig. 4A; Fig. 4B). The standard
482 RL model (M1) assumes no difference between the conditions and serves as a baseline
483 that cannot capture the empirical effect of condition. RL model M2 lets learning rates
484 depend on condition, and tests the prediction that slower learning with labels is driven
485 by different rates of reward integration. Model M3 extends model M2 with an additional
486 mechanism, parameterized by the value mixture (ρ_L), that enables the position value to
487 influence policy in the label condition.

488 Ruling out the difficulty explanation using computational modeling. Model M4, the
489 dual-noise model, is an RL model with a condition-dependent noise parameter (ϵ). M4
490 captures the hypothesis that the label condition is more difficult, resulting in a noisier
491 choice process. Models M1-4 all assume $\rho_P = 1$, with no influence of labels in position
492 blocks. Other models considered separate decay (ϕ) parameters and a free position con-
493 dition ρ_P , but did not improve fit.

494

495 Model M3 offered the best quantitative fit to the data, as measured by AIC (Fig. 4B).
496 Furthermore, only model M3 was able to qualitatively reproduce patterns of behavior.
497 Specifically, for each of the models, we simulated synthetic data sets with fit parameters
498 and tested whether the model predictions matched the empirical results. We focused on
499 2 key data features in our model validation: performance averaged over the stimulus iter-
500 ations (learning curves), and asymmetrical interference errors. Model validation showed
501 that only the model with 2 learning rates and one ρ parameter (M3) captured both prop-
502 erties of the data (Fig. 4A). These results confirm that the learned value of (irrelevant)
503 motor actions influenced the selection of more general label choices. Furthermore, model
504 comparison results show that slower learning in the label condition was not due to a
505 noisier choice process, but due to a reduced learning rate. Indeed, the position condition
506 α was significantly greater than the label condition α (sign test; $z = 6.35$ $p < .001$, effect
507 size: .81) Fig. 4C). Interestingly, the learning rates in the two conditions were correlated
508 (Spearman $\rho = .39$, $p = .003$; Fig. 4C), suggesting that the learning process in the two
509 conditions was driven by related underlying mechanisms.

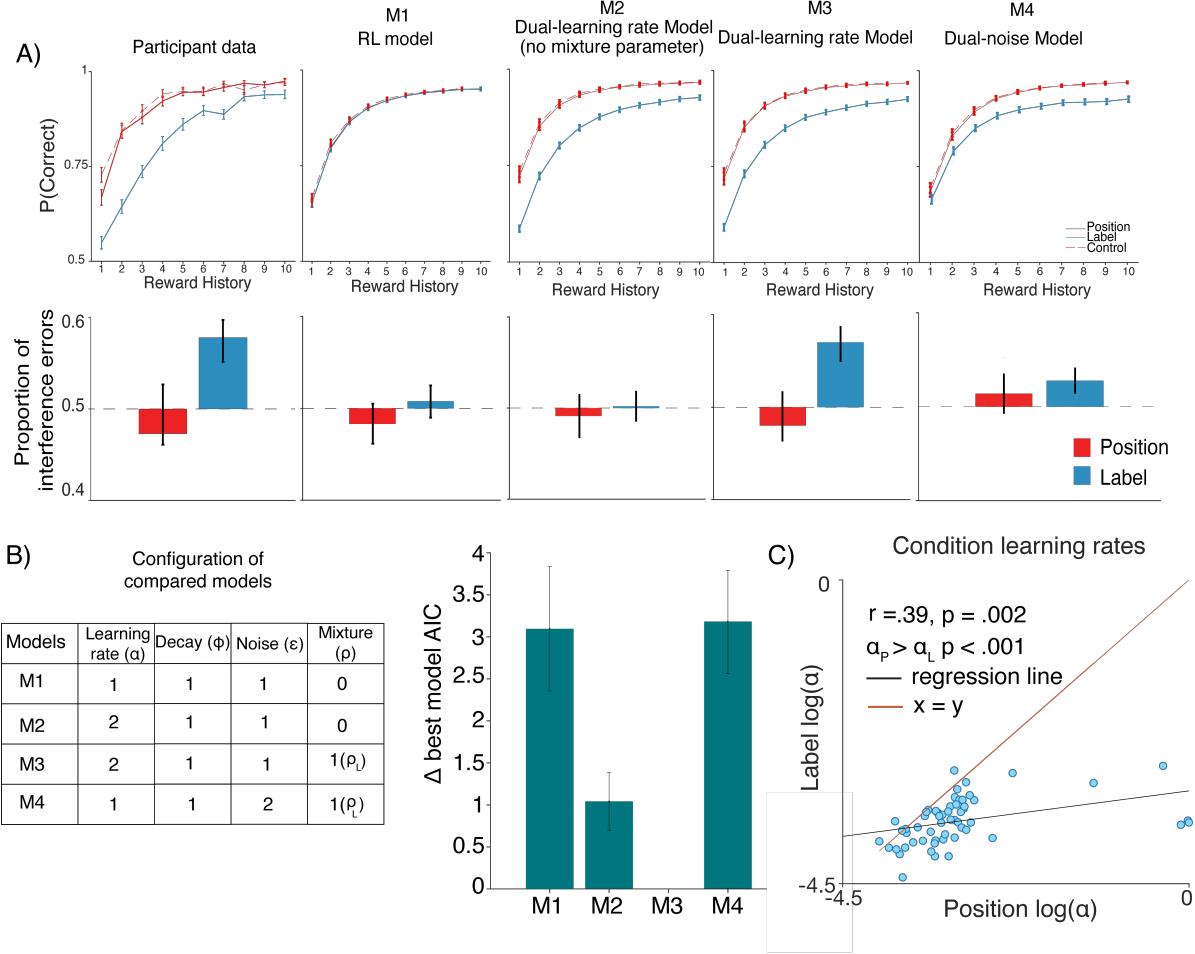


Figure 4: Experiment 1: Modeling Results. A) Model validation comparing the observed data to predictions of tested models; M3 reproduces behavior best. B) Parameters used in models M1-4 (left); M3 has best group-average AIC. C) Comparison of condition-dependent learning rates shows that learning rates are correlated, and that label condition learning rates are significantly lower compared to position condition learning rates.

510 Experiment 2: Behavioral Results

511 The results of the first experiment suggest that the choice type affects learning. However,
 512 given the experimental design, our conclusions could not dissociate whether the difference
 513 in RL parameters actually reflected a difference in RL mechanisms or in WM mechanisms.
 514 Recent work (Collins, 2018; Collins et al., 2018), nevertheless, suggest that RL behavior
 515 recruits other learning systems, such as WM. Hence, the variations that may appear to
 516 be driven by RL mechanisms might conceal what is actually a WM effect. To address

517 the question of whether the choice definition matters for learning at the level of RL
518 or WM, and whether slowed learning stems from slowed WM or RL, we ran a second
519 experiment. In Experiment 2, we varied the number of cards (set size) to manipulate WM
520 involvement. Furthermore, we fit variants of the RL-WM model to test the contribution
521 of WM mechanisms.

522 Experiment 2 results replicated findings from Experiment 1, showing that there was a
523 main effect of condition (Fig. 5A; repeated measures one-way ANOVA ($F(1, 56) = 98.95$,
524 $p < .001$, $\eta^2 = 0.63$)). Furthermore, we replicated the pattern of interference errors,
525 suggesting that the value of position choices interferes with that of label choices, but not
526 the other way around (Fig. 5B; $t(55) = 2.89$; $p = .006$, *Cohen's d* = .38).

527 We next investigated how set size manipulation affected these results. As predicted,
528 performance decreased with set size in both conditions (Position: $F(3, 56) = 11.83$, $p <$
529 $.001$, $\eta^2 = .38$; Label: $F(3, 56) = 23.498$, $p < .001$, $\eta^2 = .55$). There was an interaction
530 between set size and condition ($F(3, 56) = 16.21$, $p < .001$, $\eta^2 = .46$; Fig. 5A). There was
531 a marginal set size effect in interference errors that did not reach significance ($F(3, 56) =$
532 2.17 , $p = .09$, $\eta^2 = .20$; Fig. 5C).

533 To better understand the source of the set size effect, we ran a general linear mixed-
534 effects model to predict trial-by-trial performance. Our mixed-effects model included
535 predictors indexing WM mechanisms (set size and delay between presentations of the
536 current stimulus and the most recently rewarded stimulus; indexing capacity and sus-
537 ceptibility to decay properties of WM respectively), and RL effects (dimension-relevant,
538 card-dependent reward history, calculated from the cumulative number of earned points
539 for each card, indexing reward-based learning). We also ran a model which tests for an
540 interaction between individual RL/WM factors and the task condition.

541 A likelihood ratio test provided evidence in favor of the interaction model over a model
542 without interactions (model without interactions $f^2 = .42$; model with interactions f^2
543 = .43; LR $p < .05$). The interaction model showed that, as expected, participants' per-
544 formance increased as a function of reward history ($\beta = .62$, $p < .001$), and decreased
545 as a function of set size ($\beta = -.18$, $p = .00011$). There was no effect of block ($\beta = .04$,
546 $p = .58$) or delay ($\beta = -.04$, $p = .37$), suggesting that neither overall task exposure nor
547 delay affected performance over and above reward history and set size. The only signif-
548 icant interaction term was the condition*reward history interaction ($\beta = .16$, $p = .01$),
549 suggesting that the reward history more heavily contributed to an increase in perfor-
550 mance in the label condition. To understand our results on a more mechanistic level, we
551 turned to computational modeling.

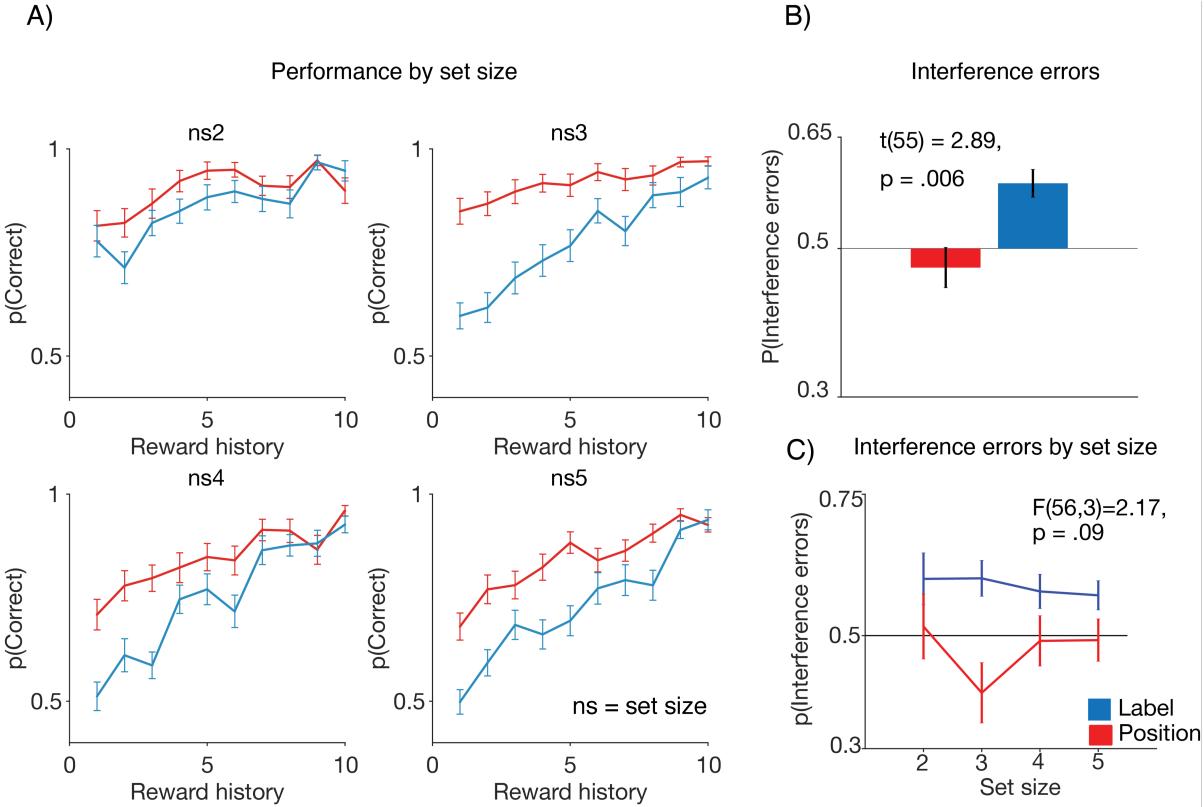


Figure 5: Experiment 2 Results. A) Participants' overall performance varied by set size (a marker of WM contribution), and was worse in the label condition. B) The asymmetry in value interference replicated from Experiment 1, showing that values of position choices interfere with values of label choices, but not the opposite. C) The interference errors did not vary by set size.

552 Experiment 2: Modeling results

553 The set size manipulation in Experiment 2 enables us to identify distinct contributions of
 554 RL and WM (Collins et al., 2012) with the full RL-WM model (see methods). Briefly, RL-
 555 WM disentangles an incremental, value-learning process (RL), as well as a rapid-learning,
 556 but decay-sensitive short-term memory-based decision process (WM). Choice policy is
 557 a weighted mixture of RL and WM (Fig. 2A,B), where the weighting is proportional
 558 to one's WM capacity. In other words, the model architecture posits that if one's WM
 559 capacity is low, one might be more likely to rely on RL than WM, especially when
 560 set size (number of items) is high. We first replicated in Experiment 2 that models
 561 including only one of those mechanisms could not adequately capture the set size effect,

562 as has been shown before (Collins et al., 2012). We then approached model comparison
563 by systematically varying the complexity of the RL-WM model (Fig. 2A), in order to
564 establish whether specificity in RL or WM module parameters (or both) is necessary
565 to capture the divergence between behavioral patterns in the 2 conditions. Because the
566 RL-WM model assumes the policy for choice generation at the level of both RL and WM,
567 we also tested if integrating irrelevant dimension interference with a ρ mixture parameter
568 in the policy of RL module or WM module (or both) could best capture our data. We
569 were interested in the condition-based dissociation between parameters.

570 Exploring all possible parameter combinations was computationally prohibitive. Thus,
571 we explored a subset of the most relevant models (see methods; in the main text, we fo-
572 cus only on a subset of models; see supplement for other non-winning models - Fig. 9).
573 Using AIC comparison, we identified the simplest model which allowed us to capture the
574 properties of the data (M1, (Fig. 6A)). In M1, the WM weight (ω) and ρ parameters
575 were condition-dependent (with free ρ parameter for label condition, and position con-
576 dition ρ fixed to 1). Capacity (K), learning rate (α), decay (ϕ), learning bias (LB), noise
577 (ϵ) were shared across the 2 conditions - model comparison showed no benefits to making
578 them independent (Fig. 9). We further consider 3 other variants of this model: no value
579 interference ρ (M2), ρ in RL policy alone (M3), and ρ in WM policy alone (M4) (Fig.
580 6A). Last, we consider a control model with condition-dependent ϵ and α , which would
581 primarily attribute the decline in label condition performance to noise/RL system (M5).
582 Consistent with Experiment 1 results, the AIC comparison revealed that M5 could not
583 capture data well, and that M1 without ρ (M2) fit worse (Fig. 6A), providing additional
584 evidence for the necessity of the interference mechanism to capture choice data, and thus,
585 the existence of motor value interference in label blocks. However, the AIC comparison
586 failed to significantly distinguish between the remaining models M1 (ρ in RLWM), M3
587 (ρ in RL) and M4 (ρ in WM) (repeated measures ANOVA: $F(2, 56) = 2.63, p = .07, \eta^2 =$
588 .08), though ρ in RL models fit numerically worse, supporting the idea that we needed
589 to include motor value interference in the WM module to account for the results. There-
590 fore, we henceforth focus on the simplest model, M1 with condition-dependent ω and ρ
591 in RL and WM policy, as this model makes the fewest specific assumptions about RL-
592 WM dissociation between the 2 conditions. Note that model comparison results were
593 identical (and stronger) when using BIC instead of AIC, and that protected exceedance
594 probability supported M1 over other models.

595 The M1 model adequately captured the data patterns in 1) learning curves (Fig. 6B),
596 2) overall interference errors (Fig. 6C) and 3) interference errors by set size (Fig. 6D).
597 Furthermore, the WM weight ω was significantly reduced in the label condition compared

598 to the position condition in M1 (Fig. 6E).

599

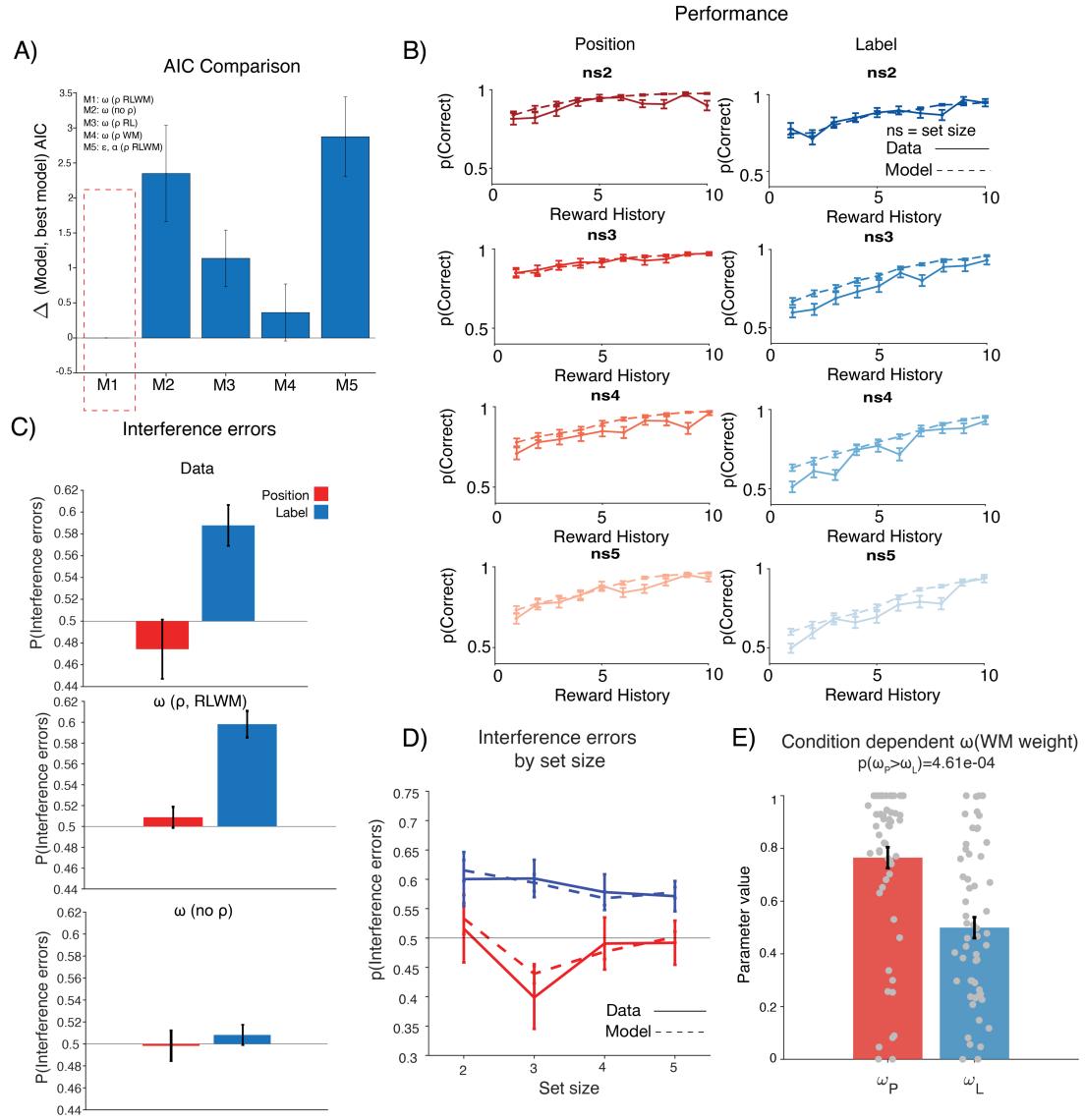


Figure 6: (A) AIC comparison allowed us to narrow down the space of models. Models with condition-specific WM weight (ω) fit the best (M1-M4). Removing the mixture parameter (ρ) harmed the model fit (M2). A model assuming impairment in RL did not fit as well (M5). See main text for model specifications. B) Model simulations of the best model M1 captured the behavioral data patterns. C) Model validation for M1 (ρ) and M2 (no ρ) confirms the necessity of ρ parameter in capturing the interference error patterns.)

Figure 6: D) M1 captured interference errors in different set sizes. We note that the numerical dip in set size 3 is not statistically significant. While it is unclear why the model simulations reproduce it, it is possible that it arises from a pattern in the stimulus sequences, which is used by participants and model simulations. E) Comparison of condition-dependent parameters shows that ω is lower in the label condition.

600 Overall, the results suggested that the performance decrease in the label condition was
601 driven primarily by deficits in WM, specifically by a smaller WM weight ω that indexes
602 the set-size independent contribution of WM to learning. Therefore, the choice type
603 (more/less general) impacted learning, and it seemed to do so by decreasing participants'
604 ability to use WM for learning. However, the value interference appeared to be present
605 in both RL and WM mechanisms.

606 Discussion

607 Humans and animals make many types of choices, at multiple levels of generality, where
608 some choices are dependent on others. We designed a new experimental protocol to
609 investigate whether and how different choice types impact learning. Across two exper-
610 iments, behavioral analyses and computational modeling confirmed our prediction that
611 the generality of choice type impacts learning, with worse performance for choices that
612 do not map onto a simple motor action. Computational modeling revealed two separable
613 sources of impairment. First, value learning for relevant choices of a more general type
614 was slower, as revealed by smaller learning rates (α) in Experiment 1. Second, choices
615 were contaminated by irrelevant motor action values. Experiment 2 examined whether
616 this dissociation originated in different neuro-cognitive systems' contributions to learn-
617 ing, namely RL and/or WM. Our results revealed that the reduction in learning speed for
618 general-format choices stemmed more from WM than the RL process, with WM weight
619 (ω) reduced but RL (α) unchanged, when controlling for WM contributions. However,
620 the interference of low level values appeared to be present in both mechanisms. The
621 selective reduction in WM weight implies that participants' executive resources might be
622 leveraged to define the choice space that is then used by both the RL and WM system; a
623 more generalized choice space requires a higher degree of such computation, thus leaving
624 reduced resources for actual learning.

625 In both experiments, we found an asymmetry in interference between choice types.
626 When participants learned to make more general choices (selecting a label) that required

627 a subsequent motor action (pressing the key corresponding to the label’s location), their
628 choices were influenced by the irrelevant reward history of motor actions. By contrast,
629 when participants learned to make less general choices (the correct response is defined
630 by pressing the same key corresponding to the box location), they were not influenced
631 by the irrelevant reward history of box labels. This result is consistent with a choice
632 hierarchy interpretation, where participants may be unable to turn off credit assignment
633 to irrelevant choice dimensions when the realization of their (abstract) choice does involve
634 this dimension (Eckstein et al., 2020), but are able to do so when the irrelevant choice
635 dimensions are more abstract, as shown here.

636 While our results imply that participants exhibit a decision bias towards motor ac-
637 tions, we acknowledge that our protocol cannot disambiguate between the motor actions
638 themselves and the corresponding spatial location of the boxes. That is, we cannot con-
639 firm whether the participants track the value of specific motor actions (index/middle/ring
640 finger key press) or of the corresponding box positions (left/middle/right). Hence, a com-
641 peting interpretation of our results would be that spatial positions, rather than motor
642 actions, are prioritized in tracking value, compared to other visual features such as la-
643 bels. To completely rule out this possibility, we would need to modify the current task
644 with a condition where the motor actions are not aligned with the specific positions, and
645 inspect whether the interference effect persists in such a condition. However, we think
646 this account is less likely than a choice abstraction account, which explains our results
647 more parsimoniously, without requiring a “special status” for a “position” visual feature.

648 Furthermore, animal research supports this interpretation, as it shows differences in
649 the neural code of choices, which are defined primarily as motor actions versus more
650 abstract choices (Luk et al., 2013; Rothenhoefer et al., 2017). Specifically, these studies
651 have utilized recordings from neurons of animals trained to perform a task that con-
652 trasted motor action choices with stimulus goal choices, in order to identify the neural
653 substrates that differentiate between the two. The results seem to implicate prefrontal
654 cortex (PFC), anterior cingulate cortex (ACC), orbitofrontal cortex (OFC), and striatal
655 regions (ventral striatum) as areas that differentiate between how choices with different
656 levels of abstraction are coded in the brain. Therefore, it is likely that it truly is a disso-
657 ciation between motor actions, rather than positions, and more abstract choices that led
658 to the interference and the effects we observed in our work. Our results have implications
659 for research on hierarchical representations. Specifically, while simple RL algorithms are
660 useful to capture reward-based learning, they are commonly criticized because they fail
661 to capture the flexibility and richness of human learning. Hierarchical reinforcement
662 learning (HRL) was developed in part to address limitations of standard RL (Botvinick

663 et al., 2009; Collins et al., 2013; Stolle et al., 2002; Xia et al., 2021). Previous research
664 suggests that the choice space might be hierarchically represented, with the lower level of
665 hierarchy consisting of primitive actions, and the higher level consisting of temporally ex-
666 tended actions (state-dependent, extended policies), also known as options (Stolle et al.,
667 2002). Evidence from this research suggests that hierarchical representations are useful
668 for enabling transfer; instead of learning from scratch in the novel context, an agent can
669 leverage higher level representations to speed up learning (Xia et al., 2021). The trans-
670 fer results also suggest that choices at different levels of hierarchy show an asymmetry
671 in flexibility in novel contexts (lower level choices being less flexible). Our results are
672 consistent with this finding since motor actions seem less flexible and less impacted by
673 competing reward information, providing additional supporting claims for hierarchical
674 representations in choice space.

675 In addition to this, there is evidence of hierarchical representations at the neural level.
676 In particular, frontal areas (primarily PFC) and basal ganglia (BG) are also frequently
677 investigated as neural mechanisms that support hierarchical reasoning/learning (Collins
678 et al., 2013). Converging insights suggest that the cortico-BG loops support represen-
679 tations of both low-level associations and abstract rules/task sets, giving rise to latent
680 representations that can be used to accelerate learning in novel settings (Collins et al.,
681 2013; Eckstein et al., 2019; Stolle et al., 2002; Xia et al., 2021).

682 Both experiments implicated overall slowed learning, in addition to value interference,
683 in the worse performance for more general choices. Our first experiment (which allowed
684 us to test RL models only) implicated the learning rate (usually interpreted as a marker
685 of the RL system (Eckstein et al., 2019)) as the mechanism driving the difference between
686 conditions with different choice types. However, our second experiment enabled us to
687 test the more holistic hybrid model of RL and WM, and revealed that the impairment
688 in the more general choice condition likely stemmed from the WM system, rather than
689 RL. Previous work has shown that executive function (EF), in its different forms (i.e.
690 WM, attention), contributes to RL computations (Collins, 2018; Niv, 2019). The general
691 summary of this work is that high-dimensional environments/tasks pose difficulty to RL;
692 EF then acts as an information compressor, making the information processing more
693 efficient for RL (Rmus et al., 2021). Operating in a more generalized choice space might
694 more heavily rely on the contribution of EF (in this case WM) relative to operating
695 in the less abstract condition. Therefore, resource-limited WM might be leveraged to
696 define the choice space (i.e. relevant features of the choice space, like labels in label
697 condition). As a result, the WM weight included in the WM + RL hybrid model, which
698 indexes the WM contribution to learning, appears to be reduced in the label condition.

699 Our interpretation of this result is that this reduction in WM contribution may indicate
700 that some of participants' limited WM resources are recruited elsewhere, and specifically
701 that it has already been used to define the choice space over which learning and decision
702 making occurs.

703 While we conclude that WM is used for defining the choice space, consistent with
704 prior results on EF contributions to RL computations (Todd et al., 2008), we do not
705 make any particular assumptions about how the use of choice space is divided between
706 RL and WM once it's defined. We tested different model variations, with the parameter
707 mixing label/position values, to explain value interference at the policy level of RL, WM
708 or both. If there was clear evidence in favor of the mixture parameter in either the RL or
709 WM policy, it would imply that the policy generation based on choice space is primarily
710 driven by that system. However, our model comparison revealed no evidence that the
711 mixture parameter is specific to either RL or WM, suggesting that the choice space is
712 shared between the two. This will be important to further explore in future research.

713 A competing interpretation for our findings of slowed learning for more abstract
714 choices is that the label condition required more attention and was more difficult. While
715 this is true, we took steps to mitigate this potential confound on two levels - task design
716 and modeling. In the task design, we constructed the single trial structure such that
717 participants had a chance to see box labels first, before the onset of the card. By
718 doing this we aimed to eliminate potential advantages of the position condition, where
719 participants do not need to perform an additional process of identifying the label location
720 prior to executing the response. Furthermore, our modeling enabled us to validate the
721 effects of our task design. Specifically, in both experiments we tested the model with
722 condition-dependent noise parameters, which predicts that different noise/difficulty levels
723 are what drive the performance difference in our conditions. This model did not fit the
724 data well (Experiment 1: Best model AIC > 2 noise model AIC $t(56) = -5.179$, $p =$
725 $3.13e-06$, *Cohen's d* = .69; Experiment 2: Best model AIC > 2 noise model AIC $t(56) =$
726 -5.05 , $p = 4.98e-06$, *Cohen's d* = .67), making it unlikely that difficulty-induced lack of
727 attention/motivation could explain our condition effect.

728 A competing interpretation of our results might be that participants simply did not
729 pay attention to the labels in the position condition, accounting for the observed asym-
730 metry. That is, because the labels are not informative for selecting a correct response
731 in the position condition, participants might simply not be attending to them at all, as
732 opposed to encoding them, with the choice process remaining unaffected by the inter-
733 fering information from labels. However, we think this competing account is unlikely,
734 for multiple reasons. First, the labels were very salient (colors, and presented prior to

735 the stimulus); thus participants would need to actively avoid them to not perceive them.
736 While we have no direct measure of participants' attention to the labels, it is unlikely
737 that they did not process them at all. Second, there is evidence from previous work
738 that participants encode and use information from unattended stimuli, especially when
739 the unattended stimuli might be relevant for the reward structure in the task (Gutnisky
740 et al., 2009; Sasaki et al., 2010). Therefore, the labels (even if not strongly attended to in
741 the position condition) would be a part of the input in the choice process that, according
742 to the results, does not strongly impact the choice of the position, which is consistent
743 with our interpretation. We thus consider the more probable interpretation to be that
744 the participants do perceive and attend to the irrelevant labels, but successfully avoid
745 learning their values. However, future work should investigate more directly how much
746 attention participants pay to irrelevant labels.

747 Another limitation is that our design did not manipulate the degree of value inter-
748 ference between the choice dimensions, since we equally counterbalanced the position of
749 labels. Instead, introducing a systematic bias such that, in a label block, for example,
750 some positions had higher value due to overlapping with correct labels more frequently,
751 would provide an opportunity to induce and measure different magnitudes of interference.
752 This would be an interesting question to explore in the future.

753 Surprisingly, we found that participants' response times (RT) on correct trials in-
754 creased as a function of position reward history difference (RHD) in the label condition.
755 This implies that when both label and position sorting rules were in agreement on the
756 best choice to make (i.e. the blue box was the correct box, and was in the position that
757 had been most rewarded so far), response times tend to be longer (the corresponding ef-
758 fect was not observed in the position condition, where label RHD had no effect on RTs).
759 This is, therefore, a counterintuitive effect, as we would expect the congruent information
760 to accelerate response execution, rather than slow it, as observed here. One possibility
761 might be that participants do engage in a form of arbitration between selection of differ-
762 ent response types. Specifically, they might be biased to execute the motor action based
763 on the reward history difference, as it seems to present itself as a default option based
764 on our results. However, because they are informed that the response based on label
765 selection is correct for the given block, they might delay the response execution, in order
766 to override the default. Nevertheless, this is a speculation - careful modeling of response
767 times is required to further explain this effect, which is beyond the scope of this paper.
768 This account would also predict the highest degree of conflict in this congruent situation,
769 rather than in situations where both rules disagree. It will be an important question to
770 solve in future research.

771 Our results highlight the importance of correct credit assignment, and investigation
772 of mechanisms which might lead to errors in the credit assignment process. Our results
773 are consistent with the previous research suggesting that motor actions might have a
774 stronger effect on the choice selection process than is usually considered (Shahar et al.,
775 2019). Our modeling approach allowed us to show that the mixture of Q values at
776 the policy level is what may lead to the interference effect/incorrect credit assignment.
777 However, as of now, we cannot conclusively say whether the mixture happens selectively
778 at the policy level of RL, WM or both.

779 Identification of correct rewarding responses is a critical building block of adap-
780 tive/goal-directed behavior. Impairments in one's ability to identify the appropriate
781 choice space, which is then used for one's inference process, may consequently result in
782 maladaptive/suboptimal behavioral patterns. Our interference effect results suggest that
783 some aspects of the choice space might be incorrectly overvalued, thus resulting in choice
784 patterns that reflect repeated erroneous selection of incorrect choice types, or an inabil-
785 ity to utilize flexible stimulus-response mappings. These kinds of perseverative responses
786 are reminiscent of the inability to disengage from certain actions, observed in conditions
787 such as obsessive-compulsive disorder (OCD) (Rosa-Alcázar et al., 2020). It would be
788 interesting to use our task and computational modeling approach to investigate whether
789 the mixture/interference of values at the policy level could also explain the behavior of
790 such populations.

791 In conclusion, our findings provide evidence that the choice type and how we define a
792 choice have important implications for the learning process. The behavioral patterns (i.e.
793 value interference from less abstract choices) are consistent with the premises of hierarchy
794 in learning and behavior (i.e. lower levels in hierarchy impacting processing in higher
795 levels), which has become an increasingly promising topic of research (Collins et al.,
796 2013; Eckstein et al., 2020; Stolle et al., 2002). We also demonstrate additional evidence,
797 relevant to the definition of the choice space, that EF (specifically WM) contributes to
798 RL in reward-driven behaviors (Rmus et al., 2021), further demonstrating the complex
799 interplay between various neuro-cognitive systems.

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919 are intertwined: A cognitive, neural, and computational perspective. *Journal of
920 Cognitive Neuroscience*, 34(4), 551–568.

921 Supplementary materials

922 Experiment 1 additional model comparisons. We tested whether an additional decay
923 parameter, an additional mixture parameter, a mixture parameter shared across the two
924 conditions and free softmax temperature parameter improved the fit to the data. These
925 models did not improve the fit compared to M3 (our winning model).

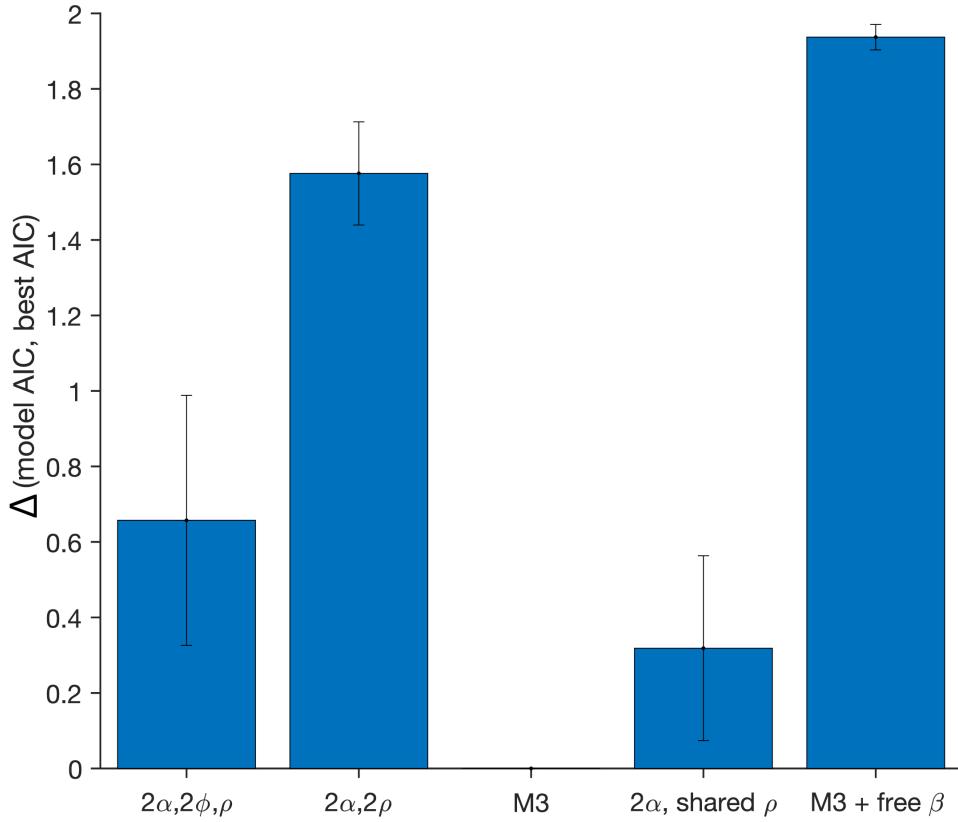


Figure 7: Additional models tested in Experiment 1.

926 Experiment 1 confusion matrix. To demonstrate the identifiability of our models (i.e.
 927 models are meaningfully different from one another), we simulated the data from each
 928 model on 62 iterations (number of participants). We used best parameter estimates for
 929 each participant to create a synthetic data set on each iteration. We then fitted each
 930 of the models to each simulated data set with 20 random starting points, to match the
 931 fitting procedure to participants' data. Next, we computed the proportion of the times
 932 each model fit the best. If the models are identifiable, the model the data was simulated
 933 from should fit the best on most iterations (i.e. the matrix should have the highest
 934 proportion of best fit values on its diagonal). The confusion matrix showed that our
 935 models are identifiable.

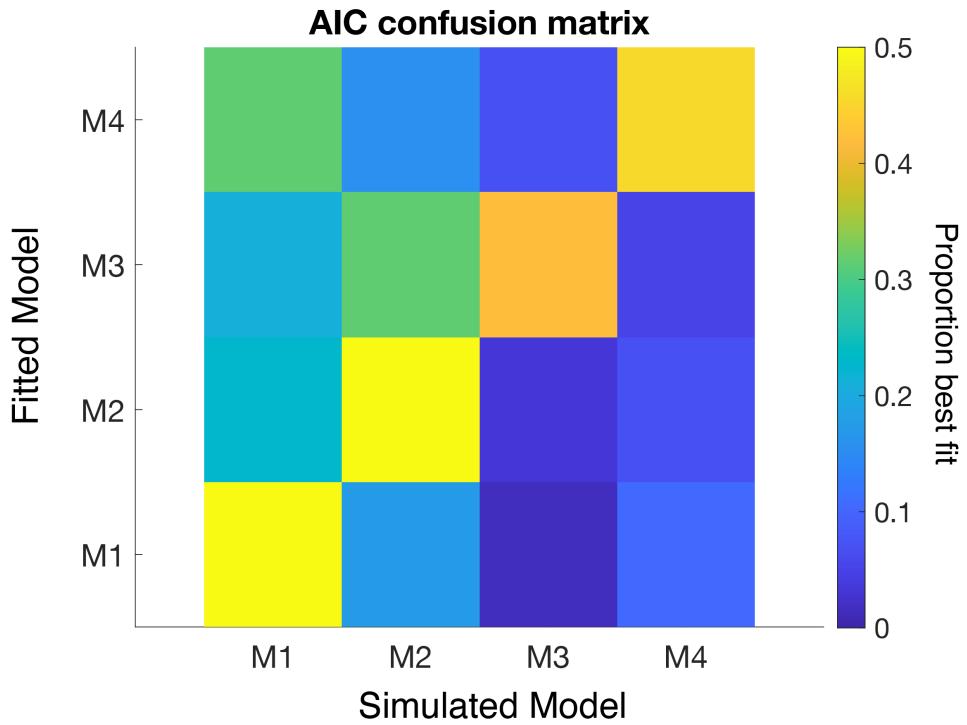


Figure 8: Confusion matrix of the main models tested in Experiment 1.

936 In our second experiment, we fit a considerable range of models, starting with the
 937 most complex (all RL + WM parameters condition-dependent), to the simplest (all
 938 parameters shared across conditions). We systematically varied the complexity of the
 939 model, while monitoring the model fit/complexity tradeoff using AIC scores, in order to
 940 test which parameters are necessary for capturing the difference between the conditions
 941 while also making sure our models are not overfitting (Fig. 9).

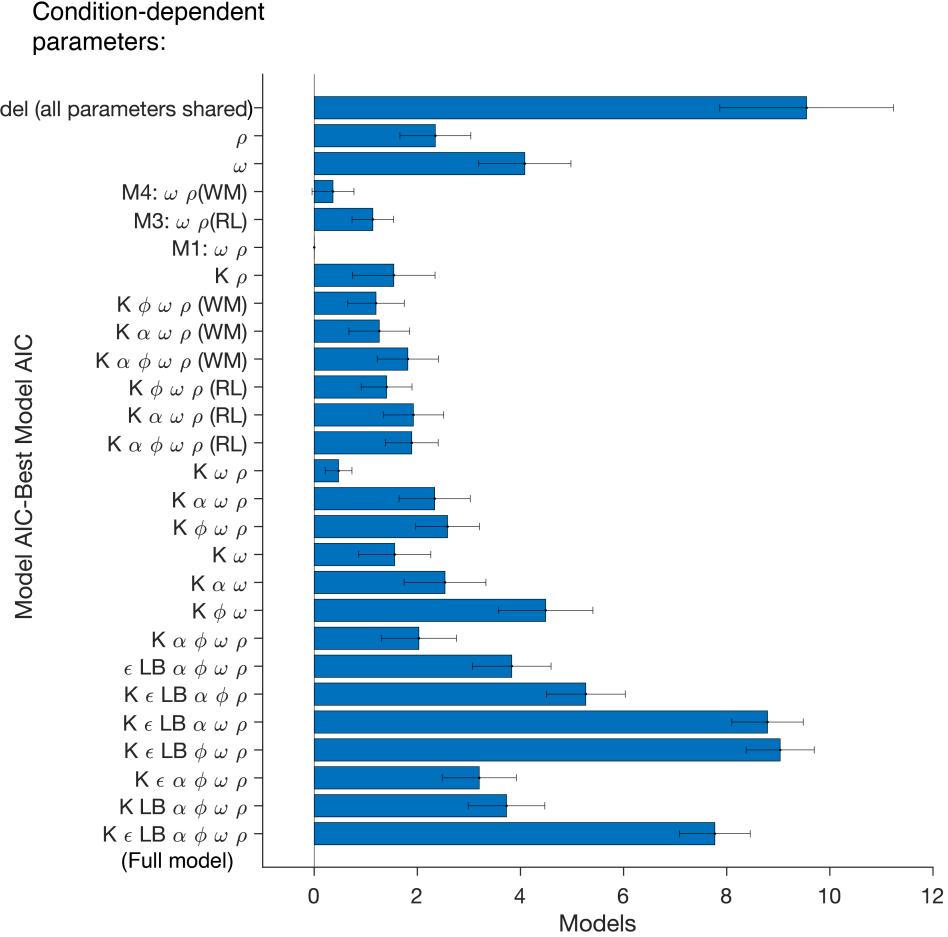


Figure 9: AIC comparison of models tested in Experiment 2. Here we show the difference in individual AIC scores between M3, and all other models that were tested.

942 Experiment 2 Confusion Matrix. We tested the identifiability of our models in Experi-
 943 ment 2 by creating a confusion matrix, similarly to Experiment 1 [Wilson et al., 2019](#). We
 944 constructed two different confusion matrices, which test for identifiability of our model
 945 along 2 different dimensions. Our first confusion matrix allowed us to test whether the
 946 models with different placements of the ρ parameter (i.e. with wrong choice dimension
 947 policy mixture in RL, WM or both) are meaningfully dissociable. The confusion matrix
 948 shows that the models with mixture ρ in RL and WM policy can be dissociated (Fig. 10).
 949 The data simulated from the model with ρ parameter in both WM and RL policy was fit
 950 equally well by that model and the model with ρ in WM policy alone. This is consistent
 951 with our results, as model comparison revealed that AIC scores did not meaningfully

952 differ between these two models. Note that the models included in the confusion matrix
 953 are nested models (differing by at most 1 parameter), or in the case of the second con-
 954 fusion matrix, identical models in terms of number of parameters, but with different *rho*
 955 parameter placements. Therefore, we did not expect the AIC scores to be considerably
 956 different for paired model fits paired with data simulated across different models.

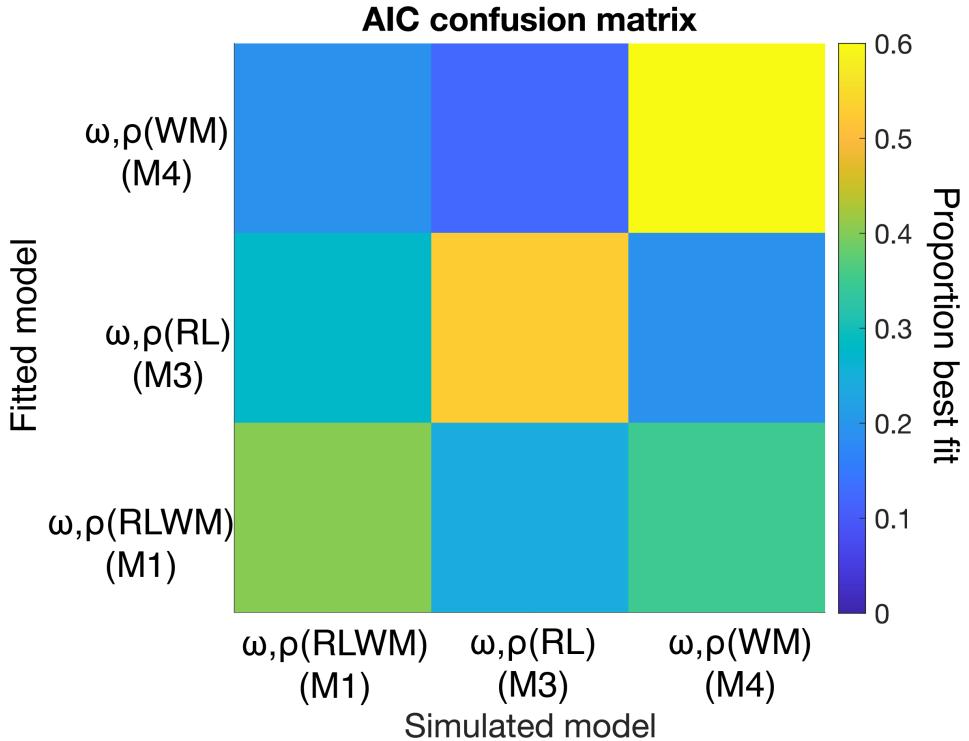


Figure 10: Confusion Matrix 1. Proportion of times the models fitted different simulated data sets best, based on cross-fit AIC scores for models with different placement of ρ parameter.

957 Our second confusion matrix tested whether we can dissociate the model we con-
 958 verged on in the main text (M1, ω with RL-WM ρ) from variations of model with 1)
 959 no ρ parameter, and 2) shared WM weight ω . Our results showed that our models are
 960 mostly identifiable, with an exception of M2 (Fig. 11). However, M2 cannot produce the
 961 observed qualitative error patterns, providing another method to rule out this model.

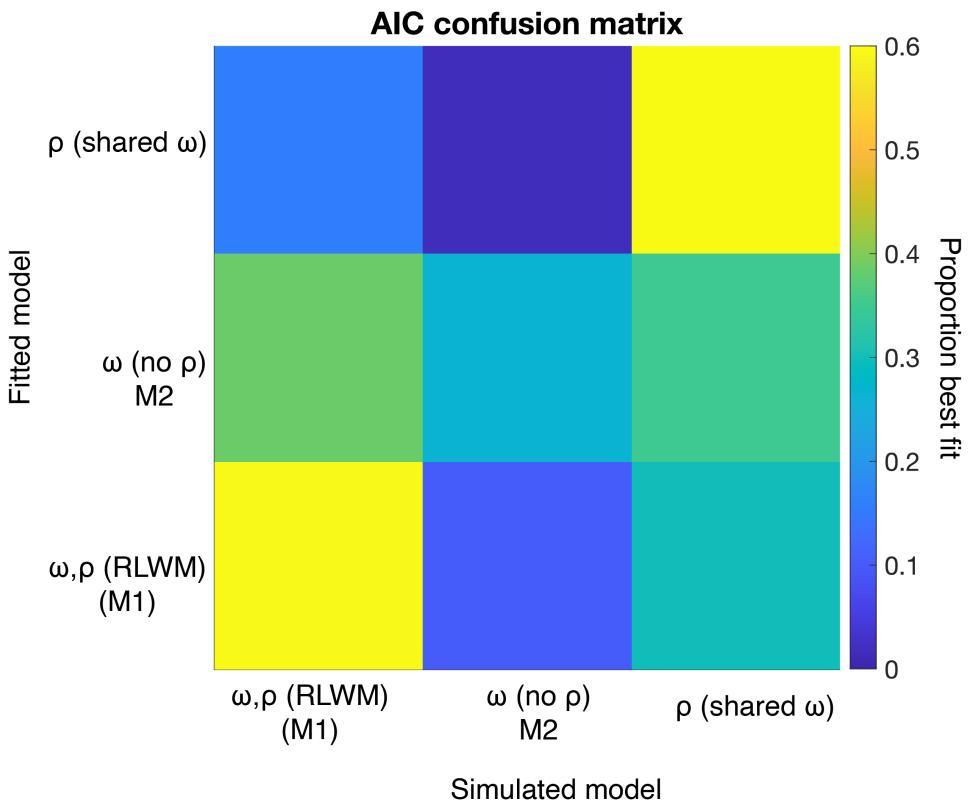


Figure 11: Confusion Matrix 2. Proportion of times the models fitted different simulated data sets best, based on cross-fit AIC scores for models with condition dependent ρ and ω parameters (M1), condition dependent ω (M2), and condition dependent ρ .

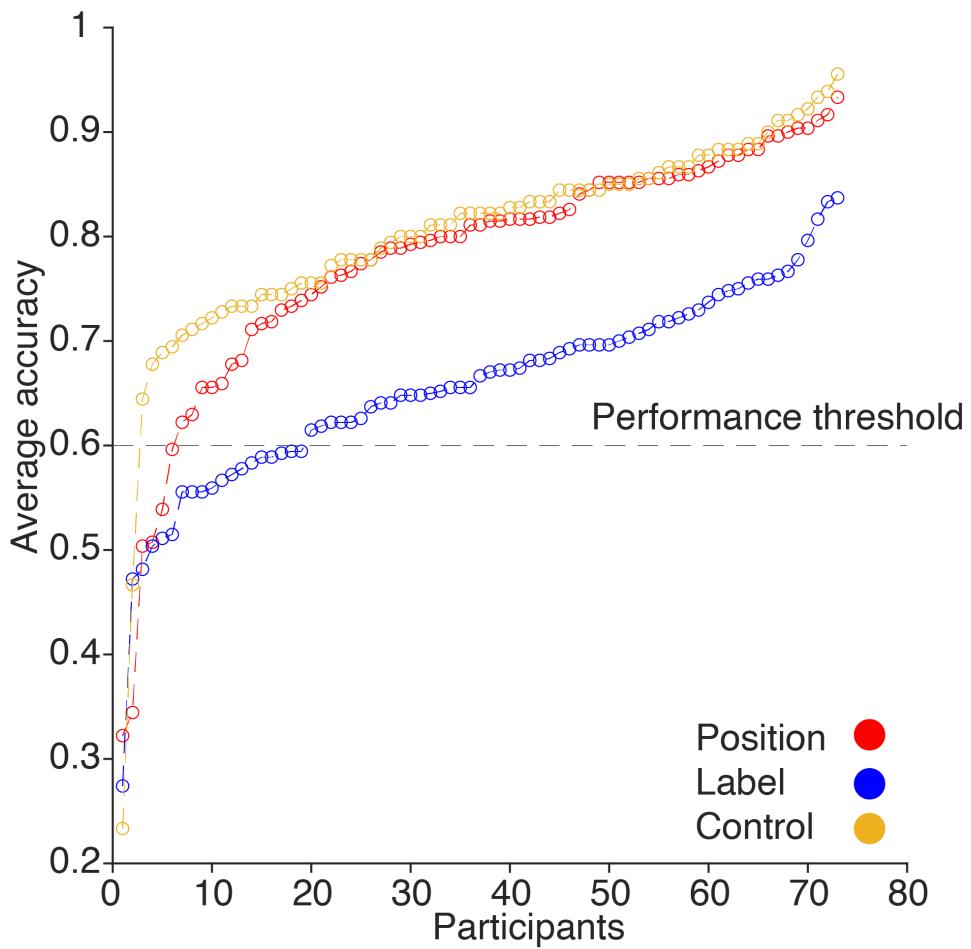
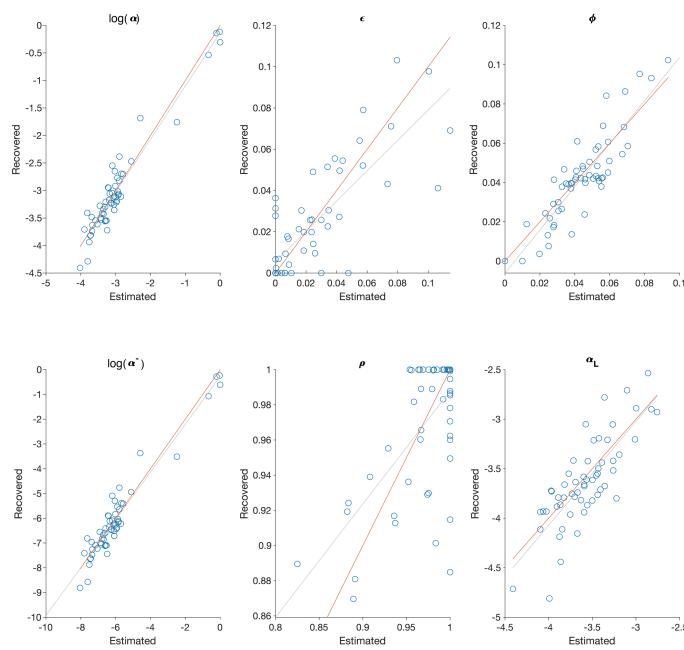


Figure 12: Exclusion criteria based on the task performance. We averaged accuracy across all conditions. Based on the “elbow point”, most participants’ performance is above .60, so we used .60 as criteria for exclusion.

Experiment 1 Best Model Parameter Recovery



Experiment 2 Best Model Parameter Recovery

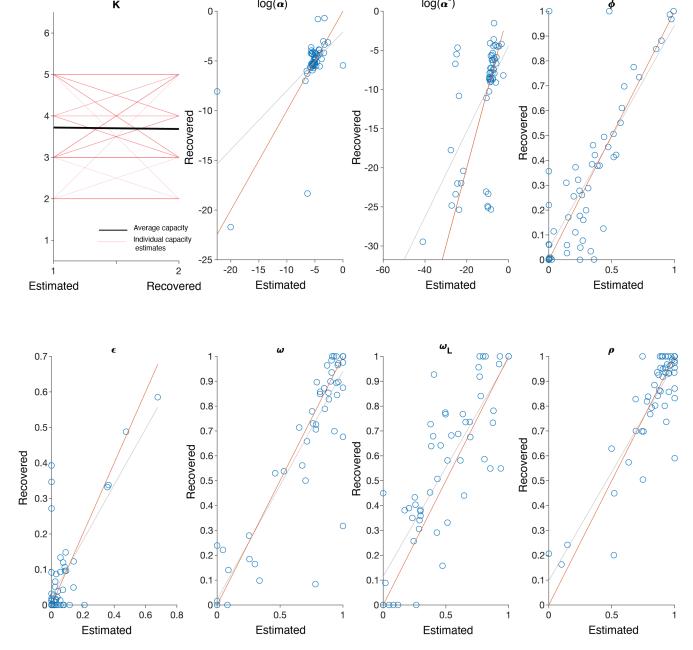


Figure 13: Parameter recovery for the best models in Experiment 1 and Experiment 2.

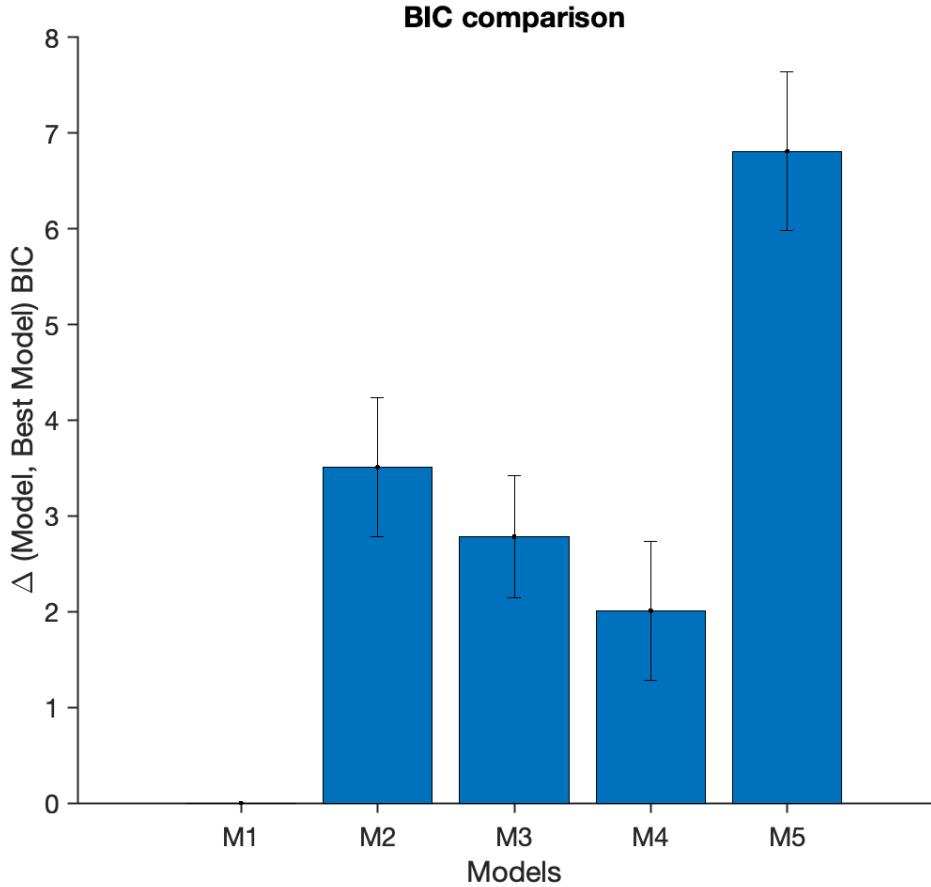


Figure 14: Parameter recovery for the best models in Experiment 1 and Experiment 2.

962

	M1	M2	M3	M4	M5
962	0.20	0.18	0.19	0.22	0.18

963 Table 1. Protected Exceedance Probability of tested models in Experiment 2, computed
 964 based on AIC evidence. Bayes Omnibus Risk *BOR* (indexing the probability that model
 965 frequencies are equal) = 0.94, which suggests that frequency is not strongly differentiable
 966 between models.

967

	M1	M2	M3	M4	M5
967	1	0	0	0	0

968 Table 2. Since BIC provided stronger differentiation between models, we computed the
 969 protected exceedance probability based on BIC evidence. Bayes Omnibus Risk (*BOR*) =

₉₇₀ $1.29e-12$, with $PXP(M1) = 1$, suggests that M1 has the highest frequency.