

Dark Energy Survey Year 3 results: Cosmological constraints from galaxy clustering and galaxy-galaxy lensing using the MAGLIM lens sample

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The cosmological information extracted from photometric surveys is most robust when multiple probes of the large scale structure of the Universe are used. Two of the most sensitive probes are the clustering of galaxies and the tangential shear of background galaxy shapes produced by those foreground galaxies, so-called galaxy-galaxy lensing. Combining the measurements of these two two-point functions leads to cosmological constraints that are independent of the way galaxies trace matter (the galaxy bias factor). The optimal choice of foreground, or *lens*, galaxies is governed by the joint, but conflicting requirements to obtain accurate redshift information and large statistics. We present cosmological results from the full 5000 deg² of the Dark Energy Survey's first three years of observations (Y3) combining those two-point functions, using for the first time a magnitude-limited lens sample (MAGLIM) of 11 million galaxies, especially selected to optimize such combination, and 100 million background shapes. We consider two flat cosmological models, the Standard Model with dark energy and cold dark matter (Λ CDM) a variation with a free parameter for the dark energy equation of state (w CDM). Both models are marginalized over 25 astrophysical and systematic nuisance parameters. In Λ CDM we obtain for the matter density $\Omega_m = 0.320^{+0.041}_{-0.034}$ and for the clustering amplitude $S_8 \equiv \sigma_8(\Omega_m/0.3)^{0.5} = 0.778^{+0.037}_{-0.031}$, at 68% C.L. The latter is only 1σ smaller than the prediction in this model informed by measurements of the cosmic microwave background by the *Planck* satellite. In w CDM we find $\Omega_m = 0.32^{+0.044}_{-0.046}$, $S_8 = 0.777^{+0.049}_{-0.051}$ and dark energy equation of state $w = -1.031^{+0.218}_{-0.379}$. We find that including smaller scales, while marginalizing over nonlinear galaxy bias, improves the constraining power in the $\Omega_m - S_8$ plane by 31% and in the $\Omega_m - w$ plane by 41% while yielding consistent cosmological parameters from those in the linear bias case. These results are combined with those from cosmic shear in a companion paper to present full DES-Y3 constraints from the three two-point functions (3×2 pt).

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I. INTRODUCTION

The discovery of the accelerated expansion of the Universe in the 1990s has opened one of the most enduring and widely researched questions in the field of cosmology: what is the nature of the physical process that powers the acceleration? The source of this increasing expansion rate—a new energy density component, called dark energy—has become a key part of the cosmic inventory, yet its physical nature and microphysical properties are unknown. Over the

course of about two decades since the discovery of dark energy, an impressive variety of measurements from cosmological probes has helped to set tighter constraints on its energy density relative to the critical density Ω_{de} , and its equation of state ratio $w = P_{\text{de}}/\rho_{\text{de}}$, where P_{de} and ρ_{de} are, respectively, the pressure and energy density of dark energy. These probes include distance measurements to type Ia supernovae [1,2], cosmic microwave background fluctuations (CMB) [3,4] and the study of the large-scale structure

(LSS) in our Universe. The latter carries a wealth of cosmological information and allows for tests of the fiducial cold dark matter plus dark energy cosmological model, Λ CDM (e.g. [5–11] and references therein).

In the past few years, early results from Stage-III dark energy surveys have been released, significantly improving the quality and quantity of data and the strength of cosmological constraints from LSS probes of dark energy. The Stage-III surveys include the Dark Energy Survey (DES)¹ [7,12], the Kilo-Degree Survey (KiDS)² [13,14], and Hyper Suprime-Cam Subaru Strategic Program (HSC-SSP)³ [15,16]. These surveys have demonstrated the feasibility of ambitious photometric LSS analyses, and featured extensive testing of theory, inclusion of a large number of systematic parameters in the analysis, and blinding of the analyses before the results are revealed. These photometric LSS surveys have (so far) confirmed the Λ CDM model and tightened the constraints on some of the key cosmological parameters. On the other hand, these surveys have also begun to reveal an apparent tension between the measurements of the parameter, $S_8 \equiv \sigma_8(\Omega_m/0.3)^{0.5}$, the amplitude of mass fluctuations σ_8 scaled by the square root of matter density Ω_m . This is measured to be higher in the CMB ($S_8 \simeq 0.834 \pm 0.016$ [4]) than in photometric surveys, including the Dark Energy Survey Year 1 (Y1) result, $S_8 = 0.794 \pm 0.028$ [12].

New and better data will be key to bring these tensions into sharp focus in order to see if they are due to new physics. The next generation of LSS surveys that will provide high quality data include the Rubin Observatory Legacy Survey of Space and Time (LSST)⁴ [17], Euclid⁵ [18], and the Nancy–Grace–Roman Space Telescope (Roman)⁶ [19]. These upcoming surveys will map the structure in the Universe over a wider and deeper range of temporal and spatial scales (see e.g. [20,21]). Two key cosmological probes that all of these surveys will use are galaxy clustering and weak gravitational lensing.

When selecting a sample of objects to use in a photometric survey, there is a trade-off between selecting the *largest* galaxy sample (to minimize shot noise) and a sample with the best *redshift accuracy*, which generally includes only a small subset of galaxies. The latter strategy typically uses luminous red galaxies (LRGs), which are characterized by a sharp break at 4000 Å [22,23]. LRGs have a remarkably uniform spectral energy distribution and correlate strongly with galaxy cluster positions. Such an approach was taken in the DES Y1 analysis [12], where lens galaxies were selected using the REDMAGiC algorithm [24], which relies on the calibration of the red sequence in

optical galaxy clusters. The KiDS survey recently made a similar selection of red-sequence galaxies [25], and such selection of LRGs in photometric data has also been adopted for measurements of baryon acoustic oscillations [23,26,27].

An alternative strategy is to select the largest galaxy sample possible. Selecting all galaxies up to some limiting magnitude leads to a galaxy sample that reaches a higher redshift, has a much higher number density, but also less accurate redshifts (larger photo- z errors). Such flux-limited samples have been used in the DES Science Verification analysis [28] and, previously, in the galaxy clustering measurements from Canada-France-Hawaii Telescope Legacy Survey (CFHTLS) data [29]; these two analyses had an upper apparent magnitude cut of $i < 22.5$. More recently, Nicola *et al.* [30] also selected galaxies with a limiting magnitude ($i < 24.5$) from the first HSC public data release to analyze the galaxy clustering and other properties of that sample, such as large-scale bias. This kind of galaxy selection is simple and easily reproducible in different datasets and leads to a sample whose properties can be well understood. For instance, Crocce *et al.* [28] showed that the redshift evolution of the linear galaxy bias of their sample matches the one from CFHTLS [29] and is also consistent with that from HSC data [30]. However, this type of selection that selects the largest possible galaxy sample has not yet been used to produce constraints on cosmological parameters.

The DES collaboration recently investigated potential gains in using such a magnitude-limited sample in simulated data in Porredon *et al.* [31]. We assumed synthetic DES Year 3 (Y3) data and the DES Year 1 METACALIBRATION sample of source galaxies and explored the balance between density and photometric redshift accuracy, while marginalizing over a realistic set of cosmological and systematic parameters. The optimal sample, dubbed the MAGLIM sample, satisfies $i < 4z_{\text{phot}} + 18$ and has $\sim 30\%$ wider redshift distributions but ~ 3.5 times more galaxies than REDMAGiC. We found an improvement in cosmological parameter constraints of tens of percent (per parameter) using MAGLIM relative to an equivalent analysis using REDMAGiC. Finally, we showed that the results are robust with respect to the assumed galaxy bias and photometric redshift uncertainties.

In this paper, we show cosmological results from DES-Y3 data using the MAGLIM sample. We specifically consider galaxy clustering and galaxy-galaxy lensing, that is, the autocorrelations of MAGLIM galaxies' positions and their cross-correlation with cosmic shear (2×2 pt). This analysis is complemented by two other papers that combine these two two-point functions from DES-Y3 data: an equivalent analysis using the MAGLIM [32] lens sample [33] and a study of the impact of magnification on the 2×2 pt cosmological constraints, using both MAGLIM and MAGLIM lens samples [34]. In addition, the results presented in this work are combined with the cosmological

¹<http://www.darkenergysurvey.org/>.

²<http://kids.strw.leidenuniv.nl/>.

³<https://hsc.mtk.nao.ac.jp/ssp/>.

⁴<https://www.lsst.org/>.

⁵<https://sci.esa.int/web/euclid>.

⁶<https://roman.gsfc.nasa.gov/>.

analysis of cosmic shear [35,36] in [37] to obtain the final DES-Y3 3×2 pt constraints.

The paper is organized as follows. Section II introduces the data, the mask, and the data-vector measurements. Section III presents different estimations of the photometric redshift distribution of the MAGLIM sample. Section IV describes the simulations used to test the methodology and pipelines. Section V presents the methodology. The validation of the methodology on the simulations and theory data vectors is presented in Sec. VI. Our main results are presented in Sec. VII, along with a discussion of some changes made postunblinding and robustness tests. Conclusions are presented in Sec. VIII. In Appendix A we compare the fiducial photometric redshift estimates for MAGLIM with spectroscopic data. We include a comprehensive discussion of our tests after unblinding the results in Appendix B. Last, in the Appendix C, we show the residuals between the 2×2 pt measurements and the Λ CDM best-fit theory model when using all tomographic bins.

II. DATA

A. DES Y3

DES is an imaging survey that has observed ~ 5000 deg² of the southern sky using the Dark Energy Camera [38] on the 4m Blanco Telescope at the Cerro Tololo Inter-American Observatory in Chile. DES completed observations in January 2019, after six years of operations in which it collected information from more than 500 million galaxies in five optical filters, *grizY*, covering the wavelength range from ~ 400 nm to ~ 1060 nm [39].

In this work we use data from the first three years of observations (Y3), which were taken from August 2013 to February 2016. The core dataset used in Y3 cosmological analyses, the Y3 GOLD catalog, is largely based on the coadded object catalog that was released publicly as the DES Data Release 1 (DR1)⁷ [40] and includes additional enhancements and data products with respect to DR1, as described extensively in [41]. The Y3 GOLD catalog includes nearly 390 million objects with depth reaching $S/N \sim 10$ up to limiting magnitudes of $g = 24.3$, $r = 24.0$, $i = 23.3$, $z = 22.6$, and $Y = 21.4$. Objects are detected using SourceExtractor from the $r + i + z$ coadd images (see [42] for further details). The morphology and flux of the objects is determined through the multi-object fitting pipeline (MOF) and its variant single-object fitting (SOF), which simplifies the fitting process with negligible impact in performance [43].

The SOF photometry is used to generate the photometric redshift (photo- z) estimates from different codes: BPZ [44], ANNz2 [45], and DNF [46]. In this work, we rely on SOF magnitudes and DNF photo- z estimates for the MAGLIM sample selection, which we describe below. For the source

galaxies, we use METACALIBRATION photometry [47] instead of SOF. This photometry is measured similarly to the SOF and MOF pipelines but, while the latter use NGMIX [48] in order to reconstruct the point spread function (PSF), METACALIBRATION uses a simplified Gaussian model for the PSF.

The total area of the Y3 GOLD catalog footprint comprises 4946 deg². For the cosmology analyses presented here we apply a masking that we describe in detail in Sec. IID, resulting in a final area of about 4143.17 deg².

In the following, we describe the selection of our lens and source samples.

B. Lens samples

In what follows, we describe the two lens samples used throughout this work, focusing on the MAGLIM sample. Both these samples present correlations of their galaxy number density with various observational properties of the survey, which they themselves are correlated too. This imprints a nontrivial angular selection function for these galaxies, which translates into biases in the clustering signal if not accounted for. This is a common feature of galaxy surveys, in particular, imaging surveys, and different strategies have been proposed in the literature to mitigate this contamination (e.g. see [49] for a recent review). We correct this effect by applying weights to each galaxy corresponding to the inverse of the estimated angular selection function. The computation and validation of these weights, for both MAGLIM and REDMAGiC, is described in Rodríguez-Monroy *et al.* [32].

1. MAGLIM

The main lens sample considered in this work, MAGLIM, is defined with a magnitude cut in the i band that depends linearly on the photometric redshift z_{phot} , $i < 4z_{\text{phot}} + 18$. This selection is the result of the optimization carried out in Porredon *et al.* [31] in terms of its 2×2 pt cosmological constraints. Additionally, we apply a lower magnitude cut, $i > 17.5$, to remove stellar contamination from binary stars and other bright objects. We split the sample in six tomographic bins from $z = 0.2$ to $z = 1.05$, with bin edges [0.20, 0.40, 0.55, 0.70, 0.85, 0.95, 1.05]. We note that the edges have been slightly modified with respect to [31] in order to improve the photometric redshift calibration.⁸ The number of galaxies in each tomographic bin and other properties of the sample are shown in Table I. In total, MAGLIM amounts to 10.7 million galaxies in the redshift range considered. The abundance of the sample as a function of redshift is shown in Fig. 1 from Ref. [31]. The number of galaxies remains approximately constant with redshift, with a slightly increasing trend in $0.6 < z < 0.9$.

⁷Available at <https://des.ncsa.illinois.edu/releases/dr1>.

⁸With these new bin edges we avoid having a double-peaked redshift distribution in the second tomographic bin.

We would expect more of a monotonically decreasing trend if the sample had a flat magnitude limit (e.g. $i < 22.2$). However, the MAGLIM selection depends linearly on the photometric redshift, which allows including more galaxies at higher redshift. We refer the reader to [31] for more details about the optimization of this sample and its comparison with REDMAGiC and other flux-limited samples. See also Sec. III and Appendix A for further information on the photometric redshift calibration and validation.

2. REDMAGiC

The other lens sample used in the DES-Y3 analysis is selected with the REDMAGiC algorithm [32–34]. REDMAGiC selects LRGs according to the magnitude-color-redshift relation of red sequence galaxy clusters, calibrated using an overlapping spectroscopic sample. This sample is defined by an input threshold luminosity $L_{\min}$ and constant comoving density. The full REDMAGiC algorithm is described in [24].

There are 2.6 million galaxies in the Y3 REDMAGiC sample, which are placed in five tomographic bins, based on the REDMAGiC redshift point estimate quantity ZREDMAGIC. The bin edges used are $z = [0.15, 0.35, 0.50, 0.65, 0.80, 0.90]$. The redshift distributions are computed by stacking samples from the redshift probability distribution function (PDF) of each individual REDMAGiC galaxy, allowing for the non-Gaussianity of the PDF. From the variance of these samples we find an average individual redshift uncertainty of $\sigma_z/(1+z) = 0.0126$ in the redshift range used.

C. Source sample

The source sample that is used for cross-correlation with the foreground lens samples consists of 100,204,026 galaxies with shapes measured in the *riz* bands Y3-shape catalog. The source galaxies cover the same effective area as the foreground lens tracers (after masking described below, 4143.17 deg²), have a weighted source number density of $n_{\text{eff}} = 5.59$ gal/arc min², and shape noise $\sigma_e = 0.261$ per ellipticity component.

The source shapes are measured using the METACALIBRATION method [47,50], which measures the response of a given shear estimator to a small applied shear. The implementation closely follows that of the previous Y1 source shape catalog [51]. For each galaxy, the point-spread function is deconvolved before the artificial shear is applied, and then the image is reconvolved with a symmetrized version of the PSF. Here, as in [51], the ellipticities are calculated from single Gaussians using the NGMIX software.⁹ The PSF models used in the aforementioned deconvolution step have been measured with the PSFs in the full field of view (PIFF) software [52]. Gatti, Sheldon

et al. [53] provide a full account of the catalog creation and a set of validation tests, including checks for B modes and correlations between shape measurements and a number of galaxy and survey properties. An accompanying paper [54] calibrates the shear measurement pipeline on a suite of realistic image simulations. The relationship between an input shear γ and measured shape ϵ^{obs} is given by

$$\epsilon^{\text{obs}} = (1 + m)(\epsilon^{\text{int}} + \gamma) + c. \quad (1)$$

MacCrann *et al.* [54] determine the multiplicative bias m and the additive bias c using our full object detection and shape measurement pipeline. ϵ^{int} is the intrinsic galaxy shape, part of which is random with mean zero and variance σ_e^2 and the other part of which is due to *intrinsic alignment*, discussed in Sec. VI. Note that ellipticity and shear have two components, so Eq. (1) is often written with appropriate indices, suppressed here.

The source sample is subdivided into four tomographic bins, with corresponding redshift distributions and uncertainties derived in Myles, Alarcon *et al.* [55] using the self-organizing map photometric redshift (SOMPZ) method. The cross-correlation redshift (WZ) approach provides further calibration, as described in Gatti, Giannini *et al.* [56]. The “source sample” section of Table I provides the number of galaxies, densities, and shape noise for the source galaxies separated into the SOMPZ-defined redshift bins (more details in Table I from [35]).

D. Mask

As mentioned previously the area of the Y3 GOLD catalog footprint spans 4946 deg². However, additional masking is imposed to remove regions with either astrophysical foregrounds (bright stars or nearby galaxies) or with recognized data processing issues (“bad regions”). This is achieved by a set of flags that we describe below, leading to a reduction of area by 659.68 deg² [41]. This mask is defined on a pixelated HEALPIX map [57] of resolution 4096. From that map we remove pixels with fractional coverage less than 80%. Lastly, we ensure that both samples used for clustering have homogeneous depth across the footprint in all redshift bins by removing shallow and incomplete regions, using the corresponding limiting depth maps (or the quantity ZMAX in the case of REDMAGiC). In all, the Y3 GOLD catalog quantities [41] we select to define the final mask are summarized by the following:

- (i) footprint ≥ 1
- (ii) foreground $= 0$
- (iii) badregions ≤ 1
- (iv) fracted > 0.8
- (v) depth *i*-band ≥ 22.2
- (vi) ZMAX_{highdens} > 0.65
- (vii) ZMAX_{highlum} > 0.90

⁹<https://github.com/esheldon/ngmix>.

where depth i -band corresponds to SOF photometry (as used in MAGLIM) and the conditions on ZMAX are inherited from the REDMAGiC redshift span. For simplicity, we apply the same mask for all our samples, resulting in a final effective area of 4143.17 deg².

E. Data-vector measurements

We are extracting cosmological information using the combination of two two-point correlation functions: (1) the autocorrelation of angular positions of lens galaxies (also known as *galaxy clustering*) and (2) the cross-correlation of lens galaxy positions and source galaxy shapes (also known as *galaxy-galaxy lensing*). These angular correlation functions are computed after the galaxies have been separated into tomographic bins, as presented in Table I.

1. Galaxy clustering

The two-point function between galaxy positions in redshift bins i and j , $w^{ij}(\theta)$, describes the excess (over

TABLE I. Summary description of the samples used in this work. N_{gal} is the number of galaxies in each redshift bin, n_{gal} is the effective number density (including the weights for each galaxy) in units of gal/arc min², “bias” refers to the 68% C.L. constraints on the linear galaxy bias from the $3 \times 2\text{pt}$ Λ CDM cosmology result described in [37], C is the magnification coefficient as measured in [34] and defined in Sec. VA, and σ_e is the weighted standard deviation of the ellipticity for a single component as computed in [35].

Lens sample 1: MAGLIM				
Redshift bin	N_{gal}	n_{gal}	Bias	C
1: $0.20 < z_{\text{ph}} < 0.40$	2 236 473	0.150	$1.40^{+0.10}_{-0.09}$	0.43
2: $0.40 < z_{\text{ph}} < 0.55$	1 599 500	0.107	$1.60^{+0.13}_{-0.10}$	0.30
3: $0.55 < z_{\text{ph}} < 0.70$	1 627 413	0.109	$1.82^{+0.13}_{-0.10}$	1.75
4: $0.70 < z_{\text{ph}} < 0.85$	2 175 184	0.146	$1.70^{+0.12}_{-0.09}$	1.94
5: $0.85 < z_{\text{ph}} < 0.95$	1 583 686	0.106	$1.91^{+0.14}_{-0.10}$	1.56
6: $0.95 < z_{\text{ph}} < 1.05$	1 494 250	0.100	$1.73^{+0.14}_{-0.10}$	2.96
Lens sample 2: REDMAGiC				
Redshift bin	N_{gal}	n_{gal}	Bias	C
1: $0.15 < z_{\text{ph}} < 0.35$	330 243	0.022	$1.74^{+0.10}_{-0.13}$	0.63
2: $0.35 < z_{\text{ph}} < 0.50$	571 551	0.038	$1.82^{+0.11}_{-0.11}$	−3.04
3: $0.50 < z_{\text{ph}} < 0.65$	872 611	0.058	$1.92^{+0.11}_{-0.12}$	−1.33
4: $0.65 < z_{\text{ph}} < 0.80$	442 302	0.029	$2.15^{+0.11}_{-0.13}$	2.50
5: $0.80 < z_{\text{ph}} < 0.90$	377 329	0.025	$2.32^{+0.13}_{-0.14}$	1.93
Source sample: METACALIBRATION				
Redshift bin	N_{gal}	n_{gal}	σ_e	C
1	24 941 833	1.476	0.243	−1.32
2	25 281 777	1.479	0.262	−0.62
3	24 892 990	1.484	0.259	−0.02
4	25 092 344	1.461	0.301	0.92

random) number of galaxies separated by an angular distance θ . Our fiducial result uses only the autocorrelation of galaxies in the same bin ($i = j$). This correlation is measured in 20 logarithmic angular bins between 2.5 and 250 arc min. Some of these bins are removed after imposing scale cuts, see Sec. VI A, leaving a total data-vector size of 69 elements for MAGLIM and 54 for REDMAGiC (only autocorrelations on linear scales). The validation and robustness of the clustering signal measurement for both MAGLIM and REDMAGiC is presented in detail in Rodríguez-Monroy *et al.* [32].

2. Galaxy-galaxy lensing

The two-point function between lens galaxy positions and source galaxy shear in redshift bins i and j , $\gamma_i^{ij}(\theta)$, describes the overdensity of mass around galaxy positions. The matter associated with the lens galaxy alters the path of the light emitted by the source galaxy, thereby distorting its shape and enabling a nonzero cross-correlation. We consider all possible bin combinations, i.e. allowing the lenses to be in front or behind the sources (in the later case, a nonzero physical signal would be due to magnification). This correlation is also measured in 20 logarithmic angular bins between 2.5 and 250 arc min. After imposing scale cuts, the total data-vector size in γ_i is 304 elements when MAGLIM is the lens sample and 248 for REDMAGiC. The validation and robustness of the galaxy-galaxy lensing signal is discussed in detail in Prat *et al.* [58].

In the Appendix C, we show the measurements of these two-point functions and compare them with the best-fit Λ CDM theory prediction from this work.

III. PHOTOMETRIC REDSHIFT CALIBRATION

We now present our three different estimations for the true redshift distributions in each tomographic bin and how we cross-validate or combine them.

A. DNF

We use DNF [46] to select the MAGLIM galaxies, assign them into tomographic bins, and estimate their redshift distributions $n(z)$, which are shown in Fig. 1. For the former, the algorithm computes a point estimate z_{DNF} of the true redshift by performing a fit to a hyperplane using 80 nearest neighbors in color and magnitude space taken from reference set that has an associated true redshift from a large spectroscopic database. In this work, this database has been constructed using a variety of catalogs using the DES Science Portal [59]. The reference catalog includes $\sim 2.2 \times 10^5$ spectra matched to DES objects from 24 different spectroscopic catalogs, most notably Sloan Digital Sky Survey (SDSS) DR14 [60], DES’s own follow-up through the Optical redshifts for the Dark Energy Survey program (OzDES) [61], and VIMOS Public Extragalactic Redshift Survey (VIPERS) [62]. Half of these spectra have been

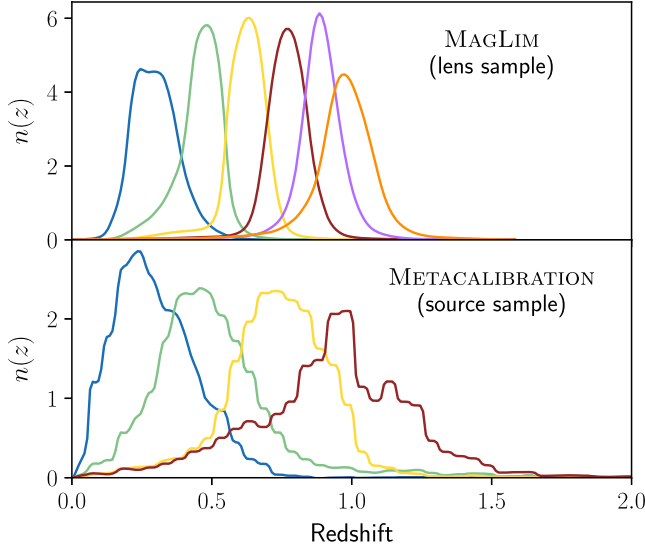


FIG. 1. Redshift distributions of the MAGLIM lens sample and the METACALIBRATION source sample. The distributions are normalized to 1, i.e. we impose $\int n(z)dz = 1$.

used as a reference catalog for DNF. In addition, we have added the most recent redshift estimates from the Physics of the Accelerating Universe (PAU) spectrophotometric catalog (40 narrow bands) from the overlapping CFHTLS W1¹⁰ wide field [63]. In Appendix A we compare the DNF point estimates with the spectroscopic redshifts from VIPERS and give more details on the photometric redshift uncertainty of the sample and its outlier rates.

DNF also provides a PDF estimation for each individual galaxy by aggregating the quantities $z_i = z_{\text{DNF}} + s_i$, where s_i are the residuals resulting from the i th neighbor to the fitted hyperplane. The sample of all z_i then undergoes a kernel density estimation process to smooth the distribution.

We then estimate the redshift distribution in each tomographic bin by stacking all the PDFs provided by DNF. These distributions will be calibrated using the cross-correlation technique (clustering redshifts) described below. Figure 2 shows that they agree very well with clustering redshifts after such calibration, which consists of applying shift and stretch parameters (see Sec. VB 1) to match the mean and width of the clustering redshift estimates. See Sec. VIC for a detailed description and validation of these parameters.

B. Clustering redshifts

We calibrate the photometric redshift distributions using clustering redshifts (also known as cross-correlation redshifts) as described in Cawthon *et al.* [64]. In that work, the angular positions of the REDMAGiC and MAGLIM galaxies

are cross-correlated with a spectroscopic sample of galaxies from the Baryon Oscillation Spectroscopic Survey (BOSS) [65] and its extension, eBOSS [66]. The amplitudes of these cross-correlations are proportional to the redshift overlaps of the photometric and spectroscopic samples. When the spectroscopic sample is divided into small bins, the cross-correlations with each bin put constraints on the true redshift distribution of the photometric samples. Since DES only has partial sky overlap with BOSS and eBOSS, the cross-correlations can only be measured on about 632 deg^2 , or 15% of the full area.

For this work, the spectroscopic samples are divided into bins of size $dz = 0.02$. Cawthon *et al.* [64] estimate the DES $n(z)$ in each of these $dz = 0.02$ size bins using clustering redshifts across the five REDMAGiC and six MAGLIM tomographic bins.

C. SOMPZ

An independent redshift calibration is also performed, analogously to the fiducial method for the source sample [55], placing constraints on the $n(z)$ distribution by relying on the complementary combination of phenotypic galaxy classification done through SOMPZ and the aforementioned clustering redshifts. The methodology and results are described in more detail in Giannini *et al.* [67]. In the SOMPZ method we exploit the additional bands in the DES deep fields to accurately characterize those galaxies and validate their redshift through three different high precision redshift samples: (1) the spectroscopic compilation by Gschwend *et al.* [59]; (2) the 30-band photometric redshift catalog in the Cosmic Evolution Survey (COSMOS) field from Laigle *et al.* [68]; (3) the PAU + COSMOS 66-band photometric redshift catalog [69]. The redshift information is transferred to MAGLIM through an overlap sample, built by the Balrog algorithm from Everett, Yanny *et al.* [70].

The output of this pipeline is a set of $n(z)$ realizations, whose variability spans all uncertainties. We combine these with clustering redshifts information, estimated in the full redshift range of the BOSS/eBOSS [65,66] used as reference samples with high quality redshifts, to place a likelihood of obtaining the cross-correlations data given each of the $n(z)$ SOMPZ estimates. The combination places tighter constraints on the shape of the distribution, despite not improving in terms of the uncertainty on the mean of the $n(z)$. The final sets of realizations have been computed in bins with $dz = 0.02$ and up to $z = 3$ and are compatible with the fiducial DNF $n(z)$, as shown in Fig. 3.

IV. SIMULATIONS

Parts of the analysis presented in this work have been validated using the BUZZARD suite of cosmological simulations. We briefly describe these simulations here and refer

¹⁰<https://www.cfht.hawaii.edu/Science/CFHLS/cfhtlsdeepwidefields.html>.

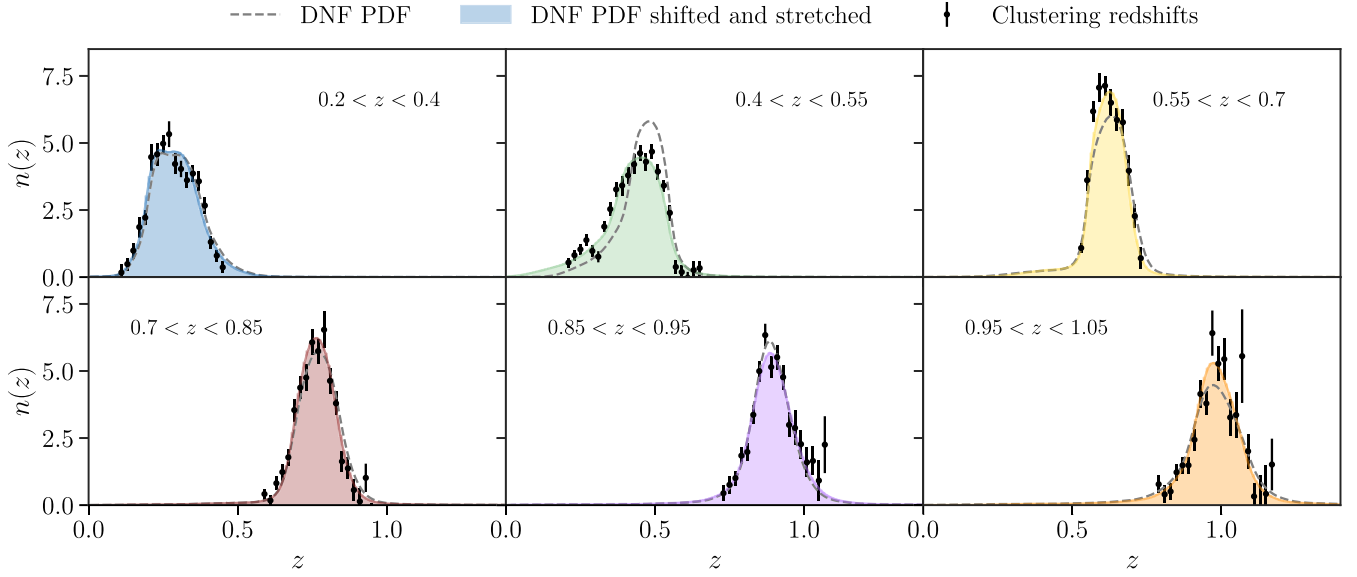


FIG. 2. Comparison of MAGLIM redshift distributions obtained with DNF (dashed) and clustering redshifts (error bars). The filled regions show the DNF redshift distributions after applying the fiducial shift and stretch parameters to match the mean and width of the clustering redshift estimates. See Secs. VB 1 and VIC for the definition and validation of these parameters, respectively.

the reader to DeRose *et al.* [71] for a comprehensive discussion.

The BUZZARD simulations are synthetic DES-Y3 galaxy catalogs that are constructed from N -body light cones, updated from the version used in the DES Y1 analyses [72]. Galaxies are included in the dark-matter-only light cones using the ADDGALS algorithm [73,74], which assigns a position, velocity, spectral energy distribution, half-light radius, and ellipticity to each galaxy. There are a total of 18 DES-Y3 BUZZARD simulations. Each pair of two Y3 simulations is produced from a suite of three independent

N -body light cones with box sizes of $[1.05, 2.6, 4.0] (h^{-3} \text{ Gpc}^3)$, mass resolutions of $[0.33, 1.6, 5.9] \times 10^{11} h^{-1} M_{\odot}$, and spanning redshift ranges in the intervals $[0.0, 0.32, 0.84, 2.35]$, respectively. These light cones are produced using the L-GADGET2 code, a version of GADGET2 [75] that is optimized for dark-matter-only simulations. Initial conditions are generated at $z = 50$ using 2nd-order lagrangian perturbation theory initial conditions (2LPTIC) [76]. Ray tracing is performed on these simulations using Curved-sky gravitational lensing for cosmological light cone simulations (CALCLENS) [77], with an effective

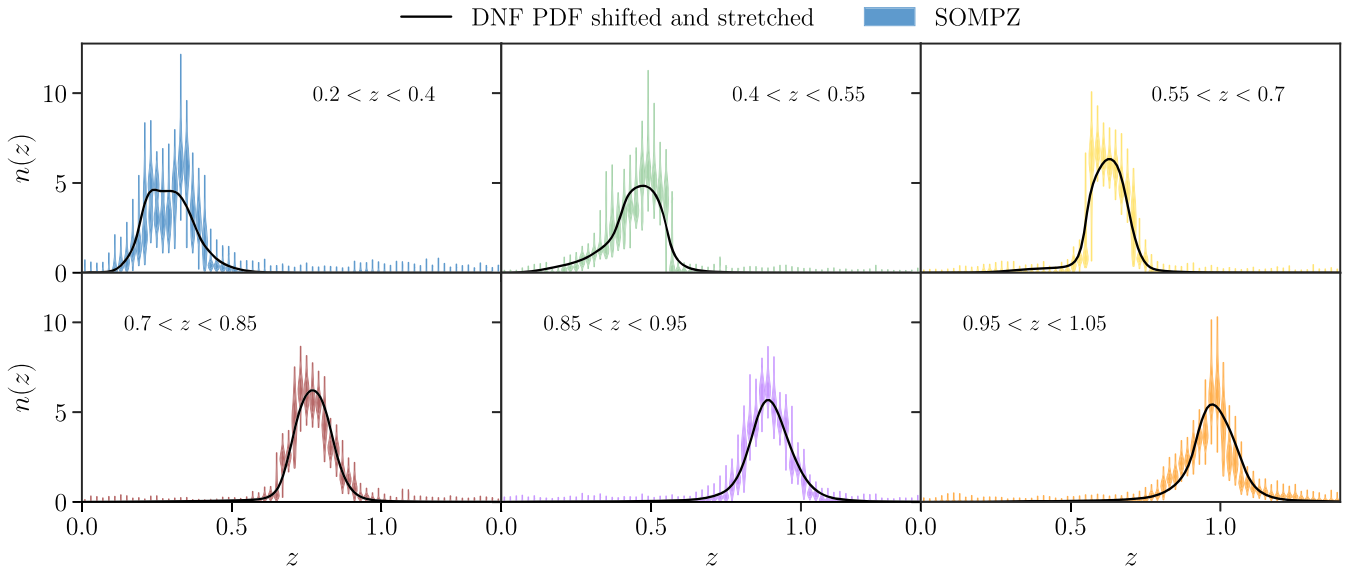


FIG. 3. Comparison of MAGLIM redshift distributions obtained with DNF (solid black) and SOMPZ (violin plot). The DNF redshift distributions are shown after applying the fiducial shift and stretch parameters from Table II.

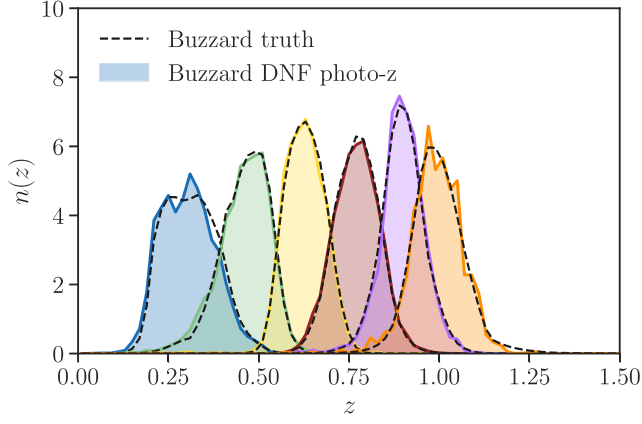


FIG. 4. MAGLIM BUZZARD redshift distributions obtained with DNF (solid filled) compared with the true distributions (dashed black).

angular resolution of 0.43 arc min. CALCLENS computes the lensing distortion tensor at each galaxy position, and this is used to calculate angular deflections and rotations, weak lensing shear, and convergence.

The DES-Y3 footprint mask is used to apply a realistic survey geometry to each simulation [41], resulting in a footprint with an area of 4143.17 deg², and photometric errors are applied to each galaxy’s photometry using a relation derived from BALROG [70]. Weak lensing source galaxies are selected using the PSF-convolved sizes and *i*-band signal-to-noise ratios, matching the nontomographic source number density in the METACALIBRATION source catalog derived from the DES-Y3 data. The SOMPZ framework is used to bin source galaxies into tomographic bins, each having a number density of $n_{\text{eff}} = 1.48$ gal/arc min², and to obtain estimates of the redshift distribution of source galaxies [55, 71]. The shape noise of the simulations is then matched to that measured in the METACALIBRATION catalog per bin.

In order to reproduce the MAGLIM sample itself in the simulation, the DNF code has been run on a subset of one BUZZARD realization,¹¹ conservatively cut at *i*-band magnitude $i < 23$ to reduce the running time. Due to the small differences in magnitude/color space between the BUZZARD simulation and the DES data, the fiducial MAGLIM selection applied in BUZZARD leads to different number densities and color distributions. When applying the fiducial MAGLIM selection to BUZZARD we find the following number densities $n_{\text{gal}} = [0.106, 0.108, 0.030, 0.072, 0.137, 0.068]$, which should be compared with the values from the data in Table I. Besides the second bin, which has n_{gal} very similar to the data, the number densities in BUZZARD are about 30% larger in the fifth redshift bin, and between ~30% and 70% smaller in the remaining bins. We therefore redefine an

¹¹Since running the DNF code on such a large *N*-body catalog is computationally expensive, we use only one BUZZARD realization to reduce the total running time.

adequate MAGLIM selection for BUZZARD by identifying the parameters of the linear relation that, in each bin, minimizes the difference in number density with respect to data, simultaneously requiring the edge values of adjacent bins to correspond to avoid discontinuity between bins. The resulting linear relation in each bin is quite similar to the data, the larger changes being an increase of around 5% on the *i*-band magnitude cut at $z = 0.2$ and $z = 0.95$, with smaller differences in the remaining redshift bin edges. We then estimate the redshift distributions stacking the DNF nearest-neighbor redshifts (see Sec. III A), which is consistent with the fiducial method used for the data. In Fig. 4 we compare these with the true redshift distributions, finding good agreement.

The 2×2 pt data vector is measured without shape noise using the same pipeline as used for the data, with METACALIBRATION responses and inverse variance weights set to 1 for all galaxies. In Sec. VI A we validate the scale cuts by analyzing these 2×2 pt data vectors using the same BUZZARD realization for both MAGLIM and REDMAGIC.

V. ANALYSIS METHODOLOGY

A. Theory modeling

1. Field level

Galaxy density field.—On large scales the observed galaxy density contrast is characterized by four main physical contributions: (1) clustering of matter, (2) galaxy bias, (3) redshift space distortions (RSD), and (4) magnification (μ), in such a way that the observed overdensity in a tomographic bin *i* projected on the sky can be expressed as

$$\delta_{g,\text{obs}}^i(\hat{\mathbf{n}}) = \delta_{g,\text{D}}^i(\hat{\mathbf{n}}) + \delta_{g,\text{RSD}}^i(\hat{\mathbf{n}}) + \delta_{g,\mu}^i(\hat{\mathbf{n}}), \quad (2)$$

where the first term is the line-of-sight projection of the three-dimensional galaxy density contrast,

$$\delta_{g,\text{D}}^i(\hat{\mathbf{n}}) = \int d\chi W_{\delta}^i(\chi) \delta_g^{i,(3\text{D})}(\hat{\mathbf{n}}\chi, \chi), \quad (3)$$

with χ the comoving distance, and $W_{\delta}^i = n_g^i(z) dz/d\chi$ the normalized selection function of galaxies in tomography bin *i*.

For the baseline analysis, we adopt a *linear galaxy bias* model with constant galaxy bias per tomographic bin,

$$\delta_g^{i,(3\text{D})}(\mathbf{x}) = b^i \delta_m(\mathbf{x}). \quad (4)$$

Throughout this work, we ignore galaxy bias evolution within a given redshift bin. This assumption is validated with *N*-body simulations in Sec. VI A.

For some cases, we employ a *perturbative galaxy bias model to third order* in the density field from [78] that includes contributions from local quadratic bias b_2^i , tidal

quadratic bias $b_{s^2}^i$, and third-order nonlocal bias b_{3nl}^i . As validated in [79] and Sec. VI, we fix the bias parameters $b_{s^2}^i$ and b_{3nl}^i to their coevolution value of $b_{s^2}^i = -4(b^i - 1)/7$ and $b_{3nl}^i = b^i - 1$ [78].

The magnification term is given by

$$\delta_{g,\mu}^i(\hat{\mathbf{n}}) = C^i \kappa_g^i(\hat{\mathbf{n}}), \quad (5)$$

with the magnification bias amplitude C^i , and where we have introduced the tomographic convergence field

$$\kappa_g^i(\hat{\mathbf{n}}) = \int d\chi W_{\kappa,g}^i(\chi) \delta_m(\hat{\mathbf{n}}\chi, \chi), \quad (6)$$

with the tomographic lens efficiency

$$W_{\kappa,g}^i(\chi) = \frac{3\Omega_m H_0^2}{2} \int_{\chi}^{\chi_H} d\chi' n_g^i(\chi') \frac{\chi}{a(\chi)} \frac{\chi' - \chi}{\chi'}, \quad (7)$$

where χ_H is the comoving distance to the horizon and $a(\chi)$ is the scale factor. See Krause *et al.* [80] for the complete expressions.

Galaxy shear field.—In a similar manner the galaxy shear γ has two components, and its modeling on large scales is mainly driven by the following contributions: (1) gravitational shear, with contributions from dark-matter nonlinear growth, as well as baryon physics, (2) intrinsic alignments (IA), and (3) stochastic shape noise.

The two components γ_α of the observed galaxy shapes are modeled as gravitational shear (G) and intrinsic ellipticity. The latter is split into a spatially coherent contribution from intrinsic galaxy alignments (IA), and stochastic shape noise ϵ_0 ,

$$\gamma_\alpha^j(\hat{\mathbf{n}}) = \gamma_{\alpha,G}^j(\hat{\mathbf{n}}) + \epsilon_{\alpha,IA}^j(\hat{\mathbf{n}}) + \epsilon_{\alpha,0}^j(\hat{\mathbf{n}}). \quad (8)$$

We model the intrinsic alignments of galaxies using the tidal alignment tidal torquing model [TATT, [81]]. This model includes linear alignments with amplitude parameter a_1 and redshift evolution parameter η_1 , quadratic alignments with amplitude parameter a_2 and redshift evolution parameter η_2 , as well density weighting of the linear alignments with normalization b_{TA} . A detailed description of these terms can be found in [80], and we refer to Secco, Samuroff *et al.* [36] for a discussion of the intrinsic alignment model. For computational convenience, the shear and intrinsic alignment fields are split into E/B-mode components; to leading order in the lensing distortion, B-modes are only generated by intrinsic alignments.

2. Two-point statistics

The observable angular power spectra are then computed by considering the different physical components at the field level. For galaxy-galaxy lensing this results in

$$C_{\delta_{g,obs}E}^{ij}(\ell) = C_{\delta_{g,D}\kappa_s}^{ij}(\ell) + C_{\delta_{g,D}IE}^{ij}(\ell) + C_{\delta_{g,\mu}\kappa}^{ij}(\ell) + C_{\delta_{g,\mu}IE}^{ij}(\ell), \quad (9)$$

where we omitted the RSD term, which is negligible for the DES-Y3 lens tomography bin choices [82]. Here, the individual terms are evaluated using the Limber approximation

$$C_{AB}^{ij}(\ell) = \int d\chi \frac{W_A^i(\chi) W_B^j(\chi)}{\chi^2} P_{AB}\left(k = \frac{\ell + 0.5}{\chi}, z(\chi)\right), \quad (10)$$

with P_{AB} the corresponding three-dimensional power spectra, which are detailed in Krause *et al.* [80].

The angular clustering power spectra has to be evaluated exactly, as the Limber approximation is insufficient at the accuracy requirements of the DES-Y3 analysis. For example, the exact expression for the density-density contribution to the angular clustering power spectrum is

$$C_{\delta_{g,D}\delta_{g,D}}^{ij}(\ell) = \frac{2}{\pi} \int d\chi_1 W_{\delta,g}^i(\chi_1) \int d\chi_2 W_{\delta,g}^j(\chi_2) \times \int \frac{dk}{k} k^3 P_{gg}(k, \chi_1, \chi_2) j_\ell(k\chi_1) j_\ell(k\chi_2), \quad (11)$$

and the full expressions, including magnification and redshift-space distortion, are given in [82]. Schematically, the integrand in Eq. (11) is split into the contribution from nonlinear evolution, for which unequal time contributions are negligible so that the Limber approximation is sufficient, and the linear-evolution power spectrum, for which time evolution factorizes. We use the generalized FFTLog algorithm¹² developed in [82] to evaluate the full angular clustering power spectrum, including magnification and redshift-space distortion contributions.

The angular correlation functions are then obtained via

$$w^i(\theta) = \sum_{\ell} \frac{2\ell + 1}{4\pi} P_{\ell}(\cos \theta) C_{\delta_{l,obs}\delta_{l,obs}}^{ii}(\ell), \quad (12)$$

$$\gamma_t^{ij}(\theta) = \sum_{\ell} \frac{2\ell + 1}{4\pi\ell(\ell + 1)} P_{\ell}^2(\cos \theta) C_{\delta_{l,obs}E}^{ij}(\ell), \quad (13)$$

where P_{ℓ} and P_{ℓ}^2 are the Legendre polynomials.

The tangential shear two-point statistic γ_t is a nonlocal measure of the galaxy-mass cross-correlation, hence the highly nonlinear small-scale galaxy mass profile contributes to γ_t even at large angular scales. Several methods have been proposed to mitigate this effect [e.g. [83–85]]. Here we adopt analytic marginalization over the mass enclosed below the angular scales included in the analysis.

¹²<https://github.com/xfangcosmo/FFTLog-and-beyond>.

Following the procedure detailed in MacCrann *et al.* [84], we implement the analytic marginalization by modifying the inverse of our fiducial covariance matrix $\mathbf{C}^{-1}$:

$$\mathbf{C}_{\text{wPM}}^{-1} = \mathbf{C}^{-1} - \mathbf{C}^{-1}\mathbf{U}(\mathbf{I} + \mathbf{U}^T\mathbf{C}^{-1}\mathbf{U})^{-1}\mathbf{U}^T\mathbf{C}^{-1}. \quad (14)$$

Here $\mathbf{I}$ is the identity matrix, and $\mathbf{U}$ is an $N_d \times n_{\text{lens}}$ matrix, where N_d is the total number of elements in the data vector and n_{lens} is the number of lens redshift bins. The i th column of matrix $\mathbf{U}$ is given by $\sigma_{B^i} \mathbf{t}^i$, where σ_{B^i} is the width of the Gaussian prior on the point-mass parameter B^i we want to marginalize over and $\mathbf{t}^i = \beta^{i,j}/\theta^2$. The $\beta^{i,j}$ parameters modulate the impact of the point-mass parameters on each lens-source pair through their dependence on the effective inverse Σ_{crit} , a geometrical factor that depends on the angular diameter distances to the lenses, to the sources, and between lenses and sources. We refer the reader to Pandey *et al.* [33] for a more detailed description of the implementation and validation of the point-mass analytic marginalization.

B. Parameter inference and likelihood

Parameter inference requires four components: a dataset $\hat{\mathbf{D}} \equiv \{\hat{w}^i(\theta), \hat{\gamma}_i^{ij}(\theta)\}$, a theoretical model $\mathbf{T}_M(\mathbf{p}) \equiv \{w^i(\theta, \mathbf{p}), \gamma_i^{ij}(\theta, \mathbf{p})\}$, a description of the covariance of the dataset $\mathbf{C}$, and a set of priors on the model M . We assume a Gaussian likelihood,

$$\ln \mathcal{L}(\hat{\mathbf{D}}|\mathbf{p}) = -\frac{1}{2}(\hat{\mathbf{D}} - \mathbf{T}(\mathbf{p}))^T \mathbf{C}^{-1}(\hat{\mathbf{D}} - \mathbf{T}(\mathbf{p})). \quad (15)$$

The covariance is modeled analytically as described and validated in [86–89]. We also account for an additional uncertainty in the $w(\theta)$ covariance that is related to the correction of observational systematics, as described in Rodríguez-Monroy *et al.* [32]. The covariance is modified to analytically marginalize over two terms, one given by the difference between correction methods and another one related to the bias of the fiducial correction method as measured on simulations.

In addition to the main galaxy clustering and galaxy-galaxy lensing likelihood described above, we also incorporate small-scale shear ratios (SR) at the likelihood level. This methodology is described in detail by Sánchez, Prat *et al.* [90]. The main idea is that by taking the ratio of galaxy-galaxy lensing measurements with a common set of lenses, but sources at different redshifts, the power spectra approximately cancel, and one is left with a primarily geometric measurement. Shear ratios were initially proposed as a probe of cosmology (see e.g. [91]), but they have proven more powerful as a method for constraining systematics and nuisance parameters of the model, especially those related to redshift calibration and intrinsic alignments.

In particular, we choose to use SR on small scales that are not used in the galaxy-galaxy lensing measurement of this work (< 6 Mpc/ h , see Sec. VI A), where uncertainties are dominated by galaxy shape noise, such that the likelihood can be treated as independent of that from the galaxy-galaxy lensing data (which also removes small-scale information via point-mass marginalization). As before, we assume a Gaussian likelihood and derive the analytic covariance matrix from CosmoLike [87–89]. Due to the relative lack of signal-to-noise ratio in the higher redshift bins, we use only the three lens bins that are lower in redshift and compute shear ratios for each lens bin l relative to the fourth source bin, $\gamma_l^{ls}/\gamma_l^{l4}$, $s \in (1, 2, 3)$. This results in three data vectors per lens bin, or nine overall. See Sánchez, Prat *et al.* [90] for the validation and discussion of the SR constraints.

The posterior probability distribution for the parameters is related to the likelihood through the Bayes' theorem:

$$P(\mathbf{p}|\hat{\mathbf{D}}, M) \propto \mathcal{L}(\hat{\mathbf{D}}|\mathbf{p}, M)\Pi(\mathbf{p}|M), \quad (16)$$

where $\Pi(\mathbf{p}|M)$ is a prior probability distribution on the parameters given a model M . We report parameter constraints using the mean of the marginalized posterior distribution of each parameter, along with the 68% C.L. around the mean. For some cases, we also report the best-fit maximum posterior values. In addition, in order to compare the constraining power of different analysis scenarios, we use the 2D figure of merit (FoM), defined as $\text{FoM}_{p_1, p_2} = (\det \text{Cov}(p_1, p_2))^{-1/2}$, where p_1 and p_2 are any two given parameters [92,93]. The FoM is proportional to the inverse area of the confidence region in the $p_1 - p_2$ space.

To support redundancy in the likelihood inference we implement two versions of the modeling and inference pipelines: CosmoSIS¹³ [94] and CosmoLike [88]. They have been tested against one another to ensure necessary accuracy in calculations of the theoretical two-point functions as described in Rodríguez-Monroy *et al.* [80]. They use a combination of publicly available packages [95–98] and internally developed code. Parameter inference is primarily performed using the PolyChord sampler [99,100], but results have been cross-checked against Emcee [101].

1. Parameter space and priors

We sample the likelihood of clustering and galaxy-galaxy lensing measurements over a set of cosmological, astrophysical and systematics parameters, whose fiducial values and priors are summarized in Table II. We do this in two cosmological models, Λ CDM and w CDM, in both cases assuming a flat universe and a free neutrino mass.

¹³<https://bitbucket.org/joezuntz/cosmosis>.

Cosmological parameters.—For Λ CDM we sample over the total matter density Ω_m , the amplitude of primordial scalar density fluctuations A_s , the spectral index n_s of their power spectrum, the baryonic density Ω_b , and the Hubble parameter h . We also vary the massive neutrino density Ω_ν through the combination $\Omega_\nu h^2$. In w CDM this list is extended to include a free parameter w for the equation of state of dark energy. In both models, flatness is imposed by setting $\Omega_\Lambda = 1 - \Omega_m$. The prior ranges for these parameters are set such that they encompass five times the 68% C.L. from external experiments, in the case they are not strongly constrained by DES itself. In all, we consider six parameters in Λ CDM and seven in w CDM. Instead of quoting constraints on A_s , we will refer to the rms amplitude of mass fluctuations on $8 h^{-1}$ Mpc scale in linear theory, σ_8 , or the related parameter S_8 ,

$$S_8 \equiv \sigma_8 \left(\frac{\Omega_m}{0.3} \right)^{0.5}, \quad (17)$$

which typically is better constrained because it is less correlated with Ω_m .

Astrophysical parameters.—In addition we marginalize over a number of parameters related to the galaxy biasing model, the intrinsic alignment model, and the magnification model. For linear galaxy bias we include one free parameter per bin b^i , or two in the case of nonlinear bias $b_1^i - b_2^i$. Tidal galaxy biases are kept fixed to their local Lagrangian expressions in terms of the linear bias, as discussed in Sec. VA and Pandey *et al.* [79]. Our baseline model for intrinsic alignment of galaxies (TATT, [81]) is parametrized by an amplitude a_i and a power law index η_i for both the tidal alignment and the tidal torque terms, in addition to a global source galaxy bias parameter b_{TA} . Lastly we consider one parameter per lens tomographic bin to account for the amplitude of lens magnification. This parameter is however kept fixed in our baseline analysis, to the value calibrated on realistic simulations, as described in Elvin-Poole, MacCrann *et al.* [34].

Systematic parameters.—Photometric redshift systematics are parametrized by an additive shift to the mean redshift of each bin, given by Δz_l for lenses and Δz_s for sources, such that

$$n^i(z) = n_{pz}^i(z - \Delta z^i). \quad (18)$$

Cordero, Harrison *et al.* [102] demonstrated that our uncertainties in higher order modes of the source $n(z)$'s, besides the mean redshift, have negligible impact in cosmological constraints from cosmic shear. Hence the above treatment is sufficient. For the lenses, however, we have found that current uncertainties on the shape of the $n(z)$'s are important, in part because the clustering and

galaxy-galaxy lensing kernels are more localized. Thus, in the case of the lenses, we also parametrize the uncertainty on the width of the redshift distribution by a stretch σz , such that

$$n^i(z) = \frac{1}{\sigma z^i} n_{pz}^i \left(\frac{z - \langle z \rangle}{\sigma z^i} + \langle z \rangle \right). \quad (19)$$

The priors for the lens shift and stretch parameters were calibrated in Cawthon *et al.* [64] and are specified in Table II. In Sec. VIC we validate this parametrization for MAGLIM, showing that it allows us to recover unbiased cosmology and galaxy bias values. See [64] for the equivalent validation of REDMAGIC shift and stretch parameters and Table I in [33] for further details (note that in the case of REDMAGIC the stretch parameter is only required for the highest tomographic bin).

In addition, the measured ellipticity is a biased estimate of the underlying true shear. This bias is taken into account in our pipeline through a multiplicative bias m correction, as defined in Eq. (1). This correction is applied as an average over all the galaxies in each source tomographic bin. The priors on these parameters are derived in [54] using image simulations and are listed in Table II. MacCrann *et al.* [54] founds the additive bias c to be negligible compared to the multiplicative bias.

In total, our baseline likelihood analysis (i.e. linear galaxy bias) marginalizes over 37 parameters in Λ CDM (or 38 in w CDM). The extension to nonlinear galaxy bias adds one parameter per lens bin.

C. Blinding

We protect our results against observer bias by systematically shifting our results in a random way at various stages of the analysis by Muir *et al.* [103] to prevent us from knowing the true cosmological results or model fit until all decisions about the analysis have been made. This process and the decision tree to unblind is described in detail in [37]. We describe some changes that were made postunblinding in Sec. VII A.

D. Quantifying internal consistency

We defined a process before unblinding for testing internal consistency of the data based on the posterior predictive distribution (PPD). We can derive a probability to exceed p from this process, which either tells us p of a dataset given a chosen model (like Λ CDM) and covariance or the p of a dataset given constraints on the model from a different potentially correlated dataset. We have verified the consistency of the final 2×2 pt data vector to the Λ CDM and w CDM models and its consistency with our cosmic shear data in [35,36]. These PPD statistics are validated in Doux *et al.* [104].

TABLE II. The parameters and their priors used in the fiducial MAGLIM Λ CDM and w CDM analyses. The parameter w is fixed to -1 in Λ CDM. Square brackets denote a flat prior, while parentheses denote a Gaussian prior of the form $\mathcal{N}(\mu, \sigma)$.

Parameter	Fiducial	Prior
<i>Cosmology</i>		
Ω_m	0.3	[0.1, 0.9]
$A_s 10^9$	2.19	[0.5, 5.0]
n_s	0.97	[0.87, 1.07]
w	-1.0	$[-2, -0.33]$
Ω_b	0.048	[0.03, 0.07]
h_0	0.69	[0.55, 0.91]
$\Omega_c h^2 10^3$	0.83	[0.6, 6.44]
<i>Linear galaxy bias</i>		
b_i	1.5, 1.8, 1.8, 1.9, 2.3, 2.3	[0.8, 3.0]
<i>Nonlinear galaxy bias</i>		
$b_1^i \sigma_8$	1.43, 1.43, 1.43, 1.69, 1.69, 1.69	[0.67, 3.0]
$b_2^i \sigma_8^2$	0.16, 0.16, 0.16, 0.36, 0.36, 0.36	$[-4.2, 4.2]$
<i>Lens magnification</i>		
C_i	0.43, 0.30, 1.75, 1.94, 1.56, 2.96	Fixed
<i>Lens photo-z shift</i>		
Δz_1^1	-0.009	$(-0.009, 0.007)$
Δz_1^2	-0.035	$(-0.035, 0.011)$
Δz_1^3	-0.005	$(-0.005, 0.006)$
Δz_1^4	-0.007	$(-0.007, 0.006)$
Δz_1^5	0.002	$(0.002, 0.007)$
Δz_1^6	0.002	$(0.002, 0.008)$
σz_1^1	0.975	$(0.975, 0.062)$
σz_1^2	1.306	$(1.306, 0.093)$
σz_1^3	0.870	$(0.870, 0.054)$
σz_1^4	0.918	$(0.918, 0.051)$
σz_1^5	1.080	$(1.08, 0.067)$
σz_1^6	0.845	$(0.845, 0.073)$
<i>Intrinsic alignment</i>		
a_i ($i \in [1, 2]$)	$0.7, -1.36$	$[-5, 5]$
η_i ($i \in [1, 2]$)	$-1.7, -2.5$	$[-5, 5]$
b_{TA}	1.0	$[0, 2]$
z_0	0.62	Fixed
<i>Source photo-z</i>		
Δz_s^1	0.0	$(0.0, 0.018)$
Δz_s^2	0.0	$(0.0, 0.013)$
Δz_s^3	0.0	$(0.0, 0.006)$
Δz_s^4	0.0	$(0.0, 0.013)$
<i>Shear calibration</i>		
m^1	0.0	$(-0.006, 0.008)$
m^2	0.0	$(-0.010, 0.013)$
m^3	0.0	$(-0.026, 0.009)$
m^4	0.0	$(-0.032, 0.012)$

VI. MODEL VALIDATION

In this section, we validate our modeling pipeline using both simulated noiseless theory data vectors and measurements from the BUZZARD N -body simulations. We quantify

the impact of several systematic effects that are not included in our baseline model (Sec. VA) in Sec. VIA and validate the parametrization choice for systematics effects that are included in the baseline model in Sec. VIB. In Sec. VIC we validate our parametrization and priors for the uncertainties in the MAGLIM redshift distributions.

The validation procedure is the same for both Secs. VIA and VIB: we generate a synthetic data vector including a variation around the baseline model, which is then analyzed with the baseline model. We carry out simulated (cosmic shear, 2x2pt, 3x2pt, 3x2pt+*Planck*) analyses in Λ CDM and w CDM on contaminated data vectors and quantify the 2D parameter bias in (Ω_m, S_8) for Λ CDM and in (Ω_m, w) for w CDM. As described in Krause *et al.* [80], we require $\Delta\chi^2 < 1$ and the 2D parameter biases to be smaller than $0.3\sigma_{2D}$ for each variation study, in order to ensure that the total potential systematic bias is well below 1σ statistical uncertainty.

A. Scale cuts

The baseline model summarized in Sec. VA is incomplete in modeling astrophysical effects, with the leading unaccounted systematics being nonlinear galaxy bias and the impact of baryonic physics on the matter power spectrum. We thus design scale cuts that remove the data points most affected by nonlinear galaxy bias and baryonic feedback and control systematic biases in the inferred cosmological parameters to less than $0.3\sigma_{2D}$.

Of these two effects, baryonic feedback is the dominant for small-scale cosmic shear modeling (see e.g. [105,106]), while nonlinear bias is the dominant contamination for galaxy clustering and galaxy-galaxy lensing. Hence we review here only the procedure for mitigating the effect of nonlinear bias through scale cuts and refer to [35,36,80] for the discussion of scale cuts mitigating baryonic effects on cosmic shear. We note that the scale cut analysis also includes baryonic effects on the matter power spectrum in galaxy clustering and galaxy-galaxy lensing, however, these contaminants are far subdominant compared to nonlinear bias effects, and we refer to [80] for details.

We employ the perturbative galaxy bias model summarized in Sec. VA to compute synthetic data vectors that include contributions from nonlinear galaxy bias to galaxy clustering and galaxy-galaxy lensing. The fiducial parameter values for b_2^i used to compute the contaminated data vector are based on bias measurements for a MAGLIM—like sample selection in mock catalogs [79]. We then run simulated cosmology analyses for a set of scale cut proposals that vary the minimum comoving transverse scale $R_{\min}$ included in the analysis, corresponding to an angular scale cut $\theta_{\min}^i = R_{\min, w/\gamma_i} / \chi(z^i)$ for each lens tomography bin i . We find that

$$(R_{\min, w}, R_{\min, \gamma_i}) = (8 \text{ Mpc}/h, 6 \text{ Mpc}/h) \quad (20)$$

meets our requirements. As mentioned in Sec. VA, γ_t is a nonlocal quantity, and therefore, its value at any angular scale θ carries information from all the scales smaller than θ . For this reason, the scale cuts in the DES Y1 3×2 pt analysis were larger for $\gamma_t(\theta)$ (12 Mpc/h) than for $w(\theta)$ (8 Mpc/h). Here, we are able to include smaller scales in our analysis of galaxy-galaxy lensing (up to 6 Mpc/h) thanks to the point-mass analytic marginalization procedure [84] that we adopt to mitigate the impact of this nonlocality. See Sec. VA and Pandey *et al.* [79] for a more detailed description of this method.

The same nonlinear galaxy bias model is also used in the analysis pipeline, which allows us to include more nonlinear scales than the linear bias analyses. We base the scale cut validation for the nonlinear bias model on mock catalogs, as extending the scale cut procedure described above to validate the third-order bias model would require higher-order perturbative modeling. Pandey *et al.* [79] compared the nonlinear galaxy bias model predictions to 3D matter-galaxy and galaxy-galaxy correlation function measurements from mock catalogs and found few-percent level accuracy down to 4 Mpc/h.

For the REDMAGiC sample, the systematic bias on cosmological parameters is characterized in DeRose *et al.* [71] using a suite of 18 DES-Y3 mock realizations; their analysis found the linear bias model with (8 Mpc/h, 6 Mpc/h) scale cuts and nonlinear bias with (4 Mpc/h, 4 Mpc/h) to be sufficiently accurate for the accuracy of DES-Y3 analyses. See also Pandey *et al.* [33] for further details on the nonlinear bias validation.

As there is only one DES-Y3 mock realization available for the MAGLIM sample (described in Sec. IV), we compare parameter inferences from REDMAGiC and MAGLIM analyses based on the same realization, which are shown in Fig. 5. We note that the assumed scale cuts in terms of Mpc/h are the same for both samples. We find parameter shifts between REDMAGiC and MAGLIM baseline analyses of the same realization at the level of $0.16\sigma_{2D}$ (linear bias) and $0.05\sigma_{2D}$ (nonlinear bias) and between baseline (linear bias) and nonlinear bias analyses of the MAGLIM realization at the level of $0.45\sigma_{2D}$. The latter is similar to the REDMAGiC parameter shift between linear and nonlinear bias analyses in Fig. 5, which is at the level of $0.5\sigma_{2D}$. These shifts are larger than our threshold of $0.3\sigma_{2D}$, however, this is due to the statistical noise in the BUZZARD data vector since it is measured from just one realization. When using the mean of the 18 mock realizations [71], this statistical noise is reduced, and we find a shift of $0.01\sigma_{2D}$ between REDMAGiC linear and nonlinear bias analyses. We hence conclude that the linear and nonlinear bias scale cuts are sufficient for the analyses presented in this paper.

Our modeling assumption of constant galaxy bias parameters in each redshift bin is validated as well through the analysis of the MAGLIM BUZZARD mock catalog, which

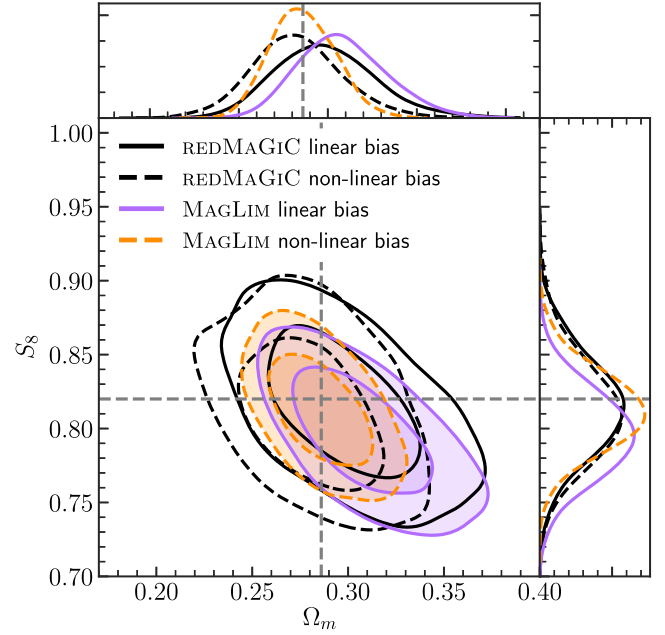


FIG. 5. Marginalized 2×2 pt constraints on S_8 and Ω_m in Λ CDM using measurements on one BUZZARD realization (see Sec. IV). The dashed gray lines indicate the true values assumed in the simulation. These results validate the assumed scale cuts for linear and nonlinear galaxy bias modeling, as described in Sec. VIA.

contains nonparametric redshift evolution and nonlinear evolution of the matter field. If this assumption were insufficient, then we would obtain cosmological constraints biased from the true values in Fig. 5. Therefore, the results from Fig. 5, which show that we recover the true cosmology, validate that systematic biases due to galaxy bias redshift evolution are insignificant for the DES-Y3 analysis.

B. Model stress tests

The baseline analysis model requires several parametrization choices to evaluate angular correlation functions. These parametrization choices are practical but imperfect approximations, and we need to demonstrate their robustness for the DES-Y3 analyses. In practice, we stress test these baseline parametrization choices by generating simulated theory data vectors using alternate parametrizations, which are then analyzed with the baseline model. A comprehensive overview of model choices and their validation is given in [80], we highlight here the systematics most relevant to the analysis presented in this paper.

1. Matter power spectrum

The baseline model adopts the Takahashi *et al.* [107] recalibration of the HALOFIT fitting formula [108] for the gravity-only matter power spectrum, including the Bird *et al.* [109] prescription for the impact of massive neutrinos.

TABLE III. Parameter biases from model stress tests, cf. Sec. VI B for details. The second and third columns report two-dimensional parameter biases relative to the 2D-marginalized parameter uncertainty of the baseline analysis in Λ CDM and w CDM, respectively. The results for 3×2 pt are also shown for completeness.

Model stress test	$\Delta_{2D} (\Omega_m, S_8)$	$\Delta_{2D} (\Omega_m, w)$
Matter power spectrum, 2×2 pt	$<0.01\sigma_{2D}$	$<0.01\sigma_{2D}$
Matter power spectrum, 3×2 pt	$0.05\sigma_{2D}$	$0.01\sigma_{2D}$
Higher-order lensing, 2×2 pt	$0.12\sigma_{2D}$	$<0.01\sigma_{2D}$
Higher-order lensing, 3×2 pt	$0.26\sigma_{2D}$	$<0.01\sigma_{2D}$

In order to quantify the model accuracy we compare HALOFIT against more recent matter power spectrum emulators, which are based on larger simulations and thus more accurate. Specifically, we compare to the EUCLID EMULATOR [110]. The results of this test are summarized in Table III, and we find the systematic parameter biases due to nonlinear power spectrum modeling to be insignificant for the DES-Y3 analysis. The results for 3×2 pt are also shown for completeness.

2. Magnification

The magnification coefficients C^i in Eq. (5) are fixed in this analysis to values derived in [34]. MacCrann *et al.* [34] demonstrates that DES-Y3 cosmology constraints are robust to biases in the estimated values for the magnification coefficients, including the extreme scenario of ignoring lens magnification in the analysis. We leave tests of the redshift evolution of these coefficients to future analyses.

3. Higher-order lensing effects

While the baseline analysis model includes weak lensing to first order in the distortion tensor, *reduced shear* [111,112] and *source magnification* [113,114] contribute to the angular correlation functions at next-to-leading order. We compute these corrections in [80]. As described above, we generate a theory data vector with these corrections and analyze it with the baseline analysis model to test the

robustness of the constraints. The results of this test for MAGLIM, summarized in Table III, show that the systematic parameter biases due to higher-order weak lensing effects are insignificant for the DES-Y3 analysis.

C. Photometric redshift parametrization

As described in Sec. V B 1, we parametrize the uncertainty in the mean and width of the redshift distributions by introducing an additive *shift* and a *stretch* parameter for each tomographic bin. In this section, we describe the calibration and validation of these parameters.

We calibrate the DNF photometric redshift distributions via a two-parameter χ^2 least squares fit to the clustering redshift estimate of $n(z)$ from Cawthon *et al.* [64] (see also Fig. 2), which we denote as $n_{wz}(z)$. The functional form of this fit is given by the combination of Eqs. (18) and (19):

$$n_{wz}^i(z) = \frac{1}{\sigma_{z^i}} n_{pz}^i \left(\frac{z - \langle z \rangle - \Delta z^i}{\sigma_{z^i}} + \langle z \rangle \right), \quad (21)$$

where $\langle z \rangle$ is the mean redshift of the initial DNF photometric redshift distribution, $n_{pz}(z)$.

Additionally, we consider an approach with only shift parameters (i.e. neglecting the uncertainty on the widths of the distributions). Similarly, we calibrate the shift parameters by doing an χ^2 fit to the clustering-redshifts estimate $n_{wz}(z)$ with Eq. (18). The details of this procedure are described in [64].

The χ^2 fits provide an estimate on the priors of these parameters. We then validate these priors by ensuring that they allow us to recover unbiased cosmological constraints and galaxy bias values. For this purpose, we use a simulated theory data vector generated with the clustering redshifts distributions $n_{wz}(z)$. Since the tails of $n_{wz}(z)$ are noisy and can have negative values, we cut the tails following [64]. Additionally, as noise in the clustering-redshift point estimates could induce biases in the cosmology, we use a smoothed version of $n_{wz}(z)$ that is the result of fitting a combination of Gaussians to the individual points.

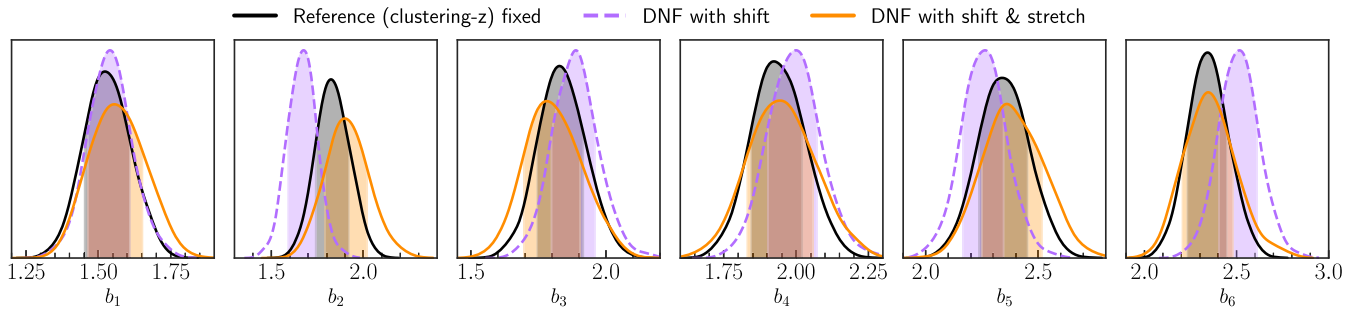


FIG. 6. Marginalized 1D constraints on the galaxy bias parameters in Λ CDM from 2×2 pt simulated theory data vectors using different $n(z)$ estimates. We use clustering redshifts as reference (solid black) and compare the contours with DNF marginalizing over Δz shifts (purple dashed) and both shift and stretch parameters (orange filled).

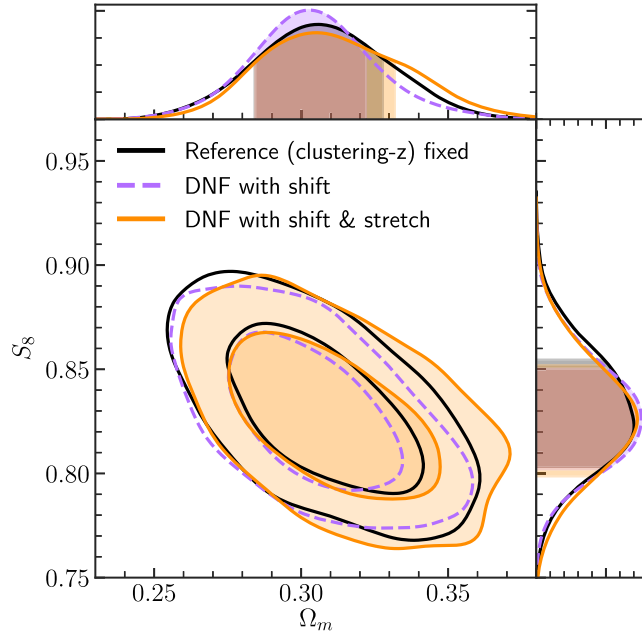


FIG. 7. Marginalized 2×2 pt constraints on S_8 and Ω_m in Λ CDM from simulated theory data vectors using different $n(z)$ estimates. We use clustering redshifts as reference (solid black) and compare the contours with DNF marginalizing over Δz shifts (purple dashed) and both shift and stretch parameters (orange filled).

We use as reference a simulated analysis with $n_{wz}(z)$ and no marginalization of photometric redshift parameters, and then we analyze the simulated theory data vector generated with $n_{wz}(z)$ using the DNF $n(z)$ marginalizing over shifts or both shift and stretch parameters. The results are shown in Figs. 6 and 7. We find that, while marginalizing over the shifts allows us to recover the reference cosmology, it underestimates the contours and fails to recover the galaxy bias parameters in all the bins. When considering the uncertainty on the width through the stretch parameters, we recover both the reference cosmology and galaxy bias values. Hence we conclude that varying both shift and stretch parameters is needed for the MAGLIM sample, and that the priors estimated in [64] and listed in Table II are sufficient.

VII. RESULTS

A. Unblinding

After passing all the tests outlined in [37] and summarized in Sec. VD, we unblinded the MAGLIM results. We then updated the covariance matrix so that its elements were computed at the best-fit parameter values found in the 3×2 pt unblinded run. The clustering parameters (galaxy bias b multiplied by σ_8) were found to be smaller in the unblinded result compared to the original parameters assumed in the covariance computation, and therefore, the updated covariance matrix assumed less clustering.

Since the error bars on $w(\theta)$ on large scales are dominated by cosmic variance, they were considerably smaller ($\sim 50\%$) in the new covariance matrix. We then reran all the chains and discovered that the fit to all cosmological models considered in this work was poor. With the old covariance matrix, our analysis passed our requirement on goodness-of-fit for unblinding ($p > 0.01$). However, the best-fit Λ CDM model with the new covariance matrix had a PPD goodness-of-fit $p < 10^{-3}$.

The problem was localized to be related to the two highest redshift lens bins. We include a comprehensive discussion of our tests after unblinding in the Appendix B and summarize here our conclusions. We found that the model struggled to provide a consistent fit to both galaxy clustering and galaxy-galaxy lensing amplitudes on the last two tomographic bins. One way to demonstrate this is to allow the galaxy bias in clustering to differ from the bias in galaxy-galaxy lensing with the ratio in the i th lens bin given by a parameter X_i . On large scales where the linear bias assumption is valid, X_i are expected to be equal to unity at the percent level (see e.g. [115]). This is true for the lowest four bins, but in the last two bins we obtain $X_5 = 0.77 \pm 0.10$ and $X_6 = 0.54 \pm 0.07$ when combining the 2×2 pt data vector with cosmic shear (see equivalent results at fixed cosmology in Pandey *et al.* [33]). These values of X in the highest redshift bins, the bins in which the redshifts of galaxies are most difficult to determine, pointed to problems with these two bins. If we had been running with a more appropriate covariance matrix pre-unblinding, we would very likely have made the decision to drop the last two bins. Therefore, in what follows, we present results using only the four lowest redshift bins. This results in an appropriate model fit to both Λ CDM and w CDM, with $p = 0.02$. We have not identified yet a specific systematic origin for these issues, but a calibration problem for high photometric redshifts (where the available spectroscopic references are extremely sparse) is highly plausible.

We present more details in the Appendix B; see Fig. 14. Without the highest two redshift bins, the cosmological constraints get weaker as expected, but using the full set of six bins is not justified given the bad fit and the internal inconsistency between clustering and galaxy-galaxy lensing, that clearly points to a systematic effect. There is also a shift in the best-fit value of the parameters, but this is at the $1/2$ -sigma level for both S_8 and Ω_m , and clearly within the statistical uncertainty when using the first four redshift bins. Furthermore, the parameter shift due to dropping the highest two redshift bins is significantly reduced when combined with cosmic shear data [37].

B. Λ CDM

Our main results using galaxy clustering and galaxy-galaxy lensing for Λ CDM are shown in Fig. 8 and Table IV

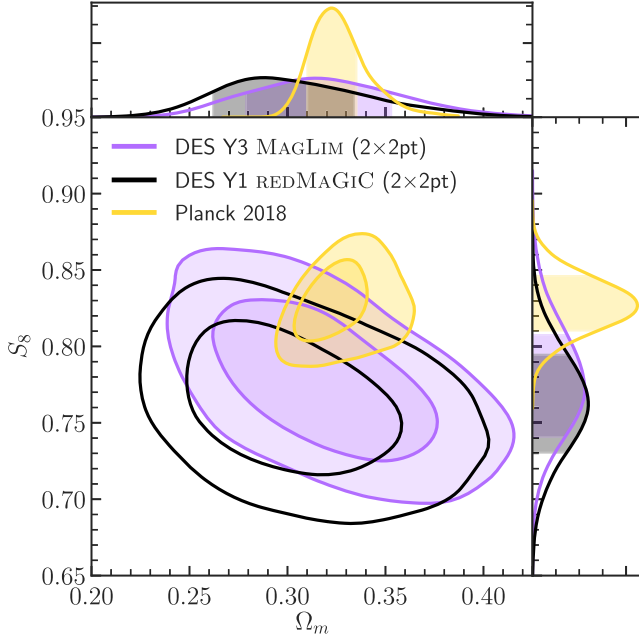


FIG. 8. Constraints on S_8 and Ω_m in Λ CDM from galaxy-galaxy lensing and galaxy clustering using the MAGLIM sample. Also shown are the DES Y1 results and constraints from the *Planck* CMB primary anisotropies.

and compared with DES Y1 [12] and measurements of the CMB temperature and polarization anisotropies power spectra by the *Planck* satellite [4]. The DES Collaboration [37] combines these two probes with cosmic shear to obtain our fiducial Y3 results. The constraints from Y3 are not significantly tighter than those from Y1, in spite of the factor of 3 gain in sky coverage. Much of this is due to several improvements in our modeling that were needed for the Y3 analysis due to the increased precision in our measurements, as described in Krause *et al.* [80].

The marginalized 68% C.L. mean values (best-fit values inside parentheses) of S_8 , Ω_m , and σ_8 are found to be

$$S_8 = 0.778^{+0.037}_{-0.031} \quad (0.809), \quad (22)$$

$$\Omega_m = 0.320^{+0.041}_{-0.034} \quad (0.306), \quad (23)$$

$$\sigma_8 = 0.758^{+0.074}_{-0.063} \quad (0.801). \quad (24)$$

In the Appendix C, we compare the theory prediction corresponding to these best-fit values with the measurements of galaxy clustering and galaxy-galaxy lensing for MAGLIM.

As mentioned before, in Fig. 8 we compare the 2D marginalized constraints on Ω_m and S_8 to the *Planck* CMB final release [4]. We include the primary temperature TT data on scales $30 \leq \ell \leq 2508$, the E-mode and its cross power spectra with temperature ($EE + TE$) in the range

$30 \leq \ell \leq 1996$, and the low- ℓ temperature and polarization likelihood ($TT + EE$) at $2 \leq \ell \leq 29$. As done in the DES Y1 analysis [12], we recompute the CMB likelihood in our fiducial parameter space from Table II.

In order to quantify the level of agreement with *Planck*, we calculate the Monte Carlo estimate of the probability of a parameter difference, presented in [116]. For this purpose, we compute the distribution of parameter shifts (in particular, we consider $\Delta\sigma_8$ and $\Delta\Omega_m$) and estimate its compatibility with zero. We use the publicly available *tensiometer*¹⁴ code to compute the parameter shift between *Planck* and our main DES-Y3 2×2 pt result in Λ CDM, finding

$$\text{Parameter shift: } 1.0\sigma \text{ (MAGLIM } 2 \times 2\text{pt vs } \textit{Planck}), \quad (25)$$

which confirms more rigorously the qualitative agreement that we see in Fig. 8.

Even though the 2×2 pt constraints from DES Y1 are not independent, we can compute a rough estimate of the parameter shift with respect to the 2×2 pt DES-Y3 results by assuming no correlation between the two. We obtain a shift of 0.22σ , confirming the good agreement that we see in Fig. 8.

Figure 5 and related discussions in Sec. VIA show that including more information from small scales with a model that goes beyond linear bias recovers more cosmological information. We apply this nonlinear bias model to the fiducial dataset that cuts scales below $(8, 6) h^{-1}$ Mpc for $(w(\theta), \gamma_l)$. The extended model applied to the same data as the linear bias model does not lose much constraining power as indicated by the purple contours in Fig. 9 and the parameter values in Table IV. The contours in the $\Omega_m - S_8$ plane are shifted by 0.4σ with respect to the linear bias analysis, therefore, both galaxy bias models yield consistent results.

When opened up to include more small scale data (orange contours), up to $(4, 4) h^{-1}$ Mpc, the analysis does provide tighter constraints. In particular, we obtain an improvement of 31% in the $\Omega_m - S_8$ plane. This is an indication that future analyses and surveys stand to benefit greatly from sophisticated modeling of small scales. The contours are shifted by 0.46σ with respect to the $(8, 6) h^{-1}$ Mpc scale cuts using the same nonlinear galaxy bias model, hence including smaller scales gives consistent results.

We have also tested the impact in the constraining power when including galaxy clustering cross-correlations in the analysis, finding a gain of 15% in the $\Omega_m - S_8$ plane. The clustering cross-correlations are much more sensitive to lens magnification than the autocorrelations, hence MacCrann *et al.* [34] further study the impact of

¹⁴<https://github.com/mraveri/tensiometer>.

TABLE IV. 68% C.L. marginalized cosmological constraints in Λ CDM and w CDM using the combination of DES-Y3 galaxy clustering and galaxy-galaxy lensing measurements (2×2 pt).

Cosmological model	Galaxy bias model (scale cut)	Ω_m	S_8	σ_8	w
Λ CDM	Linear bias (8, 6) h^{-1} Mpc	$0.320^{+0.041}_{-0.034}$	$0.778^{+0.037}_{-0.031}$	$0.758^{+0.074}_{-0.063}$	...
Λ CDM	Nonlinear bias (8, 6) h^{-1} Mpc	$0.293^{+0.037}_{-0.027}$	$0.800^{+0.037}_{-0.036}$	$0.813^{+0.074}_{-0.070}$	...
Λ CDM	Nonlinear bias (4, 4) h^{-1} Mpc	$0.284^{+0.034}_{-0.021}$	$0.836^{+0.033}_{-0.033}$	$0.863^{+0.071}_{-0.065}$	...
w CDM	Linear bias (8, 6) h^{-1} Mpc	$0.32^{+0.044}_{-0.046}$	$0.777^{+0.049}_{-0.051}$	$0.758^{+0.079}_{-0.061}$	$-1.031^{+0.218}_{-0.379}$
w CDM	Nonlinear bias (8, 6) h^{-1} Mpc	$0.301^{+0.043}_{-0.040}$	$0.798^{+0.053}_{-0.058}$	$0.802^{+0.076}_{-0.067}$	$-0.993^{+0.197}_{-0.373}$
w CDM	Nonlinear bias (4, 4) h^{-1} Mpc	$0.289^{+0.038}_{-0.033}$	$0.849^{+0.036}_{-0.052}$	$0.870^{+0.068}_{-0.067}$	$-0.937^{+0.139}_{-0.299}$

magnification on the 2×2 pt cosmological constraints when including galaxy clustering cross-correlations.

C. w CDM

While Λ CDM fits this 4-bin 2×2 pt dataset (and virtually all other datasets) well, in this section we consider its simplest possible extension, which is to allow its equation of state, $w \equiv P/\rho$, to differ from -1 , that of the cosmological constant. This extension is dubbed w CDM.

Figure 10 shows the constraints on S_8 , Ω_m , and w in this model. The Y3 constraints are slightly tighter than those

obtained from Y1, but by itself the 2×2 pt data are not very informative about the value of w . Recall that the prior imposed is $-2 < w < -0.33$, so the information gained over the prior is modest.

The results of the more aggressive analysis using smaller scales and the nonlinear bias model are shown

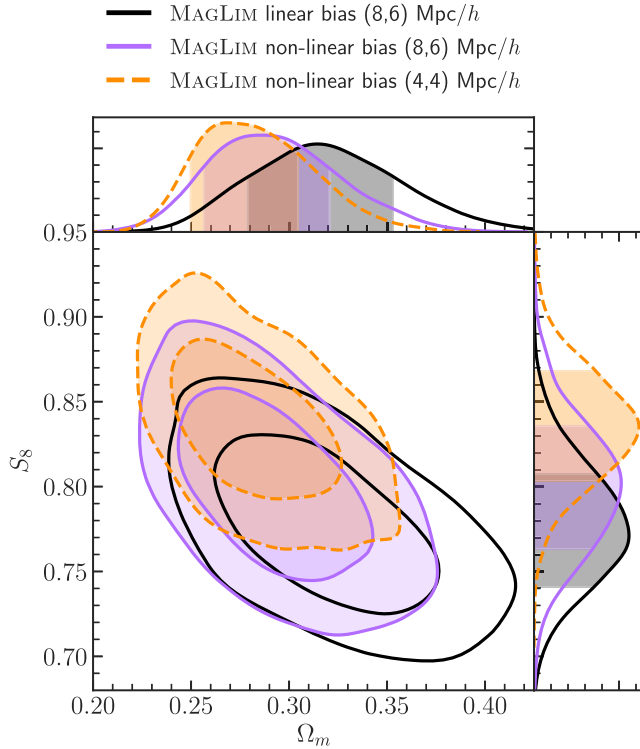


FIG. 9. Same as Fig. 8, but the two new sets of contours use the nonlinear bias model to analyze the data. This analysis agrees with the linear bias model when the same data vector is used (8,6) but provides tighter constraints when smaller scales are included.

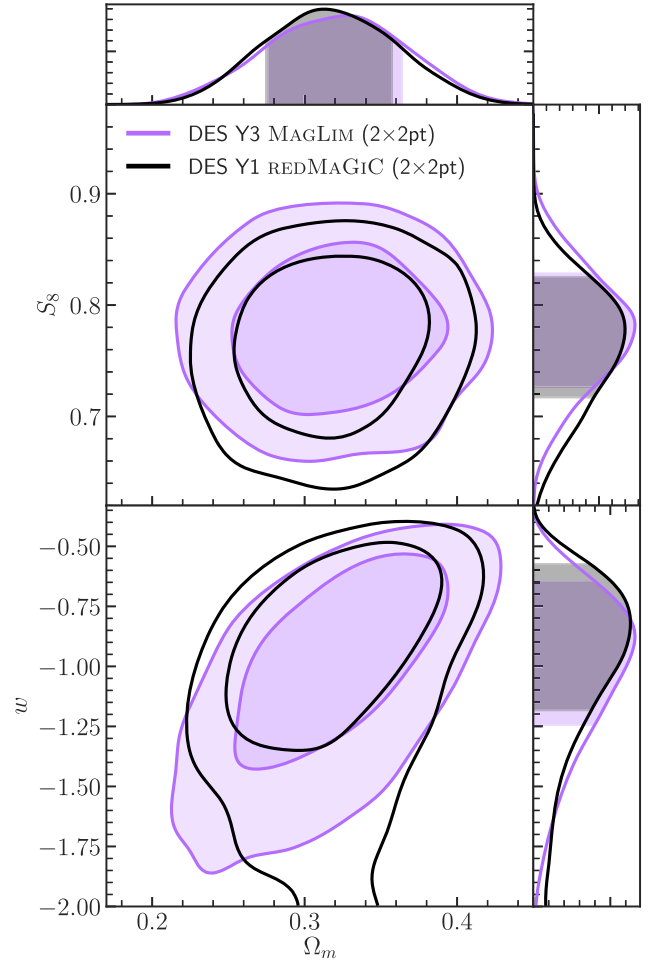


FIG. 10. Constraints from the 2×2 pt data vector in w CDM. The range of w on the vertical axis coincides with the prior on w , so not much information is added about w from the 2×2 pt data.

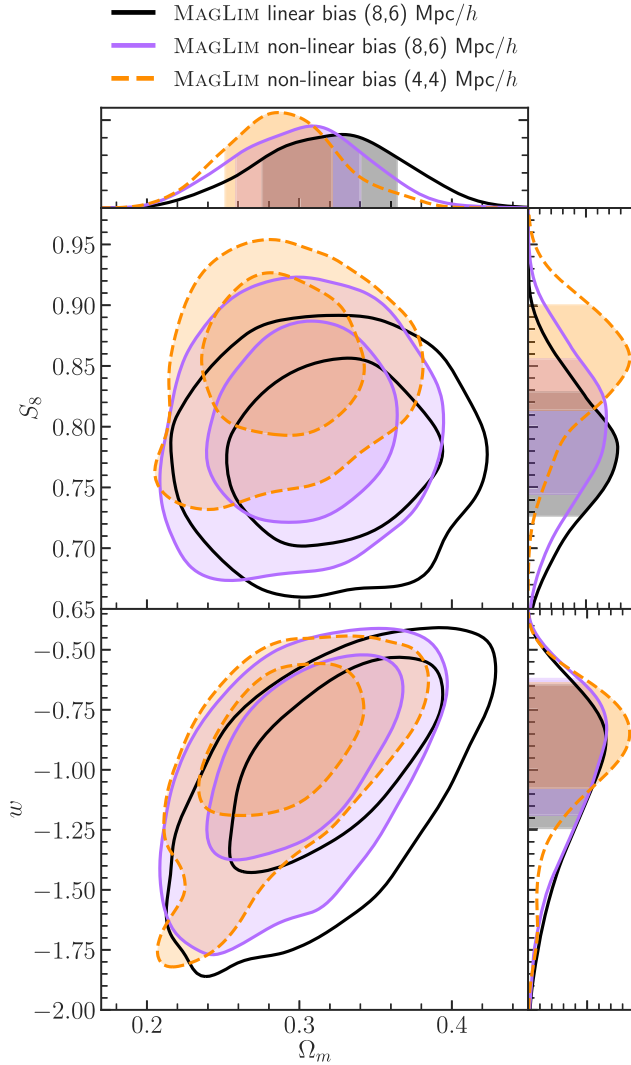


FIG. 11. Same as Fig. 10 but using smaller scales and the nonlinear bias model.

in Fig. 11. They are a bit tighter than the more conservative analysis (see Table IV for a quantitative comparison). In particular, we find improvements of 33% in the $\Omega_m - S_8$ plane and about 41% for $w - \Omega_m$. Despite the improvement on w , the lower panel in Fig. 11 shows that the 2-sigma tails extend close to the prior boundary. Therefore, 2×2 pt by itself is not very constraining on the dark energy equation of state.

D. Robustness tests

We assess the internal consistency of the data used in this analysis and robustness of the baseline model in Λ CDM in Fig. 12. The first row, as well as the shaded vertical bars, show the 1σ uncertainty on S_8 (left column) and Ω_m (right column) of the baseline Λ CDM analysis presented in Sec. VII B. For reference, we also show the corresponding CMB constraints from *Planck*, as described in Sec. VII B.

The next six rows, labeled *internal consistency*, show the parameter constraints from different splits of the data vector: The *small scales* and *large scales* analyses restrict the analysis to angular scales corresponding to physical separations below/above 30 Mpc/h; we note that the large-scale analysis does not marginalize over a point-mass contribution of γ_i , as this term scales as θ^{-2} and thus insignificant for the large scales analysis. The next four rows show the parameter constraints when excluding one MAGLIM tomographic bin at a time. The largest parameter shift is caused by removing MAGLIM bin 3, but all data splits are consistent with the baseline result, pointing to the internal consistency of the data vector in Λ CDM.

The bottom six rows, labeled *model robustness*, show the parameter constraints for different analysis model variations:

- (i) NLA: This analysis variation uses the nonlinear alignment model for intrinsic alignments, which is a subspace of the baseline TATT model with $a_2 = \eta_2 = b_{TA} = 0$.
- (ii) No SR: This analysis variation does not include the SR likelihood, which in the baseline analysis primarily adds constraining power on photometric redshift and intrinsic alignment parameters.
- (iii) w CDM: This analysis variation shows the robustness of S_8 and Ω_m constraints to the dark energy parametrization.
- (iv) Fixed neutrino mass: This analysis variation fixes the neutrino mass to the minimum mass. As the neutrino mass is unconstrained (within prior range) by the baseline analysis, this variation primarily corresponds to a reduction in prior volume effects.
- (v) Nonlinear bias: This analysis variation employs the nonlinear bias model using the same scale cuts as the linear bias analysis.
- (vi) Source $n(z)$ HYPERRANK: Here we account for the full-shape uncertainty in the source redshift distributions instead of marginalizing over an additive shift to the mean redshift. The method consists of sampling a large set of $n(z)$ realizations in the likelihood analysis with HYPERRANK [102].

The parameter constraints are consistent for all of these model variations, demonstrating the robustness of the baseline analysis choices.

Aside from the tests presented above, Rodríguez-Monroy *et al.* [32] show that the constraints are robust to the method used to estimate the weights that correct our data vector from observational systematics. Furthermore, not correcting for the existing correlations with the survey property maps biases our results from galaxy clustering, which demonstrates the importance of estimating the weights accurately. See [32] for more details.

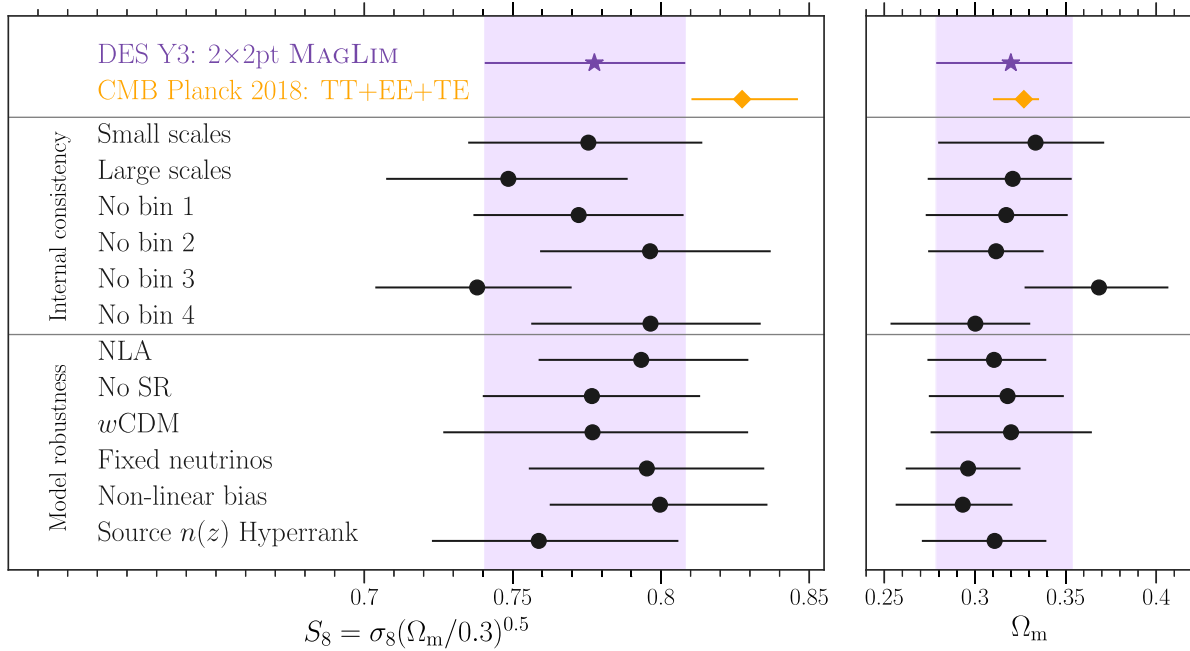


FIG. 12. Comparison of the MAGLIM 2×2 pt 68% C.L. marginalized cosmological constraints in Λ CDM when changing the analysis choices.

VIII. CONCLUSIONS

We have presented the DES-Y3 cosmological constraints obtained from the combination of galaxy clustering and galaxy-galaxy lensing (2×2 pt) using the MAGLIM lens sample. The definition of this sample was previously optimized in [31] in terms of its forecasted w CDM cosmological constraints, with the goal of exploring the trade-off between number density and photometric redshift accuracy. It has 10.7 million galaxies comprising a redshift range between $z_{\min} = 0.2$ and $z_{\max} = 1.05$, which we split into six tomographic bins (see Table I). We use as sources the METACALIBRATION catalog [53], which consists of more than 100 million shapes divided in four tomographic bins (see Fig. 1).

After validation of our modeling pipeline using both simulated theory data vectors and measurements from N -body simulations, we obtain our fiducial cosmological constraints using the first four tomographic bins of MAGLIM (see Sec. VII for further details). In Λ CDM, we measure at 68% C.L. the clustering amplitude $S_8 = 0.778^{+0.037}_{-0.031}$ and the matter energy density $\Omega_m = 0.320^{+0.041}_{-0.034}$. In w CDM, we obtain $S_8 = 0.777^{+0.049}_{-0.051}$, $\Omega_m = 0.320^{+0.044}_{-0.046}$, and also constrain the dark energy equation of state $w = -1.031^{+0.218}_{-0.379}$.

We also extend our analysis to smaller scales by using a nonlinear galaxy bias model, finding improvements of 31% in the $\Omega_m - S_8$ plane in Λ CDM and of 41% for $w - \Omega_m$ in w CDM.

In Figs. 8 and 10 we compare our fiducial results with DES Y1 2×2 pt, finding a very good agreement. In addition, we estimate the consistency of our Λ CDM cosmological constraints with the results from the CMB from the *Planck* satellite [4], TT + TE + EE]. We find that our constraints in the $\Omega_m - S_8$ plane are low with respect to *Planck* at the 1σ level. This result is in line with the slightly low S_8 values with respect to CMB that have been measured in other weak lensing surveys, such as KiDS [13,14] and HSC [15,16].

In Sec. VII D we evaluate the internal consistency of the MAGLIM 2×2 pt results. We find that our 68% C.L. constraints on S_8 and Ω_m are consistent across angular scales, tomographic bins, and modeling analysis choices. The results presented here are complemented by the equivalent 2×2 pt analysis using the REDMAGIC sample [33], a study of the impact of magnification on the 2×2 pt cosmological constraints [34], and the cosmic shear analysis in [35,36]. The MAGLIM 2×2 pt measurements are combined with cosmic shear in [37] to obtain the DES-Y3 fiducial cosmological results.

The advances in methodology implemented in DES Y3 set the stage for the analysis of the full DES dataset, comprising six years of observations. Regarding the lens samples, the improvements include the optimization of the sample in terms of its cosmological constraints [31], a full characterization of the uncertainties in the redshift distributions using self-organizing maps [67], and the inclusion

of several upgrades to our modeling [80], such as lens magnification [34], point-mass marginalization [33], and nonlinear galaxy bias [33]. These advances will be critical for the future “Stage-IV” photometric surveys such as Euclid [18], the *Nancy Grace Roman* Space Telescope [19], and the LSST [17].

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APPENDIX A: COMPARISON OF DNF PHOTOMETRIC REDSHIFTS WITH MATCHED SPECTROSCOPIC DATA

As explained in Sec. III A, we use DNF to select the MAGLIM galaxies and assign them to tomographic bins. DNF computes a point estimate of the true redshift by performing a fit to a hyperplane using 80 nearest neighbors in color and magnitude space taken from a reference set that has an associated true redshift from a large spectroscopic database. In Fig. 13, we compare the DNF photometric point estimates (Z_{MEAN}) to the spectroscopic redshifts from VIPERS. We use VIPERS for this validation because it was not included in the

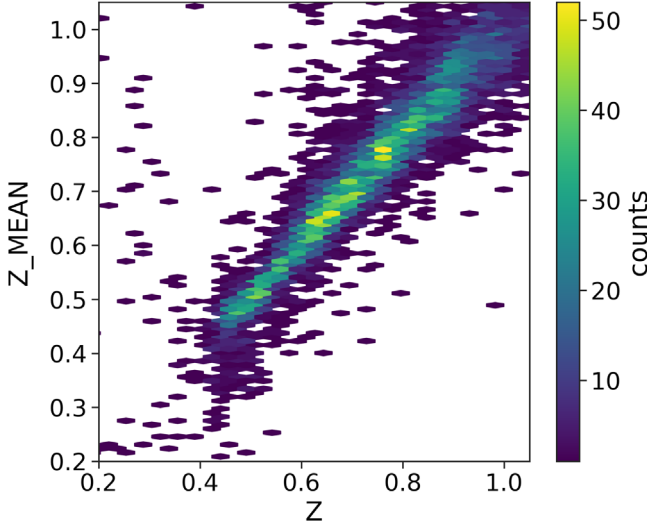


FIG. 13. MAGLIM DNF photometric redshift estimates (Z_{MEAN}) compared to the spectroscopic redshifts from VIPERS (Z).

training set for the DNF estimation of the point estimates. However, VIPERS is only complete at $z > 0.5$. Therefore, the comparison is limited by the low number of matched galaxies at lower redshifts. Using VIPERS as reference, we estimate the following two and three σ outlier rates:

$$\begin{aligned} 2\sigma \text{ outlier rate} &= 0.128, \\ 3\sigma \text{ outlier rate} &= 0.073, \end{aligned} \quad (\text{A1})$$

where the outliers in the 2σ region, for instance, are selected with

$$|Z_{\text{MEAN}} - Z| > 2\sigma_{68}(Z_{\text{MEAN}} - Z), \quad (\text{A2})$$

and $\sigma_{68}(Z_{\text{MEAN}} - Z)$ is the 68% confidence interval of values in the distribution of $(Z_{\text{MEAN}} - Z)$.

Since the MAGLIM selection includes a fraction of blue galaxies, we make a color split in order to compare the photometric quality of the blue galaxies compared to the

full MAGLIM sample. For simplicity, we select the blue galaxies from the MAGLIM sample by applying the inverse of the color cut used for the DES Baryon Acoustic Oscillations sample, which is optimized to select the reddest galaxies [118]. Therefore, we apply this color cut to the MAGLIM sample that depends on the i , z , and r band magnitudes: $(i - z) + 2.0(r - i) < 1.7$. The resulting sample has 4,953,191 galaxies, about 46% of the total MAGLIM sample. The outlier rates are very similar to the full sample. In order to estimate the redshift uncertainty, $\sigma_z/(1+z)$, we use the 68% confidence interval of values in the distribution of $(Z_{\text{MEAN}} - Z)/(1+Z)$ around its median value. For the full MAGLIM sample, we find $\sigma_z/(1+z) = 0.027$, while for the fraction of blue galaxies, we find $\sigma_z/(1+z) = 0.037$.

In order to validate the performance of DNF for the MAGLIM blue galaxies at lower redshifts ($z < 0.5$), we use the spectroscopic data set from [119]. This reference catalog contains about 2.2×10^5 spectra matched to DES objects from 24 different spectroscopic catalogs, including SDSS DR14 [60], DES's own follow-up through the OzDES program [61], and the Galaxy and Mass Assembly survey [120]. Using this data set, we find similar values for the outlier rates and $\sigma_z/(1+z)$ compared to using VIPERS as a reference. However, we note that the outlier rate and the redshift uncertainty $\sigma_z/(1+z)$ are higher in the photometric redshift range [0.5, 0.6]. The 3σ outlier rate reaches significantly higher values in that interval, $3\sigma \sim 0.12$, whereas $\sigma_z/(1+z) \sim 0.03$. This increase in the outliers is caused by degeneracies among galaxy types at $z \sim 0.4$, which are difficult to break due to the lack of u band information in the DES. As explained in [41], this spectroscopic catalog has been used as training data for DNF, and thus it is not an independent data set like VIPERS.

APPENDIX B: RESULTS AFTER UNBLINDING

As discussed in Sec. VII MAGLIM passed all the unblinding requirements and produced, at first, good model fits to both Λ CDM and w CDM. The results from these fits

TABLE V. 68% C.L. marginalized cosmological constraints in Λ CDM and w CDM using different iterations of the covariance matrix and number of tomographic bins.

Cosmological model	Iteration	Ω_m	S_8	σ_8	w
Λ CDM	6 bins, previous covariance (unblinding)	$0.322^{+0.040}_{-0.034}$	$0.729^{+0.030}_{-0.030}$	$0.707^{+0.063}_{-0.053}$	...
Λ CDM	6 bins, fiducial covariance	$0.297^{+0.033}_{-0.022}$	$0.744^{+0.034}_{-0.029}$	$0.751^{+0.061}_{-0.056}$	...
Λ CDM	4 bins, fiducial covariance	$0.320^{+0.041}_{-0.034}$	$0.778^{+0.037}_{-0.031}$	$0.758^{+0.074}_{-0.063}$	...
w CDM	6 bins, previous covariance (unblinding)	$0.349^{+0.044}_{-0.043}$	$0.755^{+0.035}_{-0.049}$	$0.703^{+0.064}_{-0.053}$	$-0.789^{+0.128}_{-0.306}$
w CDM	6 bins, fiducial covariance	$0.353^{+0.037}_{-0.038}$	$0.794^{+0.030}_{-0.037}$	$0.735^{+0.059}_{-0.049}$	$-0.58^{+0.081}_{-0.193}$
w CDM	4 bins, fiducial covariance	$0.320^{+0.044}_{-0.046}$	$0.777^{+0.049}_{-0.051}$	$0.758^{+0.079}_{-0.061}$	$-1.031^{+0.218}_{-0.379}$

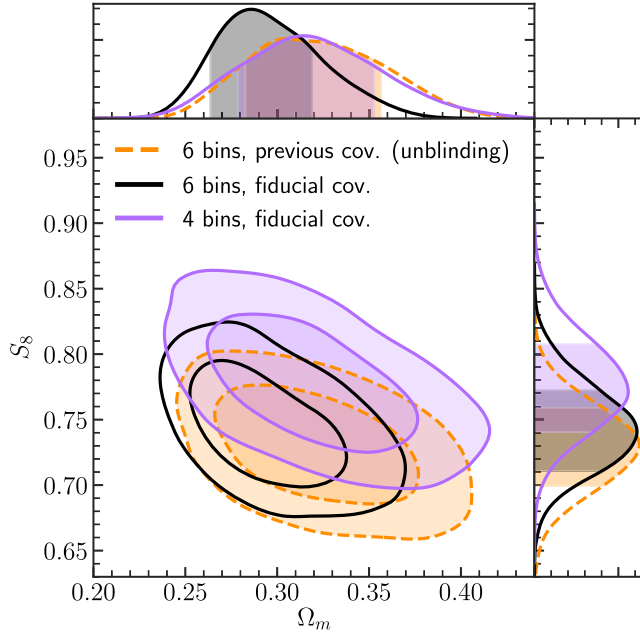


FIG. 14. Comparison of 2×2 pt Λ CDM constraints for MAGLIM using different iterations of the covariance matrix and number of tomographic bins included. The dashed orange lines correspond to the unblinding results, in which we used the whole set of bins and a covariance that assumed some fiducial cosmology and galaxy bias. Solid black corresponds to the results after updating the covariance with the 3×2 pt Λ CDM best-fit cosmology. Last, the purple filled contours show the fiducial 2×2 pt constraints, with just the first four tomographic bins included in the analysis.

however indicated a considerably lower linear galaxy bias, in particular, for the last tomographic bins. Updating the covariance with these values resulted in much tighter errors, which in turn implied that the cosmological chains with the updated covariance violated the χ^2 thresholds in Λ CDM and w CDM.

Different tests showed that the model had particular trouble in providing a consistent fit to both clustering and galaxy-galaxy lensing amplitudes on the last two tomographic bins (i.e. from 0.85 to 1.05). This can be visualized by comparing the σ_8 and galaxy bias values obtained from the combination of cosmic shear and galaxy-galaxy lensing ($\xi_{\pm} + \gamma_t$), cosmic shear and galaxy clustering ($\xi_{\pm} + w(\theta)$), or the whole three two-point functions (3×2 pt, $\xi_{\pm} + \gamma_t + w(\theta)$) from [37],

- (i) $\xi_{\pm} + \gamma_t$:
 $\sigma_8 = 0.61, b^i = \{1.81, 2.0, 2.48, 2.07, 1.49, 1.05\}$,
- (ii) $\xi_{\pm} + w$:
 $\sigma_8 = 0.86, b^i = \{1.36, 1.59, 1.63, 1.56, 1.71, 1.68\}$,
- (iii) 3×2 pt:
 $\sigma_8 = 0.733, b^i = \{1.42, 1.66, 1.92, 1.78, 1.97, 1.74\}$.

In terms of clustering amplitudes $b^i \sigma_8$ with respect to the corresponding best-fit values from 3×2 pt in Λ CDM we obtain,

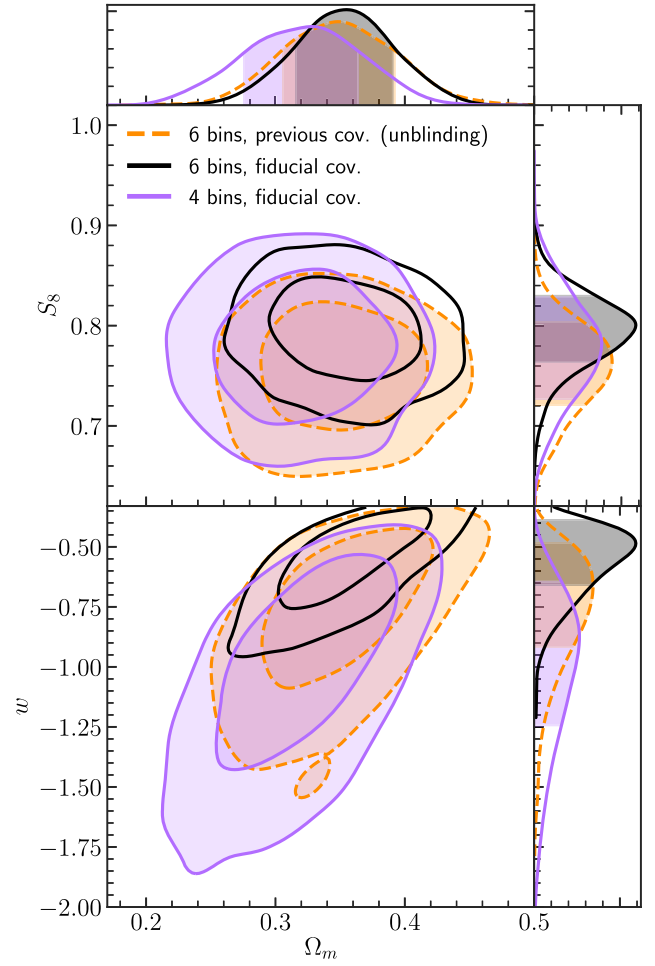


FIG. 15. Comparison of 2×2 pt w CDM constraints for MAGLIM using different iterations of the covariance matrix and number of tomographic bins included.

- (i) $\xi_{\pm} + w/3 \times 2$ pt:
 $b^i \sigma_8 = \{1.12, 1.12, 1.00, 1.02, 1.01, 1.13\}$,
- (ii) $\xi_{\pm} + \gamma_t/3 \times 2$ pt:
 $b^i \sigma_8 = \{1.06, 1.00, 1.07, 0.96, 0.63, 0.5\}$.

This seems to indicate that the galaxy-galaxy lensing signal is too low with respect to the theory model in the last two bins, leading to unexpectedly low values for the galaxy biases given the brightness of the MAGLIM sample, as well as low σ_8 . We have investigated and discarded various potential sources for this discordance, such as observational systematics [32] or underestimations of the width parameters in the redshift distributions. We have also discarded any correlation of this bias discordance with a particular region of the footprint [33]. The last bins are the ones most impacted by magnification [34], and an overestimation of the magnification coefficients (predicted magnification being too high) could indeed be driving at least part of this effect. In Fig. 7 of [58], the magnification contribution at these bins is already similar to the full galaxy-galaxy

lensing signal. In the Appendix C, we show the residuals between the 2×2 pt measurements and the best-fit theory model when using all six tomographic bins. The last two bins show some fluctuations in the measurements that contribute to the poor fit of the model ($p < 10^{-3}$). In all, these bins do not carry much signal-to-noise ratio for the 3×2 pt combination, and we decided to simply remove them from the analysis [37]. We defer further investigations to subsequent work.

The summary of best-fit χ^2 values and goodness-of-fit PPD p -values for these three sets of chains following the initial unblinding are

- (i) 2×2 pt Λ CDM unblinding, six bins: $\chi^2 = 367$ for 336 degrees of freedom¹⁵ (373 data points and 37 free parameters), calibrated PPD $p = 0.351$,
- (ii) 2×2 pt Λ CDM fiducial covariance, six bins: $\chi^2 = 463$ for 336 degrees of freedom (373 data points and 37 free parameters), calibrated PPD $p < 10^{-3}$,
- (iii) 2×2 pt Λ CDM fiducial cov., four bins: $\chi^2 = 280$ for 204 degrees of freedom (235 data points and 31 free parameters), calibrated PPD $p = 0.019$,

where the first entry corresponds to the unblinding result, the second to those using a covariance updated to the unblinding best-fit results (and keeping the full data vector), and the third to a rerun removing the last two lens bins. A further update to the covariances does not change the best-fit values or the goodness-of-fit, hence the updated covariance after unblinding became our fiducial covariance. As discussed,

the first and third stages satisfy the preestablished PPD threshold for publication of $p > 0.01$.

Furthermore, in Table V we detail the mean and 68% C.L. for the relevant cosmological parameters, at each stage, for both Λ CDM and w CDM. Removing the last two bins decreases the constraining power considerably, by 27% (38%) in the $\Omega_m - S_8$ plane in Λ CDM (w CDM) and by 62% in the $\Omega_m - w$ plane. However, the changes in the mean of the parameters are within the corresponding final 68% C.L. region (i.e. within 1σ) when removing the last two bins. Except for w , that moves by 1.5σ 's towards Λ CDM. In all, we conclude that the cosmology results are not driven by the decision on removing the last two tomographic bins from the data vector. In Figs. 14 and 15 we show the two dimensional contour plots for the posteriors in (S_8, Ω_m) for Λ CDM and (S_8, Ω_m, w) for w CDM, respectively.

APPENDIX C: DATA-VECTOR RESIDUALS

We show the measurements for galaxy clustering $w(\theta)$ and tangential shear $\gamma_t(\theta)$ using the MAGLIM lens sample. These measurements are described in detail in Rodríguez-Monroy *et al.* [32] and Prat *et al.* [58], respectively, and summarized in Sec. II E. In Figs. 16 and 17, we compare these measurements with the best-fit Λ CDM theory prediction when using all six tomographic bins (black lines) or just the first four bins (purple), which is our final result.

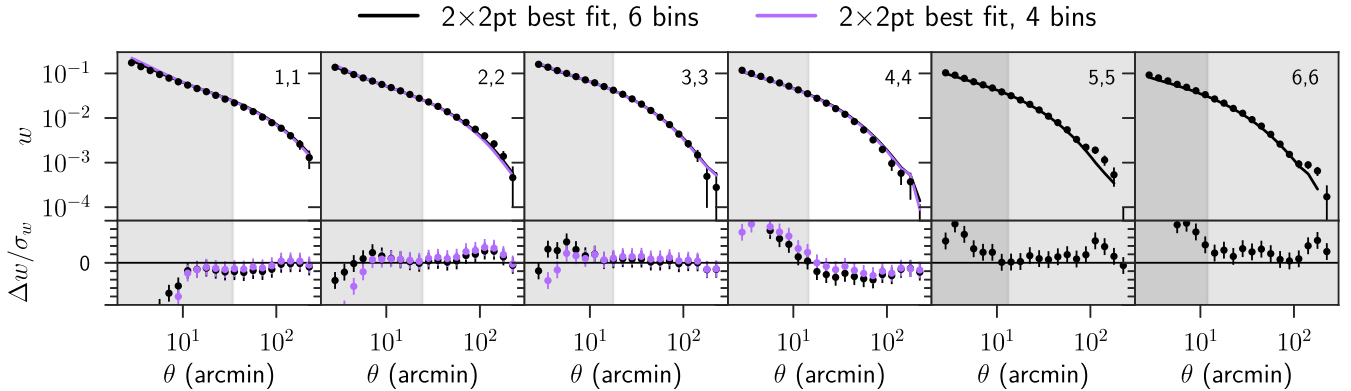


FIG. 16. Galaxy clustering $w(\theta)$ measurements for MAGLIM in each tomographic bin i . The best-fit Λ CDM model from the 2×2 pt analysis using all six redshift bins is shown with a solid black line, while the best fit when using the first four bins (the fiducial result) is shown in purple. The bottom part of each panel shows the fractional difference between the measurements and the model prediction, $(w^{\text{obs}} - w^{\text{th}})/\sigma_w$, with the y-axis range being $\pm 5\sigma$. The angular scales excluded in the analysis are shaded, and bins five and six are not included in the final analysis.

¹⁵We have not accounted for the informative priors used on the parameters when estimating the number of degrees of freedom. We expect the effective number of degrees of freedom to be lower. For example, for the cosmic shear analysis [35,36] the effective number of free parameters is ~ 5 , compared to the total number of free parameters (28).

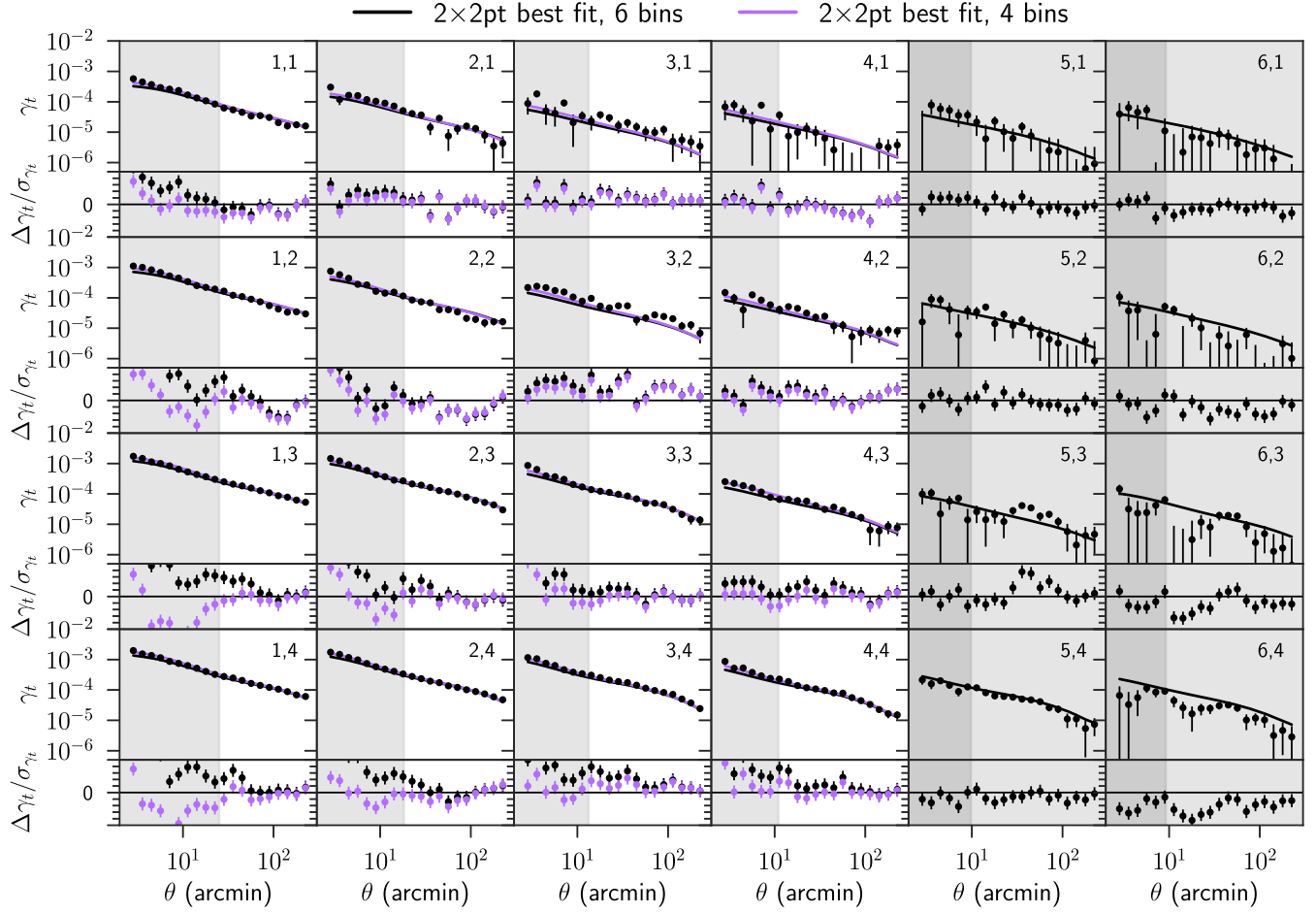


FIG. 17. Same as Fig. 16 but showing the measured tangential shear $\gamma_t(\theta)$. In each panel, the label i, j refers to the lens tomographic bin i and the source bin j .

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