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Optimizing Truss Structures Using Composite Materials under Natural Frequency Constraints with a New Hybrid Algorithm Based on Cuckoo Search and Stochastic Paint Optimizer (CSSPO)

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Abstract: This article highlights the absence of published paradigms hybridized by The Cuckoo Search (CS) and Stochastic Paint Optimizer (SPO) for optimizing truss structures using composite materials under natural frequency constraints. The article proposes a novel optimization algorithm called CSSPO for optimizing truss structures made of composite materials, known as fiber-reinforced polymer (FRP) composites, to address this gap. Optimization problems of truss structures under frequency constraints are recognized as challenging due to their non-linear and non-convex search spaces that contain numerous local optima. The proposed methodology produces high-quality optimal solutions with less computational effort than the original methods. The aim of this work is to compare the performance of carbon FRP (CFRP), glass FRP (GFRP), and steel using a novel hybrid algorithm to provide valuable insights and inform decision-making processes in material selection and design. Four benchmark structure trusses with natural frequency constraints were utilized to demonstrate the efficiency and robustness of the CSSPO. The numerical analysis findings indicate that the CSSPO outperforms the classical SPO and exhibits comparable or superior performance when compared to the SPO. The study highlights that implementing CFRP and GFRP composites in truss construction leads to a notable reduction in weight compared to using steel.

Keywords: truss structures; fiber-reinforced polymer; Cuckoo Search; Stochastic Paint Optimizer; composite materials



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1. Introduction

In the last few decades, a plethora of metaheuristic optimization approaches have been created to address diverse engineering problems. These algorithms explore the search space pseudo-randomly based on certain guiding principles without requiring gradient information. Due to their superior performance, lower computational requirements, and shorter processing times compared to deterministic algorithms, metaheuristic algorithms have gained popularity in various fields [1–5]. These algorithms rely on simple concepts and can quickly adapt to different domains. In contrast, deterministic algorithms can become trapped in local optima, especially if they lack randomness in later stages. Including random elements in metaheuristic algorithms can help avoid local optima and explore the search space more effectively. Gradient descent algorithms are generally better suited for direct and simple problems that require gradient information. However, the convergence rate of metaheuristic algorithms is often slower than that of gradient descent algorithms, which can be seen as a drawback [6].

The Genetic Algorithm (GA) [7], Particle Swarm Optimization (PSO) [8], Waterwheel Plant Algorithm (WWPA) [9], Coati Optimization Algorithm (COA) [10], Grey Wolf Optimizer (GWO) [11], Growth Optimizer (GO) [12], Artificial Rabbits Optimization [13],

Wild Horse Optimizer (WHO) [14], Circle Search Algorithm (CSA) [15], and Mountain Gazelle Optimizer (MGO) [16] are some of the well-established metaheuristic optimization algorithms. These algorithms have demonstrated their effectiveness in diverse domains, efficiently tackling a broad range of problem types.

Optimizing truss structures is a tough challenge that requires the consideration of multiple design objectives and constraints [17]. One crucial constraint in truss design is the natural frequency limitation, which limits the maximum allowable frequency of vibration that a structure can undergo without experiencing significant deformation or damage. Optimizing trusses while satisfying natural frequency constraints requires a thorough understanding of the interaction between design parameters and the natural frequency [18].

Knowledge of structural dynamics has shown that the natural frequency is a crucial factor that significantly impacts a structure's performance. The development of optimal truss designs based on their dynamic behavior has emerged as a complex area of research. The determination of natural frequencies is a crucial aspect in understanding the dynamic behavior of a structure. In the last few decades, there has been an upward trend of interest in truss improvements based on frequency constraints. Controlling the natural frequencies of a truss is essential to prevent the resonance phenomenon and improve its structural performance. However, it is also necessary to ensure that engineering structures are as lightweight as possible, which conflicts with frequency constraints and complicates truss optimization. It is imperative to employ an efficient optimization technique for these topics that adheres to primary frequency constraints. Consequently, researchers are dedicating substantial efforts in this field [19].

Creating truss structures that are both lightweight and high performing is crucial for numerous engineering applications, such as those found in aerospace, automotive, and civil engineering. Recently, the use of pultruded fiber-reinforced polymer (FRP) materials in truss structures has gained significant attention due to their excellent mechanical properties, including high strength-to-weight ratio, corrosion resistance, and durability. However, designing an optimal FRP truss that meets various design constraints, such as natural frequency limitations, can be a novel and challenging task [20].

The generalized normal distribution optimization (GNDO) algorithm was proposed by Khodadadi and Mirjalili [21] for the optimal weight design of truss structures with frequency constraints. Due to the abundance of local optima and the non-convex character of the search space, optimization problems of this kind are well recognized for being difficult. This study aimed to investigate the efficacy of the GNDO algorithm for addressing the aforementioned issues. The GNDO algorithm's performance was evaluated using three benchmark truss optimization problems that had frequency constraints. The results obtained from the numerical analysis suggest that the GNDO algorithm exhibits high levels of dependability, consistency, and effectiveness in the context of structural optimization problems, surpassing other metaheuristic algorithms in terms of performance.

Tiknov and Safnov [22] addressed the challenge of enhancing the distribution of carbon fiber in hybrid glass and carbon FRP components that form a statically determinate regular elastic truss structure for airplanes. The authors suggested a modified genetic algorithm that integrates with mathematical induction. To ensure the optimality of the process, the proposed a method that focuses on minimizing structural material costs while also satisfying the requirements of elastic strength.

Kaveh et al. [23] presented an upgraded version of The Slime Mould Algorithm, referred to as ISMA, which was designed to optimize truss structure sizes while also taking into account constraints related to the natural frequency. The algorithm known as Slime Mould was derived from the study of the morphological transformations exhibited by the acellular slime mould *Physarum polycephalum* during its foraging activities. This algorithm has been effectively employed in a range of optimization problems across the fields of science and industry. The standard Slime Mould Algorithm might exhibit slow and premature convergence towards suboptimal solutions, particularly when dealing with

problems of larger scales. In order to address these challenges, the ISMA has proposed the implementation of two notable enhancements. The efficacy and resilience of the ISMA has been exhibited through the utilization of three benchmark dome trusses with natural frequency constraints.

Liu et al. [24] introduced a new approach to enhancing the search capability of The Fruit Fly Optimization Algorithm (FOA) by implementing a memory-based search strategy. Additionally, an improved Deb rule (IDeb) was utilized to improve the computational efficiency of FOAs while dealing with constraints. Instead of a fixed search radius, the proposed strategy dynamically determined the vision search radius for each fruit fly by incorporating knowledge from both the swarm and individuals. The IDeb rule was founded on the principle of FOA elitism and effectively reduces redundant analyses throughout optimization while maintaining the high quality of the optimal solution. This study offered four optimization problems for trusses with frequency constraints to assess the effectiveness of the method. The findings suggested that the integration of standard and proposed search tactics in funding opportunity announcements (FOAs) yielded the most optimal outcome. The implementation of the IDeb rule had resulted in a notable enhancement in the computational efficiency of FOAs utilized in structural optimization.

A study introduced a metaheuristic approach known as The Modified Simulated Annealing Algorithm (MSAA) [25] to optimize the size and shape of truss structures while ensuring that they meet frequency constraints. The Modified Simulated Annealing Algorithm (MSAA) is an upgraded version of The Simulated Annealing Algorithm. It incorporates three notable modifications, namely preliminary exploration, a search step, and a new acceptance probability. The efficacy of the MSAA was assessed through the analysis of six benchmark truss optimization problems that incorporated frequency constraints. The computational results indicated that MSAA outperformed other contemporary metaheuristics approaches to optimization in terms of efficiency, stability, and reliability.

Ho-Huu [26] developed a novel approach to differential evolution (DE) that addresses truss structures' shape and size optimization challenges while adhering to frequency constraints. The new approach, which was suggested, represents a refined version of the DE algorithm that incorporates two significant enhancements. The roulette wheel selection was initially employed as a substitute for random selection in the mutation phase, as observed in the conventional differential evolution approach. Moreover, a technique based on elitism was used to replace the traditional selection approach during the selection phase to enhance the convergence rate of the method. The efficacy and reliability of the proposed approach were demonstrated using five numerical instances. The findings indicated that the algorithm put forth outperformed several optimization techniques documented in the existing literature.

The main contribution in [18] was the proposition of an enhanced iteration of The Symbiotic Organisms Search (ISOS) Algorithm, initially developed to tackle the difficulties mentioned earlier. The main inspiration for this advancement was to augment the exploitative tendencies of the initial SOS algorithm. Although the original algorithm successfully stimulated exploration to evade local solutions, it regrettably had an adverse effect on solution precision. This study analyzed the feasibility and efficiency of ISOS, utilizing six benchmark planar/space trusses. The results were subsequently compared to those of other meta-heuristics. According to the experimental findings, the ISOS algorithm exhibited more reliability and efficiency than the conventional SOS algorithm and different modern algorithms.

In order to enhance the efficacy and efficiency of addressing optimization issues related to truss shape and size while adhering to frequency constraints, a Niche Hybrid Parallel Genetic Algorithm (NHPGA) [27] was proposed. The novel methodology was designed with the objective of reducing the computational cost while simultaneously enhancing the solution's accuracy. The NHPGA achieved these objectives by integrating the advantages of parallel computing, simplex search, and a genetic algorithm with the niche technique. The efficacy of The Nondominated Sorting Hybrid Pareto Genetic Algorithm

(NHPGA) in reducing computational time and producing high-quality solutions was demonstrated through various truss optimization examples. The NHPGA exhibits potential as an algorithmic framework that integrates the robust and global search characteristics of The Genetic Algorithm, the powerful exploitation capacity of simplex search, and the rapid computation capability of parallel computing.

Recently, the study [28] aimed to enhance the efficacy of The Conventional Particle Swarm Optimization Algorithm by integrating the proficient phasor theory in mathematics and a comprehensive learning strategy for three-dimensional truss structures. Throughout the course of optimization, a phase angle was incorporated, which employed periodic sine and cosine functions to represent the fundamental parameters that define velocities. The velocities were derived from a designated exemplar's velocity, which was selected from the prior optimal positions of all particles. The aforementioned methodology expedited the acquisition of knowledge pertaining to the collective behavior of the swarm particles. Furthermore, it enabled the determination of the most secure and advantageous size distribution of the structural elements, while taking into account the external forces and inherent frequency conditions. Notably, this was achieved despite the presence of limited computational resources. The design methodology under consideration effectively resolved diverse design benchmarks in practical-scale engineering applications that encompassed three-dimensional space. The findings indicated that the algorithm exhibits high levels of precision and resilience when compared to a range of contemporary metaheuristic methods that have emerged in the field.

These studies collectively demonstrated the effectiveness of stochastic optimization algorithms in resolving various structural design challenges. According to the No-Free Lunch (NFL) [29] theorem, no optimization algorithm can solve all optimization issues, allowing scientists to propose new or improve existing algorithms to solve optimization challenges. The NFL theorem states that while current algorithms in literature can solve a wide range of optimization problems, they cannot solve all optimization problems. It has become popular to combine two or more algorithms instead of creating novel optimization techniques. This approach, known as algorithm hybridization, can overcome the limitations of one algorithm by leveraging the advantages of another algorithm.

This paper presents a study on optimizing FRP truss structures under natural frequency constraints with the hybridization of CS [30] and SPO [31] as a novel metaheuristic algorithm. The study's main objective is to determine the optimal design parameters that satisfy the natural frequency limitations while minimizing the weight of the truss with CSSPO. The paper's novel contributions are as follows:

- The study compared truss structures made of various materials (i.e., CFRP, GFRP, and steel).
- The study used composite material for the optimization of truss design for the first time.
- A novel hybrid of the SPO algorithm called the CSSPO was created, and its strength and robustness were validated by optimizing through the optimization of four different truss structures.
- The CSSPO algorithm was shown to outperform the original SPO algorithm.
- Truss structures made of composite materials resulted in a lighter weight.

The remaining sections of this paper are organized in the following manner: the different types of FRPs are briefly described in Section 2. Section 3 explains the terms related to the definition of truss structures. Section 4 presents the standard SPO and CS and introduces the CSSPO algorithm. Section 5 discusses the results and evaluations of the experiments carried out on four structure problems. Section 6 explains the statical results for all examples. Finally, Section 7 concludes the paper and discusses future work.

2. Composite Materials

Over the past few decades, pultruded fiber-reinforced polymer (FRP) elements have been widely employed in the construction of civil structures due to their numerous advan-

tages. These advantages include a higher strength-to-weight ratio, corrosion-free properties, durability, and lower maintenance. Within the realm of truss structures, FRP materials are gaining some popularity due to their consideration of sustainability. The main benefits are their high strength-to-weight ratio, corrosion resistance, and durability [22]. FRP composites can be created using a variety of fibers, including glass, carbon, aramid, basalt, and resins such as epoxy, polyester, and vinyl ester. The choice of fibers and resins depends primarily on the desired outcome and the cost of the FRP products. While FRP composites possess different mechanical properties, they are often used as replacements for traditional steel or concrete structures in harsh environments [32]. Carbon and glass fibers are the most used in civil engineering applications.

2.1. Glass Fiber Reinforced Polymer (GFRP)

Glass fiber, shown in Figure 1, is the most used fiber in FRP composites. Although it generally possesses lower mechanical properties than carbon and aramid fibers, it is significantly less expensive than carbon when utilized as a reinforcement in polymer composites. Glass fibers are offered in different variants, namely the S-type (structural type), which exhibits superior strength compared to other types, the E-type (electrical type), which has low alkali material, high mechanical characteristics, and is cost-effective, and the C-type (chemical resistance type), which demonstrates high resistance to corrosion and chemicals [33]. Glass fiber is characterized by its anti-corrosion properties, affordability, and high tensile strength. Nonetheless, it is important to note that the utilization of glass fibers is subject to certain constraints. These include comparatively inadequate mechanical properties in comparison to other fibers, such as carbon and aramid fibers, as well as reduced stiffness, low fatigue resilience, and susceptibility to chemicals in severe hygrothermal environments.

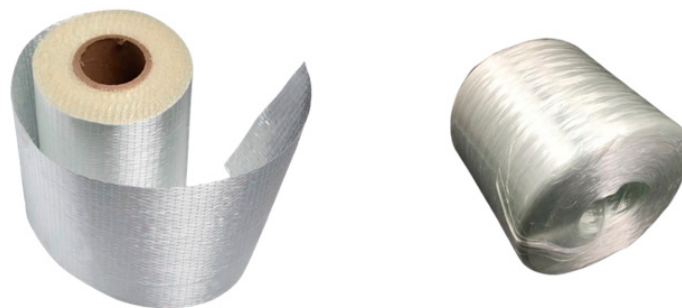


Figure 1. Glass fabrics.

2.2. Carbon Fiber Reinforced Polymer (CFRP)

The utilization of carbon fibers is mainly found in sophisticated composite applications and aerospace, owing to their exceptional stiffness and strength-to-weight ratio (refer to Figure 2). These materials exhibit resistance to elevated temperatures, fatigue, corrosion, and chemical breakdown. The mechanical characteristics of carbon fibers may exhibit significant variability based on the raw materials utilized in the production process. The essential characteristics of carbon fibers include elevated tensile strength-to-weight ratio, elevated tensile stiffness-to-weight ratio, improved resistance to fatigue and stress rupture, high dimensional stability, low abrasion, a low coefficient of thermal expansion, effective vibration damping, high resistance to corrosion, and chemical inertness. While carbon fibers possess numerous advantages, they also have some disadvantages, such as high cost, low strain to failure, electrical conductivity, electromagnetic properties, and limited potential use in specific applications [34].



Figure 2. Carbon fabrics.

The characteristics of FRP materials are subject to considerable variation based on their distinct formulation, components, and production techniques. Typical and idealized GFRP, CFRP, and steel stress–strain curves are illustrated in Figure 3, while the density and modulus of elasticity, as adopted in this study, are shown in Table 1.

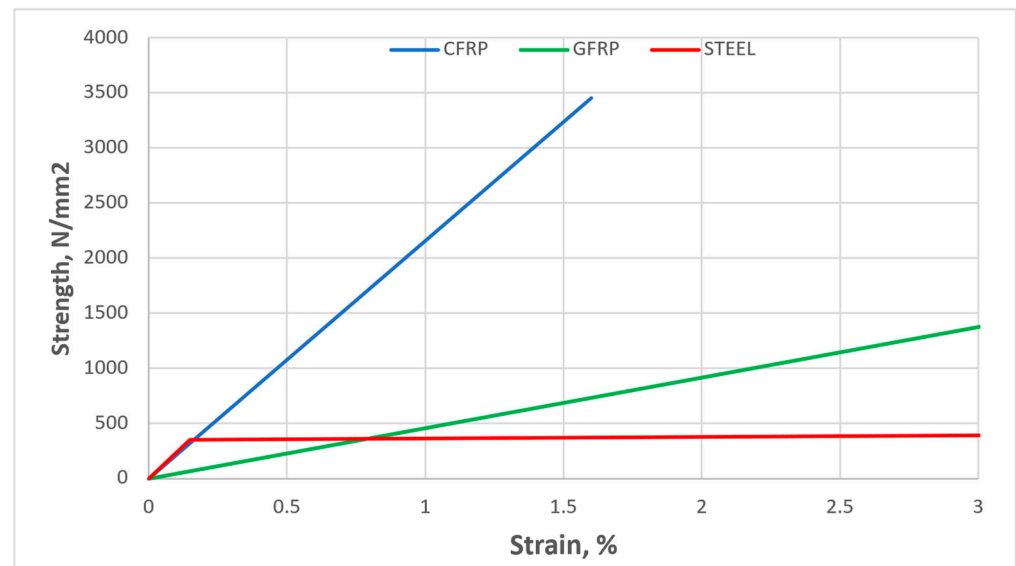


Figure 3. Typical FRP and steel stress–strain curves.

Table 1. Material properties.

Material	Density		Modulus of Elasticity	
	lb/ft ³	Kg/m ³	GPa	Ksi
GFRP	97	1550	55	8000
CFRP	109	1750	160	23,000
Steel	490	7850	207	30,000

2.3. FRP Properties

FRP materials have a low density, resulting in a high strength-to-weight ratio, which is highly significant in transportation and various structural applications. Compared to steel, CFRP and GFRP possess strength-to-weight ratios several times higher and are also lighter. In summary, the distinct characteristics of FRP, including its high strength-to-weight ratio and low density, offer advantages in handling, transportation, and insulation. These features play a significant role in reducing the weight of truss structures [33].

Compared to steel structures, FRP composites also have a higher stiffness-to-weight ratio, making them a preferred material for truss bridge structures [33]. However, deflection is the main outstanding issue for FRP trusses and space frames that need to withstand heavy loads.

Considering aging infrastructure, exploring and implementing innovative materials to extend these structures' lifespan is crucial. New resin formulations and fibers are being developed with the aim of creating enhanced materials that can endure challenging environmental and loading circumstances. Despite the potential benefits of FRP composites, their limited fire resistance remains a significant concern that hinders their widespread application.

3. Definition of Truss Structures Optimization

This section describes the development of an optimization formulation for truss structures with multiple constraints on natural frequencies. Figure 4 presents a flowchart of the truss optimization problem. Optimizing truss structures involves determining the optimal cross-sectional (A_i) values to minimize the weight (W) of the structure. The resulting design must meet the following criteria [35]:

$$\text{Find} \quad [x_1, x_2, \dots, x_{ng}] \quad (1)$$

$$\text{Minimize} \quad W(\{x\}) = \sum_{i=1}^{nm} \gamma_i \cdot A_i \cdot L_i(x) \quad (2)$$

$$\text{Subjected to} \quad \begin{cases} x_{\min} \leq x_i \leq x_{\max} \\ \omega_j \leq \omega_j^* \\ \omega_k \geq \omega_k^* \end{cases} \quad (3)$$

In the above Equation, $\{X\}$ represents the set of design variables, while ng specifies the number of design variables and nm indicates the range of structural members. The structure's weight is denoted by $W(\{x\})$, and the members' material density, length, and cross-sectional area are represented by γ_i , L_i and x_i , respectively. The j th and k th natural frequencies of the truss are stated as ω_j (with an upper bound of ω_j^*) and ω_k (with a lower bound of ω_k^*).

The ideal function for addressing the constraints arising from the fundamental principle and ease of implementation is commonly known as:

$$f_{\text{penalty}}(X) = (1 + \varepsilon_1 \cdot \nu)^{\varepsilon_2} \quad (4)$$

$$\nu = \sum_{i=1}^n \max [0, v_i] \quad (5)$$

In the equation, ν denotes the total number of violated constraints, while the constants ε_1 and ε_2 are chosen to balance the exploration and exploitation rates of the search space. In this scenario, ε_1 is assigned a value of 1, while ε_2 is selected to decrease both penalties and cross-sections. At the outset of the search process, ε_2 is initialized to 1.5 and is then gradually increased to 3, as described in [36].

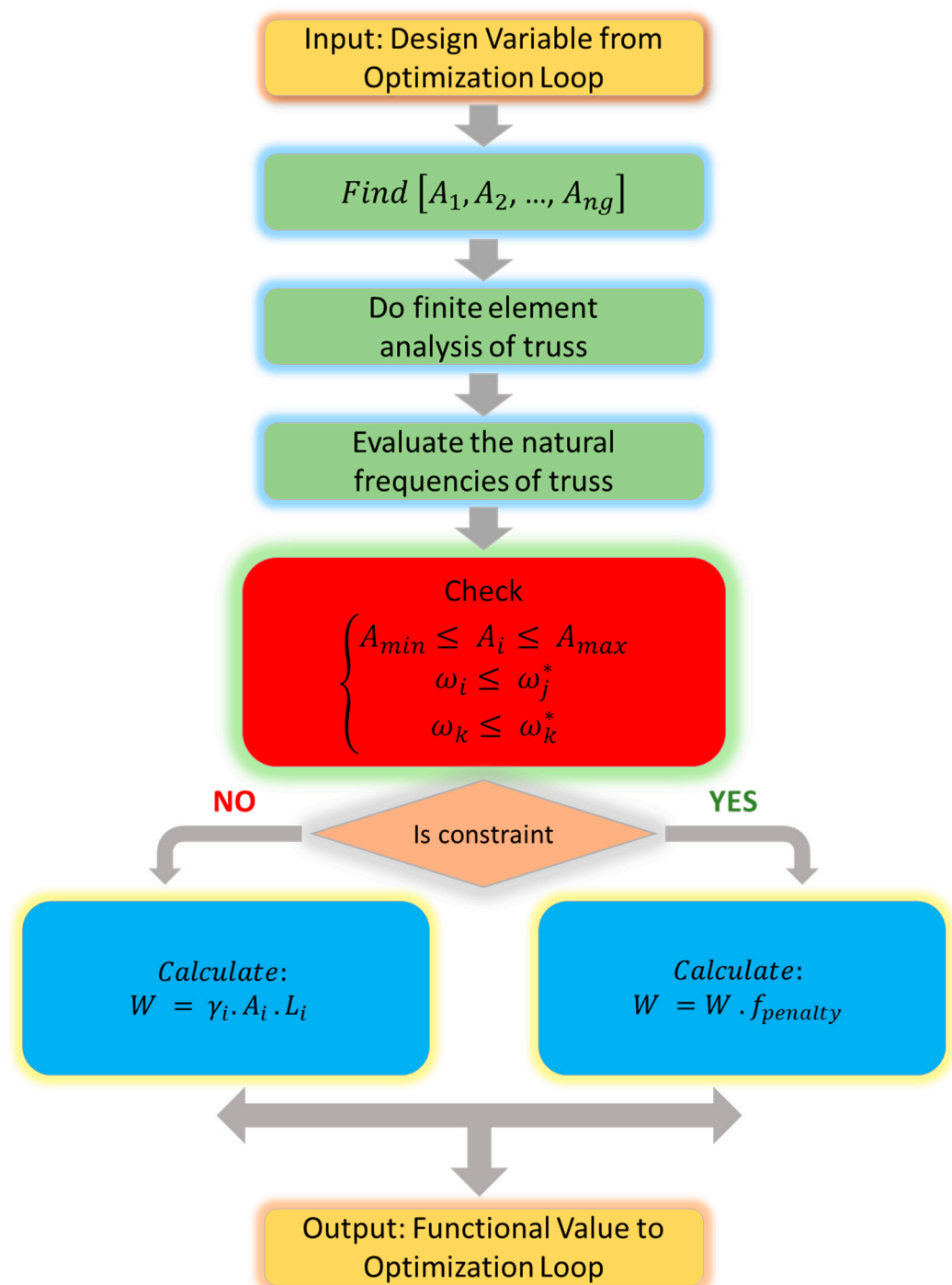


Figure 4. Flowchart of the truss optimization definition problem.

4. Methodology

4.1. Cuckoo Search (CS)

The Cuckoo Search (CS) algorithm is a metaheuristic technique that draws inspiration from nature. It was originally created by Yang and Deb [30]. The methodology is founded on the brood parasitic behavior that has been observed in certain species of cuckoos. Cuckoos are a fascinating avian species, notable not only for their melodious vocalizations but also for their extremely aggressive reproductive tactics. Certain species, such as the ani and Guira cuckoos, exhibit communal nesting behavior and may engage in the removal of foreign eggs to enhance the likelihood of successful hatching. The cuckoo search algorithm is founded upon three fundamental principles. Initially, it is important to note that each

individual cuckoo lays a single egg at a time and subsequently places it within a nest at randomly. Next, the nests containing eggs of superior quality are chosen for the succeeding generation. The quantity of host nests currently available is established and remains constant. Figure 5 shows the flowchart of the cuckoo search algorithm. The likelihood of a host bird discovering a cuckoo's egg is determined by a probability value that falls within the range of 0 to 1 [37].



Figure 5. Cuckoo search algorithm flowchart.

An initial population of host nest positions, $M = [X_1; X_2; X_3; \dots; X_m]$, is generated in a random distribution throughout the multi-dimensional host nest. Each solution X is represented by a D -dimensional vector. The cuckoo then randomly selects a host nest position to deposit its egg, using a random walk known as Levy flights. The equations for this process are given in Equations (6) and (7).

$$V_{pq}^{t+1} = V_{pq}^t + S_{pq} \times Levy(\lambda) \times \alpha \quad (6)$$

$$Levy(\lambda) = \left| \frac{\Gamma(1+\lambda) * \sin \frac{\Pi * \lambda}{2}}{\Gamma \frac{1+\lambda}{2} * \lambda * 2^{\frac{1-\lambda}{2}}} \right|^{\frac{1}{\lambda}} \quad (7)$$

In the equations given above, p , f , and q are randomly selected indices from the sets $\{1, 2, \dots, m\}$, $\{1, \dots, m\}$, and $\{1, 2, \dots, D\}$, respectively. Here, D represents the number of optimized parameters, while m represents the total population of host nest positions. The constant value, denoted by A , is used where $1 \leq \lambda \leq 3$. The current generation number is represented by t , and a is a randomly generated number that falls within the range of -1 to 1 . Additionally, $s > 0$ represents the step size. The choice of an appropriate step size is crucial, as a large value will generate a new solution that is too far away from the previous solution, while a small value will produce a change that is not significant enough to improve the search efficiency. Therefore, the step size is calculated using Equation (8).

$$S_{pq} = V_{pq}^t - V_{fq}^t \quad (8)$$

The cuckoo uses Equation (8) to determine the appropriate step size and select a host nest to lay its egg. After the egg is laid, it is evaluated. The host bird then uses Equation (9) to determine the likelihood of identifying an alien egg based on the quality associated with that particular egg.

$$Pro_p = \frac{0.9 * F(I)}{\max(Fit)} + 0.1 \quad (9)$$

In Equation (9), $F(I)$ represents the fitness value of solution p , which is proportional to the quality of the egg in the nest position p . The value Pro_p represents the survival probability rate of the cuckoo's egg. If a random probability value P that falls within the range of $[0, 1]$ is greater than Pro_p , the host bird identifies the egg as alien and proceeds to destroy it or abandon the nest. In this case, the cuckoo must find a new host's nest, located in a new position, using Equation (10) in order to lay its egg. If the probability value P is less than or equal to Pro_p , the egg survives and remains in the nest to contribute to the next generation based on the fitness function.

$$X_p = X_{pmin} + rand(0, 1) * (X_{pmax} - X_{pmin}) \quad (10)$$

X_{pmin} and X_{pmax} refer to the lower and upper boundaries, respectively, of the parameters that are being optimized.

4.2. Stochastic Paint Optimizer (SPO)

The Stochastic Paint Optimizer (SPO) [38] is a metaheuristic technique that was first created in 2020. It leverages color theory to optimize artwork. The algorithm involves several key steps, including generating initial paints, clustering, merging, and determining when to stop. The search space in the algorithm is defined as a canvas, with paints serving as solutions that comprise various colors as design variables. These paints are evaluated based on their beauty index, which reflects their objective function values. Since colors significantly impact how viewers perceive artwork, each color is assigned a score or value based on its position in the color wheel's primary, secondary, or tertiary categories. These categories are considered equal; therefore, no additional parameters are necessary for the algorithm. To create a new population, the SPO algorithm combines stochastic solutions, where colors are blended to form a new one [38]. The diagram depicted in Figure 6 illustrates four fundamental methods of color combination that are based on the principle of the color wheel. Each of these techniques has the ability to generate novel colors (C_i^{new}).

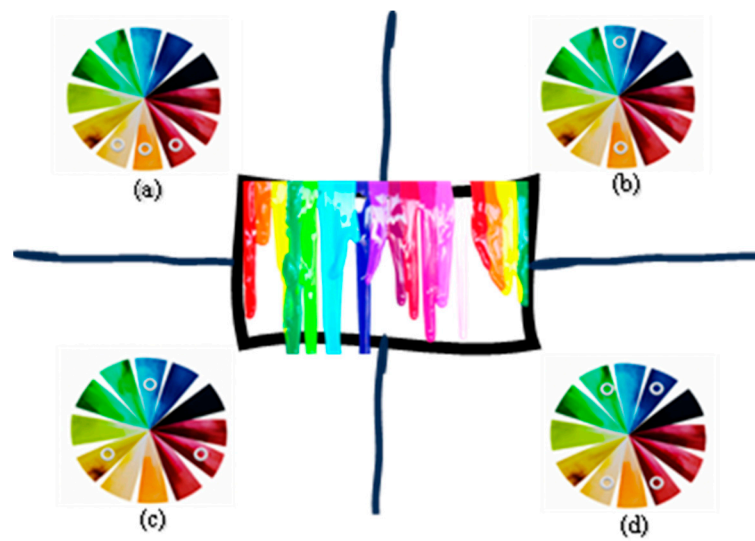


Figure 6. Four different types of color mixing in SPO. (a) Analogous Combination, (b) Complementary Combination, (c) Triadic Combination and (d) Tetradic Combination.

The following sections will provide a description and explanation of the mathematical concepts employed in the SPO for the purpose of simulating color combination patterns.

4.2.1. Analogous Combination Technique

Mixing of three adjacent colors on the color wheel, as depicted in Figure 6a, is utilized to achieve this color mixing technique. The SPO employs the following equation to accomplish this:

$$C_{new}^1 = C_i + rand \cdot (C_{i+1} - C_{i-1}) \quad (11)$$

The variables C_{i-1} , C_i , and C_{i+1} denote three solutions selected from the population, while $rand$ is a randomly generated vector within the domain of $[0, 1]$.

4.2.2. Complementary Combination Technique

Complementary colors are employed when blending colors using this method, as illustrated in Figure 6b. To replicate this process in the SPO, a primary color C_P , a tertiary color (C_T), and an already-existing color C_i are randomly selected. Equation (12) is employed to achieve this outcome.

$$C_{new}^2 = C_i + rand \cdot (C_P - C_T) \quad (12)$$

The symbols used in the equation correspond to the following: C_P refers to a primary color, C_T signifies a tertiary color, C_i denotes an already existing color, and $rand$ represents a vector that is randomly generated within the interval of $[0, 1]$.

4.2.3. Triadic Combination Technique

The approach involves producing novel colors by blending the evenly spaced colors around the color wheel (see Figure 6c). In the SPO, this is accomplished through the following method:

$$C_{new}^3 = C_i + rand \cdot \left(\frac{C_P + C_S + C_T}{3} \right) \quad (13)$$

The variables used in the equation correspond to the following: C_P signifies a primary color, C_S represents a secondary color, C_T denotes a tertiary color, C_i refers to an existing color, and $rand$ represents a vector that is randomly generated within the range of $[0, 1]$.

4.2.4. Tetradic Combination Technique

This color blending technique selects four complementary colors from rectangular arrangements on the color wheel, as shown in Figure 6d. The SPO implements this approach through the use of Equation (14):

$$C_{new}^4 = C_i + \left(\frac{rand_1 \cdot C_P + rand_2 \cdot C_S + rand_3 \cdot C_T + rand_4 \cdot C_{rand}}{4} \right) \quad (14)$$

$$C_{rand} = LB + rand \cdot (UB - LB) \quad (15)$$

where LB and UB represent the minimum and maximum bounds of the design variable, and $rand_1$, $rand_2$, $rand_3$, and $rand_4$ are four random vectors within the range $[0, 1]$. The stochastic paint optimizer flowchart algorithm is illustrated in Figure 7.

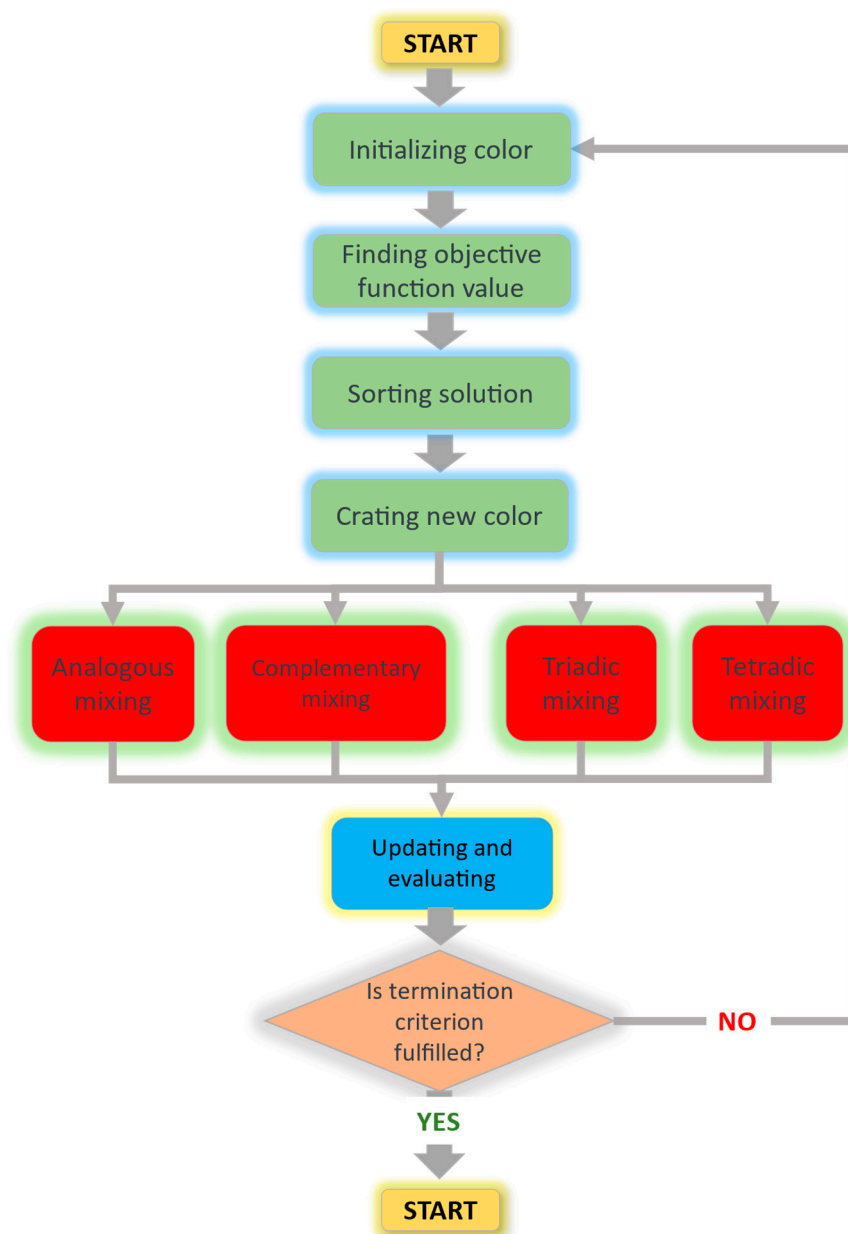


Figure 7. Stochastic paint optimizer flowchart algorithm.

4.3. The Hybrid of Cuckoo Search-Stochastic Paint Optimizer (CSSPO)

The CSSPO algorithm uses the SPO method as a starting point for a set number of iterations. The best solution obtained from SPO is then passed onto the CS algorithm, which serves as an intensification process to enhance the search and overcome the slow convergence of SPO. The CSSPO algorithm balances the CS algorithm's global exploration and the SPO method's deep exploitation, improving overall performance. The Levy flight in CSSPO is more effective in exploring the search space, as it can cover longer distances than the traditional random searching method. Thus, the Levy flight replaces the random searching method in the SPO algorithm, resulting in the modified CSSPO algorithm. This algorithm has two parameters which are set as references (Population Size = 50, Beta = 2/3). The CSSPO algorithm benefits from the lowest parameter tuning, so the number of parameters that should be tuned is at the minimum. The CSSPO algorithm follows the same steps as the standard SPO algorithm until line 9 in Algorithm 1. Then, the CS method in Algorithm 1 is applied as an intensification process to refine the best solution obtained from the previous stage in the standard SPO algorithm.

Algorithm 1: Pseudo-code of CSSPO

Inputs: The number of colors (pop size)

Outputs: The best location of colors and their objective values

1. Initialize the random colors
 2. Find the objective values
 3. *For* ($it < itMax$) *Do*
 4. Divide colors into three groups randomly
 5. *for every color*
 6. Create new colors (combine colors)
 7. Sort the fitness of all colors
 8. Find the best colors
 9. Build new nests at new locations using Levy flight
 10. Retain the best solutions (nests with quality solutions)
 11. Rank the solutions and find the current best solution
 12. *End for*
 13. *End For* (*Termination criteria are satisfied*)
 14. *Return* the best solution
-

5. Structural Examples

This section demonstrates the effectiveness of FRPs compared with steel for CSSPO by examining several common structural optimization problems. The results obtained using CSSPO are compared to those obtained using SPO. Natural frequency is an important property to consider when optimizing truss structures, as it describes the frequency at which the structure will vibrate when subjected to external forces or disturbances. In the context of structural optimization, natural frequency constraints are essential to ensure that the resulting design is both structurally sound and capable of withstanding the dynamic loads or vibrations it may experience over its lifespan. The termination criterion that relied on the maximum count of function evaluations is utilized to guarantee an impartial comparison. Problems are addressed individually, each undergoing 30 rounds of runs. The examination is carried out employing the CSSPO, using a similar number of analyses and representatives to maintain fair competition. In addition, the previously cited references contribute additional control parameters for the comparative algorithms. To preserve fairness in the competition, both the CSSPO and SPO are applied over a similar range of evaluations and representatives. The natural frequency constraints are applied to four truss designs: a 37-member planar bridge, a 72-member space truss, a 120-member dome truss, and a 200-member planar truss. These constraints, material properties, and cross-sectional area constraints are essential parameters that must be considered during optimization to achieve a design that meets the necessary performance requirements while minimizing weight or maximizing other design objectives. The constraints of these problems are shown in Table 2. The algorithm was implemented using MATLAB 2022b software, while

the trusses were solved using SAP2000 v14.1. The process of optimization entailed the utilization of the application programming interface (API). A Macintosh machine running MacOS Big Sur and equipped with an Intel Core i9 processor running at 2.3 GHz, 16 GB of RAM at 2400 MHz DDR4, and the aforementioned software was used to perform the optimization calculations.

Table 2. Design constraints for various optimization problems.

Test Problem	Cross-Sectional A (cm ²)	Natural Frequency Constraints ω (Hz)
37-member planar bridge	$1 \leq A$	$\omega_1 \geq 20, \omega_2 \geq 40, \omega_3 \geq 60$
72-member space truss	$0.645 \leq A$	$\omega_1 = 4, \omega_3 \geq 6$
120-member dome truss	$1 \leq A \leq 129.3$	$\omega_1 \geq 9, \omega_2 \geq 11$
200-member planar truss	$0.1 \leq A$	$\omega_1 \geq 5, \omega_2 \geq 10, \omega_3 \geq 15$

5.1. A 37-Member Planar Truss

The first instance presented in this subsection is the weight minimization of a planar 37-member truss structure, as depicted in Figure 8. Wang et al. [27] were the first to examine this case study, and many others have subsequently followed similar methods. Table 1 presents the material properties for this problem, which involves 14 sizes and 5 design variables. A mass of 10 kg, referred to as the lumped mass, is added to the bottom nodes of the bridge, the cross-sectional areas of the lower chord members are 0.4 cm², and the remaining members are assumed to have a cross-section of 1 cm². All nodes of the upper chord can be moved along the y -axis while maintaining the structure's symmetry. Different composite materials are used to optimize this structure. In this section, the 37-member planar bridge under natural frequency constraints is optimized using the SPO and CSSPO with a population size of 50 and 20,000 function number evaluations.

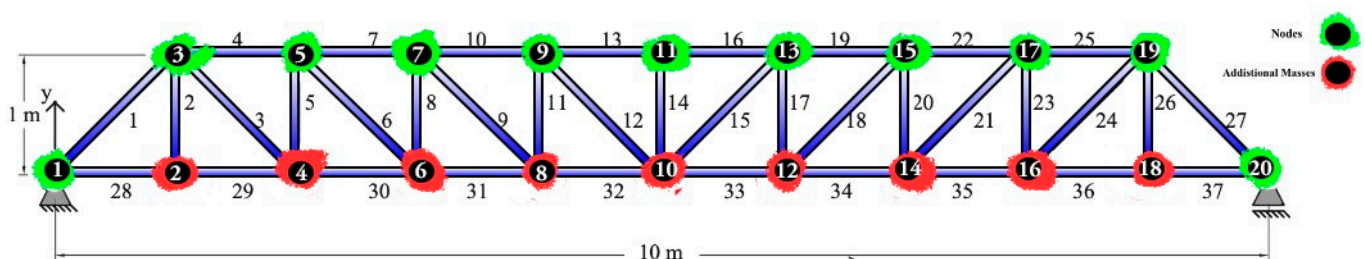


Figure 8. The 37-member planar bridge.

The results illustrated in Table 3 indicate that the CSSPO algorithm outperforms the SPO algorithm for GFRP, CFRP, and steel materials, with the best results achieved with CSSPO for all materials. The composite materials, GFRP and CFRP, showed competitive results compared to steel. The optimal weight obtained was 76.3119 kg for GFRP and 76.8983 kg for CFRP using the CSSPO algorithm. The results demonstrate that the CSSPO algorithm outperforms SPO. The standard deviation for all materials with the CSSPO was considerably less than with SPO, indicating that CSSPO is more reliable than SPO. Figure 9 depicts the convergence curve of the best weight for SPO and CSSPO with different materials. In addition, this figure demonstrates that composite materials were more optimal in weight than steel. The convergence curve of the best weight for CSSPO was significantly better than SPO, as shown in Figure 9. According to this figure, CSSPO requires less function evaluation for reaching the best solution. Moreover, the results of the CSSPO for all materials are compared in Figure 10. In the rankings, GFRP secured the top spot, with CFRP achieving a commendable second place. In summary, this figure demonstrates the superiority of composite materials.

Table 3. Optimized results of GFRP, CFRP, and steel using SPO and CSSPO for a 37-member bridge.

Materials	GFRP		CFRP		Steel	
Member Group	SPO	CSSPO	SPO	CSSPO	SPO	CSSPO
(Y ₃ -Y ₁₉) m	1.5184	1.0011	1.0001	1.0000	1.0048	1.0000
(Y ₅ -A ₁₇) m	1.8947	1.3657	1.6809	1.3292	1.3652	1.3728
(Y ₇ -A ₁₅) m	2.0950	1.5189	1.6850	1.5813	1.5746	1.5405
(Y ₉ -Y ₁₃) m	2.2646	1.6556	1.8538	1.7402	1.7213	1.6485
(Y ₁₁) m	2.3462	1.7209	1.9387	1.8052	1.8217	1.7231
(A ₁ -A ₂₇) cm ²	5.0000	4.2428	1.0000	1.0002	3.6223	2.9181
(A ₂ -A ₂₆) cm ²	1.9234	1.4950	1.0000	1.0000	1.6336	1.0191
(A ₃ -A ₂₄) cm ²	1.0002	1.2581	1.0000	1.0000	1.0013	1.0009
(A ₄ -A ₂₅) cm ²	2.0466	3.9872	1.8513	1.0451	3.2354	2.6357
(A ₅ -A ₂₃) cm ²	1.9483	1.8549	1.0002	1.0001	3.2649	1.2225
(A ₆ -A ₂₁) cm ²	2.3951	2.0886	1.0000	1.0000	1.0807	1.2106
(A ₇ -A ₂₂) cm ²	2.3431	3.7248	1.0181	1.1791	1.7398	2.6363
(A ₈ -A ₂₀) cm ²	2.1990	2.1120	2.0736	1.0000	1.0324	1.4348
(A ₉ -A ₁₈) cm ²	2.5342	2.2236	1.5062	1.0000	1.2940	1.5293
(A ₁₀ -A ₁₉) cm ²	2.0994	3.9553	1.0272	1.2119	2.0527	2.7911
(A ₁₁ -A ₁₇) cm ²	4.3423	1.8406	1.0015	1.0000	1.5098	1.2057
(A ₁₂ -A ₁₅) cm ²	2.8011	1.9479	1.8380	1.0000	1.4822	1.2726
(A ₁₃ -A ₁₆) cm ²	3.1363	3.8760	1.0000	1.2400	3.4292	2.4663
(A ₁₄ -A ₁₆) cm ²	1.0045	1.0035	1.0000	1.0000	1.0014	1.0004
Best weight (kg)	80.8917	76.3119	79.0690	76.8983	370.8402	363.2729
Average weight (kg)	140.6229	77.3588	85.0605	76.9032	434.8858	364.4259
Standard deviation	49.6651	1.1125	7.6528	0.0058	57.8664	1.1706
No. Analyses	13,150	10,500	5400	4400	6150	4600

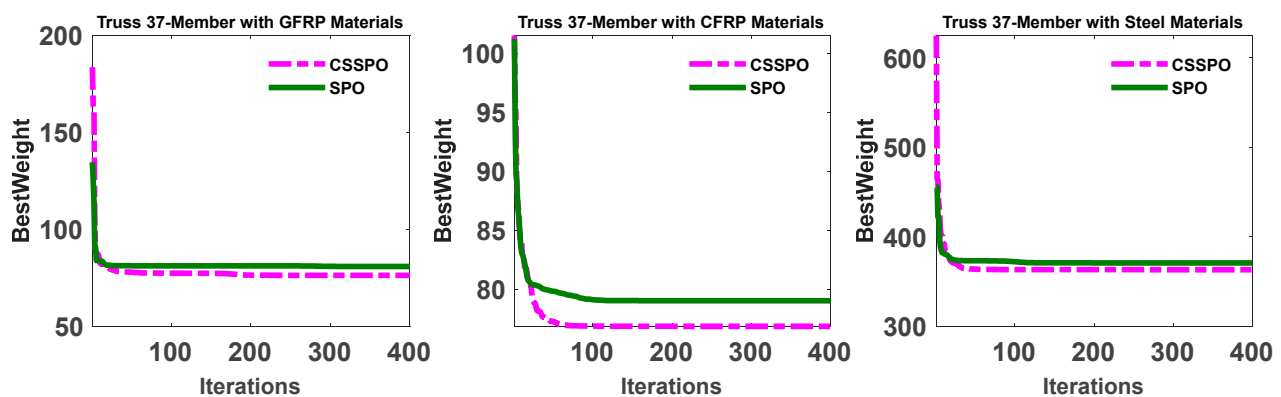
**Figure 9.** The best weight convergence curves for SPO and CSSPO with GFRP, CFRP, and steel for a 37-member bridge.

Figure 11 presents the convergence curve of the mean weight for the SPO and CSSPO approaches with GFPP, CFRP, and steel materials. The results demonstrate that the CSSPO outperforms SPO. Figure 12 is given to further demonstrate the performance of the different materials. This figure displays the mean weight for the CSSPO for all composite materials across 30 distinct runs. The figure indicates that CFRP and GFRP materials achieved the best and most competitive results. Figure 13 illustrates the outcomes of 30 distinct runs for the SPO and CSSPO. In this figure, the minimum achieved result is represented by the blue line, while the red line represents the average of all 30 runs. The results indicate that the CSSPO is able to approximate the average weight value closely, and that most of the results were near the best solution. Table 4 provides the first three natural frequencies obtained by the SPO and CSSPO algorithms. This table demonstrates that the algorithms met the satisfactory constraints for this problem.

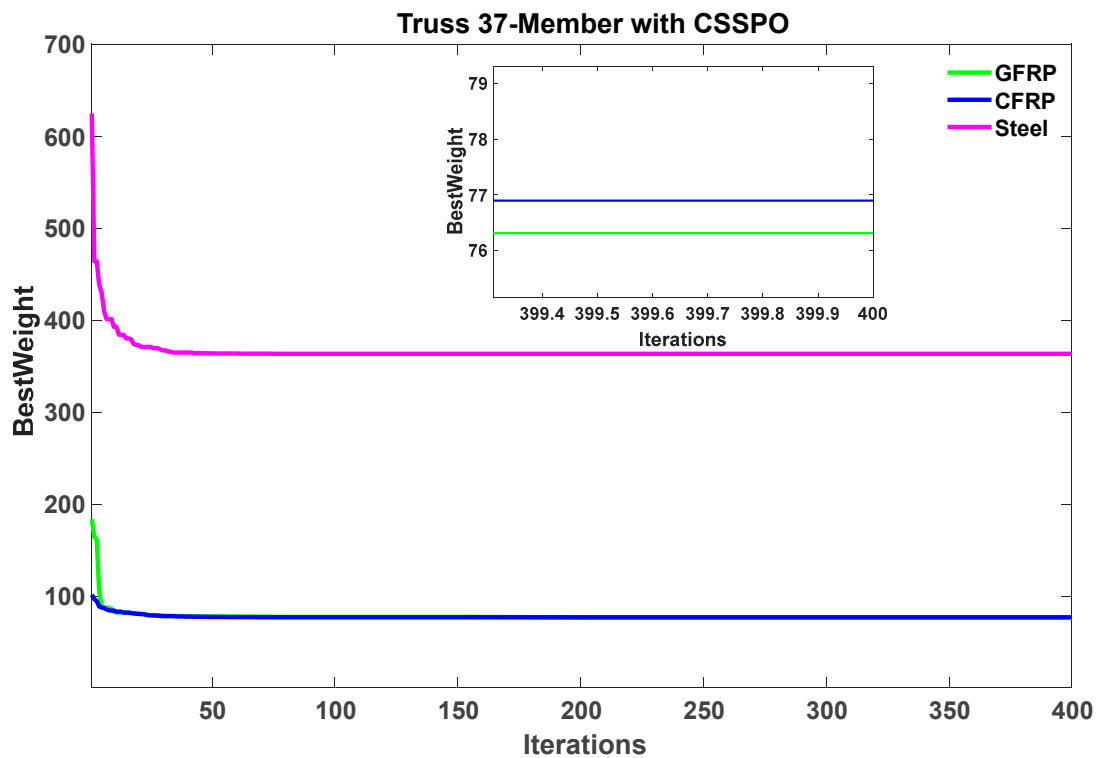


Figure 10. Comparison of best weight convergence curves for GFRP, CFRP, and steel using the CSSPO algorithm for a 37-member bridge.

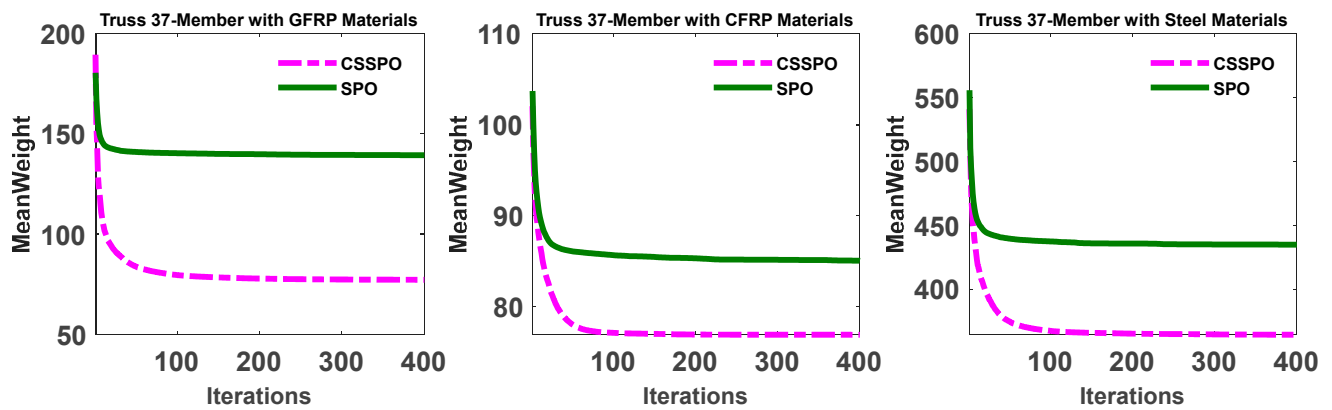


Figure 11. The average weight convergence curves for SPO and CSSPO with GFRP, CFRP, and steel for a 37-member bridge.

Table 4. Natural frequencies (Hz) for the best design of a 37-member bridge.

Materials	GFRP		CFRP		STEEL	
Frequency No.	SPO	CSSPO	SPO	CSSPO	SPO	CSSPO
f_1	20.000	20.0000	20.0024	20.0001	20.0000	20.0000
f_2	42.9544	40.0000	47.3363	42.2966	40.0049	40.0000
f_3	60.0000	60.0000	67.8965	66.0972	60.0000	60.0000

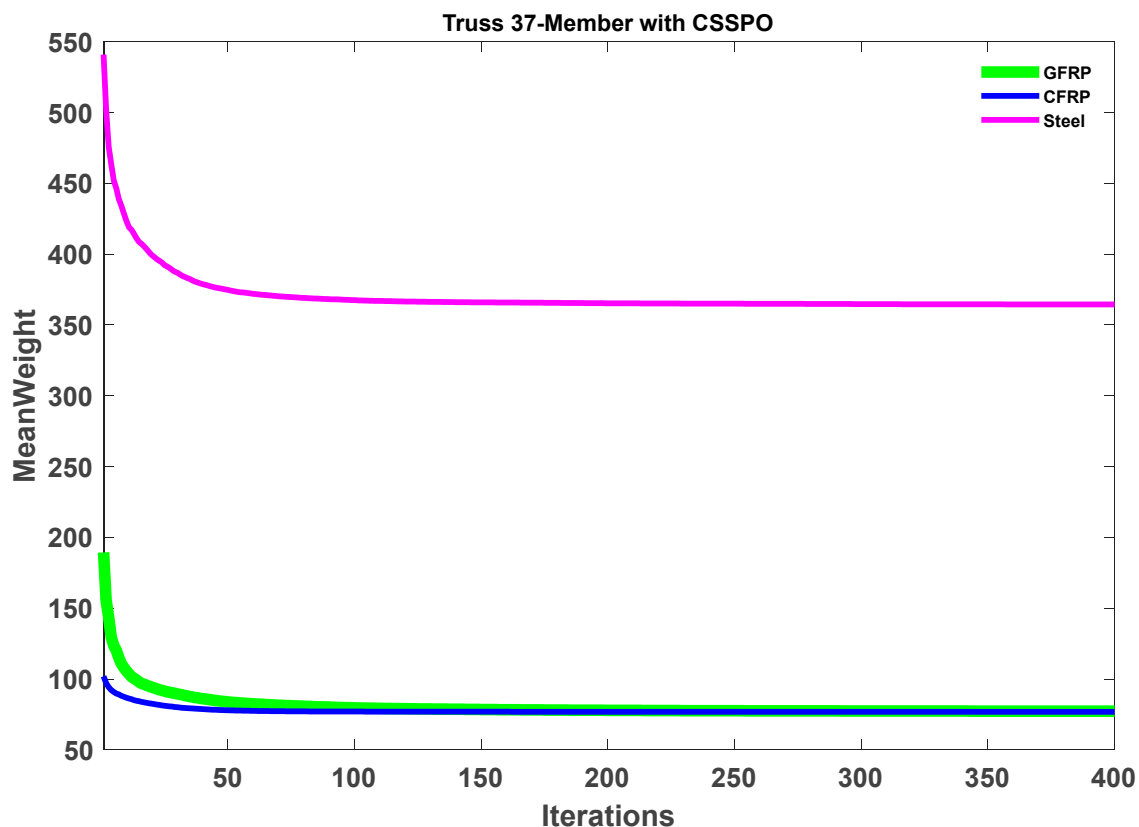


Figure 12. Comparison of average weight convergence curves for GFRP, CFRP, and steel using the CSSPO algorithm for a 37-member bridge.

5.2. A 72-Member Space Truss

The second example in this section involves the weight minimization of a spatial truss with 72-members, as illustrated in Figure 14. This problem has 16 sizing variables due to the structural symmetry, and the material characteristics and boundaries for this case are summarized in Table 2. Four non-structural masses of 10 kg are added to nodes 1–4. The SPO and CSSPO algorithms are evaluated for this problem with natural frequency constraints.

The optimization results of the SPO and CSSPO were compared using different materials (GFRP, CFRP, and steel), with a population size of 50 and 20,000 function evaluations. All statistical results and the number of function evaluations obtained from 30 runs are presented in Table 5. The outcomes of 30 distinct runs for SPO and CSSPO are shown in Figure 15. This figure displays the minimum achieved outcome, represented by the blue line, and the average of all 30 runs, represented by the red line. Therefore, most of the results are close to each other between the best and mean lines. The figure demonstrates that the solution obtained using the CSSPO with CFRP was much better than for other materials. The CSSPO approach yielded the best results, with weights of 227.2641 kg, 94.8585 kg, and 337.7553 kg, while the SPO algorithm produced weights of 236.0334 kg, 103.4361 kg, and 356.0184 kg for GFRP, CFRP, and steel, respectively (refer to Table 5).

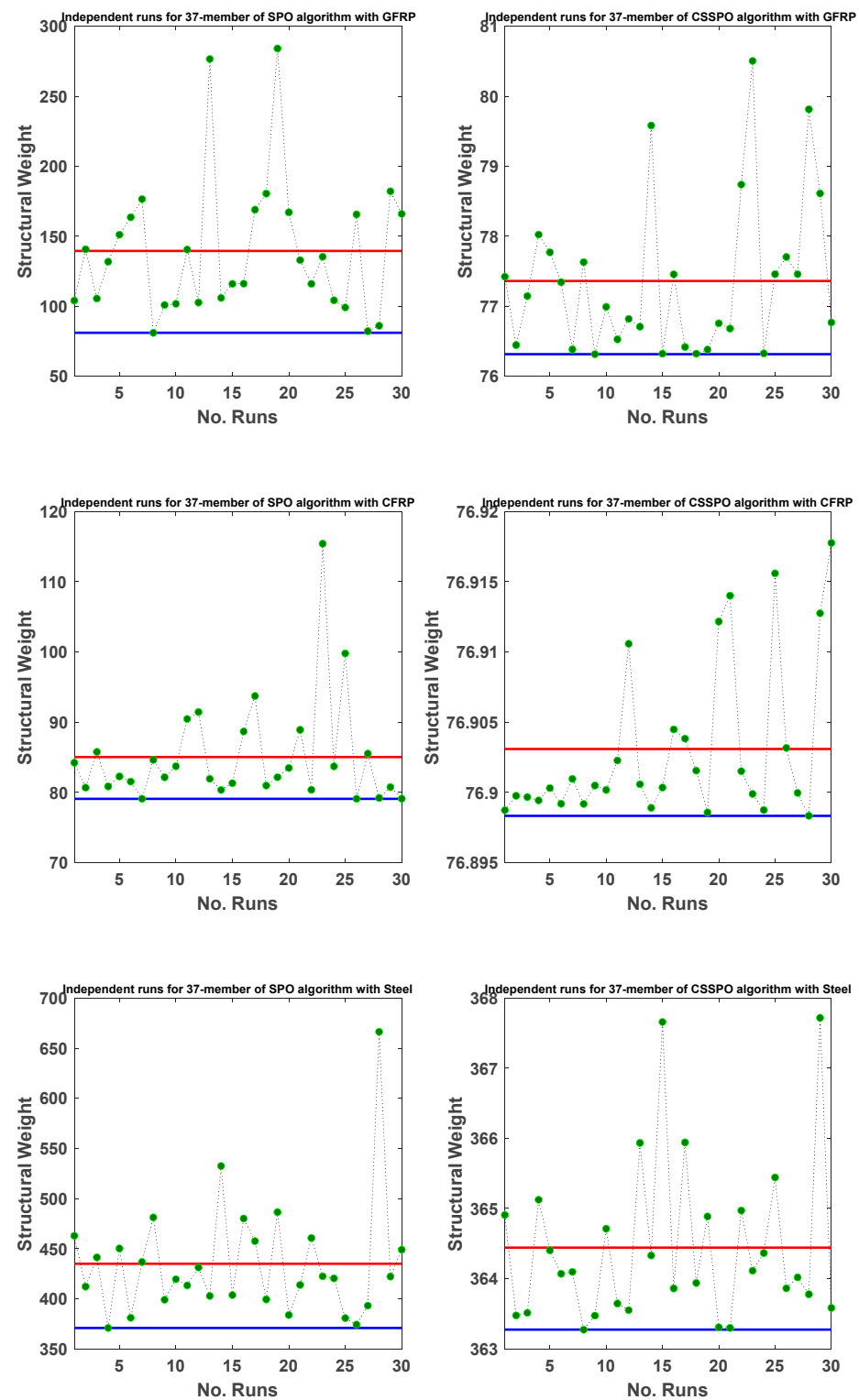


Figure 13. Weights of 30 distinct runs for SPO and CSSPO for a 37-member truss with different materials.

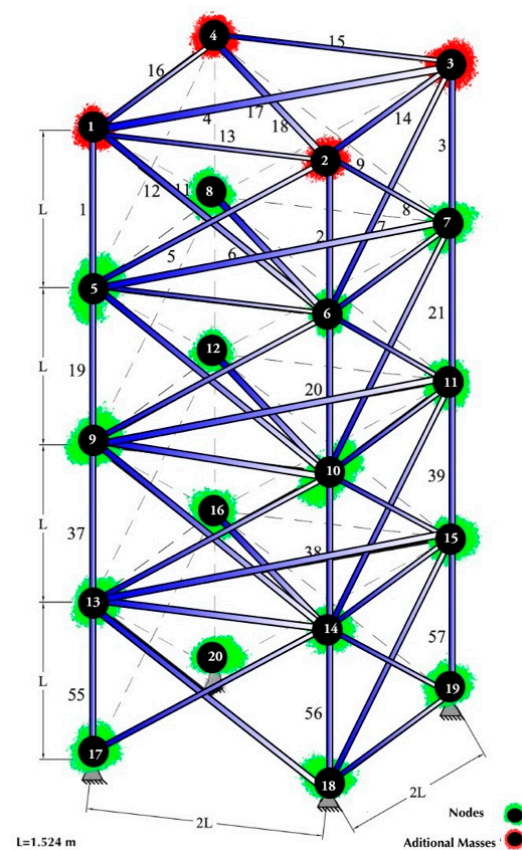


Figure 14. The 72-member space truss structure.

Table 5. Optimized results of GFRP, CFRP, and steel using SPO and CSSPO for a 72-member truss.

Materials	GFRP		CFRP		STEEL	
Member Group	SPO	CSSPO	SPO	CSSPO	SPO	CSSPO
1 (A_1 - A_4) cm^2	13.3972	4.7702	1.4932	1.4932	1.4932	1.1560
2 (A_5 - A_{12}) cm^2	9.4481	9.9981	3.4486	3.4486	3.4486	2.6751
3 (A_{13} - A_{16}) cm^2	0.6450	0.6450	0.6450	0.6450	0.6450	0.6450
4 (A_{17} - A_{18}) cm^2	0.6724	0.7181	0.6450	0.6450	0.6450	0.6450
5 (A_{19} - A_{22}) cm^2	12.0096	10.5253	3.4111	3.4111	3.4111	2.6876
6 (A_{23} - A_{30}) cm^2	11.3740	10.0562	3.5042	3.5042	3.5042	2.6555
7 (A_{31} - A_{34}) cm^2	0.6450	0.6450	0.6450	0.6450	0.6450	0.6450
8 (A_{35} - A_{36}) cm^2	0.6450	0.6450	0.6450	0.6450	0.6450	0.6453
9 (A_{37} - A_{40}) cm^2	13.6289	16.9763	5.7274	5.7274	5.7274	4.2783
10 (A_{41} - A_{48}) cm^2	8.6208	10.0865	3.5086	3.5086	3.5086	2.6824
11 (A_{49} - A_{52}) cm^2	0.6450	0.6450	0.6450	0.6450	0.6450	0.6450
12 (A_{53} - A_{54}) cm^2	0.6450	0.6450	0.6450	0.6450	0.6450	0.6452
13 (A_{55} - A_{58}) cm^2	20.0000	20.0000	7.3112	7.3112	7.3112	5.6892
14 (A_{59} - A_{66}) cm^2	11.2354	9.9604	3.4397	3.4397	3.4397	2.7112
15 (A_{67} - A_{70}) cm^2	0.6450	0.6450	0.6450	0.6450	0.6450	0.6450
16 (A_{71} - A_{72}) cm^2	0.6450	0.6450	0.6450	0.6450	0.6450	0.6450
Best weight (kg)	236.0334	227.2641	103.4361	94.8585	356.0184	337.7553
Average weight (kg)	268.0583	227.3044	129.3833	94.8953	472.1857	337.8333
Standard deviation	23.0932	0.0311	18.6853	0.0271	65.8768	0.0600
No. Analyses	19,100	6900	6800	4900	4150	4050

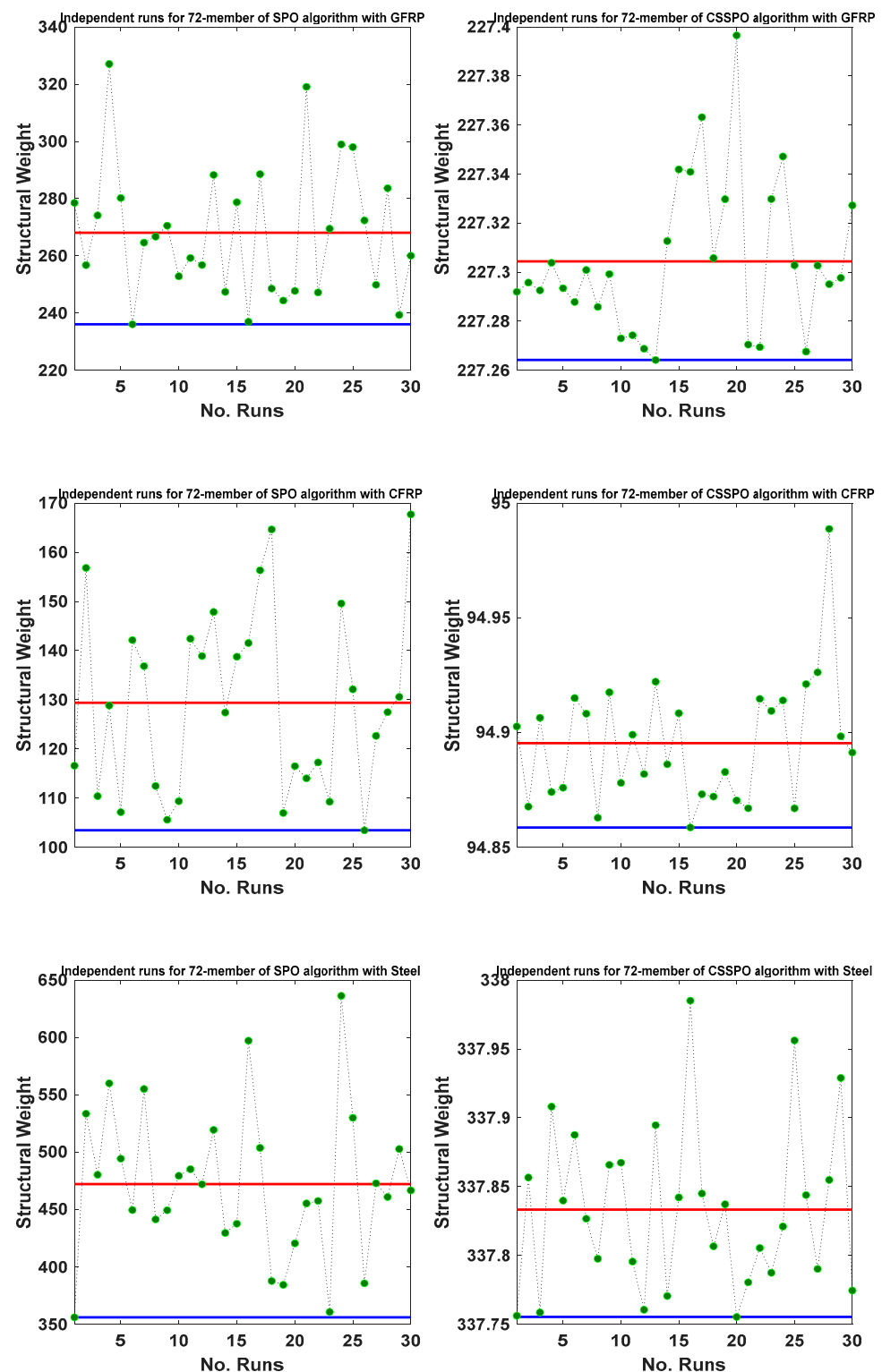


Figure 15. Weights of 30 distinct runs for SPO and CSSPO for a 72-member truss with different materials.

According to Table 5, the CSSPO algorithm with CFRP material performed the best among its competitors, with the lowest optimal weight of 94.8585 kg, the lowest average weight of 94.8953 kg, and the highest accuracy of $SD = 0.0271$. In comparison, GFRP ranked second, with an optimal weight of 227.2641 kg, an average weight of 227.3044 kg, and a standard deviation of 0.0311. The results indicate that CSSPO is more reliable and produces

superior results compared to the other results reported in the literature. Additionally, the findings demonstrate that using CFRP and GFRP is more efficient than steel. Based on Table 6, the presented method's natural frequency constraints were strictly satisfied for all bounds.

Table 6. Natural frequencies (Hz) for the best design of a 72-member truss.

Materials	GFRP		CFRP		STEEL	
Frequency No.	SPO	CSSPO	SPO	CSSPO	SPO	CSSPO
f_1	4.0000	4.0000	4.0000	4.0000	4.0000	4.0000
f_2	4.0001	4.0001	4.0000	4.0000	4.0001	4.0001
f_3	6.0000	6.0000	6.0002	6.0000	6.0000	6.0000
f_4	6.0023	6.0049	8.5403	8.2394	8.9257	9.0087
f_5	8.7654	8.6107	10.6718	9.7387	9.2840	9.8549

Figure 16 depicts the best weight convergence curves for the SPO and CSSPO with GFRP, CFRP, and steel for a 72-member truss. This figure demonstrates that the CSSPO outperforms the SPO. Based on this figure, the CSSPO for all materials requires lower function evaluations than the SPO. The best convergence curves for CFRP, GFRP, and steel are compared with each other in Figure 17. According to the details presented in the figure, CFRP was determined to be a feasible solution and had attained the highest weight ranking among all the materials examined in this study. In addition, it was observed that CFRP exhibited the lowest mean weight when employing the CSSPO compared to the other materials cited (see Figure 18). This figure indicates that the convergence rate of the CSSPO is better than that of the SPO. Figure 19 shows that CFRP ranked second among its competitors, with an average weight of 94.8953 kg. In addition, steel fell behind GFRP in the rankings, placing it at the bottom of the material list.

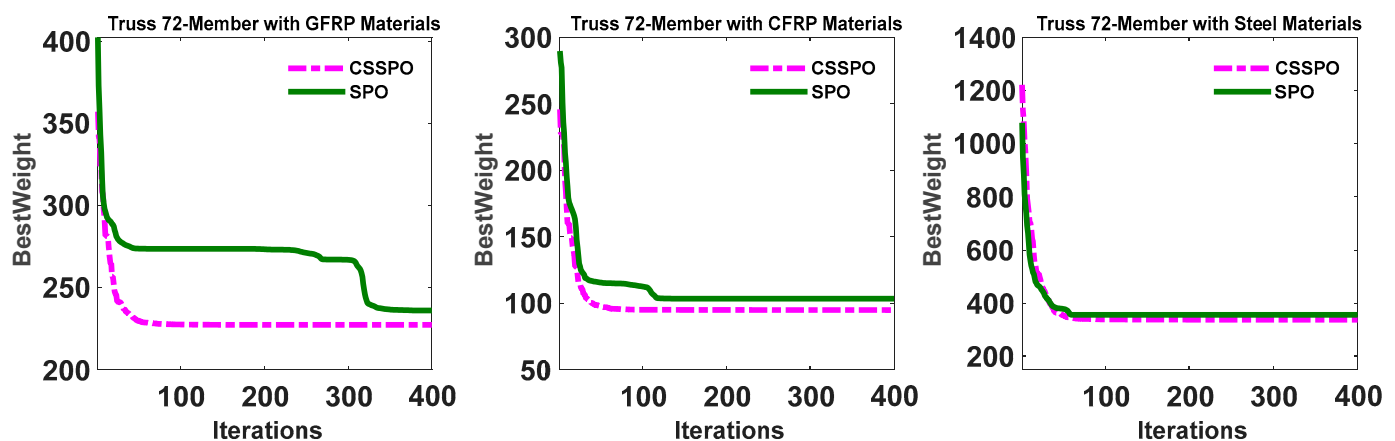


Figure 16. The best weight convergence curve for SPO and CSSPO with GFRP, CFRP, and steel for a 72-member truss.

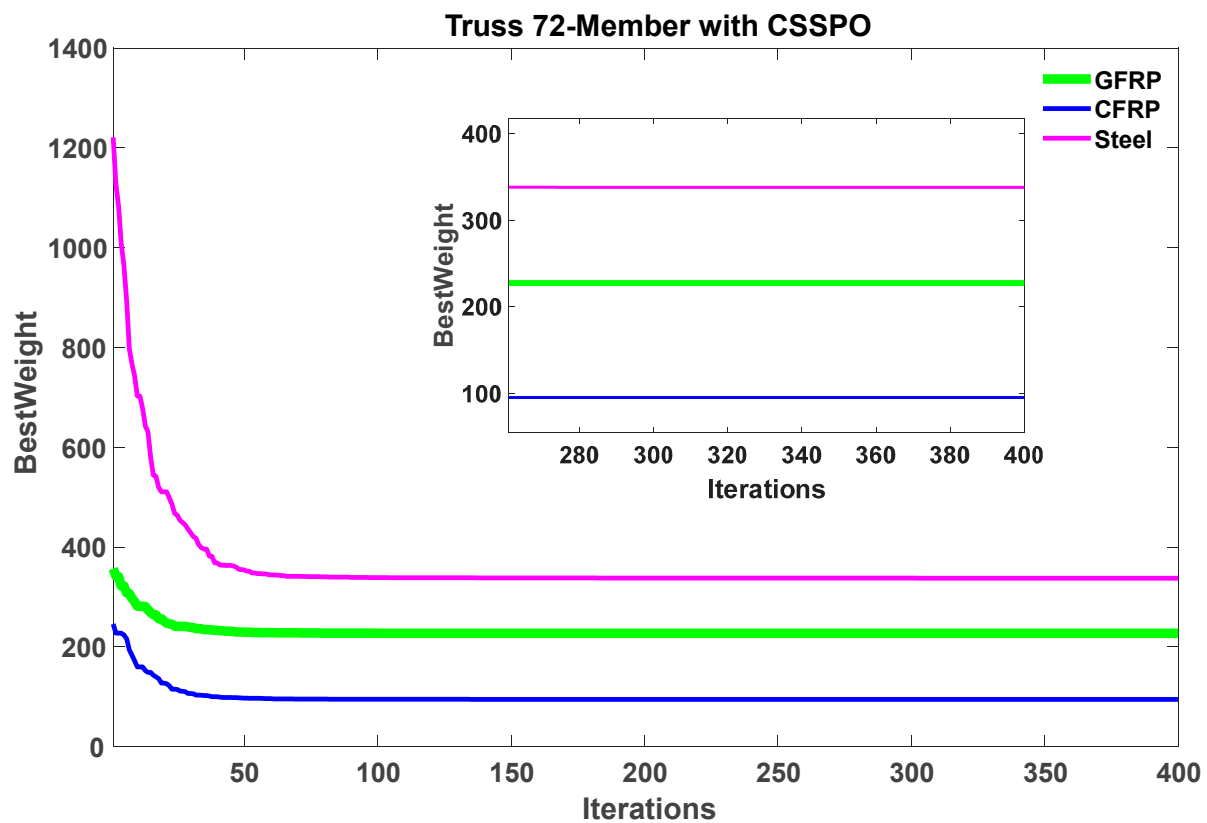


Figure 17. Comparison of best weight convergence curves for GFRP, CFRP, and steel with the CSSPO algorithm for a 72-member truss.

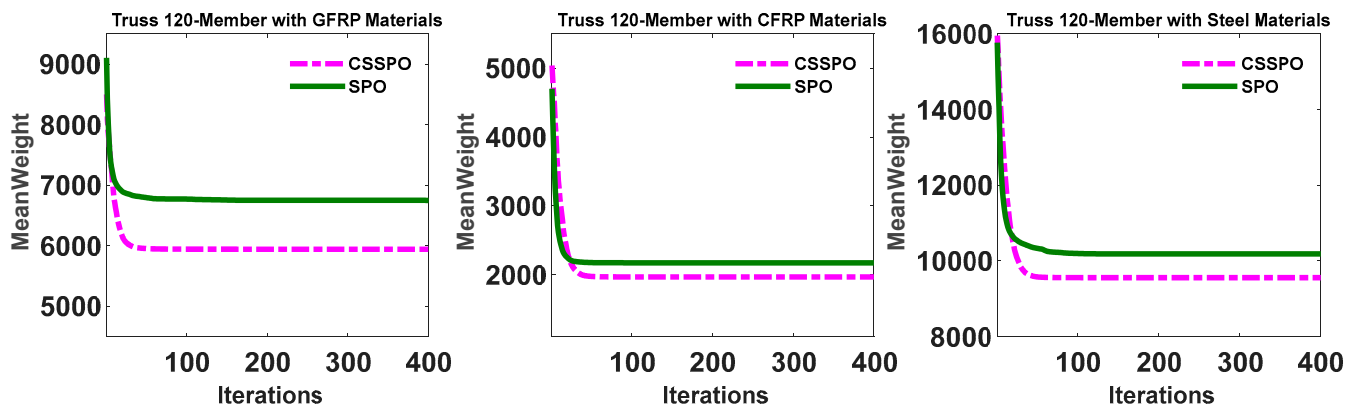


Figure 18. Average weight convergence curve for SPO and CSSPO with GFRP, CFRP, and steel for a 72-member truss.

5.3. A 120-Member Dome Truss

The third benchmark problem is illustrated in Figure 20, which involves optimizing the size of a 120-member three-dimensional dome truss. This problem was initially studied by Kaveh and Zolghadr [39], and Table 2 summarizes the design considerations. Non-structural masses were added at node 1 (3000 kg), nodes 2–13 (500 kg each), and the remaining free nodes (100 kg each). The elements were categorized into seven groups based on the assumption of symmetry around both the x -axis and y -axis. The cross-sectional areas varied between 1 and 129.3 cm².

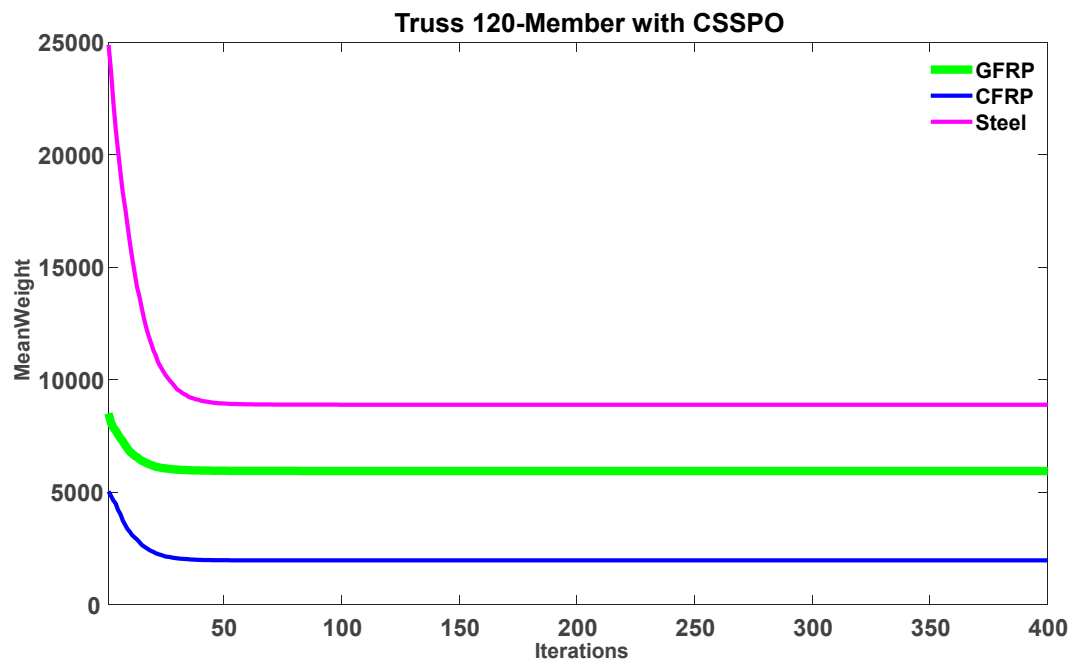


Figure 19. Comparison of the average weight convergence curves for GFRP, CFRP, and steel using the CSSPO algorithm for a 72-member truss.

The size variables, optimal weight, mean weight, weight standard deviation (STD), and the number of function evaluations are presented in Table 7. As indicated in this table, the CSSPO was able to achieve the best weight of 1965.5323 kg by conducting a lower number of analyses with CFRP, and the corresponding SD was 0.7860. The GFRP material secured second place, with an optimal response of 5939.8775 kg, and the related SD was 4.2971 using the CSSPO algorithm. These findings suggest that the CSSPO has a lower computational cost while maintaining high accuracy for composite materials. In addition, Table 8 displays the outcomes of the natural frequencies. All the algorithms for different materials successfully adhered to the constraints without any violations, thereby satisfying the specified requirements.

Table 7. Optimized results of GFRP, CFRP, and steel using SPO and CSSPO for 120-member truss.

Materials	GFRP		CFRP		STEEL	
	SPO	CSSPO	SPO	CSSPO	SPO	CSSPO
No. Group						
1	79.2113	80.0669	24.3782	24.5554	20.9089	19.8347
2	129.2908	129.3000	47.8216	46.4722	39.1228	42.1216
3	39.9363	38.0518	10.7601	11.3803	11.4432	11.4296
4	75.7910	75.1591	20.9776	21.0117	21.0978	21.6645
5	34.4651	33.3149	9.1935	9.3981	11.0651	10.0670
6	40.1374	41.8914	13.3115	12.3117	10.6454	12.9819
7	47.0609	47.8410	11.8182	11.9763	19.7014	15.2824
Best weight (kg)	5943.8442	5939.8775	1968.0971	1965.5323	9245.8842	8885.6721
Average weight (kg)	6749.4283	5942.1393	2169.862	1966.1123	10,457.864	8889.385
Standard deviation	719.3279	4.2971	279.4734	0.7860	1500.93	3.13777
No. Analyses	4400	4150	4850	4550	4100	4400

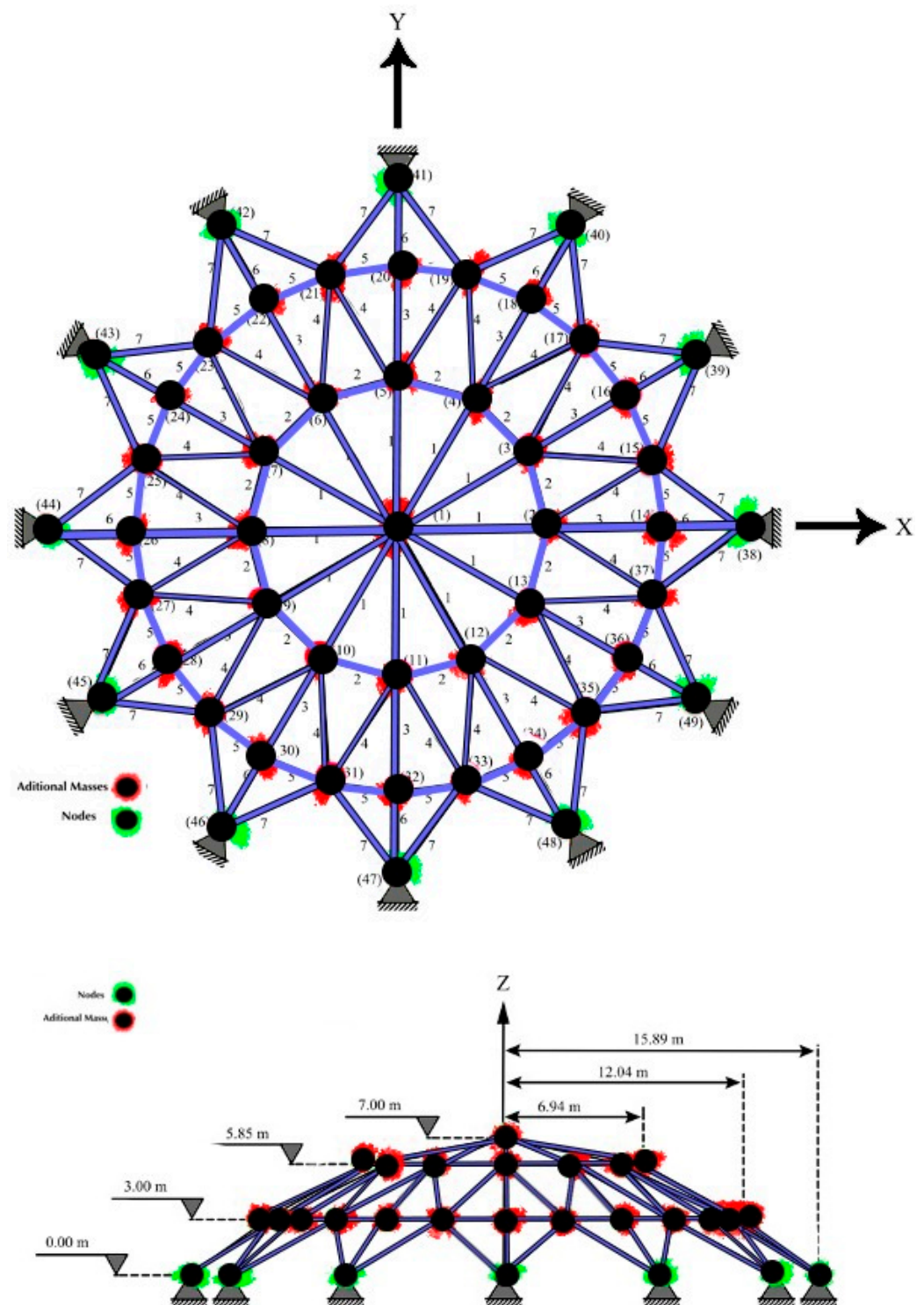


Figure 20. The 120-member dome truss structure.

Figure 21 displays the best weight convergence curves of the SPO and CSSPO using GFRP, CFRP, and steel for a 120-member truss. The evidence presented in the figure unequivocally demonstrates the superior performance of CSSPO in comparison to SPO. Figure 22 compares the best convergence curves for CFRP, GFRP, and steel. The figure shows that CFRP achieved a feasible solution and ranked first among all the materials studied in terms of weight. Additionally, using CSSPO with CFRP resulted in the lowest average weight among all the materials reviewed (refer to Figure 23). Based on the findings depicted in this figure, it is evident that CSSPO surpassed all other materials in terms of

performance. According to Figure 24, among all its competitors, CFRP obtained the best average weight of 1966.1123 kg and was ranked first.

Table 8. Natural frequencies (Hz) for the best design of a 120-member truss.

Materials	CFRP		GFRP		STEEL	
No. Frequency	SPO	CSSPO	SPO	CSSPO	SPO	CSSPO
f_1	9.0000	9.0000	9.0000	9.0000	9.0000	9.0000
f_2	11.0000	11.0000	11.0000	11.0000	11.0000	11.0000
f_3	11.0052	11.0000	11.0000	11.0000	11.0603	11.0000
f_4	11.0075	11.0075	11.0033	11.0032	11.0890	11.0096
f_5	11.0524	11.0522	11.0530	11.0535	11.1581	11.0494

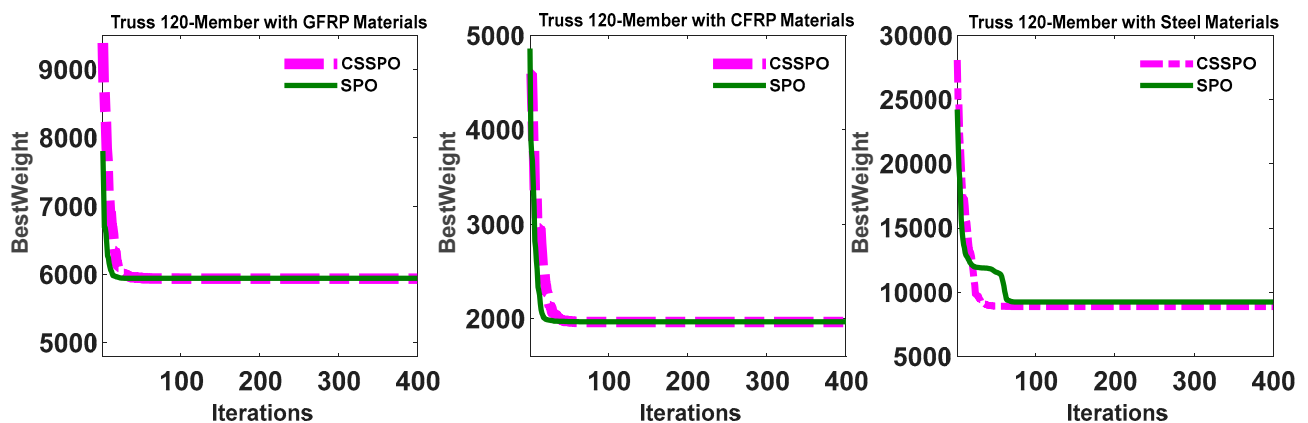


Figure 21. Best weight convergence curves for SPO and CSSPO with GFRP, CFRP, and steel for a 120-member truss.

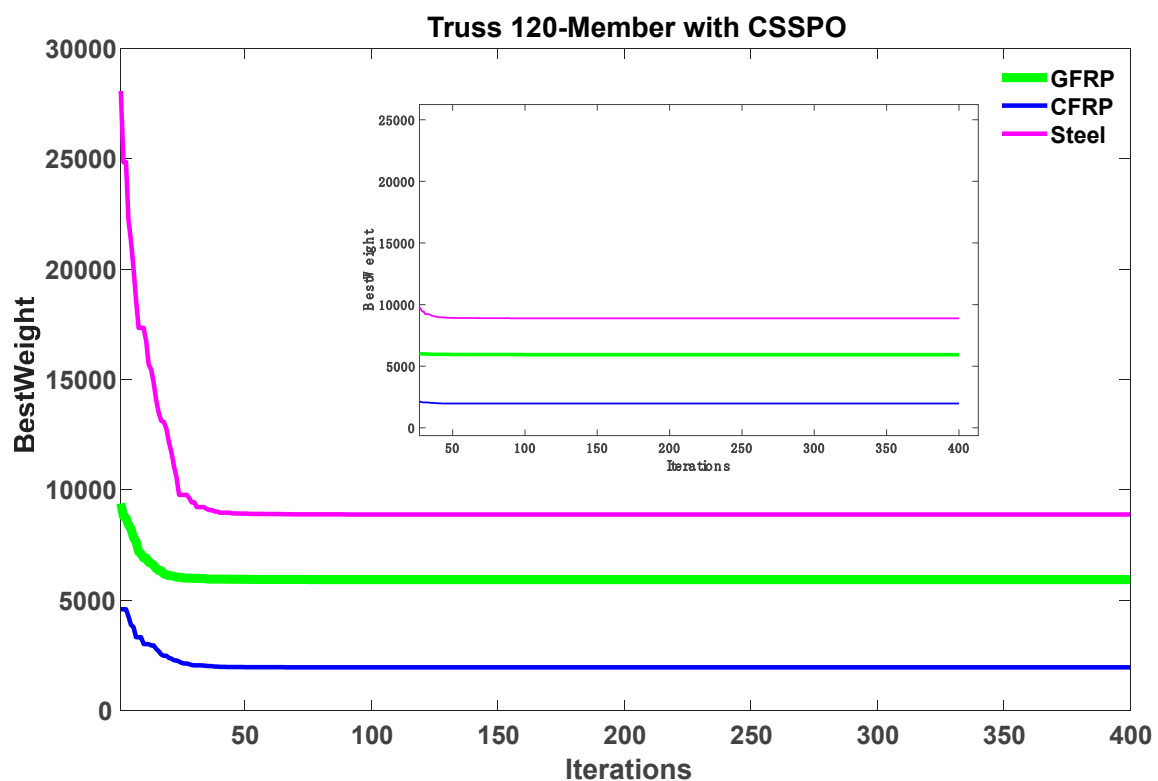


Figure 22. Comparison of the best weight convergence curves for GFRP, CFRP, and steel with the CSSPO algorithm for 120-member truss.

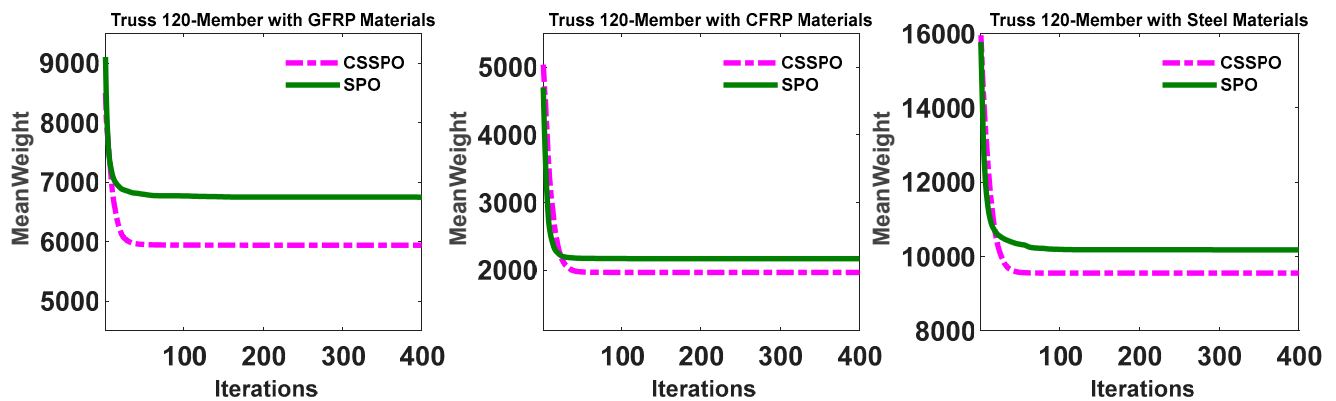


Figure 23. Average weight convergence curves for SPO and CSSPO with GFRP, CFRP, and steel for a 120-member truss.

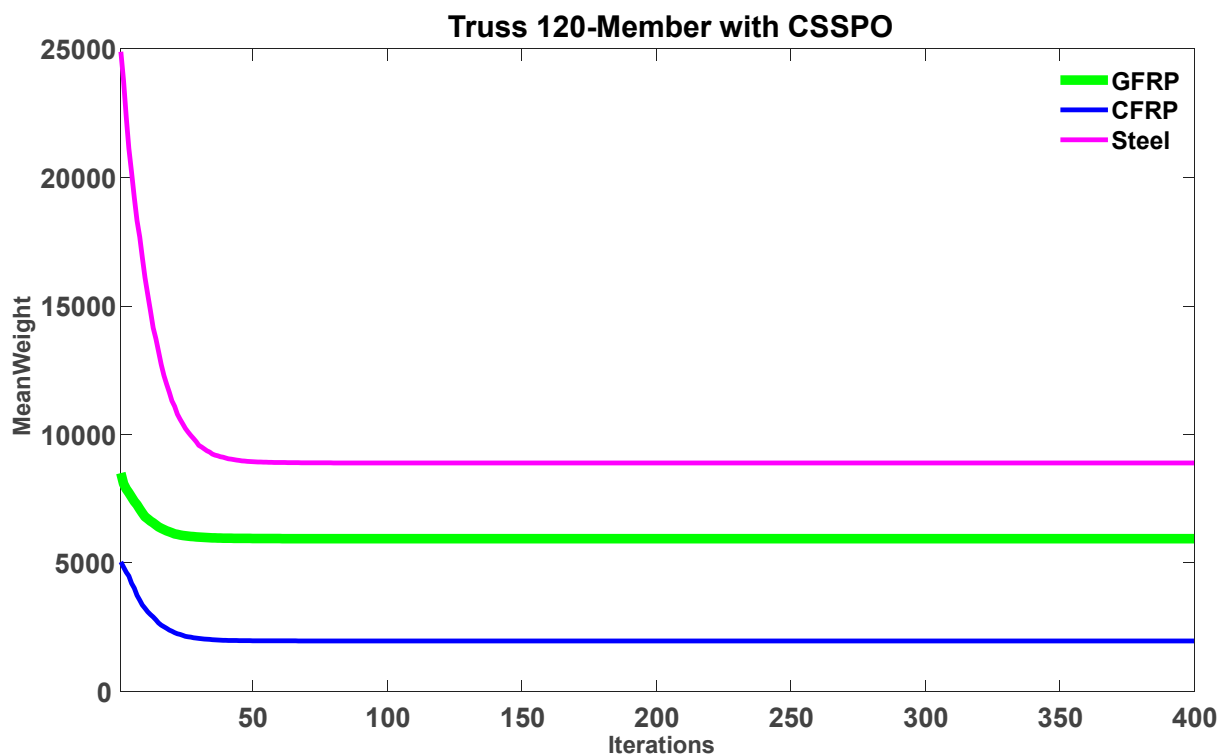


Figure 24. Comparison of average weight convergence curves for GFRP, CFRP, and steel using the CSSPO algorithm for a 120-member truss.

The CSSPO approach was found to be more effective than the standard version of the SPO, achieving the lowest weight for all the materials. This indicates that the new approach is an optimal design enhancement that utilizes the existing algorithm. Moreover, according to Table 8, this approach continues to meet the frequency constraints. The diagram depicted in Figure 25 illustrates 30 distinct runs of the ultimate weights for both the SPO and CSSPO. This diagram illustrates the lowest result achieved, represented by the blue line, while the red line represents the mean of all 30 runs. In reference to this figure, there is a notable proximity between the best and mean lines for most of the results. This indicates that the utilization of CFRP in combination with the CSSPO yields significantly superior outcomes compared to other materials.

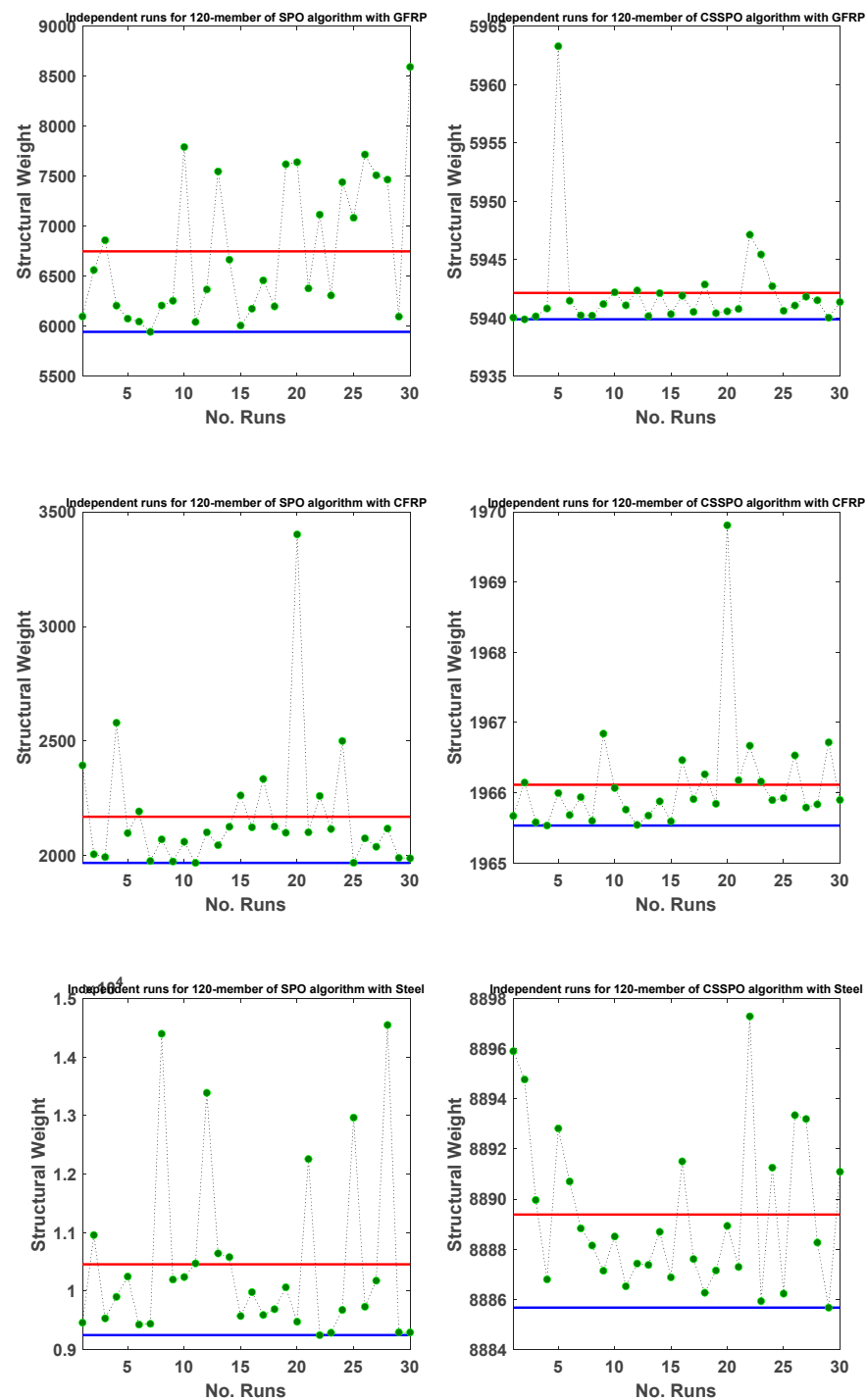


Figure 25. Weights of 30 distinct runs for the SPO and CSSPO for a 120-member truss with different materials.

5.4. A 200-Member Planar Truss

This section addresses the fourth test problem, which involves minimizing the weight of a planar structure consisting of 200-member planar truss, as shown in Figure 26. The problem encompasses 29 sizing variables that pertain to the cross-sectional areas of the element groups, as outlined in Table 9. The frequency constraints are set to $\omega_1 \geq 5$ Hz, $\omega_2 \geq 10$ Hz, $\omega_3 \geq 15$ Hz. Non-structural masses of 100 kg are attached to the truss's upper nodes (1–5). Table 10 presents the optimizing design of the mentioned structure with three different materials, showing that CFRP with fewer function number evaluations yielded the lightest weight of 483.5991 kg with the CSSPO. The best results of CFRP with the CSSPO

algorithm were lighter than the other materials. This demonstrates the effectiveness of the hybrid method with composite material over the other algorithms and materials studied in this test problem.

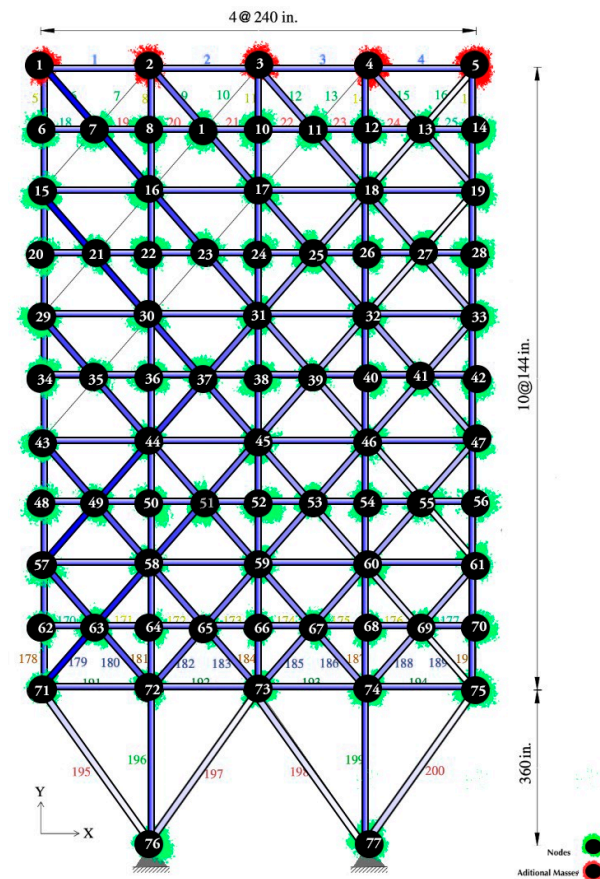


Figure 26. The 200-member planar truss structure.

Table 9. Member numbers for each group.

Group	Member Number	Group	Member Number
1	1,2,3,4	16	82,83,85,88,89,91,92,103,104,106,107,109,110,112,113
2	5,8,11,14,17	17	115,116,117,118
3	19,20,21,22,23,24	18	119,122,125,128,131
4	18,25,56,63,94,101,132,139,170,177	19	133,134,135,136,137,138
5	26,29,32,35,38	20	140,143,146,149,152
6	6,7,9,10,12,13,15,16,27,28,30,31,33,34,36,37	21	120,121,123,124,126,127,129,130,141,142,144,145,147,148,150,151
7	39,40,41,42	22	153,154,155,156
8	43,46,49,52,55	23	157,160,163,166,169
9	57,58,59,60,61,62	24	171,172,173,174,175,176
10	64,67,70,73,76	25	178,181,184,187,190
11	44,45,47,48,50,51,53,54,65,66,68,69,71,72,74,75	26	158,159,161,162,164,165,167,168,179,180,182,183,185,186,188,189
12	77,78,79,80	27	191,192,193,194
13	81,84,87,90,93	28	195,197,198,200
14	95,96,97,98,99,100	29	196,199
15	102,105,108,111,114		

Table 10. Optimized results of GFRP, CFRP, and steel using the SPO and CSSPO for a 200-member truss.

Materials		GFRP		CFRP		STEEL	
Member Group		SPO	CSSPO	SPO	CSSPO	SPO	CSSPO
1		2.4229	2.5728	4.9125	0.7093	1.2342	0.5002
2		2.3958	2.1358	0.1000	0.8604	0.1000	0.4979
3		0.1000	0.1000	6.5239	0.1016	0.1369	0.1019
4		0.2973	0.1912	0.1000	0.1000	0.1055	0.1003
5		2.2152	1.9297	0.1923	0.8845	0.2325	0.4506
6		3.9470	4.0269	2.3523	1.4840	2.1007	0.8848
7		0.1000	0.3803	1.9255	0.1024	7.3151	0.1000
8		5.7238	6.2060	0.9830	2.1670	1.0079	1.4102
9		2.2937	0.1000	0.1000	0.1008	12.9035	0.1000
10		7.0010	7.1127	0.7830	2.3657	0.3016	1.5747
11		6.2874	5.0863	2.1217	1.6194	1.9754	1.1112
12		0.6026	0.7847	4.6294	0.1198	0.1000	0.1381
13		12.0973	13.7674	1.4760	3.9790	3.1709	2.9040
14		0.1811	0.1875	0.1000	0.1019	10.6532	0.1008
15		12.8618	15.9121	6.7499	4.0400	3.7011	3.1706
16		7.7501	7.6639	1.8909	1.8853	2.8960	1.5698
17		0.9657	1.9940	5.9667	0.2114	0.1000	0.2814
18		30.0000	26.7505	3.5944	5.6836	6.9783	5.0985
19		30.0000	0.3966	0.2184	0.1149	0.1013	0.1073
20		30.0000	30.0000	4.4254	5.6443	10.8546	5.2830
21		12.2261	12.2957	1.7639	2.0817	3.4605	2.0484
22		30.0000	13.6074	0.7094	0.6481	0.1130	0.4935
23		30.0000	30.0000	13.7444	7.9415	12.5323	7.7323
24		30.0000	21.3507	1.9093	0.1193	2.1160	0.2046
25		29.9999	30.0000	7.8694	7.6309	13.7618	8.1349
26		29.9970	30.0000	1.0521	2.4493	3.0577	2.6627
27		30.0000	30.0000	15.5103	9.1655	10.8998	10.2624
28		29.9985	30.0000	25.3566	18.5299	27.1305	21.3333
29		30.0000	30.0000	29.6547	10.3016	26.2179	10.2026
Best weight (kg)		6245.0062	5645.5521	713.0536	483.5991	3632.2153	2136.1284
Average weight (kg)		10,483.24	5646.58	945.4095	486.1037	6300.8391	2153.1362
Standard deviation		2068.484	2.971819	131.2423	7.5141	1273.747	36.1414
No. Analyses		13,150	6300	15,050	6700	7250	7150

Table 11 demonstrates the natural frequencies of the best SPO and CSSPO methods designed with CFRP, GFRP, and steel materials. Each algorithm conscientiously complies with the constraints, ensuring a complete absence of violations and effectively meeting the prescribed criteria. According to the findings, the CSSPO with CFRP algorithm was able to generate the best possible answer, with an optimal weight of 483.5991 kg and SD = 7.5441. This specific instance created a significant challenge for metaheuristic techniques, primarily due to the significant number of variables. Several metaheuristics were found to be ineffective in resolving this issue. However, the CSSPO algorithm demonstrated satisfactory outcomes in contrast to the alternative approaches.

Figure 27 shows the best convergence curves for both methods with CFRP, GFRP, and steel materials. In reference to this figure, the SPO and CSSPO algorithms reached the optimal point, but the CSSPO had a faster convergence rate than the SPO. Figure 28 shows the best convergence curves for the hybrid version of SPO for CFRP, GFRP, and steel materials. The evidence presented in this figure highlights the substantial superiority of the CSSPO and CFRP combination solution over other materials.

Table 11. Natural frequencies (Hz) for the best design of a 200-member truss.

Materials	GFRP		CFRP		STEEL	
No. Frequency	SPO	CSSPO	SPO	CSSPO	SPO	CSSPO
f_1	5.0038	5.0057	5.0000	5.0000	5.0000	5.0000
f_2	14.3882	14.9355	14.8533	16.0865	14.7750	13.0865
f_3	15.0000	16.0203	19.1823	16.2436	19.0460	15.0000
f_4	19.1034	18.9980	19.5299	25.2140	19.5141	20.0789
f_5	22.7452	22.2454	25.9642	32.3189	25.8055	22.0192
f_6	25.3107	23.9112	26.4719	36.9720	26.2873	25.4215

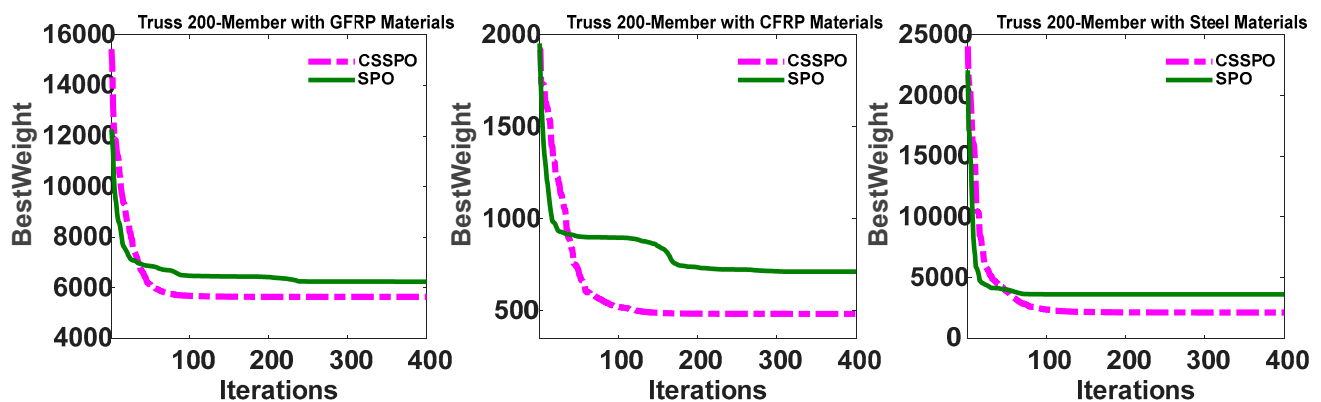
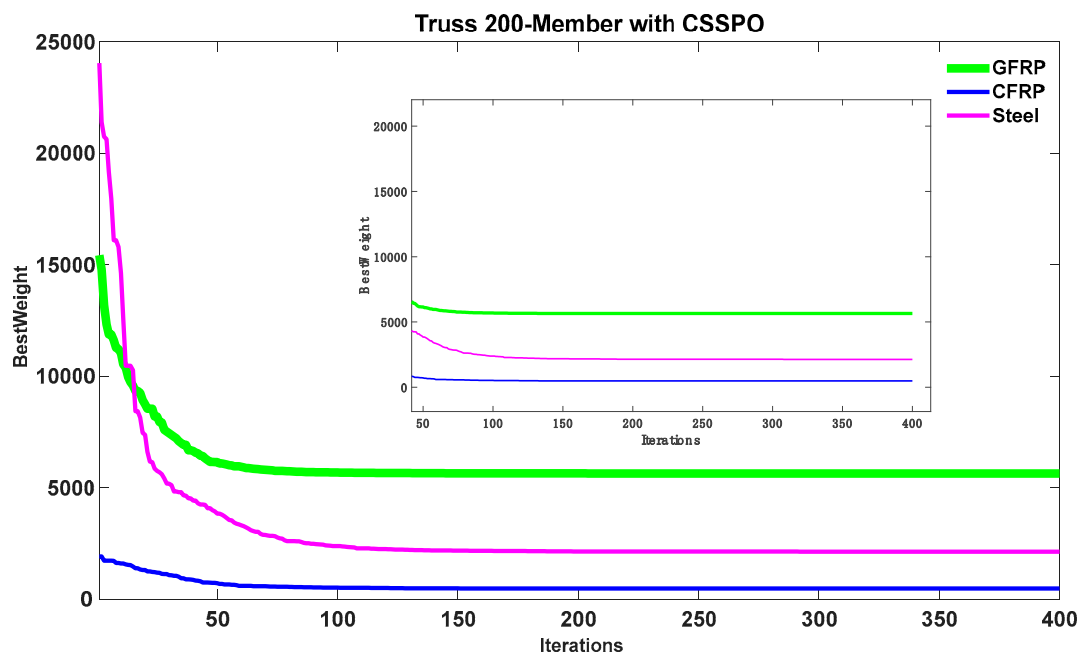
**Figure 27.** Best weight convergence curves for the SPO and CSSPO with GFRP, CFRP, and steel for a 200-member truss.**Figure 28.** Comparison of best weight convergence curves for GFRP, CFRP, and steel using the CSSPO algorithm for a 200-member truss.

Figure 29 illustrates that the average weight of the CSSPO using the CFRP algorithm was lower than that of other materials, providing evidence of the superior performance of the CSSPO algorithm. Moreover, CFRP was ranked first among all competitors, with the best average weight of 486.1037 kg, as depicted in Figure 30. In this figure, steel claimed the second position in the rankings, while GFRP achieved last place. Figure 31 presents the

final weight for this investigation, which was derived from 30 separate runs of the SPO and CSSPO. In this figure, the blue line represents the minimum achievable result, while the red line represents the average of all 30 runs. In general, these findings show that the CSSPO algorithm with CFRP performed better than the other algorithms that were examined, both in terms of its overall performance and its accuracy.

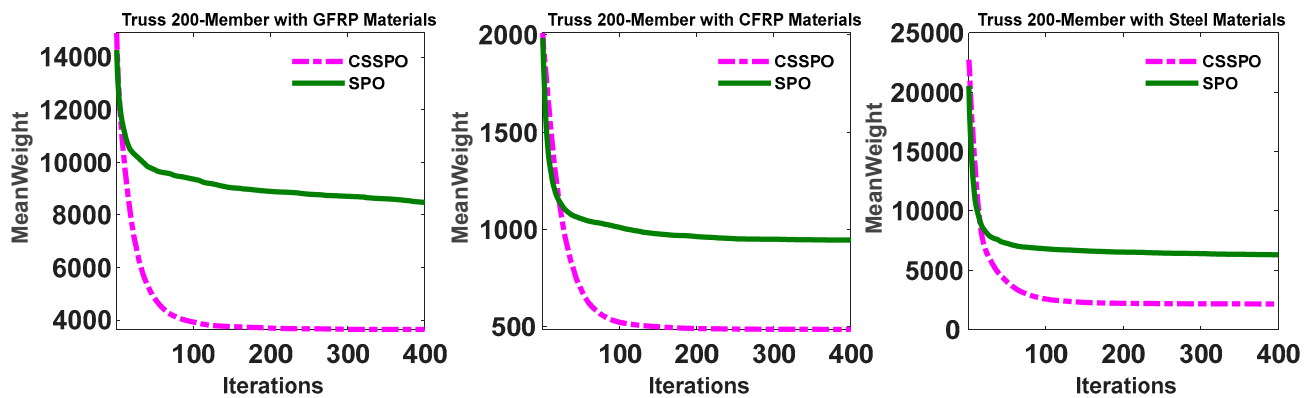


Figure 29. Average weight convergence curves for the SPO and CSSPO with GFRP, CFRP, and steel for a 200-member truss.

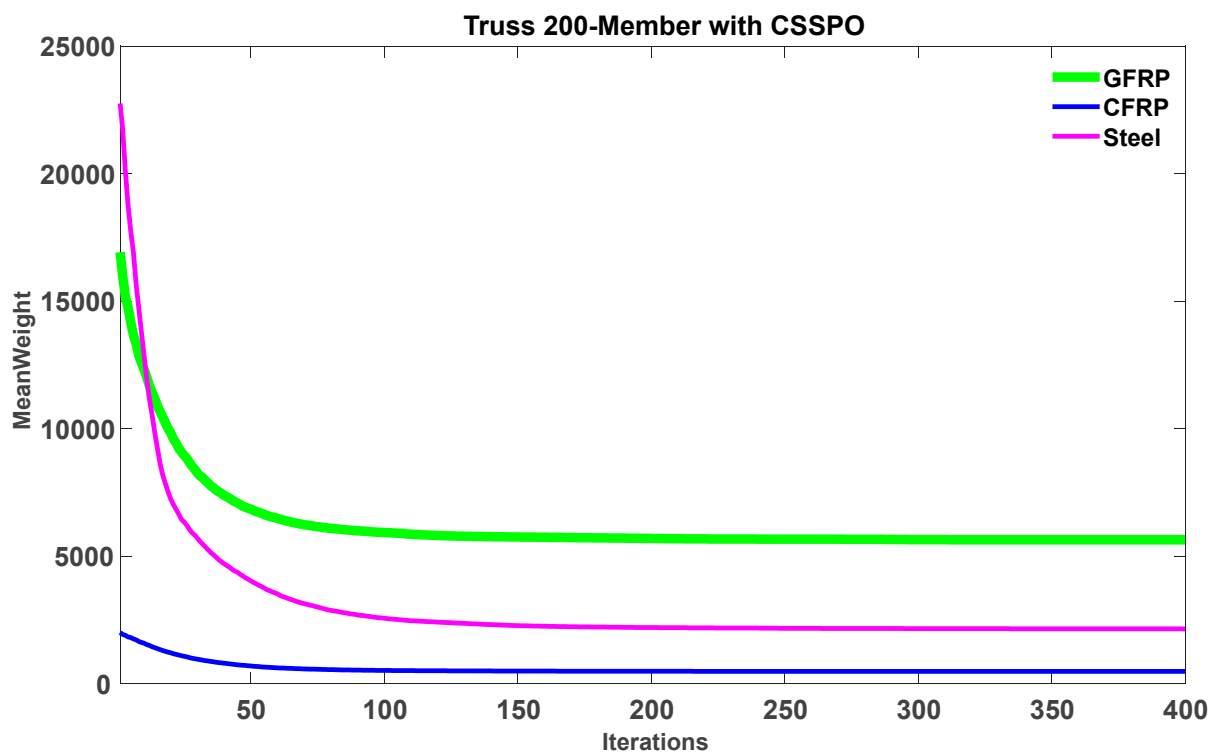


Figure 30. Comparison of the average weight convergence curves for GFRP, CFRP, and steel using the CSSPO algorithm for 200-member truss.

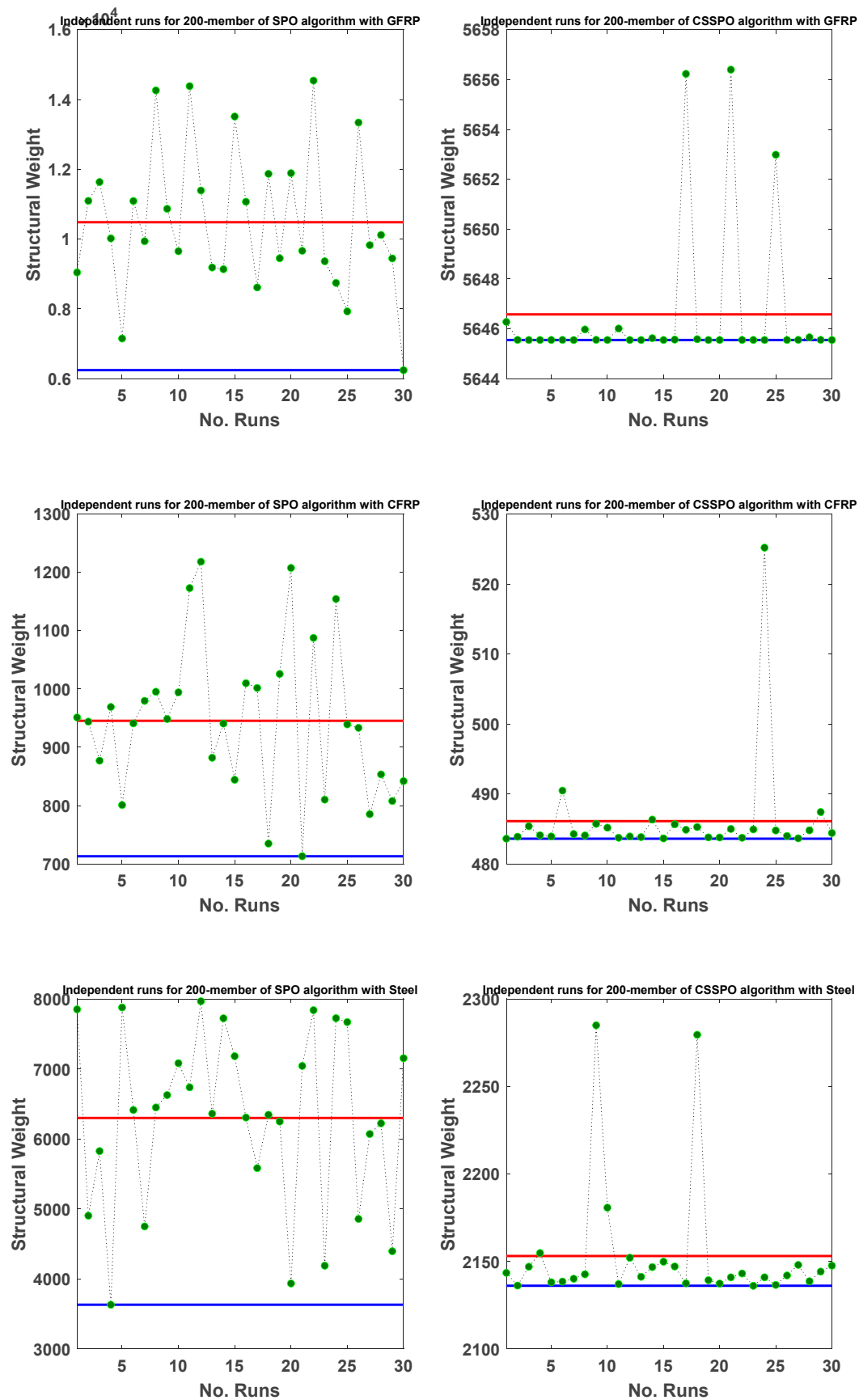


Figure 31. Weights of 30 distinct runs for the SPO and CSSPO for a 200-member truss with different materials.

6. Statistical Analysis

To determine if there is a statistically significant difference between the population means of two samples, a *t*-test can be used. The *t*-test is a useful tool assessing the similarity of two samples by evaluating their statistical significance. In this study, a paired *t*-test was employed to perform a statistical comparison. If the calculated *p*-value exceeds 0.05, it indicates a lack of statistically significant differences between the outcomes of the two algorithms being compared. Conversely, a *p*-value below 0.05 suggests the presence of statistically significant variations in the performance of the two algorithms.

The resulting *p*-values are displayed in Table 12. Based on this table, all *p*-values obtained from the examples were less than 0.05, indicating statistically significant differences in the performance of the two algorithms. Furthermore, Figure 32 presents a QQ plot, commonly referred to as a quantile–quantile plot, which is a visual tool employed to compare two probability distributions by plotting their quantiles against each other. The blue circles are two sets of quantiles against one another in the QQ plot. The QQ plot displays the quantiles of the SPO dataset (results from 30 runs) on the *x*-axis and the quantiles of the CSSPO dataset on the *y*-axis. If the datasets are derived from a standard distribution, the data points on the graph should be aligned along a 45-degree line. Any deviations observed from this line suggest that the datasets have been obtained from distinct distributions.

Table 12. The *p*-values obtained using *t*-tests for all examples.

Examples	Algorithms	GFRP	STEEL	CFRP
37-Member truss	SPO vs. CSSPO	4.37×10^{-9}	1.85×10^{-7}	1.06×10^{-8}
73-Member truss	SPO vs. CSSPO	1.08×10^{-13}	2.07×10^{-14}	4.38×10^{-16}
120-Member truss	SPO vs. CSSPO	7.79×10^{-8}	1.86×10^{-4}	3.87×10^{-7}
200-Member truss	SPO vs. CSSPO	1.50×10^{-18}	9.73×10^{-27}	3.29×10^{-25}

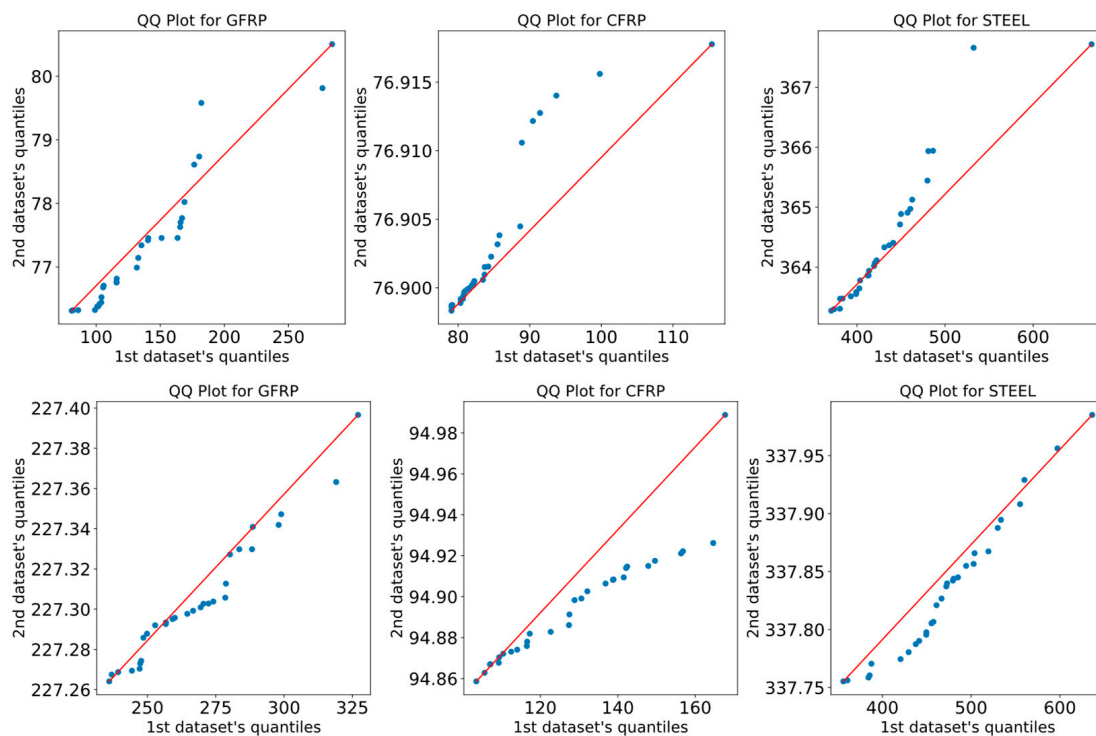


Figure 32. Cont.

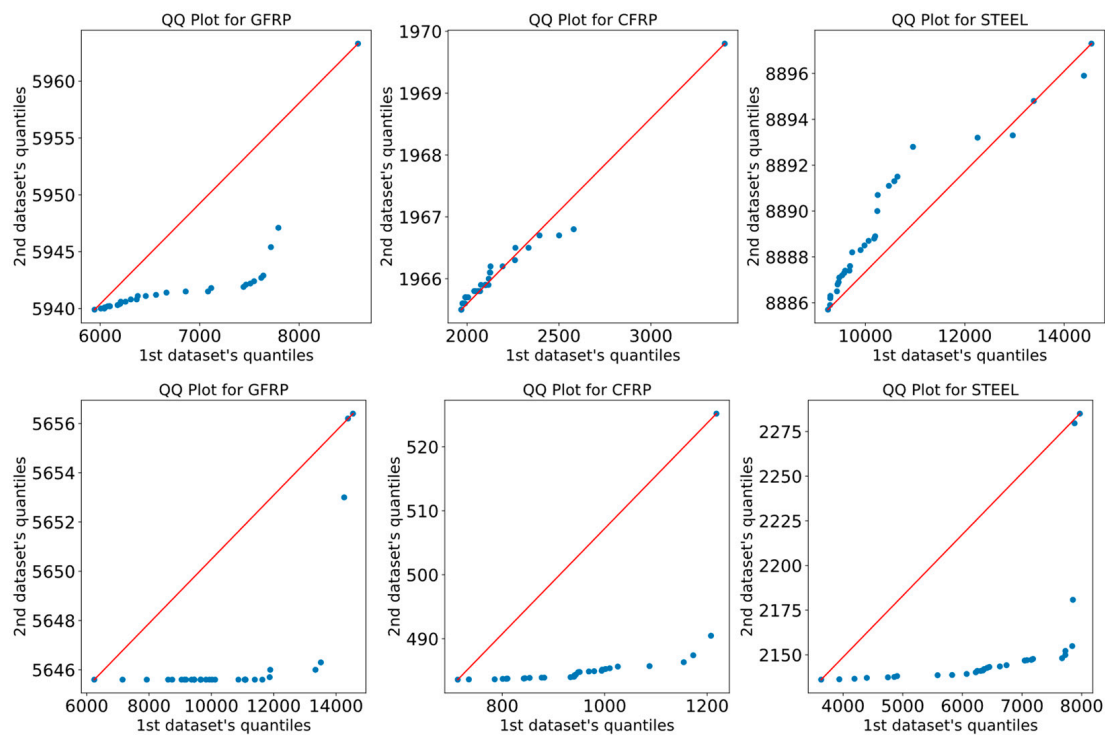


Figure 32. QQ plots for all examples of GFRP, CFRP, and steel materials.

The boxplot illustrates the distribution of data and identifies any outliers. Generating multiple boxplots on a single graph is valuable for comparing distinct datasets. The boxplot for each truss optimization is shown in Figure 33. In reference to this figure, the boxplot for the CSSPO shows the best performance compared to the SPO for all examples. In this figure, there are fewer outliers for the CSSPO. Overall, the statistical results indicate that the CSSPO performs better than the SPO.

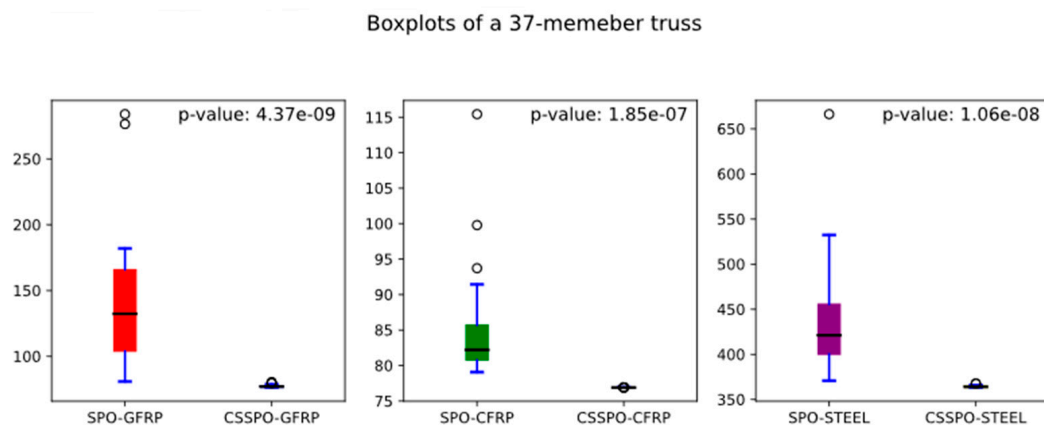


Figure 33. Cont.

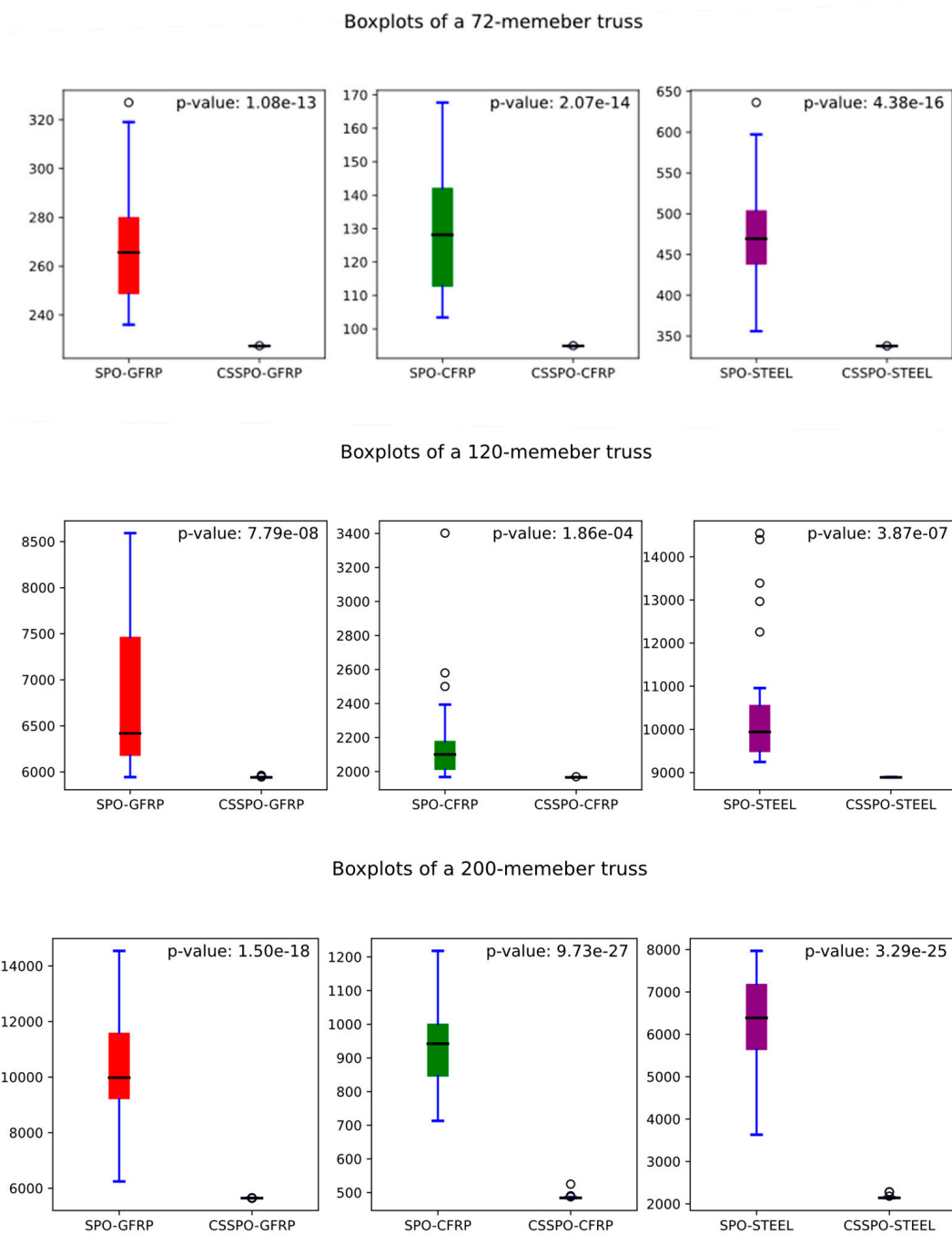


Figure 33. Boxplots of all examples for GFRP, CFRP, and steel materials.

7. Conclusions

A hybrid algorithm that combines the Cuckoo Search (CS) and Stochastic Paint Optimizer (SPO) was applied for the first time to the size optimization of truss structures that use composite materials under frequency constraints. The research conducted an in-depth comparison of truss structures constructed from various materials, including CFRP, GFRP, and steel. The composite material was utilized for the first time to optimize the truss design. The examined design examples demonstrate the effectiveness of the CSSPO algorithm with composite materials in optimizing final solutions, with statistical results showing its competitiveness with new metaheuristics. Additionally, the efficiency, accuracy, and performance of the CSSPO exceed the SPO. However, in larger-scale problems, the rapid convergence of the CSSPO algorithm to an optimal solution may pose challenges.

Additionally, statistical analyses demonstrated that the results of the CSSPO had the lowest standard deviation, indicating a high level of result reliability. The statistical results obtained from 30 independent runs for each material prove the robustness of the CSSPO compared to the SPO. The CSSPO is particularly noteworthy because it does not require parameter tuning. The performance and accuracy of the hybrid version of the SPO exceeded those of the standard version. The performance of the CSSPO was tested on four different truss structures. It was found that truss structures composed of composite materials led to a reduction in weight. This research highlights that using CFRP and GFRP composites in the fabrication of truss structures results in a significant weight decrease compared to the use of steel.

As a future direction, it is recommended to evaluate the performance of this computational approach in addressing optimization problems in other areas of design and engineering through further investigations. Another potential direction for future research would be to compare the performance of recently developed state-of-the-art methods with composite materials to the CSSPO for truss structures. The CSSPO is a versatile method that can be applied to complex engineering problems, including laminated composites, functionally graded structures, and reliability-based design optimization problems. These problems often involve high computational costs, making the CSSPO an attractive option. In addition, a potential area for future research is the application of discrete size optimization using composite materials for truss and frame structures.

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