



Aluminium-26 from Massive Binary Stars. III. Binary Stars up to Core Collapse and Their Impact on the Early Solar System

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Abstract

Many of the short-lived radioactive nuclei that were present in the early solar system can be produced in massive stars. In the first paper in this series, we focused on the production of ^{26}Al in massive binaries. In our second paper, we considered rotating single stars; two more short-lived radioactive nuclei, ^{36}Cl and ^{41}Ca ; and the comparison to the early solar system data. In this work, we update our previous conclusions by further considering the impact of binary interactions. We used the MESA stellar evolution code with an extended nuclear network to compute massive (10–80 M_{\odot}), binary stars at various initial periods and solar metallicity ($Z = 0.014$), up to the onset of core collapse. The early solar system abundances of ^{26}Al and ^{41}Ca can be matched self-consistently by models with initial masses $\geq 25 M_{\odot}$, while models with initial primary masses $\geq 35 M_{\odot}$ can also match ^{36}Cl . Almost none of the models provide positive net yields for ^{19}F , while for ^{22}Ne the net yields are positive from 30 M_{\odot} and higher. This leads to an increase by a factor of approximately 4 in the amount of ^{22}Ne produced by a stellar population of binary stars, relative to single stars. In addition, besides the impact on the stellar yields, our 10 M_{\odot} primary star undergoing Case A mass transfer ends its life as a white dwarf instead of as a core-collapse supernova. This demonstrates that binary interactions can also strongly impact the evolution of stars close to the supernova boundary.

Unified Astronomy Thesaurus concepts: Stellar evolution (1599); Stellar nucleosynthesis (1616); Stellar winds (1636); Binary stars (154); Stellar evolutionary models (2046)

1. Introduction

The presence of radioactive isotopes in the early solar system (ESS) is well established, as their abundances are inferred from meteoritic data showing excesses in their daughter nuclei. In this work, as in the previous works in this series of papers, the main focus is on ^{26}Al , a short-lived radioactive isotope (SLR) with a half-life of 0.72 Myr (Basunia & Hurst 2016). We also consider ^{36}Cl and ^{41}Ca , with half-lives of 0.301 Myr (Nica et al. 2012) and 0.0994 Myr (Nesaraja & McCutchan 2016), respectively. These three radioactive isotopes represent the fingerprint of the local nucleosynthesis that occurred nearby at the time and place of the birth of the Sun. Therefore, they give us clues about the environment and the circumstances of such birth (Adams 2010; Lugaro et al. 2018).

Massive-star winds have been suggested as a favored site not only of the origin of the ^{26}Al in the ESS (see, e.g., Arnould et al. 1997, 2006; Gounelle & Meynet 2012; Gaidos et al. 2009; Young 2014) but also of ^{36}Cl and ^{41}Ca . This is because these three isotopes can be synthesized in massive stars and expelled both by their winds and/or as a result of binary

interactions (Braun & Langer 1995; Brinkman et al. 2019, 2021) and, in equal or larger amounts, by their final core-collapse supernova (Meyer & Clayton 2000; Lawson et al. 2022). The ^{26}Al present in the stellar winds is produced by proton captures on ^{25}Mg during hydrogen burning. The majority of the ^{26}Al is expelled together with ^{36}Cl and ^{41}Ca , which are produced instead during helium burning by neutron captures on the stable isotopes, ^{35}Cl and ^{40}Ca , respectively.

In Brinkman et al. (2019, hereafter Paper I), we investigated the impact of *binary interactions* on the yields of ^{26}Al from the primary star (i.e., the initially most massive star) of a binary system. We found, in agreement with Braun & Langer (1995), that for initial primary masses up to ~ 40 – $45 M_{\odot}$ binary interactions can significantly increase the yields of ^{26}Al , especially for the lowest masses, 10–25 M_{\odot} . For these systems, the increase can be as high as a factor of ~ 150 at 10 M_{\odot} and a factor ~ 5 at 25 M_{\odot} . Above 40–45 M_{\odot} , the binary interactions do not have an impact on the yield, due to the strong mass loss through winds of these stars, which is comparable to the mass lost as a result of binary interactions. In this first paper, however, we did not consider ^{36}Cl and ^{41}Ca .

In Brinkman et al. (2021, hereafter Paper II), we investigated the yields of the SLRs ^{26}Al , ^{36}Cl , and ^{41}Ca for *single massive stars*, both rotating and nonrotating, and the impact of these yields on the ESS. We found that stars with initial masses of 40–45 M_{\odot} , depending on their initial rotational velocity, can explain the presence of ^{26}Al and ^{41}Ca in the ESS, but only stars

⁸ NuGrid Collaboration, <http://nugridstars.org>.



with initial masses of $60 M_{\odot}$ and higher can also explain the presence of ^{36}Cl .

In this paper, we explore the effect of the removal of the hydrogen-rich envelope due to binary interactions on the yields of isotopes produced in later burning stages, primarily helium burning. As mentioned above for ^{26}Al , the impact of binarity is negligible above $\sim 40\text{--}45 M_{\odot}$. It is, however, not clear yet whether for ^{36}Cl and ^{41}Ca the binary interactions might have an impact for higher masses than this limit, since these two isotopes are produced in a later stage of the evolution than ^{26}Al . We thus consider several binary configurations in the mass interval $10\text{--}60 M_{\odot}$ for the primary stars, since for these systems the impact of binary interactions is most prominent, based on the results of Paper I. We also consider one binary model for primary stars of 70 and $80 M_{\odot}$.

As in Paper II, we consider the stable isotopes ^{19}F and ^{22}Ne to establish the impact of the binary interactions on their yields. Meynet & Arnould (2000) have shown that Wolf–Rayet (W-R) stars can contribute significantly to the galactic ^{19}F abundance, while Palacios et al. (2005) found that W-R stars are unlikely to be the source of galactic ^{19}F , when including updated mass-loss prescriptions and reaction rates. In Paper II, we found that only the most massive stars in our sample produce positive net yields of ^{19}F . Binary interactions might increase the range for which positive net yields are found. As for ^{22}Ne , there are puzzling observations of an anomalous $^{22}\text{Ne}/^{20}\text{Ne}$ ratio in cosmic rays, a factor of ~ 5 higher than in the solar wind (Prantzos 2012). Comparing models and observations might be a key for finding the source of these cosmic rays, in relation to massive stars and binary systems, as has been done for single stars by Tatischeff et al. (2021).

The structure of this paper is as follows. In Section 2, we briefly describe the method and the important input parameters for our models. In Section 3, we show the results of the stellar evolution of our models and make a comparison between the models of Paper II and representative systems of Case A and Case B mass transfer, where Case A mass transfer occurs during the main-sequence evolution, while Case B mass transfer occurs during the time between core hydrogen and helium burning. In Section 4, we discuss the stellar yields and again compare the models of Paper II to representative systems of the binary interactions. In Section 5, we discuss our results, put them into the context of the ESS, and consider the composition of the winds of the models that could represent the ESS. We end our paper with conclusions in Section 6.

2. Method and Input Physics

As in Papers I and II, we have used version 10398 of the MESA stellar evolution code (Paxton et al. 2011, 2013, 2015, 2018) to calculate massive-star models, both single and in a binary configuration. We have included an extended nuclear network of 209 isotopes within MESA such that the stellar evolution and the detailed nucleosynthesis are solved simultaneously. Below we briefly describe the input physics for the single massive stars and the input parameters for the binary systems. Only the key input parameters and the changes compared to the input physics of Papers I and II are discussed. The inlist files used for the simulations are available on Zenodo under a Creative Commons 4.0 license: doi:10.5281/zenodo.7956527.

The physical input parameters for the stellar models presented here are the same as those for Paper II. The initial masses of our primary models are 10, 15, 20, 25, 30, 35, 40, 45,

50, 60, 70, and $80 M_{\odot}$. The initial composition used is solar with $Z = 0.014$, following Asplund et al. (2009). For the initial helium content we have used $Y = 0.28$. Our nuclear network contains all the relevant isotopes for the main burning cycles (H, He, C, Ne, O, and Si) to follow the evolution of the star in detail up to core collapse. All relevant isotopes connected to the production and destruction of ^{26}Al , ^{36}Cl , ^{41}Ca , ^{19}F , ^{22}Ne , and ^{60}Fe are also included in our network. Including the ground and isomeric states of ^{26}Al , the total nuclear network therefore contains 209 isotopes (see Paper II). Following Farmer et al. (2016, and references therein), a nuclear network of 204 isotopes is optimal for the full evolution of a star, especially because it includes isotopes that influence the electron fraction, Y_e , which is important for the core collapse (see Heger et al. 2000).

As in the two previous papers, we have used the Ledoux criterion to establish the location of the convective boundaries. The semiconvection parameter, α_{sc} , was set to 0.1, and the mixing-length parameter, α_{mlt} , was set to 1.5. We make use of overshooting via the “step-overshoot” scheme with $\alpha_{\text{ov}} = 0.2$ for the central burning stages. We do not use overshoot on the helium-burning shell and the later burning shells. The overshoot on the hydrogen shell was set to $\alpha_{\text{ov}} = 0.1$.

The mass-loss scheme is the same as in Paper II. For the hot phase ($T_{\text{eff}} \geq 11,000$ K) we use the prescription given by Vink et al. (2000, 2001), and for the cold phase ($T_{\text{eff}} \leq 10,000$ K) we use Nieuwenhuijzen & de Jager (1990). For the W-R phase we use Nugis & Lamers (2000). All phases of the wind have a metallicity dependence $\dot{M} \propto Z^{0.85}$ following Vink et al. (2000) and Vink & de Koter (2005).

We have evolved the stars to the onset of core collapse, using an (iron-)core infall velocity of 300 km s^{-1} as the termination point of our simulation, or until a total number of models of 10^4 , since in some cases the cores of the binary models are too small to form an iron core (see Section 3.2).

The main focus of this work is on the yields from the nonrotating primary star of the binary system. The binary input is the same as in Paper I, where we used a fixed initial mass ratio of $q = \frac{M_2}{M_1} = 0.9$ and fully nonconservative mass transfer. With this choice of mass transfer, the primary will not accrete any of the mass of the secondary, and all the mass is lost from the system. The range of periods is the same as in Paper I and based on the stellar radius of the primary. We have selected periods such that mass transfer first occurs either during hydrogen burning, commonly referred to as Case A mass transfer, or after hydrogen burning but before the central ignition of helium, commonly referred to as Case B mass transfer (Kippenhahn & Weigert 1967). The chosen periods cover the range of orbital sizes where Case A or Case B mass transfer is initiated while the star still has a radiative envelope (between 2 and 100 days). Compared to Paper I, we added a binary system with a primary mass of $10 M_{\odot}$ at a period of 104.6 days, as well as a binary system undergoing Case B mass transfer for both 70 and $80 M_{\odot}$.

We used the same stopping criteria for our primary stars as in Paper II, where we evolved the stellar models to the onset of core collapse, or to 10^4 models. In addition to these two criteria, like in Paper I, we stopped the simulations when reverse mass transfer starts taking place ($R_2 \geq R_{L,2}$, where R_2 is the radius of the secondary star and $R_{L,2}$ is the radius of the Roche lobe of the secondary). At this point, we checked manually whether a common envelope was formed ($R_1 \geq R_{L,1}$

as well), and if so, we terminated the run since the outcome of such systems is uncertain. If the primary was still within its Roche lobe ($R_1 < R_{L,1}$), we split the binary and evolved the primary star further as if it were a single star, up to the onset of core collapse, or to 10^4 models. Because the reverse mass transfer occurs at the timescale of the secondary star, the binaries are uncoupled at different stages in the evolution of the primary. However, this way we kept the binary intact for as long as possible. The uncoupling procedure might overlook some effects of binary interactions, such as further mass loss or mass gain due to future mass transfer phases, which have the potential to change the yields significantly compared to the assumptions used here. However, since we use fully non-conservative mass transfer and no accretion is involved, there is no mass gain in our models, and only extra mass loss due to mass transfer is overlooked. Despite these shortcomings, this procedure is a step closer to producing full binary yields for the isotopes of interest. A similar procedure has been used in recent papers on the effects of binary interactions on carbon yields (Farmer et al. 2021) and the structure of the presupernova of primary stars (Laplace et al. 2021).

2.1. Yield Calculations

In this work our focus is on the presupernova nucleosynthetic yields from the winds and the mass transfer of the binary systems. To calculate these yields, we integrate over time the surface mass fraction multiplied by the mass loss, because the wind mass loss and the mass transfer are not instantaneous processes, though the mass transfer has a shorter timescale than the wind loss. For the stable isotopes, there are two yields to consider, the total yield and the net yield. The total yield is calculated as described above. The net yield is the total yield minus the initial total mass present in the star. For the SLRs the net yield is identical to the total yield because the initial mass present in the stars is zero for these isotopes, and thus no distinction will be made for these yields. Hereafter, the yield will always refer to the total yield, unless otherwise indicated.

We do not make a distinction between the yields ejected by the stellar wind and those ejected by the binary mass transfer because, as shown in Paper I, the main effect of the mass transfer is not to increase the yields directly but to expose the deeper layers of the stars such that the subsequent winds can carry off the isotopes produced in the stellar interior.

3. Stellar Models: Results and Discussion

In this section, we discuss the results of the stellar evolution of the binary models and compare them to the single stars of Paper II, both rotating and nonrotating. Table 1 (see the Appendix) contains the key information about the evolutionary stages of the primary stars, as well as the same information from the single, nonrotating star with the same initial masses presented in Paper II. For the 30, 35, 40, 45, and 60 M_\odot models presented here, the system with the shortest period enters a common-envelope phase. Because the assumed spherical symmetry is broken, we did not compute the outcome of these systems with MESA, as it is beyond the scope of this work. Under certain assumptions, however, it is possible to do such calculations (see, e.g., Marchant et al. 2021). A few other systems did not reach the final stages because of computational issues. In the end, 53 of our 58 models reached a final stage for which we could compute the wind yields.

After comparing the models, we briefly consider the effect of binarity on the final stages of the stars, especially for those stars close to the supernova mass boundary, which is 8–10 M_\odot for single stars (depending on the initial conditions of the star; see, e.g., Doherty et al. 2017), as well as the effect of changing the wind prescription for the two lowest masses considered here.

3.1. The Effects of Binary Interactions and Stellar Rotation

In Figures 1–3, a selection of properties of the stellar models are shown for the single-star models at different initial rotational velocities (from Paper II), as well as for representative binary systems for Case A and Case B mass transfer. For the details on the rotating models, see Paper II.

As a reminder, in Section 3 of Paper II we considered the effects of rotation on the evolution, on the total stellar mass, on the mass loss in the various phases of the evolution, on the mass of the helium core, and on the duration of the hydrogen- and helium-burning phase. We showed there that the main effect of the rotational mixing is to extend the lifetime of hydrogen burning, especially of the models rotating at an initial rotational velocity of 300 km s^{−1}. For helium burning, rotation has the opposite effect and shortens the duration of this burning phase, except for the initially most massive models. This is shown by the blue lines in Figure 1. In addition, the rotating models lose more mass overall than the nonrotating models (see Figure 2), which is due to a combination of the extended lifetimes and the rotational boost on the stellar winds.

In Figures 1 and 2, we not only compare nonrotating models with the rotating models but also consider the effects of Case A and Case B binary mass transfer. For each mass, where possible, we have selected representative binary models, undergoing Case A and Case B mass transfer, indicated by bold-faced periods in Tables 1 and 2. The selected Case A system for 20 M_\odot did not reach core collapse but ended its evolution during silicon burning. The mass loss for this star is complete, and therefore it is still a representative system. For the 70 and 80 M_\odot models, it was not possible to create a system undergoing Case A mass transfer without a common envelope. This is because, with an initial mass ratio of 0.9, the hydrogen-burning lifetimes of the primary and the secondary become more and more similar as the initial mass of the primary star goes up. This means that for the 70 and 80 M_\odot systems the primary and the secondary evolve at such a similar pace that they move off the main sequence at almost the same time, which inhibits creating a Case A mass transfer without a common envelope. For Case B, the period is longer and the orbit is wider, and then the slight time difference in the evolution prevents the common envelope from forming. Thus, for 70 and 80 M_\odot we have only a single Case B system each.

In Figure 1, the durations of core hydrogen and core helium burning are shown, as well as the ratio of the different models as compared to the single, nonrotating model, which we use as a standard. The Case A binary systems have a slightly extended main-sequence phase owing to the shrinking of the hydrogen-burning core during the mass transfer (see also Appendices A and B of Paper I). This extension is comparable to that of the slower rotational velocity (150 km s^{−1}) on the lower-mass end, though for the single stars the lifetime is extended owing to receiving more fuel rather than a shrinking core as for the Case A binaries. For the higher initial masses, the duration of

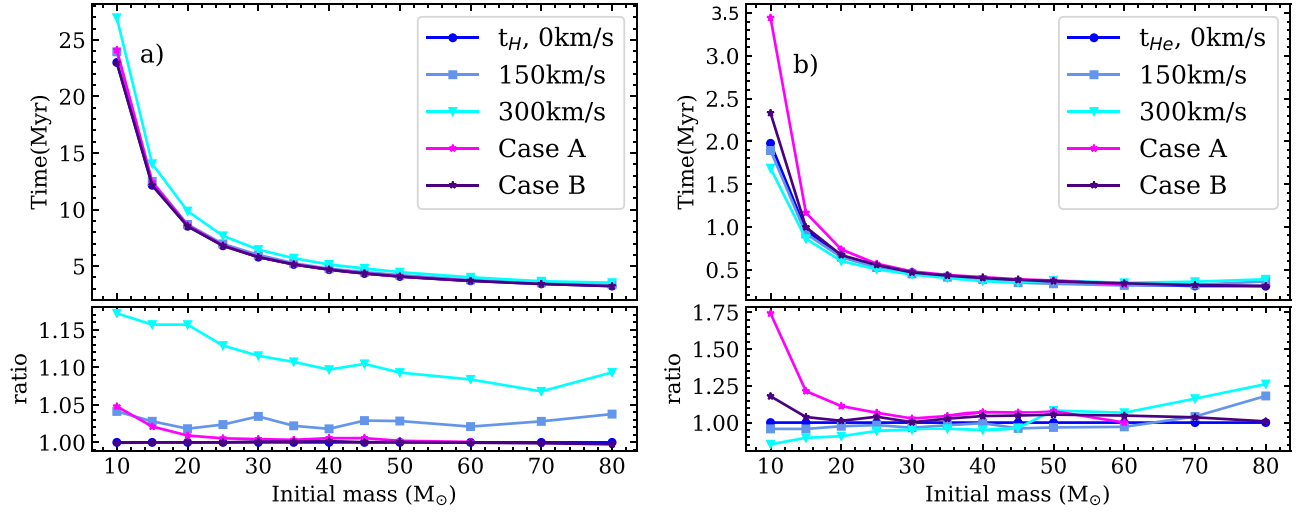


Figure 1. The duration of core hydrogen burning (t_H ; left panel) and core helium burning (t_{He} ; right panel) for rotating and nonrotating single stars, as well as for representative systems of Case A and Case B mass transfer, as a function of the initial stellar (primary) mass. To highlight the differences, the bottom panels show the ratio between the nonrotating single-star model (reference) and the other stars with the same initial mass.

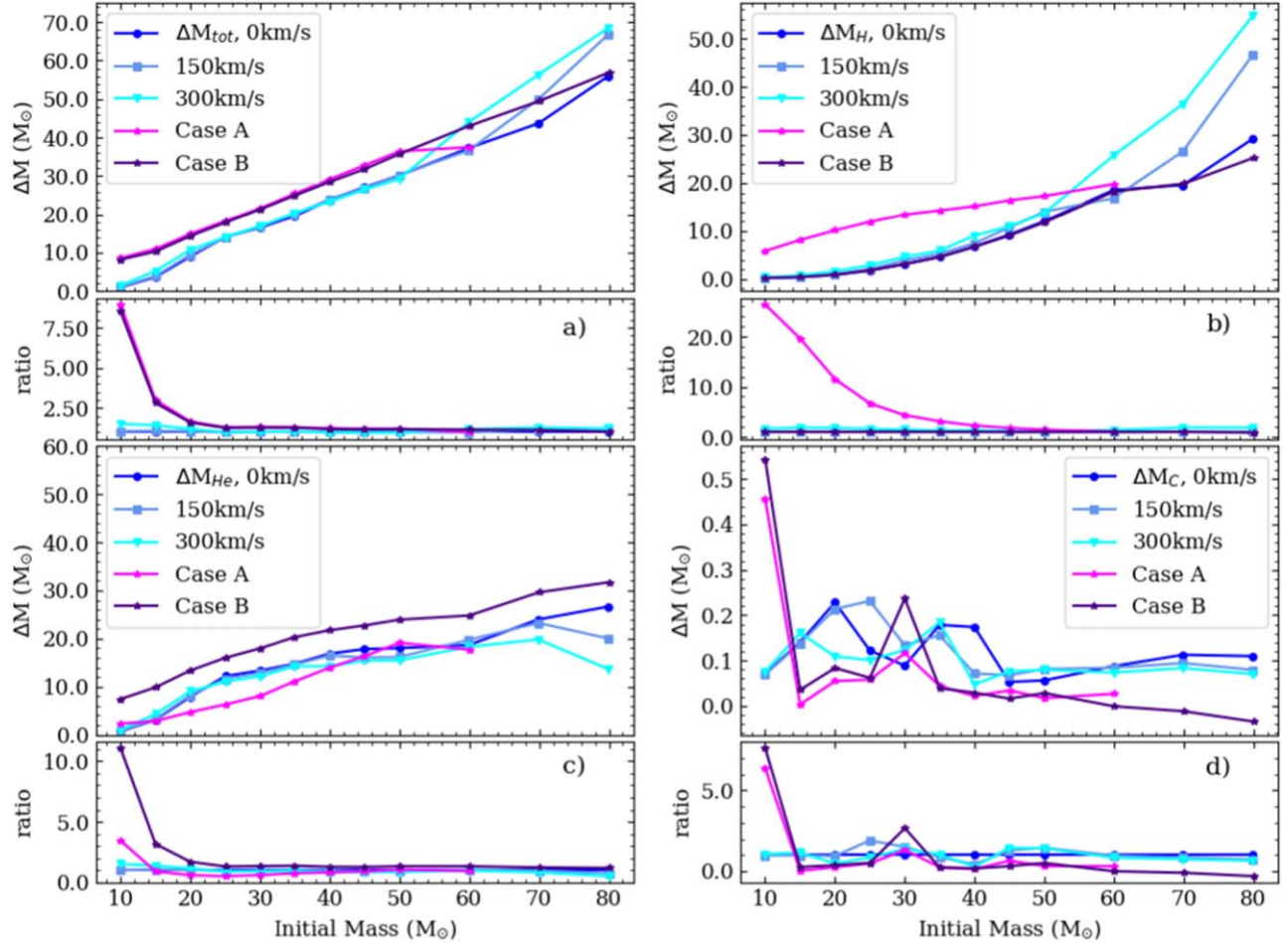


Figure 2. The mass lost in M_\odot from the different models as a function of the initial stellar (primary) mass during the entire evolution of the star ($\Delta M = M_{ini} - M_{*,f}$; panel (a)); during hydrogen burning ($\Delta M_H = M_{ini} - M_{*,H}$; panel (b)); end of hydrogen burning to the end of helium burning ($\Delta M_{He} = M_{*,H} - M_{*,He}$; panel (c)); and the mass loss from the end of helium burning, during carbon burning, and beyond ($\Delta M_C = M_{*,He} - M_{*,f}$; panel (d)). The single stars are indicated by circles, and the representative binary systems are indicated by stars (shown in Table 1). The lower panels show the ratio between the nonrotating single star (reference model) and the other stars with the same initial mass.

hydrogen burning for the Case A systems is very similar to the nonrotating single-star case. The Case B binary systems, as expected, do not differ from the nonrotating single-star case,

since the interaction between the two stars only takes place after the main sequence has already finished, and the star has evolved as if it were single up to this point.

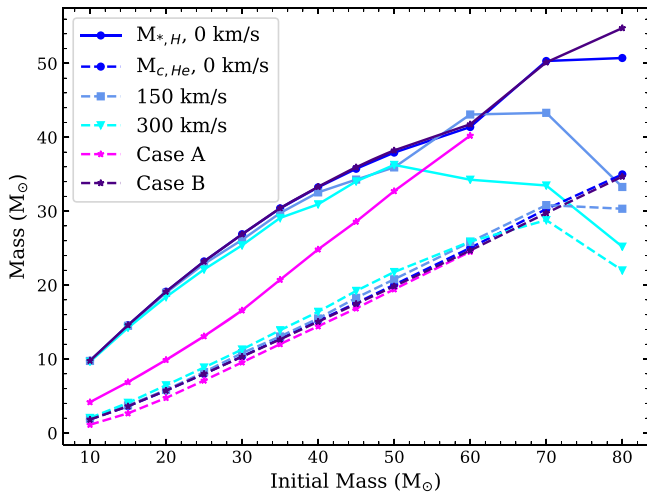


Figure 3. The total stellar mass $M_{*,H}$ (solid lines) and the hydrogen-depleted core mass $M_{c,He}$ (dashed lines) at the end of the main sequence as a function of the initial mass for the three single-star models with different initial rotational velocities and for representative binary systems (indicated in Table 1).

For core helium burning, the Case A binaries have the longest lifetimes. This is a direct result of the mass transfer during hydrogen burning. The binary interaction in this phase leads to smaller hydrogen-depleted cores at the end of core hydrogen burning (see also Figure 3). The hydrogen-depleted core is defined as the part of the star where the hydrogen content is below 0.01 and the helium content is above 0.1. Smaller hydrogen-depleted cores have lower helium-burning luminosities and therefore longer lifetimes. The Case B systems also have a slightly longer helium-burning lifetime, which is due to the smaller total masses at the end of helium burning as a result of the mass transfer just before helium burning starts. These stars have overall smaller helium-depleted cores than their noninteracting counterparts.

Figure 2 shows the total mass loss and the mass loss in different phases of the evolution. In panel (a), the total mass loss over the whole evolution is shown, while panels (b), (c), and (d) show the mass loss during hydrogen burning, between the end of hydrogen burning and the end of helium burning, and from the end of helium burning to the end of the evolution, respectively. Up to $50 M_{\odot}$, the Case A systems lose more mass than the nonrotating single star, while for the Case B systems it is not until $80 M_{\odot}$ that the mass loss becomes similar. We remind the reader that for 70 and $80 M_{\odot}$ we do not have a binary system undergoing Case A mass transfer. Especially on the lower-mass end, up to $\sim 30 M_{\odot}$, the binaries lose significantly more mass than the single stars, even compared to the rotating models. The rotating models lose more mass at the higher-mass end, from $60 M_{\odot}$ and higher, compared to both the nonrotating model and the binaries (for more details on binary evolution vs. single-star evolution, see the Appendix of Paper I).

As expected, the Case A systems lose most mass during the early phases of the evolution, though between 50 and $60 M_{\odot}$ the fastest-rotating model becomes the star that loses the most mass. The Case B models lose roughly the same amount of mass as the single nonrotating stars, except for the $80 M_{\odot}$ model, which is due to the strong winds at this mass. Then, again as expected, the Case B systems lose the most mass between the end of hydrogen burning and the end of helium burning, while most of the Case A systems lose less mass than

the nonrotating models. Finally, the mass loss in the final phases (panel (d)) does not show a predictable behavior.

Figure 3 shows the total stellar mass and mass of the hydrogen-depleted core at the end of hydrogen burning. As expected, the Case A systems have the lowest total masses, as they lose the most mass during this phase owing to the mass transfer. Their hydrogen-depleted cores are slightly smaller than those of the other models. For masses above $60 M_{\odot}$, the fastest-rotating models lose most mass in this phase, due to the stronger winds. However, their hydrogen-depleted cores are slightly larger than most of the other models, except for the most massive ones, due to the additional internal mixing due to rotation. The Case B systems are nearly identical to the nonrotating single stars.

These figures show that the binary interactions have an effect not only on the mass loss of the models but also on their internal structure. This is in qualitative agreement with the results of Laplace et al. (2021), who investigated the isotopic distribution in the core of Case B systems and how this would affect their supernova explosions.

3.2. Final Fates

The most important difference between the single stars and the primary stars of the binary systems is the amount of mass loss, which can lead to significant alteration in the stars of the binary system (see also Langer 2012; Laplace et al. 2021). While the majority of the primary stars simulated here end their lives as a core-collapse supernova, the binary systems with an initial primary mass of $10 M_{\odot}$ are an exception. The clearest example is the primary star of the system with an initial period of 2.8 days, which is plotted as the magenta line in Figure 4. The decline in the central temperature and the central density indicates that this star will end its life as a white dwarf. Eventually, the interior of the star will start cooling at a constant core density, as is shown by the orange line, representing a $10 M_{\odot}$ star at a period of 2.8 days, but with a mass ratio of 0.8 instead of 0.9. The other two $10 M_{\odot}$ primaries shown, with periods of 13.1 and 104.6 days, respectively, end their lives as supernovae, but likely as electron-capture supernovae instead of iron-core-collapse supernovae based on their central density and temperature profile (see, e.g., Figure 1 of Tauris et al. 2015). Based on previous studies of binary systems in this mass range (Podsiadlowski et al. 2004; Poelarends et al. 2017; Siess & Lebreuilly 2018), we expected to find such stars in our models. For comparison, the single stars of Paper II are also shown in Figure 4 as blue lines, where the cyan line represents the $10 M_{\odot}$ model at 300 km s^{-1} . This star shows the clearest signature of becoming an iron-core-collapse supernova. This shows that besides the impact on the stellar yields as determined in Paper I and further explored in Section 4, the binary interactions also have a strong impact on the final fate of stars close to the supernova boundary.

4. Yields from Nonrotating Binary Stars up until Core Collapse

As we showed in Paper I, binary interactions can have a large impact on the yields of massive stars by stripping off the envelope and exposing the deeper layers of the star, especially on the lower-mass end of the massive-star regime. So far, we have only considered the impact of the binary interactions

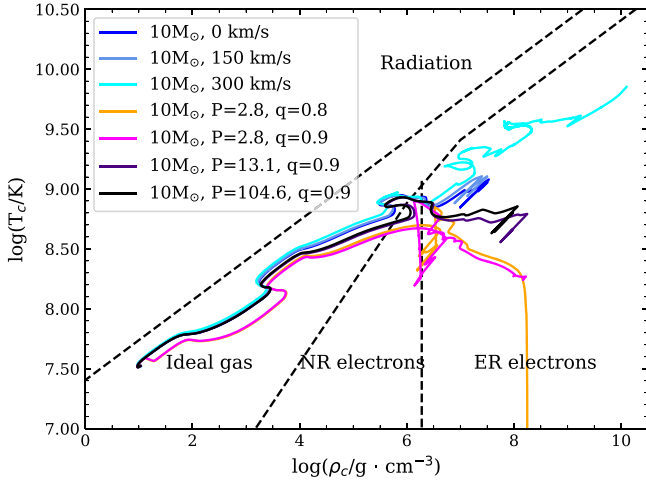


Figure 4. ρ_c – T_c diagram for different $10 M_\odot$ models. The blue lines are the single-star models from Paper II. The magenta, indigo, and black lines are for a $10 M_\odot$ primary at a period of 2.8, 13.1, and 104.6 days, respectively. The orange line is for a $10 M_\odot$ primary at a period of 2.8 days, but with a binary mass ratio of $q = 0.8$ instead of $q = 0.9$. The black dashed lines give a rough indication of the equations of state, i.e., radiative, ideal gas, nonrelativistic electron pressure (NR electrons), and extremely relativistic electron pressure (ER electrons).

on ^{26}Al . For the models presented in Paper II, we considered four more isotopes and the impact of rotation, but we did not include the impact of binary interactions. In this section, we discuss how binary interactions impact the yields of four isotopes: ^{36}Cl , ^{41}Ca , ^{22}Ne , and ^{19}F . We also briefly reconsider ^{26}Al and compare to the models of Papers I and II. The complete set of wind yields for all isotopes and models presented here is available on Zenodo under a Creative Commons 4.0 license: doi:[10.5281/zenodo.7956513](https://doi.org/10.5281/zenodo.7956513)

In this section, we use the following definitions:

1. The “effective binary yield” is the single-star yield multiplied by the binary enhancement factor, which is defined as the arithmetic average increase (over all periods considered) of the yield of the binary systems compared to the yield of the single stars. We have given all systems an equal weight in the calculations, especially since the yields are not that sensitive to the period in order of magnitude (aside from the models that break down), with the exception of the $10 M_\odot$ models. We do not consider the effect of higher-order systems, such as triples.⁹
2. The “maximum binary yield” is the maximum value of the individual wind yields for the binary systems with a certain initial primary mass.
3. The “minimum binary yield” is the minimum value of the individual wind yields for the binary systems with a certain initial primary mass. This minimum binary yield includes systems that did not complete their evolution, for example, due to the formation of a common envelope or numerical issues.

⁹ This is a slightly different definition than what was used in Paper I, where the effective binary yield was already corrected for the binary fraction, which has been renamed the “effective stellar yield.” For more details see Chapter 5 of Brinkman (2022).

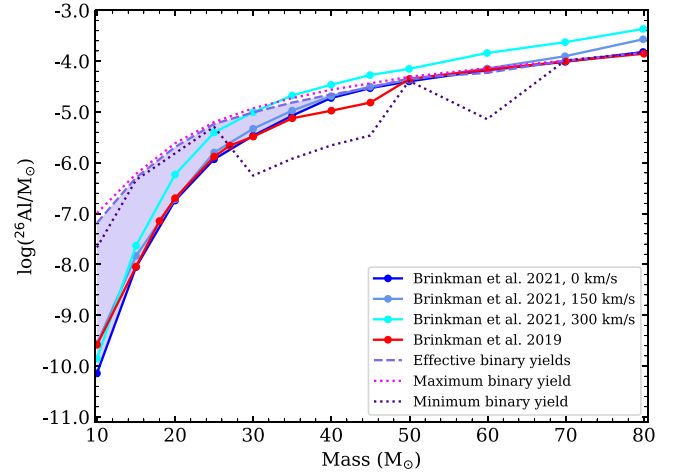


Figure 5. Single-star yields for Paper I (red circles) and Paper II (blue circles). The yields are compared to the effective, maximum, and minimum binary yields for the models presented in this work for ^{26}Al . The yields for the individual binary systems are given in Table 2. The shaded area indicates the potential effect of binarity, showing yields between the effective binary yield and the single-star yield. This is because the fully nonconservative mass transfer gives an upper limit for the binary yields.

4.1. Short-lived Radioactive Isotopes

In this section, we discuss the effects of the binary interactions on ^{26}Al , ^{36}Cl , and ^{41}Ca .

4.1.1. Aluminium-26

Evolving either single- or binary-star models up to core collapse (this work) instead of to the onset of carbon burning (as in Paper I) has a very limited impact on the ^{26}Al yield. The biggest change is for the $10 M_\odot$ star, where the model from Paper I has a 3.6 times higher yield than the model from Paper II. The model in Paper I loses slightly more mass than the model in Paper II, $1.01 M_\odot$ versus $0.96 M_\odot$, for reasons explained in Section 2 of Paper II. At this specific mass such a relatively small decrease in the mass lost from the star is enough to make a significant difference for the ^{26}Al yield. The 40 and 45 M_\odot models of Paper II have double the yields compared to the yields of Paper I because those models did not reach the onset of carbon burning in Paper I. The other single-star yields are within $\pm 10\%$ of the yields in Paper I.

Figure 5 shows the effective binary yields for the binary models computed for this work, as well as the maximum binary yield and the minimum binary yield, as defined above, along with the single-star yields of Paper I and II. For most initial masses the minimum and maximum binary yields (and hence effective values) are very similar. However, the models with the shortest initial period and initial primary masses of 30 and 45 M_\odot and 60 M_\odot enter a common-envelope phase that truncates the evolution, which leads to substantially lower (minimum) binary yield. As these short-period models are only a small subset, the effective binary yield more closely resembles the maximum yield binary predictions.

Figure 5 shows that both rotation and binary mass transfer increase the yields of ^{26}Al . At $\sim 30 M_\odot$ the fastest-rotating model of Paper II gives a similar yield to the binary system, while this happens only around $\sim 40 M_\odot$ for the lower initial rotational velocity and around $50 M_\odot$ for the nonrotating models. This demonstrates that for higher rotational velocities the increase in the wind mass loss washes out the effect of

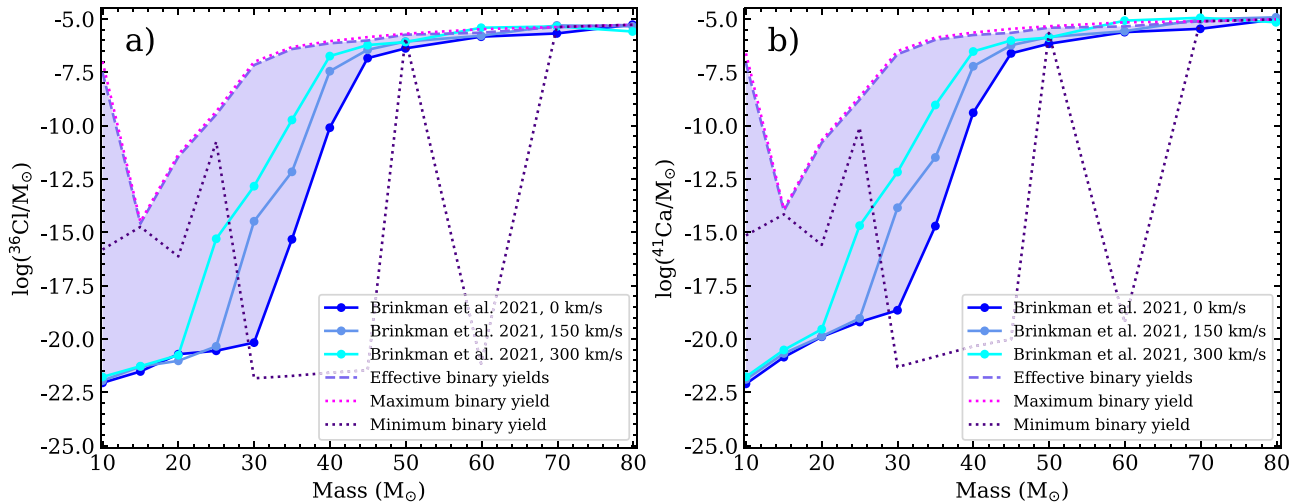


Figure 6. The yields of Paper II (blue lines with circles) with the effective binary yield (dashed line), maximum binary yield (purple dotted line), and minimum binary yield (teal dotted line) for the models presented in this work for (a) ^{36}Cl and (b) ^{41}Ca . The yields for the individual binary systems are given in Table 2. The shaded area indicates the potential binary yields, assuming that they are between the effective binary yield and the single nonrotating star yield, as fully nonconservative mass transfer gives an upper limit to the yields.

binary interactions at a lower mass than for the nonrotating models.

4.1.2. Chlorine-36 and Calcium-41

Figures 6(a) and (b) shows the yields for ^{36}Cl and ^{41}Ca , respectively. As described in Paper II, a higher initial rotational velocity decreases the initial mass for which the stars become W-R stars, leading to an earlier increase in the yields of these two SLRs. The difference between the maximum/effective binary yield and the minimum binary yield is much larger for these two isotopes than for ^{26}Al . As mentioned in the previous section, the sharp decrease in the minimum binary yield at $30 M_{\odot}$ is caused by the systems with the shortest initial period undergoing a common-envelope phase. As in the case of ^{26}Al , the binary interactions have the most prominent effect at the lower end of the mass range discussed in this work. Above $\sim 45 M_{\odot}$ the impact of the binary interactions on the yields decreases, and at $\sim 60 M_{\odot}$ the difference in yields becomes negligible. For the rotating stars, the effective binary yields become similar to the single-star yields at lower initial masses, $\sim 40 M_{\odot}$, as expected.

Just as for ^{26}Al , the effective binary yields for ^{36}Cl and ^{41}Ca follow a similar general trend to the single-star yields. However, unlike for ^{26}Al , ^{36}Cl and ^{41}Ca experience a strong increase in the yield at $10 M_{\odot}$. The increase at $10 M_{\odot}$ is caused by the fact that a deeper layer of the star is reached by the increased mass loss due to the binary interactions. Figure 7 shows the Kippenhahn diagrams (KHDs) for stars with initial masses 10, 15, and $25 M_{\odot}$, single stars on the left, and in a binary system undergoing Case B mass transfer on the right, with the ^{41}Ca mass fraction on the color scale (the ^{36}Cl mass fraction looks similar). The binary system with an initial mass of $10 M_{\odot}$ loses more mass than the single star owing to binary interactions (see also Table 1). This exposes deeper layers of the star to which ^{41}Ca (and ^{36}Cl) has been mixed, as it is produced in the convective He core. Especially during the final mass-loss phase during carbon shell burning (between $\log(\text{time until collapse/yr}) = 4$ and 2), the top layer enhanced in ^{41}Ca (and ^{36}Cl) is lost from the primary star. This is due to the fact that these stars experience an additional phase of mass transfer after core helium burning, which results from a strong increase

in the stellar radius during this phase. This is a common feature of exposed helium cores with masses of about $2.5 M_{\odot}$, which does not occur for higher masses (see, e.g., Habets 1986). This leads to a strong increase in the yield for ^{41}Ca (and ^{36}Cl) compared to the single star and a stronger dependence of the yields on the initial period than for the other systems, as can also be seen in the yields of the widest $10 M_{\odot}$ binary at a period of 104.6 days. This system does not go through the additional mass transfer phase and has a significantly lower yield for ^{41}Ca and ^{36}Cl than the shorter-period systems, though still strongly increased compared to the single star.

For the $15 M_{\odot}$ star (panels (c) and (d) of Figure 7) the mass loss after the main mass transfer phase is not strong enough to remove the upper layers of the helium core, the ^{41}Ca (and ^{36}Cl) produced in the inner layers is not reached, and this star does not experience the additional mass transfer phase. This leads to smaller yields and thus a smaller increase in the effective binary yield as compared to the $10 M_{\odot}$ case, following the general trend of the single stars. For the other single stars, 20 – $30 M_{\odot}$, the helium-burning core is barely reached, as shown by the example of a $25 M_{\odot}$ star, and these stars also do not go through an additional mass transfer phase. The resulting yields are below $10^{-20} M_{\odot}$ (see also Table 2). For these masses, the increased mass loss leads to the exposure of the top of the helium-burning core, just as for the $10 M_{\odot}$ star, giving a larger effective binary yield, which follows the same trend as the single-star yields. Around $\sim 40 M_{\odot}$, the effect of the binary interactions becomes smaller again, especially compared to the models of Paper II including the effects of rotational mixing.

4.2. Stable Isotopes: Fluorine-19 and Neon-22

The results for ^{19}F and ^{22}Ne are shown in Figure 8. The red line gives the initial mass of the stable isotopes present in the stars at the beginning of the evolution.¹⁰

For both ^{19}F and ^{22}Ne , rotation decreases the yields of the single stars as compared to the nonrotating case, up to $50 M_{\odot}$

¹⁰ In Paper II, the initial masses of the stable isotopes were mistakenly taken from a model that already had slight processing through the CNO cycle, resulting in a lower mass of ^{19}F and ^{22}Ne than based on the metallicity. This has been corrected here.

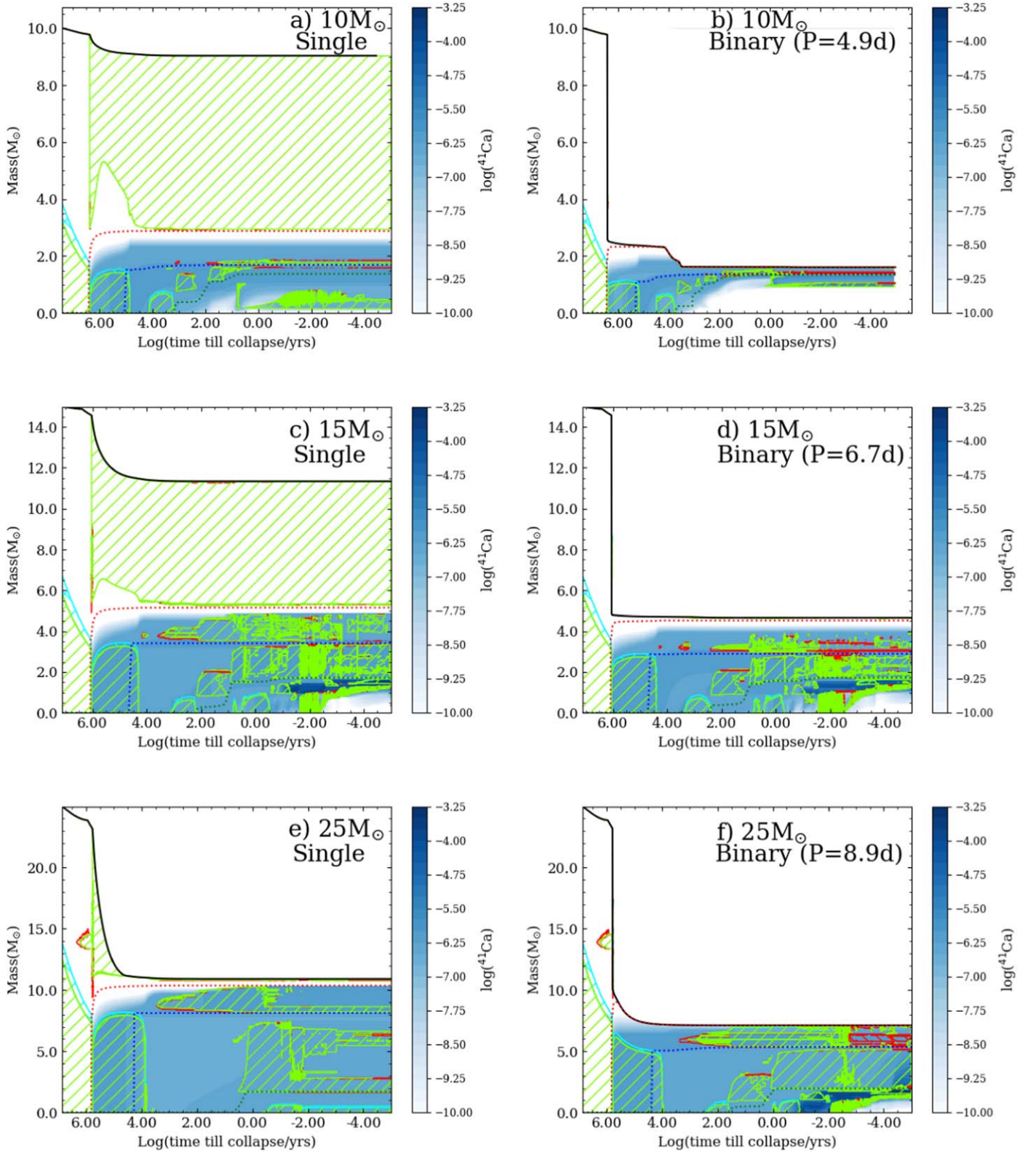


Figure 7. KHDs for 10, 15, and 25 M_\odot , single stars on the left (panels (a), (c), and (e), respectively), and as primaries of a binary system undergoing Case B mass transfer on the right. The initial periods are 4.9 days for the 10 M_\odot model (panel (b)), 6.7 days for the 15 M_\odot model (panel (d)), and 8.9 days for the 25 M_\odot model (panel (f)). The color scale shows the ^{41}Ca mass fraction in the stars. The green shaded areas correspond to areas of convection, the cyan shaded areas to overshooting, and the red shaded areas to semiconvection. The red dotted line indicates the hydrogen-depleted core, or helium core, where the hydrogen content is below 0.01 and the helium content is above 0.1. The color scale shows the ^{41}Ca mass fraction as a function of the mass coordinate and time.

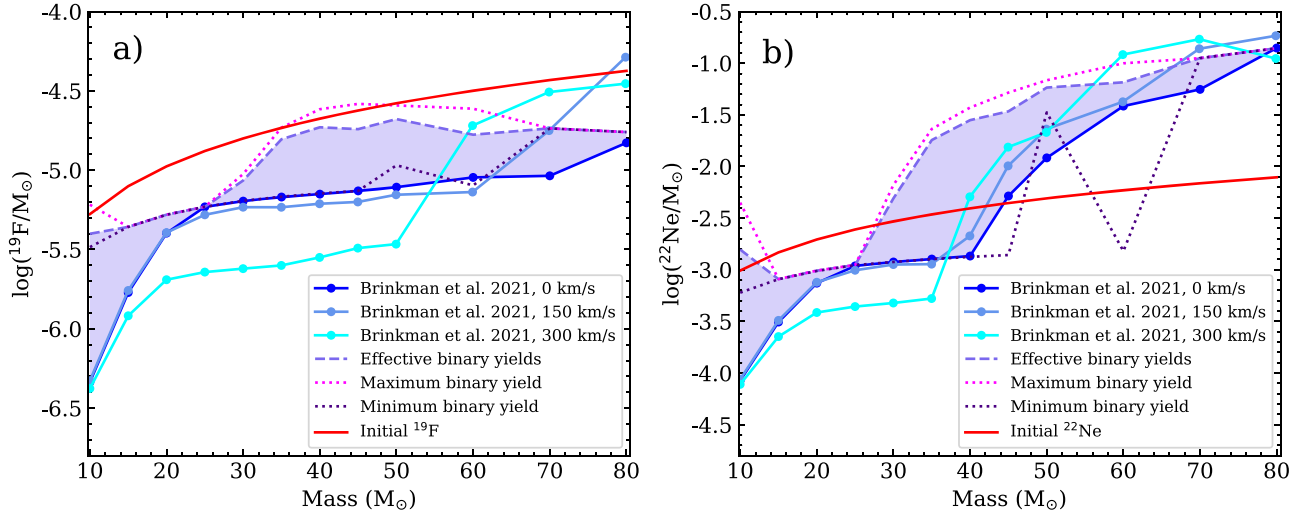


Figure 8. The yields for the single-star models, both rotating and nonrotating, of Paper II (blue lines with circles) with the effective binary yield (dashed line), maximum binary yield (magenta dotted line), and minimum binary yield (purple dotted line) for the models presented here for (a) ^{19}F and (b) ^{22}Ne . The yields for the separate binary systems are given in Table 2. The colored area indicates the potential binary yields, assuming that they are between the effective binary yield and the single-star yield. The red lines in both panels indicate the initial amounts of ^{19}F and ^{22}Ne present in the stars.

for the former and up to $40 M_{\odot}$ for the latter, as described in more detail in Paper II.

The effective binary yields for both isotopes do not follow the single-star trend as clearly as for the SLRs discussed previously. For both isotopes, the effective binary yields are almost identical to the nonrotating single-star yields around $25 M_{\odot}$. This is because for both the single star and the binary all ^{19}F and ^{22}Ne present in the envelope are stripped off, but the binary mass loss is not strong enough to reach the helium-burning core or the helium-burning shell, where these isotopes are produced. For the models with lower initial masses, the added mass loss through the binary interactions does increase the ^{19}F and ^{22}Ne yields, and thus the effective binary yields are higher than the single-star yields. For ^{19}F even the increased effective binary yields are still below the initial amount of ^{19}F present in the star. For ^{22}Ne the effective binary yield at $10 M_{\odot}$ is positive. The increase of the effective binary yields at $10 M_{\odot}$ is due to the deeper layers being reached, as seen for ^{36}Cl and ^{41}Ca previously. For the models with initial masses above $25 M_{\odot}$, deeper layers of the star are reached, leading to an increase in the effective binary yields again as compared to the single-star yields.

This is illustrated in Figure 9, showing the KHDs for three initial masses, 10 , 20 , and $40 M_{\odot}$, single stars on the left and the primary stars of selected binary systems on the right, with the ^{22}Ne mass fraction on the color scale. As already described above for Figure 7, for the $10 M_{\odot}$ star the primary star loses significantly more mass than the single star, which leads to a large increase of the yield, though either yield is too low to give a positive net yield.¹¹ Only the Case A system at $10 M_{\odot}$ gives a positive net yield for ^{19}F . For the $20 M_{\odot}$ models, even though the primary star loses more mass than a single star, the layers uncovered by the binary mass transfer do not have a large ^{22}Ne mass fraction, and thus the increase between the single star and the binary star is much smaller than for the $10 M_{\odot}$ model.

¹¹ Unlike ^{26}Al , which is not initially present in the star, there are two types of yields to consider for the stable isotopes, the “total” yield and the “net” yield. The total yield is calculated as described above, which ignores the initial amount of the stable isotope present in the star. The net yield is the total yield minus the initial amount of the isotope that was present in the star.

Finally, for the $40 M_{\odot}$ models, the extra mass loss due to the binary interactions uncovers the deeper layers of the star, and the winds strip off the upper layer of the region that belonged to the helium-burning core. This increases the yield of the primary star significantly as compared to the single star, leading to a positive net yield for the primary star. By contrast, only the fastest-rotating single-star model has a marginally positive net yield. This shows that while for the SLRs the impact of the binary interactions already tapers off around $40 M_{\odot}$, for the stable isotopes the effect is still significant for the higher masses considered here (40 – $50 M_{\odot}$).

For ^{19}F , only the maximum binary yields of the 35 – $50 M_{\odot}$ models are larger than the initial amount of ^{19}F present in the star, giving a positive net yield. This is at a significantly lower mass than for the single stars of Paper II, where the only model to give positive ^{19}F yield is the $80 M_{\odot}$ model rotating at 150 km s^{-1} . However, only the maximum yields are slightly above the initial amount of ^{19}F in these stars, which makes massive binaries unlikely candidates to explain the ^{19}F abundance in the Galaxy.

For ^{22}Ne , only nonrotating single-star models with masses $>45 M_{\odot}$ have positive yields, while this minimum mass is $40 M_{\odot}$ for the highest rotation rate. For binary models, however, the possible mass range for positive yields is much wider, including all stars in our grid with masses greater than $30 M_{\odot}$. Binary interactions may lead to a noticeable increase in the total yields from a given stellar population. To determine the yield increase of a population consisting of binaries versus a population of single stars, we consider a simple test using a Salpeter initial mass function (Salpeter 1955), in which the number of stars of a certain mass is given by

$$\frac{dN}{dM} = k \times M^{\alpha}, \quad (1)$$

where k is a constant determined by the local stellar density, M is the mass of the star in M_{\odot} , and $\alpha = -2.35$. The total yield of a population can then be expressed as

$$Y_{\text{tot}} = \int Y(M) \frac{dN}{dM} dM, \quad (2)$$

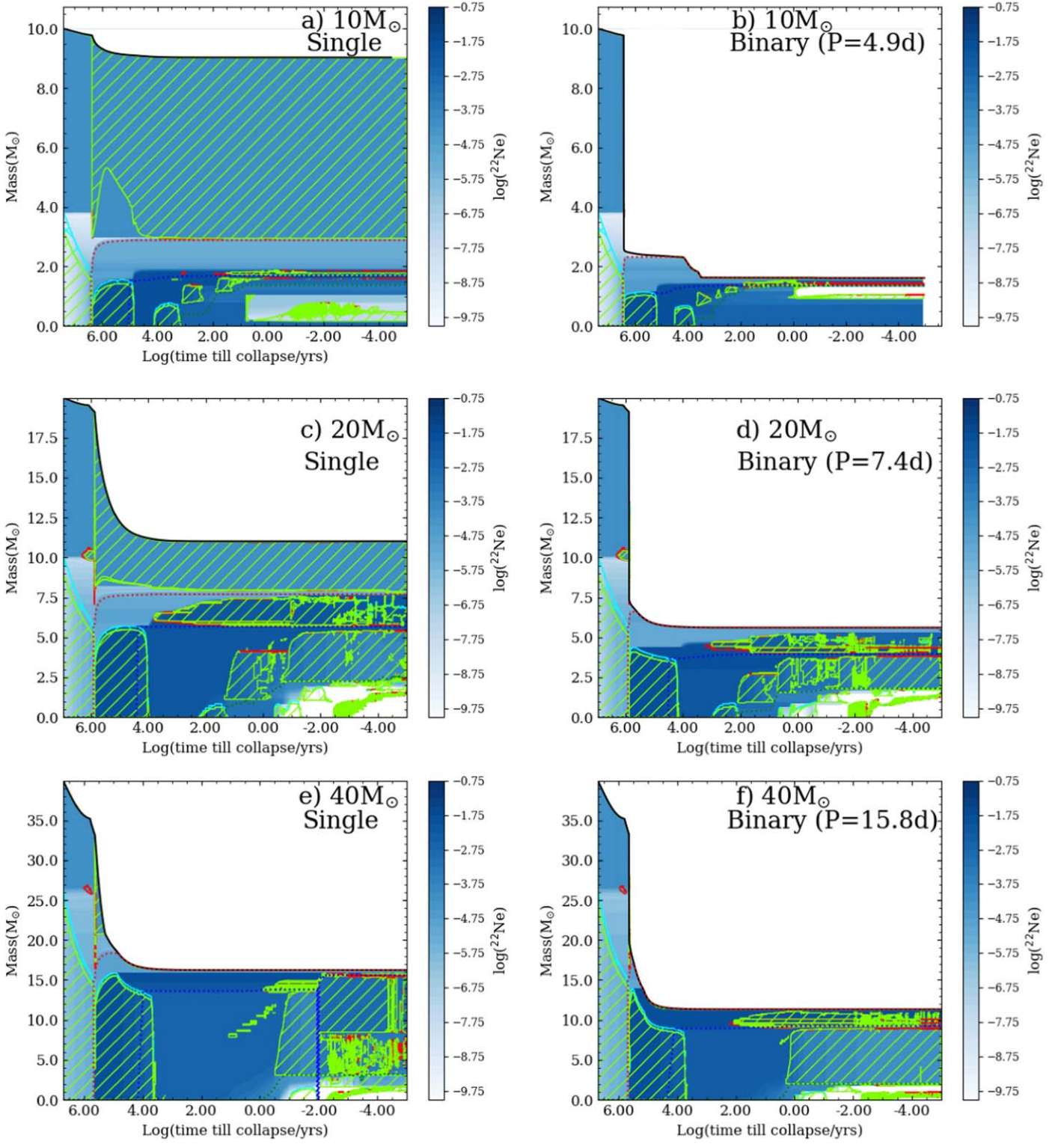


Figure 9. KHDs for masses 10, 20, and 40 M_{\odot} , single stars on the left (panels (a), (c), and (e)), binary stars on the right (panels (b), (d), and (f)). The initial periods are 4.9 days for the 10 M_{\odot} model (panel (b)), 7.4 days for the 20 M_{\odot} model (panel (d)), and 15.8 days for the 40 M_{\odot} model. All three systems undergo Case B mass transfer. The color scale shows the ^{22}Ne mass fraction in the stars. All other colors and shadings are the same as in Figure 7.

where $Y(M)$ is a function describing how the yield depends on stellar mass. However, because we have only calculated yields at a discrete set of mass values, we replace the integral by a sum over mass bins,

$$Y_{\text{tot}} = \sum_i Y_{M,i} N_{M,i}, \quad (3)$$

where $Y_{M,i}$ is the computed yield in bin i for mass M and $N_{M,i}$ is the number of stars in this bin, given by

$$N_M = \int_{M_{\text{low},i}}^{M_{\text{up},i}} \frac{dN}{dM} dM = k'(M_{\text{low},i}^{-1.35} - M_{\text{up},i}^{-1.35}), \quad (4)$$

where k' is a constant and M_{low} and M_{up} are the chosen boundaries of a mass bin based on our sample. We follow this procedure both for a population of single stars (taking for $Y_{M,i}$ the single-star yields) and for a population of binary stars, under the assumption that each star is the primary of a binary system and taking for $Y_{M,i}$ the effective binary yields. To get the yield increase of a binary population compared to the population of single stars, we divide the population yields, giving an increase by a factor of 3.95. However, to fully understand the impact of the binary population, a more detailed calculation using galactic chemical evolution models needs to be done (see Section 4.5 of Paper I), which is beyond the scope of this work. Instead, we decided to use a simpler approach that is consistent with our previous works.

4.3. Helium Star Winds

The nucleosynthetic yields from the primary stars of binary systems result from a combination of binary mass transfer and stellar winds. The stellar winds of massive stars are crucial for the evolution of these stars, but they are also very uncertain (Smith 2014). The final state of the star can be strongly impacted by the choice of mass-loss prescription (see, e.g., Renzo et al. 2017). As noted by Vink (2017), the mass-loss rates for helium stars (stars without a hydrogen-rich envelope) that are the result of a binary interaction and fall below the limit for W-R stars ($5\text{--}20 M_{\odot}$ for the helium star) are likely not the same as those for actual W-R stars, which are stars that have lost their envelope through their strong stellar winds. The difference in the wind strength is about an order of magnitude (see, e.g., Laplace et al. 2021, Appendix D), and this could potentially impact the nucleosynthetic yields of these stars. To test the impact of this different wind prescription for these stars, we have run models where we changed the wind prescription based on the size of the helium core of the stars. The only systems in our set that are strongly impacted by the change in the mass-loss rates for helium stars are the 10 and 15 M_{\odot} models, of which especially the 15 M_{\odot} models might be impacted since their helium cores are around $4\text{--}5 M_{\odot}$.

To see the impact of the mass-loss rates compared to the models earlier described in the paper (Set 1), we ran two additional sets of models using the reduced mass-loss rates following Vink (2017). The first set (Set 2) uses the reduced mass-loss rate when the helium core is smaller than $4 M_{\odot}$ and is used for the primary stars with 10 and 15 M_{\odot} . The second set (Set 3) uses the reduced mass-loss rate when the helium core is smaller than $5 M_{\odot}$ and is only used for the 15 M_{\odot} primary stars. This is because the 15 M_{\odot} models have core masses between 4 and $5 M_{\odot}$, while those for the 10 M_{\odot} models are always below $4 M_{\odot}$.

Table 3 gives the yields for the three SLRs for the different initial periods for the 10 and 15 M_{\odot} models and for the different wind prescriptions. The SLRs and their ratios are impacted by the change in the stellar winds. The stable isotopes instead, ^{19}F and ^{22}Ne , are not affected by the changes in the wind. This is because ^{19}F and ^{22}Ne are produced in deeper layers than those reached by the stellar winds, for these particular models.

For the 15 M_{\odot} models, the effects of changing the wind prescription to a reduced wind are clear. For the shortest-period binaries ($P = 3.8$ days), the helium core shrinks below the $4 M_{\odot}$ limit, and both Set 2 and Set 3 have the same yields,

which are smaller than the yields of Set 1. For the binaries with an initial period of 6.7 and 16.8 days, the yields for Set 2 are comparable to the yields of Set 1, while the yields of Set 3 are smaller. This is because for the wider systems in Set 2 the W-R wind following Nugis & Lamers (2000) is used, as it is for Set 1, while for the wider systems in Set 3 still the reduced winds are used. The effect of the reduced winds is stronger on ^{36}Cl and ^{41}Ca than on ^{26}Al , which is due to the later production of ^{36}Cl and ^{41}Ca and their location deeper under the surface. The stronger the winds, the more likely these layers are reached.

For the 10 M_{\odot} models, the behavior is less intuitive. While the ^{36}Cl and ^{41}Ca yields decrease for the reduced mass-loss rate, especially for the widest period, as for Set 3 of the 15 M_{\odot} models, the ^{26}Al yields increase for the less efficient winds. This is due to a slight change in the mass-loss history, when the ^{26}Al -rich layers are close to the surface. For the two widest periods, the change is minor and the final yields are still close to those of Set 1. For the closest period ($P = 2.8$ days), the mass loss increases earlier than for the same model in Set 1, which, combined with the still decaying ^{26}Al content of the envelope, leads to a strong increase in the ^{26}Al yield of Set 2 as compared to Set 1.

5. Early Solar System

The radioactive isotopes described in the previous section were inferred to be present in the early solar system (ESS) from observed excesses of their daughter nuclei in meteoritic inclusions. To determine whether the binary systems presented in this work can explain the presence of ^{26}Al , ^{36}Cl , and ^{41}Ca in the ESS, we use the simple dilution model for ^{26}Al , ^{36}Cl , and ^{41}Ca , described in Paper II.

5.1. Selection of the Binary Systems

We apply the same method as described in Section 5 of Paper II to determine which of the binary systems presented in this paper might be able to explain the abundances of ^{26}Al , ^{36}Cl , and ^{41}Ca in the ESS. Here we repeat the method briefly.

We determine a “dilution factor,” f_{26} , based on ^{26}Al . This is defined as $f_{26} = \frac{M_{26}^{\text{ESS}}}{M_{26}^*}$, where M_{26}^{ESS} is the mass of ^{26}Al in the ESS and M_{26}^* is the mass of ^{26}Al ejected by the stellar wind, i.e., the total yield. The initial amount of ^{26}Al , $3.1 \times 10^{-9} M_{\odot}$, is derived by assuming the solar abundance for ^{27}Al (Lodders 2003) and a total mass of $1 M_{\odot}$ to be polluted (see Lugaro et al. 2018, for more details).

This dilution factor for ^{26}Al , f_{26} , is then used to obtain the diluted amount of ^{41}Ca , which is used to calculate the “delay time” (Δt). The delay time can be interpreted as the time interval between wind ejection and the incorporation of the SLRs into the first solids to form the ESS. With the delay time, we reverse decay the initial amount of ^{26}Al in the ESS and recalculate f_{26} using the new ^{26}Al value. We then determine a new amount of ^{41}Ca . We continue this iteration until we converge to a Δt within a 10% difference from the previous value, which gives us a different value of f_{26} for each stellar model. Lastly, we apply the final f_{26} to calculate the diluted amount of ^{36}Cl and a delay time for ^{36}Cl as well.

With this method, we determined in Paper II that stars above $\sim 40 M_{\odot}$ can match the ESS $^{26}\text{Al}/^{27}\text{Al}$ and $^{41}\text{Ca}/^{40}\text{Ca}$ ratios, but only the most massive models can also match the $^{36}\text{Cl}/^{35}\text{Cl}$ ratio. For the binaries we see a similar scenario: when considering only ^{26}Al and ^{41}Ca , almost all models can match

the ESS, with the exception of the models with initial primary masses of 15 and 20 M_{\odot} , the systems with the shortest periods in the range 25–45 M_{\odot} , and the widest binary system with an initial mass of 10 M_{\odot} . To also match ^{36}Cl , higher initial masses for the primary are needed. The binaries with a primary with an initial mass of 35–45 M_{\odot} can match all three SLRs for all periods, except the shortest (and the 7.8-day period for the 45 M_{\odot}). The binaries with initial primary masses of 50 M_{\odot} and higher can match all three SLRs for all periods. Interestingly, we also find that the binary with an initial primary mass of 10 M_{\odot} can match the three SLRs for all periods, except the widest of 104.6 days. The 10 M_{\odot} systems are interesting because the shortest period of this configuration yields a white dwarf, which means that no further pollution is expected from the primary star of this system since the star will not explode and not eject other SLRs, such as ^{60}Fe and ^{53}Mn . In Figure 10 we show the binary model with an initial primary mass of 10 M_{\odot} with a period of 4.9 days compared to the isotopic ratios in the ESS. For reference, we also plotted the $^{26}\text{Al}/^{27}\text{Al}$ ratio for the 10 M_{\odot} single star of Paper II. With a dilution factor of 0.071, both the $^{26}\text{Al}/^{27}\text{Al}$ and $^{41}\text{Ca}/^{40}\text{Ca}$ ratios can be matched with this binary model. The $^{36}\text{Cl}/^{35}\text{Cl}$ ratio is not matched but is within the range of uncertainties. For the single-star model, it is not possible to match any of the ratios. However, the very large dilution factor would imply that the stellar winds composed 7% of the total solar system material, which may be considered as unrealistic. Furthermore, the timescale of the pollution by such a system can prove to be problematic for contributing to the SLR abundances in the ESS. This is because the lifetime of these stars, 25–28 Myr, is longer than the lifetime of a giant molecular cloud (see, e.g., Hartmann et al. 2001) and also because it is at the upper limit of the isolation time for the ESS, as found by Trueman et al. (2022).

5.2. Revision of the $^{41}\text{Ca}/^{40}\text{Ca}$ Ratio

Ku et al. (2022) have published a new value for the ESS of the $^{41}\text{Ca}/^{40}\text{Ca}$ ratio of $(2.00 \pm 0.52) \times 10^{-8}$, ~ 4 times higher than the value found by Liu (2017) of $(4.6 \pm 1.9) \times 10^{-9}$, which was used to determine the results above. When we apply this revised ratio determination to both the models from Paper II and the models presented here, we find that the new value barely changes which models match the ESS. The main difference is that the delay time is about a factor 20%–30% shorter for the models calculated with the new $^{41}\text{Ca}/^{40}\text{Ca}$ value as compared to the older value. This is because matching a higher ratio requires a shorter decay time. Changing the $^{41}\text{Ca}/^{40}\text{Ca}$ ratio does not affect which single stars can match both ^{26}Al and ^{41}Ca . For all three SLRs, however, the 50 M_{\odot} model with an initial rotational velocity of 300 km s^{-1} is no longer a match. For the binaries, changing the $^{41}\text{Ca}/^{40}\text{Ca}$ ratio does affect which models match all three SLRs, but for the models that only match ^{26}Al and ^{41}Ca and not also ^{36}Cl , the number of matches decreases by two—the 25 M_{\odot} binaries at 6.7 and 71.3 days are no longer a match.

5.3. Oxygen Ratios and C/O Wind Composition

There are two more considerations that may be of interest as potential constraints for this scenario of the origin of the three SLRs in the ESS. The first is if the SLR pollution also affects the oxygen isotopic ratios in the ESS, and the second is the carbon-to-oxygen ratio in the wind. The first is of interest

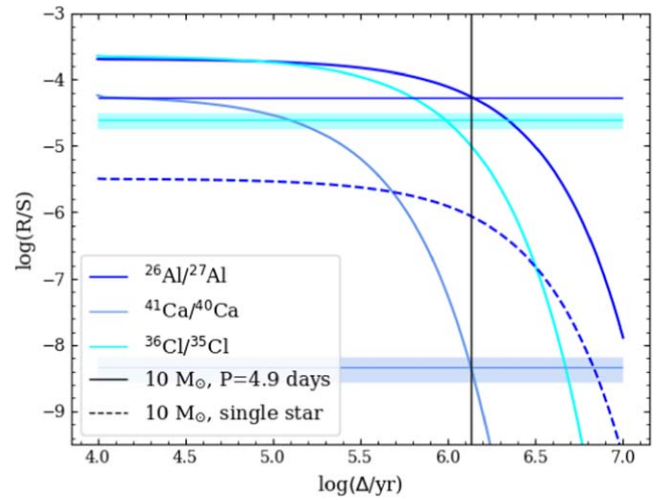


Figure 10. Abundance ratios (R/S) for the three SLRs (R) over their stable reference isotope (S) for a certain dilution factor f . The solid lines represent the 10 M_{\odot} primary star of the system with a period of 4.9 days; the dashed line is the $^{26}\text{Al}/^{27}\text{Al}$ ratio for the 10 M_{\odot} single star of Paper II. The horizontal bands represent the ESS ratios, with their respective errors. The vertical line represents the delay time for the $^{41}\text{Ca}/^{40}\text{Ca}$ ratio.

because some CAIs (the FUN class) and some corundum grains are poor in ^{26}Al , but they have virtually the same oxygen isotopic composition as those that are rich in ^{26}Al (see, e.g., Makide et al. 2011). For example, the errors on the measurement of $\Delta^{17}\text{O}$ are of the order of a percent (see Figure 2 of Makide et al. 2011). Because the oxygen ratios ($^{17}\text{O}/^{16}\text{O}$ and $^{18}\text{O}/^{16}\text{O}$) are so well constrained, the model that reproduces the SLRs cannot impact these ratios by more than their respective error bars, to avoid a correlation between ^{26}Al and a modification of the oxygen isotopic ratios (Gounelle & Meibom 2007). The composition of the oxygen isotopes in the winds is dominated by hydrogen and helium burning, and its main features are production of ^{16}O and depletion of ^{17}O and ^{18}O , relative to the initial amounts of these isotopes in the star. For the single stars, the $^{17}\text{O}/^{16}\text{O}$ and $^{18}\text{O}/^{16}\text{O}$ ratios are roughly 8 and 20 times lower than the solar value, respectively. Therefore, when we add the oxygen isotopic wind yields of the selected models diluted by f_{26} to the inferred amount of these isotopes in the solar system, we obtain a decrease of the order of 0.1%–1.5% in both the $^{17}\text{O}/^{16}\text{O}$ and $^{18}\text{O}/^{16}\text{O}$ ratios. When considering the binary models, the $^{17}\text{O}/^{16}\text{O}$ and $^{18}\text{O}/^{16}\text{O}$ ratios are roughly 13 and 20 times lower than the solar value. As for the single stars, we add the diluted yields of the oxygen isotopes to the solar values, and we find that the ratios decrease on the order of 0.1%–1.5% in both the $^{17}\text{O}/^{16}\text{O}$ and $^{18}\text{O}/^{16}\text{O}$ ratios, as before, and again with increasing stellar mass from 30–35 M_{\odot} to 80 M_{\odot} .

We also checked the C/O composition of the winds at the time of the ejection of ^{36}Cl and ^{41}Ca . This is because the C/O ratio is an indicator for possible dust formation in the stellar winds. Dwarkadas et al. (2017) state that dust may be needed to incorporate SLRs into the ESS. However, dust formation is only observed in C-rich binary cases (see, e.g., Lau et al. 2020). Thus, the binary models are more relevant in relation to dust formation than single stars. All the binary models that can match all three SLRs have C/O ratios in their winds of larger than 1 at the end of their evolution, and closer to 1 when the ^{26}Al yield reaches a value above $10^{-15} M_{\odot}$, which is when the isotopes are ejected. The exception are the 50 M_{\odot} models,

where the C/O ratio is slightly below 1. How much the C/O ratio plays a role in determining the potential source of the SLRs depends on how the different elements are incorporated in dust. This is, however, beyond the scope of this work.

6. Conclusions

We have investigated the production of the stable isotopes, ^{19}F and ^{22}Ne , and radioactive isotopes, ^{26}Al , ^{36}Cl , and ^{41}Ca , in the winds of binary systems undergoing Case A or Case B mass transfer. Then, we determined which models could self-consistently explain the ESS abundances of ^{26}Al , ^{36}Cl , and ^{41}Ca . We have found the following:

1. In terms of the structural evolution, the main effect of the binary interactions is an increased mass loss, mostly at the lower end of the mass range investigated in this work. The interactions have a secondary effect on the duration of the burning phases and also on the core structure at the moment of core collapse. For the lowest mass, the binary interactions can completely change the outcome of the evolution. In fact, our $10 M_{\odot}$ binary star ends as a white dwarf or an electron-capture supernova instead of as an iron-core-collapse supernova.
2. For the short-lived radioactive isotopes, it is mostly the W-R stars in the mass range $40\text{--}80 M_{\odot}$ that give significant yields. For ^{26}Al , the binary interactions lose their impact above $\sim 50 M_{\odot}$, while for ^{36}Cl and ^{41}Ca this happens at slightly higher masses, $\sim 60 M_{\odot}$.
3. Only a very narrow range of initial primary masses and periods produce a net positive ^{19}F yield (the maximum yields for the $35\text{--}50 M_{\odot}$ models).
4. For ^{22}Ne most systems with initial masses above $30 M_{\odot}$, except for the shortest periods in the range $35\text{--}45 M_{\odot}$, produce positive net yields. With these systems we found that a population of binaries can produce about a factor of 4 more ^{22}Ne as compared to a population of only single stars considering a Salpeter initial mass function.
5. In Section 5, we have investigated which of the stellar models described in this paper could explain the ESS abundances. Depending on the initial primary mass and initial period, only stars with an initial mass of 15 and $20 M_{\odot}$ do not explain the ^{26}Al and ^{41}Ca abundances, along with the shortest periods for $25\text{--}45 M_{\odot}$ and the widest system at $10 M_{\odot}$. All the models with mass $\geq 50 M_{\odot}$ can also explain the ^{36}Cl abundances. The $10 M_{\odot}$ models that do not become iron-core-collapse supernovae but white dwarfs or electron-capture

supernovae have very different final yields, which needs to be further investigated, also in relation to the SLRs.

A more detailed analysis of several uncertainties should be performed, which includes different prescriptions for the winds and for the rotational boost on wind loss, as well as investigations of the effect of reaction rate uncertainties specifically on the destruction of ^{19}F , ^{41}Ca , and ^{36}Cl and the neutron source $^{22}\text{Ne}(\alpha, n)^{25}\text{Mg}$ reaction (Adsley et al. 2021). The interaction between rotation and binarity will need further investigation, but it is difficult to perform owing to the complexity of the angular momentum coupling between the two stars. In addition, a more detailed analysis of the uncertainties of binary evolution and their effects on the yields should be performed. These uncertainties include, but are not limited to, the mass transfer efficiency, which includes accretion onto the secondary and potentially on the primary in a case of reverse mass transfer; the formation of common envelopes and their effect on the binary parameters; and variations in the initial mass ratio between the stars. Finally, to present a complete view, the explosive nucleosynthetic yields will need to be calculated using our models as the progenitors of the explosion.

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Software: MESA (Paxton et al. 2011, 2013, 2015, 2018).

Appendix

In Table 1, we present selected details of the evolution of the stellar models. In Table 2, we present the nucleosynthetic yields of the models. Lastly, in Table 3, we present the nucleosynthetic yields of the models with adjusted settings for the mass loss.

Table 1
Selected Details of the Evolution of the Stellar Models

M_{ini} (M_{\odot})	P_{ini} (days)	Case ...	t_{H} (Myr)	$M_{\text{c,He}}$ (M_{\odot})	$M_{*,\text{H}}$ (M_{\odot})	t_{He} (Myr)	$M_{\text{c,C}}$ (M_{\odot})	$M_{*,\text{He}}$ (M_{\odot})	$M_{*,\text{C}}$ (M_{\odot})	t_{tot} (Myr)	ΔM (M_{\odot})
10	... ^a	...	23	1.83	9.78	1.98	1.52	9.11	9.04	25.37	0.96
	2.8 ^{b,e}	A	24.1	1.11	4.17	3.44	1.10	1.86	1.85	28.18	8.71
	4.9 ^c	B	22.98	1.83	9.78	2.38	1.26	2.33	1.93	25.73	8.39
	13.1 ^c	B	22.98	1.83	9.78	2.33	1.27	2.37	2.26	25.68	8.18
	104.6 ^c	B	22.98	1.83	9.78	2.25	1.31	2.46	2.44	25.60	7.56
15	12.15	3.62	14.58	0.96	3.41	11.49	11.35	13.26	3.65
	3.8	A	12.40	2.66	6.89	1.22	1.97	3.45	3.43	13.81	11.56
	6.7	B	12.15	3.62	14.58	0.99	2.35	4.07	4.01	13.31	10.99
	16.8	B	12.15	3.62	14.58	0.99	2.39	4.11	4.05	13.3	10.95
20	8.53	5.73	19.12	0.66	5.66	11.24	11.02	9.29	8.98
	2.5 ^{1,5}	A	9.11	4.15	9.74	0.76	3.14	4.95	4.95	10.10	15.05
	5.1 ^a	A	8.61	4.74	9.88	0.74	3.28	5.18	5.13	9.45	14.87
	6.2	B	8.53	5.73	19.12	0.68	3.67	5.66	5.6	9.31	14.39
	7.4	B	8.53	5.74	19.12	0.68	3.69	5.68	5.61	9.31	14.38
	18.4	B	8.53	5.74	19.12	0.67	3.74	5.76	5.67	9.3	14.33
	66.2	B	8.53	5.74	19.12	0.67	3.8	5.79	5.73	9.3	14.26
	132.4	B	8.53	5.74	19.12	0.67	3.8	5.81	5.74	9.3	14.25
25	... ^a	...	6.8	7.99	23.2	0.53	8.13	11.04	10.92	7.41	14.07
	2.7 ^c	A	7.17	6.27	13.02	0.64	4.18	6.14	6.08	7.90	18.91
	6.7 ^c	A	6.84	7.1	13.09	0.57	4.71	6.82	6.75	7.49	18.24
	8.9	B	6.8	7.99	23.2	0.55	5.06	7.21	7.12	7.42	17.87
	17.8	B	6.8	7.99	23.2	0.56	5.09	7.24	7.18	7.42	17.83
	71.3 ^a	B	6.8	7.99	23.2	0.54	5.15	7.31	7.23	7.42	17.76
30	... ^a	...	5.8	10.35	26.89	0.47	10.73	13.56	13.47	6.32	16.52
	2.8 ^d	A
	8.4 ^c	A	5.82	9.55	16.59	0.48	6.5	8.55	8.41	6.36	21.57
	10.1 ^e	B	5.8	10.32	26.81	0.48	6.59	8.69	8.56	6.34	21.43
	12.2 ^e	B	5.8	10.32	26.88	0.48	6.58	8.67	8.53	6.34	21.46
	30.3 ^c	B	5.8	10.32	26.88	0.47	6.64	8.93	8.68	6.33	21.31
	75.4 ^e	B	5.8	10.32	26.88	0.47	6.67	8.79	8.66	6.33	21.33
35	5.15	12.74	30.38	0.42	12.95	15.64	15.46	5.62	19.51
	2.9 ^d	A
	8.8 ^c	A	5.17	12.02	20.73	0.44	7.32	9.64	9.57	5.66	25.4
	10.6 ^c	A	5.16	12.63	21.23	0.43	7.62	9.92	9.85	5.64	25.13
	12.7 ^c	B	5.16	12.66	30.42	0.43	7.57	9.89	9.81	5.64	25.17
	31.5 ^c	B	5.16	12.66	30.42	0.43	7.81	10.14	10.08	5.64	24.9
	78.6 ^c	B	5.16	12.66	30.42	0.43	8.05	10.42	10.35	5.63	24.63
40	4.69	15.17	33.23	0.39	13.63	16.4	16.24	5.12	23.74
	3.1 ^d	A
	7.6 ^c	A	4.72	14.43	24.83	0.41	8.5	10.9	10.85	5.18	29.12
	15.8 ^e	B	4.7	15.05	33.3	0.41	8.95	11.39	11.33	5.15	28.64
	20.4 ^e	B	4.7	15.05	33.3	0.4	9.03	11.42	11.36	5.15	28.61
	32.8 ^c	B	4.7	15.05	33.29	0.4	9.11	11.57	11.51	5.15	28.45
45	4.35	17.57	35.74	0.36	14.85	17.95	17.9	4.76	27.06
	3.2 ^d	A
	6.5 ^c	A	4.38	16.85	28.6	0.39	9.67	12.26	12.18	4.81	32.77
	7.8 ^a	A	4.37	16.96	28.91	4.51	...
	19.5 ^c	B	4.35	17.46	35.91	0.39	10.37	12.86	12.8	4.79	32.15
	23.4 ^c	B	4.35	17.46	35.95	0.38	10.38	12.92	12.84	4.79	32.11
	42.0 ^c	B	4.35	17.46	35.95	0.38	10.56	13.23	13.17	4.78	31.79
	69.9 ^c	B	4.35	17.46	35.95	0.37	11.36	14.09	14.02	4.78	30.93
50	4.09	20.05	37.93	0.35	16.84	19.92	19.87	4.48	30.07
	8.1 ^c	A	4.1	19.43	32.72	0.37	11.09	13.63	13.56	4.52	36.39
	14.0 ^c	A	4.09	19.61	33.1	0.37	11.2	13.82	13.74	4.51	36.21
	21.7 ^c	B	4.09	19.77	35.3	0.36	11.43	14.09	14	4.5	35.94
	29.1 ^c	B	4.09	19.85	38.23	0.37	11.61	14.31	14.23	4.5	35.71
	72.3 ^c	B	4.09	19.85	38.29	0.36	12.83	15.69	15.61	4.49	34.33
	144.6 ^c	B	4.09	19.85	38.29	0.35	14.66	17.55	17.47	4.48	32.47

Table 1
(Continued)

M_{ini} (M_{\odot})	P_{ini} (days)	Case ...	t_{H} (Myr)	$M_{\text{c,He}}$ (M_{\odot})	$M_{*,\text{H}}$ (M_{\odot})	t_{He} (Myr)	$M_{\text{c,C}}$ (M_{\odot})	$M_{*,\text{He}}$ (M_{\odot})	$M_{*,\text{C}}$ (M_{\odot})	t_{tot} (Myr)	ΔM (M_{\odot})
60	3.71	25.04	41.39	0.33	19.49	22.76	22.67	4.07	37.25
	3.5 ^d	A
	7.2^e	A	3.71	24.53	40.22	0.33	19.24	22.53	22.43	4.07	37.49
	14.9 ^e	B	3.7	24.69	41.76	0.34	13.68	16.47	16.38	4.08	43.54
	17.8 ^e	B	3.7	24.69	41.76	0.34	13.76	16.55	16.47	4.08	43.46
	37.0^e	B	3.7	24.69	41.76	0.34	14.09	16.98	16.9	4.08	43.02
	92.2 ^e	B	3.7	24.69	41.76	0.33	17.18	20.3	20.22	4.07	39.71
70	3.43	30.29	50.32	0.31	22.86	26.36	26.25	3.78	43.65
	39.1^e	B	3.43	29.74	50.14	0.32	17.28	20.54	20.46	3.79	49.45
80	3.24	34.98	50.72	0.31	20.68	24.1	23.99	3.58	55.9
	33.9^e	B	3.23	34.69	54.77	0.31	19.89	23.09	23.01	3.58	56.88

Notes. M_{ini} is the initial mass in M_{\odot} . P_{ini} is the initial period in days. Parameters t_{H} , t_{He} , and t_{tot} are the duration of hydrogen burning, the duration of helium burning, and the total evolution time in Myr, respectively. $M_{*,\text{H}}$, $M_{*,\text{He}}$, and $M_{*,\text{C}}$ are the masses of the stars at the end of their respective burning phases; $M_{\text{c,He}}$ and $M_{\text{c,C}}$ are the masses of the hydrogen-depleted core and the helium-depleted core, respectively, at the end of the corresponding burning phases in M_{\odot} ; and ΔM is the total mass lost in M_{\odot} . The single-star models were taken from Paper II. The periods printed in boldface indicate the models used as representative for Case A and Case B mass transfer in Section 3. Case indicates the first mass transfer the system undergoes, which does not include further mass transfer phases such as Case AB or BC.

^a This run was terminated before the core collapse owing to numerical difficulties.

^b This primary star has lost such a significant amount of mass that its final state will be a white dwarf. At the end of the simulation the remaining stellar mass is $1.30 M_{\odot}$.

^c The final core mass of this star is such that it is a potential electron-capture supernova.

^d Terminated owing to the formation of a common envelope.

^e The primary star of this system was uncoupled and further evolved as a single star as the secondary overflows its Roche lobe.

^f This run experienced computational difficulties in the final phases, leading to a much larger $M_{\text{c,O}}$ than for any of the other models.

Table 2
Wind Yields in M_{\odot} for the Binary Models for the Key Isotopes ^{19}F , ^{22}Ne , ^{26}Al , ^{36}Cl , and ^{41}Ca

M_{ini} (M_{\odot})	P_{ini} (days)	$^{19}\text{F}_{\text{ini}}$ (M_{\odot})	^{19}F (M_{\odot})	$^{22}\text{Ne}_{\text{ini}}$ (M_{\odot})	^{22}Ne (M_{\odot})	^{26}Al (M_{\odot})	^{36}Cl (M_{\odot})	^{41}Ca (M_{\odot})
10	— ^a	5.28e-06	4.61e-07	9.82e-4	8.47e-05	7.19e-11	8.82e-23	7.90e-23
	2.8^{b,c}	5.28e-06	6.06e-06	9.82e-4	4.47e-3	3.74e-08	1.01e-07	2.44e-07
	4.9 ^c	5.28e-06	3.27e-06	9.82e-4	6.07e-4	1.02e-07	2.05e-08	8.45e-08
	13.1^c	5.28e-06	3.27e-06	9.82e-4	6.04e-4	1.01e-07	4.61e-09	2.04e-08
	104.6 ^c	5.28e-06	3.28e-06	9.82e-4	6.01e-4	2.16e-08	1.56e-16	7.15e-16
15	...	7.93e-06	1.69e-06	1.47e-3	3.12e-4	8.85e-09	3.00e-22	1.41e-21
	3.8	7.93e-06	4.39e-06	1.47e-3	8.13e-4	6.04e-07	1.81e-15	6.96e-15
	6.7	7.93e-06	4.39e-06	1.47e-3	8.11e-4	4.71e-07	3.12e-15	1.24e-14
	16.8	7.93e-06	4.39e-06	1.47e-3	8.10e-4	4.58e-07	2.73e-15	1.09e-14
20	...	1.06e-05	4.01e-06	1.96e-3	7.43e-4	1.81e-07	1.94e-21	1.28e-20
	2.5 ^{1,5}	1.06e-05	5.24e-06	1.96e-3	9.74e-4	1.53e-06	7.43e-17	2.60e-16
	5.1^a	1.06e-05	5.24e-06	1.96e-3	9.83e-4	2.42e-06	3.05e-12	1.41e-11
	6.2	1.06e-05	5.24e-06	1.96e-3	9.90e-4	2.13e-06	4.47e-12	2.08e-11
	7.4	1.06e-05	5.24e-06	1.96e-3	9.80e-4	2.12e-06	4.44e-12	2.07e-11
	18.4	1.06e-05	5.24e-06	1.96e-3	9.80e-4	2.07e-06	4.27e-12	1.99e-11
	66.2	1.06e-05	5.24e-06	1.96e-3	9.81e-4	2.01e-06	3.85e-12	1.79e-11
	132.4	1.06e-05	5.24e-06	1.96e-3	9.81e-4	2.00e-06	3.84e-12	1.79e-11
25	— ^a	1.32e-05	5.87e-06	2.46e-3	1.09e-3	1.17e-06	2.80e-21	6.27e-20
	2.7 ^c	1.32e-05	5.88e-06	2.46e-3	1.11e-3	5.11e-06	1.75e-11	8.10e-11
	6.7^e	1.32e-05	5.88e-06	2.46e-3	1.11e-3	6.31e-06	3.46e-10	1.72e-09
	8.9	1.32e-05	5.88e-06	2.46e-3	1.11e-3	5.93e-06	4.60e-10	2.30e-09
	17.8	1.32e-05	5.88e-06	2.46e-3	1.11e-3	5.86e-06	4.41e-10	2.20e-09
	71.3 ^a	1.32e-05	5.88e-06	2.46e-3	1.11e-3	5.76e-06	3.94e-10	1.96e-09
30	— ^a	1.59e-05	6.38e-06	2.95e-3	1.19e-3	3.41e-06	6.76e-21	2.22e-19
	2.8 ^d	1.59e-05	6.41e-06	2.95e-3	1.19e-3	5.59e-07	1.44e-22	4.87e-22
	8.4^e	1.59e-05	9.46e-06	2.95e-3	6.63e-3	1.17e-05	9.78e-08	3.11e-07

Table 2
(Continued)

M_{ini} (M_{\odot})	P_{ini} (days)	$^{19}\text{F}_{\text{ini}}$ (M_{\odot})	^{19}F (M_{\odot})	$^{22}\text{Ne}_{\text{ini}}$ (M_{\odot})	^{22}Ne (M_{\odot})	^{26}Al (M_{\odot})	^{36}Cl (M_{\odot})	^{41}Ca (M_{\odot})
	10.1 ^e	1.59e-05	8.98e-06	2.95e-3	5.46e-3	1.17e-05	7.88e-08	2.57e-07
	12.2 ^e	1.59e-05	9.06e-06	2.95e-3	5.53e-3	1.18e-05	7.94e-08	2.60e-07
	30.3^e	1.59e-05	8.42e-06	2.95e-3	4.67e-3	1.16e-05	6.74e-08	2.20e-07
	75.4 ^e	1.59e-05	9.33e-06	2.95e-3	6.05e-3	1.15e-05	8.95e-08	2.87e-07
35	...	1.85e-05	6.77e-06	3.44e-3	1.27e-3	8.44e-06	4.70e-16	1.96e-15
	2.9 ^d	1.85e-05	6.80e-06	3.44e-3	1.27e-3	1.20e-06	1.86e-22	1.50e-21
	8.8^e	1.85e-05	1.84e-05	3.44e-3	2.31e-2	1.87e-05	4.84e-07	1.35e-06
	10.6 ^e	1.85e-05	1.81e-05	3.44e-3	2.24e-2	1.82e-05	4.83e-07	1.31e-06
	12.7 ^e	1.85e-05	1.86e-05	3.44e-3	2.21e-2	1.84e-05	4.75e-07	1.30e-06
	31.5^e	1.85e-05	1.68e-05	3.44e-3	2.03e-2	1.79e-05	4.55e-07	1.21e-06
	78.6 ^e	1.85e-05	1.54e-05	3.44e-3	1.90e-2	1.73e-05	4.39e-07	1.16e-06
40	...	2.11e-05	7.06e-06	3.93e-3	1.36e-3	1.88e-05	7.99e-11	4.02e-10
	3.1 ^d	2.11e-05	7.13e-06	3.93e-3	1.33e-3	2.20e-06	2.64e-22	4.51e-21
	7.6^e	2.11e-05	2.42e-05	3.93e-3	3.72e-2	2.74e-05	9.07e-07	2.30e-06
	15.8 ^e	2.11e-05	2.17e-05	3.93e-3	3.44e-2	2.66e-05	8.81e-07	2.18e-06
	20.4 ^e	2.11e-05	2.19e-05	3.93e-3	3.47e-2	2.64e-05	8.91e-07	2.21e-06
	32.8^e	2.11e-05	2.15e-05	3.93e-3	3.44e-2	2.60e-05	8.96e-07	2.19e-06
	81.7 ^e	2.11e-05	1.54e-05	3.93e-3	2.65e-2	2.40e-05	7.81e-07	1.75e-06
45	...	2.38e-05	7.40e-06	4.42e-3	5.18e-3	2.94e-05	1.45e-07	2.44e-07
	3.2 ^d	2.38e-05	7.41e-06	4.42e-3	1.39e-3	3.43e-06	3.43e-22	9.69e-21
	6.5^e	2.38e-05	2.62e-05	4.42e-3	5.19e-2	3.64e-05	1.41e-06	3.44e-06
	7.8 ^a	2.38e-05	7.40e-06	4.42e-3	1.41e-3	2.73e-05	9.51e-19	7.77e-18
	19.5 ^e	2.38e-05	2.39e-05	4.42e-3	4.91e-3	3.61e-05	1.40e-06	3.22e-06
	23.4 ^e	2.38e-05	2.36e-05	4.42e-3	4.92e-3	3.59e-05	1.41e-06	3.23e-06
	42.0^e	2.38e-05	2.14e-05	4.42e-3	4.64e-3	3.52e-05	1.37e-06	3.08e-06
	69.9 ^e	2.38e-05	1.7e-05	4.42e-3	3.98e-3	3.34e-05	1.27e-06	2.68e-06
50	...	2.64e-05	7.82e-06	4.91e-3	1.21e-2	4.00e-05	4.18e-07	6.89e-07
	8.1^e	2.64e-05	2.56e-05	4.91e-3	6.57e-2	4.9e-05	1.95e-06	4.36e-06
	14.0 ^e	2.64e-05	2.50e-05	4.91e-3	6.83e-2	4.79e-05	2.04e-06	4.56e-06
	21.7 ^e	2.64e-05	2.44e-05	4.91e-3	6.62e-2	4.73e-05	2.01e-06	4.43e-06
	29.1^e	2.64e-05	2.32e-05	4.91e-3	6.26e-2	4.71e-05	1.95e-06	4.22e-06
	72.3 ^e	2.64e-05	1.70e-05	4.91e-3	5.21e-2	4.40e-05	1.77e-06	3.54e-06
	144.6 ^e	2.64e-05	1.07e-05	4.91e-3	3.33e-2	4.09e-05	1.26e-06	2.21e-06
60	...	3.17e-05	9.00e-06	5.89e-3	3.84e-2	6.65e-05	1.48e-06	2.42e-06
	3.5 ^d	3.17e-05	8.02e-06	5.89e-3	1.52e-3	7.22e-06	6.99e-22	5.88e-20
	7.2^e	3.17e-05	8.88e-06	5.89e-3	3.57e-2	6.27e-05	1.37e-06	2.23e-06
	14.9 ^e	3.17e-05	2.44e-05	5.89e-3	9.97e-2	7.29e-05	3.32e-06	6.96e-06
	17.8 ^e	3.17e-05	2.42e-05	5.89e-3	9.88e-2	7.28e-05	3.31e-06	6.89e-06
	37.0^e	3.17e-05	2.26e-05	5.89e-3	9.44e-2	7.19e-05	3.24e-06	6.59e-06
	92.2 ^e	3.17e-05	1.23e-05	5.89e-3	6.16e-2	6.55e-05	2.37e-06	4.14e-06
70	...	3.70e-05	9.21e-06	6.88e-3	5.58e-2	9.70e-05	2.10e-06	3.46e-06
	39.1^e	3.70e-05	1.83e-05	6.88e-3	1.12e-2	1.03e-4	4.19e-06	7.76e-06
80	...	4.23e-05	1.49e-05	7.86e-3	0.14	1.51e-4	5.40e-06	9.55e-06
	33.9^e	4.23e-05	1.74e-05	7.86e-3	0.14	1.46e-4	5.34e-06	9.59e-06

Notes. M_{ini} is the initial mass in M_{\odot} , and P_{ini} is the initial period of the binary system in days. For the stable isotopes, the initial amount present in the star is given. For the radioactive isotopes, the yields are not corrected for radioactive decay that might take place during the evolution of the star. The top lines for each mass give the nonrotating single-star yields from Paper II. The periods printed in boldface indicate the models used as representative for Case A and Case B mass transfer in Section 3.

^a This run was terminated before the core collapse owing to numerical difficulties.

^b This primary star has lost such a significant amount of mass that its final state will be a white dwarf.

^c The final core mass of this star is such that it is a potential electron-capture supernova.

^d Terminated owing to the formation of a common envelope.

^e The primary star of this system was uncoupled and further evolved as a single star as the secondary overflows its Roche lobe.

Table 3Wind Yields in M_{\odot} for the Binary Models for ^{26}Al , ^{36}Cl , and ^{41}Ca Illustrating the Effect of Different Mass-loss Prescription on Stars near the Lower-mass W-R Limit

M_{ini} (M_{\odot})	P_{ini} (days)	Wind	^{26}Al (M_{\odot})	Ratio	^{36}Cl (M_{\odot})	Ratio	^{41}Ca (M_{\odot})	Ratio
10	2.8	Set 1	3.74e-08	...	1.01e-07	...	2.44e-07	...
	4.9	Set 1	1.02e-07	...	2.05e-08	...	8.45e-08	...
	13.1	Set 1	1.01e-07	...	4.61e-09	...	2.04e-08	...
	2.8	Set 2	3.81e-07	10.19	4.32e-09	0.04	1.53e-08	0.06
	4.9	Set 2	1.60e-07	1.57	4.28e-09	0.21	1.97e-08	0.23
	13.1	Set 2	1.29e-07	1.28	1.16e-12	2.52e-4	5.52e-12	2.71e-4
	3.8	Set 3	3.90e-07	0.65	1.03e-20	5.69e-6	1.35e-19	1.94e-5
	6.7	Set 3	1.92e-07	0.41	4.40e-21	2.43e-6	6.61e-20	5.33e-6
	16.8	Set 3	1.75e-07	0.38	4.14e-21	1.52e-6	6.11e-20	5.61e-6
15	3.8	Set 1	6.04e-07	...	1.81e-15	...	6.96e-15	...
	6.7	Set 1	4.71e-07	...	3.12e-15	...	1.24e-14	...
	16.8	Set 1	4.58e-07	...	2.73e-15	...	1.09e-14	...
	3.8	Set 2	3.90e-07	0.65	1.03e-20	5.69e-6	1.35e-19	1.94e-5
	6.7	Set 2	4.69e-07	0.99	3.06e-15	0.97	1.22e-14	0.98
	16.8	Set 2	4.58e-07	1	2.73e-15	1	1.09e-14	1
	3.8	Set 3	3.90e-07	0.65	1.03e-20	5.69e-6	1.35e-19	1.94e-5
	6.7	Set 3	1.92e-07	0.41	4.40e-21	2.43e-6	6.61e-20	5.33e-6
	16.8	Set 3	1.75e-07	0.38	4.14e-21	1.52e-6	6.11e-20	5.61e-6

Note. M_{ini} is the initial mass in M_{\odot} , and P_{ini} is the initial period of the binary system in days. The third column gives the type of wind used, where Set 1 stands for using the mass-loss prescription by Nugis & Lamers (2000) for the W-R star, Set 2 stands for using the mass-loss prescription by Vink (2017) for helium cores smaller than $4 M_{\odot}$, and Set 3 stands for using the same prescription for helium cores smaller than $5 M_{\odot}$. The yields are not corrected for radioactive decay that might take place during the evolution of the star.

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