



Probing FeSi, a *d*-electron topological Kondo insulator candidate, with magnetic field, pressure, and microwaves

Alexander J. Breindel^a, Yuhang Deng^a, Camilla M. Moir^a, Yuankan Fang^a, Sheng Ran^{a,1}, Hongbo Lou^b, Shubin Li^{b,c}, Qiaoshi Zeng^b, Lei Shu^{d,e}, Christian T. Wolowiec^a, Ivan K. Schuller^a, Priscila F. S. Rosa^f, Zachary Fisk^g, John Singleton^f, and M. Brian Maple^{a,2}

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Recently, evidence for a conducting surface state (CSS) below 19 K was reported for the correlated *d*-electron small gap semiconductor FeSi. In the work reported herein, the CSS and the bulk phase of FeSi were probed via electrical resistivity ρ measurements as a function of temperature T , magnetic field B to 60 T, and pressure P to 7.6 GPa, and by means of a magnetic field-modulated microwave spectroscopy (MFMMS) technique. The properties of FeSi were also compared with those of the Kondo insulator SmB₆ to address the question of whether FeSi is a *d*-electron analogue of an *f*-electron Kondo insulator and, in addition, a “topological Kondo insulator” (TKI). The overall behavior of the magnetoresistance of FeSi at temperatures above and below the onset temperature $T_S = 19$ K of the CSS is similar to that of SmB₆. The two energy gaps, inferred from the $\rho(T)$ data in the semiconducting regime, increase with pressure up to about 7 GPa, followed by a drop which coincides with a sharp suppression of T_S . Several studies of $\rho(T)$ under pressure on SmB₆ reveal behavior similar to that of FeSi in which the two energy gaps vanish at a critical pressure near the pressure at which T_S vanishes, although the energy gaps in SmB₆ initially decrease with pressure, whereas in FeSi they increase with pressure. The MFMMS measurements showed a sharp feature at $T_S \approx 19$ K for FeSi, which could be due to ferromagnetic ordering of the CSS. However, no such feature was observed at $T_S \approx 4.5$ K for SmB₆.

Kondo insulator | topological insulator | conducting surface state | pressure-induced metallization | magnetoresistance

Recently, electrical resistivity measurements on high-quality single crystals of the correlated *d*-electron small gap semiconductor FeSi revealed a cross-over from semiconducting to metallic behavior below ~ 19 K (1). The metallic behavior was attributed to the emergence of a conducting surface state (CSS) below an onset temperature $T_S \approx 19$ K, suggesting that FeSi could be a topological insulator (1). The correlated *d*-electron compound FeSi (2–4) has attracted much interest for more than six decades because of its unusual electrical and magnetic properties (e.g., refs. 4–14), which are reminiscent of those of *f*-electron Kondo insulators. This has led to the proposal that FeSi is a *d*-electron counterpart of an *f*-electron Kondo insulator (e.g., refs. 7, 13, and 15).

Originally called “hybridization gap semiconductors” because the energy gap is produced by hybridization of localized *f* and conduction electron states (16–18), “Kondo insulators” (19) comprise a set of small gap semiconducting compounds based on lanthanide and actinide elements such as Ce, Sm, Yb, and U with partially filled *f*-electron shells and an unstable valence (18–22). The members within this group that were first identified are the Sm compounds SmB₆ (21, 23) and SmS in its collapsed “gold phase” (24, 25). In both SmB₆ and the gold phase of SmS, Sm has an intermediate valence of ~ 2.7 and a nonmagnetic ground state that was attributed to “valence fluctuations” (25–29). This was followed by discoveries of Ce-, Yb-, and U-based Kondo insulators starting with CeFe₄P₁₂ (20), YbB₁₂ (22), and UFe₄P₁₂ (20). Kondo insulators have also been proposed to be topological insulators on theoretical grounds (15, 30), and mounting evidence during the past several years indicates that one of the original and most extensively investigated Kondo insulators, SmB₆, is a “topological Kondo insulator” (TKI) with a CSS that dominates electrical conductivity below $T_S \approx 4.5$ K (31–39).

The discovery of a CSS below $T_S \approx 19$ K in FeSi and the similarity of many of its properties to those of SmB₆ suggests that FeSi may also be a TKI (1). Topological materials have gained much attention in recent years owing to the possibility that topological superconductors, as well as strong topological insulators in proximity to *s*-wave superconductors, can act as hosts for Majorana modes, which have applications in quantum computing (40). If FeSi is indeed a TKI, it could be an attractive candidate for potential applications in spintronics and quantum computing since it is comprised of elements that are relatively inexpensive and compatible with Si-based electronics.

Significance

The properties of the correlated electron small gap semiconductor FeSi are reminiscent of those of a small class of lanthanide- and actinide-based compounds known as Kondo insulators. This led to the conjecture that FeSi may be a *d*-electron counterpart of an *f*-electron Kondo insulator. We recently reported evidence for a conducting surface state (CSS) in FeSi below 19 K that suggests that FeSi may be a “topological” Kondo insulator. In this work, we probed FeSi with magnetic field, pressure, and microwaves. The studies involving magnetic field and pressure yielded similar behavior to those on the putative topological Kondo insulator SmB₆. The magnetic field-modulated microwave spectroscopy measurements revealed a sharp feature at the CSS onset, possibly of magnetic origin.

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The authors declare no competing interest.

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¹Present address: Department of Physics, Washington University in Saint Louis, Saint Louis, MO 63130.

²To whom correspondence may be addressed. Email: mbmaple@ucsd.edu.

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In this work, we have probed the CSS and bulk properties of FeSi with high magnetic fields up to 60 T, high pressures up to 7.6 GPa, as well as microwaves via the magnetic field-modulated microwave spectroscopy (MFMMS) technique (41). We have compared the properties of FeSi with those of the Kondo insulator SmB_6 to address the question of whether FeSi is a d -electron analogue of an f -electron Kondo insulator and, in addition, a TKI. This has also involved making additional magnetoresistance (MR) measurements on SmB_6 . In the initial work on FeSi, we found that the temperature T dependence of the electrical resistance $R(T)$ of high-quality single crystals exhibits semiconducting behavior above 19 K, which can be described by a standard activation model with a two-gap feature at higher temperatures and metallic behavior below 19 K (1). The observation that the normalized electrical resistance $R(T)/R(120\text{ K})$ below 19 K shows a dependence on the dimensions of the FeSi specimens along with the absence of any features in the specific heat at 19 K, indicated the presence of a CSS (1). Recent research employing scanning tunneling microscopy on high-quality FeSi single crystals supports the existence of surface conductivity of FeSi and further illustrates the similarity of its correlated electron properties to those of SmB_6 (42). Electrical transport, magnetization, and polarized neutron reflectometry measurements on FeSi nanofilms revealed a ferromagnetic metallic surface state closely related to the “Zak phase” of the bulk band topology of FeSi (43). The realization of the unidirectional MR and the current-induced magnetization switching corroborates the spin-momentum locking in FeSi (43). These new discoveries utilizing novel types of characterization support our claim that FeSi has a CSS and suggest FeSi’s potential use in spintronic functionalities.

Results and Discussion

Evidence for a CSS. Evidence for a CSS below $T_S \approx 19\text{ K}$ in a high-quality flux-grown single crystal of FeSi was reported in ref. 1. In figure 3 of ref. 1, it was shown that $\rho(T)$ in the metallic region below 19 K decreases systematically with decreasing average radius r of an approximately rod-shaped FeSi single crystal of length L as the surface area A to volume V ratio, $A/V = (2\pi rL)/(\pi r^2L) = 2/r$ increases. This indicates that the contribution to the overall conductivity of the CSS is larger than that of the bulk small gap semiconducting portion of the crystal. Assuming the CSS is confined to a cylindrical shell of radius r and effective thickness t , the normalized electrical resistance $R(T)/R(120\text{ K})$ in the metallic region below $T_S \approx 19\text{ K}$ can be expressed as $R(T)/R(120\text{ K}) = \rho_m(T)/(L/2\pi rt)/\rho_s(120\text{ K})/(L/\pi r^2) = [\rho_m(T)/\rho_s(120\text{ K})]/(r/2t) \propto r$, where $\rho_m(T)$ is the electrical resistivity in the metallic region below T_S , and $\rho_s(120\text{ K})$ is the electrical resistivity in the semiconducting region at 120 K. Thus, at fixed T , one expects the normalized electrical resistance $R(T)/R(120\text{ K})$ to decrease linearly with decreasing r as the sample is thinned, and the CSS region contributes more to the conductivity. In the semiconducting region above 19 K, where the surface state contribution is negligible, $R(T)/R(120\text{ K}) = \rho_s(T)/(L/\pi r^2)/\rho_s(120\text{ K})/(L/\pi r^2) = \rho_s(T)/\rho_s(120\text{ K})$ is independent of r , and all of the normalized $R(T)$ curves collapse onto one another. This behavior is illustrated in Fig. 1 in the plot of $R(T)/R(120\text{ K})$ vs. average diameter $D = 2r$ of an approximately cylindrical rod-shaped sample of FeSi at 8 different temperatures between 2 K and 30 K (from the data reported in figure 3 of ref. 1).

MR Measurements. Fig. 2 shows the transverse electrical resistance $R_\perp$ vs. B , measured with the magnetic field B perpendicular to the direction of the current, for a single crystalline FeSi specimen at various temperatures T between 0.7 K and 27 K. The measurements

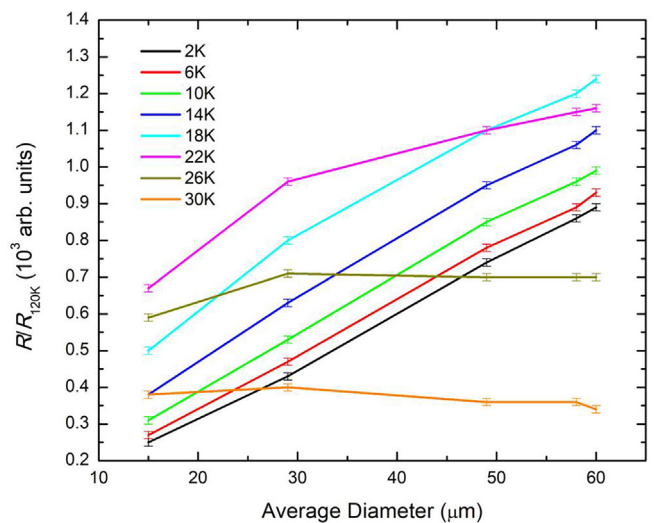


Fig. 1. Electrical resistance R , normalized to its value at 120 K, vs. the average diameter of an approximately cylindrical rod-shaped sample of FeSi, from the data reported in ref. 1. Error bars are included to account for errors in the data retrieval. The linearity of the plots suggests the formation of a CSS below around 19 K, because of the increased surface area to volume ratio associated with thinning the samples (1).

were performed upon field upswing and downswing, and the downswing data were presented because there could be a jump in the resistivity at the beginning of the pulse due to the large dB/dt . There is a small positive MR region at low magnetic fields, followed by a negative MR region at higher fields. The transition field B_m between these two regions is defined as the field where the curvature in $R_\perp(T)$ changes from negative to positive. A plot of B_m vs. T displayed in the inset of the B - T plot in Fig. 2 shows that B_m decreases with T and bends over and appears to extrapolate to zero at a value of T near $T_S \approx 19\text{ K}$, the onset temperature of the CSS (1); however, within the experimental uncertainty, B_m saturates to a value of $\sim 0.5\text{ T}$ at 20 K and 27 K.

The $R_\perp$ vs. B curves also reveal that $R_\perp$ exhibits a maximum as a function of T at $T_S \approx 20\text{ K}$, as can be seen more clearly in Fig. 3. This weak dependence of T_S on B is represented by the nearly vertical line in the inset of Fig. 2. The lines representing $B_m(T)$ and $T_S(B)$ in Fig. 2 divide the B - T plane into three regions—CSS, $dR/dT > 0$, positive MR , $MR > 0$ (except for the two lowest temperatures of 0.7 K and 1.47 K), where $MR \equiv [R(B) - R(0)]/R(0)$ (lower left); CSS, $dR/dT > 0$ with $MR < 0$ (upper right), Kondo insulator state (KIS), $dR/dT < 0$ with $MR < 0$ (far right). The positive MR within the CSS could be due to the metallic character of the CSS, while the negative MR within the CSS could be associated with a decrease in the energy gap of the semiconducting state of bulk FeSi and a suppression of the CSS with increasing B .

The transverse resistance $R_\perp$ is compared with the longitudinal resistance $R_\parallel$ vs. B , measured with the magnetic field B parallel to the direction of the current, vs. B at two temperatures below T_S , 0.7 K and 10 K, in Fig. 4. A schematic of the geometry of the transverse $R_\perp$ and longitudinal $R_\parallel$ resistance measurements, where the magnetic field is oriented perpendicular and parallel to the longitudinal axis of the sample, respectively, is shown in the inset of Fig. 4. It is clear from the data in Fig. 4 that there is significant anisotropy in the resistance R vs. B associated with the surface state, despite the cubic crystal structure of FeSi (1). These results are consistent with our previously published MR data on FeSi samples, and, as explained in our previous work, the difference caused by the change in field orientation can be understood as a

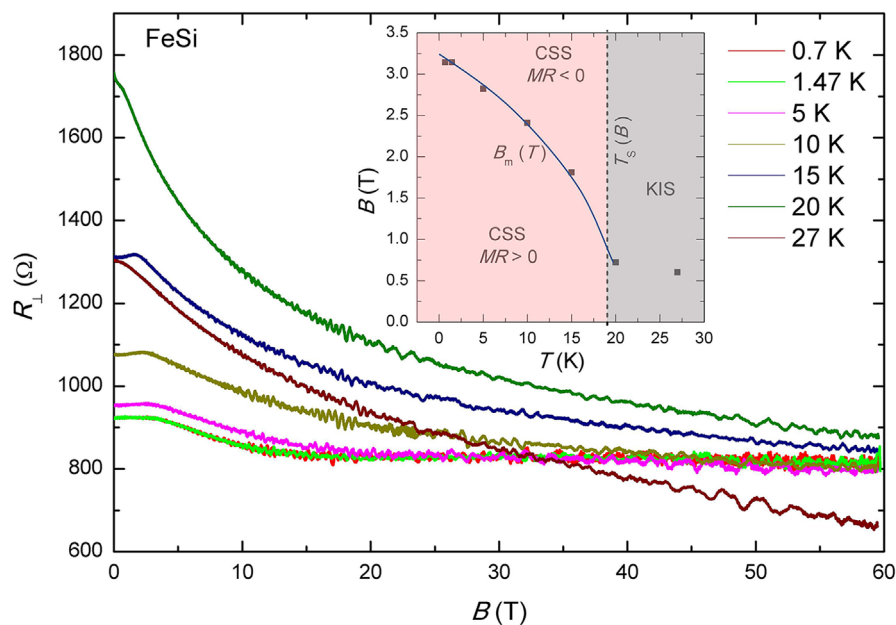


Fig. 2. Transverse electrical resistance $R_{\perp}$, measured with the magnetic field B perpendicular to the direction of the current, vs. B at various temperatures T between 0.7 K and 27 K. The data presented here were from field downsweep. There is a small positive MR region at low magnetic fields, followed by a negative MR region at higher fields. The transition field B_m between these two regions is defined as the field where the curvature in $R_{\perp}(T)$ changes from negative to positive. *Inset:* B - T plot in which the curves $B_m(T)$ and $T_s(B)$ divide the B - T plane into three regions—CSS, $dR/dT > 0$ with $MR > 0$ (Lower Left); CSS, $dR/dT > 0$ with $MR < 0$ (Upper Right); KIS, $dR/dT < 0$ with $MR < 0$ (far right). The meaning of the symbols in the *Inset* of Fig. 2 are as follows: CSS – conducting surface state, KIS – Kondo insulator state, and $MR \equiv [R(B) - R(0)]/R(0) - MR$.

consequence of a positive field response of the contribution of the surface conductivity to the overall MR (1).

MR measurements performed on SmB_6 samples show evidence of a cross-over at about 4.5 K, as can be seen in Fig. 5B, similar to those shown in Chen et al. (37). Based on the data for FeSi from Fang et al. (1), we see the same minimum in the MR (Fig. 5A).

The field-dependent data for the MR at various temperatures are shown for SmB_6 in Fig. 5D taken from Chen et al. (37) and for FeSi in Fig. 5C, based on the data shown in Fig. 2. In both FeSi and SmB_6 , there is a large temperature dependence of the MR (gray and pink regions) in Fig. 5A and B around their respective CSS onset temperatures T_s . Similar behavior for FeSi and SmB_6

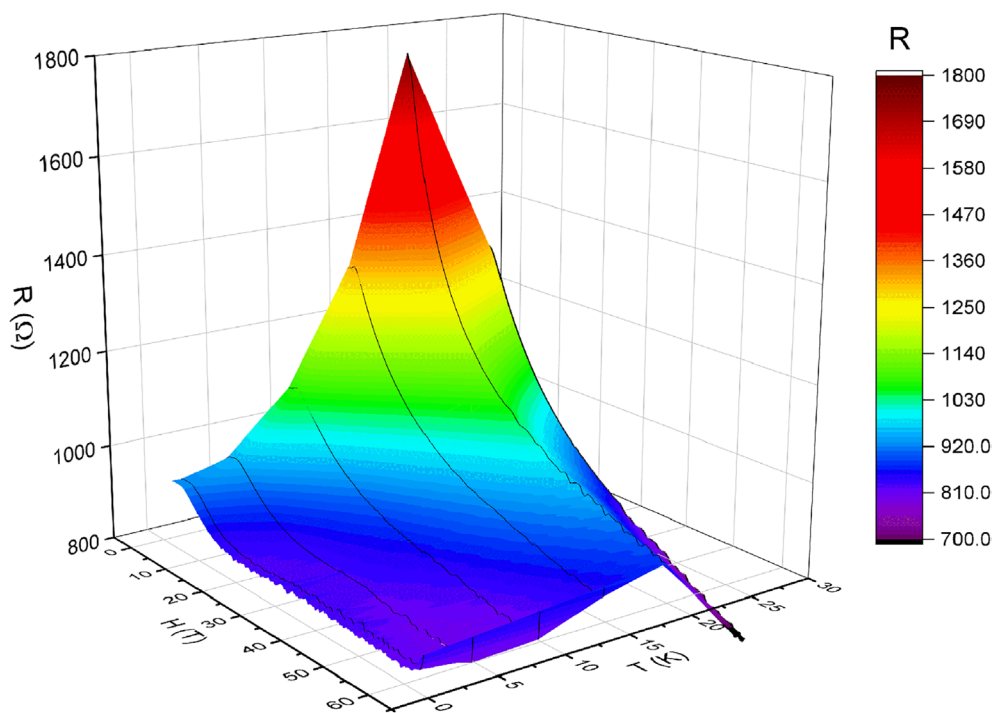


Fig. 3. 3D surface plot derived from the transverse resistance $R_{\perp}$ vs. magnetic field B and temperature T data shown in Fig. 2. There is a clear peak in the $R_{\perp}(T)$ data around 20 K for all fields, associated with the transition to the CSS (1), as well as a peak in the $R_{\perp}(B)$ data associated with the change in MR from positive for the CSS to negative for the semiconducting bulk KIS state.

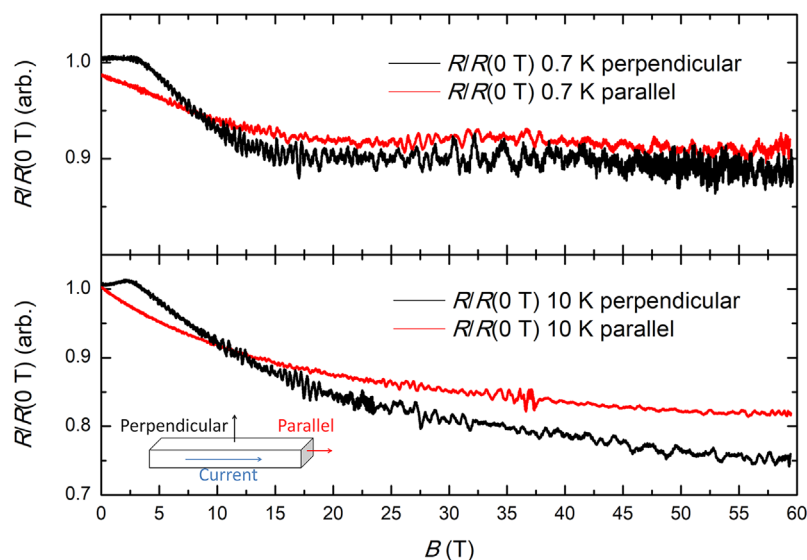


Fig. 4. Anisotropic electrical resistance $R(B)$, normalized to the value of R at $B = 0$ T, $R/R(0$ T), vs. magnetic field B curves at 0.7 K (Top) and 10 K (Bottom). The geometries used in the $R(B)/R(0$ T) measurements are shown in the *Inset*. The current is directed along the longitudinal axis of the FeSi single crystal. The transverse resistance $R_{\perp}$ (black curves) and longitudinal resistance $R_{\parallel}$ (red curves) were measured with the magnetic field perpendicular and parallel to the longitudinal axis of the FeSi single crystal, respectively. The longitudinal axis of the FeSi single crystal corresponds to the [111] direction of the cubic crystal structure.

can also be seen in the field dependence of the MR where below (above) T_S , there is a weak (strong) dependence of MR on field.

High-Pressure Studies and P-T Phase Diagram. Shown in Fig. 6 are the T -dependent resistance $R(T)$ curves for FeSi from 2 K to room temperature at various pressures up to 7.6 GPa. There is a persistent peak in the resistance around 20 K for all pressures except 7.6 GPa signifying the striking change in the transport

behavior of FeSi at T_S . On the higher temperature side of the peak in $R(T)$, the FeSi sample exhibits semiconducting-like behavior with $dR/dT < 0$, whereas on the lower temperature side, the sample displays metallic behavior ($dR/dT > 0$). The same phenomenon has been observed at ambient pressure (1) and has been attributed to the emergence of the CSS in FeSi below the temperature T_S at which the peak in $R(T)$ occurs. As the pressure is increased to 7.6 GPa, the well-defined peak in $R(T)$ vanishes, and the resistance

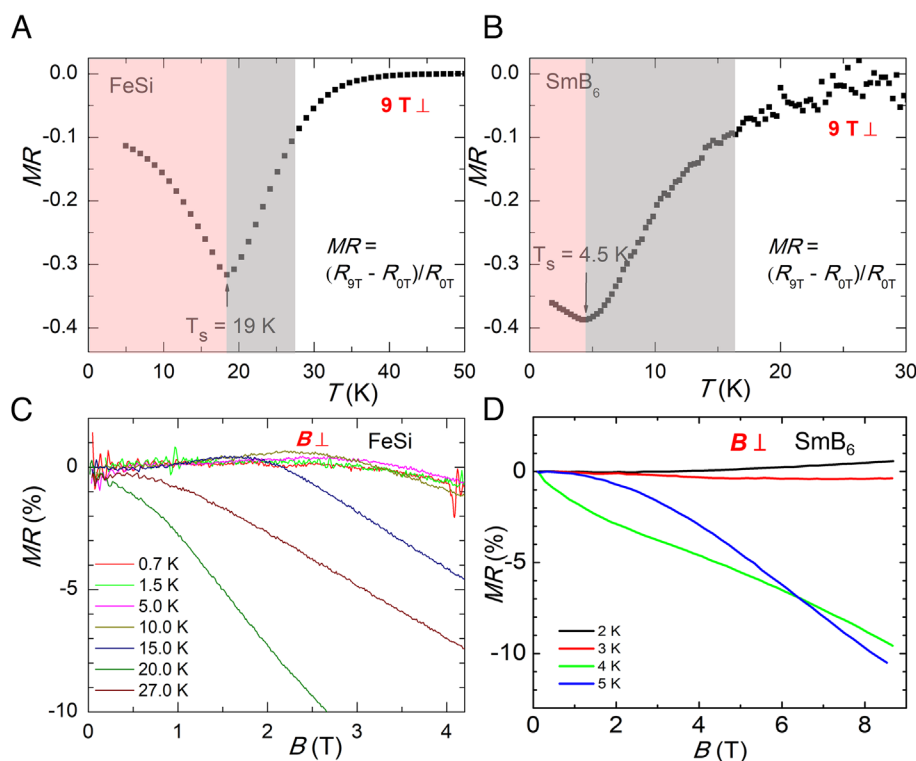


Fig. 5. Comparison of the MR of FeSi and SmB_6 as a function of temperature T through T_S at a magnetic field $B = 9$ T [A and B] and as a function of B at various values of T below and above T_S [C and D]. The MR is defined as $MR = [R(B) - R(0$ T)] / $R(0$ T), where B is the applied magnetic field. Data in A are from Fang et al. (1), in B from this work, in C from this work (data in Fig. 2), and in D from Chen et al. (37).

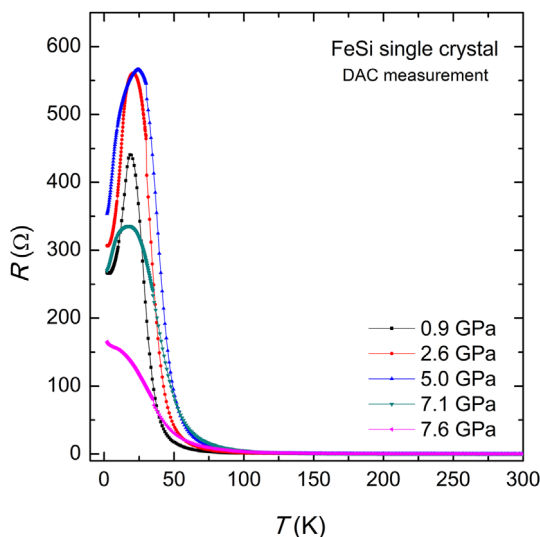


Fig. 6. Electrical resistance R vs. temperature T for an FeSi single crystal at various pressures up to 7.6 GPa measured in DAC experiments.

of the sample continues to increase as T is reduced to a base temperature of 2 K. This suggests the occurrence of a pressure-induced transition from metallic to insulating-like behavior of the surface state at this pressure. The B20 crystal structure of FeSi (ϵ -FeSi) is quite stable under high pressure. At room temperature, no phase transition was observed to at least 36 GPa. Even with laser heating to above 1,000 K, the high-pressure B2 phase (CsCl type FeSi) persists to pressures at least above 14 GPa (44, 45). Consequently, the pressure-induced change in $R(T)$ of FeSi at 7.6 GPa could be ascribed to an electronic phase transition, and independent of any structural transition.

As noted above, in many reports (7, 13, 15, 19, 46) it has been proposed that FeSi is a d -electron Kondo insulator. For a Kondo insulator, a narrow hybridization gap (16, 18) (Kondo gap) develops below a characteristic temperature called the Kondo temperature (T_K), because of the coherent spin-dependent scattering of itinerant electrons by the lattice of d - or f -electron localized magnetic moments. This Kondo scenario is partly consistent with what we found for the $R(T)$ behavior of FeSi. As shown in Fig. 7, T_K is defined as the temperature below which the resistance can be described by a gapped semiconducting activation model. The energy gap Δ has been extracted from an Arrhenius law,

$$R = R_0 \exp(\Delta / 2k_B T), \quad [1]$$

where R_0 is a constant. The energy gap Δ can be taken from the slope of the linear portion of a plot of $\ln R$ vs. $1/T$. This is illustrated in the $\ln R$ vs. $1/T$ plot in Fig. 7 based on measurements of $R(T)$ for FeSi at 0.9 GPa. The linear region from 70 K to 160 K (T_K) corresponds to an energy gap $\Delta_1 = 57$ meV, while the linear region from 37 K to 57 K yields an energy gap $\Delta_2 = 36$ meV. Thus, at 0.9 GPa, $R(T)$ of FeSi evolves from a nonactivated regime at $T_K = 160$ K to an activated regime characterized by an energy gap $\Delta_1 = 57$ meV, then to another activated regime characterized by a smaller energy gap $\Delta_2 = 36$ meV, and finally to a regime involving a CSS below $T_S = 19$ K.

The pressure dependences of both energy gaps are plotted in Fig. 8A. The energy gaps initially increase with pressure and then begin to decrease around 7 GPa. Correspondingly, in Fig. 6 it can be seen that the peak resistance also first increases and then decreases with increasing pressure, a direct result from the change in the energy gaps under pressure. Furthermore, there is a

correspondence of the suppression of the energy gap and the drop in T_S , indicated by the vertical dashed line in Fig. 8. The closing of the energy gaps is correlated with the disappearance of the CSS in FeSi. The pressure dependence of the Kondo temperature and the temperature T_S of the onset of the CSS, $T_K(P)$ and $T_S(P)$, for the single crystalline FeSi sample are plotted in a T vs. P phase diagram in Fig. 8B. Above T_K , the sample can be characterized as a bad metal (37) in which itinerant electrons are incoherently scattered by the d -electron localized magnetic moments, yielding a very high resistivity compared with that of a simple metal. Between T_K and T_S , FeSi is expected to be a Kondo insulator, whereas below T_S , a CSS appears, as discussed in our earlier publication (1).

Since the proposal of a TKI in 2010 (15), the f -electron Kondo insulator SmB₆ was considered a prime candidate. In addition to the many common attributes shared by FeSi and SmB₆, we have found that these two compounds display similar electrical transport properties at both ambient and high pressure, providing further evidence that FeSi is a d -electron analogue of the f -electron Kondo insulator SmB₆. At ambient pressure, Chen et al. also observed two-gap-semiconducting behavior in high-quality SmB₆ at intermediate temperatures and a CSS below 5 K (37). At high pressures, this study reveals that the energy gaps of FeSi increase with pressure before they start to fall upon increasing pressure above 7 GPa. In 1997, Bauer et al. (47) also reported an increase in the energy gap of FeSi under pressures up to 1.3 GPa, with no indication of metallization even at 9.4 GPa. In 2019, Hearne et al. observed a monotonic decrease in the energy gap of powdered polycrystalline FeSi. The gap closed above 15 GPa, accompanied by a residual electrical resistance that saturated in the same pressure region, pointing to a pressure-induced metallic state in FeSi (48). The reason for these discrepancies is not known, but could be due to differences in sample quality or pressure inhomogeneity between

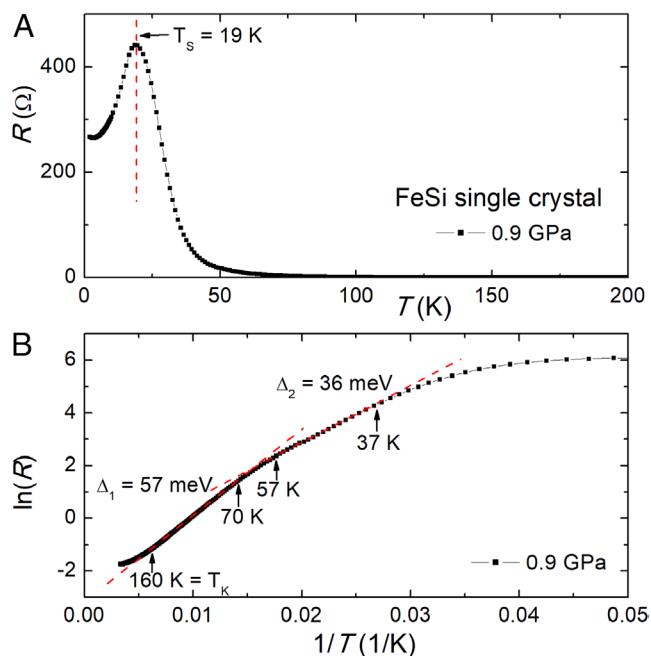


Fig. 7. (A) A representative plot of $R(T)$ at $P = 0.9$ GPa illustrating the location of T_S at the peak in $R(T)$ marked by the vertical dashed red line. (B) A plot of $\ln R$ vs. $1/T$ that allows for the extraction of the energy gaps Δ_1 (in the temperature range $T_K = 160$ to 70 K) and Δ_2 (in the range $T = 57$ to 37 K) according to an Arrhenius law. Within each region, $R(T)$ is fitted with an Arrhenius law (See Eq. (1) and discussion in text). The same procedure was used to determine the two energy gaps Δ_1 and Δ_2 at different pressures based on $R(T)$ measurements performed in PCC and DAC experiments.

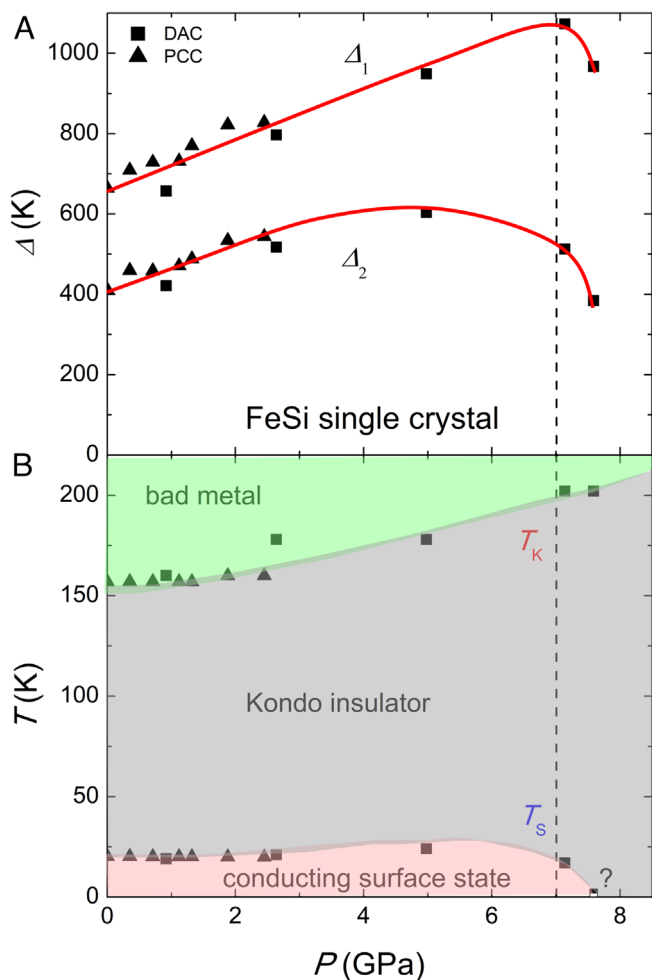


Fig. 8. (A) Evolution of the two energy gaps Δ_1 and Δ_2 with pressure obtained from electrical resistivity measurements in PCC and DAC experiments. (B) T - P phase diagram for the FeSi single crystal. The red lines in A and the boundaries between different phases are guides to the eye. The question mark in the lower right of the panel indicates the estimation of T_S at 7.6 GPa.

these experiments. Extending the pressure range for FeSi is our future goal to determine the pressure at which the energy gaps vanish. The closure of the Kondo gap at similar critical pressures (4 to 7 GPa), accompanied by a fundamental change in $R(T)$ for SmB_6 has been reported by several groups (49–53).

Using the Anderson lattice model for a Kondo insulator, the indirect hybridization gap obtained by fitting the activation behavior of $R(T)$ is of the order of V^2/D , where V is the hybridization energy between the localized d - or f - and conduction electron states and D is the half bandwidth of the conduction band. Both V and D are expected to increase asymptotically with decreasing interatomic distance with increasing pressure. This asymptotic behavior is complicated by the node in the Si $3p$ radial wave function and the angular dependence of the atomic wave functions. A nonmonotonic pressure dependence of the Kondo gap may appear because of this complication or the periodic Anderson lattice model is not applicable to this situation. At sufficiently high pressure, the hybridization and the hybridization gap would finally vanish, supported by the observations of the gap closure in SmB_6 and $\text{Ce}_3\text{Bi}_4\text{Pt}_3$ (54, 55), two typical Kondo insulators. For FeSi, the scenario is even more complicated because the $3d$ state is less localized than the $4f$ state. It would be interesting to explore whether the gaps in FeSi under pressure would finally collapse, since this might clarify the validity of the hybridization model for this d -electron counterpart of a Kondo insulator.

MFMMs. To gain further information about the transition to a CSS at 19 K in FeSi, MFMMs measurements were performed on single crystals of FeSi as a function of temperature from 4 K to 100 K in both zero field as well as in an applied DC magnetic field of 500 Oe, the results of which are shown in Fig. 9. In zero field, there are two sharp peaks with an onset of the upper peak at approximately 19 K (Fig. 9A). At an applied DC magnetic field of 500 Oe, the main peak in MFMMs intensity has shifted to higher temperatures with an onset at $T = 21$ K (Fig. 9A).

The peaks in the MFMMs signal observed for single crystalline FeSi are reminiscent of the large peaks observed at the onset of a superconducting transition, where the decrease in the surface resistivity during the superconducting transition is the cause for the spike in microwave absorption. The MFMMs signal for the FeSi samples is somewhat unexpected and remarkable for its occurrence near the onset of the surface state at $T_S = 19$ K. Previous MFMMs experiments on vanadium sesquioxide (V_2O_3), which exhibits a metal to insulator transition with a six order of magnitude change in electrical resistance upon cooling at 160 K, show no peak-like signature associated with the resistivity change (41). Similar signals have been observed in PrSi_2 , which has a ferromagnetic transition at 11 K. In this case, the MFMMs signal appears with a negative phase (41). The only other material which showed a peak similar to that of a superconducting transition was a single crystal sample of GaMnAs , which exhibits an insulator–metal transition coincident with a paramagnetic to ferromagnetic transition (41). Here, the observation of the positive peak-like signal is unique in the FeSi system presented in this paper. Recently, evidence for the formation of a ferromagnetic metallic surface state for FeSi was inferred from electrical transport, magnetization, and polarized neutron reflectometry measurements on FeSi nanofilms and claimed to be closely related to the Zak phase of the bulk band topology of FeSi by Ohtsuka et al. (43). If the FeSi CSS were to display ferromagnetic order, perhaps this could produce a sharp MFMMs signal at T_S in FeSi as it does at the paramagnetic–ferromagnetic insulator–metal transition in GaMnAs . We also note that the increase in the onset temperature of the MFMMs signal occurs in FeSi with magnetic field is consistent with expectations if it was associated with ferromagnetic order.

As a comparison, MFMMs measurements were also performed on two SmB_6 samples in zero applied DC field as shown in Fig. 9B. Unlike FeSi, the SmB_6 MFMMs signal contained no signatures of any transition for $3.8 \text{ K} < T < 100 \text{ K}$. It is possible that the low-temperature limit of the experiment was not low enough to access the transition to the CSS, reported to be at $T_S \approx 4.5$ for SmB_6 , according to resistivity measurements. The absence of any signal in the MFMMs measurement of SmB_6 may be due to the condition of the surface of the SmB_6 sample that was not of sufficiently high quality or that there are differences in the underlying physics between the two compounds.

Concluding Remarks

The CSS and the bulk phase of FeSi were probed via electrical resistivity ρ measurements as a function of temperature T , magnetic field B to 60 T, and pressure P to 7.6 GPa, and by means of a MFMMs technique. The linear plots of $R(T)/R(120 \text{ K})$ vs. the average diameter of an approximately cylindrical rod-shaped sample of FeSi based on the data reported in ref. 1 are consistent with the formation of a CSS below 19 K. The anisotropy of the transverse and longitudinal MR also supports the existence of a surface state below T_S . The overall behavior of the MR of FeSi at temperatures above and below the onset temperature $T_S = 19$ K of the CSS is

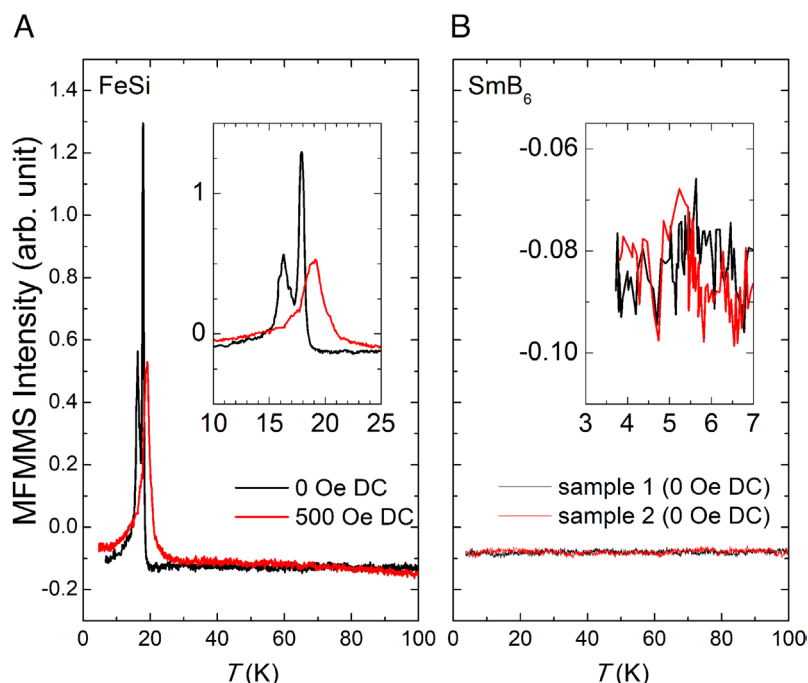


Fig. 9. Temperature dependence of the microwave absorption signal (MFMMS intensity) for both FeSi and SmB₆. (A) FeSi: The MFMMS signal for FeSi at 0 Oe (black) and 500 Oe (red) applied DC magnetic field. The intensity decreases with field and the onset temperature increases from 19 K at 0 Oe to 21 K at 500 Oe. (B) SmB₆: The MFMMS signal for two different SmB₆ samples in zero applied DC field. No peaks were observed for repeated measurements down to 4 K.

similar to that of SmB₆. The behavior of $R(T)$ of FeSi under pressure reveals that the two energy gaps, inferred from the $R(T)$ data in the semiconducting regime, increase with pressure up to about 7 GPa, followed by a drop, which coincides with a sharp suppression of the onset temperature T_S of the CSS. Experiments on SmB₆ yielded a similar collapse of the surface state upon closing the two energy gaps with pressure, but with a decrease in the magnitude of the energy gaps with pressure prior to their collapse (52, 53). The MFMMS measurements showed a sharp feature at the onset of the CSS at $T_S \approx 19$ K for FeSi, which could be due to ferromagnetic ordering of the CSS. However, the absence of a feature at $T_S \approx 4.5$ K for SmB₆ should not be regarded as conclusive for the reasons noted above and will be the subject of a future investigation.

Although there are competing interpretations (56, 57), most researchers regard the Kondo insulator SmB₆ as a topological material (30, 38). The similarity of the electrical and magneto-transport properties of FeSi and SmB₆ found in this work suggests that FeSi is also a Kondo insulator, with evidence for the existence of a CSS and topological behavior. This study may extend the scope of TKIs from f - to d -electron materials.

Recent angle-resolved photoemission spectroscopy (ARPES) measurements on FeSb₂, a material that resembles FeSi in several ways, such as a resistivity plateau below 10 K and a magnetic susceptibility that displays a broad peak near room temperature and vanishes at low temperatures, hint to the formation of a metallic surface state in this narrow gap insulator at low temperatures (58). This indicates that FeSi might not be the only member of a family of d -electron TKIs. Similar high-field, high-pressure, and microwave spectroscopy studies of FeSb₂ would be of interest to see if FeSi and FeSb₂ share other common characteristics. The synthesis of larger and higher quality FeSi single crystals would allow the bulk and surface band structures of FeSi to be further explored by means of ARPES measurements. More sensitive $\rho(B, T)$ measurements at high magnetic fields are planned to revisit the “wiggles” in $\rho(B, T)$ in Fig. 2 above 10 T to see if they are due

to quantum oscillations. Interestingly, quantum oscillations have been observed in the magnetization of the KI SmB₆ by Li et al. (36) and Tan et al. (59), but with strikingly different interpretations of the de Haas-van Alphen (dHvA) frequencies. Li et al. attributed the dHvA oscillations to a 2D CSS, whereas Tan et al. identified the dHvA oscillations with a Fermi surface of neutral quasiparticles within the insulating bulk. Quantum oscillations were also observed in $\rho(B, T)$ and the magnetization in the KI YbB₁₂ by Xiang et al. (60) and ascribed to the insulating bulk. The temperature dependence of the unconventional Shubnikov-de Haas oscillation amplitude followed the conventional Fermi liquid theory of metals with a large effective mass; however, the dHvA oscillations observed in the magnetization had a lighter effective mass. If the wiggles in Fig. 2 can be identified with quantum oscillations, it will be interesting to see how the characteristics of the quantum oscillations in the d -electron TKI candidate FeSi compare with those of the f -electron TKIs SmB₆ and YbB₁₂, and whether they yield new information about the underlying physics responsible for the unusual quantum oscillations in f -electron TKIs and their candidate d -electron counterparts such as FeSi.

Materials and Methods

The FeSi single and SmB₆ single crystals were prepared by means of flux growth methods in tin (1) and aluminum (61, 62) fluxes, respectively. MR measurements were carried out at Los Alamos National High Magnetic Field Laboratory in pulsed fields up to 60 T at temperatures from 0.7 K to 27 K. Electrical resistance measurements at ambient pressure were performed at the University of California San Diego (UC San Diego) in a Quantum Design DynaCool Physical Property Measurement System at temperatures down to 1.8 K and magnetic fields up to 9 T. Electrical resistance measurements under pressure were carried out at the Center for High Pressure Science and Technology Advanced Research in Shanghai with a diamond anvil cell (DAC) and at the UC San Diego with a hydrostatic piston cylinder cell (PCC).

A single crystalline FeSi sample (bar shape, 25 μ m thick and 80 μ m long) was compressed to a maximum pressure of 7.6 GPa in a DAC using diamond anvils, each with a culet size of 300 micrometers. A 300- μ m-thick T301 stainless steel

gasket was preindented to 48 μm , and the indent bottom was removed with a laser. An insulating layer comprised of a mixture of cubic boron nitride (cBN) and epoxy was compressed into the indent. The laser was used again to make a new hole in the cBN layer. The hole was then filled with sodium chloride (NaCl), which served as a good pressure transmitting medium. Several ruby spheres were placed within the NaCl pressure transmitting medium, serving as a pressure gauge. A standard four-point method was used to measure the resistance of the sample under pressure with 4- μm -thick platinum strips as the electrical leads. An AC resistance bridge was used with an amplitude from 0.01 to 0.1 mA, 22- or 33-Hz excitation current. The DAC containing the sample was inserted into a cryostat capable of varying temperatures from 300 K to 2 K and magnetic field from 0 T to 3 T. Pressures were determined at room temperature.

magnetic field component of the TE_{102} mode is at a maximum. The five needle-like FeSi crystals had lengths ranging from 1.15 to 1.9 mm and diameters ranging from 45 to 60 micrometers. Field cooled measurements were performed at various DC fields set with the electromagnet while the sample temperature was swept at a rate of 1 K per minute using an Oxford helium flow cryostat and temperature control. The application of an external ac magnetic field of 15 Oe at 100 KHz and the use of a lock-in amplifier provided an enhanced signal and reduction in noise for the detection of reflected microwave power. All MFMMS measurements of both FeSi and SmB₆ samples were performed at a microwave power of 1 mW.

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Author affiliations: ^aDepartment of Physics, University of California San Diego, La Jolla, CA 92093; ^bCenter for High Pressure Science and Technology Advanced Research, Pudong, Shanghai 201203, People's Republic of China; ^cUniv Lyon, Université Claude Bernard Lyon 1, CNRS, Institut Lumière Matière, Villeurbanne 69100, France; ^dState Key Laboratory of Surface Physics, Department of Physics, Fudan University, Shanghai 200433, People's Republic of China; ^eShanghai Research Center for Quantum Sciences, Shanghai 201315, People's Republic of China; ^fLos Alamos National Laboratory, Los Alamos, NM 87545; and ^gUniversity of California Irvine, Irvine, CA 92697

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