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Two new multinary chalcogenides with $(Se_2)^{2-}$ dimers: $Ba_8Hf_2Se_{11}(Se_2)$ and $Ba_9Hf_3Se_{14}(Se_2)$

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ABSTRACT

Two multinary selenides, Ba₈Hf₂Se₁₁(Se₂) and Ba₉Hf₃Se₁₄(Se₂), with unprecedented structure types have been prepared using high-temperature synthesis techniques and represent the first known compounds in the Ba-Hf-Se system. Their structures were determined from single crystal X-ray diffraction (XRD) data. The Ba₈Hf₂Se₁₁(Se₂) compound crystallizes in the monoclinic C2/c space group with a=12.3962(15) Å, b=12.8928(15) Å, c=12.8928(15) Å 18.1768(17) Å, and $\beta = 90.685(4)^{\circ}$, while Ba₉Hf₃Se₁₄(Se₂) forms in the rhombohedral $R\overline{3}$ space group with a = b= 19.4907(6) Å and c = 23.6407(11) Å. Both have pseudo-zero-dimensional structures with homoatomic Se–Se bonding in the form of $(Se_2)^{2-}$ at distances of 2.400–2.402 Å. The structure of $Ba_8Hf_2Se_{11}(Se_2)$ is comprised of $[Hf_2Se_{11}]^{14-}$, Ba^{2+} , and $(Se_2)^{2-}$ dimers. Conversely, the $Ba_9Hf_3Se_{14}(Se_2)$ structure contains a novel perovskitetype cluster constructed from eight octahedrally-coordinated Hf cations, i.e., [Hf₈Se₃₆]⁴⁰⁻, and isolated $[HfSe_6]^{8-}$ units which are separated by $(Se_2)^{2-}$ dimers and Ba^{2+} cations. Polycrystalline $Ba_8Hf_2Se_{11}(Se_2)$ is synthesized at 1073 K using a two-step solid-state synthesis method, with the co-formation of a small amount of a BaSe secondary phase. A direct bandgap of 2.2(2) eV is obtained for the polycrystalline sample of BasHf₂Se₁₁(Se₂), which is consistent with its yellow color. Density functional theory calculations reveal their bandgap transitions stem from predominantly filled Se-4p to empty Hf-5d at the edges of the valence bands (VB) and conduction bands (CB), respectively. The optical absorption coefficients are calculated to be relatively large, exceeding $\sim 10^5~\text{cm}^{-1}$ at about > 2.0~eV with effective masses in the CB varying from $\sim 0.5~\text{m}_e~(\Gamma \to A)$ in $Ba_8Hf_2Se_{11}(Se_2)$ to ~ 1.0 m_e ($\Gamma \rightarrow L$) in $Ba_9Hf_3Se_{14}(Se_2)$. Thus, their optoelectronic properties are shown to be competitive with existing perovskite-type chalcogenides that have been a focus of recent research efforts.

1. Introduction

Exploratory synthesis plays a vital role in the solid-state sciences and serves as a powerful tool in unveiling unprecedented structure types and compositions that cannot be predicted in advance. The structural chemistry of chalcogenides (Q=S, Se, and Te) is markedly different from that of oxides, such as showing intriguing catenation properties caused by the larger size and smaller electronegativity of chalcogens [1]. The catenation property of Q atoms leads to the formation of a variety of Q-Q bonding units, such as the occurrence of Q_2^2 anions in Ba₂Ag₂S-e₂(Se₂) [2], Q_c^d (e.g., Se₅⁴, Se₃⁴, and Te₅⁴ polyanions in Nb₂Se₉ [3], Ba₂Ag₄Se₅ [4], and Ba₂SnTe₅ [5], respectively), Q_c^2 chains (e.g., Te₁² and Te₁² units in (NEt₄)₂Te₁₂ [6] and Cs₂Te₁₃ [7], respectively), and square-net polyanions in EuCu_{0.66}Te₂ [8]). These and many other examples demonstrate how metal chalcogenides can stabilize a variety of polyanion Q motifs leading to a variety of new structure types with

interesting physical properties. Synthetic exploration of metal chalcogenides can also play a key role in the establishment of advanced structure-property relationships. The range of observed physical properties has been broad, including nonlinear optical properties, thermoelectric properties, photocatalytic reactivity, magnetic properties, magnetoresistance effects, as well as superconductivity [9–17]. Thus, many metal chalcogenide systems are well established as representing diverse and rich fields for technologically-relevant synthetic explorations.

Recently, the growing interest in the Hf-containing perovskite chalcogenides has been mainly attributed to their complex structures and physical properties, such as thermoelectric properties (e.g., SrHfSe₃ [18]), as light-emitting semiconductors (e.g., SrHfS₃ [19]), and in semiconductor optoelectronics (e.g., BaHfS₃ [20]). Notably, the Hf-containing chalcogenides with perovskite-type structures and compositions have recently been attracting much attention for their

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promisingly small bandgaps (1.5–2.0 eV) and especially strong band edge absorption, i.e., optical absorption coefficient, $\alpha>10^5~{\rm cm}^{-1}$. The limited known examples have included BaHfS $_3$ (*Pnma*) [21], SrHfS $_3$ (*Pnma*) [19,21], and SrHfSe $_3$ (*Pnma*) [18] that form in distorted (noncubic) perovskite-type structures. By comparison, the oxide compositions BaHfO $_3$ and SrHfO $_3$ crystallize in cubic perovskite-type structures [22,23]. A general literature survey of Hf-containing chemical systems reveals the existence of relatively few compounds in the *Alk*-(Ba or Sr)–Hf–Q (Q=S, Se, and Te) system, with nearly all occurring in the metal-sulfide systems including Ba $_6$ Hf $_5$ S1 $_6$ [24], Ba $_5$ Hf $_4$ S1 $_3$ [24], Ba $_2$ HfS4 $_4$ [25], Ba $_4$ Hf $_3$ S1 $_0$ [26], and BaHfS3 $_3$ [21]. Surprisingly, no compounds are currently reported to occur in the Ba–Hf–Se ternary system. The hypothetical BaHfSe $_3$ composition with a perovskite-type structure is not yet reported and is predicted to be thermodynamically unstable [271].

As described herein, the recent reports of Hf-containing chalcogenide perovskites have motivated our synthetic exploration of the Ba-Hf-Se and Ba-Hf-O-Se chemical systems for perovskite-type structures and compositions with interesting optical properties. These synthetic investigations have produced two new solid-state compounds, Ba₈Hf₂Se₁₁(Se₂) and Ba₉Hf₃Se₁₄(Se₂), and which represent the first reported compounds in the Ba-Hf-Se system. Both crystallize in new structure types and exhibit $(Se_2)^{2-}$ dimers. Interestingly, Ba₉Hf₃Se₁₄(Se₂) also contains the first known perovskite-type cluster unit, i.e., $[Hf_8Se_{36}]^{40-}$, in analogy to the bulk perovskite-type structure, i.e., BaHfSe₃, that is both thermodynamically unstable and has yet to be synthesized. Their electronic structures and optical properties were also probed using density functional theory calculations.

2. Experimental

2.1. Materials used and synthetic procedures

Synthetic reactions were performed using the following starting materials: Ba rod (99+% purity, Alfa Aesar), Hf powder (99.99 % purity, Alfa Aesar), HfO $_2$ powder (99.5 % purity, Alfa Aesar), and Se powder (99.99 % purity, Alfa Aesar). As some of the starting materials, including Ba and Hf, are air sensitive, the chemical manipulations were conducted inside an Argon-filled dry glove box.

2.1.1. Syntheses of $Ba_8Hf_2Se_{11}(Se_2)$ and $Ba_9Hf_3Se_{14}(Se_2)$ single crystals

Yellow- and red-colored single crystals of Ba₈Hf₂Se₁₁(Se₂) and Ba₉Hf₃Se₁₄(Se₂), respectively, were discovered during an exploratory synthesis in the Ba-Hf-O-Se phase diagram using high-temperature solid-state reactions. One of the reactions containing Ba (257.8 mg, 1.877 mmol), Hf (167.5 mg, 0.938 mmol), HfO₂ (28.2 mg, 0.134 mmol), and Se (296.4 mg, 3.754 mmol) produced the single crystals of both Ba₈Hf₂Se₁₁(Se₂) and Ba₉Hf₃Se₁₄(Se₂). The reactants were loaded into a carbon (C)-coated fused silica tube of 6 mm outer diameter (OD) inside an Ar-filled glove box, and which was then sealed using a torch under dynamic vacuum. The sealed vessel was then placed inside a programmable muffle furnace and heated to 673 K in 4 h, where it was then soaked for 6 h, followed by ramping the temperature to 1223 K in 10 h. The ampoule was annealed at 1223 K for 80 h before switching off the furnace. The furnace was then programmed to cool to room temperature radiatively. The tube was opened in the air, revealing an ingot of polycrystalline product, which was crushed and investigated under an optical microscope.

A few block-shaped red-colored and plate-shaped yellow-colored crystals were selected and picked on carbon tape for elemental analysis using energy-dispersive X-ray (EDX) spectroscopy using a JEOL SEM 6010LA spectrophotometer. An accelerating voltage of 20 kV was used for the EDX data collection. The EDX data on yellow crystals showed the presence of Ba, Hf, and Se in an average ratio of $\approx\!8\!:\!2\!:\!13$, corresponding to the formula of Ba₈Hf₂Se₁₁(Se₂) (Supporting Information, Fig. S1(a)). In contrast, the EDX data of red crystals indicated a formula of

 $Ba_9Hf_3Se_{14}(Se_2)$ (Ba:Hf:Se \approx 9:3:16) (Fig. S1(b)). The single crystals of $Ba_8Hf_2Se_{11}(Se_2)$ and $Ba_9Hf_3Se_{14}(Se_2)$ were further reproduced from stoichiometric amounts of starting materials, and the same heating profile was used that was used for the exploratory synthesis. The EDX data was recorded on selected crystals, and unit cell determinations were carried out using single-crystal X-ray diffraction data to confirm their respective compositions.

2.1.2. Syntheses of polycrystalline Ba₈Hf₂Se₁₁(Se₂) and Ba₉Hf₃Se₁₄(Se₂)

A two-step, high-temperature solid-state synthesis method was used to prepare a pure polycrystalline Ba₈Hf₂Se₁₁(Se₂) sample. First, stoichiometric amounts of Ba (265.6 mg, 1.934 mmol), Hf (86.3 mg, 0.484 mmol), and Se (248.1 mg, 3.142 mmol) were loaded into a fused silica ampule (12 mm OD) inside the Ar-filled dry glove box. The ampoule was sealed under $\sim 10^{-4}$ Torr pressure using a flame torch and loaded inside a programmable muffle furnace for heat treatment. The furnace temperature was ramped to 823 K in 6 h and soaked for 12 h before increasing the temperature to 1073 K. The furnace was switched off after annealing for 72 h at 1073 K and cooled to room temperature radiatively. The product was opened in air, revealing a dark homogeneouslooking lump. The product was then ground using an agate mortar pestle inside the Ar-filled dry glove box and pelletized in an ambient atmosphere using a hydraulic press. The pellet was placed inside a carbon-coated fused silica tube and flame sealed under $\sim 10^{-4}$ Torr pressure. The tube was ramped to 873 K in 2 h and heated for 48 h at 873 K before switching off the furnace, allowing radiative cooling to room temperature. The product was homogeneously ground inside the glove box, and powder X-ray diffraction (PXRD) data were recorded for the polycrystalline sample. The PXRD data confirms the formation of the polycrystalline Ba₈Hf₂Se₁₁(Se₂) phase with a minute secondary phase of BaSe (Fig. 1).

Attempts to synthesize $Ba_9Hf_3Se_{14}(Se_2)$ using stoichiometric amounts of starting materials with the same heating profile used to synthesize $Ba_8Hf_2Se_{11}(Se_2)$ invariably yielded only small quantities of small crystals. The majority phase produced was $Ba_8Hf_2Se_{11}(Se_2)$ along with secondary phases of BaSe. Additional reactions with varying heating profiles produced only impure polycrystalline samples of $Ba_9Hf_3Se_{14}(Se_2)$.

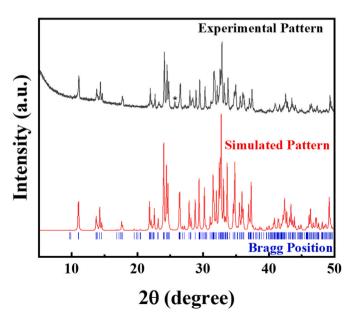


Fig. 1. The simulated (red) and experimental (black) powder X-ray diffraction patterns and Bragg positions for polycrystalline $Ba_8Hf_2Se_{11}(Se_2)$. The (*) peak shows the formation of a minute secondary phase of BaSe.

2.2. X-ray diffraction: Single crystal and polycrystalline powder analyses

The crystal structures of Ba₈Hf₂Se₁₁(Se₂) and Ba₉Hf₃Se₁₄(Se₂) crystals were established by room temperature (300(2) K) single-crystal Xray diffraction data sets of respective single crystals using a Bruker D8 Venture diffractometer. The intensity data were recorded using a Photon III mixed mode detector and a graphite monochromatized radiation source of Mo-K α ($\lambda = 0.71073$ Å). For each dataset, the Ba₈Hf₂Se₁₁(Se₂) and Ba₉Hf₃Se₁₄(Se₂) crystals were picked separately on a transparent loop under Paratone-N oil and mounted on a goniometer head for data collection. An initial fast scan data of 180 frames were collected to check the crystal quality. The APEX3 software [28] was used to determine the unit cell and collect the data. The intensity data were recorded using a working voltage and working current of 50 kV and 1.4 mA, respectively. An exposure time, frame width, and detector to crystal distance of 2 s/frame, 0.5°, and 50 mm, respectively, were employed during the intensity data collection. APEX3 software was used for the refinement of lattice parameters and integration of the data.

The XPREP software package [29] suggested a C-centered monoclinic cell for the Ba₈Hf₂Se₁₁(Se₂) crystal structure. Two space groups were possible based on the extinction conditions: C2/c (centrosymmetric) and *Cc* (non-centrosymmetric). The mean statistics of intensity (E^2-1) value of 0.988 suggested a centrosymmetric space group for the $Ba_8Hf_2Se_{11}(Se_2)$ crystal structure. The expected $|E^2-1|$ values are 0.968 and 0.736 for centrosymmetric and non-centrosymmetric space groups, separately. So, the C2/c space group was selected to solve the crystal structure of Ba₈Hf₂Se₁₁(Se₂) using the SHELX-14 [30]. The initial solution of the Ba₈Hf₂Se₁₁(Se₂) crystal structure was obtained using the direct method of the SHELXS program [31]. There were thirteen crystallographically independent atomic positions in the asymmetric unit of the structure, which were further allocated to respective elements based on peak heights, coordination environments, and bond distances. The atomic positions, scale factors, anisotropic displacement parameters, extinction corrections, and weight corrections were further refined using full-matrix least squares on the F^2 method. The final model of the Ba₈Hf₂Se₁₁(Se₂) crystal structure consists of five Ba, one Hf, and seven Se crystallographic sites.

No missing symmetry was found by the ADDSYM program of the PLATON software [32]. The atomic positions were standardized with the help of the STRUCTURE TIDY program [33]. The difference Fourier map of the final solved structure of Ba₈Hf₂Se₁₁(Se₂) is nearly featureless. A small maximum peak of 1.70 Å⁻³ (position: 0.5, 0, 0.5) and the deepest hole of -1.99 Å⁻³ (0.4966, 0.0190, 0.5781) were present at 2.32 Å and 1.68 Å away from the Se(5) atom, respectively. The crystal structure refinement and metric details for the Ba₈Hf₂Se₁₁(Se₂) crystal structure are listed in Tables 1, 2 and 4 and in the Supporting Information.

For the single crystal structure of Ba₉Hf₃Se₁₄(Se₂), the lattice dimensions and extinction conditions were found to be consistent with a rhombohedral (R) centrosymmetric cell ($|E^2-1|=1.083$). So, the R $\overline{3}$ space group was selected from the suggested R $\overline{3}$ (centrosymmetric) and R3 (noncentrosymmetric) space groups. The Ba₉Hf₃Se₁₄(Se₂) crystal structure was solved, refined, and standardized similarly as described earlier for solving the Ba₈Hf₂Se₁₁(Se₂) crystal structure. The asymmetric unit of the crystal structure of Ba₉Hf₃Se₁₄(Se₂) has seventeen crystal-lographically independent sites: six Ba, three Hf, and eight Se sites. The minimum peak (-2.46 Å⁻³) for the Ba₉Hf₃Se₁₄(Se₂) structure was found at (0.9809, 0.0084, 0.1528), which is 0.49 Å away from the Ba(5) atom. Whereas a small maximum electron density of 1.06Å⁻³ was located 1.17 Å apart from Se(4) (position: 0.1998, 0.6577, 0.0090). The metric and crystal structure refinement details of the Ba₉Hf₃Se₁₄(Se₂) crystal structure are provided in Tables 1, 3 and 4 and in the Supporting Information.

A room temperature powder X-ray diffraction (PXRD) data set was recorded at 300(2) K using a PANalytical Empyrean X-ray diffractometer

 $\label{eq:Table 1} \textbf{Table 1} \\ \textbf{Crystallographic structural data and refinement details for the $Ba_8Hf_2Se_{11}(Se_2)$ and $Ba_9Hf_3Se_{14}(Se_2)$ structures.}^a$

	$Ba_8Hf_2Se_{11}(Se_2)$	$Ba_9Hf_3Se_{14}(Se_2)$
Space group	$C_{2h}^6 - C2/c$	$C_{3i}^2 - R\overline{3}$
a (Å)	12.3962(15)	19.4907(6)
b (Å)	12.8928(15)	
c (Å)	18.1768(17)	23.6407(11)
β (°)	90.685(4)	
$V(Å^3)$	2904.8(6)	7777.6(6)
Z^{c}	4	9
ρ (g cm ⁻³)	5.676	5.832
$\mu \text{ (mm}^{-1}\text{)}$	34.04	35.87
$R(F)^{\mathrm{b}}$	0.017	0.022
$R_{\rm w}(F_{\rm o}^2)^{\rm c}$	0.035	0.046
S	1.09	1.06
No. of measured reflections	46188	85356
No. of independent reflections	4424	4283
Reflections with $I > 2\sigma(I)$	4180	3716

^a $\lambda = 0.71073$ Å, T = 300(2) K.

Table 2 Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\mathring{A}^2) for Ba₈Hf₂Se₁₁(Se₂) structure.

Atom	Wyckoff Position	x	у	Z	$U_{ m eq}$
Ba	8 <i>f</i>	0.00582	0.31184	0.48577	0.01325
(1)		(2)	(2)	(2)	(4)
Ba	8 <i>f</i>	0.31856	0.37530	0.30850	0.01334
(2)		(2)	(2)	(2)	(4)
Ba	8f	0.32104	0.47585	0.06435	0.01317
(3)		(2)	(2)	(2)	(4)
Ba	4 <i>e</i>	0	0.18211	1/4	0.01475
(4)			(2)		(6)
Ba	4 <i>e</i>	0	0.54971	1/4	0.01422
(5)			(2)		(6)
Hf(1)	8 <i>f</i>	0.25581	0.17583	0.13462	0.00998
		(2)	(2)	(2)	(4)
Se(1)	8 <i>f</i>	0.06516	0.07558	0.09675	0.01257
		(3)	(3)	(2)	(7)
Se(2)	8 <i>f</i>	0.13884	0.35228	0.16887	0.01185
		(3)	(3)	(2)	(6)
Se(3)	8f	0.24423	0.11038	0.27104	0.01269
	•	(3)	(3)	(2)	(7)
Se(4)	8 <i>f</i>	0.24907	0.21674	0.43828	0.01515
	-	(3)	(3)	(2)	(7)
Se(5)	8 <i>f</i>	0.36547	0.01203	0.08690	0.01339
	-	(3)	(3)	(2)	(7)
Se(6)	8 <i>f</i>	0.43855	0.28002	0.15545	0.01245
	•	(3)	(3)	(2)	(7)
Se(7)	4c	1/4	1/4	Ô	0.01032
					(8)

on a polycrystalline sample of Ba₈Hf₂Se₁₁(Se₂). A Cu-K α radiation source ($\lambda=1.5406$ Å) was used to collect the data over a 2θ region of 5° to 50°. An operating current and a working voltage of 40 mA and 45 kV were used to record the data with a 0.013° step size.

2.3. Spectroscopic characterization

The Raman spectrum of the polycrystalline $Ba_8Hf_2Se_{11}(Se_2)$ sample was recorded at room temperature (298(2) K) using a Horiba XploRA PLUS confocal microscope equipped with a sincerity OE detector over a wavelength range of $50\text{--}3500~\text{cm}^{-1}$. The excitation wavelength of 532~nm was used to collect the data with a resolution of $3~\text{cm}^{-1}$.

Solid state ultraviolet–visible (UV–vis) spectra were measured on the polycrystalline $Ba_8Hf_2Se_{11}(Se_2)$ sample after grinding inside an Ar-filled

^b $R(F) = \sum ||F_0| - |F_c|| / \sum |F_0|$ for $F_0^2 > 2\sigma(F_0^2)$.

 $^{^{}c}R_{w}(F_{o}^{2}) = \{\Sigma [w(F_{o}^{2} - F_{c}^{2})^{2}]/\Sigma wF_{o}^{4}\}^{1/2}.$ For $F_{o}^{2} < 0$, $w = 1/[\sigma^{2}(F_{o}^{2}) + (rP)^{2} + sP];$ where $P = (F_{o}^{2} + 2F_{c}^{2})/3$. Where r and s are 15.6886 and 0, and 0.0078 and 191.5368 for $Ba_{8}Hf_{2}Se_{11}(Se_{2})$ and $Ba_{0}Hf_{2}Se_{14}(Se_{2})$, respectively.

 $\label{eq:Table 3} \begin{tabular}{ll} \textbf{Table 3} \\ \textbf{Fractional atomic coordinates and isotropic or equivalent isotropic displacement} \\ \textbf{parameters (\mathring{A}^2) for the $Ba_9Hf_3Se_{14}(Se_2)$ structure.} \\ \end{tabular}$

Atom	Wyckoff Position	x	у	Z	$U_{ m eq}$
Ba	18f	0.04973	0.21858	0.38500	0.01440(8)
(1)	-	(2)	(2)	(2)	
Ba	18f	0.06038	0.27174	0.16607	0.01495(8)
(2)		(2)	(2)	(2)	
Ba	18f	0.21106	0.20301	0.04771	0.01510(8)
(3)		(2)	(2)	(2)	
Ba	18f	0.22389	0.16821	0.26408	0.01416(8)
(4)		(2)	(2)	(2)	
Ba	6 <i>c</i>	0	0	0.15808	0.01982
(5)				(3)	(14)
Ba	3b	0	0	1/2	0.01782
(6)					(18)
Hf(1)	18f	0.27668	0.41909	0.10223	0.01041(6)
		(2)	(2)	(2)	
Hf(2)	6 <i>c</i>	0	0	0.31314	0.01105(9)
				(2)	
Hf(3)	3a	0	0	0.000000	0.01173
					(12)
Se(1)	18f	0.00712	0.11716	0.06566	0.01496
		(4)	(4)	(2)	(12)
Se(2)	18f	0.03215	0.12950	0.25344	0.01414
		(4)	(4)	(2)	(12)
Se(3)	18f	0.06543	0.35880	0.29711	0.01687
		(4)	(4)	(3)	(13)
Se(4)	18f	0.11703	0.09044	0.37959	0.01320
		(3)	(3)	(2)	(12)
Se(5)	18f	0.15182	0.33905	0.03686	0.01387
		(4)	(4)	(2)	(12)
Se(6)	18f	0.18910	0.46024	0.16703	0.01263
		(3)	(4)	(2)	(12)
Se(7)	18f	0.24757	0.30590	0.17387	0.01434
		(4)	(4)	(2)	(12)
Se(8)	18f	0.27633	0.12382	0.13873	0.01684
		(4)	(4)	(3)	(13)

$Ba_8Hf_2Se_{11}(Se_2)$		$Ba_9Hf_3Se_{14}(Se_2)$		
Atom pair	Bond distance (Å)	Atom pair	Bond distance (Å)	
Hf(1)-Se(3)	2.6249(4)	Hf(1)-Se(7)	2.6088(6)	
Hf(1)-Se(7)	2.6273(3)	Hf(1)-Se(3)	2.6236(6)	
Hf(1)-Se(6)	2.6569(4)	Hf(1)-Se(5)	2.6359(6)	
Hf(1)-Se(5)	2.6624(4)	Hf(1)-Se(6)	2.6555(6)	
Hf(1)-Se(2)	2.7725(4)	Hf(1)-Se(4)	2.6603(6)	
Hf(1)-Se(1)	2.7732(4)	Hf(1)-Se(6)	2.6969(6)	
Se(4)-Se(4)	2.4018(7)	Hf(2)-Se(4)	$2.5994(6) \times 3$	
		Hf(2)-Se(2)	2.6784(6)	
		Hf(2)-Se(2)	$2.6785(6) \times 2$	
		Hf(3)-Se(1)	$2.7068(6) \times 6$	
		Se(8)-Se(8)	2.3999(13)	

glove box to make a homogenized powder. A Shimadzu 3600 UV–vis–NIR spectrophotometer was used to collect the reflectance data over a wavelength range of 1000 nm (1.24 eV) to 250 nm (4.96 eV). The dried BaSO₄ powder was used as the standard reference for the data collection. The Kubelka-Munk equation [34]: $\alpha/S = (1-R)^2/2R$ was used to convert the reflectance data to absorption data. Here S, α , and R are the scattering coefficient, absorption coefficient, and reflectance, respectively. Tauc plots [35] were used to evaluate the optical bandgap for the polycrystalline Ba₈Hf₂Se₁₁(Se₂) sample:

$$(\alpha h v)^n = A(h v - E_q) \tag{1}$$

In equation (1), the terms h, v, A, and E_g represent Planck's constant, frequency of light, proportionality constant, and bandgap. The value of

constant n indicates the nature of the bandgap. The n=2 and $\frac{1}{2}$ values indicate direct and indirect bandgaps, respectively.

2.4. Electronic structure calculations

Density functional theory calculations were performed with the use of the Projector Augmented Wave (PAW) method within the Vienna Ab Initio Simulation Package (VASP) software package [36,37]. The generalized gradient approximation (GGA) was used to treat the exchange-correlation functionals [38]. The criteria for energy convergence was set to $10^{-8}\,\text{eV}$ and the cutoff energy was fixed to 520 eV in accordance with the PAW pseudopotentials for the Ba, Hf, and Se contributions. Full geometry relaxations utilized a Γ -centered 4 \times 4 \times 4 k-point mesh and 36 k-points. Individual atomic orbital contributions were projected out in the calculated Densities-of-States (DOS). Calculations of the band structures were performed using 10 intersections along the standard high symmetry directions [39] of the conventional *k*-point path within the Brillouin zone of the respective crystals systems for the primitive cells of $Ba_8Hf_2Se_{11}(Se_2)$ (i.e., Γ -Y-M-A- Γ |L2- Γ -V2) and Ba₉Hf₃Se₁₄(Se₂) (i.e., Γ-L-T|P2-Γ-F). The Crystal Orbital Hamilton Populations (COHP) of the Hf-Se and Se-Se interactions were calculated with the use of the LOBSTER (Local-Orbital Suite Towards Electronic-Structure Reconstruction) software package version 4.1.0 [40-44].

3. Results and discussion

3.1. Syntheses and crystal structures

Two multinary chalcogenides, $Ba_8Hf_2Se_{11}(Se_2)$ and $Ba_9Hf_3Se_{14}(Se_2)$, with new structure types have been obtained during a synthetic exploration of the Ba–Hf-Se system by high-temperature reactions of the elements at 1223 K. These compounds represent the first reported chalcogenides in this chemical system. Stoichiometric reactions yielded $Ba_8Hf_2Se_{11}(Se_2)$ and $Ba_9Hf_3Se_{14}(Se_2)$ as yellow and red crystals, respectively, but in relatively high purity (~80 %) only for the former. Reactions loaded on the $Ba_9Hf_3Se_{14}(Se_2)$ composition mainly produced yellow plates of $Ba_9Hf_3Se_{14}(Se_2)$ along with small amounts of red-colored blocks of $Ba_9Hf_3Se_{14}(Se_2)$ in ~5–10 % yield. The polycrystalline phase of $Ba_8Hf_2Se_{11}(Se_2)$ was synthesized at 1073 K using a two-step sealed tube solid-state synthesis method. Both compounds appear stable in air for a period of days with no detectable decomposition.

The crystal structure of Ba₈Hf₂Se₁₁(Se₂) was characterized by room temperature single crystal X-ray diffraction data. It was found to crystallize in a new structure type in the C2/c space group with unit cell parameters of a=12.3962(15) Å, b=12.8928(15) Å, c=18.1768(17) Å, and $\beta=90.685(4)^\circ$ with four formula units in the unit cell (Z=4). There are thirteen crystallographically-independent atomic sites: five Ba, one Hf, and seven Se sites. The list of atomic coordinates and isotropic displacement parameter are given in Table 2. A structural view of the unit cell of Ba₈Hf₂Se₁₁(Se₂) is shown in Fig. 2(a):

The Hf atoms are coordinated within distorted HfSe₆ octahedra which are vertex-bridged through Se(7) to form a dimer unit with the anionic motif of $[Hf_2Se_{11}]^{14-}$, illustrated in Fig. 2(b). The Hf–Se distances in the HfSe₆ octahedra range from 2.6249(4) Å to 2.7732(4) Å, which compare reasonably well with Hf–Se distances in previously reported compounds such as SrHfSe₃ (2.559(2)–2.720(9) Å) [18], NaCuHfSe₃ (2.608(1)–2.788(1) Å) [45], and NaCuHf₂Se₅ (2.65(1)–2.701(2) Å) [46]. Also, the distance between neighbouring Se(4) atoms of 2.4018(7) Å is indicative of the presence of Se–Se bonding and formation of (Se₂)²⁻ dimers. The Pauling covalent radii [47] of a Se atom is ~1.17 Å, and thus two Se atoms have a total Pauling covalent radius of ~2.34 Å. The Se–Se bond distance can be compared to previously reported examples found in Ba₂Ag₂Se₂(Se₂) (2.378(2) Å) [2], Ba₃ThSe₃(Se₂) ((2.374(1) Å and 2.377(1) Å) [48], and CsAuSe₃ (2.384(1) Å)

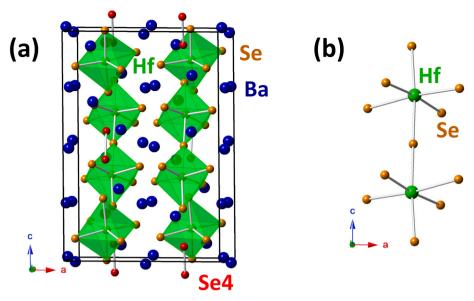


Fig. 2. A structural view of the (a) unit cell of $Ba_8Hf_2Se_{11}(Se_2)$ approximately along the [010] direction and (b) the $[Hf_2Se_{11}]^{14-}$ dimeric units.

[49]. This leads to a charge-balanced formula consisting of Ba^{2+} and Hf^{4+} cations, as well as both Se^{2-} and Se^{2-}_{2-} anions. Details of the respective Ba cation coordination environments are provided in the Supporting Information.

The second known compound in the Ba-Hf-Se system, Ba₉Hf₃S-e₁₄(Se₂), was found to crystallize in the rhombohedral $R\overline{3}$ space group with the unit cell parameters a=b=19.4907(6) Å and c=23.6407(11) Å with nine formula units (Z=9) in the unit cell. There are seventeen crystallographically-independent atomic positions, including six Ba, three Hf, and eight Se sites. A listing of atomic coordinates and isotropic displacement parameter is given in Table 3, with nearest-neighbor distances given in Table 4.

A structural view of the unit cell of Ba₉Hf₃Se₁₄(Se₂) is illustrated in Fig. 3(a). In the Ba₉Hf₃Se₁₄(Se₂) crystal structure, every Hf atom has six nearest-neighbor Se atoms, forming distorted HfSe₆ octahedra. The structure consists of isolated [HfSe₆]⁸⁻ octahedra as well as perovskite-like [Hf₈Se₃₆]⁴⁰⁻ cluster anions, shown in Fig. 3(b, c and d) respectively. In the former, the Hf(3)-centered [HfSe₆]⁸⁻ octahedra exhibit Hf–Se distances of 2.7068(6) Å. Although all Hf(3)–Se(1) interatomic distances are the same, the octahedral units are slightly distorted because of the Se (1)–Hf(3)–Se(1) bond angles (Table S4). In the perovskite-like [Hf₈Se₃₆]⁴⁰⁻ clusters, the Hf–Se distances range from 2.6088(6) Å to 2.6969(6) Å and 2.5994(6) Å to 2.6785(6) Å for Hf(1)-centered and Hf

(2)-centered octahedra, respectively. The vertex-bridged condensation of the Hf(1)Se₆ and Hf(2)Se₆ octahedra leads to the formation of the [Hf (1)₆Hf(2)₂Se₃₆]⁴⁰⁻ perovskite cluster, including 12 vertex-bridging and 24 terminal selenide anions. Interestingly, the perovskite-like [Hf₈Se₃₆]⁴⁰⁻ cluster of the Ba₉Hf₃Se₁₄(Se₂) crystal structure is like that known for the perovskite-type BaHfS₃ structure, wherein the Ba²⁺ cations are located within a cuboctahedral environment of eight vertexbridging HfS6 octahedra. The analogous selenide, i.e., BaHfSe3 in a perovskite-type structure, is not reported to occur because of an unfavorable tolerance factor and the lack of thermodynamic stability [27]. Most interestingly, the formation of perovskite-like [Hf₈Se₃₆]⁴⁰⁻ clusters can be stabilized for the first time within this selenium-richer structure. As described above for Ba₈Hf₂Se₁₁(Se₂), Se-Se bond distance of 2.3999(13) Å are also found in its structure and indicating the presence of Se–Se bonding in the form of $(Se_2)^{2-}$ dimers. This distance is similar to that found in prior reported structures, as probed in further detail below using electronic structure calculations.

Charge balancing of both compounds can be achieved by considering Ba, Hf, and Se in their closed-shell electronic configurations and consideration of the homoatomic Se–Se bonding. The short nearest-neighbor Se–Se bonding occurs in both the Ba₈Hf₂Se₁₁(Se₂) (Se(4)–Se (4) = 2.4018(7) Å) and Ba₉Hf₃Se₁₄(Se₂) (Se(8)–Se(8) = 2.3999(13) Å) crystal structures, i.e., forming $(Se_2)^{2-}$ anionic dimers. All other Se

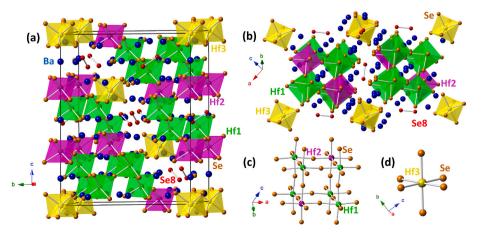


Fig. 3. A structural view of the (a) unit cell of the $Ba_9Hf_3Se_{14}(Se_2)$ structure, (b, c) packing of the individual perovskite-like $[Hf_8Se_{36}]^{40-}$ clusters (purple and green octahedra) and (d) $[HfSe_5]^{8-}$ units (yellow octahedra). All Hf-centered polyhedra are colored green, yellow or purple.

atoms are considered to be in their -2 oxidation state. There is no homoatomic or heteroatomic bonding between the electropositive Ba and Hf atoms, which indicates that the Ba and Hf atoms are present in their +2 and +4 oxidation states, respectively. So, the charge balancing for the Ba₈Hf₂Se₁₁(Se₂) structure can be considered as $(Ba^{2+})_8(Hf^{4+})_2(Se^2)_{11}(Se_2)^2$. Whereas Ba₉Hf₃Se₁₄(Se₂) can be charge balanced as $(Ba^{2+})_9(Hf^{4+})_3(Se^2)_{14}(Se_2)^2$. Additional details are provided in the electronic structure calculations, as described below.

3.2. Spectroscopic characterization methods

Measurements of elemental compositions using energy dispersive Xray spectroscopy on yellow crystals of Ba₈Hf₂Se₁₁(Se₂) yielded only the occurrence of Ba, Hf, and Se in an average ratio of \approx 8:2:13, consistent with its chemical formula. Similar measurements on red crystals of Ba₉Hf₃Se₁₄(Se₂) also gave an elemental composition of \approx 9:3:16 for Ba: Hf:Se molar ratio, consistent with its chemical formula. The EDS spectrum for each is provided in the Supporting Information. A roomtemperature Raman spectrum was acquired for polycrystalline $Ba_8Hf_2Se_{11}(Se_2)$ in the wavelength region of 50–3500 cm⁻¹ (Fig. 4). The Raman spectrum showed an intense band at 250 cm⁻¹, which is indicative of the Se–Se stretching mode of Se₂² unit in Ba₈Hf₂Se₁₁(Se₂). The vibration of the Se_2^{2-} unit of $Ba_8Hf_2Se_{11}(Se_2)$ compares well with the Se-Se stretching mode of K_2Se_2 (~253 cm⁻¹) [50], $Ba_4SiSb_2Se_{11}$ (~247 cm⁻¹) [51], and Ba₂Ag₂Se₂(Se₂) (\sim 247 cm⁻¹) [2]. The bands at \sim 147 cm⁻¹ and 200 cm⁻¹ in the Raman spectrum of Ba₈Hf₂Se₁₁(Se₂) stem from the Hf-Se stretching mode in Ba₈Hf₂Se₁₁(Se₂), which agrees well with the Hf-Se stretching modes at \sim 146 cm⁻¹ and 199 cm⁻¹ in HfSe₂ [52]. The other peaks below 200 cm⁻¹ can be assigned to various Ba–Se stretching modes [53]. All Raman stretches are generally consistent with its composition and structure.

The yellow and red-colored crystals of $Ba_8Hf_2Se_{11}(Se_2)$ and $Ba_9Hf_3Se_{14}(Se_2)$, respectively, indicated both compounds are intrinsic semiconductors. To probe the band transitions of $Ba_8Hf_2Se_{11}(Se_2)$, room temperature optical absorption data were collected in diffuse reflectance mode over a wavelength range of 1000 nm (1.24 eV) to 250 nm (5.94 eV). The direct and indirect band transitions were determined using Tauc plots [35] of the absorption data, shown together in Fig. 4(b) for both the direct and indirect transitions. A direct transition energy of $\sim\!2.2(2)$ eV is found for $Ba_8Hf_2Se_{11}(Se_2)$, consistent with its yellow color. A similar Tauc plot of its indirect transition yielded a lower energy $\sim\!1.5(2)$ eV, thus showing the indirect nature of the band gap for $Ba_8Hf_2Se_{11}(Se_2)$. Sufficiently pure samples of $Ba_9Hf_3Se_{14}(Se_2)$ could not be obtained for unambiguous Raman and UV–Vis diffuse reflectance measurements.

3.3. Electronic structure calculations

Research into chalcogenide-based perovskite semiconductors has experienced growing interest owing to their strong band-edge absorption (optical absorption coefficient, $\alpha>10^5~cm^{-1}$) and small bandgaps of $\sim\!1.5\text{--}2.0~eV$ [21,27]. Though, relationships to their crystal structures and impacts upon the nature and strength of their optical bandgap transitions have not been well explored. Density functional theory calculations were employed to probe the electronic structures, band gaps, and the underlying chemical bonding in Ba_8Hf_2Se_1_1(Se_2) and Ba_9Hf_3Se_1_4(Se_2), and usefully serving as a comparison of the non-perovskite-type structures in this Ba-Hf-Se chemical system.

Both structures were first geometry optimized followed by subsequent, separate calculations of their band structures and Density-of-States (DOS) using k-points along a conventional high-symmetry path or randomly distributed, respectively. Shown in Fig. 5 (a and b) are the calculated DOS plots for each structure, with the individual atomic orbital contributions shown for Se (green), Hf (red) and Ba (brown). These show that the edges of the valence bands (VB) consist of filled Sebased states, while the edges of the conduction bands (CB) are comprised of empty Hf-based states. The latter is mixed, at higher energies, with a minor but increasing contribution from Se-based states, further described below. The bandgap of Ba₈Hf₂Se₁₁(Se₂) was calculated to be \sim 1.61 eV (indirect; Γ -point to F-point), in close agreement with the optical diffuse reflectance data in Fig. 4. The direct transition is found to be less than ~0.1 higher in energy, likely resulting from the underestimation of band transitions that has been well documented [54]. For Ba₉Hf₃Se₁₄(Se₂), the bandgap was calculated to be smaller, ~1.55 eV (direct; Γ -point), and generally consistent with its reddish color. The calculated band structures, Figs. S4 and S5, are given in the Supporting Information. The smallest effective masses in the CB of each were $\sim\!0.5$ m_e^* ($\Gamma \to A$) in Ba₈Hf₂Se₁₁(Se₂) and ~1.0 m_e^* ($\Gamma \to L$) in Ba₉Hf₃Se₁₄(Se₂). This compares similarly to electron effective masses within chalcogenide perovksites that have recently been intensely investigated for optoelectronic applications, such as in BaHfS₃ (\sim 0.94 m_e *) and BaZrS₃ ($\sim 0.41 \text{ m}_e^*$) [55]. Further, the computed optical absorption coefficients, shown plotted in Fig. 5 (c and d), were found to be surprisingly large. Both exceed $\sim 10^5$ cm⁻¹ at photon energies greater than 2.0 eV. Similarly, the optical absorption coefficients of analogous chalcogenide perovskites reach optical absorption coefficients of $>10^5$ cm⁻¹ for photon energies greater than 2.0 eV, e.g., such as calculated for BaZrS₃ [27,55]. Thus, these results demonstrate absorption coefficients and small effective masses that are competitive with the multinary chalcogenides with perovskite-type structures.

Computations of the Crystal Orbital Hamilton Populations were performed using density functional theory on the geometry relaxed structures of $Ba_8Hf_2Se_{11}(Se_2)$ and $Ba_9Hf_3Se_{14}(Se_2)$ to probe the Hf–Se and Se–Se interactions (i.e., in the $(Se_2)^{2-}$ dimers) within each. The

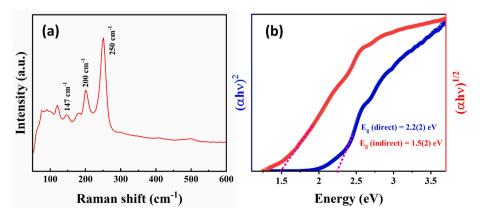


Fig. 4. Raman spectrum (a) and Tauc plots (b) for a polycrystalline sample of Ba₈Hf₂Se₁₁(Se₂).

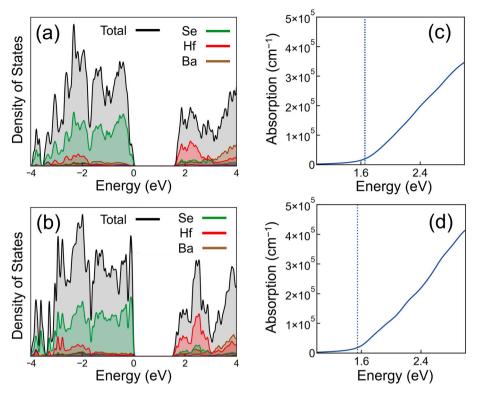


Fig. 5. Calculated electronic density-of-states (DOS) plots for the (a) Ba₈Hf₂Se₁₁(Se₂) and (b) Ba₉Hf₃Se₁₄(Se₂) crystal structures and (c, d) their respective optical absorption coefficients versus energy. For (a) and (b) the Fermi levels are located at 0 eV, while in (c) and (d) the bandgap energy is labelled by the dashed blue line.

results are plotted together in Fig. 6, showing the bonding (+) and antibonding (-) populations as a function of energy with respect to the Fermi level. Both show optimization of the Hf–Se interactions (red colored), with bonding states fully occupied and the antibonding states empty. This confirms the small but growing Se contributions to the conduction bands at increasing energies, Fig. 5 (a and b), is the result of antibonding Hf–Se interactions. Conversely, the Se–Se interactions in the $(Se_2)^{2-}$ dimers, Fig. 6 (blue colored) show an occupation of

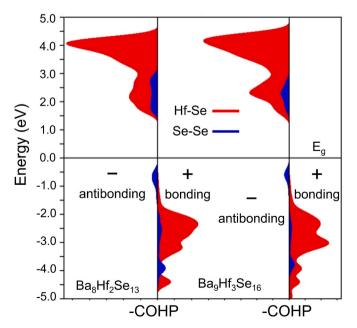


Fig. 6. Plots of Crystal Orbital Hamilton Populations (COHP) for the Hf–Se and Se–Se interactions in the (left) $Ba_8Hf_2Se_{11}(Se_2)$ and (right) $Ba_9Hf_3Se_{14}(Se_2)$ crystal structures.

antibonding states near the top of the valence bands, as well as empty antibonding states at the bottom of the conduction bands. The crystal orbital bond indices (COBI) [56], an analogue for bond order in extended systems, for the Se–Se dimer interactions were calculated to be 0.808 and 0.819 in $\rm Ba_8Hf_2Se_{11}(Se_2)$ and $\rm Ba_9Hf_3Se_{14}(Se_2)$, respectively. These are generally consistent with single bonds, formally, in the (Se_2)^2–dimers, as would be expected from electron counting. Further, the contributions of the Se–Se antibonding states, shown to occur at the edges of the conduction and valence bands, may also likely contribute to the large optical absorption coefficients and small bandgaps of both compounds. Future investigations are warranted and underway to probe the impact of the structural units of multinary chalcogenides on their optoelectronic properties.

4. Conclusions

Two new ternary selenides, Ba₈Hf₂Se₁₁(Se₂) and Ba₉Hf₃Se₁₄(Se₂), have been synthesized using high temperature reaction methods and represent the first reported compounds in the Ba-Hf-Se system. Their structures were probed by single crystal X-ray diffraction and structural refinements to consists of pseudo zero-dimensional structures with $(Se_2)^{2-}$ dimers. While $Ba_8Hf_2Se_{11}(Se_2)$ contains $[Hf_2Se_{11}]^{14-}$, the structure of Ba₉Hf₃Se₁₄(Se₂) is built from a novel perovskite-type $[Hf_8Se_{36}]^{40-}$ cluster as well as isolated $[HfSe_6]^{8-}$ octahedra. The [Hf₈Se₃₆]⁴⁰⁻ cluster is notable in that it represents the perovskite-type analogue to the fully condensed version (i.e., BaHfSe3) that is thermodynamically unstable and has yet to be synthesized. Interestingly, both compounds are calculated to exhibit small optical bandgaps (<2.0 eV) and strong optical absorption coefficients (>10⁵ cm⁻¹), with relatively small electron effective masses in their conduction bands. Density functional theory calculations show the bandgap transitions stem from predominantly filled Se-4p to empty Hf-5d at the edges of their respective valence bands (VB) and conduction bands (CB). Thus, their underlying electronic structures and optoelectronic properties augurs well for the future potential of these and other non-perovskite type chalcogenides in applications for solar energy conversion.

Supporting Information

The crystallographic data files of Ba $_8$ Hf $_2$ Se $_{11}$ (Se $_2$) and Ba $_9$ Hf $_3$ Se $_{14}$ (Se $_2$) structures are available by request to the Cambridge Crystallographic Data Centre (CCDC) in the form of crystallographic information files with CCDC numbers of 2272013 and 2274600, respectively. The data can be accessed from CCDC (https://www.ccdc.cam.ac.uk/) with no charge. The SEM data of the elemental composition, the Ba coordination environment, the atomic displacement parameters, and the metric details of Ba $_8$ Hf $_2$ Se $_{11}$ (Se $_2$) and Ba $_9$ Hf $_3$ Se $_{14}$ (Se $_2$) crystal structures are provided in the Supporting Information.

CRediT authorship contribution statement

Subhendu Jana: Investigation, synthesis, Formal analysis, Writing – review & editing. **Eric A. Gabilondo:** Data collection, Formal analysis. **Paul A. Maggard:** Conceptualization, computation, electronic structure, Formal analysis, Methodology, Writing – review & editing.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

Data will be made available on request.

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Appendix A. Supplementary data

Supplementary data to this article can be found online at https://doi.org/10.1016/j,jssc.2023.124376.

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