

# Hybrid computational methods combining experimental information with Molecular Dynamics

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## Abstract

A goal of structural biology is to understand how macromolecules carry out their biological roles by identifying their metastable states, mechanisms of action, pathways leading to conformational changes, and the thermodynamic and kinetic relationships between those states. Integrative modeling brings structural insights into systems where traditional structure determination approaches cannot help. We focus on the synergies and challenges of integrative modeling combining experimental data with molecular dynamics simulations.

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## 1. Introduction

Techniques like x-ray crystallography[1] provide an exquisite picture of the average structure of stable conformations. But challenges remain for many systems including those unsuitable for crystallization, characterizing ensembles, states with low populations, and the transition pathways between these states. Fortunately, many experimental techniques such as NMR, FRET, DEER, PREs, chemical crosslinking, and others offer indirect structural information that can be obtained even in challenging situations[2, 3].

When enough information is available (data-rich regime), the system is highly constrained, and the data typically defines a narrow **uncertainty** ensemble[4], which is **in some cases** deposited in the protein data bank (PDB)[5]. **Choices such as the computational method and how the data is modeled can affect this ensemble.** Increasingly, however, researchers operate in the data-poor regime, where the system is only weakly constrained so that the data alone is insufficient to fully define the structural ensemble. By *integrating* data from multiple experiments, it is possible to narrow down the possible structures[6]. Even in such scenarios, distinguishing between multiple models requires a *hybrid*

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approach involving computational software to explore conformational space and identify possible solutions compatible with the data.

Recently, the wwPDB-dev[7] was developed to accept models originating from integrative/hybrid approaches. Whereas the PDB contains over 200,000 structures, the wwPDB-dev holds just 112 entries as of January 2023. The stark difference arises from difficulty in identifying pipelines to model these challenging systems and the need for better assessment tools to validate the quality of the models[8]. This review focuses on integrative/hybrid modeling in which Molecular Dynamics (MD) techniques are used to generate models. Excellent reviews focus on other aspects of integrative/hybrid modeling[9, 6, 10<sup>•</sup>, 1, 11, 12].

MD is seeing a resurgence[13] thanks to improved force fields [14] and enhanced sampling techniques [15] leading to excellent agreement between experiments and simulation techniques [3]. Efforts to synergize with new sources of experimental data provide optimism for their role in integrative approaches[6, 12, 1]. However, as each experimental technique provides different outputs and uncertainties, there is no unique recipe for hybrid modelling[8, 16]. For instance, density maps can be used to restrain residue/atomic positions[17, 9], many techniques provide distance or orientation information between parts of the molecule[18, 19], and others provide average or ensemble information[20]. MD samples ensembles of conformations that, when processed using statistical mechanics principles, provide insights about the relevant states of the system. Experimental data can be used to bias the ensemble, affecting the probability of sampling different regions in the energy landscape. The resulting ensembles can be processed to learn about states compatible with the data and physics model. Alternatively, data can be used with unbiased MD ensembles to select a subset of structures compatible with the experimental information. The challenges remain similar to other integrative pipelines: determining the number of states represented by the data, how to model uncertainties, or how to validate the ensembles

## 2. Sampling strategies

The large phase space available to biomacromolecules challenges the identification of important regions (states). Multiple approaches such as quasi-static minimization, random tree forest, or normal mode analysis to name a few have been used to sample phase space. What makes techniques such as MD and Monte Carlo (MC) unique is the foundation of these sampling strategies on physical principles, such as detailed balance, that relates the explored ensembles to the relative importance of different regions of phase space through statistical mechanics. It is this physical foundation that allows us to determine thermodynamic (e.g., free energies) and kinetic (e.g., binding rates) properties. The more accurate the underlying representation of the potential energy landscape (given by the force field), the better agreement MD/MC-based sampling strategies will have with experiments.

In recent years, force field development efforts have increased, leading to a variety of force fields suited for different systems [21]. The type of experimental data as well as the initial structural knowledge determine the **type of MD sampling strategy to use**[15]. For example, describing the ensemble of conformations available for a known folded structure that is compatible with FRET data might not require access to all configuration space—only appropriate fluctuations around the starting configuration need to be sampled. On the other hand, processes like binding, folding, or describing IDP ensembles will require extensive coverage of configuration space. In *informed sampling* approaches, the data is directly used to bias sampling, leading to ensembles that satisfy the data; whereas in *uninformed sampling*, the data is used in the post-analysis stage to either select structures or reweight the ensemble to obtain agreement with experimental measurements (see Figure 1).

### 2.1. Informed search

The general premise in informed search is that we know some properties about the end-states and incorporate the knowledge as restraints to guide the system. Often this data is evaluated on the fly on the structure that is being sampled by using a *forward model*[22, 23, 24, 25]. However, experimental data represents an ensemble average, thus, imposing restraints on a single structure could inappropriately bias the results. Alternatively, some groups use time-averaged restraints or ensemble average restraints[26] to represent the ensemble nature of the data better[27]. For instance, XL-MS data might contain an ensemble where a residue might be involved in a particular cross-link in one conformation, and in an alternative cross-link in another conformation [28]. As a second example, the mapping between single structures and NMR observables (e.g. NOESY data) leads to well-known errors. Lindorff-Larsen and his group showed that when multiple states give rise to NOE observables, a consensus structure that agrees with the data might not capture the complexity of the system[29•].

In recent years, this type of informed search has been framed in terms of Bayesian inference to account for the uncertainties arising from the force field, data, and forward model used[8, 30, 31, 32]. Information-driven sampling can thus overcome limitations in the force field, and supplement the experimental data with a physics-based prior to identify structures and states that either method alone could not[23, 33].

### 2.2. Uninformed search

These approaches yield the prior distribution based on the force field redand work best when starting from a native-like structure. Enhanced sampling methods such as generalized ensemble, weighted ensemble, adaptive sampling, or accelerated MD are also commonly used for higher efficiency than conventional MD[15]. The goal is to promote a broad exploration of the energy landscape. **The prior should reflect the Boltzmann distribution based on the force field used – hence, removing any potential bias used in enhanced sampling simulations is important. Failure to do so leads to poor priors.**

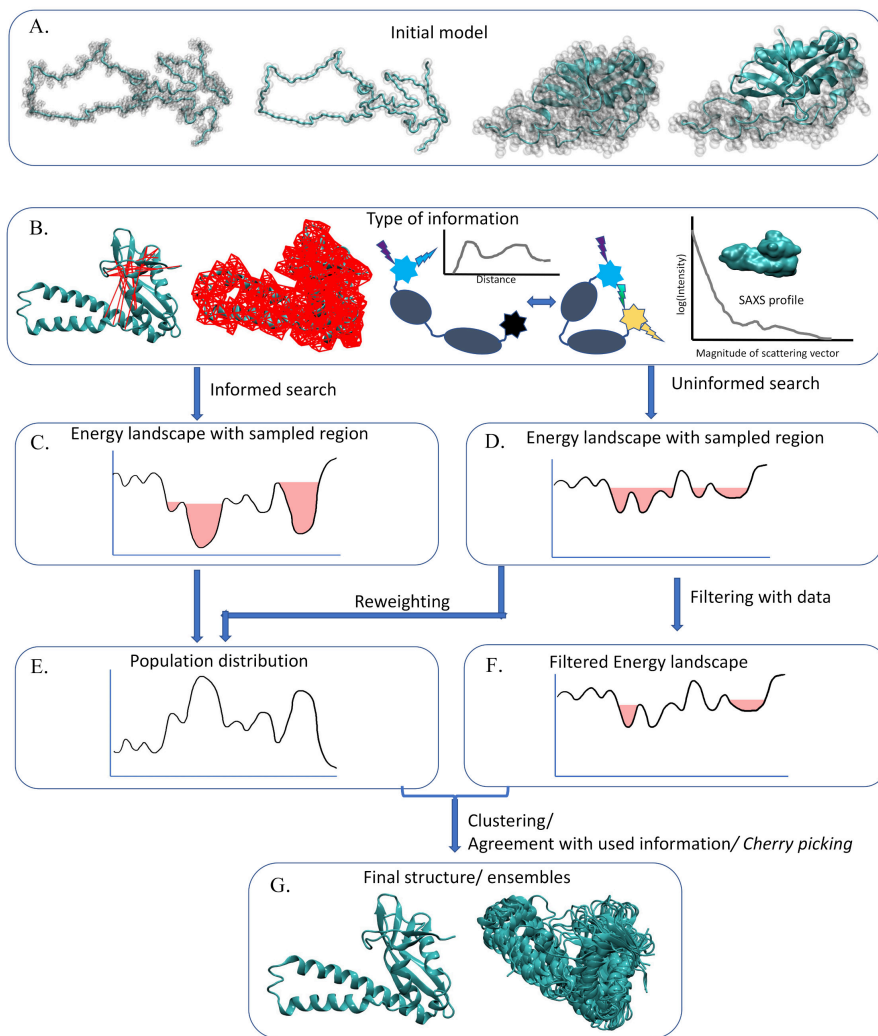


Figure 1: **Schematic representation of integrative modelling.** A. Initial models might represent extended or native conformations in an all-atom or coarse representation. B. Schematic of different types of information used to restrain simulations such as pair-wise restraints or density maps. C. *Informed search* introduces energy penalties in regions incompatible with data, focusing exploration on a few energy basins (filled in red). In contrast, *Uninformed search* (D) does not prioritize specific regions of the landscape. E. Analysis of the population distribution of either the prior (*uninformed search*) or posterior (*informed search*) yields the relevant states. F. Alternatively, the distributions can be filtered in accordance to their agreement with experimental data. G. Final representative structure(s) or ensembles that satisfy the data.

### 3. Choosing Representative Models from MD ensembles

Traditionally, similarity measures and dimensionality reduction techniques followed by clustering provide information about the relevant states in the system and their relative importance. More recently, Markov State Models (MSM)[34, 35] are becoming increasingly popular to provide kinetic information on the relationships between states. The analysis is straightforward when the ensembles are unbiased and requires prior reweighting otherwise[36].

The availability of data can then help choose the most compatible structures from the ensemble. For instance, data is used to reweight ensembles and choose representative structures or distribution of structures[37, 20]. The most popular approaches use maximum entropy, maximum parsimony, or Bayesian inference principles[38, 16, 39<sup>•</sup>, 40, 41]. In maxEnt approaches, the relative entropy with respect to the original ensemble (typically measured as a Kullback-Leibler Divergence, see eq. 1) is minimized. Thus, maintaining the original weights from the simulation will have the minimum cross-entropy – while selecting a single structure (*cherry – picking*)[42] will have the maximum relative entropy. The latter was preferred when limited sampling and force field inaccuracies were prevalent. However, with improved force field and sampling, there has been a shift towards ensemble-based methods to represent the system.

$$S(p_1|p_0) = \sum_i^N p_1(x_i) \ln \frac{p_1(x_i)}{p_0(x_i)} \quad (1)$$

Having a good overlap between the model and experimental evidence for the relevant regions of configuration is key to successful reweighting. A recent work describing IDP ensembles finds that the quality of the force field (prior distribution) is more important than the re-weighting method[43]. In other words, reweighting techniques can never recover information about a region that has not been sampled. These approaches are also useful to study conformational transitions through a two-step process which first involves the construction of an MSM, followed by a *refinement* with FRET data through an unsupervised learning model[44].

### 4. Challenges in hybrid modeling

#### 4.1. Number of states to represent the system

Proteins are dynamic molecules, accessing multiple states that explain structure/function relationships. While the information in the PDB typically yields information about a single state (either as a single structure or narrow ensemble), there are multiple computational tools and experimental approaches that can then use the initial structure to identify other relevant states that explain function. A common challenge in integrative approaches is knowing if the measured experimental observables originating from different experiments represent the same state, or if the observed signal arises from multiple states. When signals between different states overlap, advanced methods such as those based

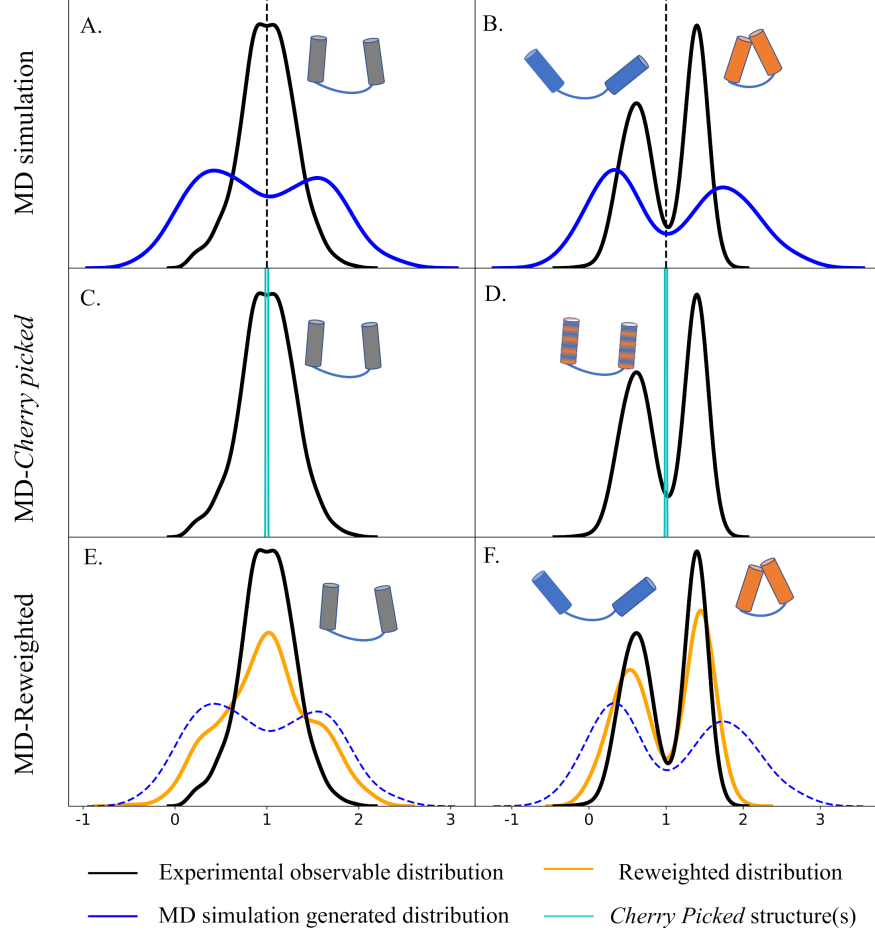


Figure 2: **Scheme for selecting structure(s)** based on distributions of an arbitrary property coming from experiments (black line) or simulations (blue line). The left panel represents an scenario where the experimental data has a unimodal distribution around the average observable (A). In this scenario, choosing a cherry-picked single structure (cyan) (C) or reweighting the MD ensemble (orange) to identify the highest population cluster will provide similar results. On the right panel, the system has two conformations leading to a bimodal distribution of the experimental observable (B). The cherry-picked average structure from the MD distribution is a bad representation of the system (D). However, reweighting the MD ensemble based on the experimental data correctly represents the underlying experimental distribution."

on maximum entropy are needed to identify the **different** states present in the distribution[45••, 46].

MD approaches, on the other hand, typically find hundreds or thousands of states through clustering of their ensembles – further classification into metastable states identifies a smaller set of states to compare with experiments[47, 48, 49]. When this process of classification benefits from experimental data, it can further help in identifying multiple biological states[50, 51]. **In this context, it is hard to ignore the progress from machine learning methods such as AlphaFold2[52] can also generate thousands of diverse structures of proteins by making clever use of sub-sampled or clustered multiple sequence alignments[53]. As with MD, agreement with experimental data can be used to choose high-accuracy structures representing different states from these ensembles. However, these ensembles lack the physics to relate thermodynamic/kinetic properties from the states, can only be used for systems trained on large databases (e.g. the PDB), include implicit biases based on databases (e.g., holo vs apo structures), and are not yet sensitive to small perturbations such as single point mutations.**

#### *4.2. Uncertainty in the data*

It remains challenging to separate errors in the physical models (force fields), experiments, and how the data is modeled (e.g., forward models)[16, 8]. Consequently, the error bars and uncertainties reported by different methods and groups do not necessarily reflect the same information [45••] leading to significant discrepancies in the reported uncertainties and lack of robustness in predictions across methods[45••]. A blind study for modeling dynamical systems using smFRET data assessed the performance of 19 participants. Participants arrived at similar results, separating the experimental signal **originating** from conformational dynamics and other sources that increase ambiguity. The study helped to define standards for error analysis and propagation in the field[54]. **A similar community-wide assessment of the reproducibility of SAXS and SANS data[55] for a set of proteins emphasizes current limitations in the field such as accurate solvent subtraction.**

#### *4.3. The need for reference standards*

Hybrid modeling is an umbrella term for many possible combinations of computational methods and sources of experimental data. Clear protocols and standards exist for determining structures using data-rich regime techniques, such as X-ray crystallography, cryo-EM, or solution NMR. In contrast, the number of tools and, therefore, the number of ways to perform hybrid modeling has increased dramatically. Addressing some of the current limitations will require coordination between scientists with different expertise[56] in order to: 1) produce homogeneous and transferable protocols across research labs (experimental and computational), 2) increase reproducibility across integrative platforms given the same initial data, 3) reduce human intervention in modeling data, and 4) provide the protocols of how the data was modeled along with

the original data and output structures. Blind studies have revealed conceptual oversights[45••, 18] due to misinterpretation of what the data represents. These oversights often originate from the lack of standardized protocols, shared expertise, and lack of communication across multiple labs.

The different PDB Task Forces (<https://www.wwpdb.org/task/>) play a fundamental role in developing and enforcing standards for the community. For example, the NMR exchange format initiative (NEF) [57, 58] strives to create a self-describing format that integrative modeling programs can learn to read to model structures and write to incorporate information on how the data was modeled. **The Small Angle Scattering Task Force aims to test and benchmark different methods that use SAXS profiles to model biomolecules. To further these efforts, the experimental data and the associated structural models are deposited in the SAS Biological DataBase (SASBDB, [www.sasbdb.org](http://www.sasbdb.org))[59].** More initiatives and widespread adoption of data deposition in software-agnostic formats are needed for other sources of data, including smFRET [60]. Task forces further promote the deposition of centralized databases[59, 61, 62, 63], and models that contain information and unified protocols to promote reproducible and transferable open science. These centralized databases are still limited in some areas like mass spectroscopy[42], where increased awareness will help modelers develop better integrative tools.

As modelers develop software to integrate different types of data, there is a lack of compatibility across tools. Ideally, a method developed by one lab for integrating data from experiment A and a method from another lab for experiment B could be used in a *plug-and-play* style. In practice, different formats and other incompatibilities prevent combining such pipelines into a single workflow[64••].

#### 4.4. How is an ensemble validated?

One major question yet to be resolved is how to validate an ensemble prediction appropriately. Most methods measure ensemble average properties of some type, but many different distributions can produce the same average. The well-known Anscombe quartet[65] illustrates different distributions that have identical descriptive statistics (mean of both variables, variance of both variables, correlation between  $x$  and  $y$ , linear regression and  $R^2$  between  $x$  and  $y$ ). It is not possible to use the goodness of fit to assess which distribution is correct, as all four distributions agree with the available statistics equally well.

This phenomenon is widespread in integrative and hybrid modeling, where there can be many—typically infinitely many!—different ensembles that are in equally good agreement with the available data. Choosing some ensembles as more correct than others typically boils down to using physical models, and regularization principles like maximum entropy or maximum parsimony [30] as naively forcing a fit to the average quantity can often time lead to incorrect inferences (see Figure 2).

A major challenge facing the field is comparing the outputs of different tools. If two methods predict different ensembles and both ensembles are in equal



agreement with the data, how do we say which one is more correct than another? Certain modeling tools may make different assumptions with data, and understanding how that influences an ensemble remains challenging. On a similar note, the noise associated with different data types should be considered when validating an ensemble. All of this must be communicated to users of these tools and consumers of these models in a transparent and accessible way.

Finally, there are few or insufficient databases to view ensembles produced by hybrid or integrative modeling. Generally, the PDB database is not an appropriate venue for these models, and PDBdev lacks sufficient validation tests for the ensembles (like proCheck for X-ray crystal structures) [10<sup>•</sup>, 66]. **In recent years, the number of deposited models and experimental data in the SASBDB has increased rapidly, making it useful for validating models. However, this database is dedicated only to SAXS/SANS data, highlighting the need for similar databases to other types of experimental data.** For IDPs even these might not be good enough, requiring databases that consider ensembles[67].

## 5. Emerging applications of integrative modeling

### 5.1. Integrative/Hybrid approaches will provide insights into cellular assemblies

As new sources of experimental data and their uncertainties become more prevalent, we see a wide range of spatiotemporal scales that dictates the need for atomistic, Coarse-grained (CG), or ultra-CG approaches[68, 69<sup>•</sup>, 70]. For instance, Hi-C restraint data is used to model genome assemblies [71, 72, 73]. With growing interest in these areas, new computational methods arise for developing and assessing benchmark sets [74]. Ultimately, the goal is to assemble large teams with overlapping expertise and a unified protocol to tackle the structural biology of whole cells (metamodeling)[75, 76, 77].

### 5.2. Advances in describing intrinsically disordered systems

Intrinsically disordered proteins (IDP) or proteins featuring intrinsically disordered regions (IDR) make up approximately 20% of eukaryotic proteomes [11]. IDPs are particularly difficult to model accurately, with force fields failing to reproduce the radius of gyration for completely disordered proteins. Most of the force fields fail to reproduce several experimental observables simultaneously[78]. Efforts to improve force field descriptions of IDPs is an ongoing area of research; however, improved descriptions of disordered proteins often come at the expense of modeling ordered proteins[79].

Force fields are often most effective at describing the local structure of ordered proteins. Hybrid approaches utilizing long-distance-based restraints offer an avenue to overcome the limitations of force fields (e.g., compact structures). For example, combining replica exchange discrete molecular dynamics (DMD) with restraints derived from FRET and DEER experiments [80] overcomes the accuracy limitations of DMD and samples helix-coil transitions in SNAP-25, an IDP. Similarly, using NMR-based Bayesian reweighting [81], SAXS-based ensemble optimization methods[82], or combining multiple experiments such as

NMR, SAXS, and single molecule FRET[83•] capture the ensembles of IDP conformations. A recent review discusses approaches to studying IDP conformational ensembles in detail[84].

## **6. Our current opinion: the ongoing efforts to standardize experimental outputs and computational pipelines will lead to a flourishing integrative structural biology community**

Hybrid modeling holds the promise to solve problems in structural biology that other methods alone could not. With increased standardization, we expect better modeling tools and more efficient workflows that will lead to a dramatic increase in wwPDB-dev depositions over the next decade.

## **7. Conflict of interest statement**

The authors declare no conflict of interest.

## **8. Acknowledgements**

The authors thank the Natural Sciences and Engineering Research Council of Canada (NSERC), the Canada Foundation for Innovation for their support, and the National Science Foundation. SL thanks the Canada First Research Excellence Fund for his postdoctoral fellowship. JLM thanks the Canada Research Chairs program. AP thanks support from the NSF CAREER award CHE-2235785.

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