

Unveiling the white dwarf in J191213.72 – 441045.1 through ultraviolet observations

Ingrid Pelisoli¹,¹★ Snehalata Sahu¹, Maxim Lyutikov², Maxim Barkov³, Boris T. Gänsicke¹,¹ Jaco Brink^{4,5}, David A. H. Buckley^{4,5,6}, Stephen. B. Potter^{4,7}, Axel Schwöpe⁸ and S. H. Ramírez¹

¹Department of Physics, University of Warwick, Gibbet Hill Road, Coventry, CV4 7AL, UK

²Department of Physics and Astronomy, Purdue University, 525 Northwestern Avenue, West Lafayette, 47907 IN, USA

³Institute of Astronomy, Russian Academy of Sciences, 119017 Moscow, Russia

⁴South African Astronomical Observatory, PO Box 9, Observatory, 7935 Cape Town, South Africa

⁵Department of Astronomy, University of Cape Town, Private Bag X3, 7701 Rondebosch, South Africa

⁶Department of Physics, University of the Free State, PO Box 339, 9300 Bloemfontein, South Africa

⁷Department of Physics, University of Johannesburg, PO Box 524, 2006 Auckland Park, South Africa

⁸Leibniz-Institut für Astrophysik Potsdam (AIP), An der Sternwarte 16, D-14482 Potsdam, Germany

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ABSTRACT

J191213.72 – 441045.1 is a binary system composed of a white dwarf and an M-dwarf in a 4.03-h orbit. It shows emission in radio, optical, and X-ray, all modulated at the white dwarf spin period of 5.3 min, as well as various orbital sideband frequencies. Like in the prototype of the class of radio-pulsing white dwarfs, AR Scorpii, the observed pulsed emission seems to be driven by the binary interaction. In this work, we present an analysis of far-ultraviolet spectra obtained with the Cosmic Origins Spectrograph at the *Hubble Space Telescope*, in which we directly detect the white dwarf in J191213.72 – 441045.1. We find that the white dwarf has a temperature of $T_{\text{eff}} = 11485 \pm 90$ K and mass of $0.59 \pm 0.05 M_{\odot}$. We place a tentative upper limit on the magnetic field of ≈ 50 MG. If the white dwarf is in thermal equilibrium, its physical parameters would imply that crystallization has not started in the core of the white dwarf. Alternatively, the effective temperature could have been affected by compressional heating, indicating a past phase of accretion. The relatively low upper limit to the magnetic field and potential lack of crystallization that could generate a strong field pose challenges to pulsar-like models for the system and give preference to propeller models with a low magnetic field. We also develop a geometric model of the binary interaction which explains many salient features of the system.

Key words: binaries: close – binaries: general – stars: individual: J191213.72 – 441045.1.

1 INTRODUCTION

Binary white dwarf pulsars are systems composed of a fast spinning white dwarf and a late-type main sequence star that show strong pulsed emission on the white dwarf spin period, detectable from radio to X-rays (Marsh et al. 2016; Pelisoli et al. 2023). Their broad-band luminosity cannot be explained by the stellar components alone, nor by any accretion mechanisms: they have low X-ray luminosities, display no aperiodic broad-band variability (also referred to as flickering, e.g. Scaringi 2014) characteristic of accreting systems, and typically only show narrow emission lines, indicating that no significant accretion occurs (e.g. Garnavich et al. 2019). Unlike the canonical neutron star pulsars, it is believed that the source of emission is intrinsically tied to binarity and is due to magnetic interaction between the two stars: free electrons are accelerated to near relativistic speeds as the magnetic field of the white dwarf sweeps past the companion, generating non-thermal pulsed synchrotron emission

(Geng, Zhang & Huang 2016; Katz 2017; Takata, Yang & Cheng 2017; Lyutikov et al. 2020).

The prototype of this class is AR Scorpii (AR Sco, Marsh et al. 2016), which was serendipitously discovered after being misclassified for many years as a δ -Scuti pulsating star, due to the orbital modulation resembling the saw-tooth shape shown by the light curves of radial pulsators. In reality, the observed 3.56-h modulation is also seen in the radial velocity of the M-dwarf companion, indicating a binary origin. The asymmetric shape can likely be attributed to phase-dependent contribution from non-thermal emission (Katz 2017). As well as the orbital modulation, high-speed optical photometry revealed strong pulses with a period of 1.97 min, interpreted as the beat period between white dwarf spin and orbit. The pulses were subsequently detected also in radio (Stanway et al. 2018) and X-rays (Takata et al. 2018). These strong pulses allow for precise timing of the white dwarf spin, which was found to be slowing down at a high rate of $P/\dot{P} = 5.6 \times 10^6$ yr (Gaibor et al. 2020; Pelisoli et al. 2022b). Additionally, strongly pulsed (~ 90 per cent pulse fraction) linear polarization, of up to 40 per cent, was also detected (Buckley et al. 2017), primarily modulated at the 1.95-min spin period. This was

* E-mail: ingrid.pelisoli@warwick.ac.uk

consistent with a strong dipole field ($\gtrsim 200$ MG), exhibiting beamed synchrotron emission within its magnetosphere (Potter & Buckley 2018). The strong magnetic field was inferred from the assumption that the luminosity is dominated by synchrotron emission from a rotation-powered dipole (Marsh et al. 2016; Buckley et al. 2017).

The combination of a fast spin, suggestive of an initially low magnetic field ($\lesssim 10$ MG), allowing the white dwarf to accrete and gain angular momentum, and rapid spin-down, pointing at a high magnetic field ($\gtrsim 100$ MG) capable of providing a synchronising torque, made of AR Sco a challenge to models of accreting binaries. Two main classes of models were put forward trying to reconcile AR Sco’s puzzling observed characteristics:

(i) *High magnetic field*: Katz (2017) proposed that the rapid spin-down could be explained by magnetic torque, which would require the white dwarf and M-dwarf to have magnetic fields of ~ 100 MG and ~ 100 G, respectively. In this scenario, the spin-down power is dissipated in the atmosphere of the M-dwarf by magnetic reconnection, which produces the observed synchrotron radiation. Similar magnetic field strengths were assumed by Geng, Zhang & Huang (2016) and Takata, Yang & Cheng (2017) in their modelling of AR Sco’s pulse profile and spectral energy distribution. The downside of these models is that such a high magnetic field would prevent the white dwarf from accreting enough matter to explain its present spin period – a very large mass transfer rate of up to $\dot{M} \sim 10^{-4} M_{\odot} \text{ yr}^{-1}$ (Ghosh & Lamb 1979; Lyutikov et al. 2020) would be required to compress the magnetosphere for enough accretion to occur. Such a rate is at least 10^5 times greater than estimated values for similar binaries (Pala et al. 2022). Additionally, there is to date no direct detection of AR Sco’s magnetic field. Garnavich et al. (2021a) constrained it to $B \lesssim 100$ MG based on the lack of Zeeman splitting of the Ly α line.

(ii) *High mass-transfer rate*: An alternative model was proposed by Lyutikov et al. (2020), who suggested that the magnetic field cannot be larger than ~ 10 MG for the white dwarf to have been spun up to current rates. They assumed a more typical mass transfer rate of $\dot{M} \sim 10^{-9} M_{\odot} \text{ yr}^{-1}$ and argued that, if the ionization rate in the M-dwarf wind is not high, neutral particles will travel through the magnetic field lines of the white dwarf unaffected. Close enough to the white dwarf, they are exposed to ultraviolet radiation and ionized, couple to the magnetic field and are then centrifugally expelled from the system, carrying away angular momentum. This would imply that AR Sco is in a propeller state similar to AE Aquarii (e.g. Patterson 1979; Chincarini & Walker 1981; Eracleous & Horne 1996) and LAMOST J024048.51 + 195226.9 (Thorstensen 2020; Pretorius et al. 2021; Garnavich et al. 2021b; Pelisoli et al. 2022a). However, unlike the confirmed propellers, AR Sco shows no observational evidence of flaring, which argues against a propeller behaviour.

A recent model for the evolution of magnetic white dwarfs in close binary stars proposed by Schreiber et al. (2021) could potentially reconcile a fast spinning white dwarf and a high magnetic field without the need for unfeasible mass transfer rates. They proposed that the white dwarfs in magnetic cataclysmic variables were not born magnetic, allowing for unimpeded accretion-driven spin-up, and only became magnetic due to a rotation- and crystallization-driven dynamo (Isern et al. 2017). This proposition resolves the theoretical issue with spinning up a highly magnetic white dwarf, reinstating models with a high magnetic field as a possibility. In short, the two proposed classes of models remain possible, but with observational shortcomings in both cases: there is no detection of a high magnetic field in AR Sco, arguing against models requiring a strong field, but there is also no strong evidence

Table 1. Details of each *HST* visit to J1912 – 4410.

Visit	Orbit	Exposure start (UTC)	Exposure duration (s)
1	1	2023-03-18 21:24:46	2508.192
	2	2023-03-18 22:54:34	2782.144
	3	2023-03-19 00:29:45	2782.144
	4	2023-03-19 02:04:57	2782.144
2	5	2023-05-05 15:22:14	2508.160
	6	No data acquired	
	7	2023-05-05 18:28:47	2782.176
	8	2023-05-05 20:07:37	2782.176
3	9	2023-05-06 15:12:58	2508.128
	10	No data acquired	
	11	2023-05-06 18:18:17	2782.176
	12	2023-05-06 19:53:40	2782.144

of flaring, contradicting models proposing a high mass-transfer rate.

The discovery of a second binary white dwarf pulsar, J191213.72 – 441045.1 (henceforth J1912 – 4410), by Pelisoli et al. (2023) and Schwöpe et al. (2023) provided the first opportunity to test the theoretical models put forward to explain AR Sco. Like the prototype of the class, J1912 – 4410 contains a compact object and an M-dwarf in a close binary. The orbital period is 4.03 h and the spin period, which in this case dominates over the beat, is 5.3 min and is also detected from radio to X-rays. The length of the spin period, over a factor of four longer than any confirmed neutron star pulsar (Caleb et al. 2022), led to the interpretation of the system as a second binary white dwarf pulsar. Due to its recent discovery, the spin-down of the white dwarf has not been constrained yet, but the spectral energy distribution shows excess flux compared to the stellar components, in a similar manner to AR Sco, pointing at possible spin-down power.

The current theoretical framework makes three observables key in determining the feasibility of proposed theoretical models: (i) the white dwarf magnetic field, (ii) the white dwarf temperature (which determines the level of crystallization), and (iii) the mass transfer rate. Pelisoli et al. (2023) reported potential flaring in J1912 – 4410, which could suggest a significant mass-transfer rate, but pointed out that continuous monitoring is required to confirm their findings, in particular as the flares could potentially be attributed to the M-dwarf companion rather than to a propeller behaviour. The white dwarf magnetic field and its temperature, on the other hand, could not be determined as the optical emission is completely dominated by the irradiated face of the M-dwarf; only an upper limit of $T_{\text{eff}} < 13\,000$ K was estimated. This work fills this gap by analysing far-ultraviolet (FUV) *Hubble Space Telescope* (*HST*) observations of J1912 – 4410, which reveal the spectrum of the white dwarf.

2 OBSERVATIONS AND DATA REDUCTION

J1912 – 4410 was observed during Cycle 30 for 12 orbits, split into three visits of four orbits each. Exposure details of each visit are shown in Table 1. For both visits 2 and 3, failure in guide-star acquisition prevented science exposures for one of the four orbits. We used the Cosmic Origins Spectrograph (COS) instrument with the G140L grating centred at 1105 Å, providing flux-calibrated coverage between ≈ 1110 and ≈ 2150 Å. TIME-TAG mode was employed, where the position and detection time of every photon is recorded with 32 ms precision in so-called `corrtag` files.

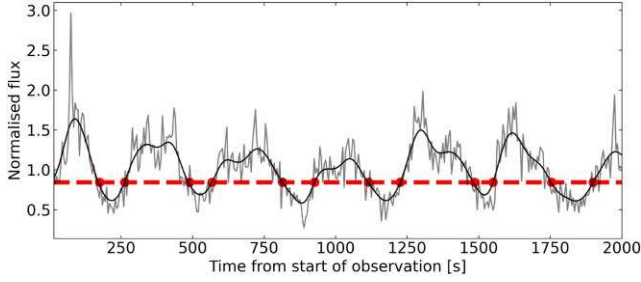


Figure 1. A section of J1912 – 4410's light curve, obtained during orbit 8, illustrating how the boundary of pulses was defined. The grey line shows the normalized light curve and the black line shows its smoothed version. The red dashed line marks the 30 percent percentile. The crossing points between the smoothed data and this line were assumed as the change between peak and off-peak status.

We downloaded all `corrtag` files and used the `LIGHTCURVE` package¹ to obtain a light curve from the observations, masking `airglow`² features and limiting the wavelength range to 1100–2000 Å as preliminary inspection showed reduced signal-to-noise above 2000 Å. Following the approach that Garnavich et al. (2021a) employed for AR Sco, we use the light curve to identify the times of emission between the pulses, where the contribution from non-thermal emission should be at a minimum and the white dwarf can be revealed. Our approach was to first normalize the light curve to minimize the orbital modulation. To do this, we smoothed the light curve by convolving it with a Gaussian kernel with a width given by $\sigma = 50$ s, which dilutes the pulse contribution, and then divided the original light curve by the smoothed version. Next we smoothed the normalized light curve using a 5 s Gaussian kernel, to remove oscillations caused by noise. The boundary times between off-pulse and pulse contributions was then determined as the 30 percent quantile, as illustrated in Fig. 1.

New `corrtag` files were generated for peak and off-peak exposures using the `SPLITTAG` function from the `COSTOOLS` package.³ Spectra were then extracted for each file using the `COS` pipeline `CALCOS` (version 3.4.6) and downloaded reference files (version `hst_1080.pmap`). All contributions identified as between or during a peak were averaged to create the off-peak and peak spectra, respectively.

A similar procedure was applied to create orbital phase-resolved spectra. We created `corrtag` files and extracted spectra for 10 orbital phase bins of equal size (0.1). Finally, we also combined the two approaches to extract off-peak spectra only around orbital phase 0.5 (0.4–0.6), when the white dwarf is at inferior conjunction.

3 PHOTOMETRIC ANALYSIS

The obtained FUV light curve for J1912 – 4410 is shown in Fig. 2. Like for the radio, optical and X-ray data, the pulses are evident in the FUV data. The flux increases by up to a factor of ≈ 8 in a few tens of seconds. The Fourier transform of the data is shown in Fig. 3. The dominant frequency is consistent with the one interpreted by Pelisoli et al. (2023) as the spin ω of the white dwarf. The next strongest contribution is, however, from the *beat* frequency $\omega - \Omega$ (where Ω is the orbital frequency), which was remarkably undetectable in the

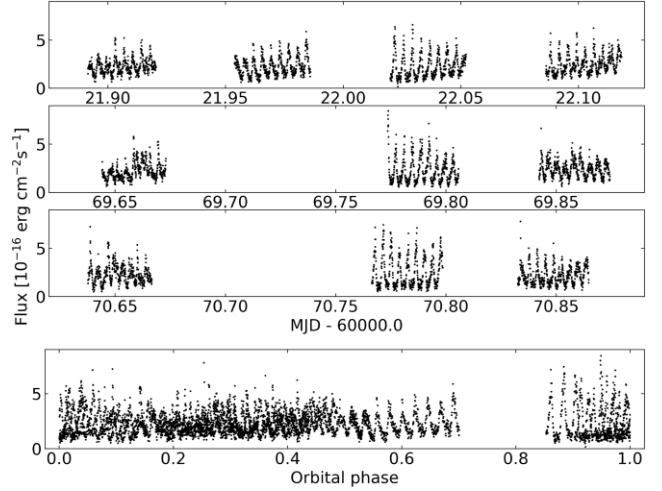


Figure 2. The top three panels show the light curve of J1912 – 4410 for each of the three *HST* visits, with flux integrated between 1100 and 2000 Å. The gaps between data correspond to different orbits; the large gaps in the middle panels are due to failure in data acquisition during orbits 8 and 10. The bottom panel shows all data folded to the orbital ephemeris of Pelisoli et al. (2023) to illustrate our phase coverage.

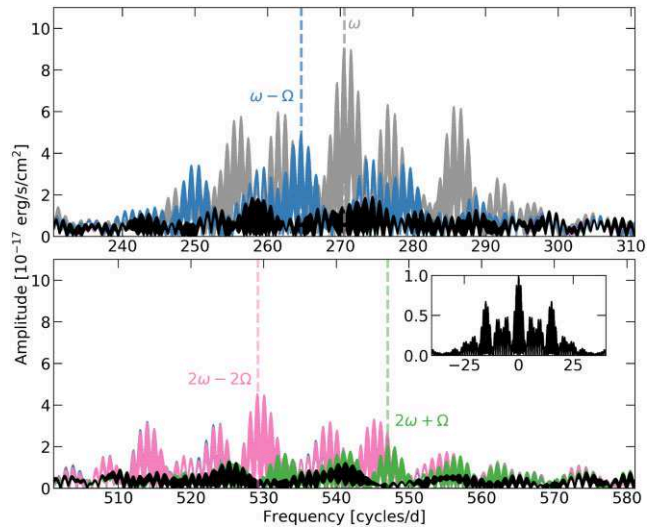


Figure 3. Fourier transform of the ultraviolet light curve of J1912 – 4410 around the spin frequency (top panel) and its first harmonic (bottom panel). The inset in the bottom panel shows the window function at the cadence of the *HST* observations. There is strong aliasing due to J1912 – 4410's orbital visibility. The different colours represent different pre-whitening stages, with the dominant frequency at each stage marked by a dashed vertical line of the same colour. The subtracted frequencies were, in order, ω (spin), $\omega - \Omega$ (beat), $2\omega - 2\Omega$ (beat's first harmonic), and $2\omega + \Omega$.

optical light curves. The next significant contributions around the spin and its first harmonic are from the beat's first harmonic (also detected in the optical) and from $2\omega + \Omega$.

Fig. 4 shows the FUV light curve folded to the spin ephemeris reported by Pelisoli et al. (2023), that is $BJD(TDB) = 2459772.142522(24) + 0.0036961693(10)E$, where E is an integer cycle number. Only the data within orbital phases 0.35 to 0.65 are used for the radio, optical and FUV plots, because the pulse shape shows some orbital dependence. As can be seen, the ephemeris seem to apply reasonably well to the FUV data. There is a hint of narrow

¹<https://github.com/justincely/lightcurve/>

²<https://www.stsci.edu/hst/instrumentation/cos/calibration/airglow>

³<https://github.com/spacetelescope/costools>

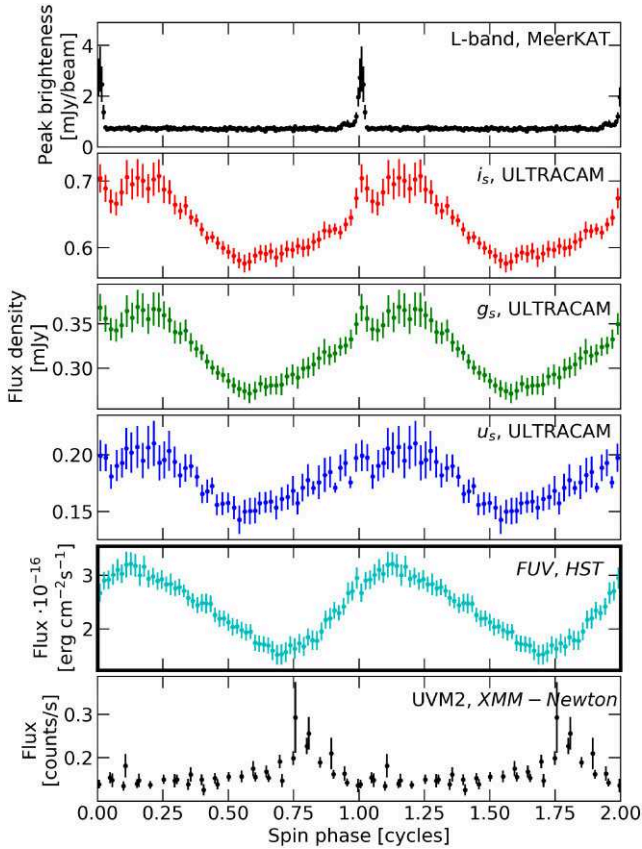


Figure 4. Data in the multiple available bands folded to the spin ephemeris. Radio (top), ULTRACAM (second, third, and fourth from the top), and X-ray data (bottom) are from Pelisoli et al. (2023). The far-FUV data (second panel from the bottom, with the thicker border) were obtained as part of this work.

peak, like the one dominant in radio and seen in the i_s , g_s , and u_s ULTRACAM bands, near phase 1.0 as expected. The broader pulse peaks shortly after phase 1.0, as also seen in the optical.⁴ With the adopted ephemeris, the optical broad pulse seems to be ≈ 0.25 ahead of the narrow pulse in phase, and the X-rays are ≈ 0.25 behind. The FUV data look somewhat transitional between the optical and the X-rays: the broad pulse peaks between the peak for optical and X-rays, and the pulse shape is a mix between the optical and X-rays. However, we caution that there seems to be a stochastic or at least not fully understood aspect to the behaviour of the pulses. Pelisoli et al. (2023) noted that, in optical data taken simultaneously with X-ray observations, the optical and X-ray broad pulses were aligned [as also noted in Schwöpe et al. (2023)], but these pulses were offset compared to the spin ephemeris, which could describe well longer optical observations taken before and after the X-ray simultaneous data (see their extended data fig. 4). In short, the observed offset might not represent a persistent behaviour and could depend on other system parameters.

As the FUV data extends the previous five-month baseline by over 9 months, it might be tempting to combine the *HST* data with that from Pelisoli et al. (2023) to further refine the spin ephemeris. However, given the strong dependence of the peak location with

⁴Note that the position of the broad peak compared to the narrow peak depends on the adopted ephemeris. Schwöpe et al. (2023) adopt slightly different ephemeris and find the narrow peak to appear after the broad peak.

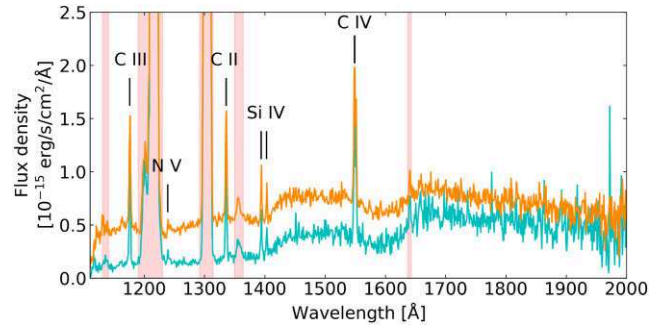


Figure 5. Spectra extracted from the peak (orange, top line) and off-peak (cyan, bottom line) exposures. The regions shaded in red are known airglow features. Some emission lines are likely stellar in origin and can be attributed to the irradiated face of the M-dwarf; these are indicated by the labelled black lines.

wavelength, that can unfortunately not be done. We have attempted to do so by following the same procedure as in Pelisoli et al. (2023), i.e. start from trial ephemeris to define windows around the expected location of peaks, cross-correlate the data in each window with a Gaussian function with width given by a standard deviation of 15 s to determine the times of maxima in each window from the maximum of the cross-correlation function, and repeat the procedure until the trial and fitted ephemeris are consistent. This resulted in a very poor fit of linear ephemeris, likely due to the natural shift between optical and FUV. In fact, the linear fit was so poor that an F -test indicated that the addition of a quadratic term would result in a significant improvement with a confidence level of over 99.9 per cent, but the quadratic term was highly dependent on the orbital phases and datasets included in the fit. In short, probing for spin-down cannot be done by combining data taken with significantly different filters, and will need to wait for more optical data extending the previous baseline.

4 SPECTROSCOPIC ANALYSIS

The obtained peak and off-peak spectra using all orbital phases are shown in Fig. 5. The emission lines are a combination of airglow features and emission lines likely originating on the surface of the irradiated M-dwarf. Features from the white dwarf, in particular the quasi-molecular H_2 absorption around 1600 Å, are visible for both peak (pulse) and off-peak (through) spectra, suggesting a significant contribution from the white dwarf at all spin phases, perhaps due to a favourable inclination. It is also noticeable that, even in the through spectra, there is significant flux at Ly α , whereas white dwarf models indicate near zero flux. This suggests that there is still some dilution from the pulsed emission. This remains true for a through spectrum extracted only around phase 0.5 (inferior conjunction of the white dwarf), which in fact is completely consistent with the spectrum obtained without any orbital phase constraint (see Fig. 6). Given that the only apparent effect of selecting on orbital phase was to decrease the signal-to-noise ratio, we carried out the analysis of the white dwarf using spectra from all phases.

To estimate the white dwarf spectrum and remove any diluting contribution, our approach followed Garnavich et al. (2021a) in subtracting a scaled version of the pulsed emission from the through spectrum. Removing the pulsed emission scaled by 20 per cent resulted in a near-zero flux consistent with white dwarf models. We used the resulting spectrum to estimate the white dwarf physical parameters (Section 4.1) and constrain its magnetic field (Section 4.2). We also analyse the phase-resolved spectra to investigate the orbital

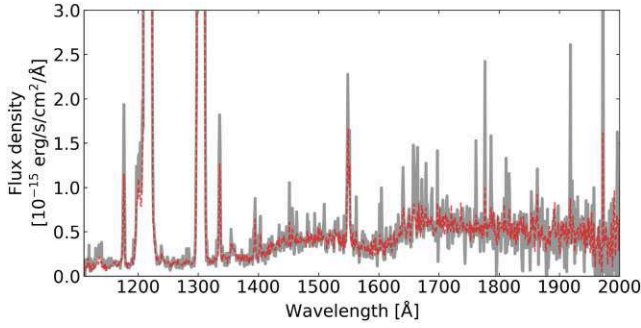


Figure 6. The solid grey line shows the spectrum obtained by extracting data only from the off-peak data between orbital phases 0.4 and 0.6. The red dashed line uses all off-peak data regardless of orbital phase. The difference in flux is seen at the metal emission lines, but Ly α and other white dwarf features show no significant change other than decreased noise when all phases are included.

dependence of the metal emission lines and derive dynamical mass constraints (Section 4.3).

4.1 Determining the white dwarf's physical parameters

We fit the white dwarf spectrum using white dwarf synthetic spectra computed from an updated grid of pure hydrogen atmosphere models based on Koester (2010). The updates include the recalculations of unified profiles of Ly α and Ly β using new atomic data (Santos & Kepler 2012; Hollands et al. 2017) and the use of Stark broadening profiles of Tremblay & Bergeron (2009). Convection is treated in the mixing length approximation parametrized with $\alpha = 0.8$. Line opacities are included for hydrogen, and molecular opacities for the quasi-molecules H_2 and H_2^+ . The fit was performed by χ^2 minimization, with the parallax fixed at the value reported in *Gaia* Data Release 3 (DR3; Gaia Collaboration 2016, 2023; Lindegren et al. 2021), 4.20 ± 0.08 mas, and reddening fixed at the value reported in 3D STILISM models, $E(B - V) = 0.035 \pm 0.004$ (Lallement et al. 2019). Emission lines were masked as they do not originate on the white dwarf. The parallax allows for a precise radius estimate, which combined with a mass–radius relationship, provides a mass estimate. We used the evolutionary La Plata models with a progenitor metallicity of $Z = 0.02$ and a hydrogen layer with a varying hydrogen mass fraction depending on the white dwarf mass ($\simeq 10^{-3}$ for masses less than $0.4 M_\odot$ to $\simeq 10^{-6} M_H/M_{WD}$ for $1.1 M_\odot$; Althaus, Miller Bertolami & Córscio 2013; Camisassa et al. 2016, 2019).

We carried out three different approaches to the spectroscopic fit: (i) fitting the estimated white dwarf spectrum (obtained by subtracting 20 percent of the pulse spectrum from the through), (ii) fitting the through spectrum with a white dwarf model and a power law (i.e. modelling the dilution with a power law rather than with the pulse spectrum), and (iii) fitting the through spectrum with a white dwarf model plus dilution from constant flux.

The resulting fits are shown in Fig. 7. For approach (i), we obtained a temperature of $T_{\text{eff}1} = 11452 \pm 75$ K and surface gravity with $\log g_1 = 7.97 \pm 0.04$. The parallax constrains the radius to $R_1 = 0.0131 \pm 0.004 R_\odot$,⁵ implying a white dwarf mass of $M_1 = 0.59 \pm 0.02 M_\odot$. Similar values are obtained when using approaches (ii) and (iii), as indicated in Table 2. Given that we obtain consistent

⁵We use subscript 1 to refer to white dwarf parameters, and 2 for M-dwarf.

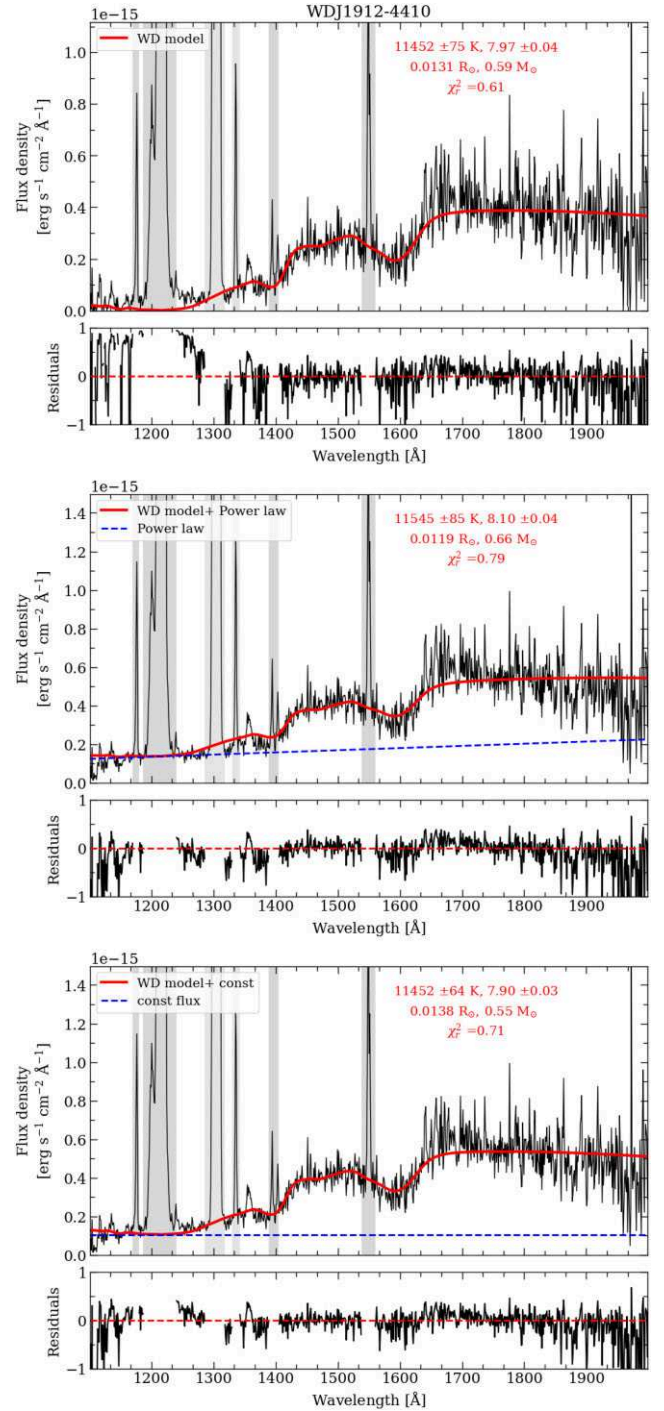


Figure 7. The top panel shows the estimated white dwarf spectrum in black and the best-fitting model in red. The emission lines that have been masked for the fit are indicated by the shaded grey areas. The bottom and middle panels show the through spectrum in black, the best model in red, and the model for the additional flux (power law or constant) as a dashed blue line. The best-fitting values (T_{eff} , $\log g$, radius, mass, and reduced χ^2) are labelled in red in all the figures.

values between all approaches, we adopt as final parameters the mean between the three methods, with uncertainty given by the standard deviation. This results in $T_{\text{eff}1} = 11485 \pm 90$ K and $M_1 = 0.59 \pm 0.05 M_\odot$.

Table 2. White dwarf parameters obtained using the three fitting methods described in the text.

Method	T_{eff} (K)	$\log g$	Radius (R_{\odot})	Mass (M_{\odot})	χ_r^2
(i)	11452 ± 75	7.97 ± 0.04	0.0131 ± 0.004	0.59 ± 0.02	0.61
(ii)	11545 ± 85	8.10 ± 0.04	0.0119 ± 0.004	0.66 ± 0.02	0.79
(iii)	11452 ± 64	7.90 ± 0.03	0.0138 ± 0.004	0.55 ± 0.02	0.71
Adopted	11485 ± 90	8.00 ± 0.09	0.128 ± 0.040	0.59 ± 0.05	

The last column reports the reduced χ^2 of each fit. The uncertainties are statistical only. The adopted values are the mean and standard deviation between the three approaches.

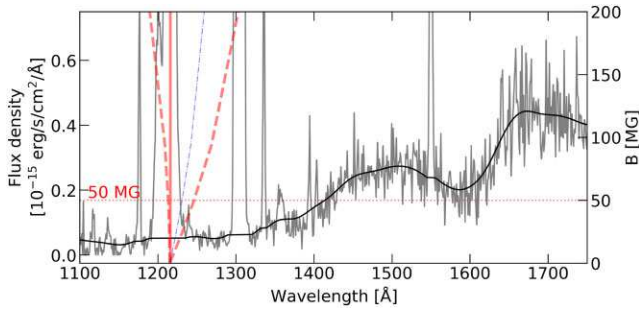


Figure 8. The grey line shows the white dwarf spectrum. The black line is the spectrum smoothed by masking the emission lines and convolving with a Gaussian of standard deviation equal to 5 Å. The solid vertical red line indicates the rest wavelength of Ly α , and the dashed red lines show the central wavelength of displaced Zeeman components according to models from Schimeczek & Wunner (2014) for the magnetic field strength indicated in the right-hand y-axis. The blue dot–dashed line shows the midpoint between the central component and the displaced component, that shows the larger shift (on the right). This is where we would expect an increase in flux if there was a magnetic field with a strength larger than ≈ 50 MG (the dotted horizontal line), as the gap between components would be beyond the geocoronal emission in Ly α .

4.2 Constraining the magnetic field of the white dwarf

Magnetic fields are detected in white dwarf spectra primarily due to Zeeman splitting of spectral lines. The existence of a magnetic field introduces a preferential direction, which lifts the degeneracy of energy levels on the magnetic quantum number m , leading to transitions with different energies for the same spectral line. The separation between line components depends on the strength of the magnetic field, thus allowing for a magnetic field estimate. The spectrum of J1912 – 4410 shows, however, no sign of Zeeman splitting, preventing a precise estimate of the white dwarf’s magnetic field. The lack of splitting can instead place an upper limit on the magnetic field, above which we would expect to see a sign of different line components. We used the energy levels calculated by Schimeczek & Wunner (2014) for hydrogen in a magnetic field to calculate the theoretical wavelength for the Zeeman split components of the $1s$ to $2p$ transition, which corresponds to Ly α . As illustrated in Fig. 8, up to a magnetic field of ≈ 50 MG, the gap between components would be filled by the strong geocoronal emission centred in Ly α . Above ≈ 50 MG, one of the gaps would be beyond the geocoronal emission and should be detected as an increase in flux. As this is not detected, we estimate that the magnetic field of the white dwarf in J1912 – 4410 is $\lesssim 50$ MG.

Another way to detect magnetic fields via spectroscopy, in particular for accreting systems, is to identify humps corresponding to the cyclotron frequency of electrons accelerated by the magnetic field (e.g. Schwöpe, Schreiber & Szkody 2006). We would expect

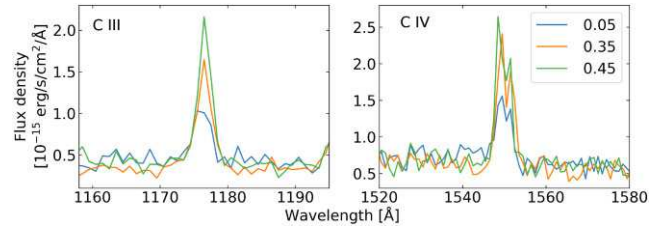


Figure 9. Spectra of two metal emission lines at three phase bins with a width of 0.1 and central value as indicated in the plot label. The emission peaks near phase 0.5 when the irradiated face of the M-dwarf is most visible.

cyclotron humps to be detected in the FUV for magnetic fields ~ 100 – 200 MG, hence the non-detection here makes fields in this range unlikely, though cyclotron humps for stronger fields would appear in the near-UV, beyond our wavelength coverage.

4.3 Inferring dynamics from the metal emission lines

The observed metal lines peak in strength at phase 0.5, when the irradiated face of the M-dwarf faces the line of sight (Fig. 9), suggesting that this is where they originate. Using the phase-resolved spectra, we have estimated radial velocities for the C III line at ≈ 1175 Å, the C II line at ≈ 1335 Å, and the Si IV line at ≈ 1394 Å. Other lines are either too weak or blended to yield good results. Radial velocity estimates were carried out by fitting a Gaussian to each line to estimate its observed central wavelength. We then folded the radial velocities using the orbital ephemeris of Pelisoli et al. (2023) and fitted them with $\gamma + K_2 \sin(2\pi\phi)$, where γ is the systemic velocity, K_2 is the radial velocity semi-amplitude, and ϕ is the orbital phase. The obtained fits are shown in Fig. 10. The overall behaviour is consistent with these lines tracing the M-dwarf’s heated hemisphere, although the C III radial velocities show scatter around phase 0.2. We find semi-amplitudes K_2 of 138 ± 69 , 160 ± 27 and 144 ± 18 km s $^{-1}$ for C III, C II and Si IV, respectively. Uncertainties were estimated via bootstrapping.

Although the uncertainties are large, the obtained values are systematically smaller than the amplitudes found for Pelisoli et al. (2023) for the Balmer emission lines. This suggests that the metal lines are originated further away from the M-dwarf and closer to the white dwarf and has implications for the Roche constraints. We repeat the same Roche analysis done in Pelisoli et al. (2023) taking the smaller semi-amplitudes derived from the metal lines into consideration. This alone constrains the mass ratio $q = M_2/M_1$ to a minimum value of $q = 0.21$ (left panel in Fig. 11). Requiring the compact object to have a mass lower than the Chandrasekhar limit increases the minimum q to 0.3, and given the K_2 difference between the centre of mass and the irradiated face set by the metal emission

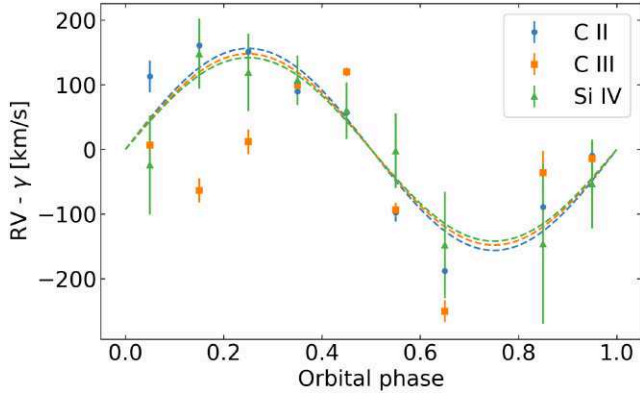


Figure 10. Radial velocities for three metal emission lines visible in J1912 – 4410's spectrum. The fitted systemic velocity of each line was subtracted because its systematic uncertainty is very large, as the central wavelength of these lines is not precise.

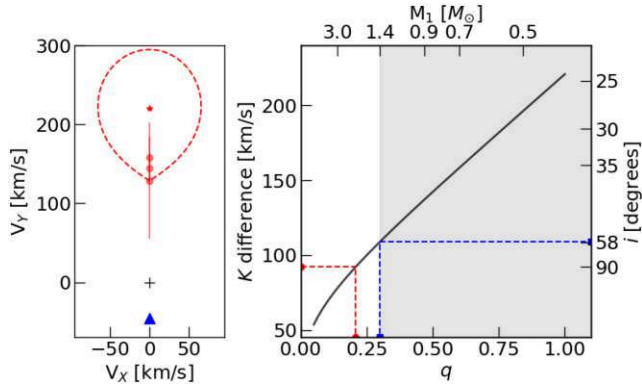


Figure 11. The left panel shows different semi-amplitude measurements obtained from phase-resolved spectra. The red star marks the location of the M-dwarf centre of mass according to Na II absorption line measurements (Pelisoli et al. 2023). The red circles mark the measurements we derived for C III, C II, and Si IV. The red dashed line is the Roche lobe of the M-dwarf for $q = 0.21$, the minimum to encompass the derived semi-amplitudes. The black cross and blue triangle mark the centre of mass of the system and of the white dwarf, respectively. In the right panel, the black line shows the semi-amplitude difference between the M-dwarf centre of mass and its irradiated face, assuming the M-dwarf is Roche-lobe filling. The right-hand y-axis shows the orbital inclination that would correspond to the K_2 difference in the left-hand axis. The observed K_2 difference sets the minimum q at an inclination of 90° (red dashed lines). The shaded grey area constraints M_1 to white dwarf values, in which case the minimum q is 0.3. Given the semi-amplitude differences measured here, this minimum q corresponds to a maximum inclination of about 58° (blue dashed lines).

lines, this implies a maximum orbital inclination of $i \approx 58^\circ$ (right panel in Fig. 11).

5 GEOMETRIC MODEL

Based on the observed properties of J1912 – 4410 and on the model by Lyutikov et al. (2020), we propose a geometric model (illustrated in Fig. 12) that can explain many of J1912 – 4410's characteristics. At the core is the idea that the emission of the white dwarf is seeded by the interaction with the companion. The emission originates in several regions and has different mechanisms.

We interpret the radio emission as electron-cyclotron maser (e.g. Melrose 2017), operating only in the white dwarf's magnetic

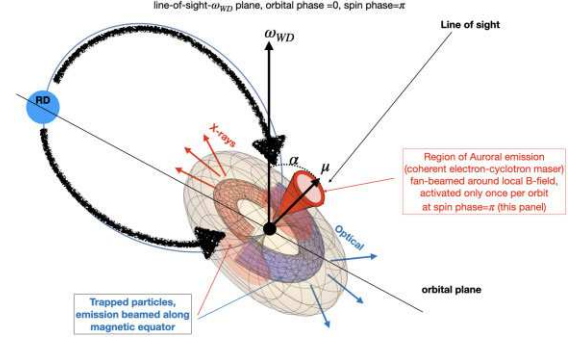


Figure 12. Geometry of the system at orbital phase 0 (superior conjunction of the white dwarf) at the moment when the magnetic moment of the white dwarf (μ) is in the same plane as the white dwarf spin (ω_{WD}) and the line-of-sight plane (spin phase = 0.5). A stream from the companion reaches the white dwarf in the magnetic polar region and produces auroral emission (coherent electron-cyclotron maser). Additional emission originates from particles trapped in the Van Allen radiation belts. The resulting emission is mildly beamed along the magnetic equator.

polar region and producing emission approximately along the local magnetic field (magnetic moment). This explains one narrow pulse per spin period. In addition, radio emission is activated only when particles from the M-dwarf can reach the polar region. This explains why the auroral emission is only observable once per orbit [orbital phase 0.5, see fig. 2 in Pelisoli et al. (2023)]: particles from the companion can reach the polar regions twice per orbit, at orbital phases 0 and 0.5 but, since the emission is highly beamed, it is observed only at orbital phase 0.5. This geometrical configuration is fixed by the fact that radio is seen only at the superior conjunction of the M-dwarf. Activation at the superior or inferior conjunction depends on the relative orientation of the line of sight, the white dwarf's spin and the magnetic moment, see Figs 12 and 13. This geometrical 'seeding' model – that the emission from the white dwarf is induced by the companion – works well for explaining the narrow-peaked radio emission.

To model this polar emission we assume that it has a Gaussian profile, so that instantaneous brightness is a Gaussian function of the angle between the line of sight and magnetic moment μ , with a given width [this is a slight simplification, as electron cyclotron maser is expected to have a conical shape around the local magnetic field (Melrose 2017)]. For the equatorial emission, we assume a Gaussian band along the equator and integrate over equatorial points. This results in the emission shown in Fig. 14.

The broad X-ray and optical pulses present a challenge – primarily because of the observed *single* peak per spin period. We have investigated two possibilities:

- (i) The broad X-ray and optical pulses are due to emission by trapped particles in the Van Allen belt, causing beamed emission along the magnetic equator rather than the pole, which would explain the phase shift between the broad and narrow pulses. This X-ray and optical emission is expected with a phase shift of approximately (and not necessarily exactly) ± 0.25 compared to the auroral emission. In fact, the broad pulses can peak around ± 0.25 , as can be seen in Fig. 4. One important fact remains unexplained by the geometrical model is that it predicts a double peak for the equatorial emission. Instead, X-rays show one single peak (at -0.25), while optical shows another single peak (at $+0.25$), with different intrinsic spread. Closer inspection of the ULTRACAM data from Pelisoli et al. (2023)

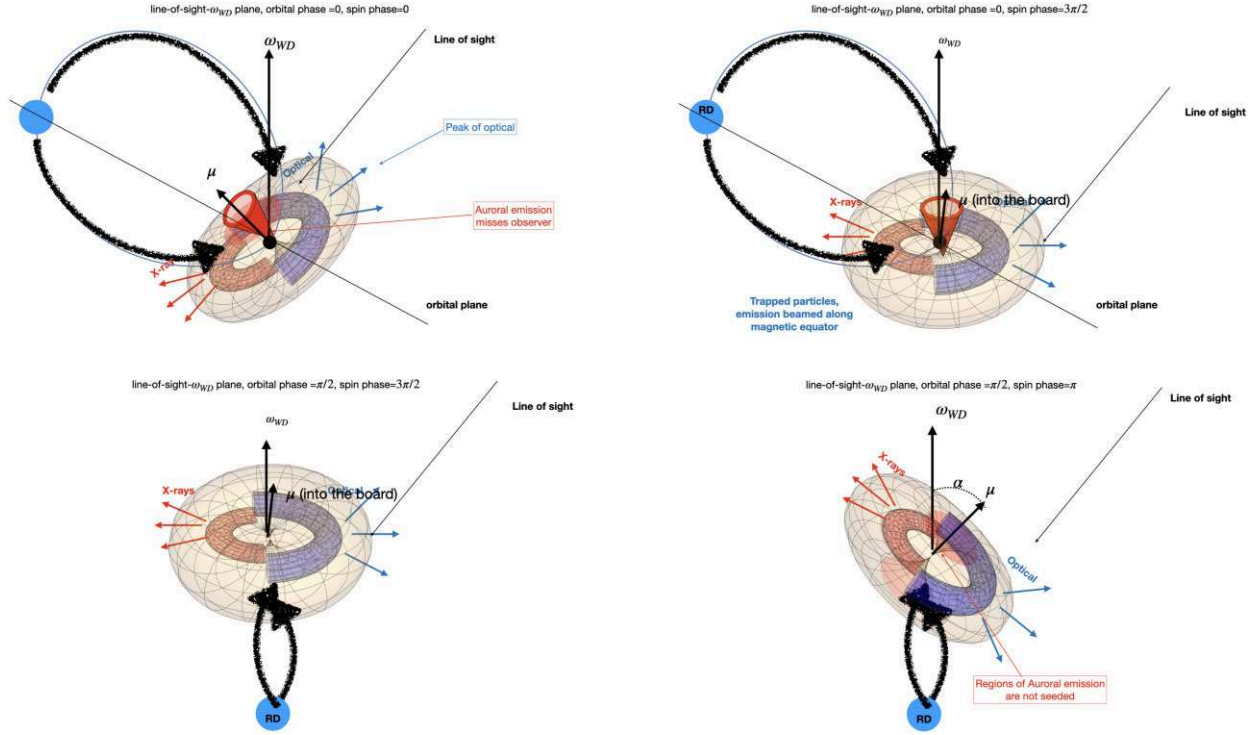


Figure 13. Examples of configurations at selected orbital and spin phases. The M-dwarf is represented by the blue circle and seeds particles towards the white dwarf, whose magnetic moment is represented by the red cone and visible only at certain spin phases as indicated. This geometrical model explains the observed behaviour of J1912 – 4410 based on the alignment of different emission regions with the line of sight.

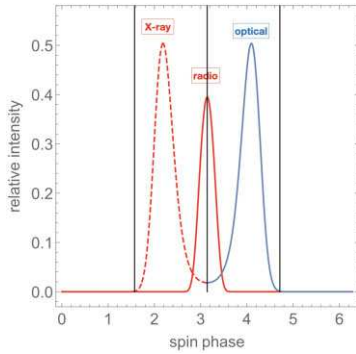


Figure 14. Example of theoretical emission profiles, using an arbitrary normalization. The x-axis shows spin phase in radians. The vertical lines are the spin phases of the maximum of the narrow peak $\pm\pi/2$, to guide the eye. Depending on the parameters of the system, the separation between radio and X-ray/optical peaks may be slightly larger or smaller than $\pi/2$ (0.25) (in this illustrated case, it is smaller).

does indicate that *occasionally* two shifted components can be seen (Fig. 15), consistent with this model.

(ii) Alternatively, the phase-shifted X-ray and optical pulses may come from the plasma stream from the companion interacting with the white dwarf’s magnetosphere, as illustrated Fig. 16. We show theoretical light curves for the following parameters: magnetic obliquity $\alpha = \pi/4$, line of sight with respect to the spin axis $\theta_{ob} = \pi/4$ (near equality of α and θ_{ob} is needed to see the narrow polar emission beam in radio), orbital inclination with respect to the white dwarf’s spin of $\pi/3$, azimuthal angle of the orbital plane of $\pi/2$ (so that the orbital normal is orthogonal to the line of sight). Different colours correspond to different orbital phases.

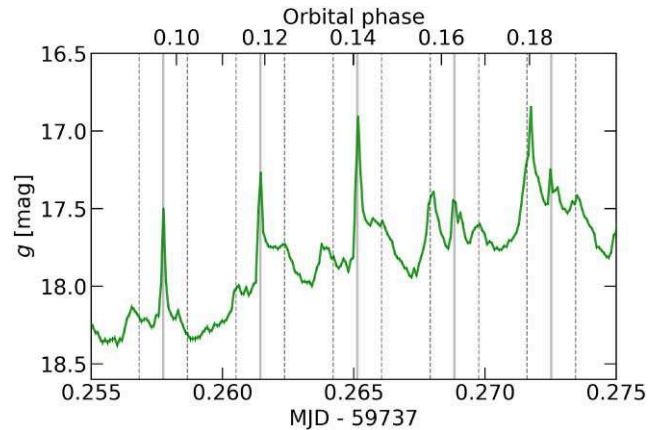


Figure 15. Fraction of ULTRACAM data from Pelisoli et al. (2023) taken on 2022 June 6, showing behaviour consistent with the proposed geometric model. The solid vertical lines mark the central peak that could be explained by auroral emission. The dashed lines are displaced by ± 0.25 in the spin phase and coincide with the location of broader peaks that could be due to Van Allen belt emission.

In conclusion, the geometrical model offers ways to understand the single-peaked, and phase-shifted profiles in X-rays and optical. The model generally explains appearances of both single-peak and double-peak spin profiles. We hypothesise that an important factor is particle diffusion (radial and azimuthal) within the white dwarf’s magnetosphere.

Importantly, the model advocates that emission in J1912 – 4410 originates/is seeded by the interaction with a companion, which is

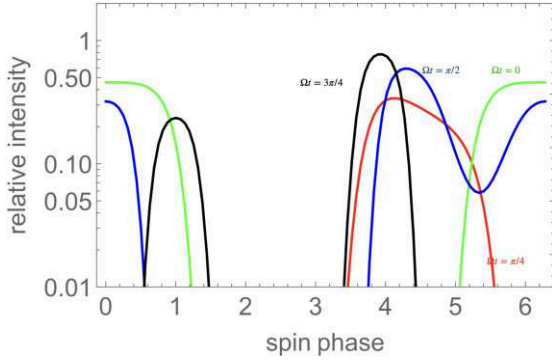


Figure 16. Emission profiles expected from the plasma stream from the companion interacting with the white dwarf’s magnetosphere in the equatorial plane for orbital phases 0 (green), 0.25 ($\pi/4$, red), 0.5 ($\pi/2$, blue), and 0.75 ($3\pi/4$, black).

supported by the fact that such pulsations are not observed in any single white dwarf.

6 DISCUSSION

6.1 The white dwarf in J1912 – 4410

The *HST* spectra confirm that the compact object in J1912 – 4410 is a white dwarf, as previously inferred from its spin period, too slow for a neutron star. The white dwarf temperature obtained from spectral fitting is consistent with the upper limit derived by Pelisoli et al. (2023). The mass, on the other hand, is $\approx 3\sigma$ below the previously reported value of $1.2 \pm 0.2 M_{\odot}$. To obtain this mass estimate, Pelisoli et al. (2023) relied on the assumption that the semi-amplitudes measured from the Na II doublet and from the H β lines traced the centre of mass and the L1 Lagrangian point, respectively, with the M-dwarf filling its Roche lobe. This resulted in a maximum inclination estimate of 37° and on a minimum white dwarf mass of $1.0 M_{\odot}$. Although the Na II doublet indeed likely traces the centre of mass, H β does not necessarily trace L1. In fact, we find that the metal emission lines observed in the FUV suggest a higher minimum inclination of 58° , which increases the white dwarf minimum mass to $\approx 0.57 M_{\odot}$, consistent with our estimate.

Fig. 17 shows our derived dynamical mass constraints compared to the mass estimates for white dwarf and M-dwarf from spectroscopic fitting. There is good agreement between the minimum values set by a Roche-lobe filling M-dwarf orbiting a white dwarf and the mass estimates. Combining Pelisoli et al. (2023)’s estimate of $0.25 \pm 0.05 M_{\odot}$ for the M-dwarf with the system’s binary mass function of $0.1879 \pm 0.0027 M_{\odot}$ and with our estimate for the mass of the white dwarf implies an orbital inclination of $59 \pm 6^{\circ}$, consistent with the dynamical lower limit.

6.2 Implications to theoretical models

Assuming that the white dwarf is in thermal equilibrium, our fit to the white dwarf spectra would suggest that, given the obtained T_{eff} and mass, crystallization has not started in the core of the white dwarf (Bédard et al. 2020). This would place a challenge to the rotation- and crystallization-driven model as a solution for generating a strong magnetic field in the white dwarf, required for explaining the behaviour of binary white dwarf pulsars as a consequence of magnetic torque and reconnection. However, if the white dwarf has previously accreted significantly from the companion, which

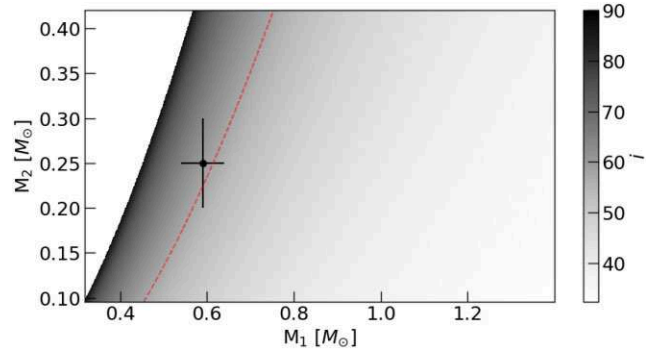


Figure 17. The colour map indicates the system’s orbital inclination required to match the observed K_2 for the values of M_1 and M_2 shown in the x- and y-axis. The red dashed line marks the maximum inclination of 58° inferred from Roche constraints. The black cross shows the mass estimates for white dwarf and M-dwarf from spectroscopic fits, which are completely independent from the Roche analysis. The derived masses are consistent with the Roche constraints.

is probably the case given its spin period, its T_{eff} will be largely affected by compressional heating, reflecting the past accretion rate rather than the core temperature (e.g. Townsley & Bildsten 2004; Townsley & Gänsicke 2009). The thermal time-scale of the white dwarf is $\sim 10^8$ yr, which is longer than the binary pulsar phase (as inferred from AR Sco’s spin down). Therefore, the T_{eff} might not reflect the core temperature of the white dwarf, such that crystallization remains possible.

Although J1912 – 4410’s T_{eff} alone does not rule out the occurrence of a rotation- and crystallization-driven dynamo, it is worth mentioning that there is growing evidence that this model might not be responsible for the late appearance of magnetic fields in white dwarfs. First, for a large fraction of single white dwarfs there does not seem to be a relation between rotation period and field strength (see e.g. fig. 4 in Ginzburg et al. 2022), which is a prediction of the rotation-driven dynamo model. Secondly, even though there is an observed increase in the relative number of magnetic white dwarfs with decreasing temperature, this actually happens before the onset of crystallization (Bagnulo & Landstreet 2021, 2022). Additionally, numerical simulations by Fuentes et al. (2023) have indicated that the energy released by crystallization is not sufficient to power a dynamo. Yet, evidence for the late appearance of strong magnetic fields in white dwarfs is overwhelming, both in single and in close binaries systems (Bagnulo & Landstreet 2021; Parsons et al. 2021; Amorim et al. 2023; Caron et al. 2023). If these fields are not triggered by a dynamo, another mechanism must explain their late appearance. Importantly, the evolutionary sequence suggested by Schreiber et al. (2021) does not depend specifically on the crystallization- and rotation-driven dynamo. It only requires the magnetic field to appear during the cataclysmic variable phase, which could be due to an alternative temperature-dependent mechanism and/or another time-dependent mechanism.

In short, the late appearance of a field remains a possibility for J1912 – 4410. However, the fact that no magnetic field has been directly detected provides a challenge for models predicting or relying on magnetic fields of the order of ~ 100 MG to explain the observed characteristics of pulsing binary white dwarfs (like those by Geng, Zhang & Huang 2016; Katz 2017; Takata, Yang & Cheng 2017). When the lack of detection was restricted to one system, AR Sco, perhaps inclination arguments could be used, as that affects the relative strength of different Zeeman components

(Hönl 1925; Unno 1956). However, with two systems displaying the same behaviour and showing no sign of a magnetic field, relying on this argument becomes more challenging. The intensity of the side components varies with $1 + \cos^2(\psi)$, where ψ is the angle between the magnetic field axis and the line of sight. Therefore, both AR Sco and J1912 – 4410 would need to have unfavourable inclinations for the Zeeman side components not to be visible. Additionally, the shape of the Ly α line is consistent with the non-magnetic models, which is not what one would expect if a magnetic field were affecting the equivalent width.

These results oppose models requiring a strong magnetic field to explain the behaviour of binary white dwarf pulsars. The alternative models, which require a significant mass-transfer rate, did not seem like a good alternative when only AR Sco was known, given that it shows no detected flares, but J1912 – 4410 has shown evidence for flaring behaviour very similar to propeller systems (see Pelisoli et al. 2023), which could point at a significant mass transfer rate for this system. In fact, we present a geometric model assuming that there is mass transfer that can reproduce most of the characteristics of J1912 – 4410's light curve.

7 SUMMARY AND CONCLUSIONS

We have obtained and analysed *HST* COS observations for the recently discovered binary white dwarf pulsar J1912 – 4410. The data were obtained in TIME-TAG mode, which allowed us to construct a light curve for the observations. The light curve shows strong pulses whose period is consistent with the spin period determined from optical observations. The beat frequency between white dwarf spin and the system's orbital period is detected in the FUV, unlike the optical. The FUV pulse shape is dominated by the broad component which is phase-shifted from the narrow component that is interpreted as tracing the spin of the white dwarf, and hence the FUV pulses cannot be used to improve the spin ephemeris and probe for spin period changes.

We used the light curve to identify times of minima and extract an off-pulse spectrum. Correcting this spectrum for a dilution from the pulse using either the pulse spectrum, a power-law, or constant flux, we obtained estimates for the white dwarf spectrum. Resulting white dwarf parameters were similar for all methods and point at a white dwarf with temperature $T_{\text{eff}} = 11485 \pm 90$ K and mass $M_1 = 0.59 \pm 0.05 M_{\odot}$. This suggests that either the white dwarf is not crystallized, or that a previous phase of accretion has led to significant compressional heating such that the white dwarf is not in thermal equilibrium. If the former, this finding would add to growing evidence that crystallization-driven dynamos are not at play in the core of white dwarfs. If the white dwarf is not in thermal equilibrium, which is possible given that we are observing this system during what is very likely a phase with lifetime shorter than the thermal time-scale, it remains possible that the core previously crystallized and that this, combined with the fast rotation, triggered a dynamo. Therefore, it is still possible that the white dwarf was spun up before it became magnetic, as proposed in the evolutionary model of Schreiber et al. (2021).

We find no evidence for a magnetic field of the order of hundreds of MG, which has implications for proposed models for the observed pulsed emission. The lack of such a detectable magnetic field, combined with the possible detection of flares from J1912 – 4410, favour models with a significant mass transfer rate to explain the pulses observed in so-called binary white dwarf pulsars, though the absence of detected flaring from AR Sco remains a puzzle. Continuous monitoring of these systems and searches for other binary

radio-pulsing white dwarfs will provide further clues onto the nature of these challenging systems.

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DATA AVAILABILITY

All data analysed in this work can be made available upon reasonable request to the authors.

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