

# Patternable Process-Induced Strain in 2D Monolayers and Heterobilayers

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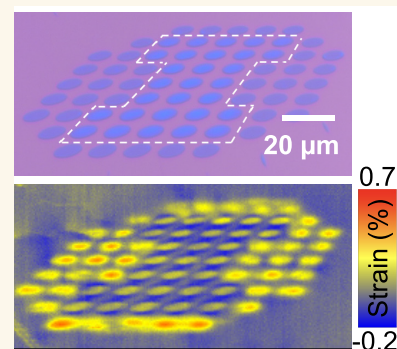
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**ABSTRACT:** Strain engineering in two-dimensional (2D) materials is a powerful but difficult to control approach to tailor material properties. Across applications, there is a need for device-compatible techniques to design strain within 2D materials. This work explores how process-induced strain engineering, commonly used by the semiconductor industry to enhance transistor performance, can be used to pattern complex strain profiles in monolayer MoS<sub>2</sub> and 2D heterostructures. A traction–separation model is identified to predict strain profiles and extract the interfacial traction coefficient of  $1.3 \pm 0.7$  MPa/ $\mu\text{m}$  and the damage initiation threshold of  $16 \pm 5$  nm. This work demonstrates the utility to (1) spatially pattern the optical band gap with a tuning rate of  $91 \pm 1$  meV/% strain and (2) induce interlayer heterostrain in MoS<sub>2</sub>–WSe<sub>2</sub> heterobilayers. These results provide a CMOS-compatible approach to design complex strain patterns in 2D materials with important applications in 2D heterogeneous integration into CMOS technologies, moiré engineering, and confining quantum systems.

**KEYWORDS:** 2D materials, nanomechanics, strain engineering, optical spectroscopy, interfacial mechanics



Strain often plays an unknown but important role in nanoscale materials properties and device behavior. Two-dimensional (2D) van der Waals (vdW) materials like graphene or transition metal dichalcogenides (e.g., MoS<sub>2</sub>, WSe<sub>2</sub>) are ideal ultrastrong materials that host rich strain-induced behavior<sup>1</sup> and where bringing deterministic design to strain will have both technological and scientific impact. For example, while 2D materials are considered contenders to extend transistor scaling or post-Moore's law technology, a current challenge is the heterogeneous integration of 2D materials with complementary metal-oxide-semiconductor (CMOS)-compatible processes and unraveling how these processes impact strain and doping.<sup>2,3</sup> Simultaneously, 2D materials exhibit exciting but difficult to control strain phenomena such as band gap tuning,<sup>4,5</sup> electron mobility enhancement,<sup>6</sup> directing or confining excitons,<sup>7–12</sup> superlattices,<sup>13,14</sup> single-photon emitters,<sup>15–19</sup> phase changes,<sup>20–22</sup> pseudomagnetic fields,<sup>23–26</sup> and magnetism.<sup>27–29</sup> Mechanically, 2D layers can withstand large strains before fracture (>10% for MoS<sub>2</sub><sup>30</sup>), and the vdW bonding allows slip at the interface with the substrate or between layers.<sup>31–33</sup> The fundamental studies above typically introduce strain via external manipulation such as nanoindentation,<sup>34</sup> electrostatic tensioning,<sup>35</sup> transferring onto nanotemplates,<sup>36,37</sup> nanorods,<sup>15</sup> trapped gases in micro/nanoballoons,<sup>9,23,38–40</sup> macroscale bending on soft substrates,<sup>4,6,41</sup> or self-assembly via nanoscale

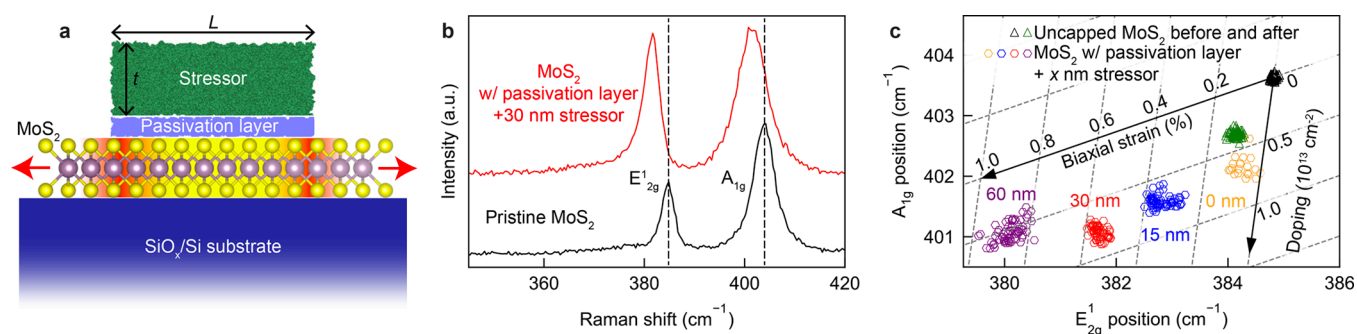
wrinkling.<sup>42–46</sup> To fully leverage the power of strain engineering in 2D materials across all applications, fabrication approaches and models are needed to predict, design, and pattern strain on the nanoscale.

A recent trend has been to apply the decades-old process-induced strain technique used by the semiconductor industry<sup>47–52</sup> to 2D materials. Process-induced strain by depositing high-stress thin films (stressors) is a powerful approach for engineering strain at the nanoscale and is widely used in CMOS processes for mobility enhancement in silicon transistors. These stressors can apply significant thin film forces > 20 N/m onto the underlying substrate. When applied to 2D multilayers, depositing stressors leads to large anisotropic strains<sup>53,54</sup> and interlayer slip.<sup>55</sup> While promising, the previous results are primarily performed on multilayers, where Raman signals are averaged through every layer. Thus, it is difficult to quantify or deconvolve the contributions from strain, doping, and layer number. Nor did the previous works develop models

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**Figure 1.** (a) Schematic cross-sectional view showing a patterned stack consisting of a passivation layer and stressor deposited on monolayer MoS<sub>2</sub> on a SiO<sub>x</sub>/Si substrate. (b) Raman spectra of pristine MoS<sub>2</sub> (black) and after capping by a passivation layer and 30 nm thick stressor (red). (c) Scatter plot of MoS<sub>2</sub> Raman E<sub>2g</sub><sup>1</sup> and A<sub>1g</sub> mode positions, for uncapped MoS<sub>2</sub> before (black triangle) and after (green triangle) the deposition, and MoS<sub>2</sub> capped by the 6 nm Al<sub>2</sub>O<sub>x</sub> passivation layer and MgO<sub>x</sub> stressor of increasing thicknesses of 0 nm (orange), 15 nm (blue), 30 nm (red), and 60 nm (purple).

to understand the spatially heterogeneous in-plane strains. The key step to deterministic strain engineering in 2D materials is to quantify the strain transfer in monolayers, discover the interfacial mechanics governing the behavior, and identify how the strain influences the material structure and properties. Here, we apply process-induced strain by patterning shapes of a magnesium oxide (MgO<sub>x</sub>) thin film on top of monolayer MoS<sub>2</sub>, then quantify the relative contributions to strain and doping using Raman spectroscopy. We observe spatially varying strain profiles and build a traction–separation model to understand the mechanics at the 2D–substrate interface. We find that the monolayers undergo interfacial slip, which minimizes the strain transfer into the substrate and isolates larger strains in the monolayer, in contrast to conventional thin film mechanics, where strain transfer is dominated by out-of-plane shear. These models and strategies can be generalized to predict and design the strain in 2D materials induced during heterogeneous integration with arbitrary thin films. We demonstrate the utility of this approach by patterning the electronic structure of MoS<sub>2</sub> into complex shapes or engineering a heterostrain in the MoS<sub>2</sub>/WSe<sub>2</sub> heterobilayer. These results demonstrate the design and control of strain in 2D monolayers and stacked heterobilayers with process-induced strain. We further show that the process-induced strain is predictable via theoretical and numerical models, which provide additional insights on understanding interface effects in the 2D strain transfer process. Together, these results offer a generalizable strategy to extract, predict, and design strain in emerging 2D systems induced during heterogeneous integration with nearly any process or thin film deposition.

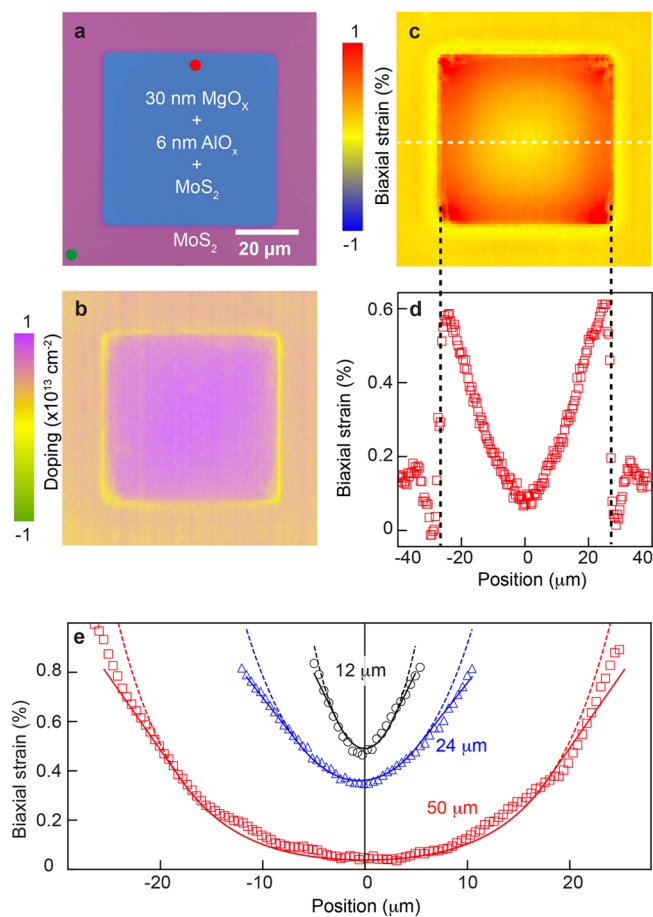
## RESULTS AND DISCUSSION

**Quantifying Process-Induced Strain in 2D Monolayers.** Figure 1 outlines how deposited stressors impact the strain and doping in the 2D materials. Figure 1a is a schematic cross-section of a patterned stressor deposited onto a monolayer of MoS<sub>2</sub> on a SiO<sub>x</sub>/Si substrate. See Methods and Supporting Information Figure S1 for fabrication details. Briefly, we use gold-assisted large-area exfoliation<sup>56</sup> to generate large monolayer MoS<sub>2</sub> with lateral dimensions > 300 μm. We then use shadow masks or e-beam lithography to pattern squares (or other shapes, discussed later) with lateral sizes of 12–50 μm on top of the continuous MoS<sub>2</sub>. We deposit a passivation layer of either Al<sub>2</sub>O<sub>x</sub> or HfO<sub>x</sub> with a thickness of 5–6 nm, then use e-beam evaporation to deposit MgO<sub>x</sub> with

thicknesses of 0–60 nm. See Supporting Information Figure S2 for low-magnification images of the patterned arrays. We chose thin film MgO<sub>x</sub> because it is an established dielectric compressive stressor,<sup>53,54</sup> which is optically transparent and electrically insulating. While not strictly necessary, the passivation layers help both ensure good attachment of the stressor to the 2D surface and decouple the effects of strain and doping but must be accounted for as low stress layers in the mechanical modeling.

Shown in Supporting Information Figure S3 and Table S1, we use wafer-scale thin film stress testing to determine that the evaporated MgO<sub>x</sub> has a built-in thickness-independent compressive stress of  $\sigma_{\text{film}} = -0.95 \pm 0.09$  GPa. After deposition, the relaxation of the compressive stress in the MgO<sub>x</sub> through expansion applies a thickness-dependent thin film force which transfers a tensile stress/strain to the underlying monolayer MoS<sub>2</sub>.

Figure 1b shows the Raman spectra of monolayer MoS<sub>2</sub> with the characteristic E<sub>2g</sub><sup>1</sup> and A<sub>1g</sub> modes before (black) and after 30 nm MgO<sub>x</sub> deposition (red), taken near the edge of a patterned, 50 μm wide square stressor (position indicated as the red dot in Figure 2a). After deposition, there is a redshift of 2.4 cm<sup>−1</sup> of the E<sub>2g</sub><sup>1</sup> mode and 3.2 cm<sup>−1</sup> of the A<sub>1g</sub> mode. Both Raman modes are sensitive to strain and doping, but shift at different rates, and so may be used as a nondestructive method to evaluate the strain and doping.<sup>57</sup> Figure 1c shows the scatter plots correlating the relative E<sub>2g</sub><sup>1</sup> and A<sub>1g</sub> peak positions before deposition (black) and after deposition of a 6 nm thick Al<sub>2</sub>O<sub>x</sub> passivation layer with no stressor (labeled 0 nm, yellow) and with increasing thicknesses of MgO<sub>x</sub> of 15 nm (blue), 30 nm (red), and 60 nm (purple), all acquired from the same region near the edge of stressors. We also include an uncapped region far away (see the green dot in Figure 2a) from the patterned stressors after deposition (green). We correlate these relative shifts to previous studies to deduce the changes in strain and doping,<sup>39,58</sup> shown as tilted axes in Figure 1c (derivation in Supporting Information S1). The data show that the initial deposition of the Al<sub>2</sub>O<sub>x</sub> passivation layer induces a change in n-doping of  $(0.61 \pm 0.07) \times 10^{13}$  cm<sup>−2</sup>, but a minimal change in strain of  $0.06 \pm 0.03\%$ . Moreover, the uncapped region shows a similar change in the doping and strain after deposition. We attribute the initial change in doping during the high-temperature e-beam deposition to both the thermal effects (far away)<sup>59</sup> and the creation of defects at the 2D/oxide interface.<sup>60</sup> Next, the addition of MgO<sub>x</sub> on top of the



**Figure 2.** Spatially varying strain under patterned stressors. (a) Optical image of a 50  $\mu\text{m}$  wide patterned square of a 30 nm thick  $\text{MgO}_x$  stressor on monolayer  $\text{MoS}_2$  on a  $\text{SiO}_x/\text{Si}$  substrate. The red dot denotes the location where the data in Figure 1b,c are taken, and the green dot corresponds to the uncapped  $\text{MoS}_2$  data in Figure 1c (green cluster). (b, c) Maps of extracted doping and biaxial strain in  $\text{MoS}_2$  extracted from hyperspectral Raman mapping. (d) Biaxial strain of  $\text{MoS}_2$  versus position corresponding with the white dashed line in (c). (e) The biaxial strain profile versus position along the center axis for square 30 nm thick stressors with widths of 12  $\mu\text{m}$  (black), 24  $\mu\text{m}$  (blue), and 50  $\mu\text{m}$  (red). The shapes are the experimental data, the solid lines are fitted piecewise functions using the analytical model, and the dashed lines are fitted hyperbolic functions.

passivation layer induces tensile biaxial strain and only minimal additional changes in n-doping. Effectively, the use of the passivation layer is decoupling the impact of strain and doping during the deposition process. Moreover, changing the thickness of the stressor increases the tensile biaxial strain nearly linearly. We estimate an effective tensile biaxial strain of  $0.58 \pm 0.02\%$  and doping density of  $(7.0 \pm 0.6) \times 10^{12} \text{ cm}^{-2}$  near the edge of a 50  $\mu\text{m}$  wide square with a 6 nm thick  $\text{Al}_2\text{O}_x$  and 30 nm thick  $\text{MgO}_x$  stressor. The increase in strain with an increase in stressor thickness is consistent with a linearly increasing thin film force. For simplicity, hereafter we will always refer to the effective biaxial strain simply as strain. As discussed in Supporting Information Section 2, this is a good approximation except right at the edges of stressors.

**Interfacial Mechanics Determine Spatial Strain Profiles.** Figure 2 investigates the spatial distribution of strain in  $\text{MoS}_2$  both inside and outside a patterned stressor. Figure 2a

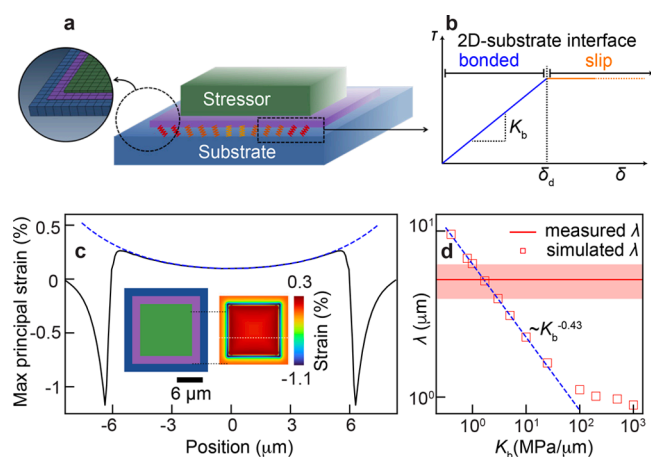
shows an optical image of a shadow-mask-patterned square stressor 50  $\mu\text{m} \times 50 \mu\text{m}$  and 30 nm thick on continuous monolayer  $\text{MoS}_2$ . Figures 2b and 2c show the corresponding doping and strain in monolayer  $\text{MoS}_2$ . We extracted this local strain and doping using Raman hyperspectral imaging to form a two-dimensional map of Raman peak shifts and then performed the transformation shown in Figure 1c. Supporting Information Figures S4–S6 provide additional maps of peak parameters and extracted strain and doping, before and after deposition and as a function of laser polarization. The doping under the stressor seen in Figure 2b shows a spatially uniform shift of  $(4 \pm 0.7) \times 10^{12} \text{ cm}^{-2}$ , compared with that of the surrounding region. In comparison, the strain under the stressor shows a complex profile following the shape of the stressor.

Figure 2d highlights these variations by plotting the strain line profile along the center of the square stressor (white dashed line in Figure 2c). The black dashed line marks the edge of the stressor. The strain reaches a minimum at the center of the stressor and increases when approaching the edges. At the edge, the strain undergoes an inversion with a small region of compressive strain that propagates outside the stressor. As a comparison, patterned stressors deposited on silicon also show complex size-dependent strain profiles and have been modeled as the local transfer of strain into the underlying substrate through combinations of 3D in-plane and out-of-plane shear and the boundary conditions set by the edges of the stressor.<sup>50,51,61,62</sup> As we will investigate, the vdW interface in the monolayer  $\text{MoS}_2$ –substrate leads to important differences in the resulting strain profile.

We further investigate the mechanics of the complex strain profile by measuring square stressors of size ranging from 12 to 50  $\mu\text{m}$ . We made different sizes of stressors in the same sample by electron beam lithography (details in Methods). Figure 2e plots the resulting extracted strain versus position on the same scale through the center line of each square with zero position corresponding to the middle of each stressor. The points are experimentally measured strains. The data right at and outside the edges are intentionally cut off to focus on the changes inside the stressors. Supporting Information Figure S7 shows the corresponding strain map of the entire stressor array as well as a plot of the middle and edge stress versus size. Discussed further in the models below, there is a nontrivial evolution in the strain profile as a function of stressor size from pure hyperbolic behavior (dashed lines) to a piecewise solution with a hyperbolic profile near the center and linear profile near the edges (solid lines).

Shown schematically in Figure 3a,b, we propose a traction–separation model<sup>63–65</sup> to describe the interfacial mechanics of out-of-plane transfer of in-plane strain across the 2D–substrate interface and resulting in-plane strain profile within the monolayer. Figure 3a depicts a schematic of the square stressor model, where the stressor is smaller than the underlying 2D layer. As shown in Figure 3b, the interface moves from the mechanically bonded to the slip regime with increasing displacement  $\delta$ . To relate this model to the measurements, the strain in the 2D layer is the derivative of the displacement  $\varepsilon(x) = \frac{d\delta(x)}{dx}$ . In the mechanically bonded regime, the in-plane displacement across the 2D–substrate interface  $\delta$  and interfacial traction  $\tau$  are linearly proportional, defined as  $\tau = K_b\delta$ , where  $K_b$  is the interfacial traction coefficient. Above the critical damage initiation threshold





**Figure 3.** (a) Schematic representing the model for a 2D monolayer sandwiched between a stressor and a substrate, with a traction–separation model defining the behavior at the 2D–substrate interface. Circled graphic shows the finite element model mesh, with size and geometry not to scale. (b) Conceptual plot of defining the constituent relation between interfacial traction stress  $\tau$  and interfacial displacement  $\delta$ , showing the transition between bonded and slip regimes. (c) Simulated strain profile of MoS<sub>2</sub> across the centerline of a 12  $\mu\text{m}$  wide stressor. Dashed blue lines show hyperbolic fitting to the FEA strain profile inside the stressor. (d) Fitted strain decay length for simulations of different  $K_b$  compared with experimentally measured strain decay lengths, with  $K_t = 10^4 \text{ MPa}/\mu\text{m}$ ,  $\delta_d = 20 \text{ nm}$ . Dashed blue line is a power law fit showing a relation of  $K_b^{-0.43}$  for  $K_b \ll K_t$ .

displacement  $\delta_d$ , the interface debonds and enters the slip regime, where the layers will slide past each other, leading to a constant  $\tau = \tau_d$  with increasing  $\delta$ . Similar models have been shown to describe strain transfer in systems such as 2D flakes on strained or bent soft substrates,<sup>66–68</sup> on strained metal foils,<sup>69</sup> and near the edges of inflated microballoons<sup>70</sup> or artificially stacked 2D heterostructures.<sup>71</sup>

We adapt the traction–separation model to describe the out-of-plane transfer of in-plane strain into monolayer MoS<sub>2</sub> sandwiched between a stressor and the underlying substrate. We assume that across the top interface the monolayer is well bonded to the stressor, which is supported by experimental studies from e-beam evaporation<sup>60</sup> or atomic layer deposition.<sup>60,72,73</sup> In contrast, the bottom interface between the monolayer and the substrate is formed by transfer of the 2D material and thus will be governed by vdW interactions and the traction–separation relation. In the model, we use the stressor thickness,  $t_{\text{film}}$ , and thin film stress,  $\sigma_{\text{film}}$ , based on experimental measurements provided above. Other material parameters can be found in [Supporting Information Table S2](#). We note that the Young’s modulus of the passivation layers is similar to the modulus of the stressor, but has low built-in stress and smaller thickness. As a result, we have found that the system is well approximated mechanically by treating the thin film stack as a single material with a lower effective stress. Before tackling the more complex 2D geometry, we describe a one-dimensional analytical model of a stressor with finite-width  $L$  but infinite length to understand the underlying behavior. The model defines a differential equation relating the local strain in the 2D monolayer  $\varepsilon(x)$  as a function of position  $x$  to the material properties and geometry. [Supporting Information Section S1.2](#) provides the full derivation. The resulting equation is a piecewise function of the strain depending on whether the

interface is bonded ( $\delta \leq \delta_d$ ) or slipping ( $\delta > \delta_d$ ). Denoting the center of the stressor as the zero position, the model predicts that

$$\frac{d^2\delta}{dx^2} = \frac{d\varepsilon}{dx} = \begin{cases} -\frac{\delta_d}{\lambda^2} & \text{if } x \leq -x_d \\ \frac{\delta_d \sinh(x/\lambda)}{\lambda^2 \sinh(x_d/\lambda)} & \text{if } -x_d \leq x \leq x_d \\ \frac{\delta_d}{\lambda^2} & \text{if } x \geq x_d \end{cases} \quad (1)$$

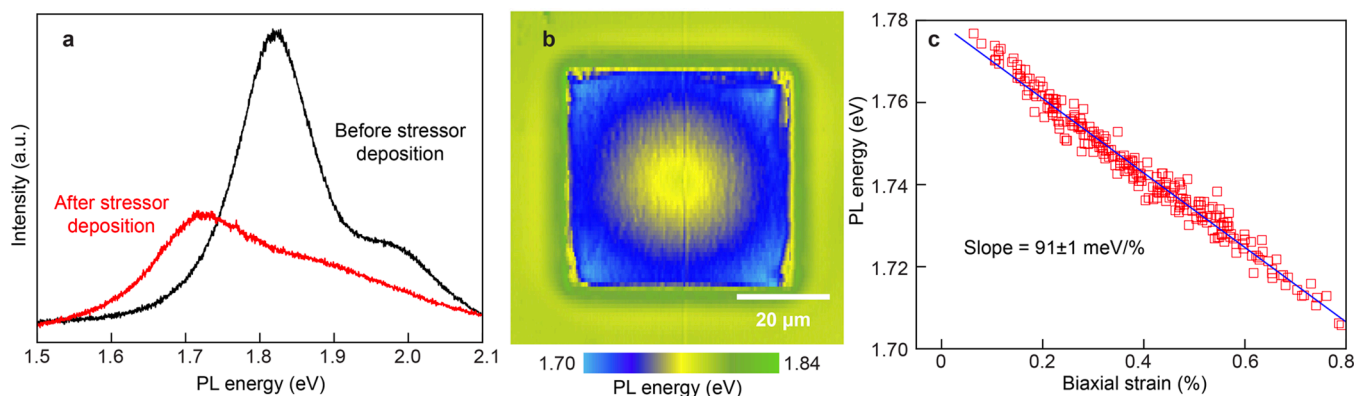
Here,  $\pm x_d$  marks the left and right position where slip begins ( $\delta(\pm x_d) = \pm \delta_d$ ). In the bonded regime, the model predicts strain decay with a characteristic strain decay length  $\lambda$  associated with  $K_b$ , defined as

$$\lambda = \sqrt{E_{\text{film}} t_{\text{film}} / K_b} \quad (2)$$

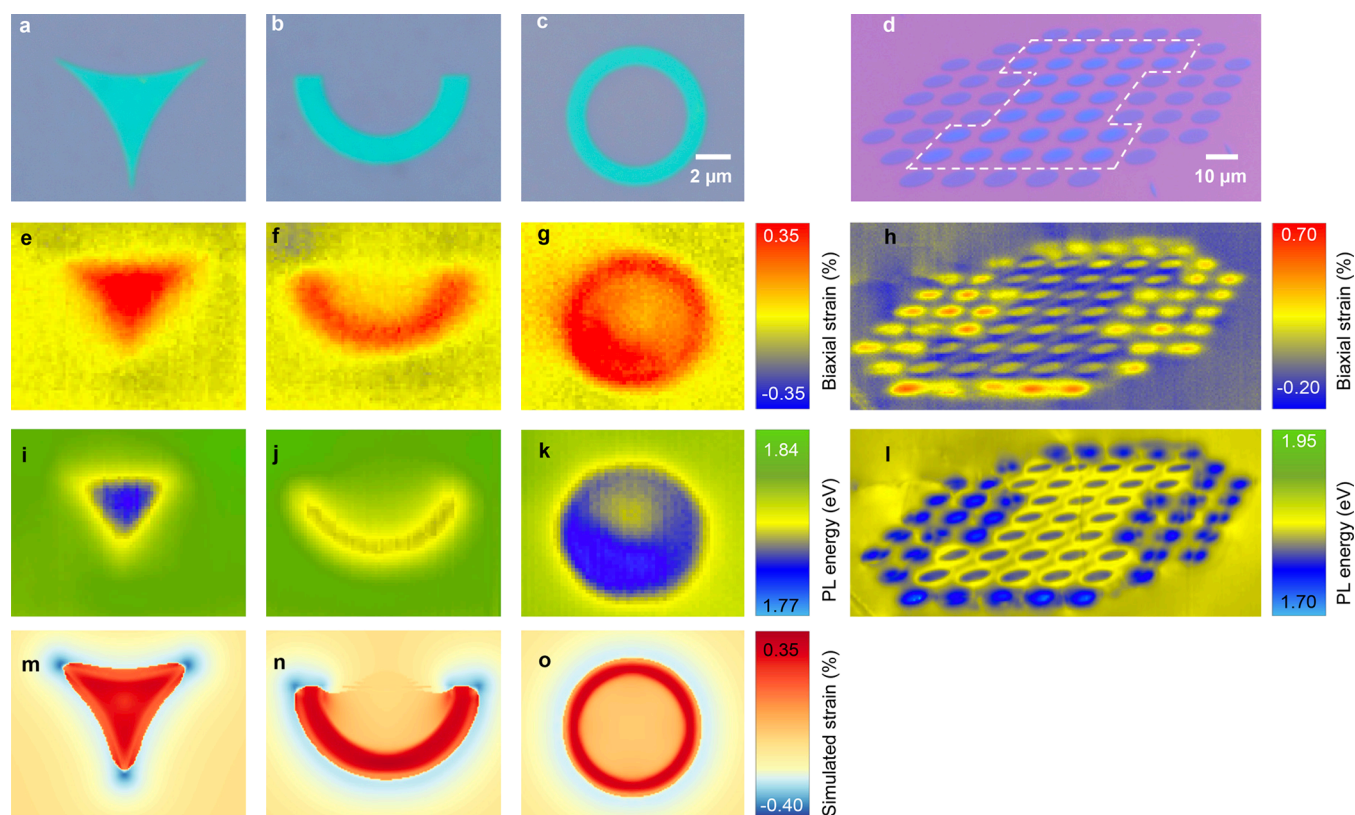
In the slip regime, above the damage initiation threshold  $\delta_d$ , the model predicts a linear strain profile. Taken together, the full solution is a piecewise function with a hyperbolic strain profile in the middle of the stressor and possible linear strain profile at the edges, though the linear strain profile onset depends on the magnitude of the applied strain and the size of the stressor. We note that the model also predicts the regions of compressive strain outside of the edges of the stressors. See [Supporting Information Section S1.2](#) for more discussion.

The analytical model explains the transition between the hyperbolic and linear regimes observed in the strain profiles of [Figure 2e](#), produces a good fit to the data, and provides a framework to understand how the strain profile will change with thickness, film modulus, and interfacial traction. We use the fits to extract the average measurable parameters for the strain profiles across all sizes: strain decay length  $\lambda = 5.5 \pm 1.2 \mu\text{m}$ , linear slope  $0.06 \pm 0.01\%$  strain/ $\mu\text{m}$ , and damage initiation threshold  $\delta_d = 16 \pm 5 \text{ nm}$ . Shown in [Supporting Information Figure S7](#), the primary sources of error arise from long length scale heterogeneity in the sample. Similar variability is observed in other studies of traction on 2D materials.<sup>74,75</sup> We attribute it to variations in initial strain and local traction arising from the transfer process, surface roughness, and cleanliness of the interface across different regions of the transferred material.

Next, we use finite element analysis (FEA) to fully capture the strain distribution of MoS<sub>2</sub> for stressors with complex geometries, quantitatively relate the experimentally measured strain profile to interfacial parameters, and extract the properties of each interface. The FEA mesh is shown in the inset of [Figure 3a](#). [Figure 3c](#) plots the simulated maximum principal strain profile extracted from the centerline of a 14  $\mu\text{m}$  wide MoS<sub>2</sub> monolayer capped by a 12  $\mu\text{m}$  wide and 30 nm thick square stressor. We assume thin film stress  $\sigma_{\text{film}} = -1.0 \text{ GPa}$ ,  $K_b = 1.3 \text{ MPa}/\mu\text{m}$ , top interface traction coefficient  $K_t = 10^4 \text{ MPa}/\mu\text{m}$ , and  $\delta_d = 20 \text{ nm}$ . [Supporting Information Table S1](#) provides the remaining material parameters. We note that this model can be adapted to parametrically study the role of any parameter in the system, but we choose the values that most closely match our experimental data. The insets compare the top-down view of the simulation geometry and the corresponding strain distribution map. [Supporting Information Section S1.3](#) and [Figure S8](#) explore anisotropic strain in the simulation. The simulated strain profiles show hyperbolic



**Figure 4.** (a) Photoluminescence (PL) spectra of pristine MoS<sub>2</sub> (black) and MoS<sub>2</sub> capped by 30 nm of MgO<sub>x</sub> (red), from the same sample and region shown in Figures 1 and 2. (b) Map of PL emission energy in monolayer MoS<sub>2</sub> capped with a square MgO<sub>x</sub> stressor. (c) Scatter plot of PL transition energy vs strain in MgO<sub>x</sub>-capped MoS<sub>2</sub>. Blue line is a linear fit.



**Figure 5.** Designing strain profiles in 2D monolayer MoS<sub>2</sub>. (a–d) Optical images of patterned stressors: (a) triangle, (b) half arc, (c) full ring, and (d) Illinois Material Science and Engineering Center (I-MRSEC) logo. (e–h) Corresponding maps of strain extracted from Raman spectroscopy. (i–l) Corresponding maps of the PL emission energy. (m–o) Corresponding simulated max principle strain profiles for the first 3 shapes from FEA.

behavior in the 2D material capped by the stressor, shown as a blue dashed line. This is in agreement with the measurements of the smallest stressor and consistent with the analytical model, although the exact magnitudes and onset of slip are sensitive to the chosen parameters. One difference is that the FEA model displays regions with larger compressive strain at the edges compared with spectroscopy measurements. We hypothesize that this difference could be explained by a combination of averaging effects arising from the diffraction-limited spatial resolution of the optical hyperspectral mapping of 0.7 μm or a different traction coefficient in the regions under versus outside the stressor.

FEA allows us to perform parametric analysis to explore the role of the key parameters affecting the strain profile, including geometric parameters (e.g., stressor thickness, size, shape, number of layers), material properties (e.g., Young's modulus, initial stress), and interfacial parameters ( $K_b$ ,  $\delta_b$ ,  $K_t$ ). In Figure 3d, the simulated hyperbolic strain decay length  $\lambda$  is plotted as a function of  $K_b$ , the interfacial traction coefficient of the bottom MoS<sub>2</sub>–SiO<sub>x</sub> interface on a log–log scale. There is a power law scaling between the parameters with a value of  $K_b^{-0.43}$ , which is in reasonable agreement with eq 2, which predicts a power law of  $K_b^{-0.5}$ . The pink line and band show the average and root-mean-square variations in the experimentally

measured hyperbolic strain decay rates of  $5.5 \pm 1.2$  MPa/ $\mu\text{m}$ , as extracted from Figure 2e. The crossover in the simulated and measured decay lengths corresponds to a  $K_b$  of  $1.3 \pm 0.7$  MPa/ $\mu\text{m}$ . To compare, this value agrees with previous study on the graphene– $\text{SiO}_x$  interface with an equivalent  $K_b$  of 0.82 MPa/ $\mu\text{m}$ <sup>45,70</sup> and 1 order of magnitude smaller than the graphene–polymer interface of 74 MPa/ $\mu\text{m}$ .<sup>66</sup> In Supporting Information Figure S9, we show an additional parametric analysis of the effect of different interfacial parameters on strain profiles. Together, the numerical and analytical models allow design and prediction of strain in 2D materials capped by a stressor in complex systems where experimental quantification is unachievable such as within device architectures and for structures below the optical diffraction limit.

**Designing and Patterning Optical Properties with Strain.** In the rest of the paper, we apply the developed techniques and models to explore applications at the forefront of 2D materials research, such as how to spatially pattern the electronic band structure and engineer layer-by-layer heterostrain in 2D heterostructures.

Figure 4 explores how spatially varying strain modulates the local optical band gap in monolayer  $\text{MoS}_2$  by performing a hyperspectral photoluminescence (PL) spectroscopy mapping. Figure 4a plots the PL intensity versus energy of  $\text{MoS}_2$  before and after deposition near the edge of a stressor. After deposition, the PL emission energy shifts toward lower energy from 1.81 to 1.71 eV, and the peak emission intensity is reduced. Figure 4b is a map of the extracted PL emission energy on the same sample from Figure 2, allowing direct comparison. Inside the stressor, the spatial distribution of the emission energy closely follows that of the strain pattern, which allows us to cross-correlate the PL and strain maps. Figure 4c plots the resulting PL emission energy versus strain. We avoid the complexity from edge effects by cropping the data  $\sim 1 \mu\text{m}$  away from the edge to show the correlation only from inside the stressor. The PL emission energy tunes linearly with strain at a rate of  $91 \pm 1$  meV/% strain.

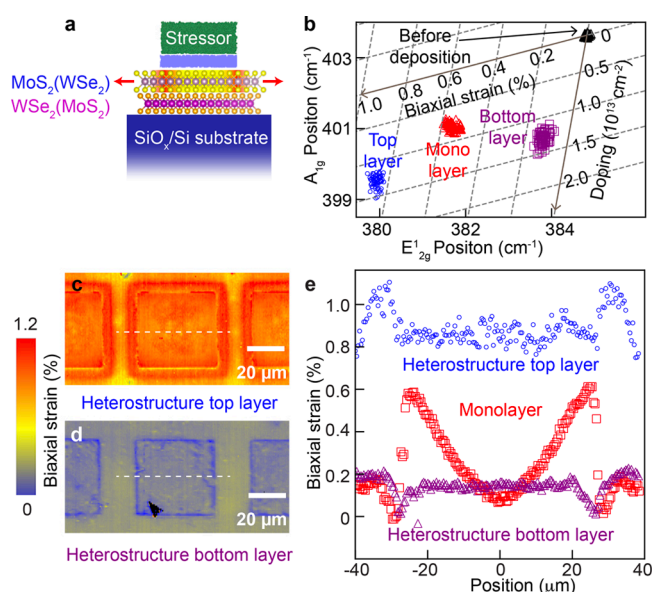
In comparison, previous studies have shown that the PL transition energy is tunable via diverse techniques including applying uniaxial strain by bending 2D materials on a substrate<sup>4,76</sup> and biaxial strain by thermal expansion on a substrate<sup>77</sup> or via inflation of microballoons.<sup>39</sup> These studies, along with simulations,<sup>78</sup> find that strain tuning rates range from 44 to 72 meV/% for uniaxial strain and 99–112 meV/% for biaxial strains. Our measured values are similar to the range set by biaxial strains.

In Figure 5, we demonstrate designable strain profiles and optical properties by using lithography to pattern different shapes of stressors on monolayer  $\text{MoS}_2$ . The first row of Figures 5a–d shows the optical images of stressors patterned into a (a) triangle, (b) half arc, (c) full ring, and (d) Illinois Material Science and Engineering (I-MRSEC) logo. The second row, Figures 5e–h, maps the corresponding strain extracted from the Raman shifts. The third row, Figures 5i–l, maps the corresponding PL emission energy. The fourth row, Figures 5m–o, shows the simulated FEA principle strain maps. In each shape, the patterns defined in the stressors by lithography are transferred into the underlying  $\text{MoS}_2$ , which allows spatial definition of the local strain and optical band gap in the material, with an overall trend consistent with the simulation.

There are two interesting highlights in the strain maps. First, in the center of the ring in Figure 5c, both simulation and

experiment show that the strain in the center region enclosed but uncovered by the stressor shows a residual tensile strain of 0.15%, showing that strain can be designed through the remote deposition and not just by depositing directly on top of the material. Second, in the MRSEC logo shown in 5d, we used two different depositions with different thicknesses to make the “I” (15 nm) stand out versus the surrounding (30 nm) and thus created two distinct strain levels in the same sample. This demonstrates that it is possible to spatially tailor the magnitude and not just shape of the strain profiles through repeated depositions. The ability to design the strain profile has diverse applications. For example, the asymmetric strain profiles made by patterning the triangles in Figure 5a have applications in directed exciton funneling. Taken together, these results demonstrate the versatility offered by patterning the process-induced strains for designing strain in 2D materials.

**Interlayer Heterostrain in 2D Heterostructures.** In Figure 6, we explore the application of stressors for



**Figure 6.** (a) Schematic of the cross-sectional view of a deposited square  $\text{MgO}_x$  stressor on a twisted  $\text{MoS}_2$ – $\text{WSe}_2$  (or,  $\text{WSe}_2$ – $\text{MoS}_2$ ) heterostructure. (b) Scatter plot of  $\text{MoS}_2$  Raman  $E_{2g}^1$  and  $A_{1g}$  peak positions near the edge of a square  $50 \mu\text{m}$   $\text{MgO}_x$  stressor for  $\text{MoS}_2$  monolayer (red) and for the heterostructure with  $\text{MoS}_2$  on the top layer (blue) or bottom layer (purple). (c, d) Strain map of the heterostructure with  $\text{MoS}_2$  as the (c) top and (d) bottom layer. (e) Corresponding cross-sectional strain profiles across the center line of  $50 \mu\text{m}$  square stressors for a  $\text{MoS}_2$  monolayer (red, from Figure 2d) and for the heterostructure with  $\text{MoS}_2$  on the top layer (blue) or bottom layer (purple).

heterostrain engineering in 2D heterostructures and the out-of-plane strain transfer across a 2D–2D interface. Figure 6a shows a schematic of a  $\text{MoS}_2$ – $\text{WSe}_2$  heterostructure on  $\text{SiO}_x/\text{Si}$  with patterned 30 nm thick  $\text{MgO}_x$  stressors deposited on top. We quantified the heterostrain between the constituent layers by fabricating two heterostructures with opposite stacking configurations: heterostructure-1 (HS-1) with  $\text{MoS}_2$  top and  $\text{WSe}_2$  bottom layer, and heterostructure-2 (HS-2) with  $\text{WSe}_2$  top and  $\text{MoS}_2$  bottom layer. The interlayer twist angles in the heterostructures are in a range of  $17$ – $27^\circ$ , as established by optical images taken during transfer. As shown in Supporting Information Figure S10, the Raman transitions of



the MoS<sub>2</sub> and WSe<sub>2</sub> are distinct, so we independently probe the peak shifts in each layer through a single spectroscopy measurement. We note that this ability to separate strain from each layer is important. In comparison, previous studies of process-induced strain were on multilayer MoS<sub>2</sub><sup>53</sup> where the signals from each layer are overlapping, making it impossible to discern strain layer-by-layer. We also note that unlike in MoS<sub>2</sub>, the Raman transitions in WSe<sub>2</sub> overlap, making deconvolution of strain and doping effects more difficult.<sup>79,80</sup> Thus, we compare the Raman transitions in MoS<sub>2</sub> in the two different configurations to probe separately the strain in the top and bottom layers.

Figure 6b is a scatter plot comparing the Raman peak positions of the MoS<sub>2</sub> in four cases: monolayer before stressor deposition (black), monolayer after stressor deposition (red), heterostructure top layer (HS-1) after stressor deposition (blue), and heterostructure bottom layer (HS-2) after stressor deposition (purple), all taken from the same region near the edge of an identically sized 50  $\mu\text{m}$  square stressor. The tilted axes quantify the biaxial strain and doping effects in MoS<sub>2</sub> from the relative peak positions. The doping induced is similar for all cases after deposition. Projecting along the strain axis, there are distinct strain magnitude differences in monolayer ( $0.58 \pm 0.02\%$ ), bottom layer ( $0.11 \pm 0.02\%$ ), and top layer ( $0.86 \pm 0.04\%$ ) MoS<sub>2</sub>.

Figure 6c and Figure 6d show the corresponding strain maps for the top MoS<sub>2</sub> layer in HS-1 and bottom MoS<sub>2</sub> layer in HS-2, respectively, while Figure 6e plots the strain through the center line of the maps, comparing the relative strain profile of the heterostructure top layer (blue), bottom layer (purple), and monolayer (red), from Figure 2. The maps show that the strain profile in the heterostructure under the stressor is more homogeneous compared with the monolayer. Additionally, for the top layer, there is a sharp rise in strain at the edge of the stressor, and the heightened strain extends significantly beyond the edge, to the point that patterned stressors separated by more than 25  $\mu\text{m}$  have interacting strain profiles. The large heterostrain across the layers and the negligible strain in the bottom layer are consistent with the structural lubricity that arises in incommensurate twisted 2D vdW interfaces, which display friction orders of magnitude lower than conventional interfaces.<sup>81</sup>

Thus, we attribute the much higher strain in the top layer as resulting from the stressor applying the in-plane stress from the top down and a much lower onset of slip at the MoS<sub>2</sub>/WSe<sub>2</sub> vdW interface compared with the underlying 2D–oxide interface. The homogeneity in the strain profile corroborates the FEA analysis from Figure 3d, which suggests that the low traction in the vdW interface will lead to a very long strain decay length compared with the size of the fabricated stressors. We note that the magnitude of the interlayer friction is well-known to depend on interlayer alignment,<sup>81</sup> so we hypothesize that aligned to low twist homo/heterostructures will show very different behavior. Finally, this same slow decay length will allow interaction between separated stressors, which partially explains the slow strain variations observed from underneath the stressors. That said, the fact that the strain rises between stressors rather than falls is surprising and does not follow from the models. Understanding the origin of these rises will require further modeling as well as analysis to deconvolve other effects not present in the monolayers like interlayer interactions which tune the Raman modes and interlayer nanoscale bubbles<sup>9</sup> and

folds<sup>82</sup> resulting from transfer that lead to residual strain or slack.

These results demonstrate that process-induced strain engineering brings powerful capabilities to engineering moiré superlattices in 2D heterostructures. As a point of reference, there is a 0.2% mismatch in the lattice constant of MoS<sub>2</sub> ( $d = 0.322$  nm) and WSe<sub>2</sub> ( $d = 0.329$  nm). In comparison, the results above demonstrate that heterostrain engineering will modify the relative lattice constant by more than 0.8%. As a result, heterostrain engineering should strongly modify the wavelength of moiré superlattices at low twist angles in ways not accessible via twist alone, such as allowing lattice matching of mismatched heterostructures, bringing patternable and designable superlattices within a single structure and producing anisotropic superlattices from anisotropic heterostrain.

## CONCLUSION

This work unites experiment and modeling to quantify strain transfer into 2D monolayers from integration with patterned thin film stressors and develop an understanding of the interfacial mechanics needed to predict and design the strain profiles. These capabilities provide a CMOS-compatible and scalable approach for patterning strain, with a drastic increase in the designability and control compared with current approaches, which we demonstrate with proof of concept applications to spatially pattern electronic structures of 2D semiconductors and pattern layer-by-layer heterostrain in 2D heterostructures. Moreover, while we focused on the combination of MoS<sub>2</sub> and MgO, our models and conclusions generalize to understanding and predicting strain in other vdW-bonded materials integrated with arbitrary thin films and other process technologies. Thus, this work serves as a foundation that is directly relevant to the design of highly strained nanosystems. A few specific examples to demonstrate the utility of this approach are as follows: (1) Exploring the size limits of patterned stressors and shape-induced gradients on 2D monolayers will enable methods for exciton confinement and funneling that cannot be achieved with the nanotemplating approaches currently used.<sup>10,12</sup> (2) Exploring how to design uniform strain profiles will have direct application to integration with nanoelectronics, such as the heterogeneous integration and strain-induced performance enhancement of 2D materials into semiconductor electronics.<sup>6</sup> (3) Exploring strain transfer in different combinations of 2D heterostructures or twisted bilayers will enable control over different dimensions of design for moiré engineering and strain-based superlattices.<sup>55</sup>

## METHODS

**Sample Fabrication.** Supporting Information Figure S1 provides a graphical view of the fabrication flow which corresponds to steps i–iv below. (i) We start with synthetic MoS<sub>2</sub> and WSe<sub>2</sub> crystals (2D Semiconductors Inc.). To obtain monolayers, we use established recipes for gold-assisted layer-by-layer exfoliation of 2D materials.<sup>56</sup> We obtained the pristine, atomically clean gold surface by depositing 100 nm thick gold film onto polished silicon wafers (Nova Wafers Inc.) using electron-beam evaporation (Temescal Ebeam evaporator). (ii) We pattern a mask on top of the exfoliated 2D layers using either e-beam or shadow mask lithography. (iii) We deposit a thin layer of either 6 nm Al<sub>2</sub>O<sub>3</sub> with e-beam evaporation (sourced from Kurt J. Lesker Company, part number EVMALO1-3MMT) or 5 nm HfO<sub>2</sub> with atomic layer deposition (ALD) (Cambridge NanoTech Savannah S100, 50 cycles) to promote the adhesion of the stressor to the 2D material and act as a passivation layer for decoupling strain

and doping from deposition. We then use electron-beam evaporation to deposit  $\text{MgO}_x$  (Kurt J. Lesker Company, part number EVMMGO3-6MMT) of thicknesses ranging from 15 to 60 nm. During the deposition, we maintained a deposition rate of 0.5 Å per second. (iv) We removed the mask. In the case of electron-beam lithography, we lift off the mask with an acetone/IPA rinse. In the case of the shadow mask, we peel off the mask and obtain the sample. Samples discussed in Figure 1, Figure 2a to d, Figure 4, and Figure 6 are patterned by using a metal TEM grid (Ted Pella Inc.) as shadow mask and have 6 nm evaporated  $\text{Al}_2\text{O}_x$  as a passivation layer. Samples in Figure 2e and Figure 5 are patterned by 100 kV electron beam lithography (Raith EBP G 5150) with poly(methyl methacrylate) (PMMA) masks and have 5 nm ALD-grown  $\text{HfO}_x$  as a passivation layer.

**Measuring the Thin Film Stress.** We extracted the thin film stress using a variable-temperature film stress measurement system, FSM 500TC, which acts as a laser profilometer. We measure the curvature of a 4 in. 285 nm/550  $\mu\text{m}$   $\text{SiO}_x/\text{Si}$  wafer (Nova wafers) before and after depositing uniform, unpatterned films of  $\text{MgO}_x$  with thicknesses ranging from 20 to 80 nm. We then use Stoney's formula<sup>83</sup> to measure the film stress. Supporting Information Table S1 summarizes the results, and Supporting Information Figure S3 shows example curvature data. The built-in thin film stress for evaporated  $\text{MgO}_x$  is  $-0.95 \pm 0.09$  GPa.

**Raman and PL Spectroscopy.** For single-point Raman and PL spectroscopy measurements, we use a Renishaw confocal Raman microscope with a 532 nm laser, 2400 lines per mm gratings, and a filter of 0.1%. The power is kept below 100  $\mu\text{W}$ , the integration time is kept below 10 s, and the laser spot size is estimated to be 1  $\mu\text{m}$ . We perform the hyper-spectral Raman and PL spectroscopy with a Nanophoton 11 confocal Raman system with a 520 nm laser source under 100 $\times$  magnification, where the spatial resolution is 0.7  $\mu\text{m}$ , the scan power is kept below 0.7 mW per line, and the scan step size is 0.2  $\mu\text{m}$ .

**Finite Element Analysis Model.** We used the commercial FEA package ABAQUS Standard solver. Material properties are summarized in Supporting Information Table S2. Unless otherwise explicitly stated, all simulations are for a 12  $\mu\text{m}$  wide square stressor of thickness 30 nm. In this model, the mesh size is largely determined by the thinnest material thickness, which is 0.001  $\mu\text{m}$  for  $\text{MoS}_2$ . Elements with high aspect ratios are undesirable because of the low accuracy of the solution due to the nodes of the element being far apart from each other. We used hexahedral 3D elements with a mesh size of 0.08  $\mu\text{m}$ . The built-in stress of  $\text{MgO}_x$  is defined as a predefined stress field of  $-1.0$  GPa. The bottom nodes of the  $\text{SiO}_x$  are constrained against all degrees of freedom, i.e., displacement and rotation. The interfacial properties are modeled as surface-to-surface interaction between the  $\text{MgO}_x$ -bottom/ $\text{MoS}_2$ -top and  $\text{MoS}_2$ -bottom/ $\text{SiO}_x$ -top surfaces using cohesive behavior with specified damage evolution properties. Here, the interfacial traction coefficients,  $K_t$  and  $K_b$ , and damage initiation threshold,  $\delta_d$ , are defined. The simulations in the text use a  $K_t$  of  $10^4$  or  $10^5$  MPa/ $\mu\text{m}$  and  $K_b$  values ranging from 0.8 to 1000 MPa/ $\mu\text{m}$ , while ensuring that  $K_t \gg K_b$ .  $\delta_d$  values in simulation range from 2 to 40 nm. Small sliding capability is included to enable the contacting surfaces to undergo small sliding relative to each other. For simulations shown in Figure 5, the top of the  $\text{HfO}_x$  and bottom of the  $\text{MgO}_x$  nodes are tied together to prevent any slip.

## ASSOCIATED CONTENT

### Data Availability Statement

The data that support the findings of this study, as well as the input files for the finite element simulations, are openly available in "Dataset for Design and Pattern Strain in 2D materials" at Illinois Data Bank, reference number 10.13012/B2IDB-2595358\_V1.

### Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acsnano.3c09354>.

Derivation of the mechanical model of stressor-capped monolayer  $\text{MoS}_2$ , the optical detection of strain and doping of  $\text{MoS}_2$  via Raman spectroscopy, the strain anisotropy and FEA settings, Supporting Figures S1–S10, Supporting Table S1 (PDF)

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### Author Contributions

Y.Z., M.A.H., and K.J.H. contributed equally to this work. A.M.v.d.Z., Y.Z., and M.A.H. conceived the concept for the study. Under A.M.v.d.Z.'s supervision, Y.Z. and M.A.H. performed monolayer sample fabrication, spectroscopy measurements, and analysis to extract local strains. M.A.H. performed heterostructure fabrication, spectroscopy measurements, and analysis of heterostrain. P.F.F. assisted in sample fabrication. J.M. assisted in thin film stressor deposition. T.P. and S.M.W. provided crucial guidance on the process



parameters and materials needed for stressor deposition and film stress analysis. Under A.M.v.d.Z.'s supervision, Y.Z. and K.J.H. developed the mechanics models. Under A.M.v.d.Z.'s and E.E.'s supervision, K.J.H. built the finite element analysis simulations. All authors read and contributed to the manuscript.

## Notes

The authors declare no competing financial interest.

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