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# Axis-Dependent Conduction Polarity in WSi<sub>2</sub> Single Crystals

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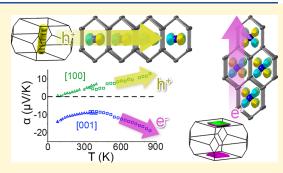
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**ABSTRACT:** Materials that demonstrate axis-dependent conduction polarity enable new technologies by integrating p- and n-type functionality into a single crystal. Certain anisotropic crystal structures give rise to this behavior by having dominant electron conduction along one crystallographic direction and dominant hole conduction along another. However, only a few materials have been experimentally shown to demonstrate this unique property. Here, we identify axis-dependent conduction polarity in tetragonal  $\alpha$ -WSi<sub>2</sub>: a durable, thermally robust, and oxidation-resistant metal synthesized from earth-abundant elements. Two single crystals of  $\alpha$ -WSi<sub>2</sub> were prepared using Xe floating zone techniques, and their anisotropic conduction properties were evaluated. Simultaneous positive and negative thermopowers measured along



the [100] and [001] directions, respectively, indicate that this material exhibits axis-dependent conduction polarity, which closely matches theoretical predictions. Hall measurements also show dominant p-type and n-type conduction along these respective crystallographic directions. Heat capacity measurements indicate that the density of states of these crystals is close to that of an exact  $\alpha$ -WSi<sub>2</sub> stoichiometry, confirming that this polarity anisotropy exists in relatively undoped crystals. In total,  $\alpha$ -WSi<sub>2</sub> is an excellent material platform for the future exploration of potential applications of this phenomenon.

### ■ INTRODUCTION

Almost all modern electronic technologies, such as transistors, solar cells, photocatalysts, thermoelectric generators, and lightemitting diodes, rely on the integration of both p-type and ntype materials to form functional devices. Materials with axisdependent conduction polarity simultaneously exhibit both ptype and *n*-type conduction behavior along different directions of a single crystal by having holes dominate conduction along one crystallographic direction and electrons along another. 1-These goniopolar materials have already been found to enable new device structures that overcome inefficiencies in existing technologies, such as avoiding the hot-side contacts in transverse thermoelectric generators, 2,3,8-11 enhancing the performance of cascaded Peltier coolers, 8,10,12 and allowing new phenomena such as the photogeneration of intense THz radiation in thin films. 13 While this phenomenon may enable new types of electronic devices, only a small but growing number of materials with this effect have been discovered so far. 1,2,4-7,14-16 Even fewer of these phases are air-stable and synthesized from earth-abundant elements, both of which are necessary for practical device applications and their eventual commercialization. The continued discovery of new materials with this phenomenon is essential for their long-term

One material with this unique effect, Re<sub>4</sub>Si<sub>7</sub>, has recently been shown to exhibit exceptional thermoelectric properties and remarkable efficiency in transverse thermoelectric generators.<sup>2,3</sup> The structure of Re<sub>4</sub>Si<sub>7</sub> crystallizes into a Si-

vacancy ordered monoclinic (Cm)  $7a + c \times b \times c - a$  supercell of the tetragonal I4/mmm  $\alpha$ -WSi<sub>2</sub> unit cell that forms due to the strong thermodynamic preference for 14 e<sup>-</sup>/transition metal.  $^{17-19}$  We have shown computationally that if a specific material exhibits axis-dependent conduction polarity, then isoelectronic materials with similar crystal structures are also likely to exhibit this effect. Considering that both Re<sub>4</sub>Si<sub>7</sub> and  $\alpha$ -WSi<sub>2</sub> feature similar bonding patterns with 14 e<sup>-</sup>/transition metal,  $^{19,20}$  we identified WSi<sub>2</sub> as a potential host for axis-dependent conduction polarity. Importantly, tungsten is over 2000x more abundant in earth's crust than rhenium,  $^{21}$  making  $\alpha$ -WSi<sub>2</sub> much better suited than Re<sub>4</sub>Si<sub>7</sub> for large-scale device applications that can exploit this phenomenon.

 $\alpha$ -WSi<sub>2</sub> and the structurally identical  $\alpha$ -MoSi<sub>2</sub> are historic materials that have long been studied and exploited for their electrical and thermal properties. Both materials have been used as electrical shunts and gate electrodes due to their high electrical conductivities. Their resistance to oxidation and thermal shock, as well as high emissivity, led to their use as high-temperature heating elements and have even made them attractive for heat shields on spacecraft reentering the

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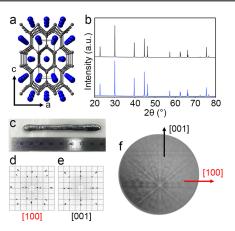


atmosphere.<sup>26</sup> More recently,  $\alpha$ -MoSi<sub>2</sub> and  $\alpha$ -WSi<sub>2</sub> have attracted significant attention after being identified as possible candidates for type II Dirac semimetals that may host topological states upon sufficient doping.<sup>27</sup> In contrast to the semiconducting Re<sub>4</sub>Si<sub>7</sub>,  $\alpha$ -WSi<sub>2</sub> is a multiband metal, <sup>28,29</sup> but it still has band structure features that suggest that it will demonstrate axis-dependent conduction polarity. Early computational and de Haas-van Alphen studies elucidated the presence of multiple anisotropic Fermi surfaces, namely a nearly cylindrical prolate-shaped hole surface oriented in the zdirection and a flat oblate ellipsoidal 4-cornered rosette shaped electron surface found in the x-y plane. <sup>20,30</sup> These indicate holes should have much higher mobilities in the x-y plane, and electrons should have much higher mobilities along the zaxis, both of which are signatures of axis-dependent conduction polarity. 1,20,30 More recently, low-temperature (2 K) Hall effect measurements on single crystals of WSi2 showed opposite signs along different crystallographic directions. Positively sloped Hall curves were measured along the [100] direction, suggesting holes are the dominant carrier, while negatively sloped Hall curves were measured along the [001] direction, indicating electrons as the dominant carrier.<sup>31</sup> For these reasons, we thought it worthwhile to evaluate whether this material can host axis-dependent conduction polarity.

To investigate the possibility of axis-dependent conduction polarity in this material, we grew large single crystals of  $\alpha$ -WSi<sub>2</sub> in a Xe floating zone furnace and fully characterized their thermal, electrical, and magnetoelectronic properties along the primary crystallographic directions. We found the crystals thermally stable up to at least 850 K and to be resistant to oxidation. We show that single crystals of WSi2 demonstrate axis-dependent conduction polarity with p-type conduction along the a- and b-axes and n-type conduction along the c-axis, as evidenced by the signs of both the Seebeck and Hall coefficients. Using density functional theory (DFT) calculations and magnetoresistance measurements, we conclude that axis-dependent conduction polarity in WSi2 arises via the multicarrier mechanism, suggesting that electrons and holes occupy separate bands in the material. WSi<sub>2</sub> is one of the only air-stable materials with axis-dependent conduction polarity to be made from earth-abundant, nontoxic elements, highlighting its promise for large-scale production, and device implementation. The discovery of axis-dependent conduction polarity in WSi<sub>2</sub> also confirms our hypothesis<sup>1</sup> that once a material with axis-dependent conduction polarity is identified, it is highly likely that materials with similar structures and electron counts will demonstrate the same phenomenon.

## ■ RESULTS AND DISCUSSION

In tetragonal I4/mmm  $\alpha$ -WSi<sub>2</sub>, each W atom is surrounded by 10 Si atoms in a bicapped cube geometry oriented along the c-axis. Each Si atom is also bonded to 5 neighboring Si atoms in a distorted square pyramidal geometry, with each Si atom forming both the apex and the corner of two adjacent bicapped cubes (Figure 1a). This phase melts at  $2160~^{\circ}\text{C}$ ,  $^{32}$  so polycrystalline samples were first prepared from the elements using arc melting. Samples were prepared with 5-10% excess Si to account for the volatilization of Si during arc melting and subsequent crystal growth. The purity of this starting material was evaluated with powder X-ray diffraction. Then, this polycrystalline arc-melted material was used as feed material in a Xenon optical floating zone furnace to grow large single crystals of WSi<sub>2</sub> measuring up to 4 cm in length and 5 mm in



**Figure 1.** Crystal structure, synthesis, and orientation of WSi<sub>2</sub> single crystals. (a) Crystal structure of I4/mmm α-WSi<sub>2</sub>. W atoms are shown in blue and Si atoms are shown in gray. (b) Powder X-ray diffraction pattern of α-WSi<sub>2</sub> single crystals 1 (top, black) and 2 (bottom, blue). (c) Single crystal of WSi<sub>2</sub>. Laue backscattering X-ray diffraction patterns of the (d) [100] and (e) [001] directions. (f) EBSD pattern of a polished cross-sectional slice of WSi<sub>2</sub> single crystal.

diameter (Figure 1c). Powder X-ray diffraction (Figure 1b) confirmed the phase purity of the crystals, and externally performed inductively coupled plasma-atomic emission spectroscopy measurements indicated a W:Si ratio of an average stoichiometry WSi<sub>1.95(2)</sub> from these two crystals, which is close to the value expected for WSi<sub>2</sub> given the  $\pm 10\%$  relative error reported for the procedure. Single crystal X-ray diffraction was also performed, and indexing and unit cell refinement of these data indicated a body-centered, tetragonal lattice belonging to the I4/mmm space group with lattice parameters (a = b = 3.2134(1) Å, c = 7.8303(4) Å) and atomic positions (W = 0, 0, 0 2a Wyckoff site; Si = 0, 0, 0.3347(2) 4e Wyckoff site). Refinement of atom site occupancies was consistent with full occupancy of both the tungsten and silicon sites, and the crystallographic data are summarized in Tables S1–S3.

Backscattering Laue X-ray diffraction was used to orient the crystals along the primary crystallographic directions ([001]/[010] and [100]) (Figure 1d,e). It was found that the crystals grew along one of the equivalent [100]/[010] directions, with the other [100]/[010], and [001] directions both lying parallel to the plane of a cross-sectional slice of the rod-shaped crystal. Electron backscattering diffraction (EBSD) patterns of polished cross-sectional slices of the crystals further confirm the single-crystallinity and the relative orientations of the crystals (Figure 1f), including the [100] growth direction of both crystals. The EBSD pattern of 50 random spots across the entire 5 mm diameter cross-section was nearly identical and all indexed to the same [100] orientation, indicating that each crystal is comprised of a single domain.

The electronic structure of  $\alpha$ -WSi<sub>2</sub> was calculated using DFT. The lattice parameters and atomic positions obtained from the Rietveld refinement of the powder X-ray diffraction pattern were used to generate band structures and their related Fermi surfaces. The band structure indicates that WSi<sub>2</sub> is metallic, with both a hole-like and electron-like band that crosses the Fermi level (Figure 2a) in the first Brillouin zone (Figure 2b). The electron pocket is a pillow-shaped oblate ellipsoid and is predominantly comprised of W  $5d_{xz}$  and  $5d_{yz}$  orbitals, suggesting that electrons will dominate conduction along the c-axis (Figure 2c,d). The hole pocket is a narrow,

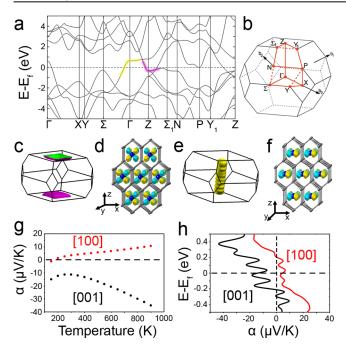


Figure 2. Calculated electronic properties of WSi<sub>2</sub>. (a) Calculated band structure of WSi<sub>2</sub> with pink band corresponding to the electron pocket and yellow band corresponding to the hole pocket. (b) The body-centered tetragonal Brillouin zone for c > a. (c) Fermi surface and (d) wavefunction ( $\psi$ ) of the bottom of the electron pocket at  $Z = E_f = -0.48 \, \text{eV}$ ), showing the W  $5 \, \text{d}_{xz} / \, \text{d}_{yz}$  orbital origin. (e) Fermi surface and (f) wavefunction ( $\psi$ ) of the top of the hole pocket at  $\Gamma = E_f = 0.59 \, \text{eV}$ ), showing the W  $5 \, \text{d}_{xy}$  orbital origin. (g) Calculated thermopowers at  $E = E_f = 0$  as a function of temperature and (h) calculated thermopowers as a function of doping level at 400 K.

cylindrically shaped prolate ellipsoid and is predominantly comprised of W  $5d_{xy}$  orbitals, suggesting that holes will dominate conduction along the a- and b-axes (Figure 2e,f). The orbital composition of these two points is very similar to the conduction band minimum and valence band maximum of  $Re_4Si_7$ . These calculated Fermi surfaces are consistent with

previously reported calculations and de Haas-van Alphen measurements. 20,30,31 Crystal Orbital Hamilton Population (COHP) calculations, partial density of states (pDOS), and orbitally resolved band structures confirmed the atomic orbital origins of both electron and hole conduction (Figures S1–S3). COHP calculations reveal that the bands near the Fermi level consist mostly of nonbonding orbital character. In particular, the W–Si bonding states appear at  $E - E_F = -3$  eV and W–Si antibonding character appears at  $E-E_{\rm F}=2$  eV. The Si-Si bonds lie much deeper in the valence band at lower energies. The low-lying Si-Si bonding states, and higher energy metal-Si bonding and antibonding states is often seen in the related 14 e per transition metal Nowotny Chimney Ladder phases. 18 The pDOS shows that the orbital composition of the valence band maximum is W 5d<sub>xy</sub> in nature, which is also confirmed by the orbital resolved band structure. In particular, the orbitally resolved W 5dxy band structure shows a large downwardcurving energy dispersion from  $\Gamma$  to  $\Sigma$  and  $\bar{\Gamma}$  to X, which corresponds to the [100]/[010] directions but is flat from  $\Gamma$  to Z, which corresponds to the [001] direction. Simultaneously, the conduction band minimum in the pDOS is comprised of W 5d<sub>xz</sub>/d<sub>vz</sub> orbitals (Figure S1) that have a strong upwardcurving energy dispersion in the orbitally resolved band structure from Z to  $\Gamma$  (Figure S2), indicating that electrons will dominate transport along the [001] direction. Overall, these calculations suggest that WSi2 will exhibit axis-dependent conduction polarity via the multicarrier mechanism, in which electrons and holes are both present in different bands such that electrons have a higher mobilities along one direction, and holes a higher mobility along another.

Seebeck coefficient tensors ( $\alpha_{xx}$  and  $\alpha_{zz}$ ) were derived from the electronic band structure assuming an isotropic scattering time approximation as implemented in the linear Boltzmann equation solver BoltzTraP, and further indicate the presence of axis-dependent conduction polarity. When nominally undoped at  $E-E_{\rm f}=0$ ,  $\alpha_{xx}$  and  $\alpha_{zz}$  are predicted to have oppositely signed thermopowers above 200 K, with  $\alpha_{xx}$  being positive and  $\alpha_{zz}$  being negative (Figure 2g). At higher temperatures, the  $\alpha_{xx}$  and  $\alpha_{zz}$  thermopowers are generated by carriers across a wider

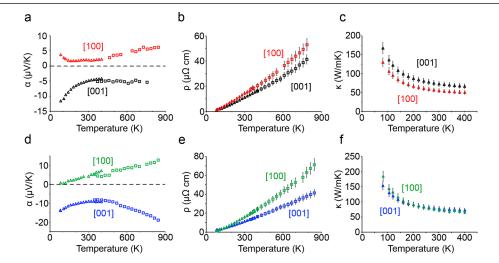


Figure 3. Thermal, electrical, and thermoelectric properties of two different WSi<sub>2</sub> crystals. Triangles denote data points collected using a liquid nitrogen cryostat, while squares indicate data collected using a Linseis LSR-3 instrument. (a) The thermopowers, (b) thermal conductivities, and (c) electrical resistivities of single crystal 1 of WSi<sub>2</sub> as a function of temperature, measured along both the [001] (black) and [100] (red) directions. (d) The thermopowers, (e) thermal conductivities, and (f) electrical resistivities of single crystal 2 of WSi<sub>2</sub> as a function of temperature, measured along both the [001] (blue) and [100] (green) directions.

range of energy close to  $E_{\rm f}$  and are less susceptible to local changes in the band structure. The  $\alpha_{\rm xx}$  and  $\alpha_{\rm zz}$  thermopowers were also calculated from 300 to 600 K across a range of doping levels (Figures 2h and S4). These calculations indicate that  $\alpha_{\rm xx}$  and  $\alpha_{\rm zz}$  should have opposite signs near the Fermi level from  $E-E_{\rm f}=+0.2$  to -0.2 eV, especially at higher temperatures. It is important to point out that this axis-dependent conduction polarity occurs at  $E-E_{\rm f}$  far below the predicted type II Dirac point at  $E-E_{\rm f}=\sim 0.71$  eV.  $^{27}$ 

To experimentally confirm that crystals of WSi2 demonstrate axis-dependent conduction polarity, the transport properties of two different crystals of WSi<sub>2</sub> were measured along the [100] and [001] crystallographic directions from 80 to 850 K (Figure 3). Special care was taken to measure along the precise [100] and [001] directions, as these correspond to the directions where the off-diagonal component of the thermoelectric tensor is zero. Positive Seebeck coefficients were measured along the [100] directions of both crystals 1 (Figure 3a) and 2 (Figure 3d) while negative Seebeck coefficients were measured along the [001] directions. At 760 K, crystal 1 had thermopowers of +6  $\mu$ V/K along the [100] direction and -5  $\mu$ V/K along the [001] direction (Figure 3a). Similarly, at 760 K, crystal 2 demonstrated thermopowers of +11  $\mu$ V/K along the [100] direction and  $-16 \mu V/K$  along the [001] direction (Figure 3d). The magnitudes of these values are quite close to the thermopower values calculated from first principles in Figure 2g, especially at higher temperatures where a larger energy window of the band structure is sampled. Below 100 K in crystal 2, the thermopower along the [100] crosses from positive to negative below 80 K which is similar to the calculated crossover at 200 K (Figure 2g), while in crystal 1 the [100] turns slightly more positive below 140 K. At lower temperatures, the charge carriers with energies much closer to  $E_{\rm F}$  participate in transport, magnifying any subtle deviations between the calculated and experimental band structures, as well as extrinsic doping and Fermi levels.

Both crystals demonstrate metallic resistivity trends with similar values measured for both the [100] and [001] directions (Figure 3b,e). In both crystals, the [100] resistivity is up to 70% higher than the [001] with the largest differences at the highest temperatures. At 300 K, the [100] resistivity of 14.3  $\mu\Omega$  cm is just 20% higher than the [001] resistivity of 11.2  $\mu\Omega$  cm for crystal 1. Temperature-dependent resistivity measurements were also performed from 2 to 300 K in a Physical Properties Measurement System (PPMS) (Figure S5). These data closely matched the values collected using a liquid nitrogen cryostat (Figure 3). Additionally, the residual resistivity ratio ( $\rho_{300\text{K}}/\rho_{2\text{K}}$ ), was measured to be 27 for WSi<sub>2</sub> crystal 1 and 8.6 for crystal 2, which are indicative of relatively few grain boundaries and scattering sites in these metallic crystals, and comparable to recent reports.

Both crystals have a high thermal conductivity and demonstrate relatively isotropic thermal conductivity along both the [100] and [001] directions (Figure 3c,f). The total thermal conductivity of a material is the sum of the lattice ( $\kappa_{\rm lat}$ ) and electronic ( $\kappa_{\rm elec}$ ) components. The electronic component of the thermal conductivity for both crystals along both directions can be readily estimated from the electrical resistivity using the Wiedemann–Franz law and the standard Lorenz number of 2.44 × 10<sup>-8</sup> V<sup>2</sup> K<sup>-2</sup>. Using this method, at 300 K,  $\kappa_{\rm elec}$  along the [100] and [001] directions are 51 and 64 W m<sup>-1</sup> K<sup>-1</sup>, respectively for crystal 1. By subtracting  $\kappa_{\rm elec}$  from the total thermal conductivity,  $\kappa_{\rm lat}$  can be derived and is found

to be 4 and 8 W m<sup>-1</sup> K<sup>-1</sup> along the [100] and [001] directions at 300 K. For comparison, Re<sub>4</sub>Si<sub>7</sub>, which is two orders of magnitude more electrically resistive, and thus thermal conductivity is almost completely dominated by  $\kappa_{\rm lat}$ , has a relatively isotropic total thermal conductivity of 4–4.5 W m<sup>-1</sup> K<sup>-1</sup> at 300 K. Thus, the lattice thermal conductivity is similar across both materials, which feature nearly identical elements in similar 3D bonding patterns. In summary, the minimal anisotropy in thermal conductivity is dictated mostly by the minimal anisotropy in  $\kappa_{\rm elec}$ .

While we determined that WSi<sub>2</sub> exhibits axis-dependent conduction polarity using thermopowers across a wide temperature range, previous reports have determined the sign of the majority carrier at low temperature using Hall measurements.<sup>31</sup> These measurements hinted that WSi<sub>2</sub> may demonstrate axis-dependent conduction polarity, with a negative Hall coefficient along the [001] direction and a positive Hall coefficient along the [100] direction. We performed Hall measurements on crystals 1 (Figure 4a) and

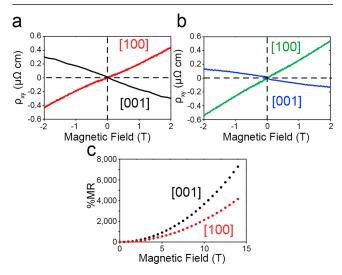
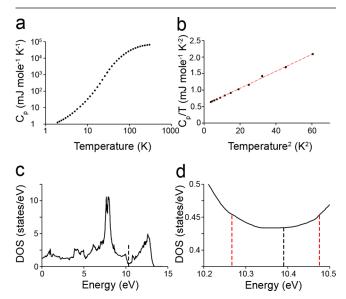


Figure 4. Hall measurements of (a) WSi<sub>2</sub> crystal 1 and (b) WSi<sub>2</sub> crystal 2 with current applied along the [100] (red, green) and [001] (black, blue) crystallographic directions at 2 K. (c) Transverse magnetoresistance of crystal 1 with current applied along the [100] (red) and [001] (black) directions at 2 K, where %MR =  $[\rho(B) - \rho(0)]/\rho(0) \times 100$ .

2 (Figure 4b), confirming the original result. Based on the slope from  $\pm 1$  T, crystal 1 has  $R_{\rm H} = -0.16 \,\mu\Omega$  cm/T along the [001] direction and  $R_{\rm H}$  = 0.21  $\mu\Omega$  cm/T along the [100] direction. Similarly, crystal 2 has  $R_{\rm H}$  =  $-0.07~\mu\Omega$  cm/T along the [001] direction and  $R_{\rm H}$  = 0.26  $\mu\Omega$  cm/T along the [100] direction. These values are close to previous measurements on single crystals.<sup>31</sup> Using a single carrier approximation, these  $R_{\rm H}$ values would correspond to carrier densities in the range of 2- $9 \times 10^{21}$  cm<sup>-3</sup>. It is important to point out that anisotropic mobility tensors in materials with axis-dependent conduction polarity precludes the direct determination of e and h+ concentrations and mobilities from Hall measurements. However, the change in sign measured along different directions suggest that holes have a higher mobility than electrons along the [100] direction, whereas electrons have a higher mobility along the [001] direction. These conclusions are supported by effective masses  $(m^*)$  calculated from the averaged curvature of the anisotropic electron and hole bands.

Along the [100] direction,  $|m_{xx,h}^*| = 0.14$  m<sub>e</sub> and  $|m_{xx,e}^*| = 2.1$  m<sub>e</sub>, suggesting that holes will dominate conduction. In the [001] direction,  $|m_{zz,h}^*| = 3.7$  m<sub>e</sub> and  $|m_{zz,e}^*| = 0.73$  m<sub>e</sub>, suggesting that electrons will dominate conduction. These values also demonstrate the greater degree of anisotropy in the hole band compared to that of the electron band, which is similarly observed in Re<sub>4</sub>Si<sub>7</sub>.<sup>2</sup> Finally, a large transverse magnetoresistance is observed (Figure 4c) along both the [100] and [001] directions, indicating that the simultaneous presence of independent electron and hole bands contribute to conduction. This is a clear signature that axis-dependent conduction polarity arises due to a multiband mechanism.<sup>1</sup>

Heat capacity measurements were also performed from 2 to 300 K to determine the doping level of the WSi<sub>2</sub> crystals (Figure 5a). At low temperature, the heat capacity of a metal



**Figure 5.** Specific heat capacity measurement of WSi<sub>2</sub>. (a) Specific heat capacity of WSi<sub>2</sub> from 2 to 300 K. (b) Linearized specific heat capacity at low temperature. (c) Calculated density of states of a primitive WSi<sub>2</sub> cell with a black dashed line marking  $E-E_{\rm f}=0$ . (d) Expanded DOS near the Fermi level showing the possible doping range of the WSi<sub>2</sub> crystals based on the DOS extrapolated from the specific heat capacity measurement. The black dashed line shows the calculated undoped Fermi level, and the red dashed lines enclose the possible doping range based on the experimentally determined DOS.

can be described by  $C_{\rm p}=\gamma T+\beta T^3$ ,where  $\gamma T$  is the electronic specific heat and  $\beta T^3$  is the phonon specific heat. <sup>33</sup> By plotting  $C_{\rm p}/T$  vs  $T^2$  at low temperature and extrapolating the linear fit to  $T^2=0$ , we found the temperature coefficient of the electronic specific heat,  $\gamma$ , to equal  $5.38-10^{-4}$  J mole <sup>-1</sup> K<sup>-2</sup> and the temperature coefficient of the phonon specific heat,  $\beta$ , to equal  $2.57\times 10^{-5}$  J mole <sup>-1</sup> K<sup>-4</sup> (Figure 5b). Then, the  $\gamma$  value can be used to calculate the density of states (DOS) using the equation  $N(E_{\rm F})=\left(\frac{3}{\pi^2k_{\rm B}^2(1+\lambda)}\right)\!\gamma$ , where N ( $E_{\rm F}$ ) is

the DOS at the Fermi level,  $k_{\rm B}$  is the Boltzmann constant, and  $\lambda$  is the electron–phonon coupling constant, which is generally nonzero for most real materials. As a result, the DOS cannot be directly determined from the heat capacity. However, if  $\lambda$  is assumed to be zero, then the measured  $\lambda$  value in our WSi2 crystal would correspond to a DOS of 0.4566  $\pm$  0.002 filled electron states per eV at the Fermi level for each primitive WSi2 cell. Using DFT, we also calculated the DOS for WSi2 to

compare to our experimental result (Figure 5c). By comparing the DOS calculated from the heat capacity measurement to the DFT-calculated DOS, we estimate that the Fermi energy of the WSi2 crystal is within 0.1 eV of the undoped Fermi energy of 10.39 eV (Figure 5d). However, it is difficult to determine precisely where the Fermi energy of the grown crystal lies because DFT calculation cannot perfectly capture the true electronic structure of a real crystal, in which defects and doping play large roles in even relatively pure crystals. Additionally, the relatively flat DOS near the Fermi level gives rise to a large uncertainty in Fermi energy, despite a relatively small uncertainty in the DOS calculated from the heat capacity measurement. However, despite the possible variation in Fermi energy due to the imprecision of this technique, little variation in physical properties, notably thermopower, would be expected across this narrow doping range (Figures 2h and S4).

## CONCLUSIONS

In this study, we grew large single crystals of WSi2 using floating zone methods and discovered the presence of axisdependent conduction polarity in this material. Positive (ptype) thermopowers along the [100] direction and negative (ntype) thermopowers along the [001] direction reveal that holes and electrons are the majority charge carriers along the [100] and [001] directions, respectively. Positive Hall coefficients along the [100] direction and negative Hall coefficients along the [001] direction reinforce the same conclusion. These experimental results can be directly traced to the band structure signatures and Fermi surfaces that give rise to axisdependent conduction polarity in this material, reinforcing the idea that Fermi surfaces and band structure signatures can be used to identify potential hosts for this phenomenon. WSi<sub>2</sub> represents one of the only air-stable materials with axisdependent conduction polarity to be grown in large single crystals with earth-abundant elements. Additionally, the discovery of axis-dependent conduction polarity in WSi2 provides conclusive evidence that materials that are isoelectronic and structurally similar to Re<sub>4</sub>Si<sub>7</sub> will also demonstrate this unique phenomenon. Ultimately, while WSi2's application in transverse thermoelectric energy generation is more limited than Re<sub>4</sub>Si<sub>7</sub> due to its much smaller thermopowers and higher thermal conductivities, it may have much better potential in technologies that can exploit its axis-dependent conduction polarity and its metallic nature.

#### EXPERIMENTAL SECTION

**Synthesis and Crystal Growth.** Pure, polycrystalline buttons of  $\alpha$ -WSi<sub>2</sub> were synthesized by arc melting stoichiometric amounts of W (99.95%, Alfa Aesar) and Si (99.999%, STREM) powder with 5–10% excess Si to account for the volatilization of Si that occurs at the high temperatures needed to congruently melt WSi<sub>2</sub>. We used the Xenon Optical Floating Zone Furnace at the NSF PARADIM facility at Johns Hopkins University to synthesize two >5 mm diameter single crystals of WSi<sub>2</sub> from arc-melted, polycrystalline WSi<sub>2</sub>. The single crystals were oriented along primary directions 100 and 001 using Laue backscattering X-ray diffraction and EBSD.

Single Crystal X-ray Diffraction. The single crystal X-ray diffraction studies were carried out on a Bruker Kappa Photon III CPAD diffractometer equipped with Mo  $K_{\alpha}$  radiation ( $\lambda = 0.71073$  Å). A 0.099 × 0.067 × 0.045 mm piece of a silver block was mounted on a MiTeGen Micromount with Paratone 24EX oil. Data were collected in a nitrogen gas stream at 100(2) K using  $\phi$  and  $\varpi$  scans. The crystal-to-detector distance was 60 mm using variable exposure

time (1–5 s) depending on  $\theta$  with a scan width of 1.0°. The data collection was 100% complete to 37.50° in  $\theta$  (0.58 Å). A total of 1847 reflections were collected covering the indices,  $-5 \le h \le 5$ ,  $-5 \le k \le 5$ ,  $-13 \le l \le 13$ . 87 reflections were found to be symmetry independent, with a  $R_{\rm int}$  of 0.0331. The data were integrated using the Bruker SAINT software program and scaled using the SADABS software program. A complete phasing model for refinement was produced through solution by dual-space method (SHELXT).  $^{34,35}$  All atoms were refined anisotropically by full-matrix least-squares (SHELXL-2014).  $^{36}$  The crystallographic data was deposited into the CCDC under deposition number 2259109.

Materials Measurement. Crystal slices were cut from the rodshaped single crystal using a diamond wire saw and were polished using 3  $\mu m$  diamond grit suspended in oil followed by 0.05  $\mu m$ alumina slurry on a precision lapping and polishing machine. These slices were cut into thin bars along the primary crystallographic directions [100] and [001]. The Seebeck coefficients, electrical resistivities, and thermal conductivities of the WSi2 crystals were measured along the [100] and [001] directions from 80 to 400 K in a Janis liquid nitrogen vacuum cryostat. A four-probe measurement geometry was used to measure sample resistance. To measure the thermopowers of these samples, an electrical current was passed through a 120  $\Omega$  Omega strain gauge attached to one end of the sample to create a temperature gradient along the direction of the crystal being measured. Two type T thermocouples, one placed near the hot side of the sample and one placed near the cold side of the sample, measured the resulting temperature gradient and the Seebeck voltage created across the sample. Thermal and electrical contacts were made to the sample's surface using Transene GE-40 gold-epoxy paste. Percent error was calculated in the resistivity and thermal conductivity measurements by dividing the electrical contact width by the length of the sample. The Seebeck coefficients and resistivities of the single crystals were measured from 350 to 850 K using a Linseis LSR-3 instrument. The temperature-dependent resistivity measurements were performed from 2 to 300 K on the same samples using a Quantum Design 14 T Physical Properties Measurement System (PPMS), and low-temperature Hall effect measurements were performed using a Quantum Design 9 T PPMS. Heat capacity measurements were performed in the Quantum Design 9 T PPMS from 2 to 300 K.

**Calculations.** The DFT calculations were performed on a WSi2 primitive cell within the Vienna Ab initio Simulation Package (VASP) $^{37}$  using Perdew–Burke–Ernzerhof (PBE) functionals. $^{38}$  The relaxed configuration was obtained using a 4  $\times$  4  $\times$  4 k-point grid and a plane-wave energy cutoff of 400 eV. The lattice parameters were fixed to experimental values obtained from the Rietveld refinement of the powder X-ray diffraction pattern to generate the electronic band structures and Fermi surfaces. The linear Boltzmann equation solver BoltzTraP $^{39}$  was used to calculate the Seebeck coefficient tensors of the WSi2 conventional unit cell. In this calculation, the k-point mesh was increased to 25  $\times$  25  $\times$  10. Crystal Orbital Hamiltonian Population analysis was performed using LOBSTER. $^{40-43}$ 

## ■ ASSOCIATED CONTENT

#### Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.chemmater.3c00183.

Crystal Orbital Hamilton Population (COHP) calculations, partial density of states (pDOS), orbitally resolved band structures, thermopower as a function of doping level and temperature, longitudinal resistivity measurements from 2 to 300 K, and crystal structure data (PDF)

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#### **Author Contributions**

K.G.K. synthesized the  $WSi_2$  single crystals, collected all experimental data presented here, and wrote the manuscript with input from J.E.G. and J.P.H. Single crystal structure solution was performed by C.E.M. Z.D. calculated the electronic structure and predicted properties of  $WSi_2$  under the supervision of W.W.

## Notes

The authors declare no competing financial interest.

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