

1 **CFD-guided patterning of tubular ceramic membrane surface by**
2 **stereolithography: Optimizing morphology at the mesoscale**
3 **for improved hydrodynamic control of membrane fouling**

4 Cyril Chevarin¹, Xunhao Wang², Denis Bouyer^{1*}, Volodymyr Tarabara^{2**}, Thierry Chartier³, André Ayral¹

5 ¹ Institut Européen des Membranes IEM – UMR 5635, ENSCM, CNRS, Univ Montpellier, Montpellier, France

6 ² Department of Civil and Environmental Engineering, Michigan State University, East Lansing, MI 48824, USA

7 ³ CNRS, University of Limoges, Institute of Research for Ceramics (IRCC), UMR 7315, European Ceramics Center,
8 Limoges, France

9 **Abstract**

10 A preliminary study was carried out on the morphological design of tubular single-channel alumina
11 membranes prepared by stereolithography, an additive manufacturing process. The geometry of the ring-
12 patterned inner surface of membranes was optimized using computational fluid dynamics calculations and
13 validated in microfiltration tests with aqueous suspensions of *P. aeruginosa*. Patterning of the inner
14 surface of tubular membranes helped reduce cake formation at a higher value of the average crossflow
15 velocity. The results highlight benefits of stereolithography-based approach to the morphological design
16 of ceramic membranes.

17 **Keywords:** ceramic membrane, computational fluid dynamics, stereolithography, fouling

19 * Corresponding author. *Institut Européen des Membranes, Univ Montpellier, Montpellier, France*

20 ** Corresponding author. *Department of Civil and Environmental Engineering, Michigan State University, East*
21 *Lansing, USA*

22 E-mail addresses: denis.bouyer@umontpellier.fr (D. Bouyer), tarabara@msu.edu (V. V. Tarabara).

24 **1. Introduction**

25 Rapid advances in additive manufacturing have paved the way for the simplified fabrication of integrated
26 systems as well as system components with complex shapes hitherto inaccessible by conventional
27 manufacturing methods. It is particularly the case for ceramic materials [1-3], which require high
28 temperature sintering to confer morphological, microstructural and mechanical properties to the shaped
29 object. These advances open up new possibilities for the design of ceramic membranes. Indeed, there is a
30 growing interest in the use of additive manufacturing methods to prepare both membranes, including
31 ceramic filters [4-6], and membrane modules [7-11].

32 Many of the current membrane processes are based on the principle of crossflow filtration, with key
33 concerns regarding the minimization of concentration polarization and fouling. Fouling management
34 often requires a regular interruption of the filtration process by cleaning sequences (e. g. backwashing)
35 limits the lifetime of the membranes. A complementary approach to minimizing fouling and its deleterious

36 effects is to promote turbulence in the feed flow. The use of turbulence promoters is possible but at a cost
37 of an increased pressure drop in the feed flow channel. Another option is to promote turbulence closer to
38 the membrane surface by altering its topography. This has been the subject of various studies, most of
39 which focused on the surface patterning of polymer membranes [12-14] although some did employ flat
40 plate ceramic membranes [15, 16].

41 Most installations use ceramic membranes in a tubular configuration, the support of which is produced by
42 extrusion. Based on a computational fluid dynamics (CFD) approach, Yang et al. explored optimization of
43 multi-channel ceramic membranes [17]. While the number and the section of the channels are easily
44 adjustable, the same cannot be said for their surface morphology. Twenty years ago a clever method was
45 developed, allowing the extrusion of tubular supports with a spiral internal surface favoring the turbulence
46 of the flow [18]. During the 2018 International Conference in Inorganic Membranes, a presentation by
47 TAMI Industries highlighted the CFD-based prediction of the benefits of having curvilinear flow inside a
48 tubular membrane channel, the practical implementation of such flow field using bundles of helical
49 membranes, as well as the potential of additive processes for manufacturing such membranes [19].

50 The present work concerns a preliminary study on the morphological design of ceramic tubular
51 membranes. Single-channel alumina tubular membranes with an inner diameter of 7 mm and an outer
52 diameter of 10 mm were selected, corresponding to usual specifications for current commercial
53 membranes of this type. The inner surface the membrane was patterned with rings – morphological
54 elements that cannot be introduced at the membrane surface by the conventional shaping method based
55 on paste extrusion. The ring profile and height as well as the inter-ring distance were optimized using CFD
56 modeling by evaluating the impact of these parameters on the turbulence near the membrane surface.
57 CFD predictions were validated in preliminary experiments with symmetric alumina microfiltration (pore
58 diameter of $\sim 0.2 \mu\text{m}$) membranes, with or without such rings, manufactured by an additive process (i. e.
59 stereolithography) from alpha alumina powder. The patterned membranes and smooth membranes
60 (controls) were comparatively evaluated in terms of fouling behavior in experiments with *P. aeruginosa*.
61 suspensions.

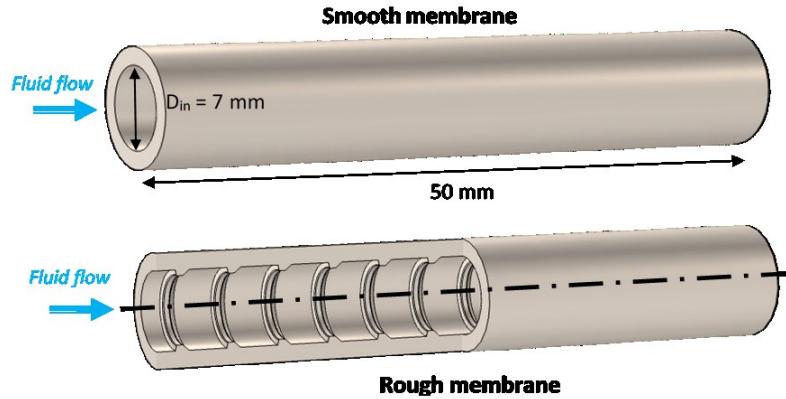
62

63 **2. Numerical model**

64 **2.1. Geometry**

65 The flow hydrodynamics in the tubular membranes was simulated for both smooth and patterned
66 membranes as shown in Figure 1. Here, “patterned” refers to a membrane with the inner (feed-facing)
67 surface having a patterned morphology. In both configurations (smooth or patterned inner surface), the
68 outer diameter and the membrane length were 10 mm and 50 mm, respectively. The inner diameter of
69 both membranes was 7 mm everywhere except in locations corresponding to roughness elements (“rings”)
70 on the surface of the patterned membrane; each such “ring” was $\sim 0.5 \text{ mm}$ high, leading to a somewhat
71 smaller inner diameter in those locations. Thanks to the axial symmetry, simulations were performed using
72 2D axisymmetric geometry thus notably reducing the calculation time.

73



74 *Figure 1. Geometry of smooth and patterned tubular membranes.*

75 **2.2. Governing equations**

76 Two feed flow rates were simulated herein, with mean velocities of $0.45 \text{ m}\cdot\text{s}^{-1}$ and $0.68 \text{ m}\cdot\text{s}^{-1}$, respectively
 77 in agreement with the values used in filtration experiments. These values are within the typical range of
 78 crossflow velocities employed in tangential filtration applications (e. g. [20]) although for ultra- and
 79 microfiltration with ceramic membranes crossflow velocities may be significantly higher – up to 4 m/s [21].
 80 Given the density and viscosity of water at 23°C , the diameter of the flow channel, and the two mean
 81 velocities, Reynolds numbers of 3100 and 4830, respectively were calculated, corresponding to the end of
 82 the transition zone between laminar and turbulent hydrodynamic regimes. Consequently, the classical
 83 Reynolds Averaged Navier–Stokes (RANS) transport equations for incompressible Newtonian fluid and
 84 turbulent regime were used in the model.

85 In the RANS model, the conservation of momentum equation is given by:

$$86 \rho(\nabla \cdot \vec{v})\vec{v} = -\nabla p + \nabla \cdot ((\eta + \eta_t)[(\nabla \vec{v} + \nabla \vec{v}^T)]) + \rho \vec{g} \quad (1)$$

87 where ρ is the water bulk density ($\text{kg}\cdot\text{m}^{-3}$), \vec{v} is the velocity vector ($\text{m}\cdot\text{s}^{-1}$), p is the static pressure (Pa),
 88 $[(\nabla \vec{v} + \nabla \vec{v}^T)] = \vec{\tau}$ is the viscous stress tensor, η is the dynamic viscosity of the water (Pa.s), η_t is the
 89 turbulent (or eddy) viscosity (Pa.s) and \vec{g} is the acceleration due to gravity ($\text{m}\cdot\text{s}^{-2}$).

90 The standard k- ε model [22] (see Supplementary Information (SI), section S1) was used to simulate the
 91 turbulence, meaning that the turbulent viscosity η_t was modeled using eq. (2) [23]:

$$92 \eta_t = \rho C_\eta \frac{k^2}{\varepsilon}, \quad (2)$$

93 where C_η is a constant, k is the turbulent kinetic energy ($\text{m}^2\cdot\text{s}^{-2}$) and ε is the turbulent energy dissipation
 94 rate ($\text{m}^2\cdot\text{s}^{-3}$).

95 **2.3. Boundary conditions**

96 Fully developed flow with a mean velocity (in $\text{m}\cdot\text{s}^{-1}$) was considered in the model for boundary conditions
 97 in the inlet side. Two mean velocities were simulated, i. e. $0.45 \text{ m}\cdot\text{s}^{-1}$ and $0.68 \text{ m}\cdot\text{s}^{-1}$. At the outlet side, a
 98 null static pressure boundary condition P_0 was fixed. A no-slip boundary condition was applied at the wall.

99 **2.4. Numerical simulations**

100 The hydrodynamic model was simulated using the commercial COMSOL Multiphysics® software, working
101 with finite element method. Using a 2D axis-symmetric model, meshes size was ranged between 0.08 mm
102 near the wall and 0.2 mm in the bulk of the flow. Boundaries layers and finer meshes were built near the
103 wall surfaces to improve the numerical accuracy in the boundary layer. The number of tetrahedral meshes
104 was close to 100 000 for the simulations without rings and 140 000 for the simulations with rings.

105

106 **3. Experimental**

107 **3.1. Membrane manufacturing and microstructural characterization**

108 The membranes were manufactured by the company 3DCERAM SINTO (Limoges, France) according to our
109 specifications. The green bodies were built using the stereolithography additive process (CERAMAKER 900
110 machine) based on the selective polymerization of a reactive mixture system under the effect of a UV
111 irradiation. The reactive system was a suspension of alumina particles (1.75 μm mean particle size) in a
112 mixture of curable monomer and oligomer, with the addition of a photoinitiator. For more details on
113 stereolithography-based processing of ceramic components, please refer to the chapter on the topic by
114 Chartier and Badey [1].

115 After debinding and sintering, the pieces were externally machined to achieve the requested dimensional
116 specifications (outer diameter = 10.0 ± 0.2 mm; inner diameter = 7.0 ± 0.2 mm; length = 49.2 ± 0.2 mm).
117 Taking into account the applied sintering conditions (maximal temperature larger than 1200°C) and the
118 nature of the used ceramic powder (i. e. pure alpha alumina), excellent stability of the membrane
119 microstructure can be expected even for long exposure to aqueous media. The experimentally observed
120 stability of membrane permeability with time is consistent with this expectation.

121 For the patterned membranes, the targeted characteristics for rings were as follows: height of 500 μm ; a
122 the upstream and the downstream edges forming an angle of 80° and 135°, respectively, with the direction
123 of the flow, and the 3mm distance between two neighboring rings. The geometry of the patterned
124 membranes was confirmed by making a cutout in one of these tubes using a diamond saw, observing this
125 sample by Keyence VHX 6000 digital microscope (VHX) and then analyzing the Keyence images with
126 suitable image processing software (VHX-6000_950F).

127 The microstructure of the membranes was investigated using a Field Emission Scanning Electron
128 Microscope (FE-SEM; Hitachi S4800). The porosity of these macroporous samples was determined by
129 mercury porosimetry (AutoPore IV 9500 Micromeritics).

130 **3.2. Fouling experiments**

131 **3.2.1. Experimental setup and membrane permeability measurements**

132 The membranes were tested using a crossflow filtration system (see SI, Figure S1), which included a
133 peristaltic pump (910-0025, Thermo Scientific), a custom-made membrane unit and a back-pressure valve
134 (SS-43S6, Swagelok). The membrane was mounted using two stainless steel push-to-connect fittings
135 (KQG2H10-00, Grainger). To seal the membrane area under the fittings and ensure it is not available for

136 permeation, the outside surface of the membrane under the fittings was coated with a thin layer of epoxy
137 (LOCTITE, Henkel). The pure water flux tests for the 3D-printed membranes were performed using DI water
138 and five different transmembrane pressure values: 1.03, 1.38, 1.72, 2.07, and 2.41 bar (15, 20, 25, 30, and
139 35 psi, respectively). The DI water (pH 5.8) was used as the feed solution in these tests. The crossflow
140 velocity was maintained constant at either $0.45 \text{ m}\cdot\text{s}^{-1}$ or $0.68 \text{ m}\cdot\text{s}^{-1}$. The permeability of each membrane
141 was calculated based on the slope of the flux vs pressure dependence.

142 *3.2.2. Bacterial suspensions: Preparation and characterization*

143 An aqueous suspension of *P. aeruginosa* (Schroeter) Migula (PA01-LAC, ATCC) was used as the feed in
144 membrane fouling tests. *P. aeruginosa* were cultured in Luria-Bertani (LB) broth to the exponential growth
145 phase. The standard curve (colony-forming units per milliliter (CFU/ml) vs absorbance at 600 nm) was
146 established. The preparation of the bacteria stock is detailed in the SI file, section S2. The bacteria were
147 enumerated by a colony count method. Briefly, the vortexed solutions were serially diluted, mixed with
148 soft agar, and poured onto LB-agar plates, which were incubated at 37°C overnight. The formed colonies
149 were counted, and then the areal density of colony-forming units (CFU/ml) was calculated. The absorbance
150 of the bacterial suspensions was measured by a spectrophotometer (Spectronic 21D). The hydrodynamic
151 diameter of bacteria was measured by dynamic light scattering (DLS). In these tests, a small sample (0.5
152 mL) of the bacterial suspension was diluted in 1 mM KCL solution, prefiltered with $0.22 \mu\text{m}$ syringe filter,
153 to the total volume of $\sim 2 \text{ mL}$.

154 *3.2.3. Membrane fouling tests*

155 Prior to each crossflow filtration test, the feed suspension was prepared by diluting the bacteria stock ten-
156 fold with DI water. The volume fraction of *P. aeruginosa* in the feed was $3.9 \cdot 10^{-5}$. With the elliptical shape
157 and the size range for *P. aeruginosa* [24] taken into account, this volume fraction translates into the
158 number-based concentration in the range from 3.9×10^7 to 19.9×10^7 bacteria/mL. Based on this low value
159 of the volume fraction and the Einstein relation between relative viscosity and volume fraction of
160 dispersed phase [25], the viscosity of this suspension was considered to be equal to that of pure water.
161 The ionic strength of the feed was 15 mM. During fouling tests, the crossflow velocity (averaged across the
162 membrane channel cross-section) was $0.45 \text{ m}\cdot\text{s}^{-1}$ or $0.68 \text{ m}\cdot\text{s}^{-1}$, which corresponded to the maximum
163 crossflow rate ($1570 \text{ mL}\cdot\text{min}^{-1}$) that the peristaltic pump could provide at the transmembrane pressure
164 used in the tests (30 psi; ~ 2.1 bar). The scope of the present study was limited to the specific values of the
165 crossflow velocity and the transmembrane pressure that were employed experimentally and matched in
166 CFD simulations. While the values assessed herein are typical, some applications (e. g. with unusually high
167 recoveries) would require additional testing and modeling to better understand how the patterned
168 morphology affects membrane performance under those conditions.

169 Prior to challenging the membrane with the bacterial suspension, the membrane was equilibrated with 15
170 mM NaCl at pH 6. The permeate was collected on a mass balance with a 1 min interval. All fouling tests
171 were done at the ambient temperature of 23°C and the relative humidity of 47%. After each fouling test,
172 the membrane was cleaned by circulating solutions in the feed channel in the following sequence: (1) DI
173 water for 30 min, (2) 5 mM EDTA at pH 11 for 30min, (3) DI water for 30 min, (4) 2 mM SDS at pH 11 for
174 30 min, (5) DI water for 30 min [26].

175 Three smooth and three patterned membranes were tested under the same experimental conditions to
176 estimate the reproducibility of the results. In order to investigate the contribution of the different fouling
177 mechanisms to the overall decline in permeate flux, additional tests were carried out in the dead-end
178 filtration regime following a procedure described earlier [27].

179

180 **4. Results and discussion**

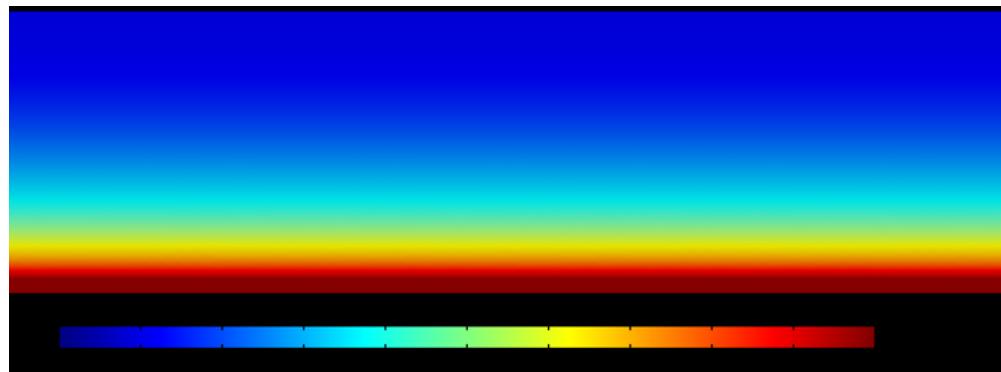
181 **4.1. Membrane design from numerical simulations**

182 As mentioned in the introduction, in the frame of this pioneering study, it was decided to pattern the inner
183 surface of the tubular membranes with simple and continuous rings. The current limitations of the existing
184 additive manufacturing in terms of dimensional tolerances were considered for sizing these rings. The
185 dimensional resolution afforded by stereolithography is $\sim 100 \mu\text{m}$ [2]. Due to the concern that features
186 approaching this size scale might lose in fidelity and in feature-to-feature consistency, the ring height was
187 chosen to be $500 \mu\text{m}$ as features of this size could be made using stereolithography with good precision.
188 With regard to rings of a larger size, one can expect that increasing the ring height would be
189 disadvantageous in terms of the distribution of ε , likely leading to large dead zones. The above
190 considerations led to the decision to prepare rings with a height and a width of $500 \mu\text{m}$.

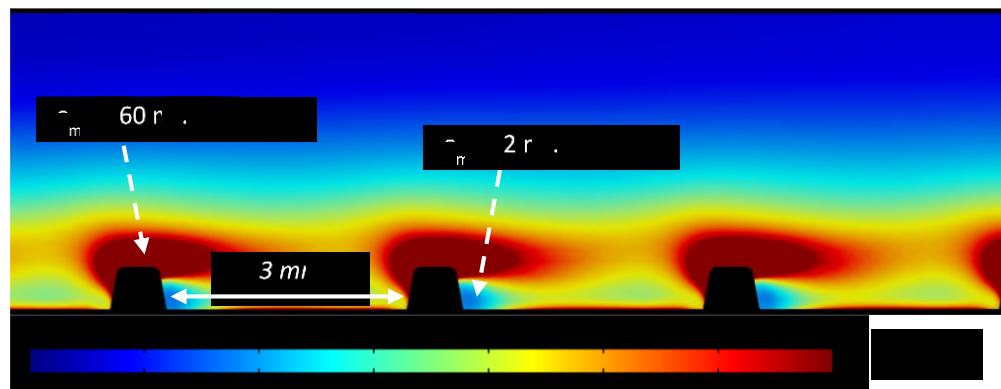
191 Moreover, using the CFD model we investigated the influence of the inter-ring distance as it changed from
192 3 to 5 mm. The results are shown in SI. Simulations for an inter-ring distance of 2 mm were also performed
193 and they exhibited the most interesting results in terms of the spatial distribution of turbulent kinetic
194 energy ε . While stereolithography does allow to prepare patterned membranes with this lower inter-ring
195 distance (2 mm), the process becomes more complex due to the difficulty of removing the unpolymerized
196 paste after manufacturing and before debinding/sintering. This is the reason why the smallest inter-ring
197 distance evaluated experimentally was 3 mm.

198 Figures 2 and 3 show the spatial distribution of the dissipation rate of turbulent kinetic energy, ε , in three
199 different configurations (smooth membrane, patterned membrane featuring rings with symmetrical
200 profile, patterned membrane featuring rings with asymmetrical profile), for average inlet velocities of 0.45
201 and $0.68 \text{ m}\cdot\text{s}^{-1}$, respectively.

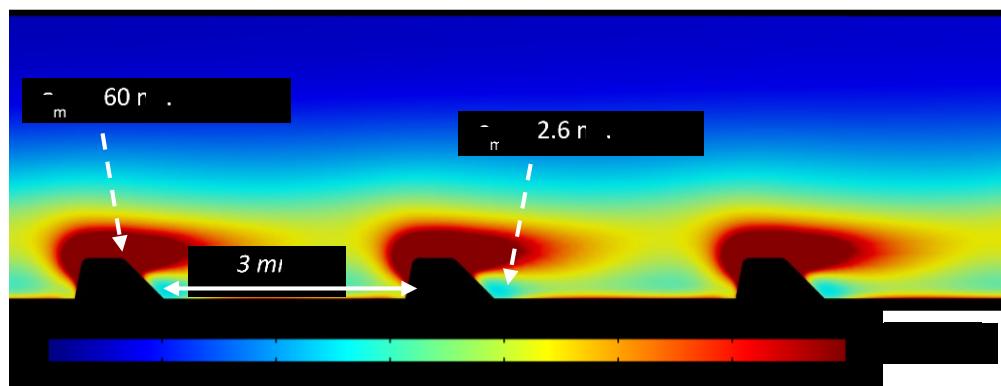
202 Whatever the configuration, ε is much higher close to the top of the rings compared to the region
203 between the rings, with a ratio close to 23 at $0.45 \text{ m}\cdot\text{s}^{-1}$ and more than 42 at $0.68 \text{ m}\cdot\text{s}^{-1}$. A 50% increase in
204 the inlet velocity (from 0.45 to $0.68 \text{ m}\cdot\text{s}^{-1}$), leads to a five-fold increase in ε at the top of the rings and a
205 three-fold increase in ε between the rings. These results confirm the intuitive predictions, highlighting
206 the interest to disturb the flow near the membrane surface to create more turbulence (more dissipation
207 of turbulent kinetic energy). With this geometrical configuration, the risk lies in the formation of dead
208 zone between the rings that is the zone with local re-circulation and characterized by a lower level of
209 turbulence. Further, when analyzing the influence of the ring shape (symmetric vs asymmetric), the
210 numerical simulations clearly show that the low ε region, localized just downstream of each ring, is
211 smaller behind rings with the asymmetrical profile. For both inlet velocities evaluated (0.45 or $0.68 \text{ m}\cdot\text{s}^{-1}$),
212 asymmetry appears to be favorable for preventing fouling phenomena. Based on these numerical
213 results, the asymmetric profile was selected.



(a) Smooth membrane

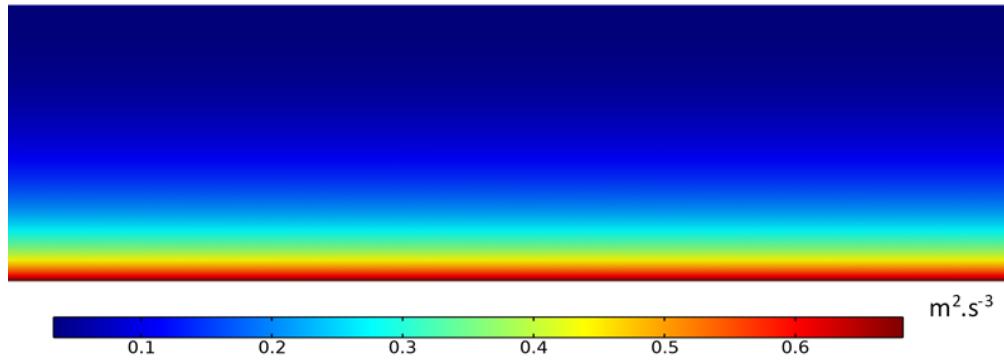


(b) Patterned membrane – symmetrical profile of surface “rings”

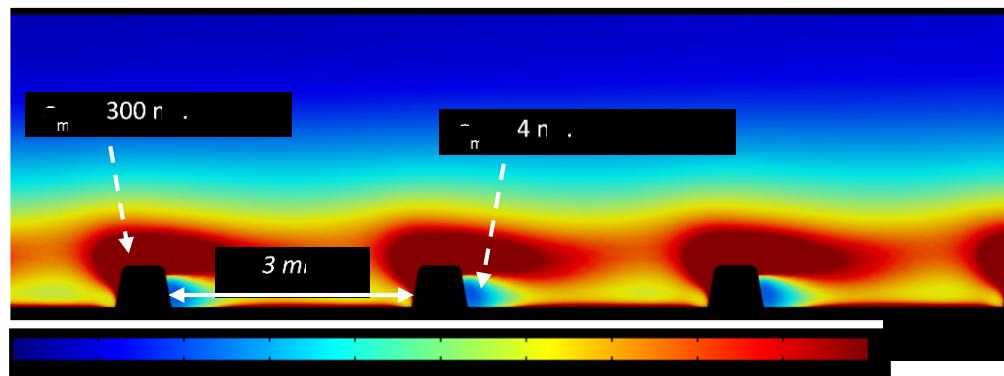


(c) Patterned membrane – asymmetrical profile of surface “rings”

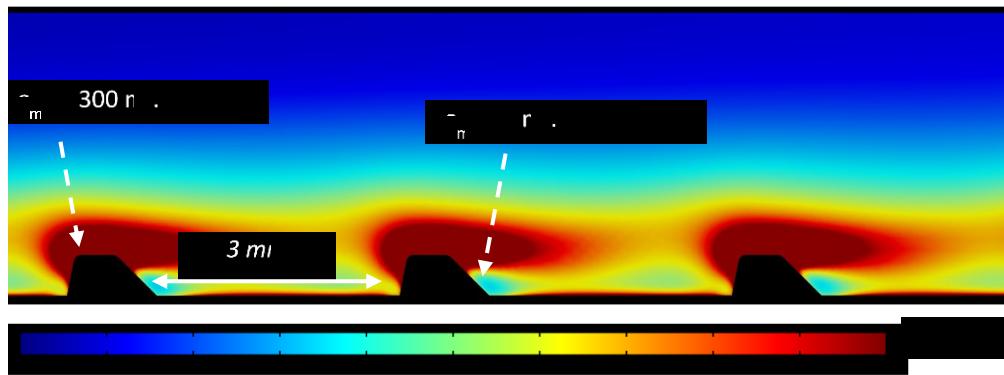
215 *Figure 2. Dissipation rate of turbulent kinetic energy, ε , in the vicinity of the rings on the surface of the tubular*
 216 *membrane for $v_{in}=0.45 \text{ m}\cdot\text{s}^{-1}$: (a) smooth membrane, (b) patterned membrane featuring “rings” with symmetrical*
 217 *profile, (c) patterned membrane featuring “rings” with asymmetrical profile.*



(a) Smooth membrane



(b) Patterned membrane – symmetrical profile of surface "rings"



(c) Patterned membrane – asymmetrical profile of surface "rings"

218 *Figure 3. Dissipation rate of turbulent kinetic energy, ε , in the vicinity the rings on the surface of the tubular*
219 *membrane for $v_{in}=0.68 \text{ m} \cdot \text{s}^{-1}$: (a) smooth membrane, (b) patterned membrane featuring "rings" with symmetrical*
220 *profile, (c) patterned membrane featuring surface "rings" with asymmetrical profile.*

221
222 Preliminary CFD study of the impact of the inter-ring distance (see SI, Figure S2) showed that it had a
223 relatively minor effect on the spatial distribution of ε . As a result of this assessment, the inter-ring distance
224 of 3 mm was selected as allowing the highest reduction in the spatial extent of low ε zones. Simulations
225 pointed out the interplay between the ring shape (symmetric vs asymmetric) and the inlet velocity as both

226 affected the spatial distribution of ε : for an inlet velocity of $0.68 \text{ m}\cdot\text{s}^{-1}$, the low ε value is increased by 75%
227 ($7 \text{ m}^2\cdot\text{s}^{-3}$ vs $4 \text{ m}^2\cdot\text{s}^{-3}$) when using the asymmetric rings, while it is only increased by 30% when the inlet
228 velocity is equal to $0.45 \text{ m}\cdot\text{s}^{-1}$.

229 Table 1 summarizes the values of the energy dissipation rate ε and the pressure loss along the membrane.
230 These values give an indication of the cost of integrating the rings as turbulence promoters within the
231 tubular membrane. Whatever the inlet velocity, the pressure loss increases by a factor 15 when using
232 patterned membranes rather than smooth ones. This result is not surprising because it is directly linked to
233 the total dissipation rate of turbulent kinetic energy, and it should be related to the energy cost of back-
234 washing frequency that should be done between two filtration cycles.

235

236 *Table 1. Specific pressure loss, ΔP_{feed} , in the feed flow along the membrane and mean value of turbulent dissipation*
237 *rate, ε_{mean} , at the membrane surface for two values of the average crossflow velocity, v_{in} . Turbulent dissipation*
238 *rate is for the membrane surface between the rings and is deduced from the simulations graphically represented in*
239 *Figure S2.*

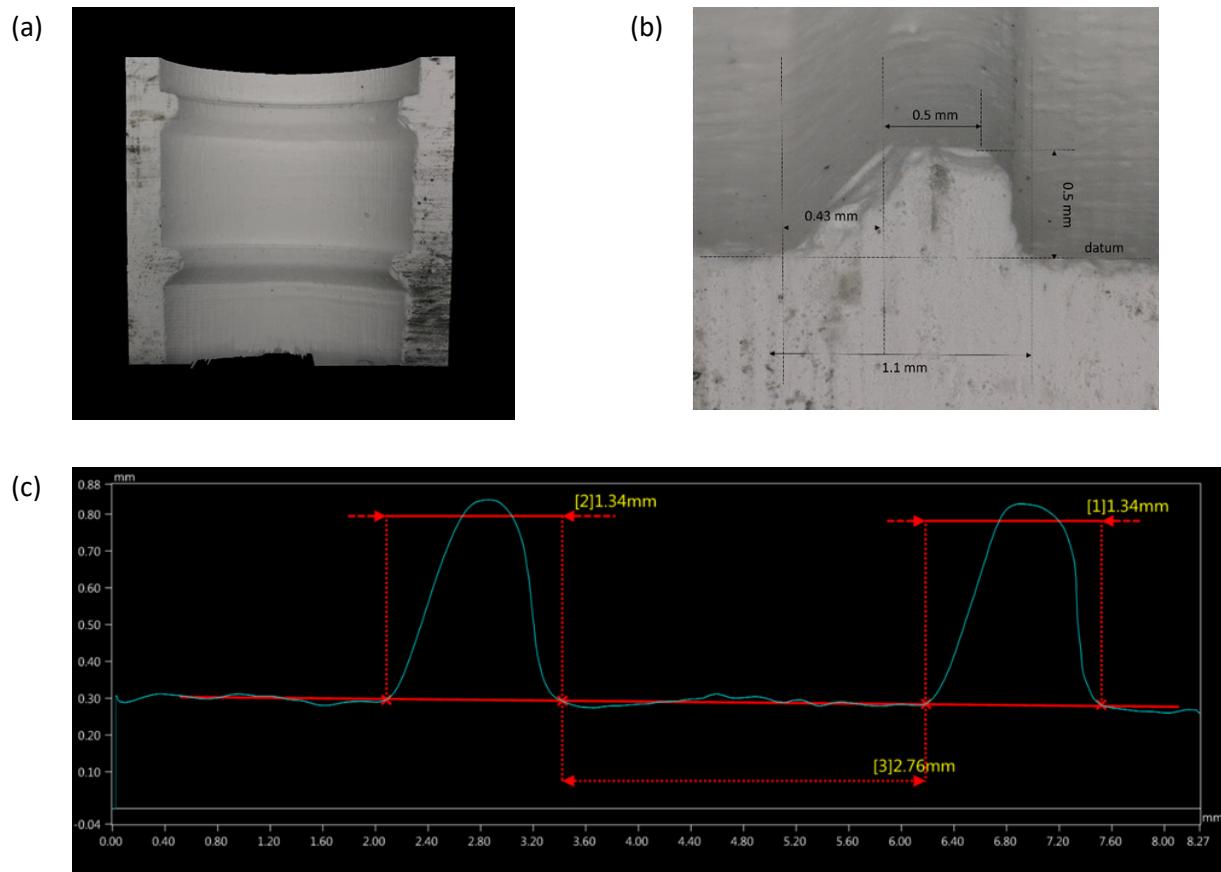
	Smooth membrane		Patterned membrane	
	$v_{in} = 0.45 \text{ m}\cdot\text{s}^{-1}$	$v_{in} = 0.68 \text{ m}\cdot\text{s}^{-1}$	$v_{in} = 0.45 \text{ m}\cdot\text{s}^{-1}$	$v_{in} = 0.68 \text{ m}\cdot\text{s}^{-1}$
$\varepsilon_{mean} (\text{m}^2\cdot\text{s}^{-3})$	0.10	0.45	4.6	16.3
$\Delta P_{feed} (\text{bar}\cdot\text{m}^{-1})$	0.006	0.013	0.092	0.204

240

241 Table 1 shows that a significant advantage can be expected with the patterned membranes in terms of
242 fouling limitation, especially for the largest value of average inlet crossflow velocity. The reported values
243 of specific pressure loss in the feed flow qualitatively account for the additional energy cost associated
244 with the use of patterned membranes. The determined values are more than one order of magnitude
245 larger for the patterned membranes but rather low in absolute value.

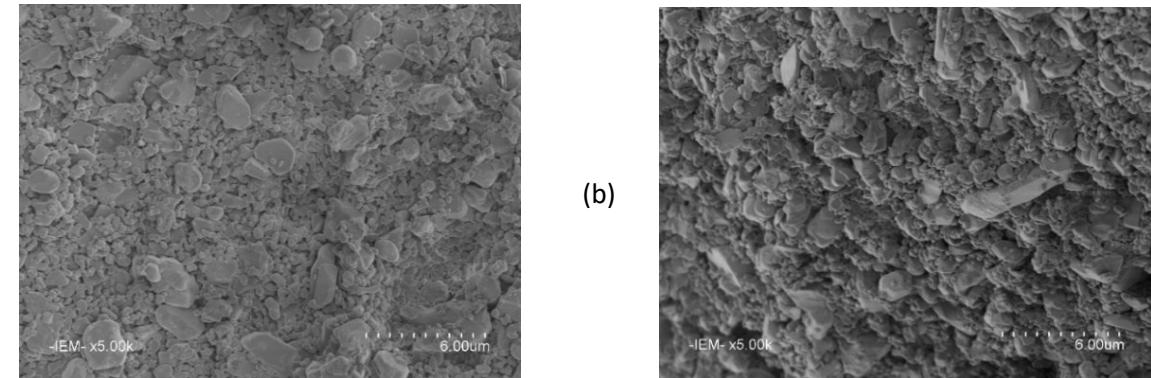
246 **4.2. Microstructural characterization of the manufactured membranes**

247 Figure 4 shows the internal morphology of the patterned membranes with the axisymmetric structure of
248 the roughness elements (“rings”) clearly shown (Figure 4a). The ring profile (Figure 4b) and the inter-ring
249 spacing (Figure 4c) correspond rather well to the targeted characteristics considering the $100 \mu\text{m}$ spatial
250 resolution of the implemented additive method. SEM imaging of the planar surface (Figure 5a) and the
251 cross-section (Figure 5b) of the membranes showed a close packing arrangement of grains with a bimodal
252 size distribution. The continuous matrix with submicron grains ($\sim 0.6 \mu\text{m}$ in size) is embedded with larger
253 grains several microns in size. One can expect the pore size to be approximately one third of the grains’
254 size. The reported pore size of $0.2 \mu\text{m}$ is indeed 3 times smaller than the grain size of the submicronic
255 fraction of the bimodal distribution.



256 *Figure 4. Geometry of the patterned membrane: (a) image of the inner surface of the membrane cutout. (b) and (c):*
257 *Characteristic sizes of roughness elements.*

258



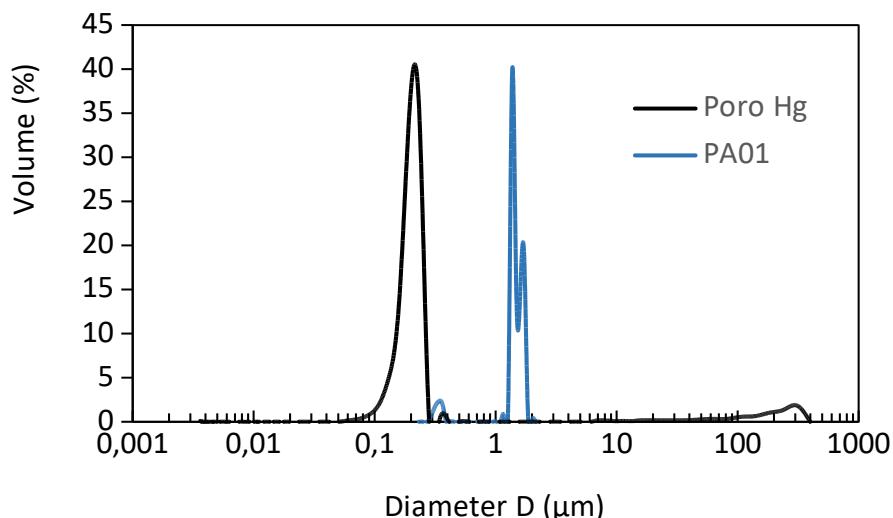
259 *Figure 5. SEM images of the membrane: (a) planar surface and (b) cross section views.*

260

261

262 Mercury porosimetry measurements yielded the porosity of $\sim 33\%$ and the specific surface area of ~ 2.5
263 $\text{m}^2 \text{g}^{-1}$. These values are consistent with what can be expected to result from the limited sintering of a
264 random close-packing arrangement of powder particles. The pore size distribution (Figure 6) is centered
265 around an average pore size of $\sim 0.2 \mu\text{m}$. The prepared membranes can thus be classified as microfilters.
266 Considering the implemented process of additive manufacturing, (stereolithography), no specific
267 microstructural changes were expected neither for smooth nor for patterned membranes. This was
268 experimentally confirmed in SEM observations of membrane cross-sections.

269



270
271 *Figure 6. Pore size distribution of ceramic membranes and the size distribution of *P. aeruginosa* bacteria*
272 *in the feed suspension.*

273 **4.3. Fouling experiments**

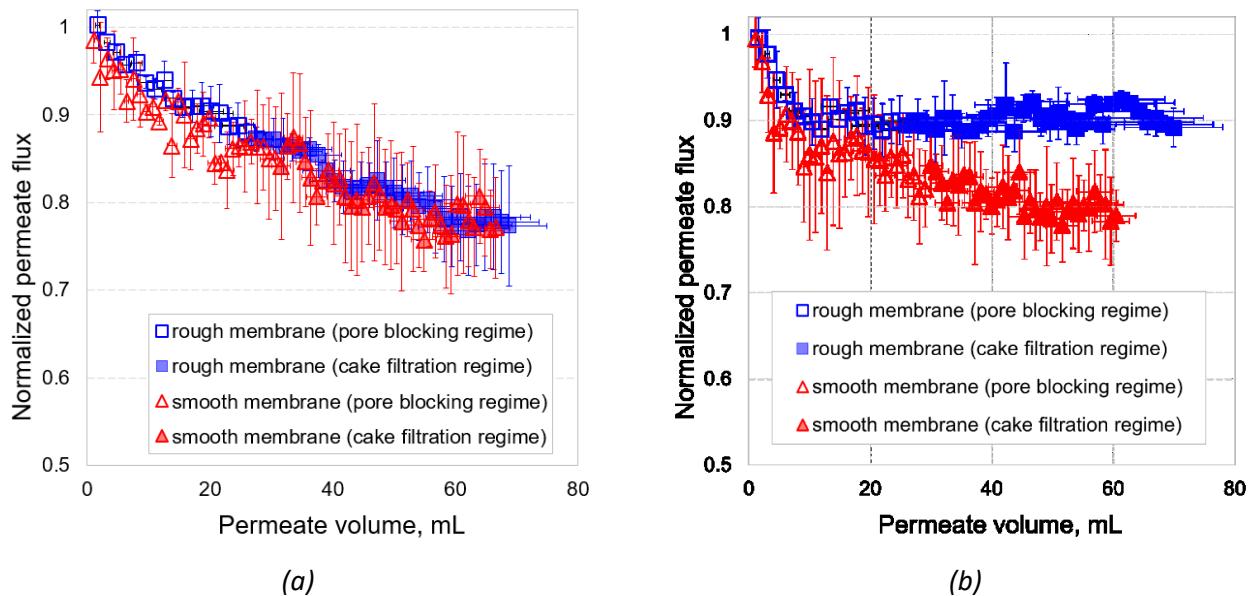
274 Based on the DLS measurements, the average size of bacteria in the feed suspension was $\sim 0.8 \mu\text{m}$, which
275 is significantly larger than the measured average pore size ($\sim 0.2 \mu\text{m}$) of the membrane (Figure 6). The DLS
276 measurements estimated the diffusion coefficient, which was then converted to particle size assuming
277 that the scatterers are spherical.

278 Application of the Carman-Kozeny relation to mercury porosimetry data [28] estimates the intrinsic
279 permeability of the membrane to be $\sim 1.6 \cdot 10^{-16} \text{ m}^2$. The expected water permeability at 23°C is thus equal
280 to $42 \pm 16 \text{ L} \cdot \text{m}^{-2} \cdot \text{h}^{-1} \cdot \text{bar}^{-1}$, which is within the experimental error from the value measured experimentally
281 for a smooth membrane ($69 \pm 15 \text{ L} \cdot \text{m}^{-2} \cdot \text{h}^{-1} \cdot \text{bar}^{-1}$). The difference of filtering area for the patterned
282 membranes was estimated to be the increase of 11.5 %, assuming an ideal geometry. The water
283 permeability experimentally measured for such a patterned membrane, and taking into account the
284 patterning effect on the filtering area, is $76 \pm 13 \text{ L} \cdot \text{m}^{-2} \cdot \text{h}^{-1} \cdot \text{bar}^{-1}$. This is very close to the value measured for
285 the smooth membrane. However, it must be noted that the average thickness of the two membranes is

286 not exactly the same. An increase of 6.5 % was estimated for the patterned one (1.6 mm rather than 1.5
287 mm for the smooth one). This is discussed in the Supplementary Information (SI), section S3.

288 The results obtained in crossflow filtration tests are summarized in Figure 7. Based on the application of
289 Hermia blocking law analysis to dead end filtration data (see SI, Figures S3 and S4), two fouling regimes
290 could be discerned: pore blockage and cake filtration. The presence of integrated rings had no effect on
291 pore blockage but led to a significant mitigation of fouling in the cake filtration regime at the higher value
292 of crossflow velocity (Figure 7b). This is in good agreement with the numerical simulations and a mean
293 value of turbulent dissipation rate at the surface of the membrane between the rings being much larger
294 for the patterned membranes.

295



296 *Figure 7. Normalized permeate flux recorded in crossflow filtration tests with *P. aeruginosa* suspension as the feed*
297 *and using smooth and patterned membranes. (a) a crossflow velocity of $0.45 \text{ m}\cdot\text{s}^{-1}$; (b) and a crossflow velocity of*
298 *$0.68 \text{ m}\cdot\text{s}^{-1}$. Empty symbols correspond to the filtration stage where fouling is due to pore blocking while filled*
299 *symbols correspond to the cake filtration regime.*

301 **4.4. Considerations of scale**

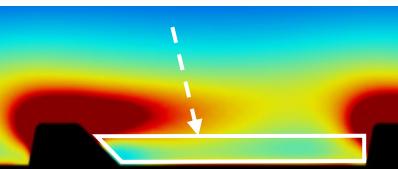
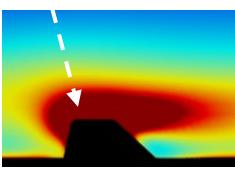
302 The fouling tests revealed a significant difference in roughness-induced mitigation of fouling between the
303 two studied crossflow velocities. For a crossflow velocity of $0.45 \text{ m}\cdot\text{s}^{-1}$, the smooth and patterned
304 membranes seem to be affected by fouling phenomena in a similar way. For both membrane types, the
305 permeate flux decreased by $\sim 22\%$ after 70 mL of permeate was collected. By contrast, significant
306 differences were observed in tests with the crossflow velocity of $0.68 \text{ m}\cdot\text{s}^{-1}$; in this case, whereas the
307 smooth membranes exhibit the same 22 % flux decrease, the flux decline was only 10 % in experiments
308 with the patterned filter. This result was very encouraging and provided the proof of concept of the
309 patterned membranes.

310 Near the membrane surface, we calculated the mean value of the dissipation rate of the turbulent kinetic
 311 energy in the zone between two rings ($\varepsilon_{mean_betw_rings}$, cf. Table 2). We compared this value to the
 312 maximum value of ε localized just above the rings ($\varepsilon_{max_above_rings}$) and in both zones, we observed that
 313 the dissipation rate of the turbulent kinetic energy (ε) is multiplied by a factor 3.5 when the velocity is
 314 increase from 0.45 and 0.68 $\text{m}\cdot\text{s}^{-1}$. $\varepsilon_{mean_betw_rings}$ is close to $3.2 \text{ m}^2\cdot\text{s}^{-3}$ for $v_{in} = 0.45 \text{ m}\cdot\text{s}^{-1}$ and $10.5 \text{ m}^2\cdot\text{s}^{-3}$
 315 for $v_{in} = 0.68 \text{ m}\cdot\text{s}^{-1}$, respectively (Table 2). Near the upper part of the rings, where the turbulence is the
 316 highest, $\varepsilon_{max_above_rings}$ is multiplied by a factor 5 when increasing the velocity (60 vs $300 \text{ m}^2\cdot\text{s}^{-3}$). The
 317 values of the Kolmogorov microscale, κ , are calculated using eq. (3) [29-31] and reported in Table 2.

$$\kappa = \left[\frac{\eta^3}{\varepsilon} \right]^{1/4} \quad (3)$$

318 Whatever the location (between the rings corresponding to the lowest values of ε , or near the upper part
 319 of the rings corresponding to the highest values of ε), κ increases 150 % with a decrease in the mean
 320 velocity from 0.68 to 0.45 $\text{m}\cdot\text{s}^{-1}$.

321 *Table 2. Kolmogorov microscale κ in low ε and high ε zones in the vicinity of the membrane surface for two values
 322 of the average crossflow velocity.*

Location along the membrane surface	Mean crossflow velocity, v_{in} ($\text{m}\cdot\text{s}^{-1}$)	Turbulent energy dissipation rate, ε ($\text{m}^2\cdot\text{s}^{-3}$)	Kolmogorov microscale, κ (μm)
Mean value between the rings $\varepsilon_{mean_betw_rings}$ 	0.45	3.2	23.6
	0.68	10.5	17.6
Local value above the ring $\varepsilon_{max_above_rings}$ 	0.45	60	11.4
	0.68	300	7.6

323
 324 Kolmogorov microscale corresponds to the lowest scale of turbulence where viscosity dominates and the
 325 turbulent kinetic energy is dissipated. So, κ is often a relevant hydrodynamic parameter, which could be
 326 linked to fouling mechanisms. As shown in Table 2, the values of κ are approximately two orders of
 327 magnitude smaller than characteristic dimensions of roughness features on the membrane surface where
 328 the size of the rings or the inter-ring distance are on the order of several millimeters (Figures 4b and 4c).
 329 We tentatively attribute the improvement in permeate flux (Figure 7b) to the disruption of the filter cake

330 growth at the scale on several microns (i. e. $\sim \kappa \mu\text{m}$). Even if the fouling mechanisms are complex and their
331 mitigation could be linked to several phenomena, the significant increase of the dissipation rate of the
332 turbulent kinetic energy and the associated decrease of the Kolmogorov microscale are in good agreement
333 with the fouling results reported in Figure 7.

334

335 **4.5. Potential of stereolithography for ceramic membrane design**

336 Through creating desired surface morphology at the mesoscale, additive manufacturing methods help
337 control flow to mitigate deposition of colloids and larger particle and, thereby, mitigate membrane fouling.
338 However, the methods impose limitations on the material properties of the membrane that supports such
339 surface features. First, small alumina particle size helps improving both the spatial resolution of the
340 stereolithography method and the mechanical properties of membranes post-sintering; however, the
341 smaller size of the primary particles leads to a low final pore size. The pore diameter of $\sim 0.2 \mu\text{m}$ reported
342 in this work is more than an order of magnitude smaller than the pore size achievable by extrusion of
343 pastes formulated from coarser and monodispersed powders. Addition of pore-forming agents in the
344 stereolithography formulation is thus recommended to increase the pore size and achieve a better balance
345 between resolution and permeability. Second, symmetrical patterned microfiltration membranes could be
346 used as a porous support for the production of patterned ultrafiltration or nanofiltration membranes by
347 deposition of successive thin layers by slip casting.

348 **5. Conclusions**

349 CFD simulations were successfully used for guiding the design of 3D-printed tubular single-channel ceramic
350 membranes and optimizing the surface morphology at the mesoscale in order to improve the
351 hydrodynamic control of membrane fouling. CFD predictions were corroborated by the experimental data
352 on membrane fouling. The mesoscale design of microfiltration membranes by additive manufacturing can
353 be combined with preparing the lower porosity separation layer by conventional methods of separation
354 layer. Such optimal combination of membrane fabrication methods may be practically implemented
355 through a multistep/multi-method morphological design as an alternative to changing the casting mixture
356 composition for pore size control.

357 **Acknowledgments**

358 We are grateful to Mr. Didier Cot and Dr. Martin Drobek (both at Institut Européen des Membranes) for
359 performing SEM and Hg porosimetry analyses, respectively. We also thank 3DCERAM SINTO (Limoges,
360 France) for the manufacturing the prototype membranes and providing them to our team. This material is
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363 State University.

364

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430

431 **Supplementary information**
432 **for the manuscript**

CFD-guided patterning of tubular ceramic membrane surface by stereolithography: Optimizing morphology at the mesoscale for improved hydrodynamic control of membrane fouling

436 Cyril Chevarin¹, Xunhao Wang², Denis Bouyer^{1*}, Volodymyr V. Tarabara^{2**}, Thierry Chartier³, André Ayral¹

⁴³⁷ *¹ Institut Européen des Membranes IEM – UMR 5635, ENSCM, CNRS, Univ Montpellier, Montpellier, France*

² Department of Civil and Environmental Engineering, Michigan State University, East Lansing, MI 48824, USA

³ CNRS, University of Limoges, Institute of Research for Ceramics (IRCCyN), UMR 7315, European Ceramics Center, Limoges, France

441
442 **S1. k - ε turbulence model**
443 To take into account turbulence effect, the standard k - ε turbulence model¹ as used. This model is robust,
444 accuracy and widely used for many flow applications.

445 In addition to the conservation of momentum equation in the Navier-Stokes equation (Eq. (1)), the
 446 standard k - ε turbulence model, which is a semi-empirical model, is based on two additional transport
 447 equations for the turbulent kinetic energy k and for the turbulent dissipation rate ε as follow:

448 For the turbulent kinetic energy k (in $\text{m}^2 \cdot \text{s}^{-2}$):

$$\rho(\vec{v} \cdot \nabla k) = \nabla \cdot \left(\left(\eta + \frac{\eta_t}{\sigma_k} \right) \nabla k \right) + P_k - \rho \epsilon \quad (\text{A1})$$

449 where P_k is the productive term of k due to the mean velocity gradients

$$P_k = \eta_t \left[\nabla \vec{v} : (\nabla \vec{v} + \nabla \vec{v}^T) - \frac{2}{3} (\nabla \cdot \vec{v})^2 \right] - \frac{2}{3} \rho k \nabla \cdot \vec{v} \quad (\text{A2})$$

451 And for the turbulent dissipation rate ε (in $\text{m}^2 \cdot \text{s}^{-3}$):

$$\rho(\vec{v} \cdot \nabla \varepsilon) = \nabla \cdot \left(\left(\eta + \frac{\eta_t}{\sigma_\varepsilon} \right) \nabla \varepsilon \right) + C_{\varepsilon 1} \frac{\varepsilon}{k} P_k - C_{\varepsilon 1} \rho \frac{\varepsilon^2}{k} \quad (\text{A3})$$

¹ B.E. Launder, D.B. Spalding, The numerical computation of turbulent flows, *Comput. Method. Appl. Mechanics Eng.*, 3 (1974) 269-289.

452 In this k- ε model, the turbulent viscosity η_t ((in $\text{m}^2\cdot\text{s}^{-2}$) was modeled by combining k and ε using the
453 equation:

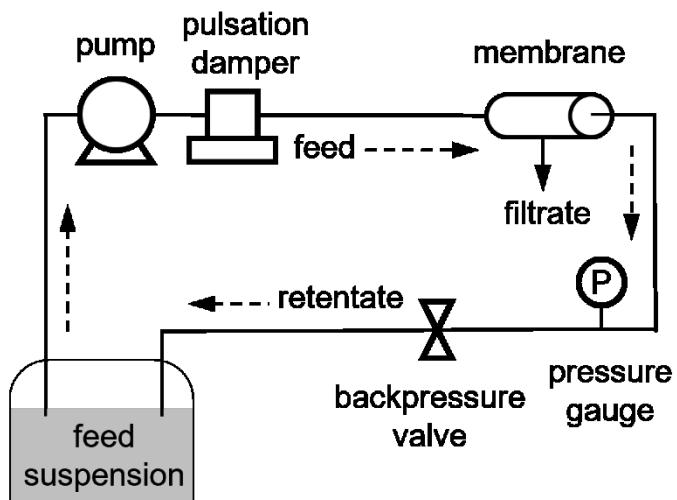
$$\eta_t = \rho C_\eta \frac{k^2}{\varepsilon} \quad (\text{A4})$$

454 The standard k- ε model constants $C_{\varepsilon 1}$, $C_{\varepsilon 2}$, C_η , σ_k and σ_ε were issued from experimental data and could
455 be adjusted. The default value of these constants are listed in Table S1.

456 *Table S1. Model constants.*

Constant	$C_{\varepsilon 1}$	$C_{\varepsilon 2}$	C_η	σ_k	σ_ε
Value	1.44	1.92	0.09	1.0	1.3

457
458 **S2. Preparation of bacteria stock**
459 To prepare the bacteria stock, one liter of PA01 (late exponential growth phase) with a final optical density
460 (600 nm) of 1 were washed twice with 150 mM NaCl, (centrifuged for 10 min at 8000 rpm and 4 °C and
461 resuspended by vortexing) and incubated in 4% formaldehyde solution for 2 h at room temperature to fix
462 the bacteria. The cells were then washed three times with 150 mM NaCl (centrifuged for 10 min at 8000
463 rpm and 4 °C, and resuspended by vortexing) [20]. The fixed bacteria stock (pH 6) was stored at 4 °C for
464 subsequent use.



465
466 *Figure S1. Schematic of the crossflow filtration setup. Dead-end filtration tests*
467 *were performed using the same system but with the retentate outlet closed.*

468

469 **S3. Comparison of water permeability values for smooth and patterned membranes**

470

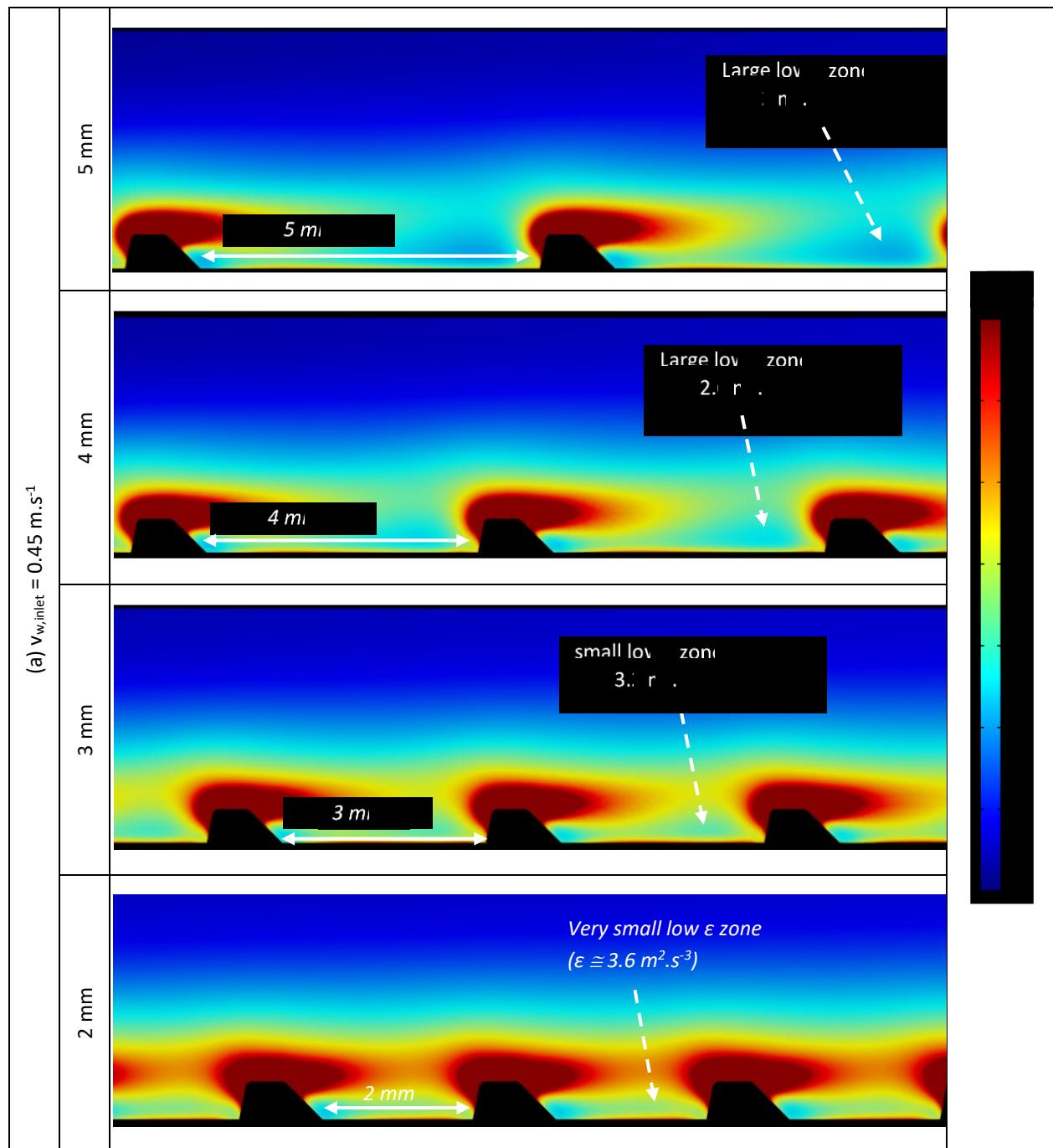
471 Because the thickness of the two types of membranes is not exactly the same (average thickness of 1.5
472 mm for the smooth ones versus 1.6 mm for the patterned ones), their measured water permeabilities
473 cannot be compared directly. Referring to the terminology used for gas permeation, the water
474 permeability corresponding to the water flux divided by the transmembrane pressure should rather be
475 named water permeance. Considering that such symmetric membranes are made with the same and
476 homogeneous membrane material, it is here recommended to rather compare the values of "coefficient
477 of permeability for water in the membrane material". It is equal to the water flux divided by the pressure
478 gradient across the membrane. It can thus be calculated by multiplying the water permeability by the
479 membrane thickness. The obtained values are as follows:

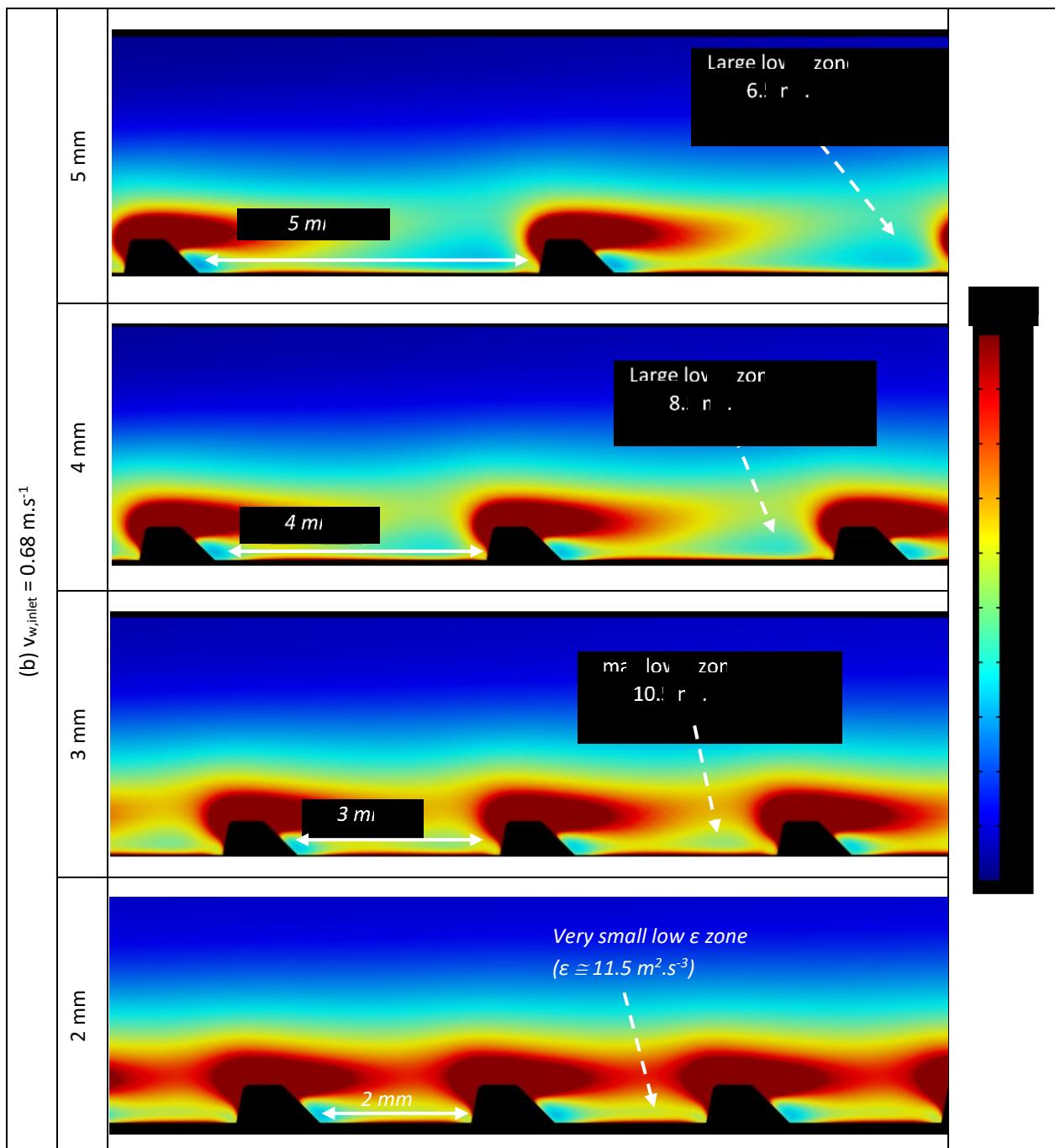
480 Value calculated from the microstructure data: $63 \pm 23 \text{ L.mm} \cdot \text{m}^{-2} \cdot \text{h}^{-1} \cdot \text{bar}^{-1}$

481 Value measured with a smooth membrane: $104 \pm 23 \text{ L.mm} \cdot \text{m}^{-2} \cdot \text{h}^{-1} \cdot \text{bar}^{-1}$

482 Value measured with a patterned membrane: $122 \pm 22 \text{ L.mm} \cdot \text{m}^{-2} \cdot \text{h}^{-1} \cdot \text{bar}^{-1}$

483



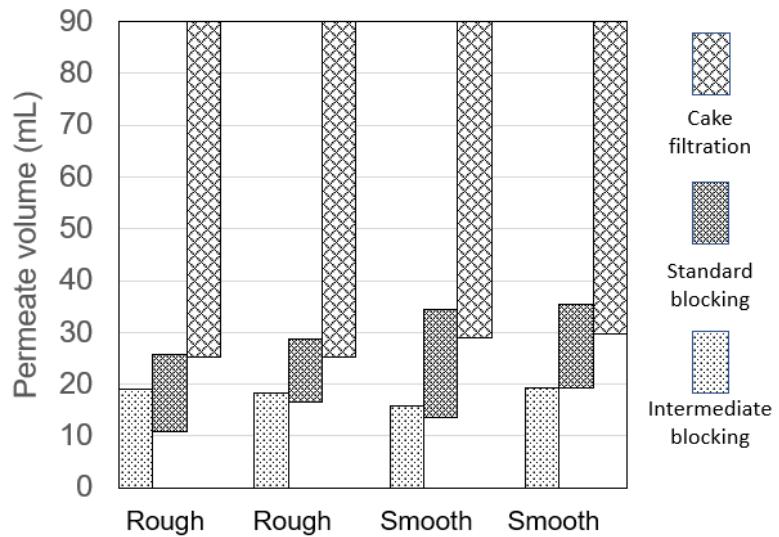


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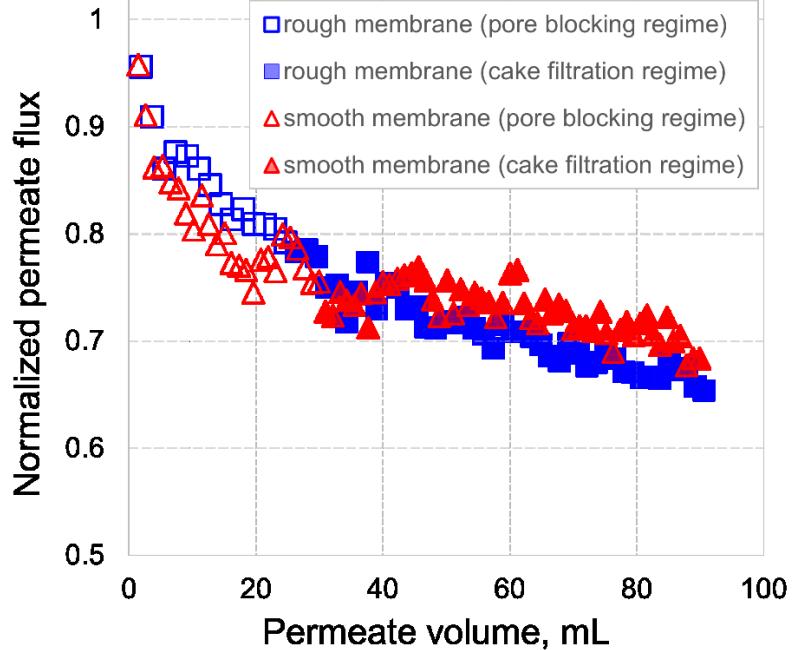
486 *Figure S2. Mapping of ϵ inside the tubular membrane for four different distances between the rings (2, 3, 4 and 5*

487 *mm) and the two explored values of v_{inlet} : (a) 0.45 m.s^{-1} ; (b) 0.68 m.s^{-1} .*

488



489
490 *Figure S3. Evolution of fouling mechanism during dead-end filtration*
491 *of bacterial suspensions by smooth and rough membranes.*



493
494 *Figure S4. Normalized permeate flux recorded in*
495 *dead-end filtration tests with smooth and rough membranes.*