

# <sup>1</sup> Seaduck: A python package for Eulerian and <sup>2</sup> Lagrangian interpolation on ocean datasets

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## Software

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## <sup>6</sup> Summary

<sup>7</sup> Numerical simulations of the Earth's oceans are becoming more realistic and sophisticated.  
<sup>8</sup> Their complex layout and shear volume make it difficult for researchers to access and understand  
<sup>9</sup> these data, however. Additionally, most ocean models, mostly finite-volume models, compute  
<sup>10</sup> and calculate spatially-integrated properties, such as grid-cell averaged temperature or wall-  
<sup>11</sup> integrated mass flux. On the other hand, in-situ oceanographic observations are effectively  
<sup>12</sup> collected at points in space and time. This fundamental difference makes the comparison  
<sup>13</sup> between observations and results from numerical simulation difficult.

<sup>14</sup> In this work, we present `seaduck`, a Python package that can perform both Eulerian and  
<sup>15</sup> Lagrangian interpolation on generic ocean datasets with good performance and scalability. This  
<sup>16</sup> package accesses numerical datasets from the perspective of space-time points. It automatically  
<sup>17</sup> navigates complex dataset layouts (grid topologies) and transforms discrete information to  
<sup>18</sup> continuous fields. The values and derivatives of those fields can be accessed at any point in  
<sup>19</sup> the domain defined by the user. Similar to fixed and drifting observational oceanographic  
<sup>20</sup> instrument platforms, the points can be either stationary (Eulerian) or advected by the flow  
<sup>21</sup> (Lagrangian).

## <sup>22</sup> Statement of need

<sup>23</sup> The `seaduck` package is different from other ocean analytical tools (e.g., `oceanspy` [Almansi et  
<sup>24</sup> al. (2019)]) because it accesses the circulation model data from the perspective of an arbitrary  
<sup>25</sup> space-time point. Users define the points of interest using longitude, latitude, depth, and time.  
<sup>26</sup> The package then reads necessary information from nearby model grid points and constructs  
<sup>27</sup> the continuous (scalar or vector) field around the points. The index lookup and space-time  
<sup>28</sup> interpolation involved in this process is done efficiently with `scipy.spatial.cKDtree` [Virtanen  
<sup>29</sup> et al. (2020)] and `numba` [Lam et al. (2015)] compiled code, respectively. As the points can  
<sup>30</sup> be defined arbitrarily in the model domain, accessing discrete numerical output feels to the  
<sup>31</sup> user like retrieving values from a continuous field, despite the complex model grid.

<sup>32</sup> The points can be stationary (fixed in space, or Eulerian) or be advected by a vector velocity  
<sup>33</sup> field (Lagrangian). Most Lagrangian particle packages (e.g., `Forget` (2021)) compute particle  
<sup>34</sup> trajectories by solving the initial value problem numerically. Instead, `seaduck` uses efficient,  
<sup>35</sup> accurate, mass-conserving analytic formulae, which assumes a step-wise steady velocity field  
<sup>36</sup> similar to that used by `TRACMASS` [Campino et al. (2020)]. The Lagrangian advection  
<sup>37</sup> code is largely `numba` compiled, and the total amount of computation is less than solving the  
<sup>38</sup> problem numerically. The Lagrangian particle functionality is based on the above-mentioned  
<sup>39</sup> interpolation utilities, thus, it automatically navigates the complex topology of numerical ocean  
<sup>40</sup> models.

41 Seaduck provides highly-customizable interpolation methods for both Eulerian and Lagrangian  
42 points. Users can control all the properties of a hierarchy of kernels, including: (1) The shape  
43 of the interpolation kernel(s) in both spatial and temporal dimensions, which defines which  
44 neighboring points are used, and therefore how the continuous field is estimated. (2) The  
45 interpolation weight function, which allows users to calculate generic linear operations on the  
46 data, such as differentiation and smoothing, in all four dimensions. The hierarchy of kernels  
47 controls behaviour near land-masked points. Specifically, the hierarchy consists of successively  
48 more compact kernels that are used depending on the proximity of land points.

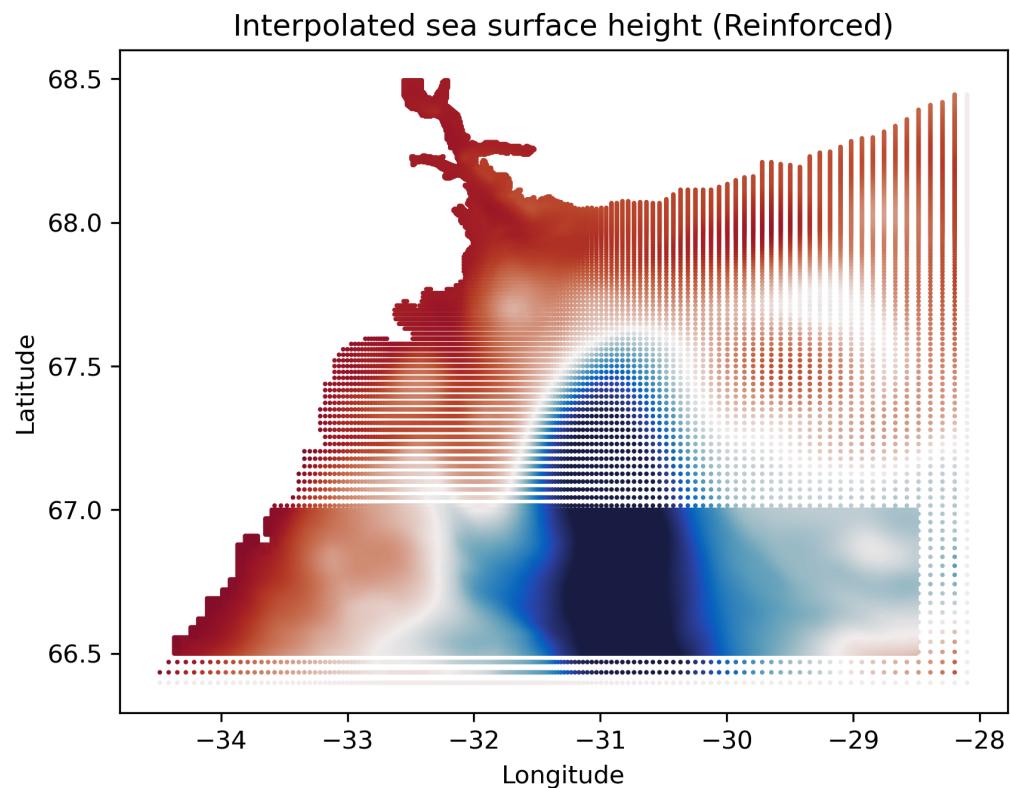
49 With the above functionality, seaduck can accomplish many common tasks in ocean model  
50 data analysis, including interpolation, regridding, and Lagrangian particle simulation. Less  
51 common tasks are also possible, such as interpolation in Lagrangian label space, and analysis  
52 of tracer budgets along Lagrangian trajectories. We also strive to make seaduck an accessible  
53 education tool by creating a very simple high-level default interface, which is intended for  
54 people with little programming background, and for people who want to quickly try the tool.

## 55 Usage Examples

56 While some usage examples are presented here, many more can be found in the docu-  
57 mentation for seaduck (<https://macekualv.github.io/seaduck/>). The notebooks of the  
58 following examples run on SciServer ([Taghizadeh-Popp et al., 2020](#)), an openly available  
59 cloud compute resource for scientific data analysis. A supplementary GitHub repository  
60 ([https://github.com/MaceKualv/seaduck\\_sciserver\\_notebook](https://github.com/MaceKualv/seaduck_sciserver_notebook)) holds all SciServer notebooks,  
61 and is being continuously maintained.

### 62 Interpolation / regridding

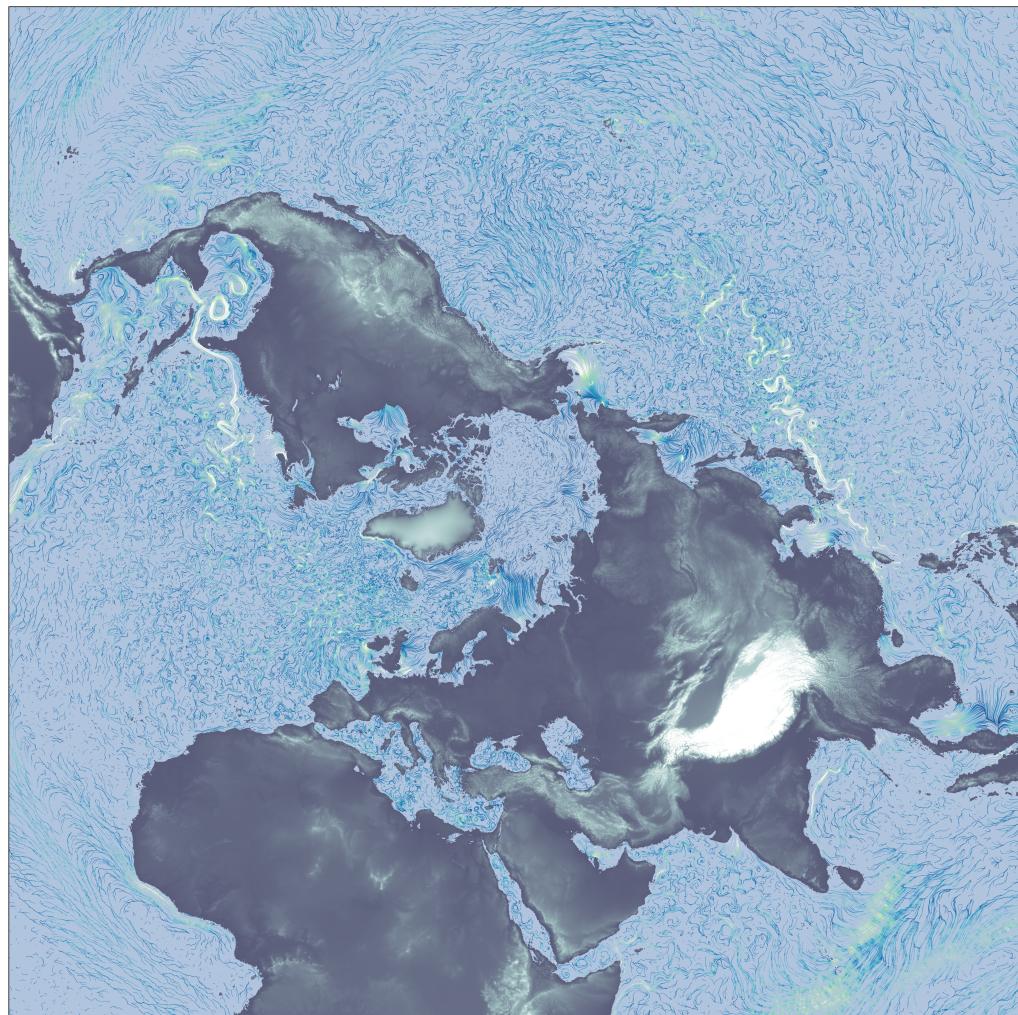
63 As an example of seaduck's interpolation/regridding functionality, consider a realistic simulation  
64 of the Kangerdlugssuaq Fjord, which is in east Greenland ([Fraser et al., 2018](#)). This is an  
65 MITgcm ([Marshall et al., 1997](#)) simulation with uneven grid spacing such that grid cells within  
66 the fjord are much more densely packed than elsewhere. The goal is to interpolate, and hence  
67 regrid, the sea surface height field,  $\eta$ , to a uniform grid spacing in the southern part of the  
68 domain. In Fig. 1, the coherent patch between 66.5 N and 67 N is a very dense scatter plot  
69 of the interpolated value where neighboring points are connected together. The rest of this  
70 plot is scatter plot of model output at center grid points. The close agreement between the  
71 interpolated and output value can be clearly seen in Fig. 1. The interpolation also remains  
72 smooth near strong gradient and land boundaries.



**Figure 1:** Fig.1 Scatterplot with colors showing the sea surface height value near Kangerdlugssuaq Fjord defined in the model and interpolated by seaduck.

### 73     **Global particle simulation on LLC4320**

74     In this example, a stationary, surface slice of the LLC4320 (Rocha et al., 2016) simulation  
 75     is used. LLC4320 is a kilometer-scale model of the global ocean circulation with complex  
 76     topology. 150,000 Lagrangian particles are released randomly and evenly on the globe, and  
 77     seaduck computes their trajectories for 30 days. Fig. 2 shows the particle trajectories for  
 78     the northern hemisphere, which contains around  $10^8$  velocity points. The colors denote the  
 79     current speed. This simulation takes about an hour to run on SciServer (Taghizadeh-Popp et  
 80     al., 2020).



**Figure 2:** Fig 2. Streaklines of particle advected by stationary 2D slice of the LLC4320 simulation. Colors denote the current speed.

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