

High-statistics measurement of antineutrino quasielasticlike scattering at $E_{\bar{\nu}}$ 6 GeV on a hydrocarbon target

A. Bashyal^{1,*}, S. Akhter,² Z. Ahmad Dar,^{3,2} F. Akbar,² V. Ansari,² M. V. Ascencio,^{4,†} M. Sajjad Athar,² A. Bercellie,⁵ M. Betancourt,⁶ A. Bodek,⁵ J. L. Bonilla,⁷ A. Bravar,⁸ H. Budd,⁵ G. Caceres,^{9,‡} T. Cai,^{10,§} M. F. Carneiro,^{1,9,§} G. A. Díaz,⁵ J. Felix,⁷ L. Fields,¹¹ A. Filkins,^{3,||} R. Fine,^{5,¶} A. M. Gago,⁴ H. Gallagher,¹² P. K. Gaur,² S. M. Gilligan,¹ R. Gran,¹³ E. Granados,⁷ D. A. Harris,^{10,6} S. Henry,⁵ D. Jena,⁶ S. Jena,¹⁴ J. Kleykamp,^{5,***} A. Klustová,¹⁵ M. Kordosky,³ D. Last,¹⁶ T. Le,^{12,17} A. Lozano,⁹ X.-G. Lu,^{18,19} E. Maher,²⁰ S. Manly,⁵ W. A. Mann,¹² C. Mauger,¹⁶ K. S. McFarland,⁵ A. M. McGowan,⁵ B. Messerly,^{21,††} J. Miller,²² O. Moreno,^{3,7} J. G. Morffin,⁶ D. Naples,²¹ J. K. Nelson,³ C. Nguyen,²³ A. Olivier,⁵ V. Paolone,²¹ G. N. Perdue,^{6,5} K.-J. Plows,¹⁹ M. A. Ramírez,^{16,7} R. D. Ransome,¹⁷ H. Ray,²³ D. Ruterborries,⁵ H. Schellman,¹ C. J. Solano Salinas,²⁴ H. Su,²¹ M. Sultana,⁵ V. S. Syrotenko,¹² E. Valencia,^{3,7} N. H. Vaughan,¹ A. V. Waldron,^{25,15} C. Wret,⁵ B. Yaeggy,³ and L. Zazueta³

(MINER ν A Collaboration)

¹Department of Physics, Oregon State University, Corvallis, Oregon 97331, USA

²Department of Physics, Aligarh Muslim University, Aligarh,
Uttar Pradesh 202002, India

³Department of Physics, William & Mary, Williamsburg, Virginia 23187, USA

⁴Sección Física, Departamento de Ciencias, Pontificia Universidad Católica del Perú,
Apartado 1761, Lima, Perú

⁵Department of Physics and Astronomy, University of Rochester,
Rochester, New York 14627 USA

⁶Fermi National Accelerator Laboratory, Batavia, Illinois 60510, USA

⁷Campus León y Campus Guanajuato, Universidad de Guanajuato,
Lascurain de Retana No. 5, Colonia Centro, Guanajuato 36000, Guanajuato México

⁸University of Geneva, 1211 Geneva 4, Switzerland

⁹Centro Brasileiro de Pesquisas Físicas, Rua Dr. Xavier Sigaud 150, Urca,
Rio de Janeiro, Rio de Janeiro, 22290-180, Brazil

¹⁰York University, Department of Physics and Astronomy, Toronto, Ontario M3J 1P3, Canada

¹¹Department of Physics, University of Notre Dame, Notre Dame, Indiana 46556, USA

¹²Physics Department, Tufts University, Medford, Massachusetts 02155, USA

¹³Department of Physics, University of Minnesota—Duluth,
Duluth, Minnesota 55812, USA

¹⁴Department of Physical Sciences, IISER Mohali, Knowledge City, SAS Nagar,
Mohali 140306, Punjab, India

¹⁵The Blackett Laboratory, Imperial College London, London SW7 2BW,
United Kingdom

¹⁶Department of Physics and Astronomy, University of Pennsylvania,
Philadelphia, Pennsylvania 19104, USA

¹⁷Rutgers, The State University of New Jersey, Piscataway, New Jersey 08854, USA

¹⁸Department of Physics, University of Warwick, Coventry CV4 7AL,
United Kingdom

¹⁹Oxford University, Department of Physics, Oxford OX1 3PJ, United Kingdom

²⁰Massachusetts College of Liberal Arts, 375 Church Street, North Adams,
Massachusetts 01247, USA

²¹Department of Physics and Astronomy, University of Pittsburgh,
Pittsburgh, Pennsylvania 15260, USA

²²Departamento de Física, Universidad Técnica Federico Santa María,
Avenida España 1680 Casilla 110-V, Valparaíso, Chile

²³University of Florida, Department of Physics, Gainesville, Florida 32611, USA

²⁴Facultad de Ciencias, Universidad Nacional de Ingeniería,
Apartado 31139, Lima, Perú

²⁵*G. O. Jones Building, Queen Mary University of London,
327 Mile End Road, London E1 4NS, United Kingdom*



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We present measurements of the cross section for antineutrino charged-current quasielasticlike scattering on hydrocarbon using the medium energy NuMI wide-band neutrino beam peaking at antineutrino energy $\langle E_{\bar{\nu}} \rangle \sim 6$ GeV. The measurements are presented as a function of the longitudinal momentum ($p_{||}$) and transverse momentum (p_T) of the final state muon. This work complements our previously reported high statistics measurement in the neutrino channel and extends the previous antineutrino measurement made in a low energy beam at $\langle E_{\bar{\nu}} \rangle \sim 3.5$ GeV out to p_T of 2.5 GeV/c. Current theoretical models do not completely describe the data in this previously unexplored high p_T region. The single differential cross section as a function of four-momentum transfer (Q_{QE}^2) now extends to 4 GeV² with high statistics. The cross section as a function of Q_{QE}^2 shows that the tuned simulations developed by the MINERvA Collaboration that agreed well with the low energy beam measurements do not agree as well with the medium energy beam measurements. Newer neutrino interaction models such as the GENIE v3 tunes are better able to simulate the high Q_{QE}^2 region.

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I. INTRODUCTION

Recent results from the neutrino oscillation experiments, NOvA [1] and T2K [2], hint that charge-parity (CP) symmetry is violated in the lepton sector and favors a normal mass ordering of neutrino mass states. Precise determination of the PMNS [3] CP violating parameter (δ_{CP}) requires new measurements with larger statistics and significantly smaller systematic uncertainties. The DUNE [4] and HyperK [5] experiments aim to measure $\delta_{CP} \neq 0$ with greater than 5σ sensitivity at maximal δ_{CP} , which require that less than 2% of interaction rate uncertainties come from cross-section models [4]. This 2% uncertainty can be achieved with improved cross-section measurements. The data presented here overlap the energy range of

the DUNE experiment, although on a hydrocarbon target instead of argon.

We present results on the charge-current quasielastic (CCQE) process, $\bar{\nu}_\mu p \rightarrow \mu^+ n$, which is a significant component of the charged-current interactions rate [6] in the few GeV energy range. To achieve high fiducial mass, present and future neutrino experiments employ detectors made of heavier nuclei (argon in the case of DUNE and water in the case of HyperK) where nuclear processes and final state interactions (FSI) will affect the interpretation of CCQE interactions. As the primary neutrino interaction occurs within a nucleus, the pure CCQE process itself is not experimentally accessible. We instead use a CCQE-like signal definition (charged-current event with no pions in the final state) based on the event topology observable outside the nucleus. Our CCQE-like definition is similar to the CC0 π definition used by other experiments [7–9]. The advantage of concentrating on CCQE-like processes is that, as a two-body process, the full kinematics of the interaction are approximately determined from the outgoing charged lepton kinematics alone. This provides an estimate of the incoming neutrino energy, as needed for oscillation measurements, and can be applied in a consistent fashion to both neutrino and antineutrino interactions, despite final state differences.

This work improves upon our previous measurement in the antineutrino channel [10] by utilizing 20 \times more statistics, improved background subtraction methods, and access to an extended kinematic region due to the higher energy beam. It complements our previous muon-neutrino cross-section measurement at similar beam energy [11]. We first present the double differential cross section as a function of muon momenta (p_T and $p_{||}$) as it is largely model independent and allows stringent tests of interaction

^{*} Also at High Energy Physics Department, Argonne National Lab, 9700 S Cass Ave, Lemont, Illinois 60439, USA.

[†] Also at Iowa State University, Ames, Iowa 50011, USA.

[‡] Also at Department of Physics and Astronomy, University of California at Davis, Davis, California 95616, USA.

[§] Also at Brookhaven National Laboratory, Upton, New York 11973-5000, USA.

^{||} Also at Syracuse University, Syracuse, New York 13244, USA.

[¶] Also at Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA.

^{**} Also at Department of Physics and Astronomy, University of Mississippi, Oxford, Mississippi 38677, USA.

^{††} Also at University of Minnesota, Minneapolis, Minnesota 55455, USA.

models. We also present cross-section measurements as a function of the estimated four-momentum-transfer squared variable, Q_{QE}^2 , using the CCQE hypothesis. Assuming the nucleus is at rest, the Q_{QE}^2 is given as

$$Q_{QE}^2 = 2E_{\bar{\nu}}^{(QE)}(E_\mu - p_\mu \cos \theta_\mu) - m_\mu^2, \quad (1)$$

where $E_{\bar{\nu}}^{(QE)}$ (neutrino energy based on CCQE hypothesis) is given as

$$E_{\bar{\nu}}^{(QE)} = \frac{m_n^2 - (m_p - E_b)^2 - m_\mu^2 + 2(m_p - E_b)E_\mu}{2(m_p - E_b - E_\mu + p_\mu \cos \theta_\mu)}. \quad (2)$$

To provide a useful comparison with global neutrino energy cross sections, we also present the total antineutrino CCQE-like cross section $\sigma(E_{\bar{\nu}})$ corrected from $E_{\bar{\nu}}^{(QE)}$ to the $E_{\bar{\nu}}$ (true neutrino energy). The correction from the observable $E_{\bar{\nu}}^{(QE)}$ to $E_{\bar{\nu}}$ is sensitive to nuclear effects and introduces additional model uncertainties. The cross section as a function of $E_{\bar{\nu}}$ is then the corrected number of events as a function of $E_{\bar{\nu}}$ normalized by the flux. Since the correction is generated using the simulation, the correction from $E_{\bar{\nu}}^{(QE)}$ to $E_{\bar{\nu}}$ introduces model dependencies.

II. THE MINERvA EXPERIMENT

The MINERvA experiment was located on-axis in the NuMI neutrino beam [12], which serves as the neutrino source. In the NuMI beamline, a 120 GeV proton beam impinges on a 1.2 meter long target to produce pions and kaons. Negatively charged mesons are then focused by two magnetic horns. The focused beam decays within a 675 meter long decay pipe to produce leptons and antineutrinos. Data were taken between June 2016 and February 2019.

The MINERvA detector consisted of planes of scintillating strips interleaved with nuclear targets, a central tracker region consisting only of scintillator, an electromagnetic calorimeter formed by adding lead planes, and a hadronic calorimeter formed from iron plates. Muon charge and momentum measurements were provided for muons with momenta above ~ 1.5 GeV/c by the MINOS near detector [13], which was located directly behind the MINERvA detector. The data presented here are from the central tracking region of MINERvA which consisted of 108 tracking planes of scintillator composed of 88.5% carbon, 8.2% hydrogen, and 2.5% oxygen. The tracker could reconstruct charged tracks with a kinetic energy (T_p) threshold of ~ 120 MeV for protons.

III. EVENT SELECTION

A. Experimental selection

The definition of CCQE-like process is given in our previous lower energy (LE) results [10]. Reconstructed

antineutrino candidates are required to have one positively charged muon, no other reconstructed charged tracks ($N_{\text{extra}} = 0$), and small recoil energy. This is intended to select the classic CCQE signature $\bar{\nu}_\mu + p \rightarrow \mu^+ + n$ where the neutron deposits little energy in our detector. CCQE-like candidate events are further defined by limits on the recoil energy deposited by the outgoing hadrons. Reconstructed nonmuon recoil energy outside a 100 mm radius around the neutrino interaction vertex is required to be less than a value that varies with Q_{QE}^2 and is similar to that of the low energy analysis [10] but has been loosened by 50 MeV due to increased instrumental backgrounds in the higher intensity medium energy beam. The final state muon is required to enter the downstream, magnetized MINOS near detector for charge determination and full momentum reconstruction. To match the forward MINOS acceptance, and assure that the muon charge is positive in the presence of neutrinos in the antineutrino beam, we require that the reconstructed $\theta_\mu < 20^\circ$ and that the muon have positive charge and p_{\parallel} between 1.5 and 15 GeV/c.

B. Signal definition

To match our detection capabilities, the CCQE-like process is defined at generator level by requiring a final state with a μ^+ with polar angle $\theta_\mu < 20^\circ$ with respect to the beam and p_{\parallel} in the range 1.5 to 15 GeV/c, no final state protons with kinetic energy T_p above the proton reconstruction threshold (120 MeV), and no mesons or heavier baryons. Interactions that include nuclear excitation photons below 10 MeV are allowed. The proton energy requirement is motivated by the requirement that there be no additional charged tracks in the interaction. For $T_p \geq 120$ MeV, the efficiency for reconstructing a proton as an additional track rises quickly, making the efficiency of the $N_{\text{extra}} = 0$ selection difficult to model. As a result, we report our results for the restricted kinematic regions where we understand our efficiency the best. The reconstruction efficiency as a function of maximum kinetic energy of final state protons is provided in the Supplemental Material to show the effect of this threshold [14].

This CCQE-like definition is designed to exclude non-elastic interactions such as resonances ($\bar{\nu}_\mu + N \rightarrow \mu^+ + \Delta$) and deep-inelastic scattering (DIS, neutrino scattering off of quarks inside the nucleons), but does include interactions with multinucleon initial states such as 2p2h [15] and any resonant events where additional pions and nucleons are absorbed in the nucleus.

In the CCQE two-body kinematic hypothesis, the initial nucleon is assumed to be at rest with a binding energy of 30 MeV in carbon. This allows an estimate of the antineutrino energy $E_{\bar{\nu}}^{(QE)}$ and momentum transfer squared Q_{QE}^2 from the muon kinematics alone [10].

IV. SIMULATION

Antineutrino interactions are simulated using the GENIE 2.12.6 event generator [16]. This implementation of GENIE uses the relativistic Fermi gas model [17] with short range correlations included via a Bodek-Ritchie tail [18]. Multinucleon events using the Valencia model [19–21] are included. The default GENIE model is referred to as GENIE 2.12.6 in subsequent figures. The simulation used for cross-section extraction is the MINERvA Tune-v1 tune described in [11]. This simulation has been tuned to match previous MINERvA data in the neutrino channel and is found to be consistent with our previous LE antineutrino measurement [10]. This tune includes

- (i) Modification of nonresonant pion production rates based on a combined reanalysis of the Argonne National Laboratory (ANL) [22,23] and Brookhaven National Laboratory (BNL) [24] bubble chamber data [25]. This modification reduces the nonresonant pion production by 57%. This modification has a negligible effect (< 1%) in this analysis and is referred to as $(\pi$ tune) in Table II but not shown separately in the figures.
- (ii) A further empirical enhancement of the Valencia model based on [26] which increases the integrated multinucleon (2p2h) event rate by 49%. This is referred to as “Low Recoil Tune” in the figures.
- (iii) Long range correlations modeled by the random phase approximation correction based on [27] and implemented for MINERvA in [28]. This is referred to as RPA in the figures.

There is an additional suppression of pion production at low Q^2 to decrease an observed tension between data and simulation in previous experiments [29,30] using an *ad hoc* fit [31]. The addition of this tune makes MINERvA Tune-v2.

The GENIE 2.12.6 model used as a basis for our full detector simulation does not include the $\Delta S = -1$ hyperon production processes [32] $\bar{\nu}_\mu + n \rightarrow \mu^+ + Y$ that contribute only in antineutrino scattering. These processes can contribute up to 6%–8% to the total antineutrino scattering cross section. However, a generator level study using a more recent version of GENIE (v3.0.6) [33] that does include these processes indicates that almost all hyperon production results in either detectable tracks or significant energy deposition that are vetoed by the multiplicity and recoil selections used to define the CCQE-like signal and data samples. Any residual hyperon processes are estimated to contribute ~1% to the final CCQE-like data sample.

A GEANT4 [34] based full detector simulation models the response of the detector [35]. The simulation is tuned to match test beam data [35] and overlaid with random detector readouts to reproduce rate dependent backgrounds. Background contributions from non-CCQE-like processes are then estimated by fitting the reconstructed recoil distribution between 100 and 500 MeV before recoil

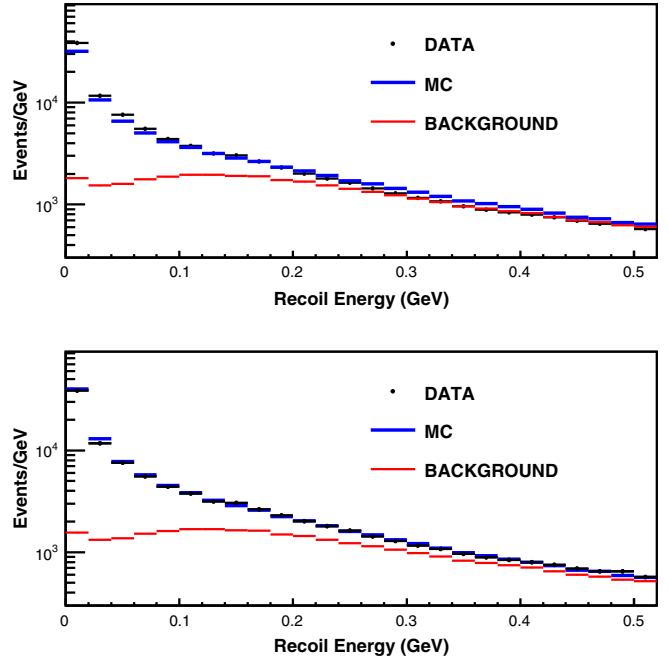


FIG. 1. The recoil energy distribution in the bin of $p_T = 0.25$ – 0.4 GeV/c, $p_{\parallel} = 1.5$ – 5 GeV/c. The top figure shows the data compared to default simulation. The bottom figure shows the contributions of simulated signal and background after their relative contributions have been constrained to the data in the region above 100 MeV. The χ^2 of this fit is 16 for 19 degrees of freedom.

selection to simulated signal and background samples in 14 p_T , p_{\parallel} bins. Figure 1 illustrates one of the fits for a typical p_T , p_{\parallel} bin.

The signal selection efficiency is estimated to be $\sim 70\%$ and the selected sample is 70%–80% pure, with the purity falling at higher Q^2 .

V. CROSS SECTION EXTRACTION

A total of $635,592 \pm 1,251(\text{stat}) \pm 13,850(\text{syst})$ events are selected after background subtraction compared to 14,839 events in the LE sample [10]. The background subtracted sample is unfolded to the true kinematic variables using an iterative Bayesian unfolding based on the RooUnfold algorithms [36,37]. To determine the number of iterations required to unfold the sample into true kinematics variables, various model predictions were used as fake data to unfold using the MINERvA Tune v1. Based on the unfolding studies, 4 and 8 iterations were determined as the optimum number of iterations to unfold the sample into true (p_T, p_{\parallel}) and $(E_{\bar{\nu}}^{(QE)}, Q_{QE}^2)$ variables, respectively [38]. One dimensional cross sections as a function of Q_{QE}^2 and $E_{\bar{\nu}}^{(QE)}$ are projected from the two dimensional $(E_{\bar{\nu}}^{(QE)}, Q_{QE}^2)$ cross section. The sample is then corrected for geometric efficiency and normalized by the total number of protons

on target (1.12×10^{21}) and the total number of nucleons in the fiducial volume of the detector (3.23×10^{30} nucleons). The total antineutrino flux integrated from 0 to 120 GeV is used to obtain the differential cross sections.

To extract the $E_{\bar{\nu}}$ cross section presented in Sec. VII D, the $(E_{\bar{\nu}}^{(QE)}, Q_{QE}^2)$ cross section is corrected to a true $(E_{\bar{\nu}}, Q_{QE}^2)$ cross section and projected into the $E_{\bar{\nu}}$ phase space. The neutrino flux is estimated both from simulation and from studies of multiple antineutrino processes and is parametrized as a function of true $E_{\bar{\nu}}$. The cross section as a function of $E_{\bar{\nu}}$ is then the corrected number of events observed as a function of $E_{\bar{\nu}}$, corrected by the flux. $E_{\bar{\nu}}^{(QE)}$ is a more robust observable defined solely from muon kinematics but generally offset from the true $E_{\bar{\nu}}$. Determination of the transformation from the observable $E_{\bar{\nu}}^{(QE)}$ to the true $E_{\bar{\nu}}$ requires simulation and hence introduces additional model dependencies as illustrated in Fig. 14.

To illustrate the effect of the T_p and θ_μ selections in our signal definition, we also provide the full cross section as a function of true antineutrino energy corrected for the T_p and θ_μ restrictions. As this additional correction has more model uncertainty, the result has significantly larger uncertainties.

VI. UNCERTAINTIES

Summaries of the uncertainties on the double differential cross section in Fig. 2 are shown in Fig. 6. Three major factors influence the uncertainties on this measurement.

First, the incoming neutrino flux has uncertainties in both overall normalization and energy dependence. The antineutrino flux is modeled using a GEANT4-based simulation of the target material and focusing systems. Focusing uncertainties are estimated by generating alternate fluxes where the focusing components of the beamline are shifted by $\pm 1\sigma$ from their nominal positions. Hadron production in the simulation is modified to match thin target datasets following the method of [39] that uses thin target data from the NA49 experiment [40] and the Barton datasets [41]. Recent constraints from $\nu + e$ [42], $\bar{\nu} + e$ scattering [43] and inverse muon decay [44] measurements in MINERvA reduce the overall flux uncertainty from $\sim 8\%$ to $\sim 5\%$.

Second, substantial uncertainties related to recoil and muon reconstruction dominate the overall uncertainty budget and are estimated by varying the muon energy scale and angle, their resolutions, and the neutron interaction cross section. As described in [45] the muon energy scale is corrected by 3.6% from its nominal value to resolve

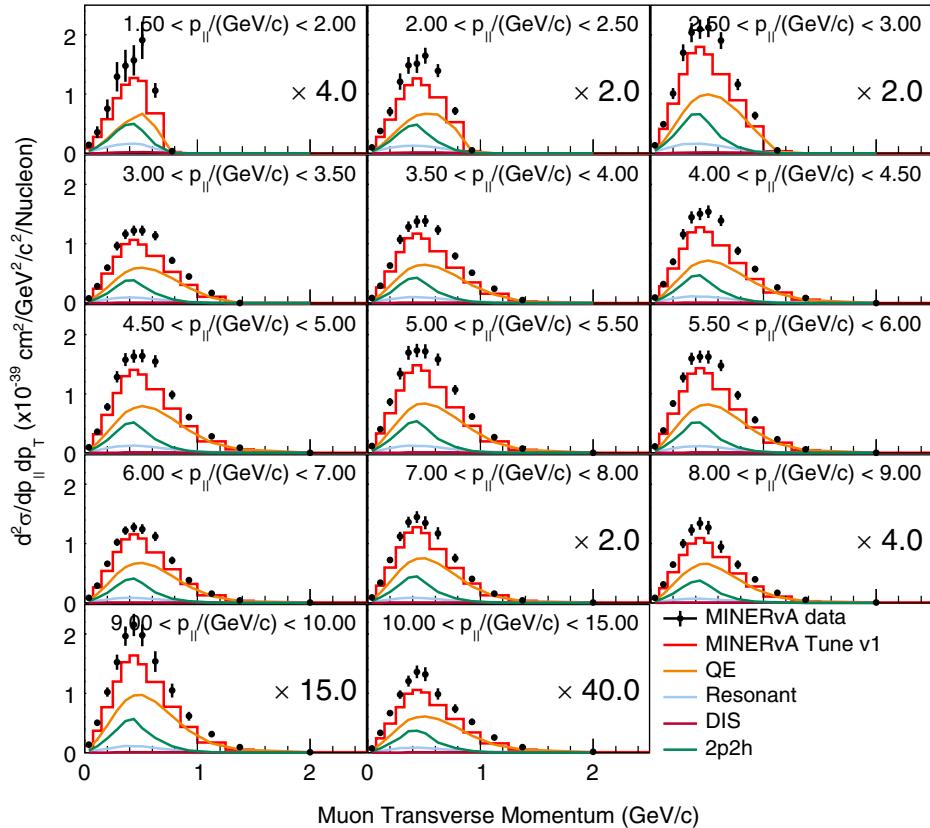


FIG. 2. The double differential CCQE-like antineutrino cross section as a function of muon p_T in bins of p_{\parallel} . The black markers are the measured cross section and the solid lines are the model predictions of MINERvA Tune v1 and its individual components. The multipliers on the panels are the scale factors used to scale the histograms.

TABLE I. Effect of input uncertainties on the cross section extraction for $d\sigma/dQ_{QE}^2$. Uncertainties which have significant effect on final cross section are listed. The $\pm 1\sigma$ is the shift of model parameters from their central values (CV).

Quantity	Variation ($\pm 1\sigma$ from CV)	Effect on cross section (%)
Angle reconstruction	± 1 mr	0–2
MINOS muon energy scale	± 1.0 %	2–6
GEANT neutron	± 10 %	2–5
Flux	Focusing/interaction parameters	5
GENIE cross-section models	GENIE cross-section parameters	1–5
GENIE 2p2h	Low recoil fit parameters	1–3
Final state interaction model	GENIE FSI models parameters	1–3

a discrepancy between data and the simulation. Correlations between neutrino flux parameters and muon energy scale, which result from that simultaneous fit to the energy scale and flux parameters, are accounted for when assessing the muon energy uncertainty. As seen in Fig. 11 the resulting uncertainties due to muon reconstruction rise to 9% at high Q_{QE}^2 .

Uncertainties in the energy loss and detection efficiency of final-state hadrons in the MINERvA detector also introduce uncertainties in the reconstruction of the recoil energy and are estimated by simulating the effects of differing hadronic interaction cross sections in the detector. The recoil response uncertainty contribution to the cross section is dominated by the model of neutron interactions and ranges from 1% at low Q_{QE}^2 to 4% at high Q_{QE}^2 .

Finally, the cross-section extraction depends on proper simulation of neutrino interactions including final state processes, which are estimated by varying input parameters to the event simulations. FSI effects contribute less than 2%–3% to the final Q_{QE}^2 cross-section uncertainty while GENIE cross-section model parameters (such as the axial mass, random phase approximation, and resonance production) contribute from 1% at low Q_{QE}^2 to 6% at high Q_{QE}^2 . For the cross section as a function of $E_{\bar{\nu}}$, model uncertainties in converting from $E_{\bar{\nu}}^{(QE)}$ to $E_{\bar{\nu}}$ increase the GENIE and FSI contributions to the uncertainty budget to 4%–6% each.

Uncertainties are propagated through the “universe” method developed by the MINERvA Collaboration and described in Ref. [46]. For each observable, separate histograms (“universes”) of the simulated reconstructed variable are stored for each of the several hundred sources of systematic uncertainty. For example, the reconstructed muon angle is replicated with $\pm 1\sigma$ offsets in two directions transverse to the beam and several GENIE parameters are similarly varied. The full analysis chain is applied to each universe independently. For the flux systematics which depend upon various beamline parameters, 500 universes are simulated where each universe is drawn from a distribution of focusing parameters that takes into account their uncertainties and their correlations. These beam parameters and their 1σ values are listed in [45]. The total systematic uncertainty and covariance for any observable

are then estimated by summing the deviations of the modified universes from the central values provided by the simulation in quadrature [39]. Table I summarizes the significant uncertainties in the measured cross section.

VII. DISCUSSION OF RESULTS

A. Differential cross sections in muon kinematics

The primary result is the measured double differential cross section in bins of muon momenta shown in Fig. 2. The relative contributions of various processes to the MINERvA v1 tune are shown in Fig. 3. This model predicts that the CCQE-like cross section is dominated by pure 1p1h QE and 2p2h processes. The low p_T region is dominated by QE and 2p2h processes whereas the high p_T region is dominated by QE processes only. Generally, the data lies above the simulation in almost all bins, with the excess growing as p_T increases. Additional comparisons to models are shown in Figs. 4 and 5 with an uncertainty summary in Fig. 6. The integrated cross section for $1.5 < p_{||} < 15$ GeV/c and $0.0 < p_T < 2.5$ GeV/c within our restricted fiducial region is $5.28 \times \pm 0.02 \pm 0.35 \times 10^{-39}$ cm²/nucleon.

Figures 7–10 show the same data as a function of $p_{||}$ in bins of p_T .

Table II shows the χ^2 for comparisons of the model variations to the 2D $p_T, p_{||}$ cross-section measurements. The χ^2 is calculated in two ways, once on the values themselves and once on the log of the values. The log method is discussed in more detail in Refs. [10,47] and is more robust in the presence of multiplicative normalization uncertainties.

B. Cross sections in Q_{QE}^2

We also present one dimensional cross sections as a function of Q_{QE}^2 and $E_{\bar{\nu}}$. Figure 12 shows the ratio of data and a suite of cross-section models to the baseline GENIE 2.12.6 which uses the Valencia 2p2h model as a function of Q_{QE}^2 . The cross-section models shown are default GENIE 2.12.6, the MINERvA tunes, and partial combinations of the components in the MINERvA tunes. All of the

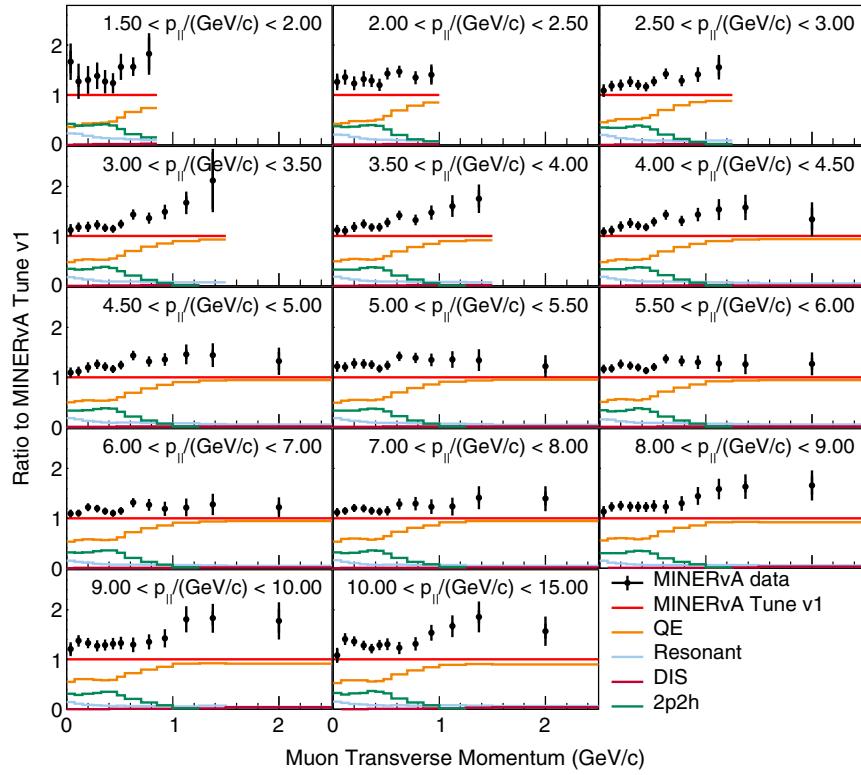


FIG. 3. Ratio of the cross-section data to MINERvA Tune v1 (points) and fractional contributions of components of MINERvA Tune v1 to MINERvA Tune v1 (colored lines).

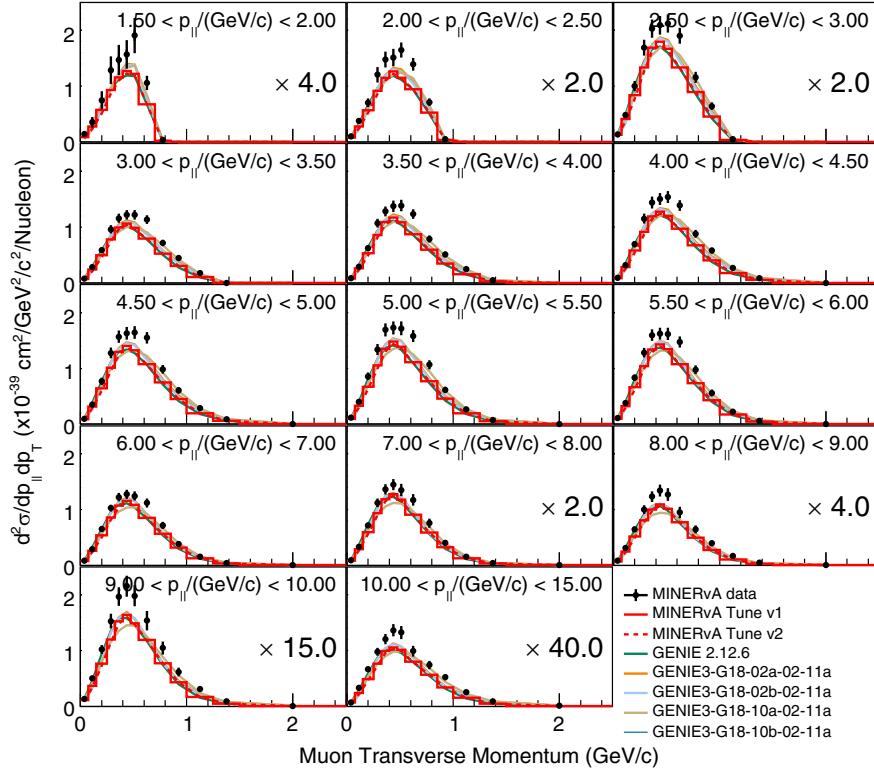


FIG. 4. Double differential cross section as a function of muon transverse momentum in bins of muon longitudinal momentum shown for GENIE 2 and tuned models along with GENIE 3 models.

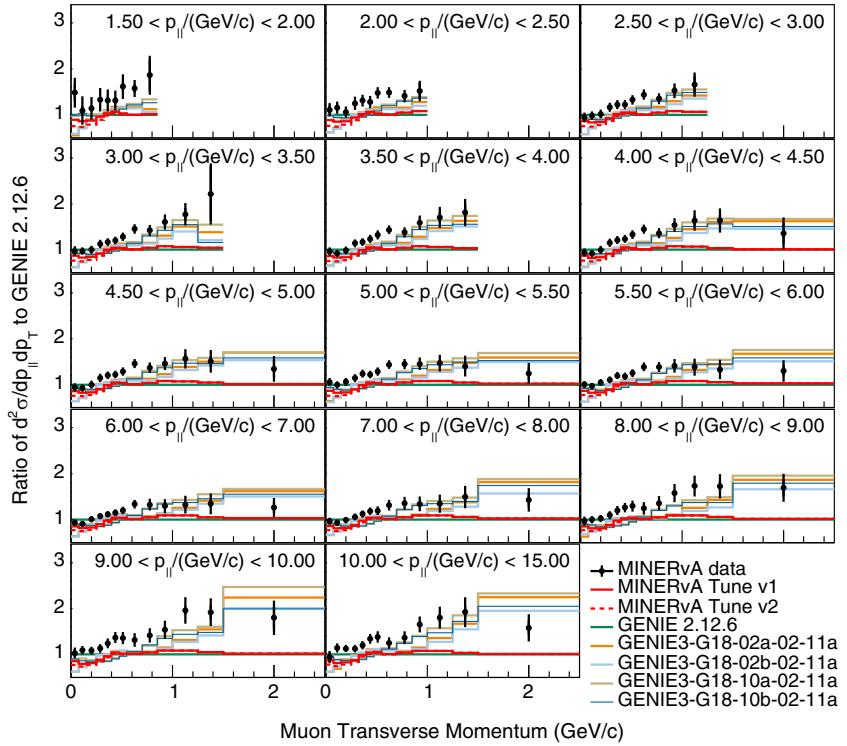


FIG. 5. Ratios of double differential cross sections to GENIE 2.12.6 as a function of muon transverse momentum in bins of muon longitudinal momentum shown for GENIE 2 and tuned models along with GENIE 3 (v3.0.6) models.

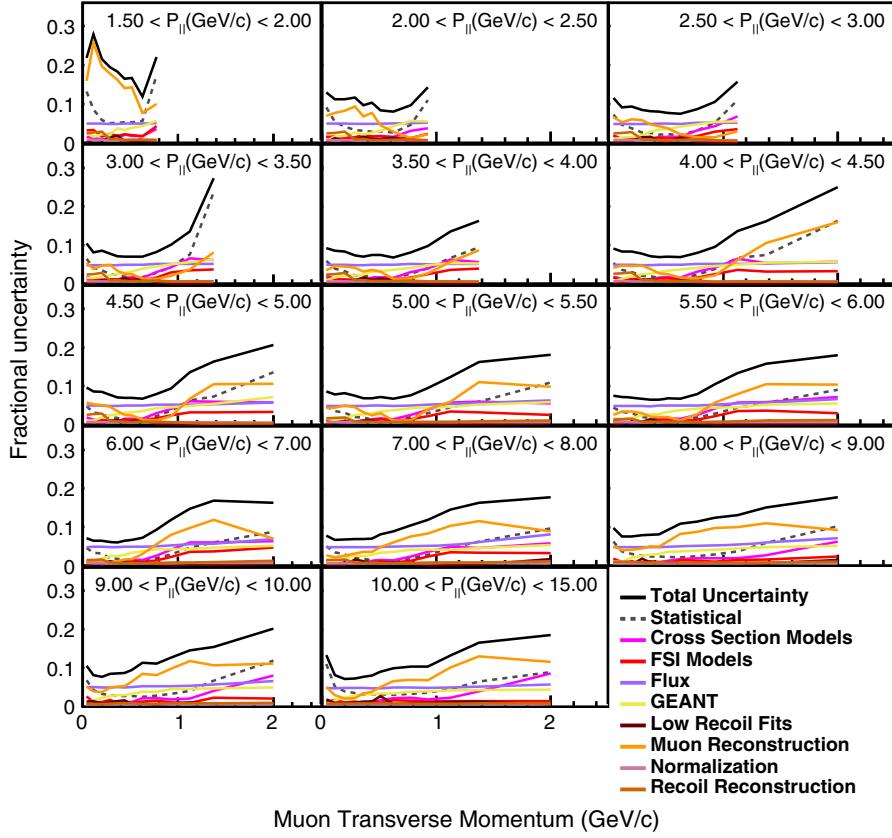


FIG. 6. Summary of uncertainties on the $p_T, p_{||}$ cross sections shown in Fig. 2.

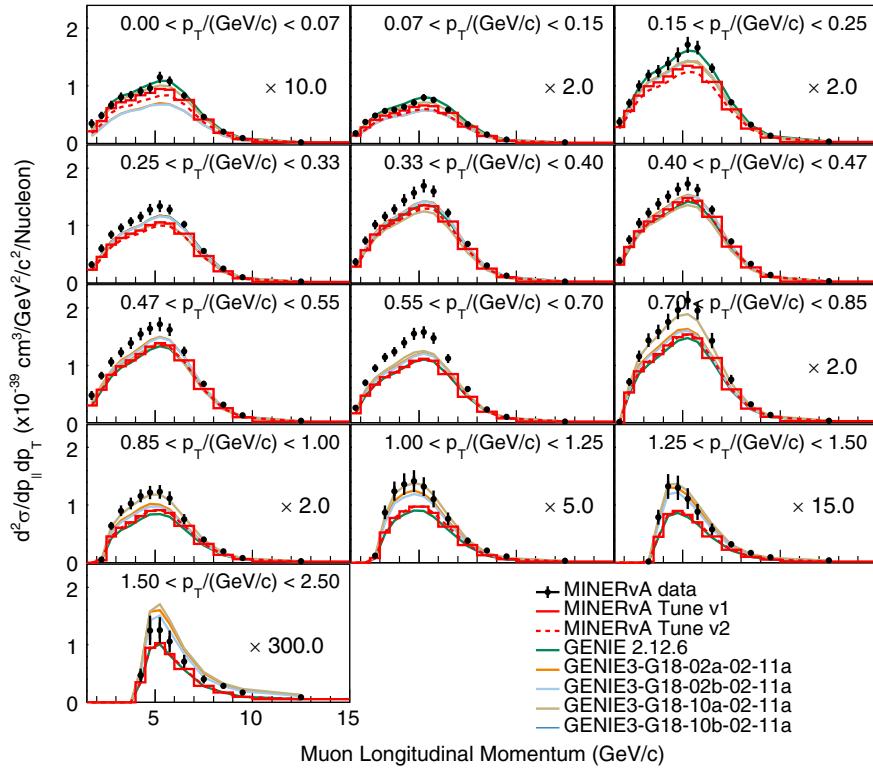


FIG. 7. Double differential cross section as a function of muon longitudinal momentum in bins of muon transverse momentum shown for GENIE 2 and tuned models along with GENIE 3 (v3.0.6) models.

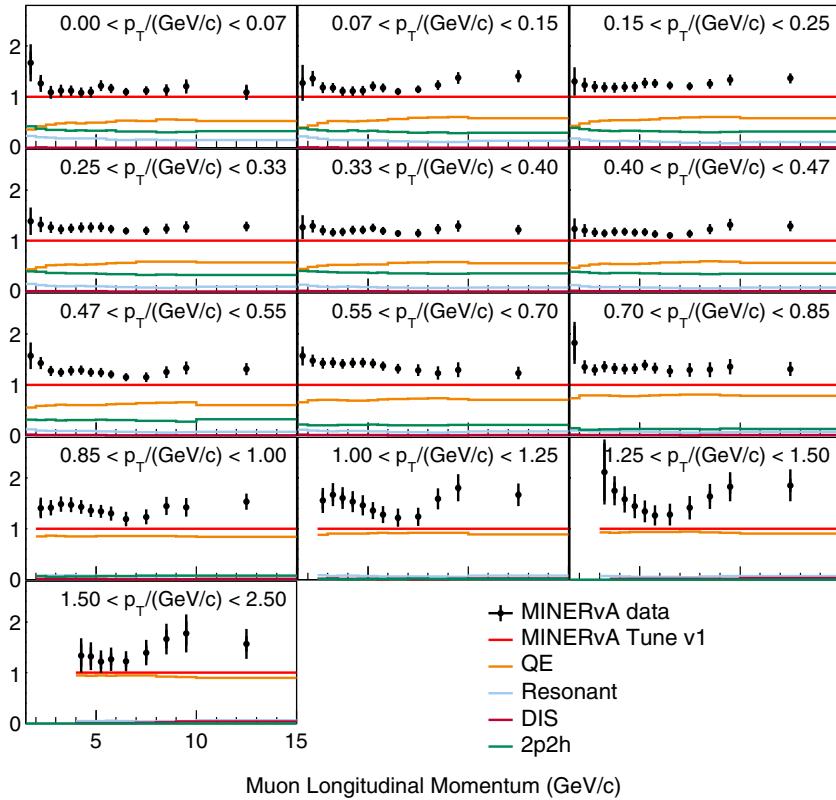


FIG. 8. Ratio of cross sections of data and various components of MINERvA Tune v1 to MINERvA Tune v1 in bins of muon transverse momentum.

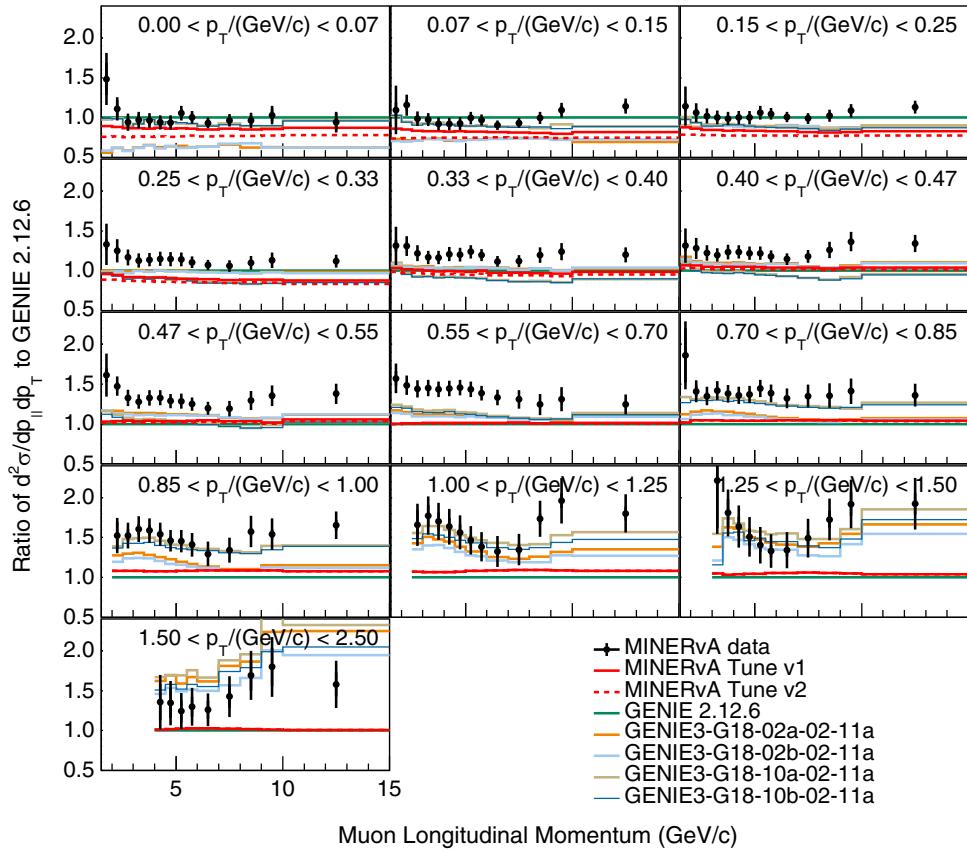


FIG. 9. Ratios of double differential cross sections to GENIE 2.12.6 as a function of muon longitudinal momentum in bins of muon transverse momentum shown for GENIE 2 and tuned models along with GENIE 3 (v3.0.6) models.

GENIE 2 models fail to reproduce the high Q_{QE}^2 behavior of the cross section. The shape of the data appears to favor models that include RPA effects while the π -tune correction appears to have little effect on the predicted rates.

C. Comparisons to GENIE 3.0.6

Recently available GENIE 3.0.6 models appear to better reproduce the high Q^2 behavior and are shown on the right-hand side of Fig. 12 and as a function of muon kinematics in Fig. 5. Comparisons are shown with two different cross-section model tunes [33]. The tune G18_02x_02_11a has a 2p2h model similar to that of default GENIE 2. GENIE 3 models G18_10a_02_11a and c G18_10b_02_11a incorporate the default Valencia [48] model. G18_10a_02_11a uses an effective “hA” intranuclear transport model while G18_10a_02_11a incorporates the full intranuclear “hN” transport model which includes additional processes [33]. The best agreement at high Q^2 among the GENIE 3 models is with model G18_10b_02_11a which incorporates the Valencia model and the hN model for final state interactions.

Figure 11 shows comparisons of data to simulation for the corresponding neutrino data [11] sample and this sample as a function of Q_{QE}^2 . Both ν_μ and $\bar{\nu}_\mu$ cross sections

are extracted from the same fiducial region of the MINERvA detector. The ν_μ cross section includes CCQE-like events with any number of protons, whereas the $\bar{\nu}_\mu$ requires no protons above T_p of 120 MeV. Only antineutrino events with $p_{||}$ less than 15 GeV/c for $\bar{\nu}$ are selected to reduce the larger wrong sign neutrino contamination in the antineutrino beams. As the beam energy is peaked well below this threshold, this restriction has negligible effect except for a $\sim 1\%$ reduction in the highest Q_{QE}^2 bin. Signal selection cuts for the ν_μ events are given in [11].

D. Cross section as a function of $E_{\bar{\nu}}$

In Fig. 13 we show the cross section as a function of true neutrino energy with and without corrections for the T_p and θ_μ selections. The left panel on Fig. 13 compares the data as a function of true neutrino energy with various models. Here the T_p and θ_μ selections are applied as in the previous results. In the right panel, the green data points and lines show the cross section and MINERvA models corrected (by 25%–40%) to all θ_μ and T_p for easier comparison to inclusive models and other experiments.

The theoretical uncertainties on the $E_{\bar{\nu}}$ results are larger than those expressed directly in terms of muon kinematics.

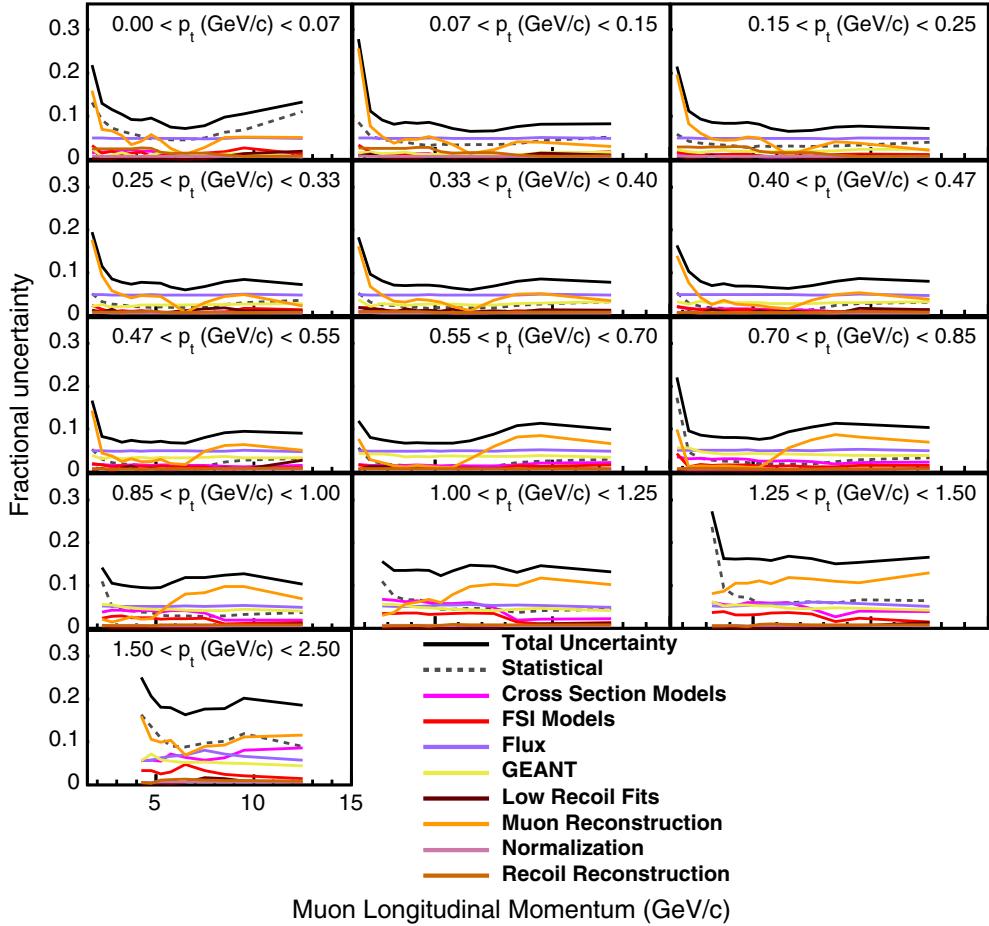


FIG. 10. Summary of fractional uncertainties on the cross section as a function of muon longitudinal momentum in bins of muon transverse momentum shown in Fig. 7.

TABLE II. $p_{\parallel} - p_{\perp}$ χ^2 between data and model variants derived from GENIE. The number of degrees of freedom is 171. Both the χ^2 between the values and between the logs of the values are listed.

Model	χ^2 -linear	χ^2 -log
<i>GENIE 2.12.6 tunes</i>		
MINERvA Tune v1	362.6	580.4
MINERvA Tune v2	364.4	601.4
GENIE w/o 2p2h	226.5	473.2
GENIE (default)	346.4	550.6
GENIE + π tune	354.3	568.5
GENIE + RPA	230.0	406.7
GENIE + RPA + π tune	231.7	414.6
GENIE + Low Recoil Tune	755.4	1059.4
GENIE + Low Recoil Tune + RPA	361.2	570.0
GENIE + Low Recoil Tune + π tune	760.6	1081.8
<i>GENIE 3.0.6 tunes</i>		
GENIE 3.0.6 G18_02a_02_11a	602.9	865.0
GENIE 3.0.6 G18_02b_02_11a	586.9	878.3
GENIE 3.0.6 G18_10a_02_11a	353.1	447.5
GENIE 3.0.6 G18_10b_02_11a	312.8	421.7

First, due to the conversion from $E_{\bar{\nu}}^{(QE)}$ to $E_{\bar{\nu}}$, which is necessary to normalize by the antineutrino flux $\Phi(E_{\bar{\nu}})$, but is affected by uncertainties in nuclear models and second, because the correction for the T_p and θ_{μ} selections necessary to go from the restricted cross section in the left panel to the full cross section in the right panel introduces additional theoretical uncertainties. Figure 14 shows the corresponding uncertainties for the restricted phase space (left) and the full phase space (right). Note that the uncertainties due to the cross-section model and FSI increase substantially when one removes the fiducial restrictions.

E. Summary

We have presented the antineutrino CCQE-like cross section measured with the NuMI $\langle E_{\bar{\nu}} \rangle \sim 6$ GeV beam in the MINERvA detector. The measurement extends our past measurements in the antineutrino channel made in the lower neutrino energy beam and complements the neutrino cross-section measurement at higher energy. We have extended the measurement of Q_{QE}^2 to 4 GeV 2 .

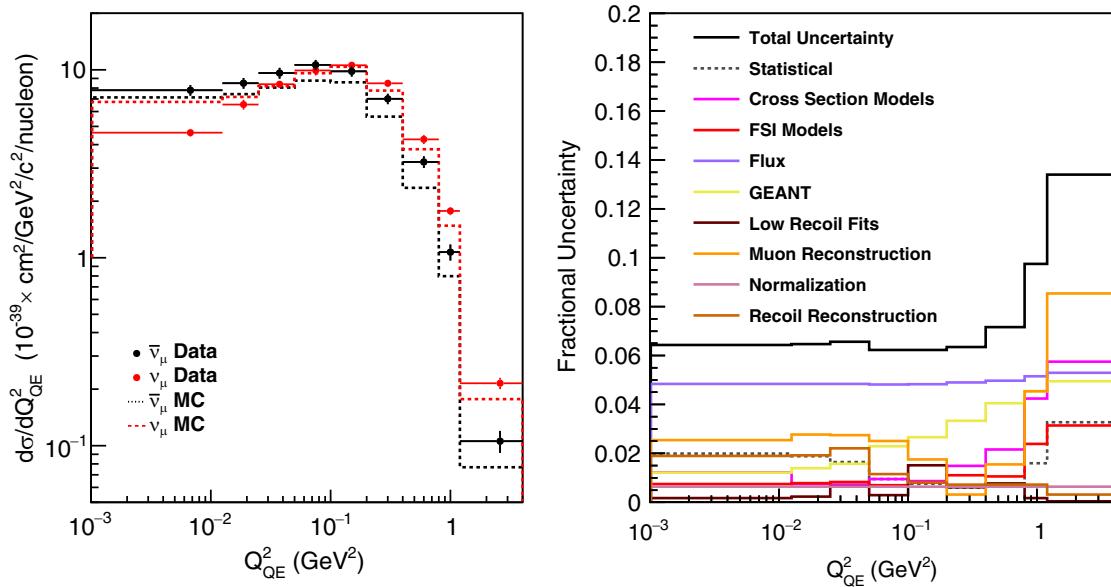


FIG. 11. Left: Measured (data points) and MINERvA Tune v1 prediction (dotted lines) of CCQE-like $d\sigma/dQ_{QE}^2$ for neutrinos (Ref. [11], red) and antineutrinos (this measurement, black) extracted with the NuMI neutrino and antineutrinos energies ~ 6 GeV. Right: Summary of fractional uncertainties on the differential antineutrino cross section as a function of Q_{QE}^2 hypothesis.

These measurements indicate that none of the variations of GENIE v2 based on the MINERvA low energy data are sufficient to describe the MINERvA medium energy data. However, GENIE v3 models appear to better describe the data especially in the high Q_{QE}^2 region

which is dominated by the QE process. This high statistics double differential cross section provides useful model inputs for future neutrino oscillation experiments. Tables of values are available in the Supplemental Materials [14].

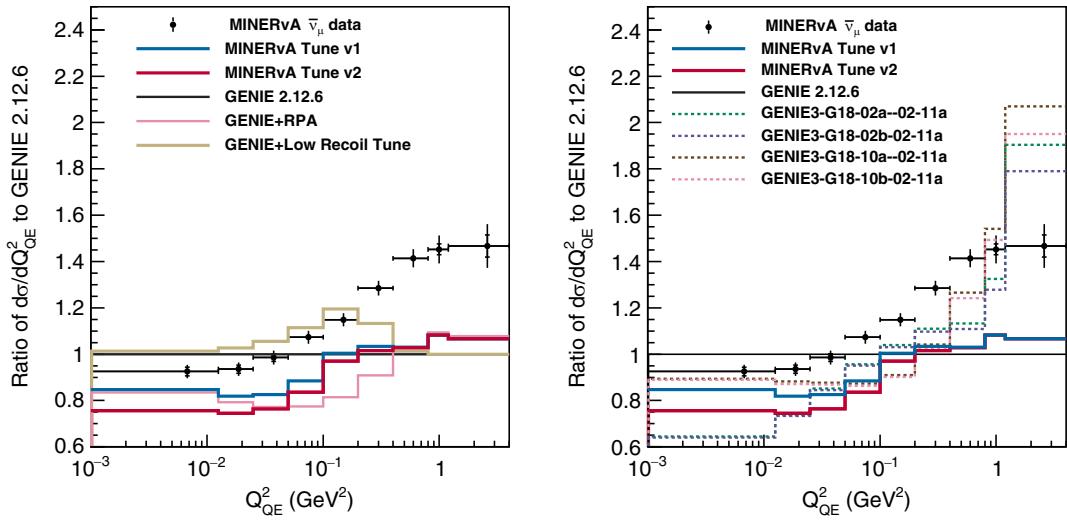


FIG. 12. Comparisons of the cross section predicted by various tunes applied on GENIE with respect to the baseline GENIE 2.12.6 (black) as a function of Q_{QE}^2 (left). MINERvA Tune v1 (blue) is the standard simulation tuned to the MINERvA low energy data. MINERvA Tune v2 (red) is MINERvA Tune v1 with nonresonant pions suppressed in the low Q_{QE}^2 region [31]. The remaining curves show the effect of enabling different corrections to the base model. The plots on the right show comparisons of cross-section predictions for GENIE v3.0.6 (dotted lines) with the MINERvA tuned GENIE v2.12.6 predictions. Inner error bars represent statistical uncertainties and outer error bars represent systematic uncertainties.

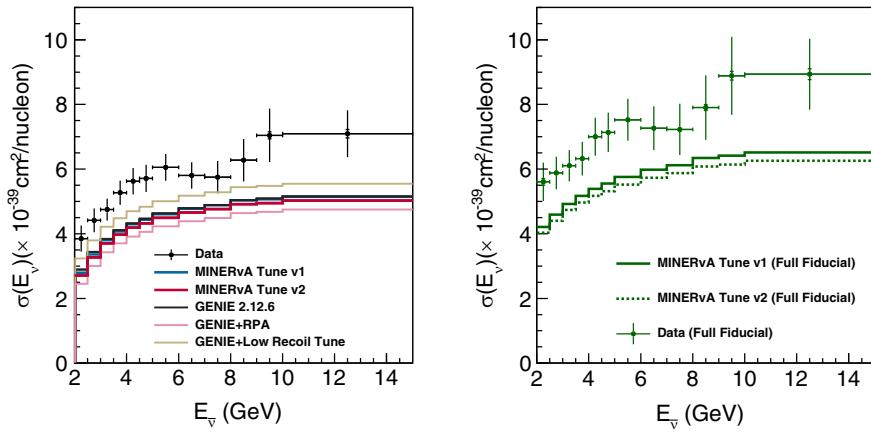


FIG. 13. CCQE-like cross section as a function of true $\bar{\nu}$ energy. The black data points on the left panel use our fiducial final state definition with $\theta_\mu < 20^\circ$ and $T_p < 120$ MeV. The green points on the right panel are data and the MINERvA tunes v1 and v2 model predictions (straight and dotted lines) for the total cross section with the θ_μ and T_p cuts removed.

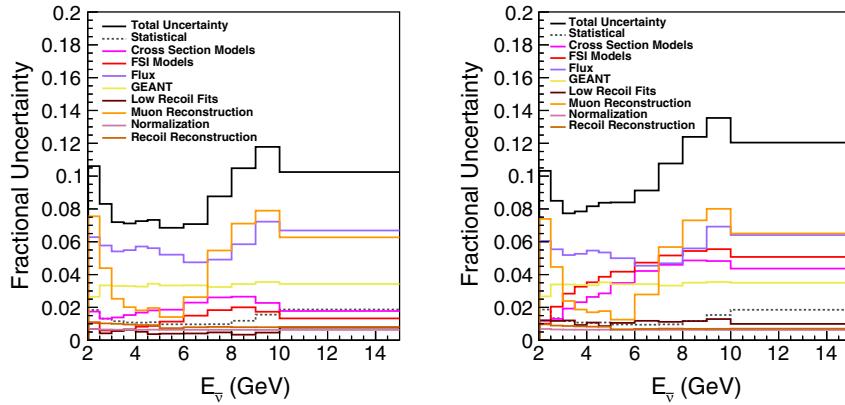


FIG. 14. Error summary on the measured fiducial restricted (left) and full fiducial (right) cross section as a function of true neutrino energy.

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