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Analysis of modeled 3D solar magnetic field during 30 X/M-class solar flares

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Using non-linear force free field (NLFFF) extrapolation, 3D magnetic fields were modeled from the 12-min cadence Solar Dynamics Observatory Helioseismic and Magnetic Imager (HMI) photospheric vector magnetograms, spanning a time period of 1 hour before through 1 hour after the start of 18 X-class and 12 M-class solar flares. Several magnetic field parameters were calculated from the modeled fields directly, as well as from the power spectrum of surface maps generated by summing the fields along the vertical axis, for two different regions: areas with photospheric $|B_7| \ge 300$ G (active region—AR) and areas above the photosphere with the magnitude of the non-potential field (B_{NP}) greater than three standard deviations above $\overline{|B_{NP}|}$ of the AR field and either the unsigned twist number $|T_w| \ge 1$ turn or the shear angle $\Psi \ge 80^\circ$ (non-potential region—NPR). Superposed epoch (SPE) plots of the magnetic field parameters were analyzed to investigate the evolution of the 3D solar field during the solar flare events and discern consistent trends across all solar flare events in the dataset, as well as across subsets of flare events categorized by their magnetic and sunspot classifications. The relationship between different flare properties and the magnetic field parameters was quantitatively described by the Spearman ranking correlation coefficient, r_s. The parameters that showed the most consistent and discernable trends among the flare events, particularly for the hour leading up to the eruption, were the total unsigned flux ϕ), free magnetic energy (E_{Free}), total unsigned magnetic twist (r_{Tot}), and total unsigned free magnetic twist (ρ_{Tot}). Strong ($|r_s| \in [0.6, 0.8)$) to very strong ($|r_s| \in [0.8, 1.0]$) correlations were found between the magnetic field parameters and the following flare properties: peak X-ray flux, duration, rise time, decay time, impulsiveness, and integrated flux; the strongest correlation coefficient calculated for each flare property was 0.62, 0.85, 0.73, 0.82, -0.81, and 0.82, respectively.

KEYWORDS

solar corona, solar photosphere, solar magnetic field, active region, solar flares, NLFFF extrapolation

1 Introduction

Solar flares are intense bursts of radiation that occur within the solar atmosphere, typically seen as hot coronal loops and bright chromospheric ribbons. Throughout the duration of these explosive events (ranging from minutes to hours), 10²² to 10²⁵ J of energy is released from the highly complex magnetic fields over active regions (ARs) on the Sun's

surface. Stronger flares (M- and X-class), along with the often accompanied/associated coronal mass ejections (CMEs) and solar energetic particle (SEP) events, can have major technological impacts on both the near-Earth space environment and on Earth, as well as biological impacts on astronauts and high-altitude flying aircrews (Davies, 1990; Eastwood et al., 2017). Considerable effort has been and continues to be undertaken toward solar flare research and flare forecasting to help mitigate the impacts of these events. However, flares remain a challenge to accurately predict due to both a limited understanding of the underlying physical processes, in particular, the triggering mechanism of magnetic reconnection, and limited data.

Historically, most of the effort in solar flare research and flare forecasting has been focused on analyzing the photospheric magnetic field measurements, considering that full vectorfield component data are only available for the photosphere. Many research workers have studied the correlations between different photospheric magnetic field parameters and flare characteristics, as well as the evolution of those parameters during solar eruptions (e.g., Leka and Barnes, 2003; 2007; Mason and Hoeksema, 2010; Wang et al., 2012; Kazachenko et al., 2017; 2022; Whitney Aegerter et al., 2020). Strong relationships have been found, for example, between the Geostationary Operational Environmental Satellites (GOES) measured peak X-ray flux and the flare ribbon reconnection flux (Kazachenko et al., 2017); however, the relationships typically involve post-eruption data and therefore are not directly applicable for flare forecasting. Furthermore, signatures of solar flare occurrence that have been found within photospheric magnetic field data, often in relation to field helicity, have yet to be shown to consistently predict when an AR will flare. Flare forecasting methods that utilize photospheric magnetic field data in combination with machine learning (e.g., Falconer et al., 2011; Bobra and Couvidat, 2015; Liu et al., 2017; Leka et al., 2018) have shown little improvement in forecasting capability over climatological forecasts. Leka et al. (2019) found that none of the 19 operational flare forecasting methods tested during a forecasting workshop performed "exceptionally well" across all performance metrics.

A major limitation is that vital aspects of the solar magnetic field that contribute to the flaring process are underestimated when parameters are calculated from the 2D imprint of the 3D field (Gupta et al., 2021). The standard model of solar eruptions (flares and CMEs) involves the accumulation of free energy within the solar magnetic field (from the photosphere through the lower corona), which is then impulsively released through a rapid reconfiguration of the field triggered by magnetic reconnection that destabilizes the field to a critical point of instability (Priest and Forbes, 2002; Shibata and Magara, 2011). Given that the buildup and release of energy occur through the lower corona, it is possible that parameters calculated from the solar magnetic field through the lower corona would provide more information on flare productivity and the nature of the events than those calculated from the photospheric field alone. Whereas regular measurements of the photospheric magnetic field have been available since the 1960s/1970s (Howard, 1967; Livingston et al., 1976; Svalgaard et al., 1978) and those of the chromospheric field since the 1980s (Jones, 1985), measurements of the coronal field remain a challenge to be obtained through traditional spectro-polarimetric methods. Measurements of the coronal field strength have been attempted using techniques such as coronal seismology (e.g., Roberts et al., 1984; Nakariakov and Ofman, 2001), radio emissions (e.g., Chen et al., 2020; Fleishman et al., 2020), and Stokes V circular polarization measurements from spectral lines (e.g., Lin et al., 2000; Kuridze et al., 2019). However, these methods provide only intermittent/discontinuous data.

Due to the lack of routine direct measurements for the coronal magnetic field, the full 3D solar magnetic field is often studied through numerical modeling. The four main types of models are the magnetohydrodynamics (MHD) model, the magnetohydrostatic (MHS) model, the force-free model, and the potential-field source-surface (PFSS) model (Wiegelmann et al., 2017). During the past several decades, several different Non-Linear Force-Free Field (NLFFF) models that use the observed photospheric vector magnetograms as an input have been developed, as discussed in the review by Wiegelmann and Sakurai (2021). Although NLFFF models have major limitations from the assumptions of static equilibrium and Lorentz force balance, they have been used in a number of studies to extrapolate and investigate the structure and evolution of the solar magnetic field through the corona, particularly over ARs during solar eruptions (e.g., Inoue et al., 2011; Sun et al., 2012; Thalmann et al., 2013; Jing et al., 2018; Thalmann et al., 2020; Yurchyshyn et al., 2022; Garland et al., 2023). While NLFFF models are generally simpler, neglecting additional physical effects, than the more computationally demanding MHS and MHD models that have been developed, Yeates et al. (2018) found that out of seven different non-potential magnetic models tested during a 2015 eclipse, the static, NLFFF extrapolation codes performed better for modeling ARs, whereas the time-dependent codes modeled quiet solar features (such as filaments) better. A possible reason for the difference includes the input data of the models; the static models used synoptic vector magnetograms, whereas the time-dependent models used the line-of-sight photospheric field and additional observations (e.g., filaments). The conclusion from the workshop was that a hybrid model, one that applied static extrapolation with additional energization informed by evolution models, would be the best approach for modeling ARs. In recent years, time-dependent models that use continuously observed magnetograms as the input have been developed to reproduce the dynamics of the corona; a review of such data-driven models can be found in the study by Jiang et al. (2022).

Studies that have utilized NLFFF extrapolation and other modeling techniques to investigate the structure and evolution of the solar magnetic field through the corona over ARs during solar eruptions (e.g., Inoue et al., 2011; Sun et al., 2012; Thalmann et al., 2013; Jing et al., 2018; Thalmann et al., 2020; Yurchyshyn et al., 2022; Garland et al., 2023) have shown the potential that parameters calculated from the modeled 3D fields possess in regards to predicting the likelihood, location, and timing of solar flares. It must be recognized that modeling introduces additional possible errors due to the inaccuracy of the extrapolation processes compared to using observed photospheric data alone. Still, promising results from modeled data have been demonstrated. For example, Kusano et al. (2020) developed a physics-based method based on the theory of double-arc instability (DAI) and utilizing NLFFF extrapolation, called the κ -scheme, which predicted most large, imminent flares

within a dataset of ~ 200 ARs. The $\kappa\text{-scheme}$ measures the critical size (r_c) of the region of trigger-reconnection within a flaring AR through calculations of the magnetic twist flux density (τ) near the PIL and the flux crossing over the strongest sheared field line rooted in the reconnection region within areas with photospheric $B_{\rm NP}>1000$ G (Kusano et al., 2020). An analysis of the X-class flares from 2008 to 2019 showed that the small-scale structure of τ near the PIL can determine when and where solar flares may occur and how large they can be. As another example, Korsós et al. (2020) applied the weighted horizontal gradient of magnetic field (WG_M) flare prediction method (Korsós et al., 2015) to 3D potential field and NLFFF-extrapolated magnetic fields of 13 flaring ARs. Potential lead-time improvement of 2–8 h for flare onset prediction was found by applying the (WG_M) method between 1,000 and 1,800 km above the solar surface, that is, within the chromosphere.

The purpose of this study is to continue the effort in modeling and investigating the 3D solar magnetic field over ARs during solar flare eruptions and perform a statistical analysis that utilizes magnetic field parameters calculated from modeled 3D magnetic field data. The analysis of a particular case study (Garland et al., 2023) was adjusted and extended to a larger dataset of strong/extreme (M- and X-class) solar flare events. Following the modeling and parameter calculation for each event, a statistical analysis similar to that of Mason and Hoeksema (2010) and Kazachenko et al. (2022) was performed. Specifically, a superposed epoch analysis was applied to the temporal evolution of the magnetic field parameters during a time interval of 1 hour before through 1 hour after the flare occurrence. Additionally, the correlations between the magnetic field parameters and different flare characteristics were examined. Through the analysis, the evolution of the 3D solar magnetic field over flaring ARs leading up to and following an eruptive event was explored, with the intent of discerning any consistent pre-eruptive signatures of solar flare occurrence or strong relationships between the state of the 3D magnetic field leading up to a flare and the different flare properties.

The ultimate vision for this study is to benefit current flare forecasting efforts, such as the Flare Likelihood and Region Eruption Forecasting (FLARECAST) project (Georgoulis et al., 2021). The FLARECAST project is an "advanced solar flare prediction system based on automatically extracted physical properties of solar active regions coupled with state-of-the-art machine learning solar flare prediction methods" (Georgoulis et al., 2021). A vast majority of the 209 predictors included as part of the FLARECAST algorithm are calculated from the observed photospheric magnetograms; the remaining include information from the National Oceanic and Atmospheric Administration (NOAA) Space Weather Prediction Center (SWPC) catalogs and photospheric intensity images. As mentioned previously, it has been shown that parameters calculated from the modeled 3D solar magnetic fields (through the corona) possess potential predictive capability. Inclusion of such modeling techniques and parameters found to have strong relationships with flaring activity in the FLARECAST system and others like it—in conjunction with the observed photospheric data/parameters calculated—could possibly improve already prediction.

The remainder of this paper is outlined as follows: Section 2 presents the dataset used for the analysis. Section 3 details the

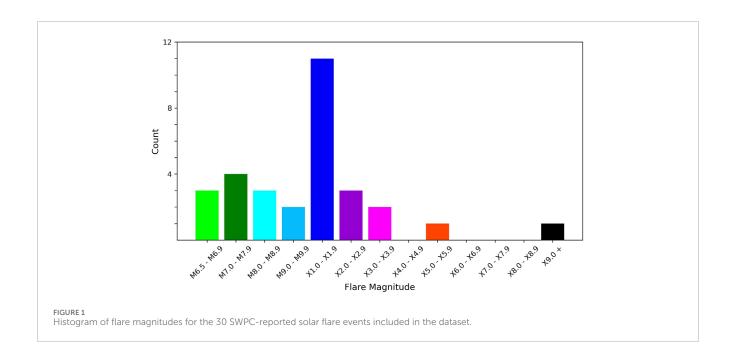
methodology for extrapolating the 3D solar magnetic field and calculating the field parameters. Section 4 discusses the results of the statistical analysis, and Section 5 summarizes the analysis and discusses future work.

2 Dataset

The dataset used in this study consists of 30 solar flare events (18 X-class and 12 M-class) from Solar Cycle 24 reported by SWPC and the 720-s (12-min) cadence HMI Active Region Patch (HARP) data from the Joint Science Operations Center (JSOC) during a 2-h window around each flare event. The solar flare event data include the flare start time, max time, end time, class/magnitude, integrated flux, and NOAA AR number. The HARP data include the date/time of observation, the HARP center longitude/latitude, HARP number, and associated NOAA AR number. HARPs are enduring, coherent magnetic structures whose size are on the scale of an AR that are identified and tracked using continuum intensity images and photospheric full-disk line-of-sight (LoS) magnetogram images produced on a 12-min cadence (Hoeksema et al., 2014; Joint Science Operations Center, 2023). Further details regarding the HMI instrument, observables, and vector field pipeline can be found in the study by Schou et al. (2012), Couvidat et al. (2016), and Hoeksema et al. (2014), respectively. The connection of the solar flare event and HARP data was established by associating the start time of the flare to the nearest HARP

Figure 1 provides the distribution of the flare magnitudes for the 30 flares in the dataset, which clearly shows the mode magnitude of X1.0–X1.9. The center coordinates of the flaring AR (in Stonyhurst Lat/Lon) at the start time of each flare event are plotted in Figure 2. It is worth noting the commonly used $\pm 45^{\circ}$ longitude threshold, which was chosen to minimize solar limb/projection effects.

For each event in the dataset, the sunspot and magnetic classifications of the associated ARs at the time closest to flaring were retrieved from the SWPC Solar Region Summary (SRS) archive (available at ftp://ftp.swpc.noaa.gov/pub/warehouse/). Sunspot classification is based on the modified Zürich/McIntosh system (McIntosh, 1990), which continues to act as a foundation for solar flare forecasting today. The general form of the modified Zürich/McIntosh classification is Zpc, where Z is the modified Zürich class, *p* is the type of largest spot (describing the penumbra), and *c* is the degree of compactness in the interior group (McIntosh, 1990). The Mount Wilson classification system, put forward by Hale et al. (1919), provides a simple way to describe the magnetic properties and morphology of ARs. The distribution of the sunspot and magnetic classifications for the 30 solar flare events in the dataset is provided in Table 1. As seen in the table, 22 of the 30 flaring ARs have a Mount Wilson classification of $\beta y \delta$. The top three modified Zürich/McIntosh sunspot classifications are (in order) Fkc, Ekc, and Dkc. The findings in Table 1 are consistent with those in other studies that have analyzed the statistics for the sunspot/magnetic classifications of flaring ARs (e.g., Smith and Howard, 1968; McIntosh, 1990; Jaeggli and Norton, 2016; Norsham et al., 2022).



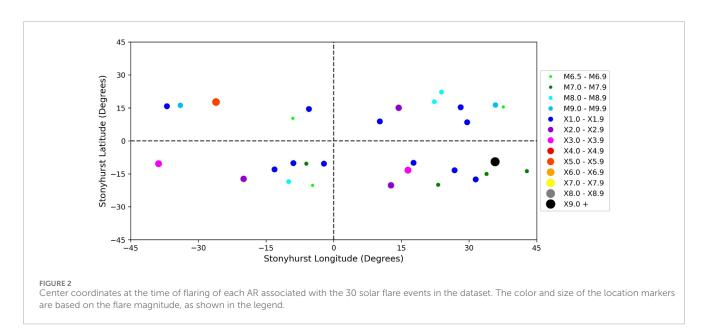


TABLE 1 Distribution of modified Zürich/McIntosh sunspot and Mount Wilson magnetic classifications for the 30 flaring ARs in the dataset.

Sunspot class Magnetic class	Dai	Dao	Dhc	Dkc	Dki	Dko	Dsi	Eai	Ehc	Ekc	Fkc	Total
В	_	-	_	_	_	1	1	_	_	_	_	2
Ву	1	-	1	_	1	_	-	1	_	1	-	5
Βδ	_	1	-	_	_	-	-	_	-	_	_	1
Βγδ	1	-	_	5	_	-	-	2	2	5	7	22
Total	2	1	1	5	1	1	1	3	2	6	7	30

3 Methodology

3.1 3D solar magnetic field extrapolation

Following the same procedure as Garland et al. (2023) and Yurchyshyn et al. (2022), HMI magnetic field measurements were re-binned to 1 Mm pixel scale and transformed to a local Cartesian coordinate system using the same cylindrical equal area (CEA) projection used to produce the hmi.sharp_cea_720s series data (Bobra et al., 2014). The Cartesian boxes (or data cubes) in which the 3D magnetic fields would be extrapolated from the HMI magnetograms, which were the base maps of the boxes, were centered over the HARP center coordinates. In other words, the center of the base map was set to the HARP center coordinates. The box structures were quite large, spanning 400 by 200 by 200 pixels (re-binned) along the x-, y-, and z-axes (with z in the vertical) in order to accommodate as much of the field-line connectivity within the ARs and their surroundings as possible, which is a requirement for successful NLFFF application to real solar data (DeRosa et al., 2009). The specific size [400,200,200] accommodated the largest AR in the dataset. As described in the next section, specific portions of the field over the ARs within the data cubes were identified and used to calculate different parameters. Therefore, different data cube sizes for each flaring AR in the dataset did not need to be specified on a case-by-case basis, and a single size could be used to more easily automate parts of the modeling process so long as the field-line connectivity within the ARs was captured.

The HMI data retrieval, coordinate transformation, and NLFFF extrapolation were accomplished using the GX Simulator package (Nita et al., 2015; 2018; Nita et al., 2023). Following user specification of AR coordinates, observation time, and size/spatial resolution for the 3D data cube, the GX Simulator downloads the HMI magnetogram and remaps it to the bottom boundary of an empty data cube, and fills the empty cube with a potential field solution obtained from the normal component of the magnetic field at the lower boundary using a fast Fourier transform (FFT) method. In order to avoid unrealistic periodic, flux-balanced boundary conditions implied by the FFT solution at the lateral boundaries, more appropriate "open" boundaries are simulated by expanding the computational domain by 50% in each direction (Nita et al., 2023). The normal component of the field at the lower boundary is padded with a constant, non-zero value that is computed such that the unbalanced magnetic flux at the original lower boundary is compensated perfectly by the total signed flux from the added areas. The final potential field solution for the original domain is cut out from the expanded domain and used as the initial condition for the NLFFF extrapolation, which utilizes the weighted optimization code from Fleishman et al. (2017). During the extrapolation, the magnetic field at the top and side boundaries is frozen to be the potential field. Further details regarding the GX Simulator Automatic Model Production Pipeline (AMPP) can be found in the study by Nita et al. (2023).

For each of the 30 solar flare events in the dataset, the *GX Simulator* was used to generate [400,200,200] box structures containing the extrapolated magnetic field from the HMI magnetograms for a time period of 1 hour before through 1 hour after the flare start time. Given the 12-min cadence of the magnetograms, this meant that 11 3D solar magnetic field

extrapolations were generated for each flare event. As mentioned previously, the box structures were centered over the HARP center coordinates, specifically, the coordinates from the HARP data time closest to the flare start time. The ± 1 h window around each solar flare event was selected in order to specifically investigate the relative changes of the solar magnetic field shortly before and after eruption, when significant reconfiguration and energy release occur. Additionally, for the purposes of correlating the state of the field prior to the eruption and the different flare properties, this window of time limits the inclusion of data with an ongoing flare event happening ahead of the main flare being investigated. The ± 1 h window also significantly limits the forecasting applicability compared to other studies that implement much longer preceding windows.

3.2 Data volumes

Similar to Garland et al. (2023), two regions were identified and used as masks to generate separate data volumes (i.e., specific portions of the total magnetic field within the box structures) from which the different magnetic field parameters would be calculated. The two regions were as follows:

- 1. Active region, AR
- 2. Non-potential region, NPR

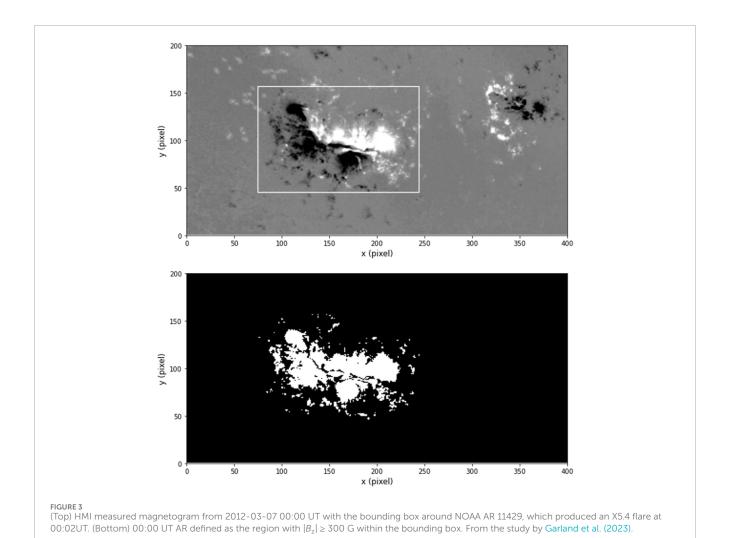
The definition of the AR in regards to the data volumes was the exact same as that used by Garland et al. (2023). The AR was defined as the areas where the magnitude of the observed photospheric vertical magnetic field ($|B_z|$) \geq 300 Gauss (G) was within a specified bounding box of the magnetogram (see Figure 3). The bounding box was constructed by the following steps:

Step 1) Isolating pixels from the magnetogram with $|B_z| \ge 100$ G. Step 2) Running a smoothing mask over the filtered image.

Step 3) Identifying the bounded area that contains all pixels with a pixel value ≥ 2 standard deviations above the mean.

For cases where multiple NOAA ARs are present within the FOV (such as in Figure 3), the bounding box is manually limited to the flaring AR. The threshold for $|B_z|$ is slightly higher than the typical threshold range of 100–200 G seen in other studies to avoid noisy, weak field data (Bobra et al., 2014; Kazachenko et al., 2017; 2022). It should be mentioned that the threshold imposes the limitation that areas of highly twisted photospheric topology but weak flux, which provide information on the field line configuration emerging from the surface into the solar atmosphere (MacTaggart et al., 2021), are ignored. The implication of this is the assumption that all of the twisted topology critical to the flaring process are fully emerged at the time of flaring.

Using the above definition, the AR data volumes (or AR fields) were determined following the same method as Garland et al. (2023). Specifically, for each flare event, the AR at the HARP time closest to the flare start identified the photospheric footprints (or seed locations) from which the field lines within the [400,200,200] box were traced pointwise with a fourth order Runge–Kutta–Fehlberg algorithm, linearly interpolating between computational grid points, as part of the *GX Simulator* package (Nita et al., 2015; 2018; Nita et al., 2023). The coordinates of these field lines within the box specified the volume elements that would



be used in the calculations of the magnetic field parameters; the collection of volume elements made up the data volume. The AR data volumes/fields were established (using the specified seed locations)

for each of the 11 extrapolated magnetic fields throughout the 2-h window around each solar flare event.

The NPR replaced the overlap region (OR) from the study by Garland et al. (2023) and is defined as the region above the photosphere where the magnitude of the non-potential component of the magnetic field ($|\mathbf{B_{NP}}|$) \geq three standard deviations above the mean $|\mathbf{B_{NP}}|$ of the AR field, and either the unsigned twist number ($|T_{\rm w}|$) \geq one turn or the shear angle Ψ) \geq 80°. The non-potential component of the NLFFF-extrapolated magnetic field was calculated as follows:

$$\mathbf{B_{NP}} = \mathbf{B} - \mathbf{B_{Pot}},\tag{1}$$

where **B** is the NLFFF solution and $\mathbf{B_{Pot}}$ is the potential field solution. $T_{\rm w}$ is the twist number of the individual field lines calculated using the code developed by Liu et al. (2016), and the threshold of one turn is considered appropriate to define a moderate twist (Patsourakos et al., 2020). The shear angle was calculated as follows:

$$\Psi = \cos^{-1}\left(\frac{\mathbf{B} \cdot \mathbf{B}_{\mathbf{Pot}}}{|\mathbf{B}||\mathbf{B}_{\mathbf{Pot}}|}\right). \tag{2}$$

The 80° threshold for Ψ is the higher of two commonly used thresholds for shear (e.g., Lu et al., 1993; Leka and Barnes, 2007).

The purpose of the NPR was the same as that of the OR (Garland et al., 2023), which was to isolate the portions of the magnetic field expected to be involved with the flaring process and predict the location of the eruption. The hypothesis is that the portion of the solar magnetic field that has the greatest degree of non-potentiality above the photosphere would be associated with the location where energy is built up/released, that is, the location of the eruption of a solar flare. The thresholds for Tw and Ψ further stipulate that the non-potentiality of the field is due in large part to either or both of those properties being high, which is generally expected for flaring. The consideration of Y for the NPR, which was not considered for the OR, was motivated by the fact that both sheared magnetic arcades (SMAs) and magnetic flux ropes (MFRs), or a hybrid of the two, are the pre-eruptive magnetic field configurations considered viable (Patsourakos et al., 2020).

The NPR is established from similar parameters that are involved in the κ -scheme proposed by Kusano et al. (2020). The κ -scheme assumes a DA magnetic loop structure and provides a more specific estimate of flaring location ($r_c < 1$ Mm) along a PIL, whereas the NPR is a more generalized estimate (generally $\sim 10^2$ Mm² in size)

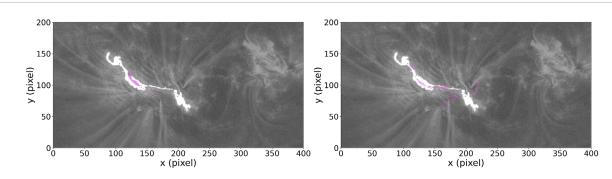


FIGURE 4
NPR (left) and OR (right) (purple shading) plotted over the 2012-03-07 00:08 UT grayscale AIA imagery, which highlights the flare brightening at the approximate start of the eruptive/flash phase of the X5.4 solar flare.

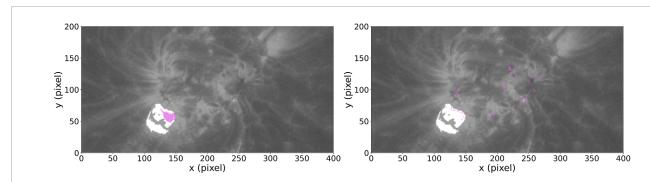


FIGURE 5
NPR (left) and OR (right) (purple shading) plotted over the 2013-11-08 04:26 UT grayscale AIA imagery, which highlights the flare brightening at the approximate start of the eruptive/flash phase of the X1.1 solar flare.

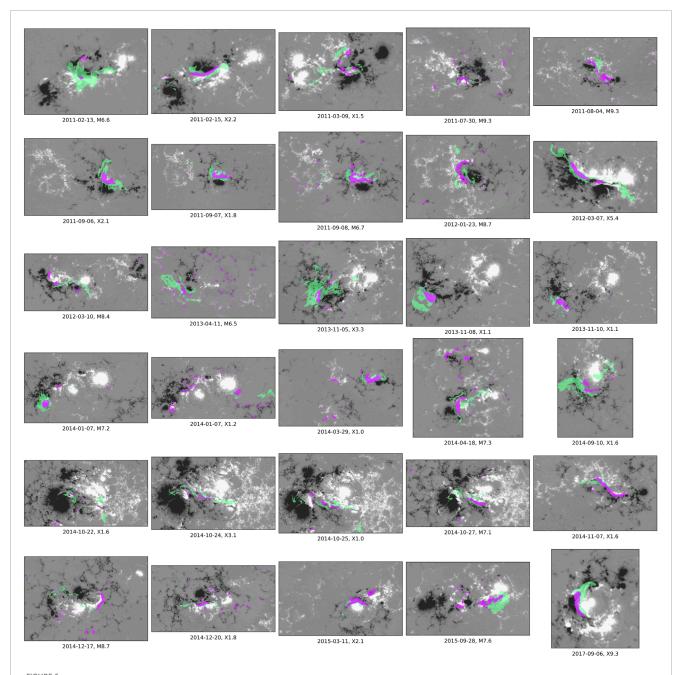
not constrained to a PIL and assumes the presence of a MFR, SMA, or hybrid configuration within the magnetic field structure.

Figure 4 shows a comparison of the OR and NPR for the X5.4 solar flare event that was analyzed as a case study by Garland et al. (2023). Both the OR and NPR aligned well with the area of initial flare brightening for this event. However, the NPR is less noisy and more concentrated over the point of eruption, whereas the OR contains many scattered, less coherent portions on the peripherals of the large sunspots. Figure 5 provides an example of an event where the NPR aligned far better with the area of flare brightening than the OR did, which was the common result for several test events from the full dataset. For the majority of the 30 flare events in the dataset, the NPR aligned well with the area of initial flare brightening (Figure 6). The alignment was worse for events where the AR did not have a well-defined PIL compared to those that did, as well as for events where the flare occurred on the edge of the AR away from an inversion line versus directly over one. In these cases, the magnetic field configurations were generally more conducive to emerging-flux-type flares (Thalmann, 2010) as opposed to that of "two-ribbon" flares. Details regarding how the areas of initial flare brightening were identified for the flare events using the SDO atmospheric imaging assembly (Lemen et al., 2012) 171 Å, 211 Å, and 1600 Å imagery can be found in the study by Garland et al. (2023).

Unlike the AR, which was defined at the surface and thus directly identified the seed locations that would be used to trace field lines from at each timestep, the NPR was defined above the photosphere within the corona. Therefore, the first step to determine the seed locations was to identify which field lines from the AR data volume/field came into contact with the NPR region at the start time of the flare. The footprints of those field lines determined the seed locations for the NPR data volume/field at each timestep throughout the 2-h window around the event (see Figure 7).

3.3 Magnetic field parameters

The magnetic field parameters calculated from the data volumes are shown in Table 2 with their description, units, and formulas. The summations for the parameters occur over the individual volume elements within the different data volumes, with the exception of ϕ , which is the surface flux. The parameters investigated were selected due to the potential predictive capability of these parameters found in other studies (e.g., Bobra and Couvidat, 2015; Kusano et al., 2020; Georgoulis et al., 2021). It is worth noting that all the investigated parameters are summed values, which was prompted by the findings of multiple studies showing that solar flares tend to be guided more by the total quantities than mean quantities (e.g., Leka and Barnes, 2007; Kazachenko et al., 2022). It is also worth highlighting that the parameters were calculated from data contained within the observed photospheric, modeled chromospheric, and modeled coronal fields. Whereas the finding of Korsós et al. (2020) shows that the optimal height for the WG_M method is 1,000-1,800 km, suggesting that the chromospheric



2D projection of the cumulative NPR leading up to the flare start (purple shading) and the areas of flare brightening through the approximate start of the eruptive/flash phase (green shading) plotted over the bounding box portion of the magnetogram closest to the flare start time for each of the 30 solar flare events in the dataset.

magnetic field may be the key driver flare physics, signatures of flare occurrence have still been found within observed photospheric data and modeled coronal data. Therefore, data from all layers of the solar atmosphere were incorporated in the hopes of capturing the dynamics involved with the flaring process at each layer.

3.4 Power spectra

In addition to the parameters calculated directly from the different data volumes/fields themselves, the power spectra of the

surface maps created for each of the parameters listed in Table 2 (with the exception of V) was calculated. This was motivated by the finding of Abramenko (2005) that the power spectrum of magnetograms is related to an AR's future flare productivity/eruptive behavior. For each data volume/field (AR and NPR) at each timestep within the 2-h window around the flare events, surface maps were created for the magnetic field parameters by summing the volume elements along the vertical z axis. E_{Free} surface maps for both the AR and NPR fields for the X5.4 flare that occurred on 7 March 2012 are provided as an example in Figure 8. Following a similar approach as Abramenko (2005), the 2D power spectrum was calculated

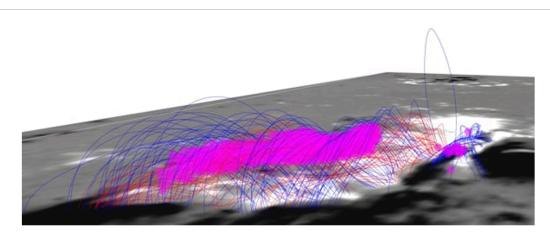


FIGURE 7 2012-03-07 00:00 UT NPR (purple) with the field lines from the 00:00 UT AR field that came into contact with the NPR. The footprints of these field lines determined the seed locations for the NPR data volumes at each timestep for this X5.4 flare event. Blue field lines indicate closed field lines with $1 \le |T_w| < 2$ and red field lines indicate closed field lines with $|T_w| \ge 2$.

TABLE 2 Investigated magnetic field parameters with associated descriptions, units, and calculations.

Description	Units	Formula
Total unsigned flux	maxwell	$\phi = \Sigma B_z dA$
Total free magnetic field energy	Joule	$E_{Free} = \sum rac{B^2 - B_{Pot}^2}{2\mu_0} dV$
Total vertical magnetic field energy	Joule	$E_{B_z}=\sumrac{B_z^2}{2\mu_0}dV$
Total vertical field gradient	G/Mm	$\nabla B_{z_{\text{Tot}}} = \sum \sqrt{\left(\frac{\partial B_z}{\partial x}\right)^2 + \left(\frac{\partial B_z}{\partial y}\right)^2}$
Total unsigned vertical current	A	$J_{z_{Tot}} = \sum J_z dA$
Total unsigned vertical current helicity	G ² /m	$H_{c_{Tot}} \propto \sum B_z J_z $
Absolute value of the net vertical current helicity	G ² /m	$H_{c_{Abs}} \propto \sum B_z J_z $
Total unsigned twist	Turns	$T_{w_{Tot}} = \sum T_{\mathbf{w}} $
Total unsigned unit magnetic twist flux	G * Turns	$\tau_{\mathrm{Tot}} = \sum T_{\mathrm{w}}B_{\mathrm{z}} $
Total unsigned unit free magnetic twist flux	G * Turns	$ \rho_{\mathrm{Tot}} = \sum T_{\mathrm{w}} B_{\mathrm{NP}} $
Total volume	Mm^3	$V = \sum dV$

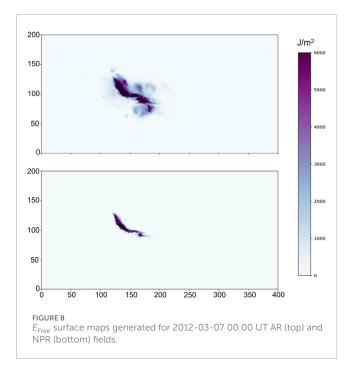
from each surface map. The total power was then calculated as the area under the power spectra curves within the wavenumber range of 0.3 rad/Mm \leq k \leq 3 rad/Mm, corresponding to the spatial scale 2Mm \leq r \leq 20 Mm, which is the ideal inertial subrange for magnetographic measurements (Abramenko, 2005). The NPR field E_{Free} power spectra for the X5.4 flare event are provided as an example in Figure 9.

4 Statistical analysis

Once the parameter data for all 30 flare events had been calculated following the methodology outlined in Section 3, superposed epoch (SPE) plots, similar to that proposed by Mason and Hoeksema (2010), were created to examine any consistent trends within the time series

of the different magnetic field parameters. Additionally, correlation coefficients between the parameters and flare properties were calculated using only data prior to the start of the flares in order to find relationships between the state of the 3D solar magnetic field leading up to an eruption and the flare characteristics. With the addition of the power spectrum calculations, there were two sets of magnetic field parameters calculated for each data volume/field at each timestep for every flare event:

- 1. The 11 parameters listed in Table 2 calculated as total quantities directly from the data volumes/fields themselves—field parameters
- 2. The total power of the same parameters (except for *V*) calculated from the power spectra of the surface maps of each parameter—power spectrum parameters.



Only the field parameters were used to produce the SPE plots, whereas both the field parameters and power spectrum parameters were used to calculate the correlation between the parameters and different flare properties. The power spectrum parameters are denoted with Pow() around the parameter symbol; for example, $Pow(J_{z_{Tot}})$ denotes the total power calculated from the $J_{z_{Tot}}$ surface map.

4.1 Superposed epoch plots

An SPE plot is a sensitive tool used to discover the average (possibly weak) response of a complex system to a particular event

(Mason and Hoeksema, 2010). The SPE plots are combinations of the individual time series for the 30 flare events in the dataset, aligned by the flare start times. Unlike the time series plotted for the case study analysis (Garland et al., 2023), which were generated from the parameters normalized to the value at the flare start time, the individual time series used in the SPE plots were generated from the field parameters normalized to the value at the start of the 2-h window around the flare event. Such normalization still allowed for effective comparison of the relative changes, but it also revealed the consistency in any trends from a forecasting perspective. The data shown in the plots are the mean and standard deviation of the individual time series.

SPE plots were produced for each data volume/field for the solar flare dataset as a whole, as well as for flare events of similar magnetic and sunspot classifications. However, as Table 1 indicates, the categorization by each specific magnetic and sunspot classifications would result in too small data subsets. In order to maintain a degree of statistical significance, data subsets were established for only the most common Mount Wilson magnetic classification and modified Zürich/McIntosh sunspot classification. Thus, SPE plots were produced for the following:

- 1. Full solar flare dataset—30 flare events (18 X-class and 12 M-class)
- Subset of flare events with a Mount Wilson magnetic classification of βγδ—22 flare events (15 X-class and 7 M-class)
- 3. Subset of flare events with any Mount Wilson magnetic classification other than $\beta y\delta$ —8 flare events (3 X-class and 5 M-class)
- Subset of flare events with modified Zürich/McIntosh largest spot (penumbra) and distribution classification 'kc'—18 flare events (13 X-class and 5 M-class)
- Subset of flare events with any modified Zürich/McIntosh largest spot (penumbra) and distribution classification other than 'kc'—12 flare events (5 X-class and 7 M-class).

The SPE plots for the full flare dataset are shown in Figures 10 and 11. Overall, the parameters that showed the most consistent

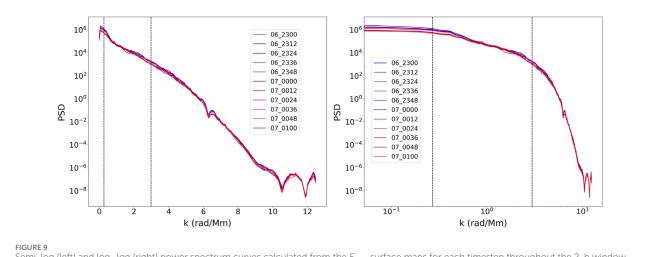
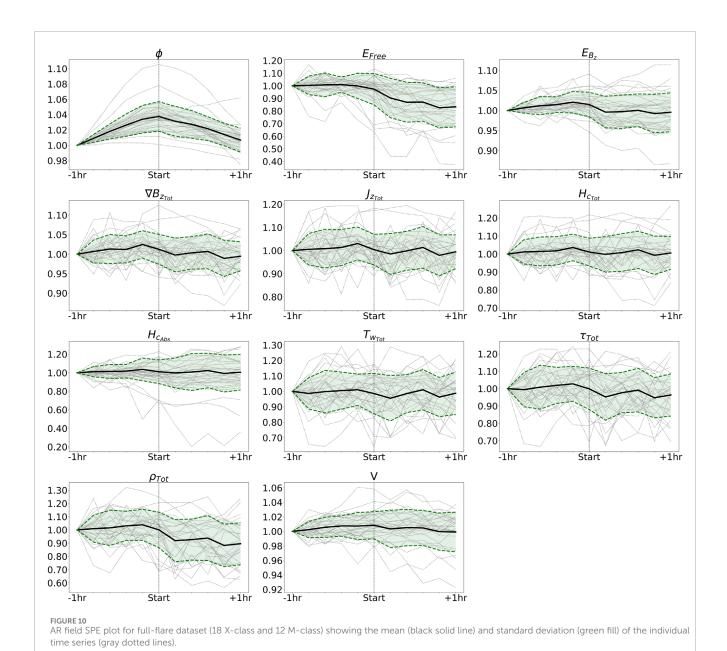


FIGURE 9 Semi-log (left) and log-log (right) power spectrum curves calculated from the E_{Free} surface maps for each timestep throughout the 2-h window around the 2012-03-07 X5.4 solar flare. The dashed vertical lines indicate the wavenumber range, in which the total power was calculated as the area under the curves.



trends among the flare events, particularly for the hour leading up to the eruption, were ϕ , E_{Free} , τ_{Tot} , and ρ_{Tot} . Consistency was based on the relative standard deviation, which was calculated as the standard deviation divided by the range of the averaged data. The parameters ϕ , E_{Free} , τ_{Tot} , and ρ_{Tot} had the four lowest relative standard deviations, respectively, and therefore will be the focus of discussion for this section. The trends seen for these parameters were the same across all the data subsets. However, it is worth noting that a greater relative change and smaller standard deviations were found for the subsets of flare events with any magnetic classification other than $\beta y \delta$ and any penumbra/distribution classification other than 'kc'. Although this could just be a result of the smaller sample sizes, it could also be due to the nature of the larger and more complex ARs, which showed greater overall variability in the evolution of the parameters, particularly after eruption. In several of the flare events with the largest and most complex ARs, the post-flare values of the parameters quickly increased back to the pre-flare values, indicating that the magnetic fields did not fully relax to less stressed states. These ARs were typically more active, in line with the well-known rule of thumb of flare persistence (Mason and Hoeksema, 2010).

The most consistent trend across all the flare events was the steady increase in ϕ for the AR field over the hour leading up to the flare start, peaking at the time of the flare, and then decreasing throughout the remainder of the event. This could be explained by the processes of flux emergence and cancellation, which have been associated with flaring activity (e.g., Nitta et al., 1996; Li et al., 2000; Wang et al., 2002; Kutsenko et al., 2021). It could also be the result of the stretching (in the vertical) and relaxing of the magnetic field for the "two-ribbon" flare model. As the strapping or envelope field lying over the expanding flux rope is stretched in the vertical, the z-component of the field and therefore ϕ increases. Once the instability

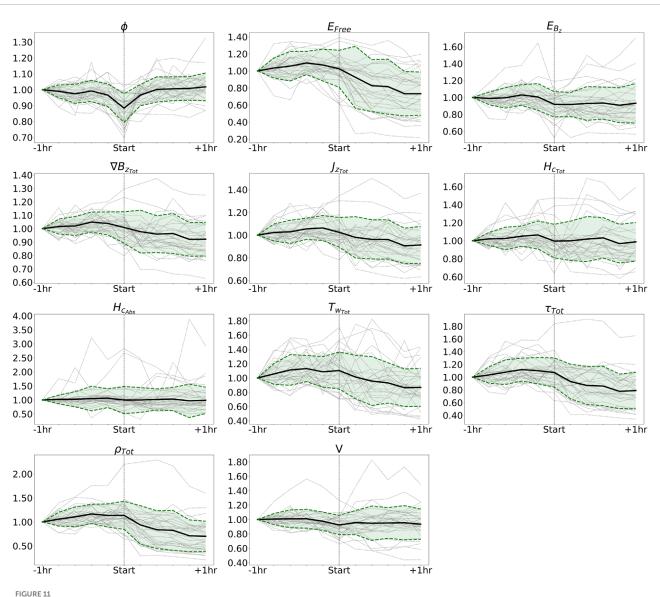


FIGURE 11

NPR field SPE plot for full-flare dataset (18 X-class and 12 M-class) showing the mean (black solid line) and standard deviation (green fill) of the individual time series (gray dotted lines).

of the magnetic field reaches the point to trigger the eruption, the magnetic field relaxes to a less stressed state in the form of the simple post-flare arcade that is no longer stretched as extensively. Leka and Barnes (2003) studied the temporal evolution of the ϕ during a similar time interval for two ARs that produced X- and M-class flares, finding "some flux growth" prior to the flares, but no post-event decrease. The difference in the observed trend for ϕ found in this study and theirs could be due to the different magnetogram data used or the higher AR defining threshold ($|B_z| \ge 300$ G) utilized in the present study. Similar to that the values in the study by Leka and Barnes (2003), the relative changes in ϕ are small, only about 1%–5%.

An opposite trend is seen for ϕ for the NPR field, where on average, there was approximately 10% decrease over the two timesteps leading up to the start of a flare, followed by a roughly equal increase over one to two timesteps after the flare start (Figure 11). Relating to the changing structure of the magnetic field,

this can be explained by the shearing and reconnecting of the non-potential field lines associated with the SMA/MFR structures as the field destabilizes, leading up to the flare, and then relaxes into the post-flare arcade after the eruption. Essentially, field lines in close proximity to the expanding flux rope reconnect below the flux rope, causing them to wrap around the twisted axis. As these field lines become a part of the flux rope, they become more elongated in the horizontal, leading to a decrease in the z-component of that portion of the magnetic field. Following the eruption and decay of the flux rope, the post-flare arcade sets up with more vertically oriented, simple loop structures compared to the flux rope that was present prior to eruption. Higher cadence data would be useful to further examine the rate of this "dip" in ϕ for the NPR field around the start of the flare.

On average, for the NPR field, there is an initial increase in E_{Free} until 24 min before flare start, followed by a slight decrease

TABLE 3 Summary of r_s values calculated from the AR data volumes for the field parameters and flare properties. The coefficients shown are the maximum r_s values from the different timesteps leading up to the flare start time. Weak correlations are highlighted in red, moderate in yellow, strong in green, and very strong in blue.

	Peak flux	Duration	Rise time	Decay time	Impulsiveness	Integrated flux
φ	0.17	0.40	0.28	0.43	-0.09	0.52
E_{Free}	0.44	0.29	0.25	0.31	0.16	0.57
E_{B_z}	0.22	0.36	0.22	0.42	-0.01	0.53
$\nabla B_{z_{Tot}}$	0.19	0.41	0.31	0.44	-0.11	0.54
$J_{z_{Tot}}$	0.19	0.40	0.31	0.40	-0.12	0.50
$H_{c_{Tot}}$	0.31	0.32	0.24	0.35	0.08	0.54
$H_{c_{Abs}}$	0.38	0.54	0.40	0.60	-0.02	0.77
$T_{w_{Tot}}$	-0.06	0.41	0.35	0.36	-0.30	0.35
$ au_{ ext{Tot}}$	0.19	0.44	0.36	0.42	-0.16	0.52
$ ho_{ m Tot}$	0.25	0.41	0.38	0.38	-0.12	0.54
V	0.07	0.35	0.25	0.31	-0.14	0.35
ϕ/E_{Free}	-0.49	0.16	0.08	0.16	-0.41	-0.19
E_{B_z}/E_{Free}	-0.25	0.38	0.22	0.39	-0.34	0.19
$\nabla B_{z_{Tot}}/E_{Free}$	-0.51	0.11	0.04	0.10	-0.40	-0.24
$J_{z_{Tot}}/E_{Free}$	-0.54	0.04	-0.03	-0.05	-0.39	-0.36
$H_{c_{Tot}}/E_{Free}$	-0.42	0.13	0.04	0.16	-0.33	-0.16
$H_{c_{Abs}}/E_{Free}$	-0.14	0.44	0.27	0.53	-0.26	0.34
$T_{w_{Tot}}/E_{Free}$	-0.49	-0.07	-0.10	-0.12	-0.35	-0.41
$ au_{Tot}/E_{Free}$	-0.49	0.16	0.14	0.12	-0.45	-0.23
$ ho_{Tot}/E_{Free}$	-0.50	0.04	0.05	-0.06	-0.43	-0.36
V/E_{Free}	-0.45	0.11	0.06	0.07	-0.37	-0.25

up to the flare start and a more significant decrease from the flare start to 1 h after. The mean dissipated energy is $41\% \pm 19\%$ of the maximum free energy, which is lower yet overlapping with the $60\% \pm 26\%$ found by Aschwanden (2019). The initial decrease in E_{Free} following the peak just before the flare start suggests that the free magnetic pressure reaches a point where the field can no longer fully contain it and it starts to "leak" out. This "leaking" of the pressure and slight loss of free energy is likely brought about by the ongoing reconnection as the field destabilizes but before the critical point of destabilization is reached and the bulk of the energy is released. In other words, once enough free energy has been built up and the free or non-potential magnetic pressure is high enough, each reconnection event that occurs before the eruptive instability is reached releases a small amount of the free energy. It is plausible that these small releases of the free energy

just before the eruption are associated with the short-lived small-scale brightening seen in UV and EUV imagery (e.g., Leka et al., 2023).

It should be noted that while the trend just discussed was the average trend seen in many of the 30 flare events investigated, some events did show more a more variable evolution of E_{Free} , with intermittent instances of energy buildup and dissipation superimposed on the overall change of higher pre-flare energy to lower post-flare energy. Other studies that have analyzed the temporal evolution of E_{Free} estimated from NLFFF extrapolation have reported only step function decreases in E_{Free} following the occurrence of the strong flares examined (Thalmann and Wiegelmann, 2008; Murray et al., 2013; Sun et al., 2012), in line with the store-and-release concept for solar eruptions. However, the findings of Aschwanden

TABLE 4 Summary of r_s values calculated from the AR data volumes for the power spectrum parameters and flare properties. The coefficients shown are the maximum r_s values from the different timesteps leading up to the flare start time. Weak correlations are highlighted in red, moderate in yellow, strong in green, and very strong in blue.

	Peak flux	Duration	Rise time	Decay time	Impulsiveness	Integrated flux
$Pow(\phi)$	0.35	0.16	0.15	0.22	0.19	0.45
$Pow(E_{Free})$	0.55	-0.35	-0.27	-0.32	0.57	0.10
$Pow(E_{B_z})$	0.36	0.23	0.13	0.31	0.20	0.51
$Pow\left(\nabla B_{z_{Tot}}\right)$	0.44	0.09	0.15	0.13	0.29	0.41
$Pow(J_{z_{Tot}})$	0.41	-0.07	-0.03	-0.05	0.33	0.30
$Pow(H_{c_{Tot}})$	0.50	-0.10	-0.11	-0.05	0.44	0.31
$Pow(H_{c_{Abs}})$	0.50	-0.09	-0.11	-0.04	0.45	0.32
$Pow(T_{w_{Tot}})$	0.22	0.23	0.31	0.18	-0.09	0.42
$Pow(au_{ ext{Tot}})$	0.38	0.22	0.25	0.23	0.20	0.50
$\mathit{Pow}(ho_{\mathrm{Tot}})$	0.47	-0.10	0.09	-0.08	0.35	0.29
$Pow(\phi/E_{Free})$	-0.52	0.52	0.46	0.50	-0.67	0.16
$Pow(E_{B_z}/E_{Free})$	-0.39	0.62	0.50	0.62	-0.60	0.36
$Pow\left(\nabla B_{z_{Tot}}/E_{Free}\right)$	-0.48	0.56	0.54	0.55	-0.70	0.23
$Pow(J_{z_{Tot}}/E_{Free})$	-0.49	0.59	0.52	0.55	-0.68	0.22
$Pow(H_{c_{Tot}}/E_{Free})$	-0.25	0.52	0.38	0.53	-0.41	0.34
$Pow(H_{c_{Abs}}/E_{Free})$	-0.24	0.51	0.38	0.52	-0.41	0.34
$Pow(T_{w_{Tot}}/E_{Free})$	-0.50	0.45	0.39	0.42	-0.63	0.06
$Pow(au_{Tot}/E_{Free})$	-0.49	0.63	0.55	0.59	-0.72	0.26
$Pow(\rho_{Tot}/E_{Free})$	-0.36	0.53	0.61	0.42	-0.65	0.22

(2019) and the present study suggest that the evolution of energy during solar flares is more complex than a single-step function, exhibiting a more fragmentary and impulsive nature. The different findings could be the result of different temporal resolution, extrapolation techniques, and/or the portion of the modeled 3D solar magnetic field from which E_{Free} was calculated.

The evolution of τ_{Tot} and ρ_{Tot} for the NPR field, on average, is similar to that of E_{Free} , which was expected. For the majority of flare events examined, $|T_{\mathrm{w}}|$ either increased or remained fairly constant in the hour before flare start and then decreased following the eruption as the field relaxed. This was more evident in the flare events where highly twisted $(|T_{\mathrm{w}}| \geq 2)$ structures were present in the pre-flare field configuration than in events where the pre-flare twist was more moderate $(|T_{\mathrm{w}}| \approx 1)$, which saw a more variable evolution of twist. Considering τ_{Tot} and ρ_{Tot} are essentially $T_{w_{\mathrm{Tot}}}$ weighted by $|B_{\mathrm{z}}|$ and $|B_{\mathrm{NP}}|$, respectively, the evolution of τ_{Tot} and ρ_{Tot} is also a factor in the evolution of the vertical and non-potential fields, which is indicated by E_{B_z} and E_{Free} .

4.2 Correlation with flare properties

Similar to the study by Kazachenko et al. (2017), the relationship between different flare properties and the magnetic field parameters was quantitatively described by the Spearman ranking correlation coefficient (r_s), which measures the monotonic relationship between two variables. The different flare properties are as follows:

- 1. GOES measured peak X-ray flux in W/m^2 .
- 2. Duration from the start to the end in seconds.
- 3. Rise time—the difference between the flare start and max times, in seconds.
- Decay time—the difference between the flare max and end times, in seconds.
- 5. Impulsiveness—the ratio of peak X-ray flux to rise time, in W/m^2s .
- 6. GOES reported integrated flux in J/m^2 .

The method of bootstrapping (Efron and Tibshirani, 1986) was used to estimate the uncertainty in the correlation coefficient due to

TABLE 5 Summary of r_s values calculated from the NPR data volumes for the field parameters and flare properties. The coefficients shown are the maximum r_s values from the different timesteps leading up to the flare start time. Weak correlations are highlighted in red, moderate in yellow, strong in green, and very strong in blue.

	Peak flux	Duration	Rise time	Decay time	Impulsiveness	Integrated flux
φ	0.34	0.09	0.11	0.07	0.17	0.31
E_{Free}	0.46	-0.18	-0.16	-0.18	0.44	0.22
E_{B_z}	0.41	0.12	0.14	0.12	0.21	0.42
$ abla B_{z_{Tot}}$	0.36	0.16	0.20	0.12	0.15	0.33
$J_{z_{Tot}}$	0.32	0.08	0.11	0.05	0.17	0.27
$H_{c_{Tot}}$	0.44	-0.20	-0.13	-0.20	0.40	0.15
$H_{c_{Abs}}$	0.36	-0.27	-0.25	-0.27	0.45	0.05
$T_{w_{Tot}}$	0.08	0.43	0.42	0.35	-0.30	0.36
$ au_{ m Tot}$	0.27	0.36	0.36	0.30	-0.09	0.46
$ ho_{ m Tot}$	0.33	0.22	0.25	0.16	0.13	0.38
V	0.08	0.35	0.34	0.28	-0.23	0.28
ϕ/E_{Free}	-0.53	0.35	0.35	0.34	-0.64	-0.07
E_{B_z}/E_{Free}	-0.35	0.52	0.49	0.52	-0.58	0.36
$ abla B_{z_{Tot}}/E_{Free}$	-0.51	0.53	0.53	0.47	-0.76	0.14
$J_{z_{Tot}}/E_{Free}$	-0.59	0.43	0.45	0.37	-0.75	-0.09
$H_{c_{Tot}}/E_{Free}$	-0.37	-0.17	0.14	-0.17	-0.30	-0.27
$H_{c_{Abs}}/E_{Free}$	-0.35	-0.38	-0.23	-0.37	-0.10	-0.46
$T_{w_{Tot}}/E_{Free}$	-0.50	0.59	0.57	0.51	-0.75	0.21
$ au_{Tot}/E_{Free}$	-0.48	0.67	0.66	0.60	-0.76	0.33
$ ho_{Tot}/E_{Free}$	-0.45	0.69	0.70	0.57	-0.81	0.29
V/E_{Free}	-0.47	0.48	0.47	0.40	-0.69	0.12
(ϕ/E_{Free}) $H_{c_{Abs_{AR}}}$	0.14	0.75	0.61	0.80	-0.37	0.77
$\left(E_{B_z}/E_{Free}\right)\ H_{c_{Abs_{AR}}}$	0.26	0.69	0.58	0.73	-0.27	0.82
$\left(\nabla B_{z_{Tot}}/E_{Free}\right)\ H_{c_{Abz_{AR}}}$	0.14	0.76	0.63	0.80	-0.36	0.79
$\left(J_{z_{Tot}}/E_{Free}\right)H_{c_{Abs_{AR}}}$	0.17	0.74	0.63	0.77	-0.36	0.81
$\left(H_{c_{Tot}}/E_{Free}\right)\ H_{c_{Abs_{AR}}}$	0.31	0.56	0.45	0.63	-0.10	0.76
$(H_{c_{Abs}}/E_{Free})$ $H_{c_{Abs_{AR}}}$	0.26	0.32	0.22	0.38	0.13	0.51
$\left(T_{w_{Tot}}/E_{Free}\right)\ H_{c_{Abs_{AR}}}$	-0.14	0.85	0.73	0.82	-0.60	0.69
(au_{Tot}/E_{Free}) $H_{c_{Abs_{AR}}}$	0.09	0.83	0.72	0.83	-0.48	0.82
(ho_{Tot}/E_{Free}) $H_{c_{Abs_{AR}}}$	0.19	0.76	0.64	0.76	-0.35	0.77
(V/E_{Free}) $H_{c_{Abs_{AR}}}$	-0.10	0.83	0.69	0.82	-0.56	0.66

TABLE 6 Summary of r_s values calculated from the NPR data volumes for the power spectrum parameters and flare properties. The coefficients shown are the maximum r_s values from the different timesteps leading up to the flare start time. Weak correlations are highlighted in red, moderate in yellow, strong in green, and very strong in blue.

	Peak flux	Duration	Rise time	Decay time	Impulsiveness	Integrated flux
$Pow(\phi)$	0.53	-0.19	-0.14	-0.17	0.45	0.23
$Pow(E_{Free})$	0.62	-0.48	-0.38	-0.48	0.71	-0.07
$Pow(E_{B_z})$	0.54	-0.13	-0.06	-0.12	0.41	0.32
$Pow(\nabla B_{z_{Tot}})$	0.54	-0.45	-0.31	-0.44	0.58	-0.08
$Pow(J_{z_{Tot}})$	0.53	-0.51	-0.38	-0.49	0.64	-0.13
$Pow(H_{c_{Tot}})$	0.50	-0.50	-0.43	-0.50	0.66	-0.14
$Pow(H_{c_{Abs}})$	0.50	-0.50	-0.43	-0.49	0.66	-0.13
$Pow(T_{w_{Tot}})$	0.27	0.43	0.51	0.34	-0.23	0.49
$\mathit{Pow}(au_{\mathrm{Tot}})$	0.46	0.11	0.18	0.07	0.30	0.36
$Pow(ho_{ m Tot})$	0.48	-0.24	-0.16	-0.25	0.47	0.13
$Pow(\phi/E_{Free})$	-0.51	0.59	0.52	0.56	-0.72	0.21
$Pow(E_{B_z}/E_{Free})$	-0.30	0.59	0.54	0.59	-0.57	0.41
$Pow\left(\nabla B_{z_{Tot}}/E_{Free}\right)$	-0.48	0.50	0.51	0.45	-0.69	0.18
$Pow(J_{z_{Tot}}/E_{Free})$	-0.46	0.36	0.36	0.32	-0.57	-0.03
$Pow(H_{c_{Tot}}/E_{Free})$	-0.24	-0.08	-0.05	-0.10	-0.16	-0.19
$Pow(H_{c_{Abs}}/E_{Free})$	-0.24	-0.12	-0.10	-0.13	-0.14	-0.24
$Pow(T_{w_{Tot}}/E_{Free})$	-0.39	0.70	0.69	0.60	-0.75	0.37
$Pow(au_{Tot}/E_{Free})$	-0.41	0.75	0.72	0.67	-0.75	0.44
$Pow(\rho_{Tot}/E_{Free})$	-0.31	0.68	0.68	0.55	-0.67	0.35

sampling. Specifically, r_s was calculated 10^4 times for 30 randomly selected data pairs from the dataset with replacement. The mean r_s calculated from the bootstrap method was the reported r_s for the particular parameter and flare property correlation, with the standard deviation of r_s reported as the correlation's statistical uncertainty. In addition to r_s , the p-value (p) and its uncertainty were calculated as well. The commonly used thresholds for r_s to express the qualitative strength of the correlation are as follows: $|r_s| \in [0.0, 0.4)$ —weak, $|r_s| \in [0.4, 0.6)$ —moderate, $|r_s| \in [0.6, 0.8)$ —strong, and $|r_s| \in [0.8, 1.0]$ —very strong (Dodge, 2008). For strong and very strong correlation coefficients, the relationship between the parameter and flare property was fitted with a power-law function of the form

$$Y = aX^{b}, (3)$$

where Y is the flare property and X is the magnetic field parameter. The scaling factor, a, and exponent, b, were found using linear regression in the log–log space.

The process of correlation coefficient calculation was carried out for each data volume/field (AR and NPR), each set of parameters (field parameters and power spectrum parameters), and each timestep leading up to flare start, as well as the sum across the timesteps leading to the start. Tables 3 and 4 provide a summary of r_s values calculated from the AR data volumes for the field parameters and power spectrum parameters, respectively. Tables 5 and 6 provide the same for the NPR data volumes. Listed in the tables are the maximum r_s values from the different timesteps for each parameter and flare property examined.

4.2.1 Individual parameters

For the individual parameters (the top rows of Tables 3–6), the peak flux is strongly correlated with $Pow(E_{Free})$; impulsiveness is strongly correlated with $Pow(E_{Free})$, $Pow(J_{z_{Tot}})$, $Pow(H_{c_{Tot}})$, and $Pow(H_{c_{Abs}})$; and the decay time and integrated flux are strongly correlated with the net current helicity, $H_{c_{Abs}}$. The strongest correlation was between the integrated flux and

 $H_{c_{Abs}}$, with $r_s=0.77\pm0.08$ at 24 min before the flare start. The strong relationship between $H_{c_{Abs}}$ and the integrated flux could be explained by the eruption associated with solar flares acting as a catalyst for further reconnection of field lines of the AR field near the point of eruption. Essentially, the more complex the AR field is near the eruption, the more primed the field lines are for reconnection events that are prompted by the explosive motions, which dissipates additional free energy, leading to greater integrated flux. The post-flare reconnection within the complex portions of the AR field would also act to prolong the decay time of the flare event; hence, there is a strong correlation between $H_{c_{Abs}}$ and decay time as well.

The relationship found here between $H_{c_{Abs}}$ and the integrated flux and decay time is not surprising. Solar flares with longer decay times, leading to greater integrated flux, are typically associated with CME occurrence. The statistical analysis performed by Kawabata et al. (2018) for 211 M- and X-class solar flares showed very strong Spearman correlation coefficients between the flare decay time and CME occurrence. Several studies that have investigated the magnetic helicity of active ARs have shown that helicity-based parameters are promising candidates for discriminating between ARs that produce eruptive (CME associated) and those that produce confined (no CME) solar flares. Recent work using MHD (e.g., Pariat, E. et al., 2017; Zuccarello et al., 2018) and NLFFF (e.g., James et al., 2018; Thalmann et al., 2020; Gupta et al., 2021) simulations suggests that the eruptive potential of an AR can be characterized by the helicity ratio $(|H_I|/|H_V|)$, which is the ratio of the current-carrying helicity to the total helicity. It is worth highlighting that in addition to differing simulation methods, only the vertical current helicity was calculated in the present study and not the helicity ratio. Still, the findings here regarding $H_{c_{Abs}}$ seem to be in line with the aforementioned studies, suggesting that helicity plays an important role in solar eruptions and helicity-based parameters have predictive potential.

The strong correlation between the $Pow(E_{Free})$ and peak flux was expected, given that numerous studies have found predictive capability with the parameter E_{Free} regarding flare activity (e.g., Yamamoto and Sakurai, 2009; Bobra and Couvidat, 2015; Aschwanden, 2019). Although the correlation between E_{Free} and peak flux was only moderate, the correlation plots from each timestep, as well as the sum across timesteps, did show a welldefined upper limit to peak flux that was fitted with a quadratic function (see Figure 12). $Pow(E_{Free})$, $Pow(J_{z_{Tot}})$, $Pow(H_{c_{Tot}})$, and $Pow(H_{c_{Abc}})$ all correlate strongly with the impulsiveness of the solar flares, with $Pow(E_{Free})$ having the strongest correlation of $r_s = 0.71 \pm 0.10$ at 60 min before the flare start. At least in regard to the individual parameters, it is possible that the power spectrum parameters correlate more strongly with impulsiveness, given that their calculation is focused on the inertial subrange, that is, the length scale over which energy is transferred. However, as will be discussed in Section 4.2.2., the ratios of the parameters calculated from the field parameters have higher correlation coefficients overall than the power spectrum parameters.

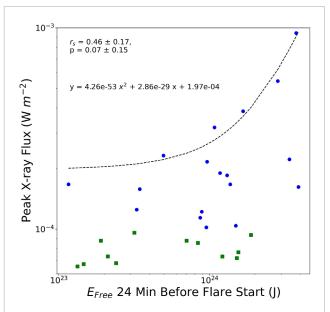


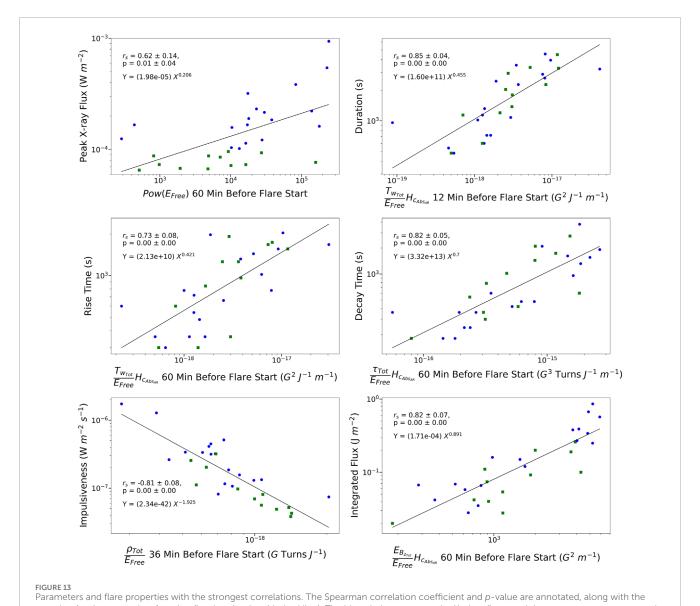
FIGURE 12 NPR field E_{Free} 24 min before flare start vs. peak X-ray flux. The Spearman correlation coefficient and p-value are annotated, along with the equation for the curve fitted to the apparent relationship for maximum possible peak flux (dashed line). The blue circles represent the X-class flares and the green squares represent the M-class flares.

4.2.2 Free magnetic energy ratio parameters

Given the well-documented relationship of E_{Free} to flaring activity, as well as the strong correlations with the peak flux and impulsiveness just discussed, the next step in examining the relationship of the parameters with the different flare properties was to analyze the ratio of the parameters to the free energy (the bottom rows of Tables 3; 4, and 6; the middle rows of Table 5). The ratios of both sets of parameters were found to correlate well with flare impulsiveness. Strong correlations were found between the power spectrum parameter ratios and the flare duration, rise time, decay time, and impulsiveness for both AR and NPR fields. Strong to very strong correlations were found between the field parameter ratios and the same flare properties for the NPR field. Overall, the power spectrum parameter ratios had stronger correlations for the duration, rise time, and decay time, whereas the field parameter ratios had stronger correlations with the impulsiveness. The strongest correlations for the free energy ratios across both sets of parameters were between $Pow(\tau_{Tot}/E_{Free})$ and flare duration, rise time, and decay time, with $r_s = 0.75 \pm 0.06$, $r_s = 0.72 \pm 0.09$, and $r_s = 0.72 \pm 0.09$ = 0.67 \pm 0.08; and between (ρ_{Tot}/E_{Free}) and impulsiveness, with r_s = -0.81 ± 0.08 .

4.2.3 Weighted net current helicity

As discussed in Section 4.2.1., the $H_{c_{Abs}}$ of the AR field correlates strongly with the integrated flux, which is likely a result of the eruption acting as a catalyst for further reconnection (which dissipates additional energy) of field lines of the AR field that are highly helical and primed for reconnection. Therefore, the $H_{c_{Abs}}$ of the AR field provides a good indication of the nature



equation for the power-law function fitted to the data (dashed line). The blue circles represent the X-class flares and the green squares represent the M-class flares of the event following the initial eruption; hence, there is a

strong correlation with the decay time as well. Presumably, if combined with a parameter that provided a good indication of the nature of the eruption itself, the combination would relate well to the event as a whole and theoretically correlate more strongly with the integrated flux. To test this, the $H_{c_{Ahs}}$ of the AR field was weighted by the field parameter free energy ratios of the NPR field, which had strong to very strong r_s values with impulsiveness, that is, providing a good indication of whether the solar flare eruption will be more impulsive or more gradual. The correlation coefficients between the flare properties and the weighted $H_{c_{Abc}}$ parameters are shown in the bottom rows of Table 5. As expected, strong to very strong correlations were found for the duration, decay time, and integrated flux. The strongest correlations for the weighted $H_{c_{Ahs}}$ parameters were between $\left(T_{w_{Tot}}/E_{Free}\right)H_{c_{Abs_{AR}}}$ and flare duration, with $r_s=0.85\pm0.05;$ between $\left(\tau_{Tot}/E_{Free}\right)H_{c_{Abs_{AR}}}$ and decay time, with $r_s=0.83\pm0.06;$ and between (E_{B_z}/E_{Free}) $H_{c_{Abs,a,p}}$ and integrated flux, with $r_s = 0.82$ ± 0.07.

4.2.4 Overall

Figure 13 provides the correlation plots for the parameters with the strongest correlation coefficients for each flare property, annotated with the corresponding $r_s \pm \triangle r_s$, $p \pm \triangle p$, and powerlaw function. The timestep with the strongest correlations was 60 min before the flare start. However, the range of r_s values was generally consistent across the different timesteps.

Although the correlation coefficients found are similar to those of other statistical studies that have examined the same flare properties (e.g., Yamamoto and Sakurai, 2009; Kazachenko et al., 2017; 2022; Reep and Knizhnik, 2019), it is worth highlighting that the data used to calculate r_s in the present study were all within the hour before flare occurrence. In addition to furthering the space weather community's investigation and understanding of

the physical processes involved in solar flares, the findings from the present study more directly benefit flare forecasting. Using the power-law functions in Figure 13 and the fitted quadratic function in Figure 12, the properties of a flare can be well estimated up to an hour before it is triggered. In theory, estimates of the properties could be continuously calculated with the influx of near real-time HMI data, providing a constant approximation to the nature of any strong flare that may occur within an hour's time. This of course assumes that the relationships found in this analysis using the wellcalibrated HMI data hold true for the near real-time (NRT) HMI data series, which does not go through the same data processing. Alternatively, quasi real-time magnetic field extrapolations could be obtained through the method put forth by Jarolim et al. (2023), which utilizes a neural network that integrates observational data and a NLFFF model, from which estimates of flare properties could be calculated efficiently for forecasting purposes.

5 Conclusion

5.1 Summary

In this study, the 3D solar magnetic field was modeled using optimization-based NLFFF extrapolation during 30 strong and extreme solar flare events. Specifically, 3D magnetic fields were modeled using the 12-min cadence HMI photospheric vector magnetograms, spanning a time period of 1 hour before through 1 hour after the start of 18 X-class flares and 12 M-class (greater than M6.5) flares. Using the modeled data, several magnetic field parameters were calculated from the fields directly, as well as from the power spectrum of surface maps generated by summing the fields along the vertical axis, for the following two different regions:

- 1. Active region (AR): areas with photospheric $|B_z| \ge 300$ G.
- 2. Non-potential region (NPR): areas above the photosphere with B_{NP} greater than three standard deviations above $\overline{|B_{NP}|}$ of the AR field and either $|T_{\rm w}| \ge 1$ turn or $\Psi \ge 80^{\circ}$.

The superposed epoch (SPE) plots of the magnetic field parameters were analyzed to investigate the evolution of the 3D solar field during the solar flare event and discern consistent trends across all solar flare events in the dataset, as well as across subsets of flare events categorized by their Mount Wilson magnetic classification and modified Zürich/McIntosh sunspot classification. The relationship between the different flare properties (peak X-ray flux, duration, rise time, decay time, impulsiveness, and integrated flux) and the magnetic field parameters was quantitatively described by the Spearman ranking correlation coefficient, r_s . In addition to the individual parameters, ratios of the parameters to the free energy, as well as the net current helicity of the AR fields weighted by those ratios, were included in the list of parameters from which correlation with the flare properties were calculated. The key results of the study are as follows:

For the majority of the 30 flare events in the dataset, the NPR
aligned well with the area of initial flare brightening through
the start of the eruptive/flash phase. The alignment was worse
for events where the magnetic field configuration was more
conducive to emerging-flux type flares, that is, the AR did

not have a well-defined PIL or the flare occurred on the edge of the AR away from an inversion line *versus* directly over one. Overall, the NPR provides a good indication of where within the magnetic field over an AR an eruption will occur if triggered.

- 2. The parameter that showed the most consistent and discernable trends among the flare events, particularly for the hour leading up to the eruption, was the total unsigned flux (ϕ) . For the AR field, ϕ showed a consistent increase up to the start of the flare, followed by a steady decrease following the eruption. This could be the result of flux emergence and cancellation on the timescale of minutes, or the vertical stretching and relaxing of the magnetic field lying over highly twisted/sheared portion of the field from which the eruption is triggered. The opposite was seen for ϕ for the NPR field, which showed a "dip" within one to two timesteps around the flare start.
- 3. The parameter that showed the second most consistent and discernable trend was E_{Free} . On average, for the NPR field, E_{Free} peaked around 24 min before flare start, and then decreased slightly up until the start, at which point a more significant decrease from the flare start to 1 h after occurred. The mean dissipated energy was found to be 41% ± 19% of the maximum free energy, which is lower yet overlapping with the 60% \pm 26% found by Aschwanden (2019). The decreases in E_{Free} prior to eruption could be associated with short-lived small-scale brightening seen in UV and EUV imagery (e.g., Leka et al., 2023). The intermittent instances of energy buildup and dissipation superimposed on the overall change of higher pre-flare energy to lower post-flare energy suggest a more fragmentary and impulsive evolution of the free energy during solar flare events than the single-step function of the storeand-release model, which is consistent with the findings of Aschwanden (2019).
- 4. Greater consistency in the evolution of the magnetic field parameters during the solar flare events was found for the subsets of any magnetic classification other than $\beta y \delta$ and any penumbra/distribution classification other than 'kc'. In several of the flare events with the largest and most complex ARs, the post-flare values of the parameters quickly increased back to pre-flare values, indicating that the magnetic field did not fully relax to a less stressed state.
- 5. A strong correlation ($r_s = 0.62 \pm 0.14$) was found for the NPR data volumes/fields between $Pow(E_{Free})$ 60 min before flare start and the peak X-ray flux, whereas only moderate correlation was found between E_{Free} and peak flux. $Pow(E_{Free})$ denotes the total power calculated from the E_{Free} surface map generated by summing the NPR data volumes along the vertical axis. It is possible that the power spectrum parameter correlated more strongly given that its calculation is focused on the inertial subrange, that is, the length scale over which energy is transferred. However, although the correlation between E_{Free} and peak flux was only moderate, correlation plots from each timestep, as well as the sum across timesteps, did show a rather well-defined upper limit to peak flux.
- 6. Strong to very strong correlations were found between the ratio of the parameters to the free energy and impulsiveness, for both sets of parameters (field parameters and power spectrum

parameters) calculated from the NPR data volumes/fields. The strongest correlation with impulsiveness was between (ρ_{Tot}/E_{Free}) , with $r_s=-0.81\pm0.08$.

7. Given that the net current helicity of the AR field provided a good indication of the nature of the flare event following the initial eruption (strong correlation with decay time and integrated flux) and some of the free energy ratios provided a good indication of the nature of the eruption itself (strong to very strong correlation with impulsiveness), it was hypothesized that weighting the net current helicity of the AR field by the free energy ratios would relate well to the event as a whole and correlate more strongly with the integrated flux. This was confirmed with very strong correlations found for the duration, decay time, and integrated flux. The strongest correlations for the weighted $H_{c_{Abs}}$ parameters were between $(T_{w_{Tot}}/E_{Free})$ $H_{c_{Abs_{AR}}}$ and flare duration, with $r_s = 0.85 \pm 0.05$; between (τ_{Tot}/E_{Free}) $H_{c_{Abs_{AR}}}$ and decay time, with $r_s = 0.83 \pm$ 0.06; and between (E_{B_z}/E_{Free}) $H_{c_{Abs_{AB}}}$ and integrated flux, with $r_{\rm s} = 0.82 \pm 0.07$.

The findings of this study suggest that the specific magnetic field parameters calculated from the identified portions of the modeled 3D magnetic field have potential predictive capability and could benefit flare forecasting efforts. The location of a flare within an AR if triggered can be forecasted reasonably well through identifying the NPR. Although a perfectly consistent, distinct signature that specifies the exact timing of flare occurrence may not be seen in the time series of the parameters calculated from the modeled magnetic field, the destabilization of the field that is conducive to an eruption is observable. The relationships discussed in this study, calculated solely from data that were within an hour timeframe leading up to flare occurrence, could provide reasonable estimates of the flare properties of any strong/extreme flare that may occur within an hour's time.

5.2 Limitations and future work

While the trends and relationships found from the statistical analysis show high potential for flare forecasting, a major limitation of the study is the number of events included in the dataset. Although as a rule of thumb a minimum of 30 observations is generally considered sufficient to conduct significant statistics, the confidence in the results is limited. Thus, the next logical step would be to expand the dataset, initially including more X- and M-class flares, then expanding into the lower-class flares as well to find possible differences between the weaker and stronger flares. Following the initial expansion of more flare events, the next step would be to include data from non-flaring ARs to test whether the trends that hold consistent across flare events are discriminating in regards to flare occurrence.

Another limitation of the study is the use of only a single model; therefore, it was not able to determine if the findings are an artifact of the specific model used. To make such a determination, the analysis could be re-performed following the exact same procedures, only utilizing different models to extrapolate the 3D solar magnetic field. If the trends and relationships found continue to hold for varying extrapolation techniques, it would

increase the confidence that the findings are grounded in the actual physical processes occurring within the solar magnetic field during flare events. Of particular interest would be the use of models that utilize physics-informed neural networks, such as the method of Jarolim et al. (2024), which builds upon the work of Jarolim et al. (2023) by incorporating chromospheric magnetic field measurements into the extrapolation process to generate more realistic field simulations. The inclusion of the chromospheric data helps correct the lower portions of the solar magnetic field, where the force-free assumption is not valid due to the dense plasma conditions present. As discussed in the study by Korsós et al. (2024), such neural network-based methods provide more realistic field extrapolations with considerable improvement in computational efficiency compared to the standard NLFFF extrapolation, proving more suitable with respect to real-time flare forecasting application.

Finally, the 12-min cadence between observations of the standard $hmi.B_720s$ dataset brings about another limitation: for time scales less than 12 min, for example, flare eruptions, changes in the magnetic field are lost. Sun et al. (2017) created a new high-cadence vector magnetogram dataset for HMI that is more suited for investigating the evolution of the magnetic field during such quick phenomena. The 135-s cadence series $hmi.B_135s$ has the same format and is processed with nearly identical pipeline options as the 720-s data (Sun et al., 2017). Although the noise level in the field strength for the higher cadence dataset is about 50 G higher than that of the standard dataset, measurements in the strong-field regions ($|B| \ge 300 \, \mathrm{G}$) agree well between the two. Performing the same analysis with the higher cadence could highlight signatures that were potentially missed with the standard 12-min cadence dataset.

Data availability statement

Publicly available datasets were analyzed in this study. These data can be found here: http://jsoc.stanford.edu/ajax/exportdata.html.

Author contributions

SG: writing-review and editing, writing-original draft, methodology, investigation, formal analysis, and conceptualization. VY: writing-review and editing, resources, and investigation. RL: writing-review and editing and investigation. BA: writing-review and editing. DE: investigation, writing-review and editing, and supervision.

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that could be construed as a potential conflict of interest.

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Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships

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