MATERIALS SCIENCE

Out-of-plane ferroelectricity and robust magnetoelectricity in quasi-two-dimensional materials

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Thin-film ferroelectrics have been pursued for capacitive and nonvolatile memory devices. They rely on polarizations that are oriented in an out-of-plane direction to facilitate integration and addressability with complementary metal-oxide semiconductor architectures. The internal depolarization field, however, formed by surface charges can suppress the out-of-plane polarization in ultrathin ferroelectric films that could otherwise exhibit lower coercive fields and operate with lower power. Here, we unveil stabilization of a polar longitudinal optical (LO) mode in the n=2 Ruddlesden–Popper family that produces out-of-plane ferroelectricity, persists under open-circuit boundary conditions, and is distinct from hyperferroelectricity. Our first-principles calculations show the stabilization of the LO mode is ubiquitous in chalcogenides and halides and relies on anharmonic trilinear mode coupling. We further show that the out-of-plane ferroelectricity can be predicted with a crystal-lographic tolerance factor, and we use these insights to design a room-temperature multiferroic with strong magnetoelectric coupling suitable for magneto-electric spin-orbit transistors.



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INTRODUCTION

Ferroelectrics have been intensively studied since the discovery of BaTiO₃ and are of modern interest because of their ability to achieve bistable electrical polarizations that can be used in nonvolatile memory devices (1-5). Recently, Hf-based ferroelectrics have demonstrated a path to achieve complementary metal-oxide semiconductor (CMOS)-compatible ferroelectric integration; however, they suffer from a variety of limitations, including sizable leakage, and large coercivity, especially in ultrathin films that lead to poor energy efficiencies (6-11). For device integration and miniaturization, the ferroelectric polarization should be oriented in the out-ofplane direction, i.e., along the film-growth direction, and persist as the film thickness decreases. The former requirement can be realized more often in perovskite oxides, but it is much more challenging to realize in layered (quasi-)two-dimensional compounds, e.g., in Ruddlesden-Popper (RP) structures (12-15), with a rock-salt layer interrupting the perovskite layers, which imposes a coherence length constraint on the polar distortion (16), and to achieve strong polar mode-strain coupling to reorient the bulk in-plane polarization to an out-of-plane direction in thin films. In cases where the out-of-plane polarization naturally occurs or is engineered, the second requirement can be challenging to satisfy as the polarization in the thin film can be suppressed by the depolarizing field formed by surface charges. As a result, there is frequently an unavoidable critical thickness for most ferroelectrics below which the out-ofplane polarization vanishes (17, 18), rendering them nonfunctional for device applications.

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There are two unique ferroelectric materials classes distinct from conventional proper soft-mode and second-order Jahn-Teller active systems that can exhibit electric polarizations under open-circuit boundary conditions: hyperferroelectrics (19) and geometric improper ferroelectrics (19, 20). In contrast to the rarer hyperferroelectrics class (19, 21-24), a subset of improper ferroelectrics (12, 25–29), so-called hybrid improper ferroelectrics, circumvent depolarizing field effects owing to their geometric rather than electrostatic origins for an electric polarization. The known available materials exclusively exhibit in-plane ferroelectricity, however, transverse to the desired normal direction of the film. Nonetheless, they can be readily predicted by lowering the tolerance factor through changes in chemistry to favor rotations of metal-oxygen octahedra. Although the ferroelectric (FE) mode is stable, its condensation is induced by mode-mode coupling among the FE mode and other nonpolar phonon modes, such as octahedral rotational modes. These RP-structured materials have a range of functional properties derived from the form of the trilinear interaction coupling the modes, including the switching of weak ferromagnetism (wFM) with an electric field in Ca₃Mn₂O₇ (27) and a low coercive field for the switchable polarization and abundant charged FE domain walls in (Ca,Sr)₃Ti₂O₇ single crystals (30), leading to topological vortices and antivortices (31). Nonetheless, the polar ground-state structure always exhibits Cmc2₁ symmetry with an in-plane polarization, although an electric-field stabilized Pna2, phase with out-ofplane polarization was observed in experiment in nonmagnetic Li₂Sr_{1-x}Ca_xNb₂O₇ (32). To make these RP materials competitive alternatives for microelectronic integration, a polar phase with persistent out-of-plane ferroelectricity is required. Furthermore, controllable wFM still has not been observed in RP (33, 34) or Dion-Jacobson phases (35, 36), which may be because the controllable wFM through the out-of-plane rotation and in-plane tilt (e.g., X_2^+ and X_3^- in RP phases, respectively) requires different magnetic structures. In addition, selectivity of the octahedral rotation mode involved in the polarization switching path is not easy to achieve. Therefore, a deterministic and intrinsic constraint on the

polarization switching is desirable. To realize this constraint, there should be a single magnetic structure that allows either rotation mode to be active in the polarization reversal, avoiding the need for selectivity and kinetic control in the switching process.

Here, by using first-principles calculations, we unveil a general polar longitudinal optical (LO) mode, which both produces out-ofplane ferroelectricity and persists under open-circuit boundary condition in n = 2 RP halides and sulfides. This previously unidentified polar mode comprises cation and anion displacements in the rocksalt layers and transforms as the irreducible representation (irrep) Γ_3^- . We find that KAg₂Mn₂Cl₇, SrTb₂Fe₂S₇, and BaLa₂In₂S₇ exhibit hybrid improper ferroelectricity (HIF) and trilinear interactions stabilize the Γ_3^- mode with calculated electric polarizations ranging from 0.012 to 4.03 μC cm⁻² in films of unit cell thicknesses. We further show with constrained electric displacement field calculations and in a slab structure (e.g., 2.3-nm thin film) of KAg₂Mn₂Cl₇ that the polarizations persist under open-circuit boundary conditions. Furthermore, KAg₂Mn₂Cl₇ and SrTb₂Fe₂S₇ are magnetoelectric (ME) multiferroics with strong coupling between the out-of-plane polarization and magnetization. The Néel temperature for KAg₂Mn₂Cl₇ and SrTb₂Fe₂S₇ can be as high as 50 and 800 K, respectively, and their FE Curie temperatures are 274 and 455 K, respectively. Last, we show that the appearance of the Γ_3^- mode in the halides and sulfides can be understood with the perovskite tolerance factor; low tolerance factors favor a polar phase with the polar LO displacements, which makes it a useful descriptor to find additional ferroic materials. Our work provides a general strategy to design strong ME coupling with out-of-plane hybrid improper ferroelectricity for integration into future microelectronic devices.

RESULTS

K₃Mn₂Cl₇ has been synthesized and exhibits both HIF and G-type antiferromagnetic spin orders in the vicinity of ~64 K (37). With this as our prototype material, we substitute K ions in the rock salt layers with Ag while maintaining K in the perovskite layers to create KAg₂Mn₂Cl₇ (Fig. 1). This A-site ordering can produce an orthorhombic Cmc2₁ polar phase with an in-plane polarization if the tolerance factor remains sufficiently low (14, 30, 33, 37). After we perform our genetic algorithm structural search (38, 39), however, we uncover three polymorphs with lower energies: P1, Pna2₁, and Pc. We use these structures and a few additional candidate polymorphs to determine the ground state. As shown in Fig. 2A, the *Pc* structure is lowest in energy in our density functional theory (DFT) calculations at the Perdew-Becke-Erzenhof functional for solids (PBEsol) (2 meV/f.u. lower than Pna2₁) and local density approximation (LDA) (11 meV/f.u. lower than Pna2₁) levels and it is dynamically stable (fig. S1). The greater stability of the Pc phase, obtained by using LDA rather than PBEsol, is because the Pc phase can accommodate the decrease of the cell volume better than the others through its stronger ability to host oxygen octahedral rotations (table S2). Full structural details are provided in table S3. Even with disorder on the A site, a Pc-like phase remains most stable. Thus, a weak A-site distribution disorder will still favor out-of-plane ferroelectricity in the halides (fig. S3).

The monoclinic *Pc* phase (tolerance factor $\tau = 0.944$) exhibits an electric polarization with both out-of-plane and in-plane components. The polarization vector in a Cartesian coordinate system [i.e., pseudo-tetragonal (pt) system] is given by P = (0.77, 0.77, 4.03) μ C cm⁻² with 97% percent of the polarization out-of-plane. The out-of-plane and in-plane polarizations arise from modes transforming as Γ_3^- and Γ_5^- (Fig. 1). Figure 2B shows that the Γ_3^- mode is a hard mode with respect to the I4/mmm phase and therefore cannot condense alone; furthermore, the in-plane polarization $\Gamma_5^$ only makes a minor contribution to the energy lowering. Our group theoretical analysis shows that there are three trilinear terms coupling these modes to other inversion-symmetry preserving displacements: $Q_{(\Gamma_3^-)}Q_{(M_5^+)}Q_{(M_5^-)}$, $Q_{(\Gamma_3^-)}Q_{(X_2^+)}Q_{(X_1^-)}$, and $Q_{(\Gamma_5^-)}Q_{(X_2^+)}Q_{(X_3^-)}$. Although the X_2^+ mode is a rotational mode, and has been found in previous studies to stabilize the in-plane polarizations in HIF (12, 14, 27, 30, 40, 41), here, we find that X_2^+ is two dimensional with order parameter direction (a, b) and cannot be described as an effective one-dimensional order parameter as it is in polar RP phases with $Cmc2_1$ symmetry, i.e., (a, 0). It is essential to both the in-plane and out-of-plane polarizations. M_5^+ and $M_5^$ describe two antiferroelectric (AFE) modes and X₁⁻ is an octahedral rotational mode (Fig. 1). Therefore, the Γ_3^- mode also produces hybrid improper ferroelectricity and is induced by the two AFE modes and two rotational modes. Similarly, the latter trilinear interaction leads to condensation of the Γ_5^- mode and in this case, the displacements are to the chloride octahedra, i.e., tilting X₃ and rotations X_2^+ .

phenomenological using By Landau model a $F(u,\mathscr{E}) = E(u) - \Omega(u) \left[P(u)\mathscr{E} + \frac{1}{2} \varepsilon_0 \chi_\infty(u) \mathscr{E}^2 \right]$, the persistent polarization $P = -\frac{1}{\Omega} \frac{\partial F}{\partial \mathscr{E}} = \varepsilon_0 \chi_\infty(u) \mathscr{E} + P(u)$ can be obtained when the electric displacement field $D = \varepsilon_0 \mathscr{E} + P$ is zero (19, 21). This nonzero polarization is highly sought, because it does not vanish in very thin films where the depolarizing field (\mathcal{E}_d) is very strong. Here u is the dimensionless order parameter for the polar mode in the Pc phase, i.e., u = 1 in the ground state. In our calculations, u is fixed at each value between 0 and 1.1, and the other internal degrees of freedom, amplitudes of the other phonon modes, and lattice parameters are relaxed. \mathscr{E} , Ω , P, ε_0 , and χ_{∞} are the depolarizing field, volume per formula unit, polarization, dielectric constant of free space, and the diagonal component of the high-frequency dielectric permittivity along the polarization direction, respectively. Because of the existence of the trilinear coupling interactions, the polynomial expansion of E(u) can be equal to $\alpha u + \beta u^2 + ...$ in our calculations (fig. S4). Last, $\chi_{\infty}(u) = \varepsilon_{\infty} - 1$, where ε_{∞} is the electronic contribution to the dielectric constant, and we find that it is nearly the same for the out-of-plane ($\varepsilon_{\infty} = 3.67$) and in-plane directions ($\varepsilon_{\infty} = 3.66$). We linearize $P(u) = P_s u$ as in previous studies (19, 21), where P_s is the computed spontaneous polarization in the Pc phase. We thus obtain (0.17, 0.17, 0.76) μ C cm⁻² as the persistent polarization, which is comparable to that computed in the hexagonal FE ABC semiconductors (19). Our calculations with a slab model further show a remnant polarization under open-circuit boundary conditions (fig. S5), which is useful for achieving ultrathin film ferroelectricity (42). The out-of-plane polarization is comparable to that reported for YMnO₃ slab calculations (20), which is the prototype improper FE with a persistent polarization, exotic ME coupling, and vortex/antivortex domain structure (20, 28, 43, 44), and is further

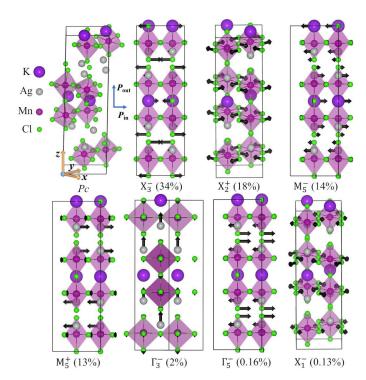


Fig. 1. Atomic structure of KAg₂Mn₂Cl₇. Ground-state structure of Pc KAg₂Mn₂Cl₇ and the main displacements, transforming as the designated irreps of the Id/Imm phase, contributing to its structure. Mode contributions (in percent) are given in descending order (as specified in parentheses). The pseudotetragonal Cartesian system and directions of the electric polarization (P_{out} out-of-plane polarization; P_{in} , in-plane polarization) are also shown.

enhanced owing to surface polarization charges. Unlike YMnO₃, the out-of-plane persistent polarization occurs in KAg₂Mn₂Cl₇ from a trilinear coupling interaction with a positive LO mode yet will also lead to unambiguously strong ME coupling. Furthermore, the polar LO mode contributes 80% of the total out-of-plane polar distortion in the Pc structure, which is larger than those contributions found in the hexagonal ABC FEs (25 to 75%). The remnant polarization at D = 0 takes 19% of the polarization at E = 0 in KAg₂. Mn₂Cl₇, which is much larger than those in the hexagonal ABC FEs (2 to 3.7%) (19), and may be attributed to the large portion of the LO mode and its lower frequency than the transverse optical (TO) mode in the out-of-plane polarization. Therefore, the RP phases may be a promising family for finding large remnant polarization at D = 0. We find that the LO-TO splitting is usually smaller in improper FE RP materials than other materials (table S4). Unexpectedly, the polar LO mode in some RP improper FEs has a lower frequency than the polar TO mode, such as in KAg₂Mn₂Cl₇.

We find that $KAg_2Mn_2Cl_7$ exhibits the same G-type spin orders as $K_3Mn_2Cl_7$ with spins aligned along the long c axis of the crystal. wFM occurs, order 10^{-3} µB/Mn, which is comparable to that calculated for $K_3Mn_2Cl_7$ and measurable in experiment (37). It is oriented along the $[\overline{1}10]$ direction, such that it is in-plane and perpendicular to the in-plane component of the electric polarization (Fig. 2C). We use our computed Mn spin exchange parameters, $J_1 = 2.64$ meV and $J_2 = 3.16$ meV (in plane) and $J_3 = 2.25$ meV (out of plane), in our Monte Carlo simulations to obtain a Néel temperature of 50 K that is comparable to that in $K_3Mn_2Cl_7$ (Fig. 2D). A

computed FE Curie temperature of 274 K in KAg₂Mn₂Cl₇ is higher than 89 K (180 K measured in experiment) in K₃Mn₂Cl₇ (37).

Previously, the trilinear coupling interaction $Q_{(\Gamma_{\varepsilon}^{-})}Q_{(X_{2}^{+})}Q_{(X_{2}^{-})}$ was predicted to produce robust ME coupling, in which the wFM can be switched if the polarization and X_3^- tilt mode can be switched simultaneously (27). This ME mechanism largely relies on the switching path, in which the change in the direction of the polarization must induce a change of the X_3^- tilt mode; however, the path cannot be guaranteed. Here, we find that the trilinear coupling interaction $Q_{(\Gamma_3^-)}Q_{(X_3^+)}Q_{(X_1^-)}$ underlying the out-of-plane polarization can be exploited to realize strong ME coupling, in which the X₂⁺ and X₁ modes control the direction of the wFM through a Dzyaloshinskii-Moriya (DM) interaction: $E_{DML} = \mathbf{D} \cdot (\mathbf{L} \times \mathbf{M})$, where \mathbf{D} is the DM vector, $L = S_1 - S_2$ is the AFM vector, and $M = S_1 + S_2$ is the wFM vector for neighboring spins S. X_2^+ and X_1^- will lead to an effective D vector along the [001]_{pt} direction (hereafter specified as $D_{[001]}$ given by $D \sim r_1 \times r_2$, where r_i (i = 1, 2) is the unit vector pointing along the S_i -O bond direction (45); hence, [001]_{pt} is determined by $r_1 \times r_2$. Switching of the wFM direction then requires a reversal in the sense of either X_2^+ or X_1^- , which can be realized by switching the Γ_3^- mode, i.e., the direction of the out-of-plane polarization that can be coupled to an out-of-plane electric field in a standard FET geometry. Our climbing nudged elastic band (46) calculation shows an energy barrier of 82 meV/f.u. for reversing the monodomain state (fig. S8), which is comparable to other RP oxides such as Sr₃Sn₂O₇ and Sr₃Zr₂O₇ (14, 45, 47, 48) and supports switchablilty of the out-of-plane polarization in the Pc phase.

There are only four Γ_3^- switching scenarios. Two cases are related to switching of the Γ_3^- mode and X_2^+ mode together $[(\Gamma_3^-, M_5^+, X_2^+,$ X_3^-) and $(\Gamma_3^-, \Gamma_5^-, M_5^-, X_2^+)$]; the other two are related to switching of the Γ_3^- mode and X_1^- mode simultaneously $[(\Gamma_3^-, \Gamma_5^-, M_5^-, X_1^-, X_3^-)]$ and $(\Gamma_3^-, M_5^+, X_1^-)$]. Thus, one of either the X_2^+ or X_1^- mode must reverse upon switching the Γ_3^- mode. As can be seen in Fig. 1, the X_2^+ and X_1^- modes are in-phase and out-of-phase rotations, respectively, and will result in different alignments of the layer-resolved contributions to the wFM (Fig. 2C). For example, if X_2^+ is reversed 180° from a clockwise sense (as depicted) to counterclockwise, then the symmetry requires that wFMs in layers 1 to 4 will change so that the spin moments in layer $1 \rightarrow$ layer 4, layer $2 \rightarrow$ layer 3, layer $3 \rightarrow$ layer 2, and layer $4 \rightarrow$ layer 1 change, although the total wFM direction is unchanged. This switching of the wFM spin directions is also found in our DFT calculations including spin-orbital coupling (SOC).

As an alternative, we propose a ME coupling form for the RP compounds that does not depend on the switching path, where the polarization switching will uniquely change the wFM direction if the magnetic anisotropy (MA) is in plane. An in-plane MA can be obtained through a spin-flop mechanism (49). The magnetic field (H) to induce such a spin flop is proportional to $2S\sqrt{JK}$ (45), where S is the magnetic moment for each Mn, J is the maximum spin exchange parameter (i.e., J_2), and K is the single-ion anisotropy parameter. The computed H = 3.7 T in $KAg_2Mn_2Cl_7$, which is consistent with our Monte Carlo (MC) simulation with an applied magnetic field. Furthermore, the out-of-plane MA may be overcome by temperature effects, as an in-plane MA is observed near the Néel temperature in our MC simulations (fig. S10). The MA can also be changed in other ways such as a controllable

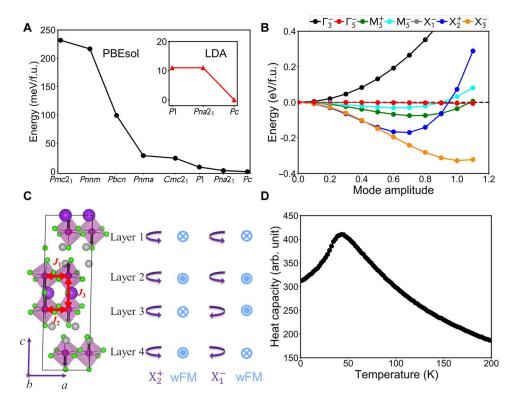


Fig. 2. Energetics and magnetism in $KAg_2Mn_2Cl_7$. (A) Energies for several symmetries of $KAg_2Mn_2Cl_7$. (B) Energy as a function of mode amplitude for each mode in the *Pc* structure. The mode amplitude is scaled by the original mode amplitude in Å in the *Pc* structure. (C) *Pc* structure with G-type magnetic structure along the pseudote-tragonal *z* direction. The spin exchange interaction parameters are shown with the red arrows. X_2^+ and X_1^- rotations are represented by the arcs rotating about the pseudotetragonal *z* direction. The directions of the layer-resolved wFM components are indicated by the filled and crossed circles pointing to the *b* axis. (D) The simulated heat capacity as a function of temperature.

lateral MA in a heterostructure by atomic-scale design of the oxygen octahedral rotation (50, 51).

To further elucidate the generality of the Γ_3^- mode for producing out-of-plane polarizations in the n = 2 RP family, we investigate Asite ordered $AA'_2B_2S_7$ sulfides. $ATb_2Fe_2O_7$ (A = Sr, Ca) were reported in a previous study combining experiment measurements and DFT calculations (33), in which the ground-state structures of $SrTb_2Fe_2O_7$ ($\tau = 0.944$) and $CaTb_2Fe_2O_7$ ($\tau = 0.941$) are $P4_2/mnm$ and Cmc2₁, respectively. We find, however, that the ground-state structure of CaTb₂Fe₂O₇ is *Pnma* by carrying out the DFT calculations at 0 K with the parameters provided in the previous study (33). This is consistent with another study on $Li_2SrNb_2O_7$ ($\tau = 0.964$) (52), in which the ground-state structure is *Pnma* and the *Cmc*2₁ phase is stabilized at finite temperatures owing to vibrational entropy. Therefore, the observed room-temperature Cmc2₁ phase in (Ca, Sr)Tb₂Fe₂O₇ occurs for the same reason as finding a Cmc2₁ phase at the high temperature in Li₂SrNbO₇. We hypothesize that the ground-state n = 2 RP phases are more complex than expected and the prior heuristic of lowering the tolerance factor may not lead to a polar ground state with *Cmc*2₁ symmetry.

With the low tolerance factor sulfide $SrTb_2Fe_2S_7$ ($\tau=0.941$), we compare the energetics of common polymorphs identified from previous studies and find that the centrosymmetric $P4_2/mnm$ phase has the lowest energy (Fig. 3A). Our phonon calculations, however, reveal that the $P4_2/mnm$ phase is dynamically unstable (Fig. 3C), and the most unstable modes occur at the (0.5, 0.5, 0)

and (0.5, 0.5, 0.5) k points in the Brillouin zone. Upon condensing different permutations of multiple modes from the same and different wave vectors (table S5), we find that the polar $I4_1cd$ structure is lowest in energy and comprises four main distortion modes (Fig. 4). The four phonon modes include one out-of-plane polar mode Γ_3^- , two AFE modes N_1^- and N_2^+ , and one tilt mode X_3^- . The polar mode is distinct from that found in materials comprising second-order Jahn-Teller ions. Here, the X₃ mode is different from the tilt mode in $Cmc2_1$ phase (one in-plane polar mode Γ_5^- , two rotational modes X_2^+ , and X_3^- that results in *Cmcm* symmetry), where the rotational axes between the two double-perovskite layers are perpendicular to each other resulting in P42/mnm symmetry and the DM vectors are along their rotational axes and normal to each other. In our magnetic calculations, we find a G-type magnetic structure with an in-plane MA. Then, the direction of wFM in a double-perovskite layer will be along the out-of-plane direction (see Fig. 5A).

Upon analyzing the symmetry relationships among the modes with I4/mmm as reference, we obtain two important trilinear coupling interactions: $X_3^-N_1^-N_2^+$ and $\Gamma_3^-N_1^-N_2^+$. Thus, the direction of the X_3^- mode can be tuned by switching the Γ_3^- mode, in which the reversal of Γ_3^- will lead to a change of the sign of $N_1^-N_2^+$ that will result in a switching of X_3^- as to keep $X_3^-N_1^-N_2^+$ and $\Gamma_3^-N_1^-N_2^+$ invariant. Because the X_3^- mode can control the wFM and the existence of the trilinear coupling interactions as mentioned above, the switching of the polarization will unambiguously change the wFM, which does not depend on the switching path. Although the wFM

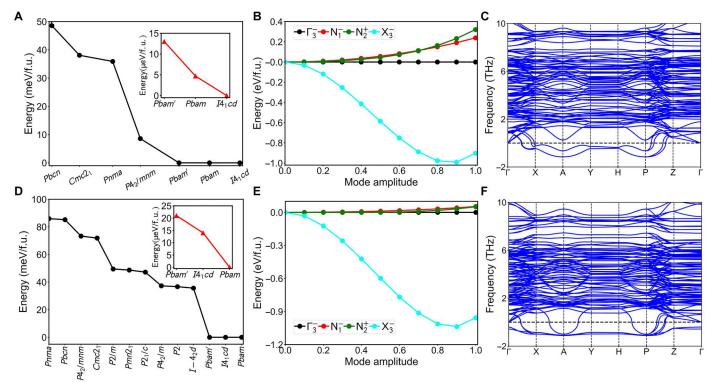


Fig. 3. Energetics and dynamical stability of SrTb₂Fe₂S₇ and BaLa₂In₂S₇. (**A**) Energies for several symmetries of SrTb₂Fe₂S₇. (**B**) Energy versus mode amplitude in SrTb₂Fe₂S₇ with the mode amplitude given relative to the mode amplitude found in the equilibrium $I4_1cd$ phase. (**C**) Phonon spectrum of $P4_2/mnm$ SrTb₂Fe₂S₇. (**D**) Energies for several symmetries of BaLa₂In₂S₇. (**E**) Energy versus mode amplitude in BaLa₂In₂S₇ with the mode amplitude given relative to the mode amplitude found in the equilibrium $I4_1cd$ phase. (**F**) Phonon spectrum of $P4_2/mnm$ BaLa₂In₂S₇.

components align in an antiparallel manner, so that there is no net magnetism, their directions in each perovskite layer can be switched upon changing the X₃⁻ mode as in KAg₂Mn₂Cl₇. Alloying may provide a route to canted magnetism. Furthermore, our ME coupling can be applied in devices on the basis of topological defects formed at the domain walls, in which a Z₈/Z₄ vortex or antivortex is formed in a P4₂/mnm phase in (Nd, Tb, Sr)₃Fe₂O₇ (44) and SrCa₂Ti₂O₇ (31). The Z₈/Z₄ vortex and antivortex form because of the X_3^- mode in the $P4_2/mnm$ phase. If the X_3^- mode is further coupled to the polar Γ_3^- mode, such as in the $I4_1cd$ phase, then the robust ME coupling in Fig. 5A may be realized at a Z₈ vortex (see Fig. 5B and fig. S11). The in-plane and out-of-plane spin exchange parameters are computed and the Néel temperature is predicted to be 800 K from our MC simulations (Fig. 5C). The I41cd structure is always more stable than the competitive *Pbam* phase at finite temperature and we calculate its FE Curie temperature as 455 K. Therefore, we predict SrTb₂Fe₂S₇ is a room-temperature multiferroic with strong ME coupling.

DISCUSSION

Multiferroics have been intensively studied since the discovery of room-temperature multiferroic BiFeO₃ (53) and type II multiferroic TbMnO₃ (54). Nowadays, electric-field control of magnetism has become a key to realize ultralow-power logic memory devices in recently developed device architectures (55, 56). One priority for the scientific community is to broaden the set of materials that exhibit

multiferroic and ME behavior at room temperature. From a technology perspective, finding robustly coupled FE and magnetic order parameters at the 10-nm length scale and at room temperature that are CMOS compatible for integration is critical. Therefore, combining persistent out-of-plane polarization and magnetism to realize strong ME coupling is of both scientific and technological importance. It is rarely reported with an unambiguously determined ME coupling mechanism (24, 57). SrTb₂Fe₂S₇ may be such a promising room-temperature multiferroic with strong ME coupling satisfying the above requirements. Moreover, the most recent study showed that Hf-based FEs exhibit both ferroelectricity in ultrathin films (e.g., ~2 nm) and a large dielectric constant (~34), which has been intensively investigated and showed a very small equivalent oxide thickness (EOT) of 6.5 Å in a HfO2-ZrO2 superlattice (11). To obtain the small EOT, the small thickness and large static dielectric constant are required. In our studied compounds, KAg₂Mn₂Cl₇ may have a persistent polarization at a thickness of 2.3 nm with a dielectric constant of 3.6. SrTb₂Fe₂S₇ may have a persistent polarization at a thickness of 4.5 nm with a dielectric constant of 99 that is much larger than those of HfO₂ and ZrO₂ (58). Therefore, SrTb₂Fe₂S₇ may also be a potential candidate for designing advanced transistors with small EOT.

We also investigated other nonmagnetic A-site ordered RP sulfides and our results show that lower tolerance factors (e.g., $\tau < 0.944$) may lead to an unstable $P4_2/mnm$ structure and then a lower-energy polar phase with out-of-plane polarization (fig. S13 and table S7). With this principle, we can select BaLa₂In₂S₇. We find that it adopts a competitive polar phase with $I4_1cd$ symmetry,

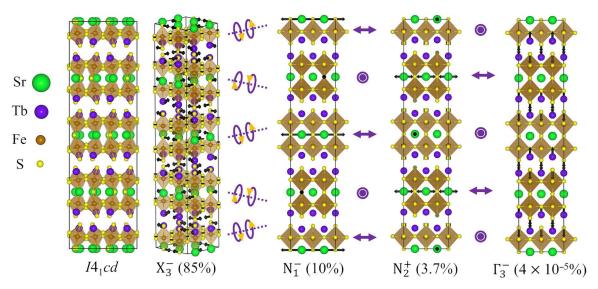


Fig. 4. Atomic structure of SrTb₂**Fe**₂**S**₇. Ground-state structure of $I4_1cd$ SrTb₂Fe₂S₇ and the main distortion modes obtained by a phonon decomposition with respect to I4/mm. The schematic displacement patterns (e.g., purple arrows and circles) for the X_3^- , N_1^- and N_2^+ modes are shown for better visualization. Mode contributions (in percent) are given in descending order (as specified in parentheses).

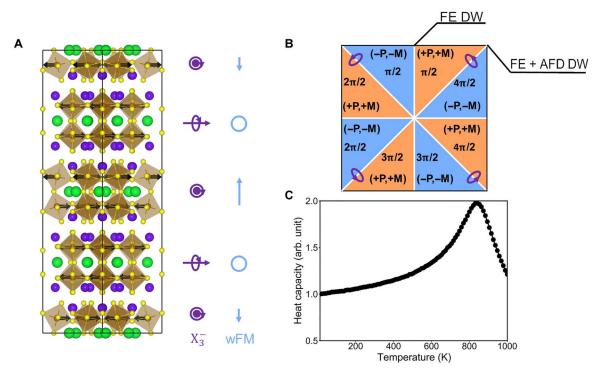


Fig. 5. Distortions and magnetism in SrTb₂Fe₂S₇. (**A**) The $I4_1cd$ SrTb₂Fe₂S₇ structure with G-type magnetic structure along the in-plane diagonal direction (i.e., ab direction). X_3^- rotations are represented by the arcs rotating around the in-plane directions. Black arrows within the octahedra indicate local spin vectors. The purple arrows on the right of the structure indicate the directions of the wFM in each perovskite bilayer. The wFM vectors along the c axis in the different double-perovskite layers will be opposite and cancel so that there is no net wFM. The blue circles indicate that there will be no wFM in the layers. (**B**) Schematic illustration of the switching paths between +**P** and -**P** states at a Z_8 vortex in SrTb₂Fe₂S₇. The degrees indicate the rotational angles of the X_3^- mode. The Z_8 vortex is formed by the X_3^- and Γ_3^- modes. The **P** and **M** represent the polarization and wFM, respectively. The white lines are the FE domain wall (FE DW) and FE DW plus antiferrodistortive domain wall (FE + AFD DW). The blue and orange areas represent the (-**P**, -**M**) and (+**P**, +**M**) states, respectively. (**C**) The simulated temperature-dependent heat capacity of SrTb₂Fe₂S₇.

whose ground-state structure is an AFE *Pbam* structure. The electric polarizations in SrTb₂Fe₂S₇ and BaLa₂In₂S₇ are due to hybrid improper ferroelectricity and 0.012 and 0.027 μ C cm⁻², respectively (Fig. 3 and fig. S14). A large portion of their polarizations arise from the positive LO modes (see fig. S15), which indicates that the polarization in SrTb₂Fe₂S₇ and BaLa₂In₂S₇ should also persist under open-circuit boundary conditions. Our results also indicate that the ground-state $I4_1cd$ structure may be obtained in a RP sulfide compound with 0.938 < τ < 0.944. The larger τ may lead to a $P4_2/mnm$ ground-state structure and smaller τ may result in an AFE *Pbam* structure. This rule is also consistent with that found in RP oxides, where the ground-state phase has *Pnma* symmetry when τ is too small

Regarding our studied materials, we expect that similar experimental measurements are applicable to reveal their FE and ME features. We notice that the melting points of halides are lower than oxides, implying that it is likely easier to obtain large single crystals, which are more suitable for precise physical property measurements especially for studying the polarization anisotropy, which is crucial for studying the persistent polarization, for example, in KAg₂Mn₂Cl₇. It adopts a polar monoclinic Pc structure with both in-plane and out-of-plane polarization. Large single crystals would enable the deconvolution of these contributions, allowing for a direct measurement of polarization and its switching along different directions. There are other possible experiments to further elucidate the FE and ME behaviors in our proposed materials. For example, in situ synchrotron x-ray diffraction experiment under applied electric fields can help understand the FE switching mechanism, as already demonstrated in HIF oxide Ca_{2,15}Sr_{0,85}Ti₂O₇ (59). Variable-temperature high-resolution neutron diffraction is also helpful in observing the coupling effect between electric polarization and magnetic order (60). Notably, this method has been particularly successful in our recent study on the first halide HIF ME K₃Mn₂Cl₇ (37), from which we observed that the long-range magnetic order induces a clear reduction in electric polarization. Beyond these reported experimental approaches, we believe that polarized-neutron diffraction experiments under electric fields would also be useful in directly observing electric field-induced modulation (or even switching) of the ferromagnetic component in our proposed materials.

In summary, we unveiled an out-of-plane LO mode in the n = 2RP sulfides and halides that leads to persistent polarizations and makes them hybrid improper FEs. On the basis of a crystallographic tolerance factor, this out-of-plane polar mode can be predicted and more FE/multiferroic materials with out-of-plane hybrid improper ferroelectricity can be found when $0.938 < \tau < 0.944$. Our results show that KAg₂Mn₂Cl₇ and SrTb₂Fe₂S₇ are within this tolerance regime and are multiferroics. The Néel temperature for SrTb₂Fe₂S₇ is well above the room temperature. Both multiferroics exhibit strong ME couplings because of the existence of an out-of-plane polarization, in which switching of the polarization unambiguously induces a change in the wFM in the double-perovskite layers. We believe that our proposed polar mode is ubiquitous in the n = 2RP family, for example, it may also be obtained in n = 2 RP oxides by an electric field when an antipolar Pnma polymorph is the ground-state structure ($\tau = 0.964$) (32), which provides a way to find promising FEs and multiferroics for device integration.

MATERIALS AND METHODS

Our total energy calculations are based on DFT within the generalized gradient approximation using the revised PBEsol (61) implemented in the Vienna Ab Initio Simulation Package (62, 63). We use a 550-eV plane wave cutoff energy for all calculations and the projector augmented wave method (64, 65). We use Gaussian smearing (0.10 eV width) for the Brillouin-zone integrations and a sufficiently dense k-point mesh. The pseudopotentials for the A- and B-site ions are chosen to treat the s or p core electrons as the valence electrons if available. The electric polarization is computed with the Berry phase method (66, 67). The DFT plus Hubbard U method (68) is used with the Hubbard U and the exchange parameter J set to 6 eV and 1 eV for Mn, respectively, which reproduces the ground-state Cmc2₁ structure and the experimentally G-type antiferromagnetic structure in K₃Mn₂Cl₇ (37). The magnitude of wFM can be changed from $1 \times 10^{-4} \mu B/Mn$ to $1 \times 10^{-3} \mu B/Mn$ when changing the Hund's parameter J from 1 to 2 eV. Our DFT + U calculations also showed good agreement with the experiment structural parameters (lattices and atomic coordinates) and Néel temperature for K₃Mn₂Cl₇ (37). U and J are set to 5.5 and 1 eV for Fe, respectively, which reproduces the experimentally G-type antiferromagnetic structure in SrTb₂Fe₂O₇ (33). SOC is included for the MA studies.

To compute the symmetric spin exchange parameters, we use a four-state mapping method (69, 70). We calculate the effective symmetric spin exchange parameters, which are obtained by setting $|\mathbf{S}_i|$ =1, namely, $J_{ij} = J_{ij}^{\text{eff}} S_i S_j$ for a spin dimer ij. Our parallel tempering MC (PTMC) simulations are based on an exchange MC method (39, 71), which can simulate the classical Heisenberg spin system with a Hamiltonian $E = E_0 + \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$, where J_{ij} is the symmetric spin exchange parameter. To obtain the plot of the specific heat (C) versus temperature (T), we calculate the specific heat $C_{\sim}(\langle E^2 \rangle - E_{\sim})$ $\langle E \rangle^2 / T^2$ after the system reaches equilibrium at a given temperature T in the simulation. Then, we obtain the critical temperature by locating the maximum in the C(T) plot. In our PTMC simulations of the effective Hamiltonian, a $6 \times 6 \times 3$ supercell of the 48-atom unit cell is adopted for KAg₂Mn₂Cl₇ and a $6 \times 6 \times 3$ supercell of the 384atom unit cell is adopted for SrTb₂Fe₂S₇, which we confirmed are converged. The number of replicas is set to 96.

For our phonon calculations, we use the finite displacements method (72). The symmetry-adapted mode distortion vectors of the polar phase are obtained by performing a mode decomposition with respect to *I4/mmm* using the ISODISTORT software (73).

To relax the mode amplitudes at each u (the amplitude of the fixed mode Γ_3^- or Γ_5^-), we minimize the Landau phenomenological expansion obtained using group theory by directly carrying out the DFT calculations rather than fitting the coefficients in the expansion (48). Here, the normalized distortion modes (with the amplitude of each mode vector normalized to 1 Å) in the Pc phase (some of them are shown in Fig. 1) are constrained, that is, the order parameter direction is fixed; however, the internal atomic positions are allowed to vary according to the directions of the phonon distortions considered (the magnitude is relaxed in the optimization) and the lattice constant is also optimized. This allows us to obtain the total energies and dielectric constants efficiently and accurately as described in fig. S4.

To implement this constraint in our DFT calculations, we project the forces on the atoms in the DFT calculations onto the

normalized distortion modes except for the fixed mode (i.e., Γ_3^- or Γ_5^-) so that the order parameter direction is fixed, but the magnitude of the mode is relaxed in the optimization. Then, the amplitudes of phonon modes in the Pc phase will change for different u, but the modes vectors will all be the same as those at u = 1 (i.e., the ground state) (48).

The tolerance factor is obtained by using $\tau_i = \frac{r_A + r_X}{\sqrt{2}(r_B + r_X)}$, where r_{A} , r_{B} , and r_{X} are the radii of the A, B cations, and anion, respectively. The averaged $r_{A-X} = r_A + r_X$ is computed by considering the nearestneighboring oxygen atoms around the A atom for all A atoms. The averaged r_{B-X} is computed in the same way as r_{A-X} . Here, we consider 12-coordination for A, 9-coordination for A', and 6-coordination for B. The τ is computed in Pc phase for KAg₂Mn₂Cl₇, in Pnma for CaTb₂Fe₂O₇ and SrLi₂NbO₇, and in $P4_2/mnm$ for SrTb₂Fe₂O₇, SrTb₂Fe₂S₇ and BaLa₂In₂S₇ (table S7).

Supplementary Materials

This PDF file includes:

Supplementary Text Figs. S1 to S15 Tables S1 to S9 References

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