

# QuantumEyes: Towards Better Interpretability of Quantum Circuits

Shaolun Ruan , Qiang Guan , Paul Griffin , Ying Mao , and Yong Wang 

**Abstract**—Quantum computing offers significant speedup compared to classical computing, which has led to a growing interest among users in learning and applying quantum computing across various applications. However, quantum circuits, which are fundamental for implementing quantum algorithms, can be challenging for users to understand due to their underlying logic, such as the temporal evolution of quantum states and the effect of quantum amplitudes on the probability of basis quantum states. To fill this research gap, we propose *QuantumEyes*, an interactive visual analytics system to enhance the interpretability of quantum circuits through both global and local levels. For the global-level analysis, we present three coupled visualizations to delineate the changes of quantum states and the underlying reasons: a Probability Summary View to overview the probability evolution of quantum states; a State Evolution View to enable an in-depth analysis of the influence of quantum gates on the quantum states; a Gate Explanation View to show the individual qubit states and facilitate a better understanding of the effect of quantum gates. For the local-level analysis, we design a novel geometrical visualization *dandelion chart* to explicitly reveal how the quantum amplitudes affect the probability of the quantum state. We thoroughly evaluated *QuantumEyes* as well as the novel *dandelion chart* integrated into it through two case studies on different types of quantum algorithms and in-depth expert interviews with 12 domain experts. The results demonstrate the effectiveness and usability of our approach in enhancing the interpretability of quantum circuits.

**Index Terms**—Interpretability, data visualization, quantum circuits, quantum computing.

## I. INTRODUCTION

Quantum computing has experienced remarkable advancements in recent years. The rapid growth in the quality and quantity of quantum computers by leading IT companies, such as IBM, Google and Amazon, are making potential quantum advantages increasingly realistic for both theoretical quantum algorithms [1]–[4] and emerging applications [5]–[9]. For example, quantum computing has shown its superior speedup on classical problems, such as *Grover’s algorithm* for unstructured search [1], and *Shor’s algorithm* for integer factoring [2]. Meanwhile, researchers began to explore the power of quantum computing in various applications, such as machine learning [7], finance [8], and chemistry [9]. The quantum supremacy experiment by Google [5] has shown the potential advantage of quantum computers over their classical counterparts.

Building upon the proliferation of quantum computers, the number of people learning quantum computing has experienced rapid growth in recent years [10], [11]. However, prior research has identified that grasping abstract concepts in quantum computing remains challenging [12], [13]. For example, *quantum circuits*, the most fundamental routine to perform any quantum program, lack the transparency and interpretability needed for easy comprehension [13]. Consequently, a graphical representation [14] known as quantum circuit diagrams was proposed decades ago and has been widely used in research papers and textbooks on quantum computing. Despite its prevalence, it primarily overviews a quantum circuit and has limitations in revealing deep insights into quantum circuits’ behaviors. From a quantum circuit diagram, it is difficult for quantum computing developers and researchers to understand the functionality of each quantum gate and the final measured probability of each basis state. For example, the viewers cannot inspect the quantum states’ initial generation and further evolution or the functionality of each quantum gate from a quantum circuit diagram (e.g., Fig. 1A). Thus, how to intuitively reveal the detailed inner workings of a quantum circuit still remains under-explored.

However, it is non-trivial to fill this research gap. According to our extensive literature survey [12], [15]–[20] and close collaborations with six quantum computing experts, the major challenges mainly come from the counter-intuitive nature and intrinsic complexity of *quantum gate operations* and *measured probability* of quantum circuits. First, the quantum gates are the fundamental and crucial operators to manipulate the state of qubits. But quantum gate operations are essential matrix multiplications that are difficult to visualize and explain. What makes matters worse is the matrix transformations of quantum gates involves complex numbers [21] that are counter-intuitive. Second, the measured probability, determined by the quantum amplitudes of each basis state, is critical to understand the output of quantum circuits. But users often do not possess a mathematical intuition regarding the underlying cause of each basis state’s amplitude [20]. Also, quantum system states of multiple qubits can be entangled together rather than being a simple accumulation of multiple individual single-qubit states, and there will be  $2^N$  possible basis states if the qubit number is  $N$ , making it extremely challenging to visualize multi-qubit states and the corresponding measured probabilities in a limited space [20].

To address the above challenges, we propose *QuantumEyes*, a visualization approach to enhance the interpretability of quantum circuits. *QuantumEyes* can intuitively explain the functionality of each quantum gate and the measured prob-

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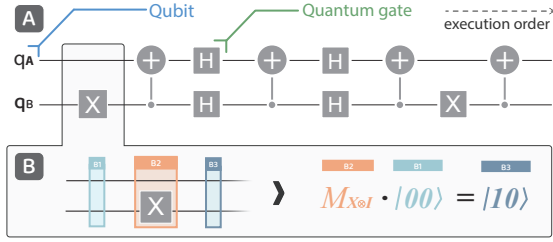


Fig. 1. (A) An example quantum circuit reproduced from the prior work [22], which consists of qubits and quantum gates. (B) The intuitive illustration that shows how the matrix multiplication is performed given the quantum gate and initial quantum state.

ability of each basis state for a given quantum circuit. We follow a user-centered design process [23] by working closely with six domain experts in quantum computing for over five months. By summarizing the expert feedback, we distilled design requirements in terms of two levels of analysis - **global** analysis and **local** analysis. For the global analysis, we propose three coordinated views to enhance the interpretability of quantum gates' operations: a Probability Summary View summarizes the changes of all quantum states along a circuit (Fig. 5A), a State Evolution View supports analyzing how quantum gates affect the evolution of multiple quantum states over time (Fig. 5B), and a Qubit Explanation View further explains the quantum gates' effect from the view of the single qubit and its acting quantum gate (Fig. 5C). For the local analysis, we propose a novel geometrical visualization *dandelion chart* (Fig. 4), which can visualize and explain the measured probability of numerous basis states based on amplitudes. To evaluate the usefulness and effectiveness of *QuantumEyes*, we present two case studies based on the famous quantum algorithms, *i.e.*, *Grover's Algorithm* and *Quantum Fourier Transform*. We further conducted in-depth interviews with 12 domain experts with carefully designed tasks. The results show that *QuantumEyes* can effectively help developers and researchers better understand the behaviors of quantum circuits.

The major contributions of this paper can be summarized as follows:

- We formulate the design requirements for improving the interpretability of quantum circuits by working closely with quantum computing experts.
- We introduce *QuantumEyes*, an interactive visualization system to assist quantum computing users in intuitively understanding the behaviors of quantum circuits, including three coordinated views for global analysis and a novel design *dandelion chart* for local analysis.
- We present two case studies and in-depth user interviews with domain experts to demonstrate the effectiveness and usability of *QuantumEyes*.

To further benefit quantum computing developers and researchers, we have made our system *QuantumEyes* publicly accessible online<sup>1</sup>. Also, we have published *dandelion chart*

as an independent NPM package<sup>2</sup>.

## II. RELATED WORK

Our work is relevant to prior research on visualization of quantum circuit evolution and quantum state visualization.

### A. Quantum State Visualization

Many existing approaches studied how to represent quantum states, the mathematical description of the state of a quantum system. We classify existing visual representations for quantum states based on whether the visualization is state vector-based or probability-aware.

**State vector-based approaches.** The state vector-based approach aims to visualize the quantum amplitudes of quantum states. The most widely-used representation in the quantum computing community is *Bloch Sphere* [24], which is integrated into many popular quantum computing SDKs like IBM Qiskit [25] and Google Cirq [26] to visualize quantum states. Bloch Sphere leverages a point on the unit sphere to represent the quantum amplitude of a pure single-qubit state. Meanwhile, Bloch Sphere can also reflect two important visual effects, *i.e.*, single-qubit rotation gates and statistical mixtures of pure states. Prior work has introduced various extensions of Bloch Sphere [27]–[29]. Also, many researchers have studied how to represent quantum states using 2D shapes. Wille et al. [30] visualized the components of state vectors using a tree-like design. Several studies explored how to better visualize quantum states by enabling multi-qubit visualization, such as the stellar representation [31] and the visualization based on multi-qubit Bloch vectors [32]. However, several issues exist in the above visualization approaches. First, these visualizations do not enable a direct comparison of the probabilities of basis states, making it hard for users to inspect the measured probability. Second, for 3D representations, they have been proven less effective than 2D counterparts when conducting precise measurements [33], [34].

**Probability-aware approaches.** Some prior work focused on improving the state vector-based approach by explicitly visualizing the probability based on the state vector representation. For example, Galambos et al. [35] utilized a fractal representation of a multiple-qubit system via a set of rectangles. Also, Chernega et al. studied several variants [36]–[38] based on Triada of Malevich's squares mapping the state vectors of a qubit onto the vertices of a triangle. More recently, Ruan et al. [20] introduced a 2D geometrical visualization to highlight the impact of the state vector on the probability.

Similarly, Miller et al. [39] proposed an interface with an embedded node-like graph to explain circuits and stabilizer groups, allowing the observation of updates of quantum states. Although the prior work can visualize the probability of quantum states, they still suffer from scalability issues. Most studies can only support the visualization of one qubit [36], [38] or two qubits [20], [35], whereas most of the accessible quantum computers are already exceeding this number of qubits. Therefore, it is crucial to enable the inspection of more

<sup>1</sup><https://quantumeyes.github.io/>

<sup>2</sup>[https://www.npmjs.com/package/dandelion\\_chart](https://www.npmjs.com/package/dandelion_chart)

qubits. Our work aims to support quantum state visualization with multiple qubits, while preserving the property of being probability aware.

### B. Visualization of Quantum Circuit Evolution

We categorize existing work into two groups: depending on whether the proposed visualization technique is for a specific algorithm or general quantum circuits.

**Algorithm-specific visualization.** Visualization approaches in this category often aims at a specific quantum algorithm without the generalizability for general quantum programs. For example, Tao et al. [40] utilized a Bloch Sphere and a disk-like design to portray the evolution of each quantum states along each step of *Shor's algorithm*. Karafyllidis et al. [41] studied how to visually explain the QFT algorithm by visualizing the changes of the probability of each quantum state, but it cannot support the trace-back analysis of basis states. Meanwhile, two online platforms [42], [43] enabled users to visually understand quantum states and quantum circuits in Quantum Error Correction, respectively. But it is challenging to extend to arbitrary quantum circuits, which significantly limits their benefits and impact.

**Generally-applicable visualization.** Unlike algorithm-specific explainability, generally-applicable methods can be applied to arbitrary quantum circuits and thus are more flexible. One common approach is leveraging measured probability to depict each step's behavior in a quantum circuit. For example, Williams [13] and Lin et al. [12] showed the probabilities of all possible states after each quantum gate to interpret the gate's functionality. Wen et al. [44] also studied to improve the scalability of large-scale circuits. Lamy [45] studied how to reveal the gate effect by visualizing the change of quantum state in each step with a rainbow box design, while preserving the display of phases. Moreover, Van de Wetering [46] proposed a graphical representation of a linear map between qubits. Another type of work focuses on explaining the noise in quantum circuits. For example, Ruan et al. [47] introduced a visualization approach for the awareness of noise hidden in quantum computers and compiled quantum circuits. Meanwhile, Quirk [48] and Q-Sphere [49] also enable users to interact with quantum circuits via a web-based platform.

While all the above methods focus on visualizing the quantum circuit evolution via the sequence of basis states' probability, our work aims to depict the development of a quantum circuit by visualizing the basis states' relationship with a more effective visual channel, *i.e.*, position [50]. Also, *QuantumEyes* uses Gate Explanation View and *dandelion chart* to explicitly explain gate functionality with greater clarity.

## III. BACKGROUND

This section introduces the background of quantum computing relevant to our study, including quantum states and quantum circuits.

### A. Quantum State

In quantum computing, quantum states are the mathematical entities that provide the probability of multiple basis states. Meanwhile, the actual calculation of gate operation can be represented as the matrix multiplication of quantum states and gates (*e.g.*, Fig. 1B). Recalling that for one qubit, the single-qubit state can be expressed as  $\alpha|0\rangle + \beta|1\rangle$ . Generally, any quantum state with  $n$  qubits can be represented as a linear combination of  $2^n$  basis states:

$$\alpha \cdot |0 \cdots 00\rangle + \beta \cdot |0 \cdots 01\rangle + \cdots + \gamma \cdot |1 \cdots 11\rangle, \quad (1)$$

where the complex number  $\alpha, \beta, \cdots, \gamma$  are called quantum amplitudes (*a.k.a.* amplitudes) which is used to describe the basis state (*e.g.*,  $|0 \cdots 01\rangle$ ) of a quantum state. An arbitrary amplitude (*e.g.*,  $\alpha$ ) can be expressed as a complex number:

$$\alpha = a + b \cdot i, \quad (2)$$

where  $a$  is the real part, and  $b \cdot i$  is the imaginary part ( $i$  is the imaginary unit). Note that the amplitude of any quantum state can be used to determine the probability of measuring the corresponding basis state, which can be written as follows:

$$Pr(|0 \cdots 00\rangle) = |\alpha|^2 = |a|^2 + |b|^2. \quad (3)$$

Since the amplitudes of all basis states satisfy a normalization constraint that the sum of the probabilities of all basis states equals 1, thus all amplitudes satisfy  $|\alpha|^2 + |\beta|^2 + \cdots + |\gamma|^2 = 1$ . Note that we use the phrase “measured probability” in this paper to refer to the probability of a certain basis state if the qubits were measured.

### B. Quantum Circuit

Similar to classical circuits, quantum circuits describe how quantum algorithms can be decomposed into a sequence of physical gates (Fig. 1). The manipulation of a quantum circuit can be represented as a calculation of unitary matrices [51]. In this paper, we refer to each manipulation module highlighted by the grey rectangle as a *block*. Thus, the execution of an arbitrary quantum circuit consists of the matrix calculation of a set of blocks, as illustrated in Fig. 5A.

Upon completing the final quantum gate, the execution result would be measured for the probability distribution of all basis states. Note that the intermediate quantum state after each gate's unitary transformation can be measured if the device is a quantum simulator [52]. In contrast, only the final quantum state can be obtained for a real quantum computer due to the collapse of the quantum state upon measurement. Hence, for intermediate states, the visualization takes place in a “god mode” where the probabilities are known although the state is not actually measured.

## IV. DESIGN FORMATION

In this section, we first report the preliminary study with the design requirements distilled from the study. We then introduce the dataset we used to fulfill the requirements.

### A. Preliminary Study

Following the guideline [53] of task abstractions for the design study, we designed the preliminary study as follows:

**Participants:** The study involved six domain experts (**P1-6**) (6 males,  $age_{mean} = 36.5$ ,  $age_{sd} = 4.9$ ) from educational institutions and a national research laboratory. Specifically, **P1-3** are professors from three different universities in Singapore and the U.S. **P4** is a research scientist from Pacific Northwest National Laboratory, and **P5-6** are two Ph.D. students whose research direction is quantum computing. Among them, **P1-2** and **P5** are working on Quantum Machine Learning, while **P3-4** and **P6** study Quantum Systems, Quantum Chemistry and Quantum Error Modeling, respectively. All the experts have an average of 6.8 years of research and development experience in quantum computing.

**Procedures:** For five months, we collaborated closely with the experts in quantum computing to conduct the preliminary study. To ensure our approach was tailored to seamlessly fit into domain users' routine tasks, we divided the whole procedure into two separate sessions. First, we began the first session by performing one-on-one, semi-structured, hour-long interviews with all the domain experts. During the interview, we posed carefully-crafted questions (see Appendix ??) relevant to the interpretability improvement of quantum circuits. For the second session, we summarized the initial design requirements and developed a low-fidelity prototype to meet the basic needs according to their feedback. Next, we presented this prototype to the experts for iterative expert tests in the next three months. They were then asked to explore the prototype freely and share their concerns and suggestions in a think-aloud manner; we then use their feedback to refine and improve the prototype accordingly.

### B. Design Requirements

We distilled the collected feedback from the preliminary study to inform our design. Overall, we summarized users' general process as two levels of analysis, *i.e.*, **global** analysis and **local** analysis. Specifically, the global analysis (**R1-3**) aims to explain the effects of quantum gates from a high-level perspective, while the local analysis (**R4-6**) provides a more fine-grained explanation for the *quantum states* by illustrating the rationale of the measured probability of each basis state.

**R1** **global** **Provide an overall summary of the quantum circuit.** Five participants (**P1-4**, **P6**) emphasized the importance of providing users with a coarse-grained overview of the whole quantum circuit regarding the temporal changes of *probabilities*, making it easier to interactively select the blocks of interest from a large number of gate operations. **P2** also mentioned the necessity to break the *blocks* into a linear sequence of the individual gate operation, namely *steps*, to illustrate the effect of each quantum gate better.

**R2** **global** **Explain the effect of quantum gates visually.** All participants (**P1-6**) strongly suggested that the visual designs should focus on the detailed explanation of the most basic ingredients (*i.e.*, quantum gates). Specifically, three participants (**P1**, **P5-6**) encouraged us to utilize the

basis states to depict the evolution of quantum states. Meanwhile, three experts (**P2-4**) also expressed the need to “*visualize the quantum gate's effect via comparing how the amplitudes change the measured probability before and after the quantum gate.*”

**R3** **global** **Support the trace-back analysis of quantum states.** Three participants (**P1**, **P3**, **P5**) expected the approach to enable the trace-back analysis of quantum states. They all confirmed that it is significant to visually reveal how a specific quantum state was generated from the beginning of the quantum circuit. Moreover, **P3** emphasized that the intuitive visualization of the original quantum circuit can significantly flatten the learning curves for domain users.

**R4** **local** **Explain the probability of basis states visually.** All participants (**P1-6**) confirmed that it would significantly help to inform users of each basis state's probability change, enhancing their confidence in understanding the effects of the quantum gates. In particular, four participants (**P1-3**, **P5**) emphasized the importance of visually correlating the amplitudes and probabilities other than by a set of individual visualizations (*e.g.*, several bar charts), because they believed that the explicit and correlated visual channels could intuitively highlight how amplitudes determined the measured probabilities.

**R5** **local** **Support the visualization of multi-qubit quantum states.** According to the suggestions from four participants (**P1**, **P3**, **P5-6**), the most common visualization for quantum states, *i.e.*, Bloch Sphere, cannot support multi-qubit state visualization. **P3** commented that this issue is unacceptable because the real power of quantum computing, *i.e.*, entanglement, requires multiple qubits. **P6** also said “*I really hope there exists a visual representation to make the multi-qubit state more intuitive.*”

**R6** **local** **Address the issues of visual scalability.** **P1** and **P3** pointed out the issue of visual scalability. Specifically, **P1** emphasized that scalability issues are typical quantum-specific problems that need to be addressed. Also, **P1** commented “*There will be a substantial quantity of basis states in the common cases.*” **P3** also comments that visualizing many basis states is a complex task, given the requirement to display both the probability and amplitudes of each basis state concurrently.

### C. Dataset

Building upon the above design requirements, we developed the system *QuantumEyes* based on *Qiskit* [54], which is an open-source framework for the implementation of quantum circuits. We utilized a quantum simulator, *i.e.*, *AerSimulator* [55], to extract quantum states. The raw dataset extracted contains the properties of the quantum circuit: the sequence and implementation of quantum gates on the individual qubits, the state vectors of the quantum states over each step, and the transformation matrices of the quantum gates.

Next, to obtain the probability of each basis state, we leveraged Equation 3 to calculate the amplitudes from the quantum state's state vector. Also, we decomposed the matrix



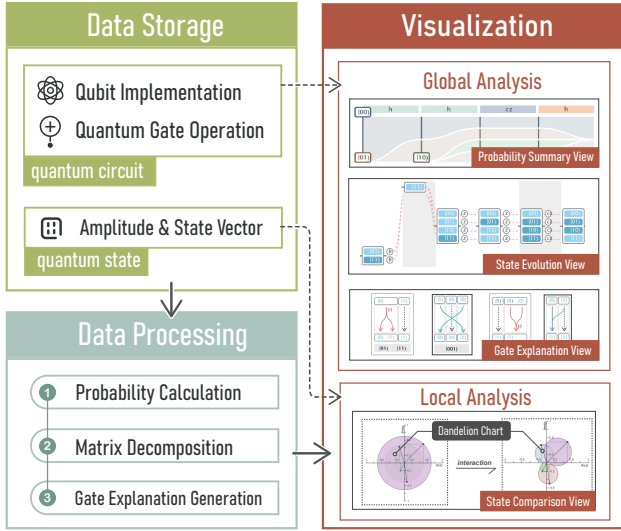


Fig. 2. The system architecture of *QuantumEyes* consists of a **data storage** module, a **data processing** module, and a **visualization** module.

of state vector by rows to extract all basis states of a quantum state, making it available for analysis of the trajectory of the quantum states (see Appendix ??). Furthermore, based on the principle of unitary transformation [56], we deconstructed each block (Fig. 6C) into multiple *steps* (Fig. 6B) to better clarify the workflow of a quantum circuit.

### V. *QuantumEyes*

We proposed *QuantumEyes*, an interactive visualization system to enhance the interpretability of quantum circuits. The architecture of *QuantumEyes* consists of three tightly-connected modules: (1) data storage module, (2) data processing module, and (3) visualization module, as shown in Fig. 2. In particular, the data storage module stores all raw input data of the original quantum circuit. The data processing module supports the data preparation procedure before visualization, including the probability calculation of each quantum state, the decomposition of state vectors for state evolution analysis, and the generation of the transformation representation based on the qubit states. The visualization module reveals insights hidden in the quantum circuits, where three views (*i.e.*, Probability Summary View, State Evolution View, and Gate Explanation View) are applied for the **global** analysis and the novel design (*i.e.*, *dandelion chart*) is used for the **local** analysis. Furthermore, we also implement an original quantum circuit (Fig. 5D), enabling domain users to efficiently conduct the comparative analysis with our visual designs. The system interface of *QuantumEyes* is shown in Appendix ??.

#### A. Probability Summary View

We propose the Probability Summary View (Fig. 3A) to provide an intuitive summary of the quantum circuit in terms of probability changes of basis states over each step (R1). We leverage the stacked area chart to portray the basis state's measured probability on each step, where the length of line segments encodes the probability (Fig. 3A2). Specifically, we

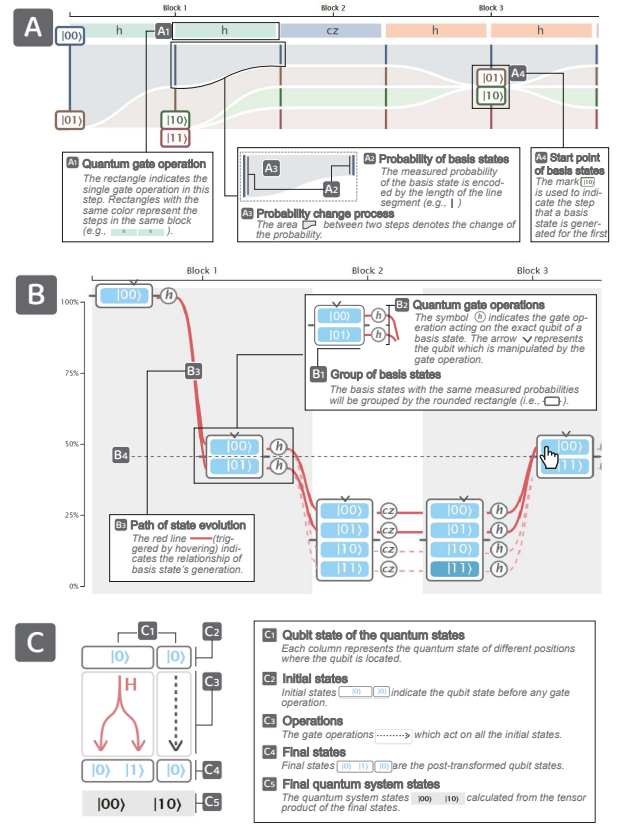


Fig. 3. The three coordinated views in *QuantumEyes* for **global** analysis. (A) Probability Summary View summarizes a quantum circuit via all basis states' temporal change of probabilities. (B) State Evolution View supports a fine-grained analysis of the basis states' evolution across each step. (C) Gate Explanation View visually explains the effect of quantum gates from the perspective of the qubit state.

use a set of line segments arranged vertically to reveal the probability proportion at each step. The total vertical length of all line segments at each step is a constant as the sum of all basis states' probabilities will always be 1.0. Also, we utilize the area (Fig. 3A3) to highlight the probability change of each basis state between steps. Moreover, we use a set of rectangles to denote the hierarchy of blocks and steps, where the rectangles in the same color are in a common block (Fig. 3A1). Note that the order of qubit labeling in the annotation is from left to right, while the qubit order in the view of original quantum circuit is from bottom to top. Furthermore, we append the annotations (*e.g.*,  $|101\rangle$ ) at the left-most area (Fig. 3A4) to depict the creation of a basis state. To enable the drill-down analysis from the summary of the quantum circuit (R1), users can interactively brush the steps of interest in Probability Summary View.

#### B. State Evolution View

The State Evolution View (Fig. 3B) enables a drill-down analysis of the evolution of quantum states such as the separation and merging of basis states for Hadamard gates [57] (R2). The design also supports the trace-back analysis (R3), making users aware of how a basis state was generated and further transformed by quantum gates.

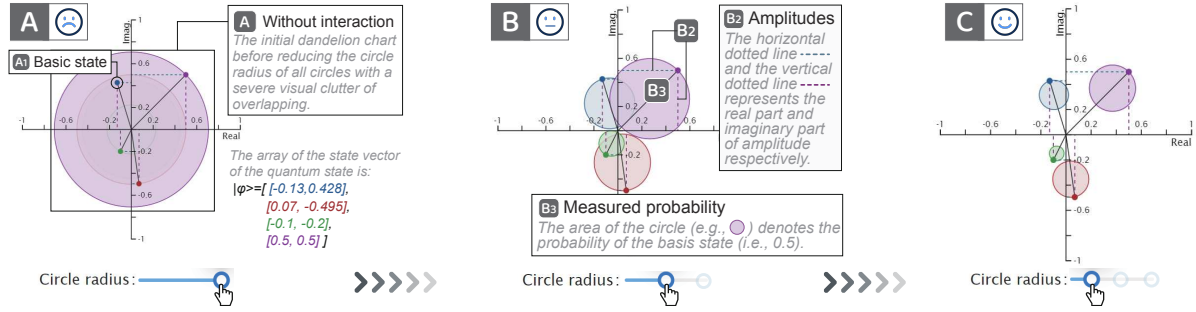


Fig. 4. The *dandelion chart* embedded in Probability Explanation View. (A) The *dandelion chart* before interaction with all circles overlapped with each other. (B) The *dandelion chart* after reducing the area of all circles by a factor of **0.5**, where the visual clutter is mitigated slightly. (C) The *dandelion chart* after reducing the area of all circles by a factor of **0.25**, where all circles are completely separated apart and can be compared clearly.

We visualize the evolution of all the basis states using a graph-like design. Due to the consistency of the encoding of the horizontal axis, State Evolution View can also enable users to better compare with the Probability Summary View (R1). The horizontal coordinate indicates the steps of the quantum circuit, while the vertical coordinate represents the basis state's measured probability. We use rounded rectangles to represent the entity of the basis state. Meanwhile, those basis states with the same probability are grouped by the outer rectangle (i.e.,  $\square$ ), as shown in Fig. 3B1, where the outer rectangles' short line segments refer to each group's measured probability. Moreover, we encode the evolving relationship between the two steps using pink dotted lines. To indicate the gate operation, we use a symbol with the acronym inside after each basis state (Fig. 3B2); we then mark the qubit that the quantum gate acts on by the arrows. Note that the rectangles will be colored in light blue  $\square$  if the basis state's real part is positive; otherwise, it will be colored in blue  $\square$ . We enable flexible interactions to enhance the usability of the system for users within the domain (R3). Precisely, users can hover over the specific state to analyze the evolution path highlighted in red lines (Fig. 3B3).

**Justification.** Prior work has also studied to explain quantum circuits by visualizing measured probability. Lin et al. [12] and Karafyllidis et al. [41] studied how to explain the behaviors of the overall quantum circuit using the encoding of color. Williams [13] utilized the length to indicate the measured probability of single qubits. In *QuantumEyes*, we use the vertical position of the basis state instead of the encoding of color or length since the position has been proven a more effective visual channel for human perception [50].

### C. Gate Explanation View

The Gate Explanation View (Fig. 3C) aims to allow users to understand a gate operation based on the qubit state (R2). We first deconstruct the quantum system states (e.g.,  $|01\rangle$ ) into qubit states (e.g.,  $|0\rangle$  and  $|1\rangle$ ); we then visualize the explanation via a table-like design.

We define an arbitrary transformation as three parts, i.e., the initial state, operation, and the final state; we then represent the three parts with the table's first, second, and third row, respectively. The column denotes each qubit in the original basis state. Meanwhile, we apply various colored lines (e.g.,

for Hadamard gates) to represent the operation of quantum gates acting on the individual qubits (Fig. 3C3). Note that the operation will be represented as the dotted grey line if no quantum gate acts on a qubit. For example, as shown in Fig. 3C, assume there is a basis state ( $|00\rangle$ ), the post-processed initial state is  $|0\rangle$  and  $|0\rangle$ . After the Hadamard gate on the first qubit  $|0\rangle$ , the first qubit converts to a state in superposition, i.e.,  $|0\rangle$  and  $|1\rangle$  each with a probability of 0.5, while the second qubit keeps as it is, i.e.,  $|0\rangle$ . Thus, the final state will be  $|00\rangle$  and  $|10\rangle$ .

### D. Dandelion Chart

To enable the explanation of measured probability (i.e., **local** analysis), we propose *dandelion chart*, a novel geometrical representation to visually explain the measured probabilities of basis states (Fig. 4). According to the quantum theory, we encode the amplitudes by 2D shapes to visualize arbitrary quantum states, including multi-qubit states (R5). We also visually correlate the probability with the corresponding amplitudes based on geometry principles to explicitly explain the measured probability of basis states (R4). Moreover, *dandelion chart* allows users to mitigate the visual clutter of numerous basis states via a geometry-based approach (R6). The *dandelion chart* is incorporated into *QuantumEyes* to facilitate the comparison between two quantum states before and after a gate operation, as shown in Fig. 6B4-7.

**Amplitudes encoding.** To visually represent a quantum state and the respective basis states, we leverage amplitudes of quantum states as they are the basic components of a specific quantum state [58], [59]. Recall that the amplitude of each state is intrinsically a complex number, consisting of a real and imaginary part, as illustrated by Equation 2. For each quantum state, we first apply a Cartesian coordinate system to represent the series of its amplitudes of each basis state based on Equation 1, where the x-axis encodes the real part, and the y-axis encodes the imaginary part. Thus, all the basis states of a quantum state are visualized as a set of points, as shown in Fig. 4A1. To further highlight amplitudes, the absolute values of real and imaginary parts are encoded by perpendicular lines in green and red from a point to the y-axis and x-axis (Fig. 4B2). Furthermore, we visualize the line connecting the point to the system's origin to highlight its position.

**Probability explanation.** According to Equation 3, the measured probability of each basis state can be calculated by the real and imaginary parts of the amplitudes. Meanwhile, based on geometry principles, the circle's area can be calculated using the radius, which is equal to the distance between the basis states' points and the origin of the system:

$$S_{circle} = \pi \cdot (|a|^2 + |b|^2), \quad (4)$$

where  $a$  and  $b$  are the real and imaginary parts of the amplitude. Thus, building on the Equations 3 and 4, we conclude that the area of the circle can represent the measured probability of a basis state as the area of the circle is proportional to the measured probability, as shown in Fig. 4B<sub>3</sub>. By this means, users are allowed to visualize the probability of the basis state in terms of their corresponding amplitudes indicated by the x- and y-coordinates of the points. However, there can exist a severe overlap between the circles (Fig. 4A<sub>1</sub>).

**Visual clutter mitigation.** We mitigate the visual clutter by scaling the area of circles through user interaction. By this means, all circles can be separated apart by decreasing all circles' radii, like the process from Fig. 4A<sub>1</sub> to Fig. 4C<sub>1</sub>, while preserving the nature of reflection of the state's probability using amplitudes.

Specifically, if the radii of all the circles are reduced with the same factor  $k$  while keeping the point on the edge of the circle. Then circle area satisfies the following equation:

$$S'_{circle} = \pi \cdot k^2 \cdot (|a|^2 + |b|^2), \quad (5)$$

where  $k \in [0,1]$  is the factor for shrinking the area of circles. Meanwhile, based on Equations 3 and 5, then the area of the circle is still proportional to the measured probability due to the constant factor  $k$ . This finding means that users can scale the area of circles freely to mitigate the overlap while preserving the property of the representation of probabilities by the circles. Hence, *dandelion chart* can support probability explanations regarding amplitudes of the basis state through the user interaction of scaling the circles' radii. We name the design as "*dandelion chart*" due to the dandelion metaphor for each basis state like each entity in Fig. 4C<sub>1</sub>.

**Justification.** The prior work by Lamy [45] also utilized the rectangle area to facilitate the measured probability analysis as well as the portray of entanglement and phase. Our novel design *dandelion chart*, however, can *explain* the measured probability regarding the amplitudes by the location and the corresponding circle area, while preserving the capability of phase and entanglement representation. Specifically, building upon Cartesian coordinates, *dandelion chart* encodes the probability by circle areas and further explains it by the location of the points based on the quantum mechanism constraints.

## VI. CASE STUDY

In this section, we conducted two case studies on two popular quantum algorithms, *i.e.*, Grover's Algorithm [60] and Quantum Fourier Transform (QFT) algorithm [61], to demonstrate the usefulness of *QuantumEyes*. Also, all experts were asked to use a monitor with a resolution of  $1920 \times 1080$  beforehand.

### A. Case Study I - Grover's Algorithm

Grover's algorithm [60] is a quantum computing algorithm for searching an unsorted database, which is shown to be more efficient than classical algorithms. It works by repeatedly applying a process called amplitude amplification, which increases the probability of selecting the correct item(s) and decreases the probability of other items. We worked with E12, whose research interest includes applying Grover's Algorithm to speed up the unstructured searching problems. To find more insights behind the quantum circuit used in his research, E12 leveraged *QuantumEyes* to interactively explore Grover's Algorithm. Following the example [62], we implemented a 2-qubit Grover's Algorithm for the study.

**Identifying the functionality block from the visualization.** E12 began by examining the Probability Summary View and quickly noticed that the probability of State  $|00\rangle$  was the largest at the beginning of the circuit. However, this dominance gradually diminished and was replaced by State  $|11\rangle$  eventually. He noted that this transition occurred due to the functionality block of *amplitude amplification* identified by the stacked areas (Fig. 5A<sub>3</sub>), despite having no prior knowledge of the specific basis state being sought (R1). Bearing this in mind, E12 became curious about the other functionality blocks of Grover's Algorithm, *i.e.*, the initialization and the *oracle*. With the clear goal, E12 found that the probabilities of the four basis states were identical, each having a probability of 0.25 as shown in Fig. 5A<sub>1</sub>. E12 identified the step following the two Hadamard gates (*i.e.*, H gates) at the end of the initialization, as all basis states are in a state of superposition with equal probability, precisely reflecting the characteristic of the initialization. E12 then noticed that the identified initialization was succeeded by a gate sequence of the "H-CX-H" combination. "*These three gates are commonly employed as an oracle that flips the signs of states.*" We directed E12's attention to the *dandelion chart* for analyzing the amplitudes (R2, R4). Utilizing this function, E12 discovered the amplitudes of State  $|11\rangle$  were flipped to negative values (Fig. 5A<sub>2</sub>). "*This is precisely what I anticipated. The flip of State  $|11\rangle$  aligns with the findings of the target state we speculated earlier. Moreover, the flip of the amplitude confirmed that the three quantum gates are an oracle for sure.*"

**Uncovering the facts of the initialization and oracle.** After the identification, E12 started to perform an in-depth analysis of each functionality block. By brushing the steps of initialization and the oracle from the stacked area chart, the State Evolution View was displayed as shown in Fig. 5B<sub>1</sub>. To delve further into the quantum gate's effect from a high-level perspective (R2), E12 clicked the "h" symbols of the Hadamard gate and displayed the visual explanations of the Hadamard gates (Fig. 5C<sub>1</sub>). Taking a close look at the appended view, E12 observed that the first qubit stayed still without any operation, while the second qubit was split into two states  $|0\rangle$  and  $|1\rangle$  in superposition. E12 commented "*I am truly impressed that this visualization can easily explain why the final states are  $|00\rangle$  and  $|01\rangle$  through the decomposition of the gate operation.*"

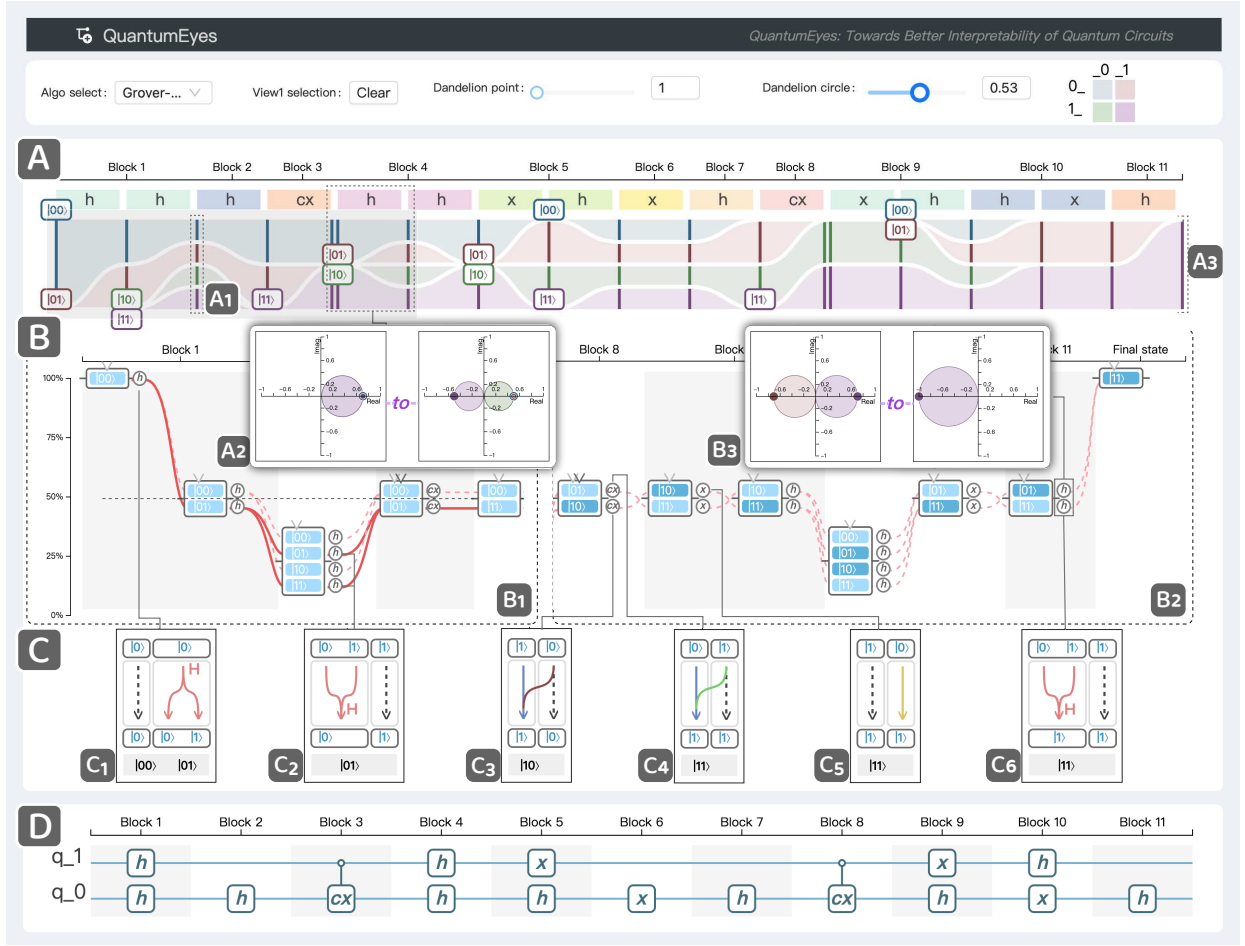


Fig. 5. The visualization system *QuantumEyes* enhances the interpretability of Grover's Algorithm through the global analysis (A-C) to explain the operations of quantum gates and local analysis (A<sub>2</sub> and B<sub>3</sub>) to reveal the implicit reasoning of basis state's measured probability. The original quantum circuit (D) is given for a better comparison of *QuantumEyes* and quantum circuit diagrams. The execution order for the two-gate block is from the qubit with a higher number to a lower number (e.g., from  $q_1$  to  $q_0$ ).

The expert then moved on to the analysis of the oracle, which is used to flip the signs of the target state (i.e.,  $|11\rangle$  in Block 4). “I am curious about how the target  $|11\rangle$  was generated before the amplification process” (R3), E12 commented. Through hovering over the target state  $|11\rangle$ , E12 noticed an eye-catching red path to indicate how the  $|11\rangle$  was generated, as shown in Fig. 5B<sub>1</sub>. He could confidently identify that the States  $|01\rangle$  and  $|11\rangle$  are the origin of the evolution, which were merged by the following Hadamard gate (Fig. 5C<sub>2</sub>).

**Exploring the hidden insights of the amplification.** E12 proceeded to analyze the functionality block of amplification, which is employed to amplify the probability of the flipped target state. By brushing the corresponding steps in the stacked area chart, E12 got a quick intuition of the operations of the CNOT gate (Fig. 5C<sub>3</sub> and C<sub>4</sub>) and the NOT gate (Fig. 5C<sub>5</sub>). To determine the reason for the sudden increase in the probability of State  $|11\rangle$  (R2), E12 took a glance at Fig. 5C<sub>6</sub> and quickly noticed that the Hadamard gate merged the first qubit's state (i.e.,  $|0\rangle$  and  $|1\rangle$ ) and generated a new qubit state (i.e.,  $|1\rangle$ ). “This is mainly because the first state  $|0\rangle$  is negative, leading to the new state of  $|1\rangle$  other than  $|0\rangle$ ”, E12 said, “However, I cannot still understand why the probability changes into 1

instead of other numbers” (R4).

Thus, as hinted by us, E12 further moved to the *dandelion chart* of the step by clicking the last step's background. After a glance, he noticed there are two states (i.e.,  $|01\rangle$  and  $|11\rangle$ ) at the left system and only one state (i.e.,  $|11\rangle$ ) at the right with a symbol denoting the operation gate (Fig. 5B<sub>3</sub>). E12 found that the imaginary parts of all states are zero, as indicated by their zero y-coordinates. Furthermore, the real part of State  $|11\rangle$ 's amplitudes changed from around 0.7 in the left chart to -1.0 in the right-hand chart. “I am surprised that the dandelion chart tells me that the flip of phase did not cause the change of the probability, the real part of the amplitude actually makes the state's probability two times its initial state.”

#### B. Case Study II - Quantum Fourier Transform Algorithm

We worked with E3, whose research direction is Quantum Uncertainty, to understand a widely-used quantum algorithm, i.e., Quantum Fourier Transform (a.k.a., QFT) algorithm [63]. The QFT algorithm converts the amplitudes of a quantum state into the corresponding values in the frequency domain, which is similar to what the classical Fourier Transform does with signals. It forms a foundation for other quantum algorithms,



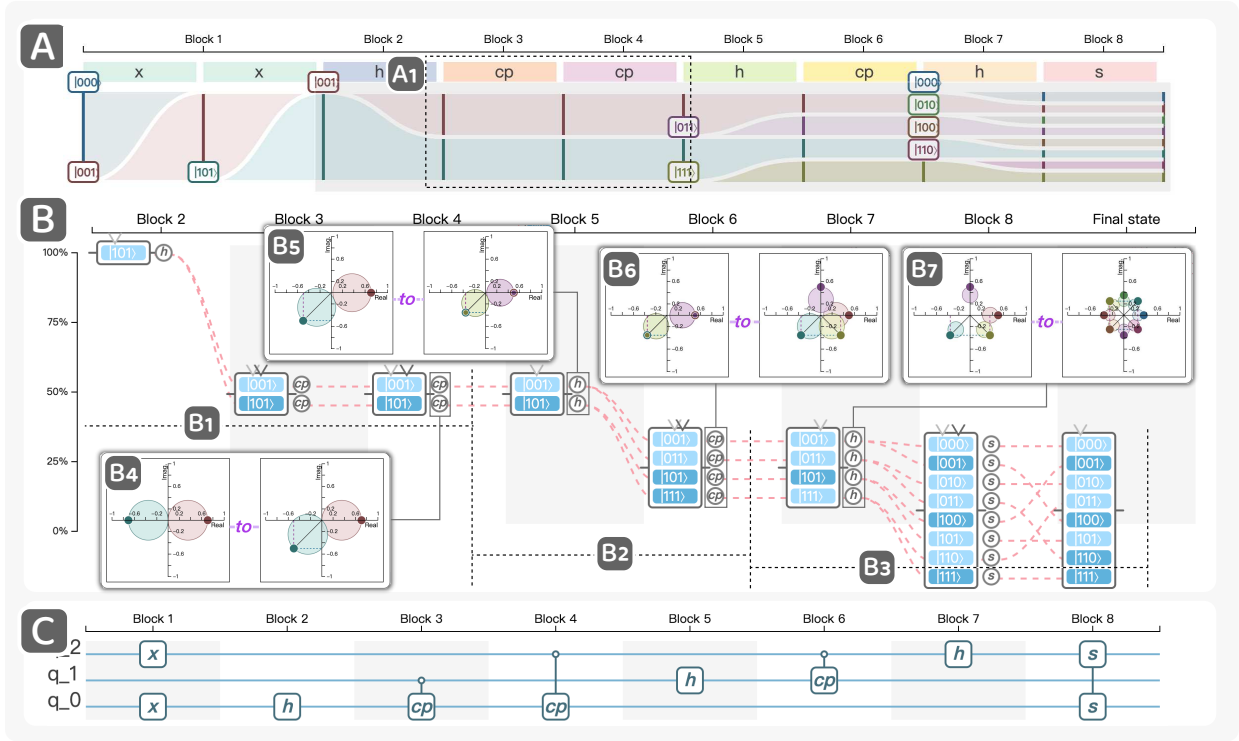


Fig. 6. The case for Quantum Fourier Transform algorithm. Three coordinated views (A-C) visualize the development of basis states for the global analysis, while *dandelion chart* (B4-B7) explains how measured probabilities are determined by amplitudes for the local analysis. The CP symbols in the quantum circuit diagram (C) indicate the Controlled-Phase gates and S symbols indicate the SWAP gates.

such as Shor’s Algorithm [64]. We implemented the quantum circuit following the guidelines of Qiskit [65].

**Understanding the architecture of QFT algorithm.** The expert E3 started by brushing the whole quantum circuit from the probability overview because he thought the QFT algorithm is an entity that cannot be split into different functionality blocks. Indicated by the first two X gates with probabilities of 1.0, E3 commented, “These two X gates are for the state preparation because the lengths of the line segments remain the same during Block 1.” Meanwhile, he speculated the number to be mapped is 5 due to the decimal of State  $|101\rangle$ . After identifying the number to be mapped, E3 started to investigate the quantum circuit architecture of the QFT algorithm (R2). By exploring the State Evolution View along with the original circuits, E3 quickly found that the three key processes of the algorithm “I can easily identify the three iterations of QFT (as shown in Fig. 6B<sub>1</sub>, Fig. 6B<sub>2</sub>, and Fig. 6B<sub>3</sub>) from the three continuous processes with the downward trend of probabilities from the middle view, each making the probability drop to 0.25”. He also praised the advantage of the evolution view to intuitively reveal the temporal change of states’ probabilities along the circuit, making the analysis of the gate’s functionality more efficient and smooth.

**Disclosing the implicit reasons of the measured probability.** E3 then glanced at the probability summary of the QFT algorithm and found that the probability of the two States  $|001\rangle$  and  $|101\rangle$  did not change after the two Controlled-Phase gates (Fig. 6A<sub>1</sub>). Thus, he planned to find more hidden insights about this phenomenon by drilling down to the local

analysis using *dandelion chart*(R4, R5). According to the geometrical representation of Fig. 5B<sub>4</sub>, E3 noticed that the circle of State  $|101\rangle$  rotates around 45 degrees anticlockwise after the Controlled-Phase gate, making the amplitudes change but preserving the circle area. “This design is fascinating to me because I can analyze the gate’s effect from a perspective of geometry intuitively.” Next, he clicked the following Hadamard gate to find the reason for superposition using the *dandelion chart*. From Fig. 6B<sub>5</sub>, E3 noticed the both of the two original States  $|101\rangle$  and  $|001\rangle$  became two smaller circles. “Before today, I can only observe the four states with the same probability of 0.25 after Hadamard gates. It is brilliant to build a mathematical intuition of the measured probability and the amplitudes.” After analyzing the individual quantum gate, E3 planned to investigate how the QFT algorithm represents a random quantum state by a series of continuous basis states (i.e.,  $|000\rangle \cdots |111\rangle$ ). Hence, E3 clicked the last two quantum gates before the final SWAP gate and then adjusted the radius to separate all circles (R6), as shown in Fig. 6B<sub>6</sub> and Fig. 6B<sub>7</sub>. “This actually matches what I expected,” E3 commented “From the first chart, I realized that the Controlled-Phase gate can only ‘rotate’ a state but never ‘separate’ a state into multiple states.” E3 further noticed that the four states are located in four different directions (i.e., cardinal directions and diagonal) (Fig. 6B<sub>6</sub>). And then, the Hadamard gate generates each state into a new basis state in the opposite direction (Fig. 6B<sub>7</sub>), making it possible to handle eight basis states with smaller circle area. “The dandelion chart provides me a holistic picture of how the quantum gate changes the amplitudes of basis

states, which makes the analysis of amplitudes more effective than ever before.”

## VII. EXPERT INTERVIEW

We further conduct a well-designed interview with actual domain experts to demonstrate the effectiveness and usability of *QuantumEyes* and the embedded *dandelion chart*.

### A. Study Design

**Participants and apparatus.** We recruited 12 domain experts (E1-12) (12 males,  $age_{mean} = 34.0$ ,  $age_{sd} = 5.8$ ) from 6 different educational institutions (E1-12) in the U.S. to join our in-depth expert interview. These participants were selected by mainly considering their research background in quantum computing and checking whether they have relevant research experience, guaranteeing the reliability of the collected feedback. More specifically, five participants (E1, E9-12) are working on Quantum Error Mitigation, six experts (E4-7, E8, E13-14) study Quantum Machine Learning (QML), two experts (E2-3) are working on Quantum Uncertainty, and one expert (E7)’s research direction is Quantum System Design. All participants have an average of 5.9 years of experience in quantum computing. The interview was conducted via the online Zoom meeting with a  $1920 \times 1080$  resolution monitor.

**Procedures.** The study was conducted on the online system *QuantumEyes*. We carried out the one-on-one, semi-structured study for all experts. Specifically, we first introduced the visual design of all views of *QuantumEyes* along with *dandelion chart*. Afterward, we invited all participants to accomplish six pre-defined tasks using *QuantumEyes*. The first four tasks are designed to evaluate the effectiveness of *QuantumEyes* for global analysis, including analyzing the overall trend of basis state probabilities, identifying the gate effect, and explaining the gate effect in terms of the changes of basis states and qubit states. The remaining two tasks aim to evaluate the effectiveness of the dandelion chart’s effectiveness for local analysis. The detailed task list can be found in Appendix ??.

We then asked them to verbally explain how the quantum states are evolving across the quantum circuit. The aforementioned process lasts approximately 40 minutes. After completing the tasks, all participants were encouraged to provide feedback on all the proposed visual designs in a think-aloud manner. Furthermore, followed by prior work [47], we also invited participants to rate *QuantumEyes* using a 7-point Likert scale based on the post-study questionnaire (Table I) regarding each aspect of design requirements we collected beforehand. The post-study interview lasted approximately 20 minutes, during which we recorded and took notes about the entire study process.

### B. Result

We summarized all collected feedback regarding the four aforementioned aspects of the evaluation as Fig. 7.

**Effectiveness.** Most participants appreciated the effectiveness of *QuantumEyes* to enhance the interpretability of quantum circuits ( $rating_{mean} = 6.02$ ,  $rating_{sd} = 1.18$ ).

TABLE I  
THE QUESTIONNAIRE CONSISTS OF FOUR PARTS, *i.e.*, THE EFFECTIVENESS (Q1-4), USABILITY (Q5-7), USER INTERACTION (Q8-9), AND VISUAL DESIGNS (Q10-12).

Q1	The workflow of global and local analysis can explain the quantum circuits comprehensively.
Q2	The system can effectively support the evolution analysis of each basis state.
Q3	The system can intuitively explain the gate effect via the visualization of qubit states.
Q4	The dandelion chart can effectively explain the measured probability based on the amplitudes.
Q5	The system is easy to learn.
Q6	The publicly-available QuantumEyes system is helpful for domain users.
Q7	I would like to use the QuantumEyes system to better understand quantum circuits in the future.
Q8	The user interaction of the system is smooth.
Q9	The user interaction is easy to use for domain users.
Q10	The overall design is easy to understand.
Q11	For global analysis, the three coordinated views are helpful in understanding the effects of quantum gates.
Q12	For local analysis, the dandelion chart is useful to visualize how amplitudes affect the probability intrinsically.

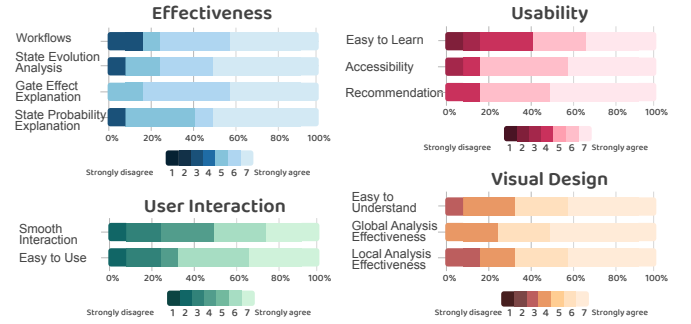


Fig. 7. The summary of the feedback of the questionnaire.

E3-6 agreed that the workflow of global and local analysis is exactly what quantum computing users expect to see to explain the effects of quantum gates. Meanwhile, the trace-back analysis is praised by E1-2 and E9. “I need to manually calculate the state vectors to figure out how a state was produced and developed in my daily work before. This function provided by *QuantumEyes* is really fascinating to me”, E2 said. Furthermore, most participants (E1-7, E9-11) highly appreciate the novel design *dandelion chart*, “which is helpful to grasp the measured probability of basis states.” E11 also commented that *QuantumEyes* can help him with circuit design and debugging due to the intuitive visualization of probability regarding the state’s amplitudes.

**Usability.** The majority of participants applauded the usability of *QuantumEyes* in interactively enhancing the quantum circuit’s interpretability ( $rating_{mean} = 5.88$ ,  $rating_{sd} = 1.65$ ). E2-5 mentioned that the visualization system is user-friendly for quantum computing researchers and learners. Among them, E4 commented, “I can easily interact with the interface and accomplish all tasks, even though I do not have any background in visualization before.” E7 and E12 emphasized that they prefer the easy-to-understand visualizations, and *QuantumEyes* indeed provides the visualizations that they are familiar with in their daily routine tasks, like the

original quantum circuit diagram and the visualization of the transformation of the qubit states.

**User interactions.** Most participants generally agreed that the user interactions in *QuantumEyes* are easy-to-use for quantum computing users ( $rating_{mean} = 5.54, rating_{sd} = 1.66$ ). Among all feedback, **E3-4** and **E9** gave highly positive feedback for the interactions of decreasing the circle radius in *dandelion chart* to reduce the visual clutter. **E3** pointed out that he feels struggle to adopt Bloch Sphere to inspect only the single-qubit state. Dandelion chart addresses the limitations perfectly while preserving the characteristic of displaying the quantum amplitudes. Meanwhile, **E9** confirmed that reducing the circle area is feasible “because users always need to focus on the circle with the largest area.” Furthermore, **E12** also expressed the desire to recommend *QuantumEyes* to his research group members due to the easy-to-use system interactions.

**Visual designs.** Most participants gave positive feedback about the visual designs in *QuantumEyes* ( $rating_{mean} = 6.05, rating_{sd} = 0.99$ ). Specifically, **E5** mentioned that the visual designs for global analysis are informative. “I like the visualization to show the how state evolves because it can directly tell when and how a basis state is developed. This characteristic would truly aid the analysis of quantum algorithms in my daily tasks.” Also, **E7** was willing to adopt *dandelion chart* for his own local analysis of the quantum states, “To my surprise, this design is brilliant because everyone can find the rationale of probability changes without the complex matrix calculation, even for the beginners in quantum computing.”

**Suggestions.** In addition to the positive feedback, several participants also offered constructive suggestions. **E4** suggested that incorporating a feature to fold and unfold the blocks would be helpful for comparative analysis. **E9** also noted that *QuantumEyes* could be extended to visualize the temporal change of parameters in variational quantum circuits. **E10** expressed that a transition might be useful to highlight the difference when comparing a pair of *dandelion charts*.

## VIII. DISCUSSION

In this section, we first summarize the lessons learned during the development of *QuantumEyes* and *dandelion chart*. Then, we discuss the limitations of our proposed visual designs.

### A. Lessons Learned

We reported the learned lessons from the development of *QuantumEyes*.

**Indispensable necessity of visualization to interpret quantum computing.** During the process of working with domain experts in the requirement collection and evaluation, they confirmed the great importance of interpreting quantum computing using visualization approaches. According to the actual use of *dandelion chart*, experts appreciated the impressive design, while also pointed out that quantum computing is not transparent for users to learn, which is exactly the domain where visualization can aid. Thus, they also mentioned that

they preferred the designs with linked visual channels to offer the explanation intuitively.

**Design considerations tailored for quantum computing users.** By working with domain experts, we realize that lowering the learning costs of the proposed visual design for domain users is significant. In our study of design requirements, all participants preferred solutions that were easy to learn, simplifying the paradigm shifts from reading to understanding. For example, the overview of the probability is appreciated and used as the starting point of the system. Also, they praised the implementation of the original quantum circuit in *QuantumEyes* because the comparative analysis with the original circuit can significantly shorten their learning curves.

### B. Limitations and Future Work

There are still several limitations of *QuantumEyes*.

**Application scope.** All the participants highly appreciate the effectiveness of *QuantumEyes* in helping quantum computing developers and users understand the working mechanism of static quantum circuits, which is the widely-used quantum circuits. However, with the growth of another type of quantum circuits, i.e., variational quantum circuits (VQC), also gain more and more attention. Although our novel design *dandelion chart* can be seamlessly applied to VQC applications to analyze quantum state evolution, the visual analytics system (i.e., *QuantumEyes*) as a whole cannot be directly applied to VQC for now. In future work, we plan to extend *QuantumEyes* to analyze variational quantum circuits and other features such as the generalization of the visual feature “Path of state evolution” of *QuantumEyes* to a “Path of Bloch coefficient/Pauli probability evolution”.

**Scalability.** The evaluation has demonstrated that our visualization works well for visualizing the states of two and three qubits. However, due to the limited screen space, the visualization components in *QuantumEyes* for global analysis, i.e., the Probability Summary View, State Evolution View and Gate Explanation View, may suffer from scalability issues with the increase of qubits in quantum circuits. The visualization component of *QuantumEyes* for local analysis, i.e., *dandelion chart*, has better scalability than the above three views, as it can reduce the radii of circles to explain the measured probabilities of more basis states. But when there are a large number of qubits in the quantum circuits, visual clutters may also appear. In the future, it is worth further exploration on how to enhance the scalability of *QuantumEyes*.

**User-friendly interactions.** The availability of *QuantumEyes* gained positive feedback from all participants. However, there are still several limitations regarding the user interactions we collected during the interview. First, to aid the obscure connection between the State Evolution View and the original circuit, we plan to implement the folding and unfolding of basis states and their corresponding quantum gates. Also, the comparison of two quantum states in *dandelion chart* can be improved by utilizing the transition of circles to highlight the effect of quantum gates. Further, to address the issue that the entangled states sometimes cannot be clearly distinguishable in the *dandelion chart*, we plan to add extra

visual elements to highlight those basis states that are entangled using sector length distributions. Last, *QuantumEyes* is expected to enable the functionality of simulator customization and circuit data loading to enhance the system's flexibility.

## IX. CONCLUSION

We present *QuantumEyes* an interactive visualization system to enhance the interpretability of quantum circuits. By working closely with domain experts, we formulate six design requirements in terms of two analysis levels to guide the design of our system. Specifically, we propose three coordinated views (*i.e.*, a Probability Summary View, a State Evolution View, and a Gate Explanation View) to support the global analysis of the quantum state evolution over the whole quantum circuit. Further, we propose a novel geometrical visual design *dandelion chart* for local analysis, enabling users to visually analyze the correlation of basis states' probability and amplitudes based on geometry principles. We conduct two case studies and expert interviews to demonstrate the effectiveness and usability of the proposed visualization approaches. The result shows that our approaches can effectively facilitate domain users to better understand quantum circuits.

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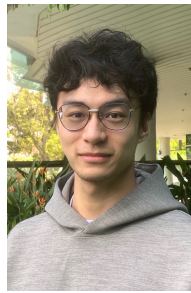
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