

# Two-Dimensional Double Perovskites in the Dion–Jacobson Phase Alleviate Parity Forbidden Transitions for Photovoltaic Applications

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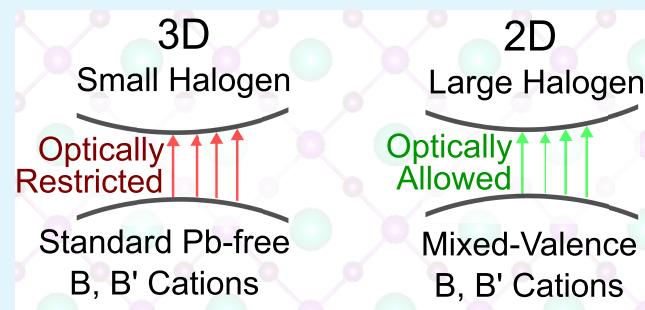
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**ABSTRACT:** Two-dimensional double perovskites have recently been identified as a potential class of materials for the improvement of halide-perovskite-based solar cell technology. The expanded set of utilizable B- and B'-site cations afforded to double perovskites, combined with tunable structural and electronic properties in two-dimensional perovskites, leads to a highly modifiable set of materials, which have yet to be explored. In this study, we investigate the structural, electronic, and thermoelectric properties of these materials and identify a number of key structure–property relationships governing their performance. In the process, we demonstrate a link between the relative electronegativities of the building components and the resultant geometric structures. Furthermore, we provide insights aimed toward alleviating concerns associated with parity forbidden transitions which plague many double perovskite systems. In addition, we identify a number of two-dimensional double perovskites including the mixed-oxidation state  $\text{In}_{25}\text{Tl}_{75}\text{Cl}$ -based system which displays optically active transitions as low as 1.41 eV across the Brillouin zone and indicators pointing toward stable experimental synthesis.

**KEYWORDS:** *double perovskites, two-dimensional materials, photovoltaics, thermoelectric, solar energy harvesting, absorption*



## INTRODUCTION

Perovskite-based photovoltaics have served as an indispensable class of materials in solar energy harvesting for decades, with improvements over the past decade leading to power conversion efficiencies as high as 25.8%.<sup>1–3</sup> Perovskite solar cells, however, exhibit persistent challenges regarding stability, toxicity of building components, and device longevity which motivate ongoing research efforts to mitigate these pitfalls.<sup>4–8</sup> These efforts can largely be categorized by one of three approaches: (1) the investigation into perovskite-based materials of reduced dimensionality, most commonly two-dimensional perovskites (2DPKs), (2) the utilization of a singular replacement divalent B-site cation such as tin or germanium, or (3) the employment of lead-free mixed-metal perovskites that have been termed double perovskites (DPKs) in the literature.<sup>9–16</sup> The above approaches have broadly expanded the search space of perovskite-based photovoltaic materials, and mixed success has been achieved in identifying materials which maintain the optoelectronic properties that make lead-iodide perovskites so attractive while mitigating the concerns that come along with them.<sup>17–19</sup>

Bulk perovskites exhibit a chemical formula of  $\text{ABX}_3$ , with the most typical A/B charge ratio being 1:2 for photovoltaic applications. The additional complexity of double perovskites comes in the form of allowing for combinations of monovalent and trivalent metals at the B-site, which results in a chemical formula of  $\text{A}_2\text{BB}'\text{X}_6$ .<sup>11,20,21</sup> While mixed-divalent cations at the

B-, B'-sites are also possible, these are not as well-explored as the  $\text{B}^{\text{I}}$ ,  $\text{B}^{\text{III}}$  double perovskites in the literature. In terms of perovskites of reduced dimensionality, the family of 2DPKs come in several phases, the two most common of which are the Ruddlesden–Popper (RP) and Dion–Jacobson (DJ) phases.<sup>22</sup> These respectively have chemical formulas of  $\text{A}'_2\text{A}_{n-1}\text{B}_n\text{X}_{3n+1}$  and  $\text{A}'\text{A}_{n-1}\text{B}_n\text{X}_{3n+1}$ , where the  $\text{A}'$  cation represents a long organic molecule which spatially separates adjacent perovskite layers, and  $n$  represents the number of inorganic octahedra in each two-dimensional layer of the material. The difference in stoichiometry of the  $\text{A}'$  cation between the RP and DJ phase comes from the fact that in the DJ phase, the spacer molecule is typically shared between adjacent inorganic layers, resulting in a 1+ (2+)  $\text{A}'$  cation in the RP (DJ) phase.

The introduction of these new approaches to generate highly performant photovoltaic perovskites naturally comes with its own sets of challenges. DPKs have been established to display parity-forbidden transitions in a number of materials which would otherwise serve as highly desirable photovoltaics.<sup>23–25</sup> 2DPKs, on the other hand, struggle with wider bandgaps when

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**Table 1. Structural Properties Associated with the 18 2DDPKs Used in the Present Study**

2DDPK	$\Sigma$ (deg)	$\Delta$	$\Delta_2$ ( $\text{\AA}^2$ )	$t_g$	$\mu$	$X_{\text{BX}}$	$B\text{-}X_{\text{ave}}$ ( $\text{\AA}$ )	$E_{\text{form}}$ (eV)
AuBiCl	10.93	$2.8 \times 10^{-2}$	$1.9 \times 10^{-01}$	0.87	0.66	0.88	3.04	-3.78
AuBiI	11.14	$2.3 \times 10^{-2}$	$2.0 \times 10^{-01}$	0.85	0.55	0.38	3.34	-3.57
AuSbCl	11.33	$3.0 \times 10^{-2}$	$3.0 \times 10^{-01}$	0.91	0.59	0.87	3.02	-3.77
AuSbI	10.89	$2.5 \times 10^{-2}$	$7.0 \times 10^{-01}$	0.88	0.48	0.37	3.34	-3.57
In <sub>25</sub> Tl <sub>75</sub> Cl	4.87	$1.6 \times 10^{-3}$	$8.9 \times 10^{-02}$	0.88	0.64	1.50	2.86	-3.78
In <sub>25</sub> Tl <sub>75</sub> I	3.46	$6.9 \times 10^{-4}$	$6.7 \times 10^{-02}$	0.86	0.53	1.00	3.17	-3.56
In <sub>75</sub> Tl <sub>25</sub> Cl	4.83	$2.0 \times 10^{-3}$	$7.3 \times 10^{-02}$	0.83	0.73	1.42	2.86	-3.81
In <sub>75</sub> Tl <sub>25</sub> I	3.56	$2.7 \times 10^{-4}$	$7.5 \times 10^{-02}$	0.82	0.60	0.92	3.16	-3.59
InBiCl	4.66	$4.6 \times 10^{-4}$	$9.5 \times 10^{-02}$	0.87	0.66	1.26	2.90	-3.80
InBiI	3.26	$2.9 \times 10^{-4}$	$4.9 \times 10^{-02}$	0.85	0.54	0.76	3.18	-3.59
InSbCl	4.75	$1.7 \times 10^{-3}$	$7.7 \times 10^{-02}$	0.91	0.58	1.25	2.88	-3.79
InSbI	3.04	$3.4 \times 10^{-4}$	$4.7 \times 10^{-02}$	0.89	0.48	0.75	3.15	-3.58
InTlCl	4.08	$4.5 \times 10^{-4}$	$3.9 \times 10^{-02}$	0.89	0.62	1.46	2.85	-3.81
InTlI	3.59	$3.6 \times 10^{-4}$	$8.1 \times 10^{-02}$	0.87	0.51	0.96	3.16	-3.58
TlBiCl	5.06	$5.8 \times 10^{-4}$	$9.3 \times 10^{-02}$	0.85	0.70	1.34	2.94	-3.80
TlBiI	4.15	$4.0 \times 10^{-4}$	$1.1 \times 10^{-01}$	0.83	0.58	0.84	3.23	-3.59
TlSbCl	5.11	$1.0 \times 10^{-3}$	$8.6 \times 10^{-02}$	0.89	0.62	1.33	2.90	-3.79
TlSbI	3.86	$4.2 \times 10^{-4}$	$8.5 \times 10^{-02}$	0.87	0.51	0.83	3.19	-3.58

compared with their bulk counterparts, particularly when the layer thickness,  $n$ , is on the order of 1–5.<sup>26</sup> Combinations of double perovskites and two-dimensional perovskites, herein referred to as 2DDPKs, have only emerged very recently in the literature.<sup>27–30</sup> The introduction of 2DDPKs allows for many combinations of monovalent and trivalent cations to mitigate the wide bandgap concerns of 2DPKs, as well as selection of the A' spacing cations to reduce symmetry and alleviate the otherwise forbidden optical transitions at the band edge. While the potential of 2DDPKs is very promising, limited research has been carried out on a subset of these materials simultaneously to aid in generalizing the key structure–property relationships in this subclass of perovskites.<sup>31</sup> To address this gap in the literature, in this work, we use *ab initio* density functional theory (DFT) calculations to consider 18  $n = 2$  2DDPKs in the DJ phase all employing A' = 3-(aminomethyl)piperidinium (3AMP), and A = cesium (Cs). We investigate the structural, electronic, and thermoelectric properties of these materials and uncover the importance of elemental electronegativities for the resulting 2DDPK geometry, key insights toward alleviating concerns associated with parity forbidden transitions, and an excellent linearly scaling relationship between PBE band gaps and those which can be directly compared with the experiment by way of the GLLB-sc functional.<sup>32</sup> Furthermore, we identify a number of new 2DDPKs including the novel mixed-oxidation state In<sub>25</sub>Tl<sub>75</sub>Cl-based 2DDPK, which displays optically active transitions as low as 1.41 eV across the Brillouin zone (BZ) and indicators pointing toward stable experimental synthesis.

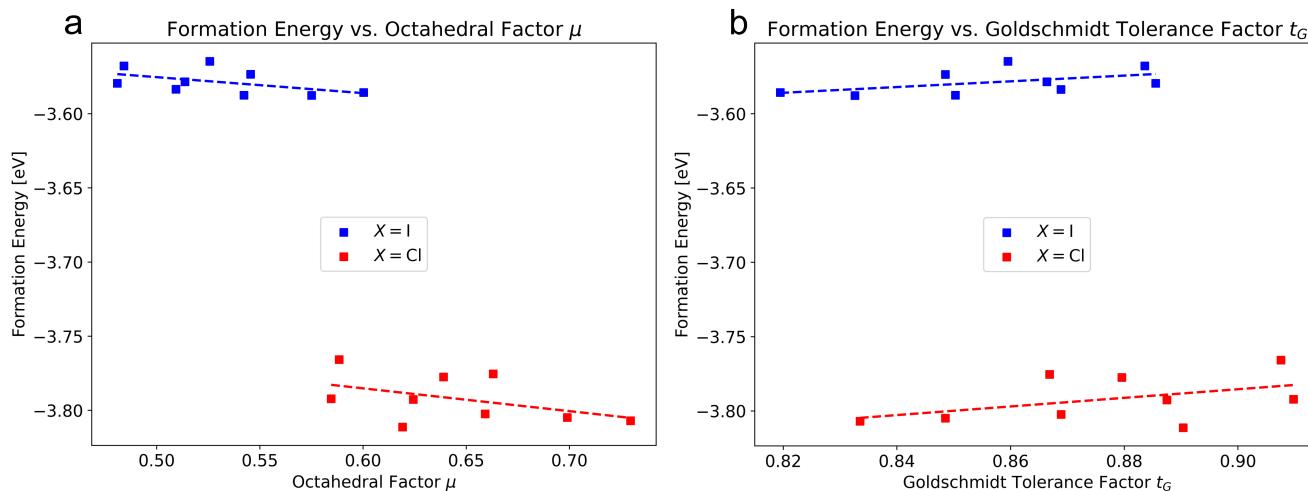
## RESULTS AND DISCUSSION

We constructed initial structures of all 2DDPKs using the Pyrovske package, allowing for the uniform generation of 2DDPKs with varied building components.<sup>33</sup> We employed combinations of monovalent metals at the B-site of M<sup>I</sup> = Au, In, Tl, trivalent metals at the B'-site of M<sup>III</sup> = Bi, Sb, Tl, and halogens at the X-site of X = Cl, I. This selection comprises both novel B-, B'-site combinations as well as some known to exhibit band gaps in the bulk phase which are favorable to photovoltaic applications such as In, Sb.<sup>34–36</sup> Our selection here was informed by previous work carried out by Meng et al.

concerning the optical availability associated with different B-, B'-site pairings in bulk double perovskites.<sup>23</sup> Noted in their work are the large optical issues associated with monovalent B-site cations such as Na, K, Rb, Cs, Ag, Au, and Cu. With this being the case, we focus primarily on the more favorable In- and Tl B-site cations, with the inclusion of Au to assess the extension of their work to double perovskites. Due to the fact that all 2DDPKs in the present study contain A' = 3AMP, and A = Cs, in discussion we identify the perovskite by the B, B', and X building components, such as InSbI. We also exploited the fact that both In, and Tl can exhibit 1+ and 3+ oxidation states, to consider 0.25 and 0.75 occupancies of these cations, herein referred to as In<sub>25</sub>Tl<sub>75</sub>X and In<sub>75</sub>Tl<sub>25</sub>X, respectively.<sup>37</sup> The full list of structures and associated geometric properties can be found in Table 1. We found all structures except those containing Au at the B-site to crystallize in stable perovskite structures with intact octahedra upon density functional theory (DFT) geometry optimization. In all four Au-containing 2DDPKs, the Au-X interactions result in the formation of AuX<sub>2</sub> fragments which do not generate a stable perovskite structure. We've computed octahedral distortion parameters  $\Sigma$ , which represents the deviation from idealized X-B-X bond angles in the BX<sub>6</sub> octahedra;  $\Delta$ , which represents deviations from average B-X bond lengths; and  $\Delta_2$ , which describes diagonal dislocations of the B-cation within the planes of the octahedra.  $X_{\text{BX}}$  in Table 1 represents a weighted absolute difference between the Pauling electronegativities of the B, B' site cations and the X halogens, as detailed in eq 1 below where  $w_B$  and  $w_{B'}$  correspond to the stoichiometric weightings of the B-, B'-sites cations, and  $X_i$  corresponds to the Pauling electronegativity of element  $i$ .

$$X_{\text{BX}} = \left| \frac{w_B X_B + w_{B'} X_{B'}}{2} - X_X \right| \quad (1)$$

We computed Pearson correlation coefficients between  $X_{\text{BX}}$  and the octahedral distortion parameters across the 18 2DDPKs and note a strong negative correlation between these octahedral distortion parameters and  $X_{\text{BX}}$  ranging from -0.48 to -0.57. This implies that the large electronegativity difference between B, B', and X components confers a rigidity to the resultant perovskite which we rationalize by the



**Figure 1.** (a) Formation energy vs octahedral factor  $\mu$  and (b) formation energy vs Goldschmidt tolerance factor  $t_G$  for the 18 2DDPKs in the present study. Dashed lines represent linear fits for each subset of X-halogens.

increased ionic nature of B-X and B'-X interactions, producing closer to idealized octahedral structure. This provides valuable insight for scenarios where distortions in perovskite octahedra are necessary to facilitate the tuning of band gaps, or to increase the optical availability of low energy transitions by reducing or removing symmetries present. Additionally, average B-X, B'-X bond distances (B-X<sub>ave</sub> in Table 1) are reduced in the Cl-containing perovskites compared with the corresponding I-containing systems by 0.295 Å, resulting in smaller in-plane lattice parameters as well as increased stability as indicated by formation energies which experience a commensurate decrease of on average 0.21 eV. This is largely attributed to the smaller ionic radius of the chloride ion compared to that of iodide.<sup>38</sup>

The Goldschmidt tolerance factor ( $t_G$ ) and octahedral factor ( $\mu$ ) are two parameters computed from the ionic radii of the A-, B-, and X-site ions in bulk perovskites as a heuristic to indicate the stability and phase of the perovskite once synthesized.<sup>39,40</sup> We adapt these formulas to use a weighting of the B- and B'-site ions to compute an average ionic radius  $\tilde{R}_B$  for usage in DPKs as detailed in eqs 2, 3, and 4. In eq 2,  $w_i^I$  and denote the stoichiometric weighting necessary to obtain the weighted average of ionic radii, and  $R_{B_i^I}$  denotes the ionic radius of element  $i$  in oxidation state  $I$  obtained from Shannon et al.<sup>38</sup>

$$\tilde{R}_B = \sum_{B_i^I} w_i^I R_{B_i^I} \quad (2)$$

$$t_G = \frac{(R_A + R_X)}{\sqrt{2}^* (\tilde{R}_B + R_X)} \quad (3)$$

$$\mu = \frac{\tilde{R}_B}{R_X} \quad (4)$$

Regions of stability for the tolerance factors in bulk DPKs are  $0.813 < t_G < 1.107$ , and  $0.377 < \mu < 0.895$  respectively.<sup>41</sup> The dimensional reduction to 2DPKs, especially for low layer thicknesses,  $n$ , can in some cases expand the acceptable  $t_G$  and  $\mu$  ranges. This is largely because corrugation in the out-of-plane direction can alleviate the geometric issues associated

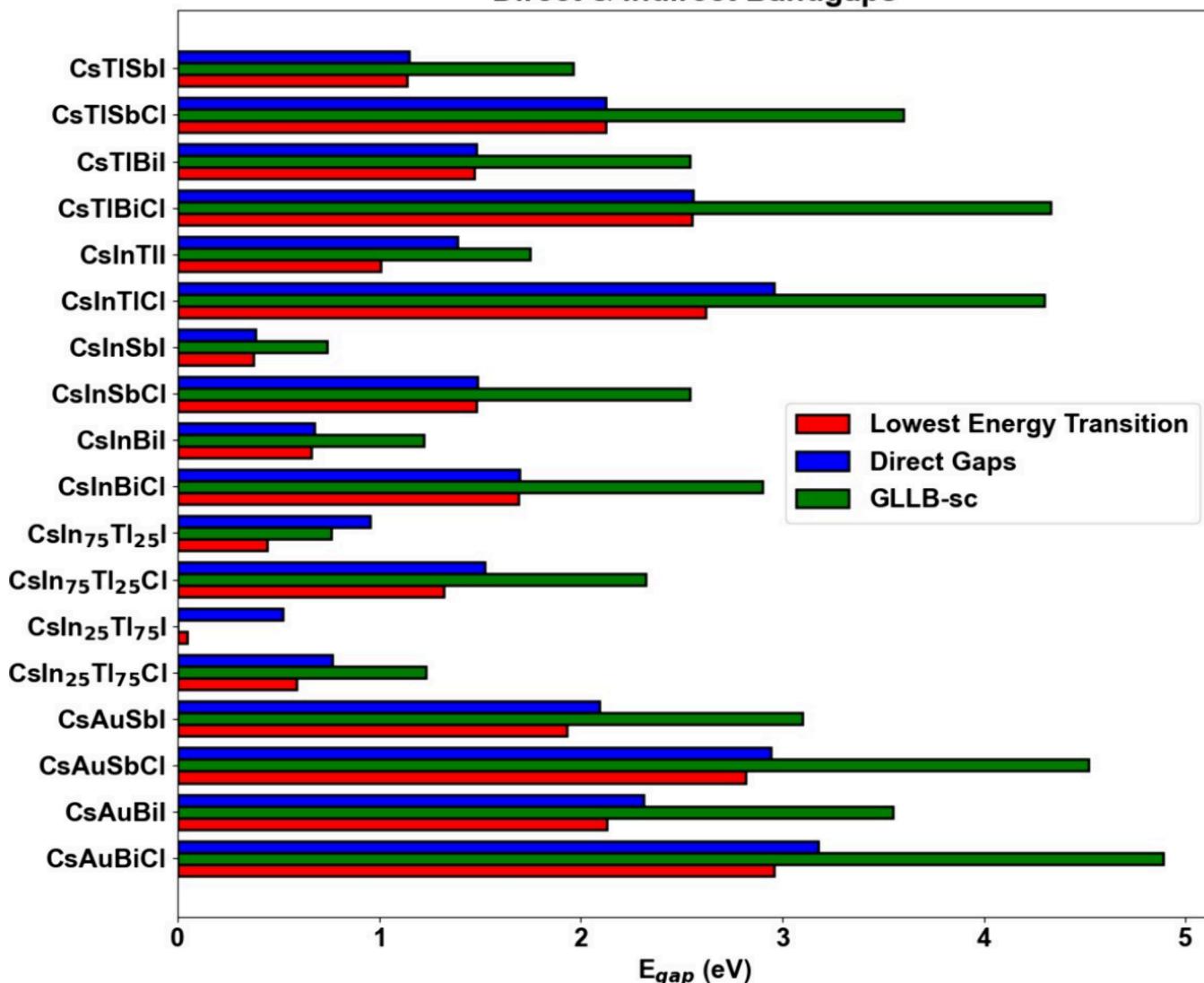
with mismatched ionic radii.<sup>38</sup> Figure 1 shows the formation energies plotted against  $t_G$  and  $\mu$  for all 18 2DDPKs in the present study. Formation energies are computed as shown in eq 5, where  $E_{2DDPK}$  is the DFT energy of the full 2DDPK system,  $N_i$  represents the number of atoms in the unit cell of element  $i$ , and  $E_i$  represents the DFT energy of the lone element  $i$ . With this formulation, a lower  $E_{\text{form}}$  corresponds to an increasingly stable atomic configuration compared with the constituent atoms in the system.

$$E_{\text{form}} = E_{2DDPK} - \sum_i N_i E_i \quad (5)$$

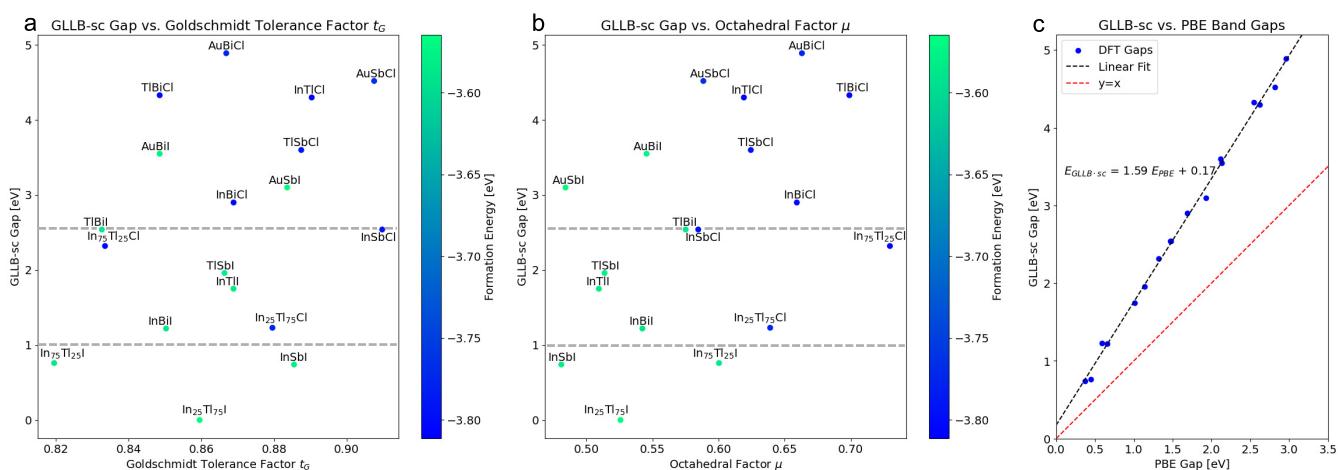
We observe a trend toward energetic preference of larger values of  $\mu$  in the 2DDPKs shown here which is consistent with the orthorhombic phases obtained upon DFT optimization.<sup>41</sup> It is important to note that the 2DDPKs consistently showed improved formation energies approaching the lower bound of what are considered acceptable  $t_G$  values in bulk perovskites. For reference  $t_G$  of the ubiquitous MAPbI<sub>3</sub> perovskite is 0.81, and our results suggest that 2DDPKs may be feasible to synthesize at or beyond this boundary.<sup>42</sup> Thus, our results show that the search space of potentially stable 2DDPKs may include B, B' cations of larger ionic radii than would otherwise be tolerable in bulk DPKs. Furthermore, this indicates that setting hard boundaries comparable to those used in the high-throughput screening of bulk perovskites should not be done so rigidly in future investigations of 2DDPKs. In fact, this remains true when considering not only the structural but also the optoelectronic properties of these 2DDPK systems.

Optoelectronic properties are the key determining factors for the photovoltaic performance of a given set of materials. With this being the case, we carried out an extensive investigation of the electronic structure present in the 18 2DDPK systems used in the present study. We computed electronic band structures with and without spin-orbit coupling (SOC) at the DFT+PBE level. Additionally, because both DFT-level and DFT+SOC-level calculations tend to severely underestimate electronic bandgaps, for all systems gapped at the PBE level we compute the GLLB-sc band gap, which has been demonstrated to provide excellent agreement with experiment.<sup>43</sup> The GLLB-sc approach serves as a

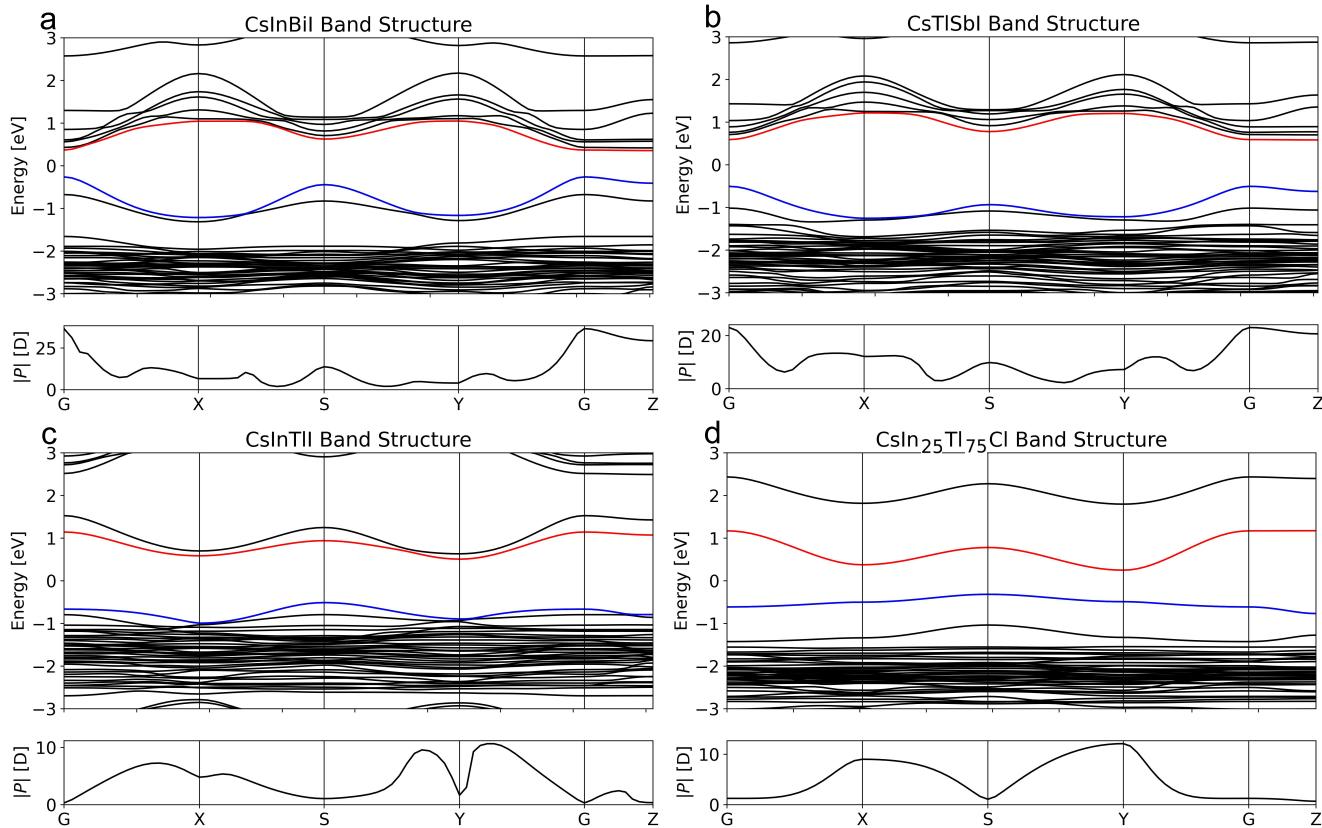
## Direct &amp; Indirect Bandgaps



**Figure 2.** Electronic bandgaps computed at the PBE, and GLLB-sc level for all 18 2DDPKs used in the present study. Lowest energy transitions and direct band gaps correspond to the directly gapped 2DDPKs.



**Figure 3.** GLLB-sc gaps vs (a) Goldschmidt tolerance factor  $t_G$ , and (b) octahedral factor  $\mu$  for the 18 2DDPK systems used in the present study. Points are colored by the formation energies. The regions enclosed by dashed lines represent systems exhibiting band gaps between 1.0 and 2.5 eV. (c) GLLB-sc gaps compared with PBE gaps from DFT computed band structures with the linear scaling relationship in the inset.



**Figure 4.** Band structures of the (a) InBiI, (b) TlSbI, (c) InTlI, and (d)  $\text{In}_{25}\text{Tl}_{75}\text{Cl}$  perovskites. Transition dipole moments across the high symmetry paths are presented below each respective band structure and were computed for direct transitions between the VBM (blue) and CBM (red).

correction to typical DFT band gaps, whereby the underestimation is mitigated by a correction associated with the derivative discontinuity in the system of interest. This approach has been benchmarked across a wide array of semiconductor systems, including hybrid double perovskites, consistently outperforming even approaches using hybrid functionals like HSE06.<sup>43,44</sup> Figure 2 displays electronic band gaps associated with direct and indirect (where applicable) DFT+PBE level results, as well as the GLLB-sc level results computed for more direct correspondence with expected experimental values. As noted by Zhan et al. desirable photovoltaic materials in the subclass of perovskites have experimental band gaps of approximately 1–2.5 eV, with the ideal band gap as dictated by the Shockley-Queisser limit of 1.34 eV.<sup>41</sup> Figure 3a, b displays the GLLB-sc band gaps against both  $t_G$  and  $\mu$ , with the dashed region representing the 2DDPKs with band gaps within this desirable region. We largely see that the Au-containing 2DDPKs exhibit band gaps well outside of this range, making them undesirable for usage in photovoltaic solar cells, even if the previously mentioned structural instability indicators could be remedied. Furthermore, the interchange of X-site halogen from chloride to iodide leads to a relatively uniform decrease in band gap of on average 1.68 eV, with a standard deviation of 0.36 eV. An additional insight is the very linear relationship between DFT gaps computed at the PBE level and at the GLLB-sc level (Figure 3c). Simple linear regression suggests an effective and accurate means for approximating band gaps at the GLLB-sc level from a simple PBE calculation detailed in eq 6.

$$\tilde{E}_{\text{GLLB-sc}} = 1.59E_{\text{PBE}} + 0.17 \quad (6)$$

Here  $\tilde{E}_{\text{GLLB-sc}}$  is the zero-cost approximation to the GLLB-sc gap which can be obtained from directly from the band gap at the PBE level,  $E_{\text{PBE}}$ . Information of this nature can greatly aid in future computational workflows that aim to mitigate computational cost by forecasting band gaps for closely related perovskite systems of interest. The large energy range of accuracy observed from this extrapolation technique (Figure 3c) suggests its applicability to similar 2DPKs and 2DDPKs which may be the focus of future investigations. We would, however, caution the usage of this extrapolation technique to perovskite systems that differ significantly in their chemical composition, such as perovskite oxides or perovskites including lanthanides or actinides as B-site cations. The dashed regions of Figure 3a, b display a number of 2DDPK systems that are candidates for photovoltaic applications, the four of which that are closest to the idealized gap of 1.34 eV while remaining between 1.0 and 2.5 eV are TlSbI, InTlI, InBiI, and the novel mixed oxidation state  $\text{In}_{25}\text{Tl}_{75}\text{Cl}$  systems. We also note that the InSbI, and  $\text{In}_{75}\text{Tl}_{25}\text{I}$  systems, while having band gaps slightly below 1.0 eV, may also serve as effective materials in photovoltaic applications. Previously Zhang et al. have investigated a bulk analog to the InSbI system with  $X = \text{Cl}$  and found it to have optically active transitions at the band edge and a desirable band gap, in congruence with our results (Figure S12), albeit with notable structural instabilities.<sup>34</sup>

As previously mentioned, a key concern in the usage of DPKs is the presence of optically inactive transitions, which

**Table 2. Thermoelectric Properties of the 2DDPKs Used in the Present Study<sup>a</sup>**

2DDPK	$E_{\text{VBM}}$ (eV)	$E_{\text{CBM}}$ (eV)	$C^{2\text{D}}$ (Nm <sup>-1</sup> )	$m_{\text{h}}^*$	$m_{\text{e}}^*$	$\tau_{\text{h}}$ (fs)	$\tau_{\text{e}}$ (fs)	$\text{TPF}_{300\text{h}}^{300\text{h}}$ (mW K <sup>-2</sup> m <sup>-1</sup> )	$\text{TPF}_{300\text{e}}^{300\text{e}}$ (mW K <sup>-2</sup> m <sup>-1</sup> )	$\text{TPF}_{300\text{e}}^{300\text{e}}$ (mW K <sup>-2</sup> m <sup>-1</sup> )	$\text{TPF}_{300\text{e}}^{300\text{e}}$ (mW K <sup>-2</sup> m <sup>-1</sup> )
AuBiCl	8.83	6.68	32.50	1.18	1.96	3.00	2.86	0.08	0.08	0.09	0.08
AuBiI	9.51	6.43	37.20	1.76	1.98	3.67	1.88	0.09	0.09	0.11	0.15
AuSbCl	8.67	6.25	31.74	1.31	1.60	4.10	2.61	0.08	0.06	0.09	0.08
AuSbI	9.10	6.52	32.44	1.86	1.60	3.85	1.70	0.09	0.06	0.08	0.09
In <sub>25</sub> Tl <sub>75</sub> Cl	10.47	7.33	46.66	1.30	0.39	17.74	2.65	0.47	0.27	0.14	0.24
In <sub>75</sub> Tl <sub>25</sub> Cl	11.51	6.89	48.50	1.08	0.46	18.08	2.73	0.54	0.56	0.14	0.22
In <sub>75</sub> Tl <sub>25</sub> I	11.63	7.30	38.32	0.40	0.50	11.67	5.77	0.57	0.39	0.27	0.31
InBiCl	12.06	7.33	44.88	0.14	0.36	18.79	17.80	0.97	1.63	0.99	1.92
InBiI	11.39	8.03	40.80	0.04	0.06	83.62	57.55	3.71	10.16	3.48	9.11
InSbCl	11.05	6.41	40.32	0.27	0.33	23.69	9.75	1.23	2.16	0.54	1.05
InSbI	11.16	8.00	40.27	0.05	0.07	68.99	49.02	2.78	7.39	4.01	8.04
InTlCl	10.50	7.16	43.32	0.69	0.54	12.52	4.57	0.42	0.46	0.24	0.40
InTlI	10.32	7.74	30.65	0.96	0.51	8.08	2.42	0.34	0.40	0.12	0.23
TlBiCl	10.67	7.02	40.03	0.19	0.43	15.36	15.27	0.75	1.16	0.82	1.52
TlBiI	10.54	8.24	38.40	0.12	0.14	31.82	22.41	1.49	2.69	1.81	3.77
TlSbCl	9.97	7.06	39.65	0.41	0.46	13.99	7.78	0.66	1.08	1.39	2.62
TlSbI	10.55	8.12	38.90	0.11	0.14	35.18	26.23	1.64	3.15	2.33	4.87

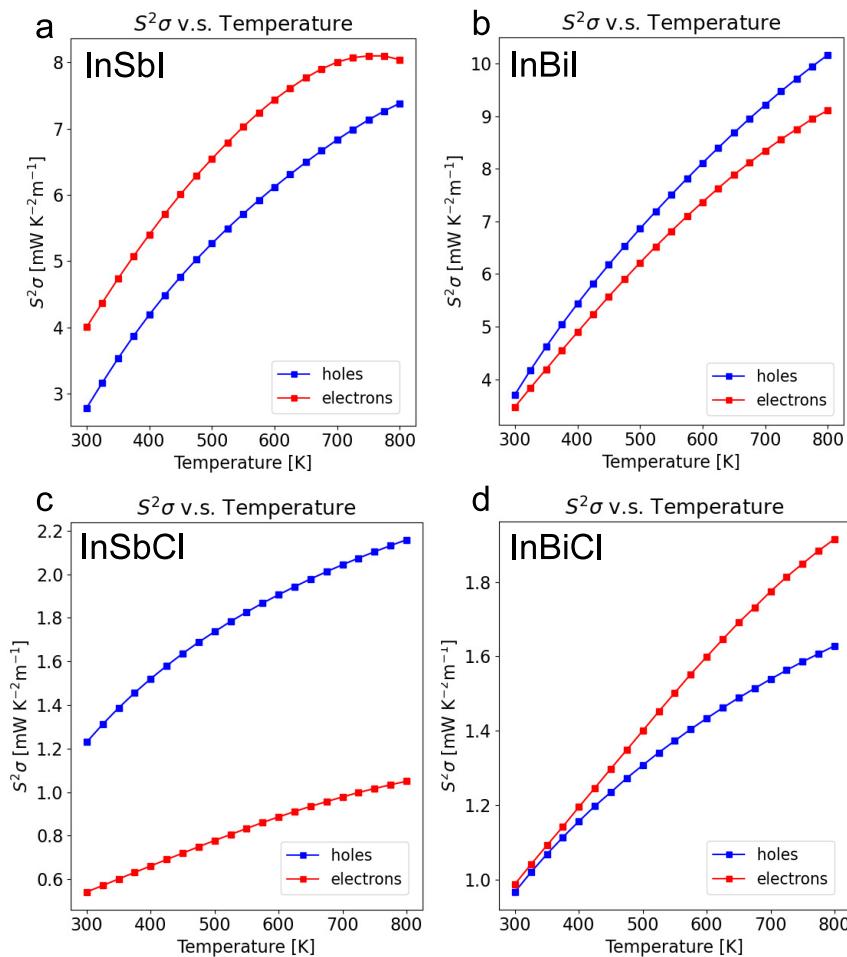
<sup>a</sup>The gapless In<sub>25</sub>Tl<sub>75</sub>I perovskite is omitted from these results due to its lack of band gap at the PBE level.

render an otherwise desirable photovoltaic material ineffective for solar energy harvesting. With this being the case, for all perovskites, we compute the transition dipole moments (TDMs) between the valence band maxima (VBM) and conduction band minima (CBM) across the high symmetry paths used for computation of the DFT band structures. Figure 4 shows band structures and TDMs between the VBM and CBM for the four candidate materials identified above as promising photovoltaics. The band structures, TDMs and density of states (DOS) for all perovskites are also available in the Supporting Information (Figures S3–S29). From Figure 4, we see that both InBiI and TlSbI are directly gapped at the  $\Gamma$ -point, with TDMs of over 20 D between the band edges and GLLB-sc gaps of 1.22 and 1.95 eV respectively. In the case of InBiI, transitions at the band edge correspond to primarily I(p) and In(s) states at the VBM, and Bi(p), I(p), and In(p) states at the CBM. Similarly, in the TlSbI 2DDPK, the VBM consists of I(p) states and the CBM is constituted by Sb(p), Tl(p), and I(p) states. Tabular information about whether the system is directly or indirectly gapped, the primary subshells contributing to the band edges, the PBE as well as GLLB-sc band gaps, and the optical availability of low energy transitions can be found in Table S1. The InTlI and In<sub>25</sub>Tl<sub>75</sub>Cl 2DDPKs are both indirectly gapped with GLLB-sc gaps of 1.75 and 1.23 eV, respectively, which correspond to 2.13 and 1.41 eV for the corresponding direct transitions. Both structures contain large portions of the band paths, which are optically active near these lowest energy direct transitions. In particular, the In<sub>25</sub>Tl<sub>75</sub>Cl presents itself as a key candidate photovoltaic material with optically active transitions in key parts of the BZ. Moving from S-X and Y-X, optical gaps narrow and TDMs increase to approximately 10 D. This fact combined with its direct gap of 1.41 eV makes this a very promising candidate 2DDPK.

Further investigating the novel mixed-valence In<sub>25</sub>Tl<sub>75</sub>Cl system, we note that the wide availability of low energy transitions from the X–S–Y path contrasts with the case of InBiI and TlSbI, whereby band gaps widen significantly across the BZ when moving away from the  $\Gamma$  and S points. Additionally, we compute Bader charges to quantify how

charge distributes across the mixed-valence sites, and find partial atomic charges of  $q_{\text{In}} = +1.59$  for the lone indium in the unit cell, and  $q_{\text{Tl}} = +0.74$ , +0.71, and +1.23. This indicates a clear retention of the mixed oxidation states of the three thallium atoms in the unit cell. We found that symmetry breaking associated with introducing mixed stoichiometries can aid in reducing the prevalence of parity forbidden transitions in this class of materials. The In<sub>25</sub>Tl<sub>75</sub>Cl system contains band edges consisting of Cl(p) and In(s,p), Cl(p) bands near the CBM. Typically, metal-to-metal transitions of similar character are those which exhibit the parity forbidden transitions in DPKs, attributable to the symmetry of the corresponding orbitals. Our results, however, suggest that considering mixed oxidation states can drastically modify the shapes of these orbitals (Figure S30), and result in over a 2-fold increase in TDMs when comparing the mixed oxidation state In<sub>25</sub>Tl<sub>75</sub>Cl system to that of the InTlCl system. In fact, a similar increase in TDMs by way of antimony doping in the Cs<sub>2</sub>AgIn<sub>0.75</sub>Sb<sub>0.25</sub>Cl<sub>6</sub> bulk DPK was observed by Zhang et al. supporting this conclusion.<sup>34</sup> As a final note on the remediation of parity forbidden transitions in 2DDPKs, we uncovered a consistent two- to 4-fold increase in TDMs (Figures S3, S6, S9, S12, S15, S18, S21, S24, and S27) for all I-containing systems when compared with their Cl-containing counterparts. This appears to be attributable to the large ionic radius of iodide (2.2 Å) compared with that of the chloride ion (1.81 Å), inducing greater mixing of states compared to the high-symmetry lone atomic orbitals. This is further supported by the modulation of TDMs upon band crossing between B-, or B'-site cations and I-anions. An illustrative example of this can be seen in the InTlI perovskite (Figure S27) whereby a band crossing along the S–Y path drastically increases the magnitude of the TDMs when the I-band is found to be lower in energy than the Tl-band.

To broaden the scope of applicability for perovskite based solar energy harvesters, much research in the literature has been put forth to investigate their usage in hybrid photovoltaic-thermoelectric (PV-TE) devices. With this being the case, we have used a two-step approach of pairing DFT-based



**Figure 5.** Thermoelectric power factor of the n-doped and p-doped configurations of the (a) InSbI, (b) InBiI, (c) InSbCl, and (d) InBiCl 2DDPKs from 300 to 800 K.

deformation potential theory with solution of the Boltzmann Transport Equations (BTEs) to assess the thermoelectric performance of these 2DDPKs under a broad range of conditions. All BTE calculations are carried out in the relaxation time approximation as implemented in Boltz-TraP2.<sup>45</sup> Deformation potential theory was used to obtain approximate relaxation times for the 18 perovskite systems of interest as detailed in *eqs 7 and 8*, carried out in an identical manner to our previous work.<sup>46,47</sup> Here the index *i* corresponds to the charge carrier type and *e* and *h* to electrons and holes, respectively.  $C^{2D}$  represents the in-plane stiffness constant, and  $E_{VBM}$ ,  $E_{CBM}$  are deformation potentials at the valence and conduction band edge, respectively, for which more information regarding the computational details can be found in the Computational Methods. The constants  $e$ ,  $h_b$ ,  $T$  represent the charge of an electron, Boltzmann constant, and temperature, respectively. Finally,  $\mu_i$  represents the mobility of charge carriers of type *i*, and  $m_i^*$  represents the effective mass computed from parabolic fits of the valence and conduction bands of the SOC band structure.

$$\mu_i = \frac{2e\hbar^3 C^{2D}}{3k_b T E_i^2 m_i^*} \quad (7)$$

$$\tau_i = \frac{\mu_i m_i^*}{e} \quad (8)$$

The summarized findings regarding the elastic and thermoelectric properties of the 2DDPKs used in this study can be found in **Table 2**. The key quantity with which we quantify thermoelectric performance is the thermoelectric power factor (TPF) of holes and electrons at ambient and high temperatures of 300 and 800 K. The TPFs are computed as  $TPF_{Ti} = S_{Ti}^2 \sigma_{Ti}$  where  $S_{Ti}$  represents the Seebeck coefficient,  $\sigma_{Ti}$  the electrical conductivity, and the indices *T* and *i* again represent temperature and either electrons or holes as charge carriers. **Figures S31–S47** show plots of  $S$ ,  $\sigma$ , and TPF for electrons and holes ranging between 300 and 800 K for all 18 2DDPKs used in the present study. We note the flat bands associated with the frontier Au(d)-bands result in large effective masses, small electrical conductivities, and thereby extremely small TPFs, further reinforcing the notion that these Au-based 2DDPKs are unsuitable to not only photovoltaic but also thermoelectric applications. There is a consistent increase in TPFs when considering iodide as the halogen instead of chloride, with two representative examples in **Figure 5a–d**. This can be directly attributed to the fact that most band edges consist in part of the halogen p-orbitals, for which the dispersion of I(p) orbitals is more pronounced than that of Cl(p), resulting in favorable TE properties as they enter the BTEs through their band derivatives. Similarly, 2DDPKs which have strong dispersion at the band edge, such as those containing bismuth and antimony, show significantly improved

TPFs when compared the narrower bands present in the only In- and Tl-containing 2DDPKs. This highlights the difficulty of obtaining an abundance of near-band gap transitions (such as is the case in the  $\text{In}_{25}\text{Tl}_{75}\text{Cl}$  2DDPK), while also obtaining optimal TE performance, as strong dispersion necessitates large fluctuations from the band gap across the BZ. With that said, the iodide based Bi- and Sb-containing 2DDPKs display promise for both n-doped and p-doped configurations, with TPF for p-doped configurations as high as  $3.71 \text{ mW K}^{-2} \text{ m}^{-1}$  in  $\text{InBiI}$ , and n-doped configurations as high as  $4.01 \text{ mW K}^{-2} \text{ m}^{-1}$  in  $\text{InSbI}$  at 300 K as seen in Figure 5a, b. This makes the  $\text{InSbI}$  2DDPK one of the key candidates for implementation in hybrid PV-TE devices owing to its high TPF, which is maintained over a broad range of temperatures (Figure 5a) for both n- and p-doped configurations as well as a suitable 0.74 eV band gap.

## CONCLUSION

In conclusion, we have conducted a systematic analysis of the structural, electronic, and thermoelectric properties of 18 2DDPKs consisting of a broad range of building components. Our analyses indicate the strong link between octahedral distortions and the electronegativity difference between the B-X and B'-X building components. Furthermore, we provide the simple linear relationship between band gaps in perovskite systems computed at the PBE level and the GLLB-sc level for direct comparison with experimental band gaps of  $\tilde{E}_{\text{GLLB-sc}} = 1.59E_{\text{PBE}} + 0.17$  which can greatly aid in the future high-throughput screening of 2DDPKs. Additionally, we have identified several candidate photovoltaic materials, one of which is the mixed-oxidation state  $\text{In}_{25}\text{Tl}_{75}\text{Cl}$  2DDPK. This perovskite has optically active transitions as low as 1.41 eV across much of the BZ which is very close to the ideal band gap obtained in the Shockley-Quiesser limit for single junction solar cells of 1.34 eV. We have demonstrated how the novel approach of mixed-oxidation state cations in the 2DDPKs can alleviate concerns associated with otherwise parity forbidden transitions in DPKs which prevent utilization of an otherwise desirable material for photovoltaic applications. Finally, we highlight the  $\text{InSbI}$ -based 2DDPK for its potential in mixed PV-TE applications owing to the high TPF for both n-doped and p-doped configurations over a broad range of temperatures, as well as its strongly optically active direct bandgap of 0.74 eV. The combination of these insights can be used to guide the future generation of 2DDPK systems which are of interest for photovoltaic applications while mitigating structural and electronic concerns that are so commonly found in this class of materials.

## COMPUTATIONAL METHODS

All density functional theory calculations were carried out using the plane-wave mode of the GPAW package with a kinetic energy cutoff of 550 eV.<sup>48,49</sup> A  $4 \times 4 \times 2$  k-point mesh was used for all variable and fixed cell optimizations, which were carried out until force components did not exceed 0.02 eV/Å, and a  $6 \times 6 \times 2$  k-point mesh was used for self-consistent field calculations prior to non-self-consistent field calculations for the density of states and band structures. Self-consistent field calculations were converged to within 0.5 meV/valence electron and  $10^{-4}$  e/valence electron for the energy and density, respectively. The atomic simulation environment, pymatgen, matminer, and Pyrovske were used for the computation of structural descriptors of the optimized 2DDPK systems.<sup>33,50–52</sup> The PBE exchange correlation functional together was used in all

calculations, and the DFT-D3 empirical dispersion correction was included to aid in accurately describing noncovalent interactions associated with the spacer molecules.<sup>53,54</sup> Band structures were computed with 100 k-points along the high symmetry paths, and unoccupied bands were converged up to 2 eV above the CBM.

For the computation of thermoelectric properties, we compute the effective masses and relaxation times as described in the manuscript. All thermoelectric properties are computed at fixed charge carrier densities of  $\pm 10^{19} \text{ e/cm}^3$  for holes and electrons, respectively. To compute the deformation potentials  $E_{\text{VBM}}$  and  $E_{\text{CBM}}$ , we apply a linear fit to the energies at the band edges of the perovskite systems under the application of between  $-1.5\%$  and  $1.5\%$  strain. We use the same  $-1.5\%$  to  $1.5\%$  strain for computation of the in-plane stiffness constant  $C^{2D}$ , where we extract the second order coefficient of a parabolic fit. A relaxed-ion approach was used in all cases, as we find the clamped-ion approach to overestimate material stiffness.<sup>55</sup> Effective masses were computed using the effmass code with a 5-point least-squares fit, and all effective masses were computed from the SOC included band structures, as SOC provides more reliable curvature at the band edge.<sup>56</sup>

## ASSOCIATED CONTENT

### Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acsaem.3c03276>.

Additional details regarding structural and electronic properties about the perovskites utilized in this work; schematic representation of perovskite systems under investigation; plots of electronic band structure, density of states, and bond distance distributions of 2DDPKs under investigation; plots demonstrating thermoelectric performance of the 2DDPKs under investigation (PDF)

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### Notes

The authors declare no competing financial interest.

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