

Title:

Theory cracks old data: rovibrational energy levels of *ortho*H₂–CO derived from experiment

Short title:

Rovibrational energies of *ortho*H₂-CO from experiment

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Teaser:

A synergistic method was developed combining highest accuracy quantum mechanical calculations with analysis of experimental spectra.

Abstract:

Measurements of rovibrational spectra of clusters provide physical insight only if spectral lines can be assigned to pairs of quantum states and further insight is obtained if one can deduce the quantitative energy-level pattern. Both steps can be so difficult that some measured spectra remain unassigned, one example is *ortho*H₂-CO. To extend the scope of spectroscopic insights, we propose to use theoretical information in interpretation of spectra. We first performed high accuracy, full-dimensional calculations of the *ortho*H₂-CO spectrum, at the highest practically achievable levels of electronic structure theory and quantum nuclear dynamics. Then, an iterative, theory-guided method developed here allowed us to fully interpret the spectrum of *ortho*H₂-CO, extending the range of van der Waals clusters for which spectroscopy can provide physical insights.

INTRODUCTION

Spectroscopy is among the most important methods of probing matter, it is also one of the most precise methods. For van der Waals (vdW) clusters, even the smallest ones, this precision cannot be yet matched by theory. For example, for the $\text{H}_2\text{--CO}$ complex discussed here, the energies of most infrared transitions (line positions) are measured with precision of 0.0005 cm^{-1} (Ref. (1)), while the *para* $\text{H}_2\text{--CO}$ transitions computed in Ref. (2), among the most accurate for any vdW dimer, have root-mean square error (RMSE) of 0.0081 cm^{-1} with respect to the experimental transitions shifted by the (experimental) value of CO fundamental (3). However, in some cases spectroscopy measurements are hard to assign and therefore to interpret. Without proper interpretations, such measurements are of very limited value. In particular, a measurement of infrared (IR) spectra of a vdW cluster often results in a “forest of spectral lines”, as in the case of the *ortho* $\text{H}_2\text{--CO}$ experimental spectrum shown in Fig. 1, top row. Clearly, it is very difficult to identify the two energy levels from which a given spectral line originates.

Interpretation of the spectrum of $\text{H}_2\text{--CO}$ is of great interest due to the importance of this dimer. It is obviously prominent in astrophysics since H_2 and CO are, respectively, the most abundant and the second most abundant molecules in space. Since H_2 is difficult to observe directly, easy to detect CO serves as an H_2 tracer (4). This requires an assumption that the CO to H_2 density ratio is approximately constant in space. This ratio is usually assumed to be equal to 10^{-4} , an assumption that is hotly debated (4–7). Information on this ratio and its variation in space can be inferred from observations of the $\text{H}_2\text{--CO}$ complex, but such attempts (8, 9) have been unsuccessful so far. The search for this dimer may become successful with new, more precise devices including the James Webb Space Telescope (10). The detection of $\text{H}_2\text{--CO}$ in the cold interstellar medium would also serve as a sensitive indicator of temperature. Since astronomical observations record a mixture of *para* $\text{H}_2\text{--CO}$ and *ortho* $\text{H}_2\text{--CO}$ spectra, full interpretation of both is needed to guide the observations, [in particular because the latter spectrum is much denser](#). Furthermore, inelastic collisions of CO with H_2 play a key role in establishing the observed molecular populations in regions that are not in local thermodynamic

equilibrium and theoretical calculations of the relevant cross-sections use the same potential energy surfaces (PESs) as the investigations of the bound states of $\text{H}_2\text{-CO}$ (11). This complex is also of interest in several fields of science beyond astrophysics. For instance, it was studied, both theoretically and experimentally, in the context of the detection of superfluidity in the *para*- H_2 clusters (12). Moreover, $\text{H}_2\text{-CO}$ is an important model system for van der Waals interactions, as it is a molecular dimer with interactions partly similar to those of rare gases: the negative dispersion energy dominates for most intermonomer separations R , while for small R the positive exchange-repulsion energy becomes larger in magnitude. However, in contrast to rare gases, the electrostatic interactions although smaller in magnitude than the dispersion and exchange ones (18), impact the depth and the position of the van der Waals minimum. This is a similar physical origin of binding to that between aromatic hydrocarbons. Thus, a better characterization of $\text{H}_2\text{-CO}$ should help in understanding such complex systems, for which our intuitions remain undeveloped.

Interpretation of observed spectra can be accomplished at two levels. At the first level, one can identify qualitatively (in terms of quantum numbers) the energy levels associated with a given spectral line. Such identification is performed based on characteristic spectral patterns and usually only a subset of lines can be assigned. At the next level, one can determine quantitatively the relative energies of all levels from which the spectral transitions stem. The latter is an ultimate interpretation of spectra and brings an abundance of physical insight into investigated systems. In particular, one can fit an empirical PES to these data, getting information about the nature of intermolecular interactions. The different possible levels of spectral interpretations are well illustrated on the example of $\text{H}_2\text{-CO}$. Observations of this complex date back to 1967 (13–15) and the 1998 infrared experiment by McKellar (1) achieved the ultimate interpretation of *para* $\text{H}_2\text{-CO}$, i.e., the quantitative pattern of the rovibrational energy levels was deduced from experiment, and still provides the benchmark values. These energy levels were much more accurate than those from theoretical investigations of that time (16–18): the best theory vs. experiment RMSE on the bound energy levels was 0.4 cm^{-1} (18). As the quality of

ab initio PESs gradually improved, this RMSE dropped to 0.05 cm^{-1} in 2005 (19) and to 0.005 cm^{-1} in 2012 (2, 20) (in both cases now including also the resonance states), small errors compared to the dissociation energy of about 20 cm^{-1} . The latter error constitutes one of the best agreements of theory with experiment for spectra of van der Waals molecules. Spectral measurements were also performed in the millimeter-wavelength range of energies (21, 22), directly relevant for astrophysical observations. In contrast to *para*H₂–CO, the *ortho*H₂–CO spectrum, also recorded in 1998 (1), remained completely unassigned for a long time. The reason was that the *ortho* spectrum is much more complicated than the *para* one due to different nuclear spin couplings in the two cases, resulting in the angular momentum quantum number of H₂, j_1 , to be odd and even for *ortho*H₂ and *para*H₂, respectively. At sufficiently low temperature, j_1 is equal to 1 (a triply degenerate p-type state) for *ortho*H₂ and 0 (a spherically symmetric state) for *para*H₂. As the result, *ortho*H₂ motions can be coupled with CO motions in more ways than in the case of *para*H₂. The increased couplings also result in probing the PES more extensively. With the increased accuracy of the 2012 PES (2, 20), denoted as V_{12} , an attempt was made to assign *ortho*H₂–CO spectrum. This attempt was partly successful as over 200 infrared transitions were assigned (out of about 1000 possible reasonably strong transitions determined from theory), as well as 26 millimeter-wavelength transitions. These assignments were made by identifying transition-energy regions where the observed and theoretical spectra were so close to each other that the known theoretical characteristics of a line could be used to label an experimental line (see Fig. 1). However, despite significant efforts and the guidance from theory, only a small number of energy levels were deduced, in subsets that could not be linked together.

We present here work aimed at cracking the problem of deducing energy levels from the *ortho*H₂–CO spectra. There are two areas where progress has been made: increased accuracy of theoretical spectra including line intensities and the development of a better deduction protocol. An obvious improvement of theory is the extension of spectral calculations from four dimensions (4D) (2, 20) to full dimensionality (6D), and we present here such an extension. The previous level-deduction protocol was essentially a single-sweep trial and error procedure

from lines to levels. The new level-deduction protocol developed here is iterative: the previously deduced energy levels are used to assign more lines and then these newly assigned lines are used to deduce more levels. The effect of this effort has been an essentially complete interpretation of the *ortho*H₂–CO spectra: we were able to deduce from experiment the energies of 84% of all possible rovibrational levels. This is close to the maximum possible number since several spectral regions are not accessible to experiment.

RESULTS

Potential energy surface

The first step in our investigations was the development of a 6D potential energy surface. The most accurate published H₂–CO spectra were obtained from a 4D V_{12} surface (2, 20). The *ab initio* calculations in Refs. (2, 20) were actually performed on a 6D grid, although the intra-monomer separations were probed only in a narrow range enabling numerical calculations of derivatives needed in the Taylor-expansion method (23). The 6D surface was then averaged over the motions within monomers. The resulting 4D set of averaged interaction energies was fitted by an analytic function. In the present work, we have obtained an analytic 6D PES. 6D PESs for H₂–CO have been published previously (24–26), but used only in scattering and virial coefficients calculations. Due to the steep increase in the number of 6D grid points, necessitating the use of lower levels of theory, and due to higher fit uncertainties in 6D, 4D averages of these surfaces would be less accurate than V_{12} . Our new 6D surface, denoted as V_{23} , overcomes these problems. The interaction energies were computed in the same way as in Ref. (27). The uncertainty of these energies was estimated to be equal to 0.6 cm^{−1} relative to the exact relativistic adiabatic value or 0.8% of the total interaction energy at the global minimum (20). The interaction energies computed on a grid of 34,559 short-range and 11,265 long-range points were fitted by analytic functions, see the Supplementary Materials (SM) for details. The RMSE of the fit is 0.34 cm^{−1} on all points and 0.02 cm^{−1} for points with negative values of E_{int} , most important for spectra. The latter value can be compared to that of the 6D PES from Ref. (26)

equal to 0.16 cm^{-1} . Clearly, a very significant improvement has been achieved. The intermolecular interaction surface V_{23} supplemented by monomer potentials gives the total 6D PES denoted as U_{23} . A computer code calculating V_{23} is provided in SM.

Nuclear motion calculations

The $\text{H}_2\text{-CO}$ complex has six rovibrational degrees of freedom and we have performed most of the calculations in full (6D) dimensionality. For some calculations, specified below, we used a reduced dimensionality PES, depending only on the four intermolecular degrees of freedom (4D). The simplest way to obtain a 4D PES is to fix the H–H and C–O bond lengths. A much better way (28) is to obtain first a 6D surface and then average it over the intramolecular bond lengths in the ground rovibrational state of each monomer, which is what we did. The 6D calculations of rovibrational spectra for the *para* and *ortho* $\text{H}_2\text{-CO}$ systems have not been done before and are challenging since computing energies up to CO vibrational state with $v_2 = 1$ (at about $2,000 \text{ cm}^{-1}$) requires using a very large rovibrational basis set. Numerically exact calculations for vdW dimers have been performed up to 12 dimensions (29), but the energy range involved was an order of magnitude smaller. Our calculations for the bound rovibrational states uses a discrete variable representation (DVR) basis for the radial coordinates and spherical harmonic type basis for the bends. The variational eigenproblem in the product of the two bases was solved using a symmetry-adapted Lanczos algorithm. The method is denoted as DSL (DVR+spherical+Lanczos) (30, 31). The 6D rovibrational calculations were numerically converged to 0.0001 cm^{-1} for the lowest bound state with $v_2 = 0$ or $v_2 = 1$ and to much better than 0.001 cm^{-1} for all other bound states of *ortho* $\text{H}_2\text{-CO}$. The rovibrational states of $\text{H}_2\text{-CO}$ are labeled by $(J, P, n_{J,P}, v_2)$, where J is the rotational quantum number of the complex, P is its spectroscopic parity, and $n_{J,P}$ denotes consecutive states with these values of J and P . Further details of 6D rovibrational calculations are given in [the Methods section](#).

For the resonance states, the 6D calculations are difficult and we instead did 4D scattering calculations. They are numerically converged to better than 0.001 cm^{-1} for all considered states.

We have also performed 4D calculations for bound states in order to compare them to 6D ones. All 4D calculations used a 4D set of interaction energies computed on-the-fly from V_{23} (i.e., no analytic 4D fits were done). The same Taylor-expansion method (23) as in Refs. (2, 20) was applied in averaging over motions within the monomers, except that the values and derivatives of energy were computed from V_{23} . The resulting surfaces are denoted by $\langle V_{23} \rangle_{v_1=0, v_2=0,1}$ or in short as $\langle V_{23} \rangle$. We have employed the BOUND and MOLSCAT programs (32) to perform the 4D rovibrational and scattering calculations (see SM for details). All intensities were computed from 4D wave functions. For the quasibound states the wave functions were obtained from the stabilization method (2, 20). Since accuracy requirements for intensities are not as high as for line positions, this approach is fully satisfactory (also, the 6D and 4D approaches are nearly equally accurate, as discussed below).

Assessment of theoretical spectra

Stringent validations and error estimates of the computed spectra come from comparisons with experiment. A qualitative comparison of experimental *ortho*H₂–CO spectra data with the spectra from the 6D+4D approach (V_{23} for bound states and $\langle V_{23} \rangle$ for resonances) is shown in Fig. 1 and in fig. S1. In order to easily see the differences between the two spectra, the range of the horizontal scale of fig. S1 is 1 cm⁻¹ per panel. On the condensed plot of Fig. 1, the two spectra appear to be nearly identical, but fig. S1 shows that while many of strong lines closely overlap also at this scale, some lines are shifted up to about 0.06 cm⁻¹. This demonstrates the difficulties in assigning the experimental transitions.

To evaluate accuracy of the 6D+4D calculations in quantitative terms, we first compare them to the experimental energy levels for *para*H₂–CO: the RMSE is 0.0051 cm⁻¹ for all experimental levels with $v_2 = 0$ given in Ref. (1). Thus, this RMSE is virtually the same as 0.0054 cm⁻¹ found in the 4D calculations of Refs. (2, 20) with V_{12} . For the $v_2 = 1$ levels, the corresponding RMSEs are 0.0089 cm⁻¹ and 0.0069 cm⁻¹. Thus, both theoretical approaches are of similar accuracy with respect to experiment. In the case of *ortho*H₂–CO, we can compare the perfor-

mance of the two methods on the list of 209 transitions initially assigned in Refs. (2, 20) and revised in the present work. The calculated RMSE between theoretical and experimental transitions is 0.0177 cm^{-1} for the 6D+4D approach, virtually the same as the corresponding value of 0.0172 cm^{-1} obtained here from V_{12} of Ref. (20). In all cases discussed here, $\langle V_{23} \rangle$ spectra have similar RMSEs.

These virtually identical predictions from the V_{12} -based 4D, $\langle V_{23} \rangle$ -based 4D, and V_{23} -based 6D+4D calculations are quite astonishing. For the purposes of the present work, this shows that the quality of V_{23} in the rigid-monomer sector is the same as that of V_{12} . More generally, this shows that the monomer-flexibility effects beyond those included in $\langle V_{23} \rangle$ are negligible for $\text{H}_2\text{--CO}$ at the present level of theory. Whereas similar conclusions were found in scattering calculations for this system (25), the present findings are at much higher level of precision. While calculations of all-dimensional PESs became quite popular in recent years, little is known about the importance of monomer-flexibility effects. To our knowledge, rigorous comparisons involving $\langle V \rangle$ -type PESs have been performed earlier only for Ar-HF (28), i.e., between 2D and 3D approaches. Note that only the reduced-dimensionality PESs obtained from full-dimensionality ones by averaging over intramonomer motions provide such good agreement, the same is not true for rigid-monomer PESs computed at fixed intramonomer geometries. Although energy levels calculated on an averaged PES obtained with the Taylor-expansion method may differ from those on a full-dimensional PES more substantially for more strongly bound vdW dimers, it is encouraging that they are extremely close for $\text{H}_2\text{--CO}$. One can clearly expect this closeness to be the case for other weakly-bound vdW dimers as well. Rovibrational calculations on an averaged PES are clearly much easier because, for dimers, there are at most 6 intermolecular coordinates. Whereas flexible monomer spectral calculations are only possible up to 12 dimensions, calculations with only the intermolecular coordinates are becoming routine.

An all-dimensional approach naturally predicts values of monomer properties within a dimer, such as shifts of intramonomer fundamental transitions due to intermolecular interactions. Our 6D approach gives -0.172 cm^{-1} (red) shift for the CO fundamental, which agrees very well with

the experimental value of -0.179 cm^{-1} (Ref. (1)). This shift can be also computed in the 4D approach with $\langle V \rangle$ -type PESs by comparing the dissociations energies from $v_2 = 0$ and $v_2 = 1$ surfaces. The calculation with $\langle V_{23} \rangle$ gives the value of -0.173 cm^{-1} , while the value computed in Ref. (20) was -0.176 cm^{-1} .

Deduction of experimental energy levels

The most essential improvement over the published work, which allowed us to find the experimental rovibrational energy levels of *ortho*H₂–CO, was the development of an iterative protocol for deducing energy levels from spectra. Our new protocol consists of two similar but not identical stages. Each stage is composed of three steps: (1) assignment of experimental transitions, (2) deduction of experimental energy levels from the assigned transitions, and (3) generation of the spectrum from all the experimental levels deduced so far (with theoretical intensities). Essential elements of our protocol are utilization of symmetries of the rovibrational wave functions and of the selection rules.

We started from the set of transitions assigned in Ref. (20). Our initial application of the protocol was not particularly successful. We realized that the reason could be that a few previous assignments are incorrect, and any misassigned lines wreak havoc in the level-deduction protocol. We have, therefore, critically reviewed the previous assignments (20) using the new theoretical values of line positions and intensities. We have also analyzed the experimental spectrum by fitting lines that theory indicated as resulting from overlapping transitions with a sum of Voigt profiles, assigning two or three transitions to a peak earlier assigned to a single transition energy. As the result of this reanalysis, we have rejected a few assignments, reducing their number to 209, and have corrected another few of them. The reduced list of 209 assigned transitions is given in table S1 and has been used as the input to step 2 of stage I. With the improved methodology, we could have assigned a number of new lines, but we wanted to start from the level used in Ref. (20) to compare the protocols.

The level-deduction procedure (step 2) used by us is similar to the standard combination-

differences method (33) and is illustrated in Fig. 2. In this method, one selects all transitions ending in a given energy level $(J', P', n'_{J', P'}, 1)$ and originating from a set of initial energy levels $(J, P, n_{J, P}, 0)$, $(J', P', n'_{J', P'}, 1) \leftarrow (J, P, n_{J, P}, 0)$, and from the transition energies (in oval fields) calculates the relative energies of the levels with $v_2 = 0$. A group of transitions starting from a cluster of 4 rovibrational states with $v_2 = 0$ in the green panel and ending up in the $(2, e, 2, 1)$ state gives us information about the energies of the 3 states relative to the $(1, e, 1, 0)$ one. One can next find other clusters, such as that shown in the blue box, and link them together via common states, such as $(3, e, 3, 0)$, into the cluster shown in the red box. We were able to construct a single large cluster of relative energy levels for each of the (J, P) symmetry blocks allowed by the selection rules, predicting 63% of all theoretically possible states.

In the third step of each stage, the experimental levels found in step 2 are used to generate all allowed transitions between these levels. The agreement with the previously assigned transitions provides a verification of the correctness of the deduction procedure. Moreover, the generated set of transitions allows one to assign a number of new transitions: 69 such transitions have been assigned in stage I. Note that these 69 transitions contain no information about energy levels that were not yet deduced. The closeness of the matching of these 69 generated transitions with the actual experimental transitions confirms indirectly the correctness of the already determined experimental energy levels involved in these transitions. This process is assisted by comparisons with the corresponding theoretical positions and intensities. It also identifies energy levels ending up mostly in transitions belonging to unobservable spectral regions (yellow regions of Figs. 1 and S1) and therefore impossible to deduce from the experimental spectrum. For instance, the $(4, f, 5, 0)$ state is active in 6 transitions with relative intensities larger than 0.01, one of them even as large as 0.47. However, 5 of these transitions are in the unobservable areas. The last one is overlapped by the strong $^{12}\text{C}^{17}\text{O}$ line at 8.6263 cm^{-1} . Thus, the experimental energy of the $(4, f, 5, 0)$ state cannot be determined from the analyzed IR spectrum.

Conceptually, stage II was identical to stage I. The main difference is that we looked at

one energy level at a time, used theoretical guidance more extensively, and iterated steps 1-3 several times. In the first step of each iteration, we picked one theoretical energy level whose experimental counterpart was missing, and looked for theoretical transition energies involving this state and all the levels that had an experimental counterpart. We compared each transition energy with the experimental spectrum near this transition. This focused survey of experimental spectrum allowed us to assign transitions that were too weak or situated in a too dense region to allow an assignment in stage I. The stage II assignments are helped by the 69 lines assigned in stage I. This is possible in cases of a group of a few close-lying experimental lines corresponding to a similar group of theoretical lines. If some members of such a group are assigned, the remaining experimental and theoretical lines can often be found to be related to each other. Even one newly assigned transition gives us immediately the experimental level corresponding to the chosen theoretical one, which constitutes step 2. In some cases, additional new experimental energy levels were obtained because it became possible to link previously unlinked clusters of transitions. In step 3, we used the extended set of experimental energy levels to generate experimental spectrum and compared this spectrum with the measured one (this comparison also sometimes led to assignment of new transitions). In this way, we could immediately validate our assignments in step 1 and possibly discard or correct them. In the next iteration, another theoretical level with missing experimental counterpart was picked. Overall we were able to increase the number of experimental energy levels to 84% of all possible ones. For the $v_2 = 0$ case, we have found 56 experimental levels of odd parity out of 66 levels predicted by theory (56 out of 65 for even parity), whereas for the $v_2 = 1$ case, the corresponding numbers are 54/55 out of 66/65. In Fig. 3, the diagram of the energy levels for $v_2 = 0$ is presented, the numerical values for $v_2 = 0$ and 1 are given in tables S2 and S3, respectively. In all iterations of stage II, we assigned 41 transitions in step 1 and 35 ones in step 3. The latter transitions are marked by short red vertical arrows in the bottom rows of each panel of fig. S1. The total number of assigned lines is now 354 (209+69+41+35), much more than the total number of 219 experimental lines (assigned with a few mistakes) published in Ref. (20). All these transition energies

are given in tables S4 and S5, whereas a complete list of calculated theoretical transitions is presented in table S6.

Our deduction of 84% of the levels is close the limit for the existing experimental data. One can show from the comparison of theoretical and experimental spectra that the remaining 16% cannot be obtained because experimental transitions providing required information are very weak, or are obscured by much more intense lines, or lie in the ranges of energies not covered in the present experiment. Our work provides information to help plan a future experiment for *ortho*H₂-CO to fill the current gaps in the experimental energy pattern. One method could be to repeat the experiment at reduced pressure in the chamber, which makes the monomer lines narrower and reveals more features of the spectrum, as it was done (20) for *para*H₂-CO (although this change degrades the signal-to-noise ratio and can cause the transitions of low intensities to be lost in the background noise). The new experimental techniques such as ultra-high finesse cavity-enhanced laser spectroscopy (34) and spectroscopy in cryogenic regime (35) should achieve this narrowing without degrading the signal-to-noise ratio.

DISCUSSION

We have developed a synergistic method which combines highest possible accuracy quantum mechanical calculations with analysis of experimental spectra to fully interpret the spectrum of the *ortho*H₂-CO complex. The computed spectrum was used to guide the process which succeeded in deduction of experimental energy levels of this systems, the task that eluded all efforts in the past 25 years. 84% of all possible levels have been found, while most of the remaining 16% cannot be deduced due to missing regions in the experimental spectrum (but they can be taken from theory). Our work provides therefore solid reference data for searches of H₂-CO in space, in particular since the generated transitions energies partly fill the gaps (maintaining experimental accuracy). Also, theoretical transition energies can be used in parts of the spectrum currently unobservable in the laboratory, despite the fact that the theoretical data is less accurate. The methodology developed here extends applicability of spectroscopy

to van der Waals clusters. Future applications to such clusters will increase understanding of these important systems and of the intermolecular interactions in general. Our calculations pushed the current limits of theory, in particular, we used a full-dimensional approach and the highest currently practical level of theory. The *ab initio* interaction energies on the 6D grid were computed for the first time at such high level of theory for grid points beyond the 4D cut of the PES. The analytic 6D fit is of high fidelity, in particular, in its regions probed in the calculations of spectra, the RMSE of the fit is several times smaller than the estimated uncertainty of the *ab initio* calculations. This high fidelity was possible due to our extensions of the previously used PES fitting methodology. The final theoretical spectrum was built from energy levels obtained in 6D quantum nuclear motion calculations for all bound states and from 4D calculations (with a 4D PES obtained by averaging the 6D PES) for all resonance states.

METHODS

Calculations of interaction energies

The interaction energies were computed in the same way as in Ref. (27), i.e., using the supermolecular approach, $E_{\text{int}} = E_{\text{H}_2\text{-CO}} - E_{\text{H}_2} - E_{\text{CO}}$, where E_X is the total electronic energy of system X , levels of theory up to the coupled clusters method with single, double, triple, and noniterated quadruple excitations [CCSDT(Q)], basis sets up to the augmented quintuple-zeta quality, and extrapolations to the complete basis set limits. Since $r_1 = r_{\text{H-H}}$ and $r_2 = r_{\text{C-O}}$ are the same in calculations of E_{H_2} and E_{CO} , respectively, as in $E_{\text{H}_2\text{-CO}}$, the limit of E_{int} for the intermolecular separation $R \rightarrow \infty$ is zero for any value of the other coordinates. All electrons were correlated and the counterpoise correction for the basis set superposition error was used.

6D fit of potential energy surface

The interaction energies were computed on a grid of 34,559 points. In addition, 11,265 interaction energies were computed for R larger than 13.5 bohr using a lower level of theory, adequate in this region: only the CCSD(T) method and basis sets up to the augmented quadruple-zeta

size were used. The interaction energies were fitted by an analytic function that consisted of short- and long-range parts, with a smooth switching at R values between 10 and 12 bohrs, using the switching function from Ref. (36). The form of the long-range part was taken from Ref. (25), but the parameters were refitted to the present set of interaction energies at large R . The short-range part was taken in the form of a sum of products of exponentials $e^{-\alpha r_{ab}}$, where r_{ab} are atom-atom distances (37, 38). In contrast to most published work that uses the same α for all terms, we used four different, optimized values. The number of linear parameters was 1198. The intermolecular interaction surface V_{23} was supplemented by monomer potentials V_{H_2} and V_{CO} (39–41).

On-the-fly calculation of interaction energies in 4D

The calculations of interaction energies in 4D were performed on-the-fly, i.e., for each point in 4D coordinates needed by a nuclear dynamics program. The averaging of the V_{23} surface was over the ground vibrational state of H_2 , $v_1 = 0$, and two lowest-lying vibrational states of CO, $v_2 = 0, 1$. In contrast to earlier work, the state $v_1 = 0$, $j_1 = 1$ was used for *ortho*- H_2 -CO, which improved agreement with experiment.

Full-dimensional rovibrational calculations

The 6-D rovibrational Schrödinger equation was solved with a product basis and the symmetry-adapted Lanczos method (42, 43). The method is explained in Refs. (30, 31, 44, 45). The product basis functions are

$$f_{\alpha_0}(r_0)f_{\alpha_1}(r_1)f_{\alpha_2}(r_2)u_{j_1j_2m_2K}^{JM\bar{p}}(\theta_1, \theta_2, \phi; \alpha, \beta, \gamma), \quad (1)$$

where $f_{\alpha_i}(r_i)$ is the discrete variable representation (DVR) function and $u_{j_1j_2m_2K}^{JM\bar{p}}$ is a parity-adapted bend-rotation function. α, β, γ are Euler angles specifying the orientation of the body-fixed frame in the space-fixed frame. r_0 is the inter-monomer distance; r_1 and r_2 are the monomer bond lengths. θ_1, θ_2, ϕ are polyspherical angles. $\bar{p}$ labels the parity.

Basis parameters are chosen to ensure energy levels are converged. Potential optimised DVR (PODVR) bases (46, 47) are used for r_1 (H_2) and r_2 (CO) coordinates. With the basis II specified

in table S7, all the bound states are converged to within 0.0001 cm^{-1} except for a few bound states near the dissociation limit and the resonance states.

The infrared spectrum was recorded in the vicinity of the CO $v_2 = 0 \rightarrow 1$ transition at $2143.2711 \text{ cm}^{-1}$ (3). The density of states is high. We label each state with a value of v_2 . $v_2 = 1$ states exist in a dense set of $v_2 = 0$ states. To label, we compute the expectation value of $\hat{H}' = -\frac{1}{2\mu_{\text{CO}}} \frac{\partial^2}{\partial r_2^2} + V_{\text{CO}}(r_2)$, where $V_{\text{CO}}(r_2)$ is the free CO potential. $v_2 = 1$ states have expectation values close to $1.5 \omega_{\text{CO}}$, where ω_{CO} is the CO frequency. The expectation values are computed using the Hellmann-Feynman theorem by computing energy levels of the perturbed Hamiltonian $\hat{H}(\lambda) = \hat{H}_0 + \lambda \hat{H}'$, where $\hat{H}_0$ is the H₂-CO Hamiltonian and $\lambda = 10^{-5}$, following Ref. (48).

4D rovibrational bound and scattering calculations

We have employed the BOUND and MOLSCAT programs (32) to perform the 4D rovibrational and scattering calculations. The rotational constants were the same as in Refs. (2, 20): $B_0(\text{H}_2) = 59.322 \text{ cm}^{-1}$, $B_0(\text{CO}) = 1.9225 \text{ cm}^{-1}$ and $B_1(\text{CO}) = 1.9050 \text{ cm}^{-1}$ (49). The basis set and integration ranges were increased compared to Refs. (2, 20): CO rotational quantum number j_2 from 8 to 12 (to 15 in scattering calculations), the partial wave expansion of the PES in BOUND/MOLSCAT was increased from $l = 10$ to 12, the numerical integration step was decreased from 0.4 to 0.3 Å in the bound-state calculations and was equal to 0.05 bohr in the scattering calculations. The scattering energy was scanned with a step size of 10^{-4} cm^{-1} . Narrow resonances were first localized with the stabilization method and then scanned in scattering calculations with adaptive steps.

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Supplementary Materials

This PDF file includes:

Fig. S1

Tables S1 to S7

Other Supplementary Materials for this manuscript include the following:

Computer routine generating the V_{23} surface

Computer program for deducing experimental rovibrational energy levels of *ortho*H₂–CO from the assigned transitions.

Fig. 1

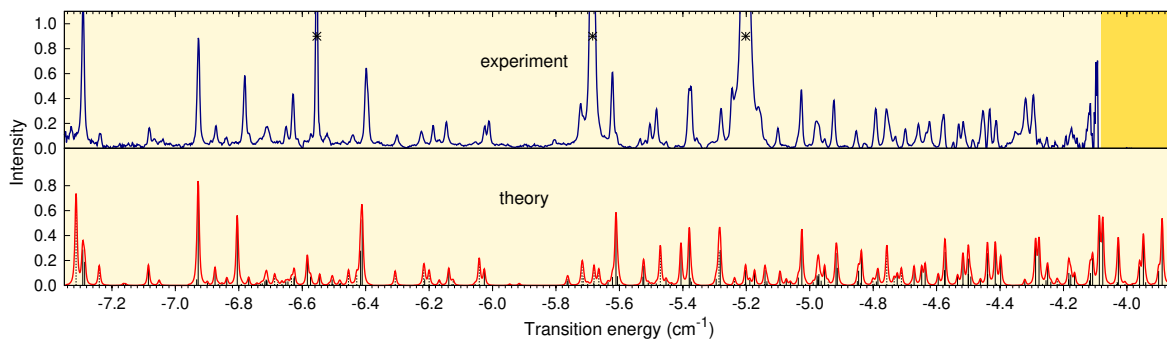


Fig. 1: A partial comparison of experimental and theoretical infrared spectra of *ortho*-H₂-CO. *Continuous lines:* measured spectrum (blue, top row) (2) and the theoretical one (red, bottom row) from the present work; *solid (dashed) vertical bars under the peaks:* transitions between two bound (involving at least one resonance) rovibrational states; *asterisks:* various isotopologues CO monomer lines; *yellow-shaded area:* region where measurements of the H₂-CO spectra were not possible; *zero of energy:* 2143.2711 cm⁻¹, the $v = 0 \rightarrow 1$ vibrational frequency of the isolated CO monomer.

Fig. 2

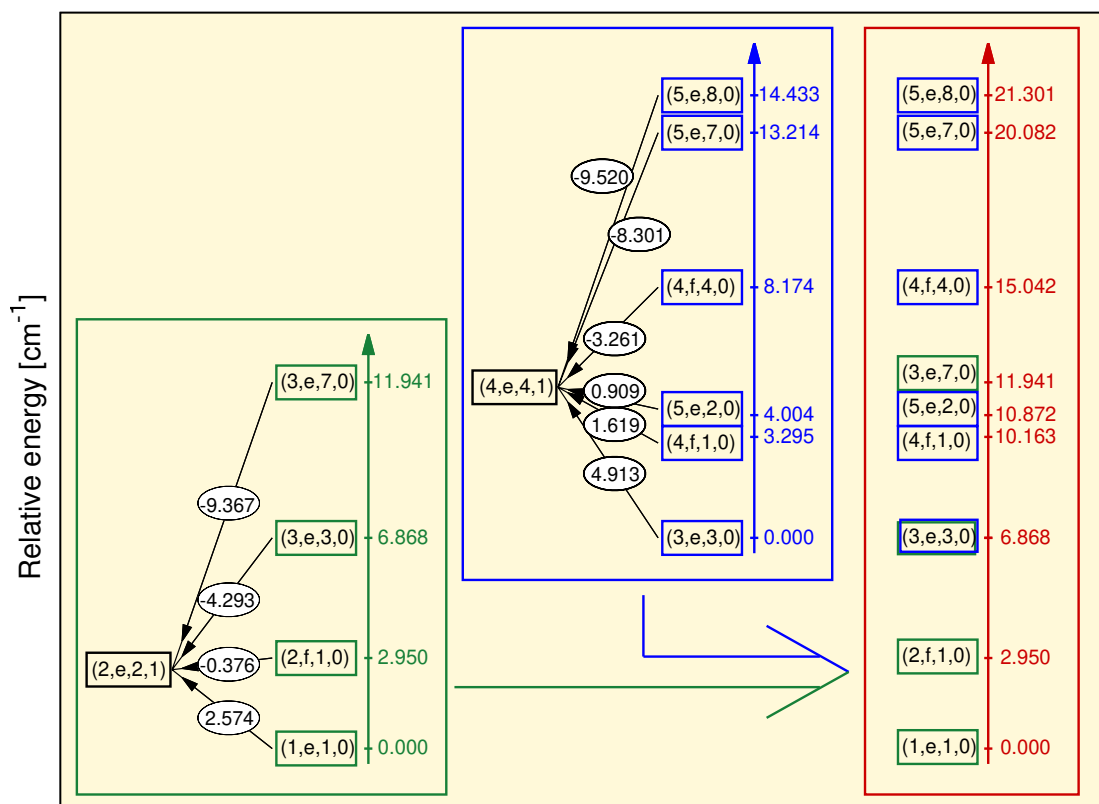


Fig. 2: Illustration of the protocol for deducing rovibrational energy levels from assigned infrared transitions energies.

Fig. 3

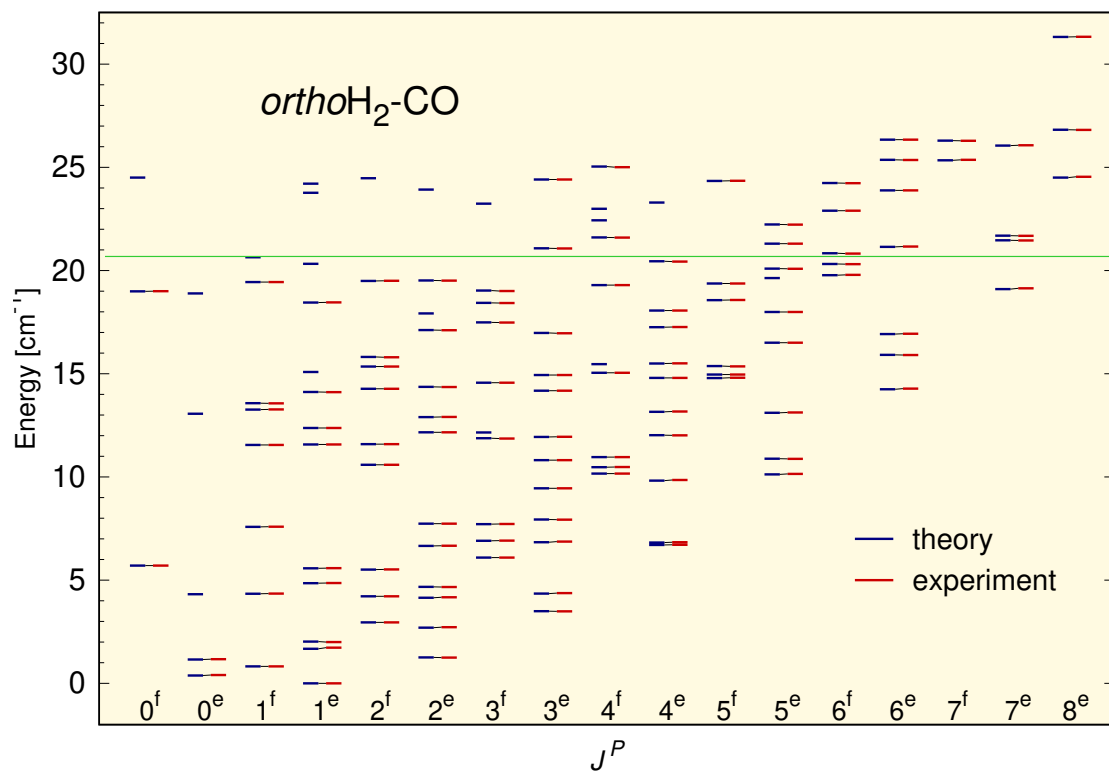


Fig. 3: Experimental and theoretical energy levels of *ortho*H₂-CO for $v_2 = 0$. The theoretical levels (in blue) are given relative to the lowest rovibrational state (1, e, 1, 0). The experimental levels (in red) are given relative to the corresponding experimental one. The green line marks the dissociation threshold.