

Arbitrary Aperture Synthesis with Nonlocal Leaky-Wave Metasurface Antennas

Gengyu Xu¹, Adam Overvig¹, Yoshiaki Kasahara^{1,2}, Enrica Martini³, Stefano Maci³ and Andrea Alù^{1,4,5}✉

¹ Photonics Initiative, Advanced Science Research Center, City University of New York; New York, NY 10031, United States

² Department of Electrical Engineering, The University of Texas at Austin; Austin, TX 78712, United States

³ Department of Information Engineering and Mathematics, University of Siena; Siena, 53100, Italy

⁴ Department of Electrical Engineering, The City College of New York; New York, NY 10031, United States

⁵ Physics Program, Graduate Center, City University of New York; New York, NY 10016, United States

✉ email: aalu@gc.cuny.edu

Abstract: The emergence of new technological needs in 5G/6G networking and broadband satellite internet access amplifies the demand for innovative wireless communication hardware, including high-performance low-profile transceivers. In this context, antennas based on metasurfaces – artificial surfaces engineered to manipulate electromagnetic waves at will – represent highly promising solutions. In this article, we introduce leaky-wave metasurface antennas operating at micro/millimeter-wave frequencies that are designed using the principles of quasi-bound states in the continuum, exploiting judiciously tailored spatial symmetries that enable fully customized radiation. Specifically, we unveil a new degree of control of leaky-wave radiation by demonstrating pointwise control of amplitude, phase and polarization state of the metasurface aperture fields by carefully breaking relevant symmetries with tailored perturbations. We design and experimentally demonstrate metasurface antenna prototypes showcasing a variety of functionalities advancing capabilities in wireless communications, including single-input multi-output and multi-input multi-output near-field focusing, as well as far-field beam shaping.

Introduction

Leaky wave antennas (LWAs) are travelling wave transceivers with highly desirable practical features, including high directivity, low profile, simple feeding architecture and inherent beam-scanning capability enabled by frequency dispersion¹. They leverage tailored perturbations that partially couple guided electromagnetic modes into directive free-space radiation. Owing to their flexibility, LWAs have found application not just in wireless communications, but also for imaging^{2,3}, radar detection⁴ and remote sensing⁵ systems. The key design parameters for a traditional LWA are the attenuation and propagation constants, which respectively control, to a limited degree, the effective aperture and scan angle of the radiated beam (typically a simple linearly-polarized plane wave). The polarization is usually fixed to a single state, dictated by the antenna architecture.

The limited set of degrees of freedom (DoFs) offered by conventional LWAs do not meet the large demand from today's wireless infrastructures for data capacity, channel diversity and energy efficiency. Hence, recent years have witnessed a proliferation of advanced antenna designs based on electromagnetic metamaterials and metasurfaces⁶⁻¹⁰. These artificial structures consist of subwavelength building blocks called "meta-atoms" or "meta-units" with engineered electromagnetic scattering responses. Their ability to manipulate fields and waves has unlocked a plethora of novel high-performance radio-frequency wireless devices, including LWAs with unprecedented capabilities. For example, ultra-thin artificial impedance surfaces supporting surface waves can be made radiating via periodic or quasi-periodic perturbations to their effective electric impedance, forming holographic leaky-wave metasurfaces (LWMS)^{11,12}. With properly engineered anisotropy, the effective impedance takes a tensorial form, leading to radiation with controlled polarization states^{13,14}. To exert simultaneous and independent control over all aspects of the aperture field, and accordingly the far-field radiation, LWAs incorporating Huygens' metasurfaces¹⁵⁻¹⁷ or cascaded tensorial impedance sheets have been proposed¹⁸. Instead of modelling the meta-atoms as continuous sheets of effective electric and magnetic polarization currents, it is also possible

to treat them as discrete arrays of non-interacting resonant dipoles¹⁹⁻²¹. This latter approach trades some of the beamforming DoFs of the former, for simpler designs which are easier to realize in practice.

Besides the aforementioned metasurfaces exploiting an engineered local response to external fields, the emerging field of “nonlocal” metasurfaces has been showing that it is possible to fully tailor all aspects of electromagnetic wave interactions by harnessing the mutual coupling among meta-units (e.g., mediated by a guided mode). These nonlocal metasurfaces have been receiving intense investigation in the optical regime, particularly in the context of bound states in the continuum (BICs), which are resonant modes that remain confined despite their compatibility in terms of momentum with a continuum of radiating waves (i.e., accessible radiation channels)^{22,23}. One class of BICs, known as symmetry-protected BICs, are of particular interest to the scientific and engineering communities^{23,24}. They arise from certain symmetries in the modal field profile that inhibit coupling to far-field radiation due to mismatched field parity. However, when these modal symmetries are broken through tailored perturbations, they turn into “quasi-BICs” (q-BICs), which can radiate with fully controlled features^{25,26}. Researchers have utilized this concept to shape the wavefront, polarization and spectra of coherent as well as thermal emission²⁷ with extreme precision. Very recently, this concept has also enabled integrated photonic leaky-wave metasurfaces leveraging spatially varying perturbations to symmetry-broken photonic crystal slabs to convert guided optical modes into customized free-space emission²⁸.

The q-BIC framework is very powerful in terms of added degrees of freedom and waveform control, since its underlying principles stem from spatial symmetries²⁵. Hence it is generalizable to any frequency regime and it is agnostic to details of the physical implementation (to first order in perturbation theory). Furthermore, it enables a completely rational design scheme for highly sophisticated nonlocal metasurfaces, by providing a set of simple algebraic relations linking the four DoFs of a monochromatic wave (amplitude, phase, orientation and ellipticity of polarization) to four

independent geometrical DoFs embedded inside the constituent meta-unit. This feature represents a significant advantage over conventional metasurface design approaches, which often require cumbersome numerical optimization or the construction of extensive meta-atom look-up tables to bridge the gap between idealized analytical models and physical implementations.

In this work, motivated by emerging technological needs in 5G/6G networking, satellite internet, autonomous vehicles and smart/cognitive radio environments^{29,30}, we translate the concept of q-BICs from optical frequencies into the micro/millimeter-wave spectrum to empower advanced nonlocal leaky-wave metasurface antennas with fully controlled radiation features. Although the underlying design principles are consistent with integrated photonic LWMs²⁸, operation at mm-waves enables increased flexibility by the much more versatile and accessible printed circuit board (PCB) manufacturing platform. For example, the incorporation of a conductive ground plane admits unidirectional radiation with significantly higher directivity than attainable at optical frequencies (for which compact and low loss reflectors near the guided mode are not trivially achieved). Furthermore, we can feed the LWM with sophisticated and compact substrate-integrated wave launchers, opening the opportunity for more advanced modes of operation (e.g., multi-port excitations). Moving into radio-frequencies also introduces new challenges, such as limitations on the aperture size and the overall device footprint (due to increased wavelength), demanding innovative solutions that take full advantage of the available fabrication technologies.

As proofs of concept, we present three q-BIC-based LWM antenna prototypes with unprecedented functionalities for leaky-wave radiation control. The first metasurface antenna is a single-input multiple-output (SIMO) LWM lens that generates two distinct orthogonally polarized focal spots placed at arbitrary locations from a single guided mode input. The second design realizes a multiple-input multiple-output (MIMO) lens that focuses its radiation to different locations within the Fresnel zone, depending on which of its two ports is excited. Lastly, we present a multi-beam LWM antenna

with dual-polarized far-field beam-shaping capabilities. All three implementations are validated through full-wave numerical simulations, as well as experimental measurements.

Results

Working Principle. The physical principles governing the radiative behavior of symmetry-protected q-BICs are general, and they can be applied to a range of vastly different device platforms. Here, for illustrative purposes we utilize a parallel plate waveguide (PPWG) with thickness h and relative permittivity ϵ_r , perforated by a staggered array of rectangular slots (Fig. 1), which supports a q-BIC in the form of a quasi-transverse-electromagnetic (TEM) mode. The shape and the orientation of the slots have been tailored such that the mode leaks energy in a fully controlled fashion as it propagates. Here, the parameters A and Φ refer to the local field amplitude and phase over the LWM aperture, while ψ and χ refer to longitude and latitude of the local polarization state on the Poincaré sphere. The dependence of these parameters on the spatial coordinates (x, y) and a global time convention of $e^{j\omega t}$ are left implicit for brevity. In the following subsections, we summarize the design methods

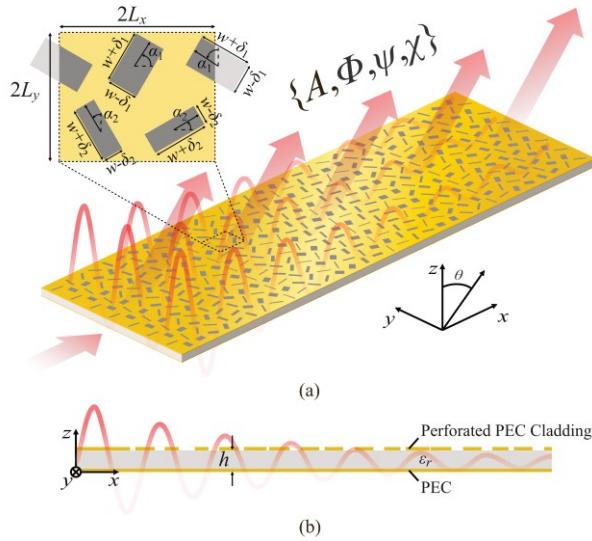


Figure 1: Leaky-wave metasurface antenna supporting quasi-bound states in the continuum. (a) Isometric and (b) side view of a schematic drawing. The amplitude A , phase Φ and polarization state ψ, χ of the aperture fields can be independently controlled in a point-wise fashion by locally engineering the geometrical perturbations (inset) to the perforated parallel plate waveguide.

employed to rationally pattern the slot array and exert pointwise control over all four DoFs of the aperture field [22], along with new physical insights into the underlying phenomena.

Control of Radiation Magnitude. We begin by examining the simplest case of an LWM perforated by uniformly sized staggered square slots (with width w), whose primitive unit-cell (when considering a rectangular lattice) is pictured in Figure 2a, marked by the dotted outline and with dimensions $L_x \times 2L_y$. Using numerical simulations (see Methods), we evaluated the first Brillouin Zone (FBZ) of a typical dispersion diagram for x -directed wave vectors (Figure 2b), in which the purple dashed line represents the free-space light line. The lowest-order eigenmode is a quasi-TEM travelling wave with respect to \hat{x} . At the X high-symmetry point ($k_x = \pi / L_x$) of the FBZ, such a mode (marked by the green star) can be referred to as an “artificial BIC” (a-BIC)³¹: when we artificially double the metasurface periodicity along \hat{x} by considering two adjacent primitive cells as a collective meta-unit, as done in Figure 2c, the mode is shifted to the Γ point ($k_x = 0$) of the new folded

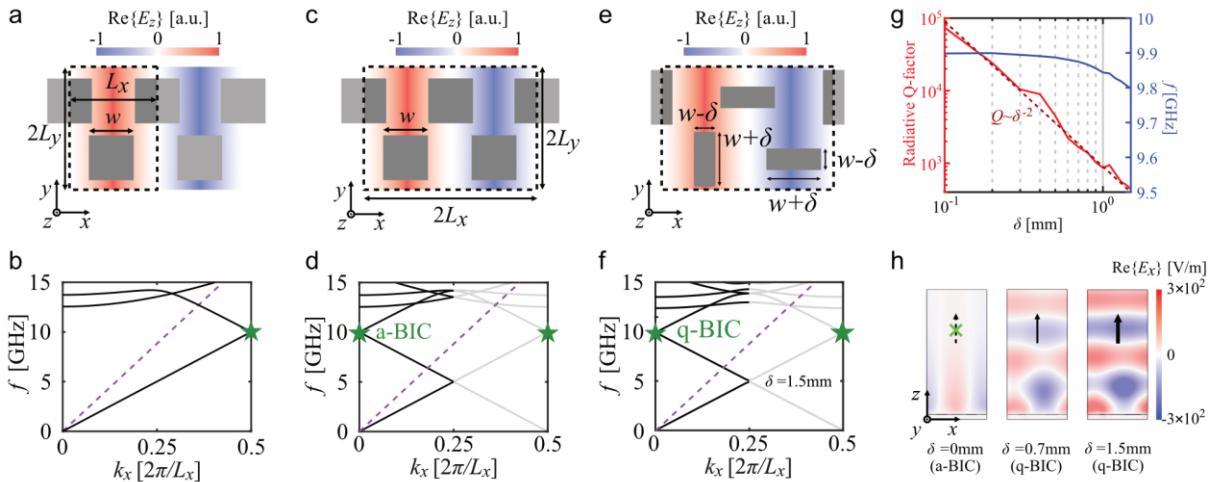


Figure 2. Quasi-bound state in the continuum with controlled radiative Q-factor. (a) Sketch of the electric field of a bound quasi-TEM mode supported by the perforated waveguide and (b) its simulated dispersion diagram, assuming $2L_x = 8.5$ mm, $L_y = 6.5$ mm, $w = 3$ mm, $\epsilon_r = 3$, $h = 1.52$ mm. (c) Artificial periodic doubling along the \hat{x} direction corresponds to (d) folding the FBZ, which moves the mode of interest (green star) to the Γ point in an artificial continuum. (e) A period-doubling, symmetry-breaking perturbation with strength δ converts the mode from an artificial-BIC to a quasi-BIC, with minimal disturbance to the (f) band structure. (g) The radiative Q-factor of the q-BIC varies as δ^{-2} , while its resonant frequency is mostly independent of δ . (h) Simulated electric field intensity above the waveguide, showing stronger radiation due to larger perturbation.

FBZ (Figure 2d), where it now resides above the light line. Despite *artificially* coexisting with a continuum of radiating waves, this mode cannot couple to the far-field. One interpretation for the lack of energy leakage is provided by the symmetry of the modal field profile: since the aperture electric field over each two adjacent slots have the same magnitude but are in anti-phase, they destructively interfere with each other in far-field. As a result, the a-BIC possesses an ideally infinite radiative Q-factor. Ultimately, it is important to remember that, in the current configuration, the mode in fact resides below the light line. Therefore, its confinement to the waveguide is not surprising, and it is guaranteed by translational symmetry.

The key realization to enable leaky-wave metasurfaces is that we can revoke the *symmetry protection* that inhibits the a-BIC from radiating by introducing a period-doubling symmetry-breaking perturbation to the meta-unit as depicted in Figure 2e (and with corresponding band diagram in Figure 2f), where the parameter δ quantifies the degree of introduced asymmetry. In this way, one of the two neighboring slots radiates stronger than the other, and the mode is transformed into a leaky q-BIC with finite radiative Q-factor. Hence, the “artificial continuum” is promoted to a “true continuum”. As seen in Figure 2g, the Q-factor varies approximately as δ^{-2} , implying that a higher degree of asymmetry leads to more intense radiation^{23,24}. To illustrate this further, Figure 2h showcases snapshots of the simulated electric field distribution above the waveguide for several values of δ . Larger perturbations evidently produce stronger radiated fields. It is also possible to map the Q-factor to the corresponding attenuation (leakage) constant, more commonly used in the leaky-wave antenna literature³².

The degree of asymmetry of each meta-unit can be individually controlled, allowing us to precisely pattern the amplitude profile of the entire LWM aperture in a point-wise fashion. In this study, we have neglected the tapering of the q-BIC power density as it propagates along the LWM. Such an approximation will not cause significant issues for weakly perturbed designs, since they generally

have small leakage rates. It is also worth noting that, as revealed by Figure 2g, the resonant frequency of the q-BIC, i.e., the eigenfrequency at the Γ point, is only weakly dependent on the perturbation strength. When larger perturbations are considered, it may be necessary to slightly adjust the slot dimensions in order to compensate for the frequency drift, which may otherwise lead to undesirable radiation squinting.

Control of Linear Polarization State. The polarization of the radiated field can be customized by breaking the mirror symmetries of each adjacent pair of slots. For instance, we can introduce a rotation angle α as shown in the inset of Figure 3. When $\alpha \in [0^\circ, 90^\circ]$, the aperture electric fields of both slots are symmetric around the xz –plane. A magnetic wall bisects both slots, leading to purely x –polarized radiation into the far-field. Conversely, when $\alpha \in [45^\circ, 135^\circ]$, a magnetic wall is formed between the slot pair, giving rise to purely y –polarized radiation. Continuously sweeping α from 0° to 180° allows us to traverse the equator of the Poincaré sphere twice, covering all possible combinations of linear polarization states and polarity.

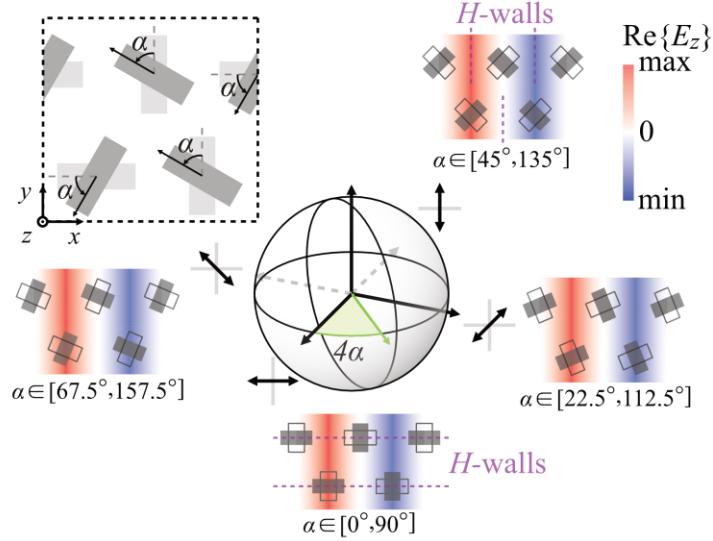


Figure 3: Control of the linear polarization state of radiation through rotation of the slots. The two choices of α (differing by $\pi/2$) are depicted as gray solid rectangles and empty rectangles; the fields produced differ by a phase factor π .

Control of Aperture Phase. To locally control the phase of the radiated fields, we introduce another geometric degree of freedom, imparting different perturbation strengths to the upper and lower rows of the meta-unit. At the Γ point, the modal profile of the q-BIC includes two rows of radiating apertures that are 90° out of phase, as they are staggered by $1/4$ of a guided wavelength. Hence, the perturbation strengths for the lower and upper pairs (δ_1 and δ_2) can independently control the in-phase and quadrature components of the radiating part of the aperture field, granting us full 360° phase coverage. In Figure 4, we demonstrate how to tailor the phase for x -polarized fields. The same scheme can be used for any other linearly polarized radiation if we set $\alpha \notin [0^\circ, 90^\circ]$, following

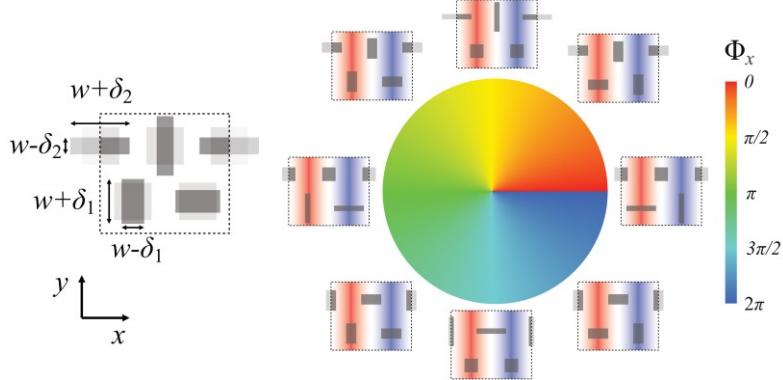


Figure 4: Phase control with two symmetry-breaking perturbations. The perturbations to the upper and lower rows can independently control the in-phase and quadrature components of the aperture, resulting in a geometric phase for x -polarized radiation (Φ_x).

Figure 3.

We can parameterize the perturbation strengths of the two rows as

$$\delta_1 = \delta \cos \Phi, \quad \delta_2 = \delta \sin \Phi, \quad (1)$$

where Φ is the desired phase. This mapping reveals the geometric nature of the aperture phase, implying that, when patterned with slowly varying profiles, the LWM is robust against performance degradations typically associated with the sharp geometric discontinuities at phase wraps ³³.

We note that the introduction of this final degree of freedom breaks the translational symmetry between the top and the bottom rows of the meta-units (i.e., they are shifted copies of one another), and such broken symmetry opens a bandgap at the Γ point of the folded FBZ. However, this gap is typically very small, with negligible influence over the performance of a finite-size device.

Full control of Leaky Wave Radiation. Based on these principles, we may exert full control over the four degrees of freedom for the radiated waves from each meta-unit by imparting different perturbation strengths $\delta_{\{1,2\}}$ and rotation angles $\alpha_{\{1,2\}}$ to the lower and upper slot pairs (see inset of Figure 1). In turn, these degrees of freedom allow us to tailor both the magnitudes and linear polarization states of the in-phase and quadrature components of the aperture field. More precisely, the radiated electric field of each meta-unit can be described by

$$\begin{bmatrix} E_x \\ E_y \end{bmatrix} = \delta_1 \begin{bmatrix} c_x \cos 2\alpha_1 \\ c_y \sin 2\alpha_1 \end{bmatrix} + j\delta_2 \begin{bmatrix} c_x \cos 2\alpha_2 \\ c_y \sin 2\alpha_2 \end{bmatrix}. \quad (2)$$

The weights c_x and c_y account for the unequal coupling strengths of the quasi-TEM mode with x - and y -polarized radiation (i.e., the Q-factor varies sinusoidally with α). Here, we have assumed that the radiated field magnitude varies approximately linearly with respect to δ , which is valid within the small perturbation regime and is consistent with Figure 2g.

Equating (2) with the most general form of an arbitrarily stipulated aperture field

$$\begin{bmatrix} E_x \\ E_y \end{bmatrix} = \begin{bmatrix} A_x e^{j\Phi_x} \\ A_y e^{j\Phi_y} \end{bmatrix} = \begin{bmatrix} E'_x \\ E'_y \end{bmatrix} + j \begin{bmatrix} E''_x \\ E''_y \end{bmatrix}, \quad (3)$$

we obtain deterministic design equations for all geometrical parameters of the meta-unit:

$$\alpha_1 = \frac{1}{2} \tan^{-1} \left[\frac{c_x E'_y}{c_y E'_x} \right], \quad \alpha_2 = \frac{1}{2} \tan^{-1} \left[\frac{c_x E''_y}{c_y E''_x} \right], \quad (4a)$$

$$\delta_1 = \delta \cos t_\delta, \quad \delta_2 = \delta \sin t_\delta, \quad (4b)$$

$$t_\delta = \tan^{-1} \left[\sqrt{\left| \frac{E_x''}{c_x} \right|^2 + \left| \frac{E_y''}{c_y} \right|^2} / \sqrt{\left| \frac{E_x'}{c_x} \right|^2 + \left| \frac{E_y'}{c_y} \right|^2} \right] \quad (4c)$$

Here, δ is the maximum perturbation strength, which can be chosen in compliance with design considerations such as overall footprint and fabrication tolerance. Note that the only system-specific parameters in (4) are the two unknown coupling constants c_x and c_y , which can be retrieved through full-wave numerical simulations of physical models. Hence, we can use the same set of equations to design LWMs with much more sophisticated slot topologies, e.g., meandered slots, or even one with a totally different physical implementation, e.g., a grounded dielectric slab with metallic patch claddings, or additively manufactured metallic pillar arrays³⁴. This is in sharp contrast with conventional metasurface design methods which heavily rely on phenomenological descriptions, such as equivalent circuits or homogenization theory, which cannot be easily transferred between different technological platforms.

In the following examples, we adopt these rational design principles to synthesize and experimentally validate several LWM antennas with a wide range of functionalities. For simplicity, we restrict our attention to one-dimensional designs which are periodic along the y direction.

Single-input / Multiple-output Focusing. As a first remarkable demonstration, we design a SIMO leaky-wave metasurface antenna that generates two spatially separated near-field focused spots with orthogonal circular polarizations from a single input wave (Figure 5a). We stipulate an aperture electric field distribution consisting of two superimposed converging cylindrical wavefronts centered at $\vec{r}_{\{R,L\}}^*$, described by

$$\begin{bmatrix} E_x \\ E_y \end{bmatrix} = \frac{1}{\sqrt{2}} \begin{bmatrix} E_R + E_L \\ jE_R - jE_L \end{bmatrix}, \quad (5a)$$

$$E_{\{R,L\}} = H_0^{(1)}(k_o |\vec{r} - \vec{r}_{\{R,L\}}^*|), \quad (5b)$$

where $E_{\{R,L\}}$ are the complex amplitudes of the two circularly polarized aperture field components,

$H_0^{(1)}$ is the 0^{th} -order Hankel function of the first kind, and k_o is the free-space wavenumber.

We select a design frequency of 20.55GHz in the mm-wave range, and focal points $\vec{r}_R^* = (-2\lambda_o, 6\lambda_o)$,

$\vec{r}_L^* = (\lambda_o, 4\lambda_o)$, where λ_o is the free space wavelength. The unperturbed square slots have widths

$w = 1.85$ mm, while the maximum perturbation strength δ is set to 1.55mm. The meta-unit

dimensions are $2L_x = 8.25$ mm and $2L_y = 6.25$ mm. The y -periodicity is made smaller than the x -

periodicity in order to shift all transversely propagating modes up in frequency, thereby suppressing

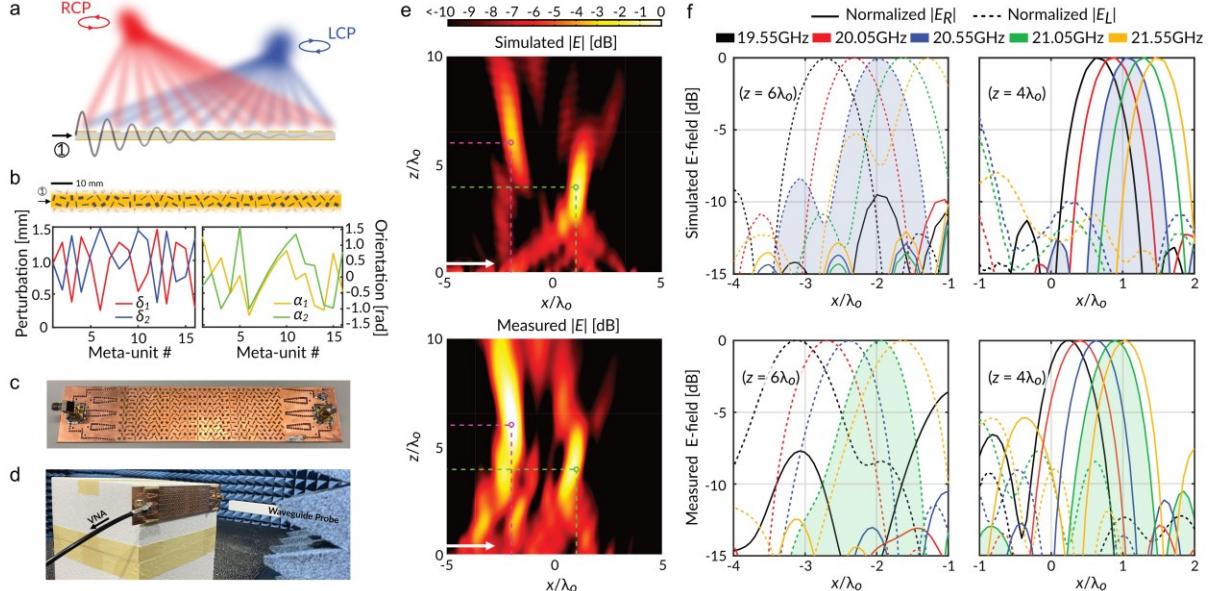


Figure 5: Single-input multi-output focusing LWM. (a) When excited by an input wave from port 1, the realized LWM focuses its output power to two distinct spots in the Fresnel zone, one right-handed circularly polarized, the other left-handed. (b) Analytically derived geometrical parameters for the meta-units. (c) Fabricated LWM sample. (d) Near-field scanning experimental setup. (e) Simulated (20.55GHz) and measured (20.05GHz) electric field intensity produced by the LWM. The pink and the green circles mark \vec{r}_R^* and \vec{r}_L^* respectively. (f) Polarization-resolved simulation and measurement results in the $z = 6\lambda_o$ and $z = 4\lambda_o$ planes confirm the correct CP state for the two focal points. As the input frequency is swept from 19.55GHz to 21.55GHz, the focal spots can be scanned laterally in those planes. The shaded curves correspond to the frequencies used to generate panel e.

them in the band of interest²⁸. The antenna aperture consists of 16 distinct meta-units, making it approximately $9\lambda_0$ long. The substrate is assumed to have a dielectric constant of $\epsilon_r = 3$ and thickness of $h = 1.52$ mm. Materials with higher dielectric constants can be used to miniaturize the meta-unit dimensions with respect to the free-space wavelength, which serves to reduce the overall device footprint and enable more precise control over the aperture field distribution. For simplicity, we assume that the q-BIC can couple to x – and y – polarized radiation with equal efficiencies (i.e., $c_x = c_y$). Then, inserting (5) into the synthesis equations (4), we directly obtain the required meta-unit geometries of our LWM, which have been summarized in Figure 5b.

To excite the q-BIC mode, conventional compact TEM-wave launchers can be employed³⁵⁻³⁷. However, they typically suffer from severely restrictive bandwidths or implementation complexity. Considering both factors, we choose to feed our LWM with a four-way substrate integrated waveguide (SIW) power divider that tapers into a horn array (see Supplementary Figure 1). A photograph of the fabricated prototype is shown in Figure 5c. Figure 5d depicts our experimental measurement set up (see Methods for details). To verify the functionality of our design, we first performed preliminary full-wave numerical simulations with a simplified model of the LWM which is infinitely periodic along the lateral direction (see Methods). The calculated normalized Fresnel-zone electric field intensity is plotted in the top of Figure 5e. There are two clearly observable focal spots centered at \vec{r}_R^* and \vec{r}_L^* , marked by the pink and green circles respectively. Similar results can be observed in the experiment (bottom plot). Due to nonidealities such as lateral truncation, imperfection in the input wavefront, fabrication tolerances [See Supplementary Figure S3 for additional discussion], and deviation of the dielectric substrate properties from their nominal values, the optimal operating frequency was downshifted from 20.55GHz to 21.05GHz. Hence, we have plotted the measured field intensity at the latter frequency. Despite the slight discrepancy between simulation and measurements, we can observe two high-field-intensity regions near the designated

focal spots. The measured -10dB input reflection bandwidth is approximately 2.3GHz (see Supplementary Figure 2), which may be further improved by optimizing the transition between the launcher and the LWM.

To resolve the polarization state of the LWM output, we evaluate the LCP and RCP components at the two designated focal planes, according to³⁸

$$\begin{bmatrix} E_R \\ E_L \end{bmatrix} = \frac{1}{\sqrt{2}} \begin{bmatrix} E_x - jE_y \\ E_x + jE_y \end{bmatrix}, \quad (6)$$

In Figure 5f we plot the normalized simulated (top) and measured (bottom) intensities of RCP (solid lines) and LCP (dotted lines) fields, for various input frequencies. As expected, the focal spot can be continuously scanned in the x – direction simply by tuning the operating frequency, owing to the radiation mechanism of the leaky wave. Importantly, except for a single measurement (19.55GHz, $z=6\lambda$), we observe outputs with very high polarization purity, exhibiting at least 15dB cross-polarization discrimination at the focal spots. This corroborates our ability to independently control the amplitude and phase profiles of the two orthogonally polarized field components. The lateral displacement between the simulated and measured focal spots is again attributed to the nonidealities in the fabricated sample.

We note that the experimentally measured size of our focusing LWM spot is larger than an ideal diffraction limited spot. This is because the tapered aperture profile which we have stipulated through (5b) serves to broaden the focal spot. As shown by Fig. S4 in the Supplementary Material, considering this factor, the focusing power our LWM is very close to the theoretical predictions.

Multi-input Multi-output Focusing. To further exploit the full aperture customizability offered by our nonlocal LWM, we implement a device that focuses its output to different arbitrary near-field positions when excited from different ports. This capability enables MIMO near-field communication

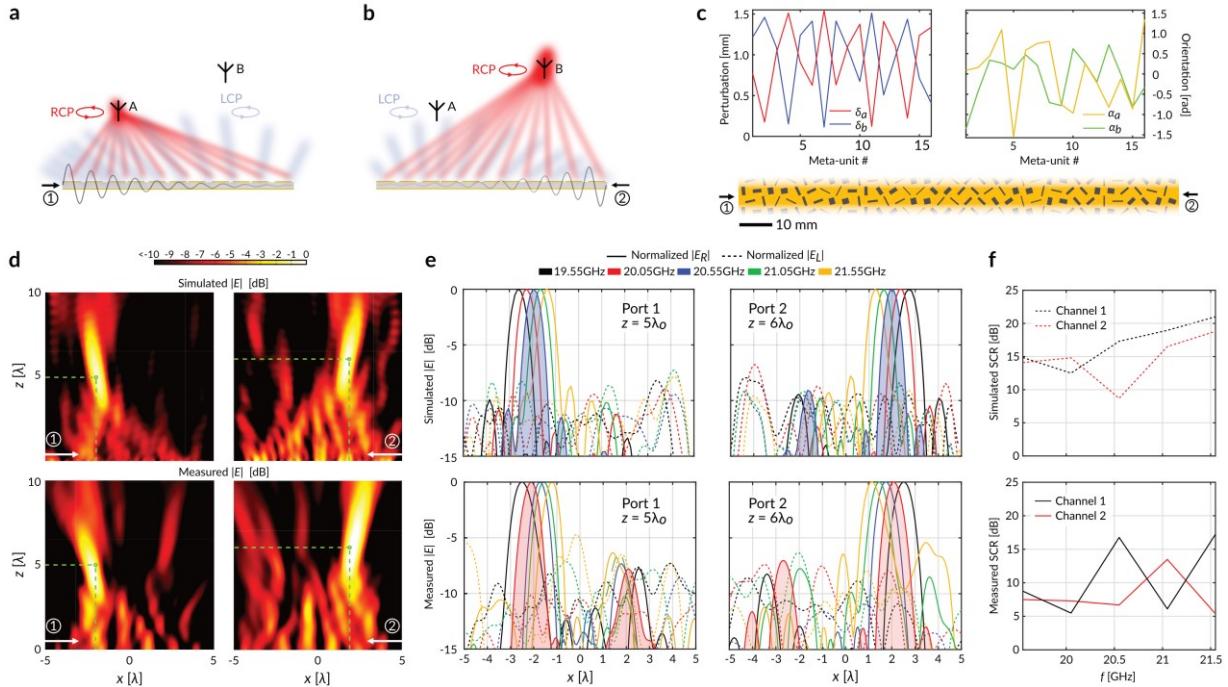


Figure 6: Multi-input multi-output focusing LWM. (a) When excited by an input wave from port 1, the LWM produces a focused RCP wave. (b) When excited from port 2, the same device emits another RCP wave focused to a different spot. In both cases, there is a weak LCP background. (c) Analytically derived geometrical parameters for the meta-units of the MIMO LWM. (d) Simulated and measured Fresnel-zone field electric field intensities when the two ports of the LWM are excited individually. The white arrow denotes the excitation port, while the green circle denotes the theoretically predicted output focal spot. (e) Simulated and measured electric field intensities at the two designated focal planes, demonstrating frequency-scanned focal spots with high polarization purity. The solid and dashed lines denote the RCP and LCP components of electric field, respectively. (f) Simulated and measured signal-to-crosstalk ratio, showing good isolation between the two independent channels in half-duplex.

via spatial-division multiple access with scannable focal spots - a desirable feature for high-throughput smart radio environments powered by reconfigurable intelligent surfaces³⁹.

We again stipulate an aperture field distribution consisting of two superimposed orthogonal circularly polarized cylindrical waves. However, we now assign a negative focal length for the LCP component (i.e. $y_L^* < 0$), and encode a diverging phase front described by

$$E_L = H_0^{(2)}(k_o |\vec{r} - \vec{r}_L^*|), \quad (6)$$

where $H_0^{(2)}$ is the Hankel function of the second kind. The RCP component of the aperture field remains the same as that given in (5). Effectively, this means that when the leaky q-BIC is excited from port 1 of the LWM, an RCP wave focused at \vec{r}_R^* and a diverging LCP wave emanating from a

virtual source at \vec{r}_L^* will be generated. This results in a region of high field intensity in a right-handed CP state and weak background radiation with left-handed CP (Figure 6a).

On the other hand, when the LWM is excited from the opposite port, a time-reversed copy of the q-BIC is excited, leading to two key consequences. First, the radiated LCP and RCP components are exchanged as they are linked to each other by time-reversal. In other words, the aperture profile previously encoded for LCP is now responsible for the RCP radiation, and vice versa. Second, the patterned phase profiles are conjugated due to time-reversal symmetry, transforming a converging (diverging) wavefront into a diverging (converging) one. The combined result is that the radiation of the LWM again consists of a focused RCP spot and a weak LCP background (Figure 6b). Notably, the focal points produced by port 1 and port 2 excitations can be independently stipulated, as they are controlled by two completely uncorrelated aperture field profiles. This allows the LWM to be used as a MIMO transceiver which communicates with sources at different locations using different ports.

In contrast with conventional techniques to achieve this effect such as the physical partitioning of a single shared aperture⁴⁰, our proposed concept trades efficiency for more effective aperture illumination. Since each output spot fully leverages the entire physically available aperture area, we obtain significantly enhanced spatial resolution while performing near-field focusing, albeit with reduced polarization purity and power efficiency due to the cross-polarized background radiation.

Interestingly, the physical mechanism by which we achieve MIMO operation is reminiscent of the well-known phenomenon of spin-momentum-locking, which has been reported in metasurfaces with broken rotational symmetries supporting circularly polarized chiral surface waves with out-of-plane spin⁴¹. In our platform, the momentum (direction of propagation of the guided mode) is not necessarily locked to a circularly polarized state (spin). Instead, the customized symmetry-breaking perturbations allow us to couple the q-BIC with any arbitrary polarization state on the Poincaré

sphere, such that when its momentum is reversed, the generated output field can still provide a useful functionality.

We designed and fabricated a MIMO LWM prototype with the same operating frequency and key geometrical features as the previous example. The focal spots are chosen as $\vec{r}_R^* = (-2\lambda_o, 5\lambda_o)$ and $\vec{r}_L^* = (2\lambda_o, -6\lambda_o)$. The analytically derived meta-unit shapes are presented in Figure 6c. In Figure 6d, we plot the simulated and measured near-field electric field intensities with port 1 and port 2 excitations respectively. For each input, a distinct focused spot around the intended location (marked by the green circle) is generated, confirming the MIMO functionality of our LWM. Since the optimal frequency was downshifted by nonidealities in the prototype, we have plotted the measured fields at 20.05GHz and the simulated fields at 20.55GHz. Nevertheless, we observe an excellent qualitative agreement between experimental and simulated results, which further confirms the practical viability of our proposed LWM and feeding architecture.

Next, we examine the polarization state of the outputs in the two prescribed focal planes. In Figure 6e, we plot the RCP (solid) and LCP (dashed) components of the simulated and measured electric field for various input frequencies, at the planes $z=5\lambda$ and $z=6\lambda$. As predicted by theory, while one of the two ports is excited, we observe a region of high RCP field strength in its corresponding focal plane. The position of the spot can be steered by tuning the frequency. There is a weak LCP background which is at most -5dB below the peak RCP intensity. The polarization purity is significantly improved at the center of the focal spots where the cross-polarization level is at most -9.3dB (-9.7dB) below the co-polarized radiation, for port 1 (port 2) excitation, throughout the measured frequency range.

To quantify the isolation between the two channels of our MIMO LWM in half-duplex operation, we define the signal-to-crosstalk ratio (SCR) as for channel i as

$$\text{SCR}_i = 10 \log_{10} \left(\frac{P_{i,A}}{P_{i,B}} \right), \quad (7)$$

where $P_{i,j}$ is the power received (sent) by port i from (to) an RCP transmitter (receiver) at location j . As indicated in Figure 6a and Figure 6b, $j \in [A, B]$ denotes one of the two prescribed focal spots of our LWM. The measured and simulated SCR of our LWM for various input frequencies are shown in Figure 6f. We observe satisfactory inter-channel isolation in the measurements (solid lines), with at least 5dB SCR throughout the entire measured scan range. The simulated SCR (dashed lines) is much better, suggesting that the inter-channel interference may be alleviated by considering the effects of the realistic SIW wave launchers. Specifically, due to imperfect wave impedance matching, the launcher on the terminating side of the LWM can generate significant unwanted reflections, which act as input from the opposite port. This effect is especially evident in the bottom left plot of Figure 6d, which shows that port 1 excitation resulted in a weak signature at the focal spot assigned to port 2. Besides improving launcher-to-metasurface transitions, we may increase the aperture size or the leakage rate, ensuring that the q-BIC radiates most of its power before reaching the end. This solution may also unlock full duplex operation by isolating the two ports. Finally, the non-ideal phase front of the excited q-BIC, and the edge effects introduced by the lateral truncation of the sample, both serve to degrade the performance of our practical LWM prototype.

Dual-Polarized Multi-beam LWM Antenna. In the final design example, we demonstrate an LWM antenna capable of generating multiple independent, arbitrarily directed high-gain beams with custom polarizations. It can be useful for spot beam coverage in satellite communications, especially when paired with reconfigurable elements to facilitate dynamic beam-steering and beam-shaping

^{21,42}.

A schematic of the proposed antenna layout is shown in Figure 7a. We consider an illustrative design producing two RCP beams directed at $\theta_{R,1}$ and $\theta_{R,2}$, as well as a single LCP beam directed at $\theta_{L,1}$. For simplicity, we attribute each beam to a uniform aperture with appropriate linear phase gradient. Furthermore, we assign different weights ($A_{R,1}$, $A_{R,2}$, $A_{L,1}$) to the three summands of the complete aperture, to scale their relative gain in the far-field. We assume the parameters $f = 20.55$ GHz, $\theta_{R,1} = -\theta_L = 10^\circ$, $\theta_{R,2} = 20^\circ$, $A_{R,1} = A_L = 1$, $A_{R,2} = 1.14$, for which the synthesis equations yield an antenna design described by Figure 7b. The experimentally measured radiation patterns at the slightly detuned optimal frequency of 20.8GHz match simulation results (see Methods) almost exactly in terms of the realized gains and the directions of the main beams. In both results, we observe two distinctive RCP beams with -10dB side lobe levels (SLL), as well as a single LCP beam with a -8dB back lobe at around -30° , but otherwise low SLL. The back lobe is caused by the counter

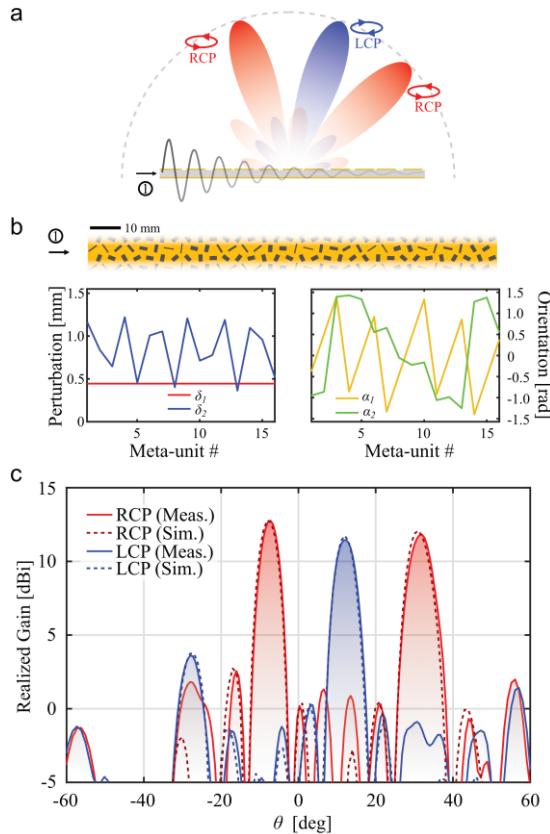


Figure 7: Dual-polarized multi-beam LWM antenna. (a) When excited at port 1, the LWM radiates two RCP beams and one LCP beams with arbitrarily specified directions and relative gain. (b) Analytically derived geometrical parameters for the meta-units. (c) Simulated and measured (realized) gain of the LWM antenna.

propagating wave due to reflections at the transition between the LWM and the SIW power divider.

Hence, to suppress it, one can optimize the impedance matching between these two components. It is possible to further enhance the directivity of the main beams by numerically optimizing its aperture field profile, with the objective of suppressing all spurious lobes. In both the simulation and the experiment, a small amount of beam squinting from the prescribed scan angles is observed, due to frequency dispersion.

In this work, we limit ourselves to the small perturbation regime for simplicity, hence the antenna designs may suffer from reduced efficiency. For instance, the numerically simulated radiation efficiency (including dielectric and conduction loss) of the multi-beam LWM is 44%. This metric can be significantly improved by: 1) increasing the physical size of the antenna aperture; and 2) utilizing more sophisticated meta-unit designs with lower radiative Q-factors, such as a set of four meandered slots⁴³. However, for each given meta-atom design, there exists a maximum bound on the leakage rate, since the size of the slots and the allowable perturbations are limited by the meta-unit footprint. Hence, in order to obtain a certain level of radiation efficiency, the physical size of the LWM aperture must exceed a corresponding lower limit (i.e., it must contain sufficiently many meta-atoms).

Additionally, it is important to keep in mind the inherent trade-off between radiation efficiency and aperture efficiency, since large leakage rates will lead to lower q-BIC power density near the end of the LWM. This issue can be corrected using an analytically derived aperture amplitude envelope to counterbalance the tapered excitation intensity^{1,44}. Finally, we emphasize that our perturbative design framework assumes a primarily dipolar-like element factor for all meta-units, which is most accurate near broadside. At very large oblique angles (i.e., towards the end-fire directions), the presented design formulae lose accuracy in their ability to capture the nature of the radiation. To address this issue, future work can rigorously model higher order multipole terms in the element factors⁴⁵.

Outlook and Conclusion

In this work, we introduced a class of leaky-wave metasurface antennas empowered by quasi-bound states in the continuum and associated nonlocal phenomena. By judiciously breaking and tailoring relevant symmetries in the constituent meta-units, we can independently engineer the amplitude, phase and polarization state of the aperture fields in a pointwise manner, thereby enabling full customization of the radiated fields (see Table S1 in Supplementary Information for comparison with prior arts). The proposed framework admits an almost fully rational design scheme that eschews the cumbersome numerical optimization routines or look up tables required by conventional approaches. Using this concept, we realized several metasurface prototypes with different functionalities, ranging from near-field wavefront shaping to far-field beam forming, all of which were validated through numerical simulations and experimental measurements. In contrast to conventional LWA approaches, which judiciously choose the position and periodicity of scattering elements in order to control the output phase profile (i.e., an aperiodic tiling), our approach uses a fixed periodicity with a spatially varying geometric phase. Future work may explore the combination of both approaches in order to more flexibly create custom aperture fields with dispersion control.

We envision straightforward application of the presented design principles to facilitate arbitrary two-dimensional aperture engineering. The main challenge is the implementation of compact and wide-band wave launchers which can uniformly distribute the input power of a localized feed into a wide aperture. Besides conventional solutions, such as substrate integrated reflectors, one potential alternative is the utilization of multiple independent inputs²¹, which also has the added benefit of enabling fixed-frequency beam scanning in the yz – plane, with the incorporation of phase shifters. It is also worth noting that all the designs discussed in this paper utilize a single guided q-BIC mode. We can augment an LWM with a suite of additional functionalities by leveraging multiple orthogonal q-BIC modes⁴⁶. For instance, it is possible to at least double the number of independent channels in

our proposed MIMO LWM, with just one added mode (along with its time-reversed counterpart). Overall, our results demonstrate the power of q-BICs in a PCB-compatible radiofrequency platform and encourage further investigation of controlled symmetry as an attractive ingredient for engineering advanced microwave and mm-wave wireless devices. The generality and elegance of the symmetry-based principle introduced here also invites exploration into the terahertz regime, in which physics-informed design principles are particularly welcome due to strict technological limitations.

Methods

Numerical Simulations. The band diagrams in Figure 2 were obtained using the eigenfrequency solver in COMSOL Multiphysics (Electromagnetic Waves, Frequency Domain interface). A single meta-unit, consisting of a lossless dielectric substrate sandwiched between two perfect electric conductor (PEC) surfaces, the top one being perforated and both with infinitesimal thickness, is placed between two sets of Floquet periodic boundaries. The bottom side of the simulation domain is terminated by the ground plane, while the top side is implemented as a scattering boundary. Such a setup will occasionally produce spurious eigenmodes that are not supported by the metasurface, but rather, by the simulation domain itself. These modes can be easily identified by their non-physical power densities (e.g. growing intensities away from the surface), and have been rejected from our results.

To perform efficient preliminary confirmation of the functionality of the SIMO and MIMO focusing LWM, we conducted simplified full wave numerical simulations using the frequency domain solver in COMSOL. In the analysis, the LWMs were made infinitely periodic along the transverse (y) direction using the “continuity” boundary condition. The LWM is again implemented as a lossless dielectric slab sandwiched by two PEC sheets, the top one being perforated. The two ends of the LWM were connected to short sections of unperforated PPWG. To excite the surface, the waveguide

corresponding to port 1 is fed by an ideal TEM wave (launched by a uniform wave port), while the other side is terminated by a matched wave port.

To accurately predict the realized gain of the multi-beam LWM antenna, we use ANSYS High Frequency Structure Simulator to analyze the full prototype, consisting of a laterally truncated LWM (with seven identical columns), as well as the realistic feeding networks and RF connectors. In the model, the antenna is built on a lossy dielectric substrate ($h = 1.52$ mm, $\epsilon_r = 3$, $\tan \delta = 0.001$), with conductive copper claddings (thickness 0.018mm, conductivity 5.8×10^7 S/m). The SIW horn arrays were modelled as copper via posts. The radiation efficiency of the antenna was evaluated using the radiation surface integral method.

Device Fabrication. All three designs presented in this article were fabricated in house using LPKF prototyping systems (Protomat S104, Protolaser S4, Contac S4), on Rogers RO3003 substrates with thickness of 1.52mm, dielectric constant $\epsilon_r = 3$, and loss factor $\tan \delta = 0.001$.

For each sample, seven identical columns of meta-units were etched onto the substrate, repeated along the transverse direction to form a quasi-1D LWM. Ideally, a sample should contain as many columns as permitted by the device footprint, which would serve to suppress the guided wave components with non-zero transverse wavevectors, thereby minimizing the edge effects associated with the lateral truncation. However, the required SIW wave launcher would be substantially more complex due to the expanded aperture. In our simulations and experiments, we observed that seven columns provided a good compromise between device complexity and performance.

The SIW horn array launchers were fed by flange-mount SMA connectors (Amphenol P/N: 2933-6004), whose pins have been trimmed to a length of 1.52mm to match the substrate thickness.

Measurement. The Fresnel-zone field distributions of the SIMO and MIMO focusing LWMs were measured using a near-field planar scanner from NSI-MI Technologies. The near-field radiation

profiles of the prototypes were sampled with a K-band open-ended waveguide probe placed 5cm away from the metasurface aperture. Then, the fields were projected to various planes parallel to the measurement plane, yielding the field intensity holograms reported in Figure 5 and Figure 6. The far-field radiation pattern of the multi-beam LWM antenna was obtained using the same set up. Then, its gain was evaluated by direct comparison with a K-band standard gain horn antenna (Pasternack PE-9852/2F-15, 15dBi gain) in a separate far-field measurement setup.

During measurement, the input port of the prototype is connected to a vector network analyzer, while the opposite port is terminated by a 50Ω matched load.

Acknowledgements. This work was supported by the CHARM program, the Air Force Office of Scientific Research and the Simons Foundation.

Data Availability Statement. Authors can confirm that all relevant data are included in the paper and/or its supplementary information files, and raw data are available upon reasonable request from the corresponding author.

Code Availability Statement. The codes used to produce these results are available upon reasonable request from the corresponding author.

Competing Interests. The authors declare no competing interests.

References

1. Jackson, D. R. & Oliner, A. A. Leaky-Wave Antennas. 325–367 (2008).
2. Gupta, S., Abielmona, S. & Caloz, C. Microwave Analog Real-Time Spectrum Analyzer (RTSA) Based on the Spectral–Spatial Decomposition Property of Leaky-Wave Structures. *IEEE Trans. Microw. Theory Tech.* **57**, 2989–2999 (2009).
3. Vázquez, C., García, C., Álvarez, Y., Ver-Hoeye, S. & Las-Heras, F. Near Field Characterization of an Imaging System Based on a Frequency Scanning Antenna Array. *IEEE Trans. Antennas Propag.* **61**, 2874–2879 (2013).
4. Ettorre, M., Sauleau, R., Le Coq, L. & Bodereau, F. Single-Folded Leaky-Wave Antennas for Automotive Radars at 77 GHz. *IEEE Antennas Wirel. Propag. Lett.* **9**, 859–862 (2010).
5. Yang, S.-T. & Ling, H. Application of a Microstrip Leaky Wave Antenna for Range–Azimuth Tracking of Humans. *IEEE Geosci. Remote Sens. Lett.* **10**, 1384–1388 (2013).
6. Pfeiffer, C. & Grbic, A. Metamaterial Huygens' surfaces: Tailoring wave fronts with reflectionless sheets. *Phys. Rev. Lett.* **110**, 1–5 (2013).
7. Selvanayagam, M. & Eleftheriades, G. V. Discontinuous electromagnetic fields using orthogonal electric and magnetic currents for wavefront manipulation. *Opt. Express* **21**, 14409 (2013).
8. Achouri, K., Salem, M. A. & Caloz, C. General Metasurface Synthesis Based on Susceptibility Tensors. *IEEE Trans. Antennas Propag.* **63**, 2977–2991 (2015).
9. Tretyakov, S. A. Metasurfaces for general transformations of electromagnetic fields. *Philos. Trans. R. Soc. Math. Phys. Eng. Sci.* **373**, (2015).
10. Epstein, A. & Eleftheriades, G. V. Arbitrary power-conserving field transformations with passive lossless omega-type bianisotropic metasurfaces. *IEEE Trans. Antennas Propag.* (2016) doi:10.1109/TAP.2016.2588495.

11. Fong, B. H., Colburn, J. S., Ottusch, J. J., Visher, J. L. & Sievenpiper, D. F. Scalar and Tensor Holographic Artificial Impedance Surfaces. *IEEE Trans. Antennas Propag.* **58**, 3212–3221 (2010).
12. Patel, A. M. & Grbic, A. A Printed Leaky-Wave Antenna Based on a Sinusoidally-Modulated Reactance Surface. *IEEE Trans. Antennas Propag.* **59**, 2087–2096 (2011).
13. Minatti, G., Caminita, F., Martini, E., Sabbadini, M. & Maci, S. Synthesis of Modulated-Metasurface Antennas With Amplitude, Phase, and Polarization Control. *IEEE Trans. Antennas Propag.* **64**, 3907–3919 (2016).
14. Faenzi, M. *et al.* Metasurface Antennas: New Models, Applications and Realizations. *Sci. Rep.* **9**, 10178 (2019).
15. Abdo-Sánchez, E., Chen, M., Epstein, A. & Eleftheriades, G. V. A Leaky-Wave Antenna With Controlled Radiation Using a Bianisotropic Huygens' Metasurface. *IEEE Trans. Antennas Propag.* **67**, 108–120 (2019).
16. Kim, M. & Eleftheriades, G. V. Guided-Wave-Excited Binary Huygens' Metasurfaces for Dynamic Radiated-Beam Shaping with Independent Gain and Scan-Angle Control. *Phys. Rev. Appl.* **15**, 1 (2021).
17. Ataloglou, V. G. *et al.* Static and Reconfigurable Huygens' Metasurfaces: Use in Antenna Beamforming and Beam Steering. *IEEE Antennas Propag. Mag.* **64**, 73–84 (2022).
18. Tierney, B. B. & Grbic, A. Controlling Leaky Waves With 1-D Cascaded Metasurfaces. *IEEE Trans. Antennas Propag.* **66**, 2143–2146 (2018).
19. Smith, D. R., Yurduseven, O., Mancera, L. P., Bowen, P. & Kundtz, N. B. Analysis of a Waveguide-Fed Metasurface Antenna. *Phys. Rev. Appl.* **8**, 054048 (2017).
20. Boyarsky, M., Imani, M. F. & Smith, D. R. Grating lobe suppression in metasurface antenna arrays with a waveguide feed layer. *Opt. Express* **28**, 23991 (2020).
21. Boyarsky, M., Sleasman, T., Imani, M. F., Gollub, J. N. & Smith, D. R. Electronically Steered Nyquist Metasurface Antenna. *Sci. Rep.* **11**, (2021).

22. Hsu, C. W., Zhen, B., Stone, A. D., Joannopoulos, J. D. & Soljacic, M. Bound states in the continuum. *Nat. Rev. Mater.* **1**, (2016).

23. Koshelev, K., Lepeshov, S., Liu, M., Bogdanov, A. & Kivshar, Y. Asymmetric Metasurfaces with High- Q Resonances Governed by Bound States in the Continuum. *Phys. Rev. Lett.* **121**, 193903 (2018).

24. Overvig, A. C., Shrestha, S. & Yu, N. Dimerized high contrast gratings. *Nanophotonics* **7**, 1157–1168 (2018).

25. Overvig, A. C., Malek, S. C., Carter, M. J., Shrestha, S. & Yu, N. Selection rules for quasibound states in the continuum. *Phys. Rev. B* **102**, 1–28 (2020).

26. Overvig, A., Yu, N. & Alù, A. Chiral Quasi-Bound States in the Continuum. *Phys. Rev. Lett.* **126**, 73001 (2021).

27. Overvig, A. C., Mann, S. A. & Alù, A. Thermal Metasurfaces: Complete Emission Control by Combining Local and Nonlocal Light-Matter Interactions. *Phys. Rev. X* **11**, 21050 (2021).

28. Huang, H. *et al.* Leaky-wave metasurfaces for integrated photonics. **40**.

29. Renzo, M. D. *et al.* Smart radio environments empowered by reconfigurable AI meta-surfaces: an idea whose time has come. *EURASIP J. Wirel. Commun. Netw.* **2019**, 129 (2019).

30. Di Renzo, M., Danufane, F. H. & Tretyakov, S. Communication Models for Reconfigurable Intelligent Surfaces: From Surface Electromagnetics to Wireless Networks Optimization. *Proc. IEEE* **110**, 1164–1209 (2022).

31. Abujetas, D. R., van Hoof, N., ter Huurne, S., Gómez Rivas, J. & Sánchez-Gil, J. A. Spectral and temporal evidence of robust photonic bound states in the continuum on terahertz metasurfaces. *Optica* **6**, 996 (2019).

32. Rahmeier, J. G. N., Tiukuvaara, V. & Gupta, S. Complex Eigenmodes and Eigenfrequencies in Electromagnetics. *IEEE Trans. Antennas Propag.* **69**, 4644–4656 (2021).

33. Moustafa, L. *et al.* The Phoenix Cell: A New Reflectarray Cell With Large Bandwidth and Rebirth Capabilities. *IEEE Antennas Wirel. Propag. Lett.* **10**, 71–74 (2011).

34. Gonzalez-Ovejero, D. *et al.* Additive Manufactured Metal-Only Modulated Metasurface Antennas. *IEEE Trans. Antennas Propag.* **66**, 6106–6114 (2018).

35. Ettorre, M., Sauleau, R. & Le Coq, L. Multi-Beam Multi-Layer Leaky-Wave SIW Pillbox Antenna for Millimeter-Wave Applications. *IEEE Trans. Antennas Propag.* **59**, 1093–1100 (2011).

36. Gomez-Guillamon Buendia, V. *et al.* Compact Leaky SIW Feeder Offering TEM Parallel Plate Waveguide Launching. *IEEE Access* **7**, 13373–13382 (2019).

37. Ruiz-García, J., Martini, E., Giovampaola, C. D., González-Ovejero, D. & Maci, S. Reflecting Luneburg Lenses. *IEEE Trans. Antennas Propag.* **69**, 3924–3935 (2021).

38. Gómez-Tornero, J. L., Blanco, D., Rajo-Iglesias, E. & Llombart, N. Holographic Surface Leaky-Wave Lenses With Circularly-Polarized Focused Near-Fields—Part I: Concept, Design and Analysis Theory. *IEEE Trans. Antennas Propag.* **61**, 3475–3485 (2013).

39. Huang, C. *et al.* Holographic MIMO Surfaces for 6G Wireless Networks: Opportunities, Challenges, and Trends. *IEEE Wirel. Commun.* **27**, 118–125 (2020).

40. Gonzalez-Ovejero, D., Minatti, G., Chattopadhyay, G. & Maci, S. Multibeam by Metasurface Antennas. *IEEE Trans. Antennas Propag.* **65**, 2923–2930 (2017).

41. Kandil, S. M., Bisharat, D. J. & Sievenpiper, D. F. Chiral Surface Wave Propagation with Anomalous Spin-Momentum Locking. *ACS Photonics* **acsphotonics.2c00491** (2022) doi:10.1021/acsphotonics.2c00491.

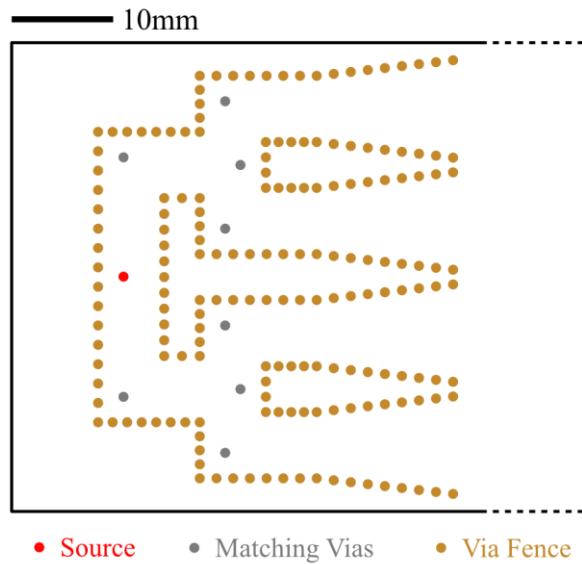
42. Xu, G., Eleftheriades, G. V. & Hum, S. V. Wide-Angle Beam-Steering and Adaptive Impedance Matching With Reconfigurable Nonlocal Leaky-Wave Antenna. *IEEE Open J. Antennas Propag.* **3**, 1141–1153 (2022).

43. Lee, H., Choi, J. H., Wu, C.-T. M. & Itoh, T. A Compact Single Radiator CRLH-Inspired Circularly Polarized Leaky-Wave Antenna Based on Substrate-Integrated Waveguide. *IEEE Trans. Antennas Propag.* **63**, 4566–4572 (2015).

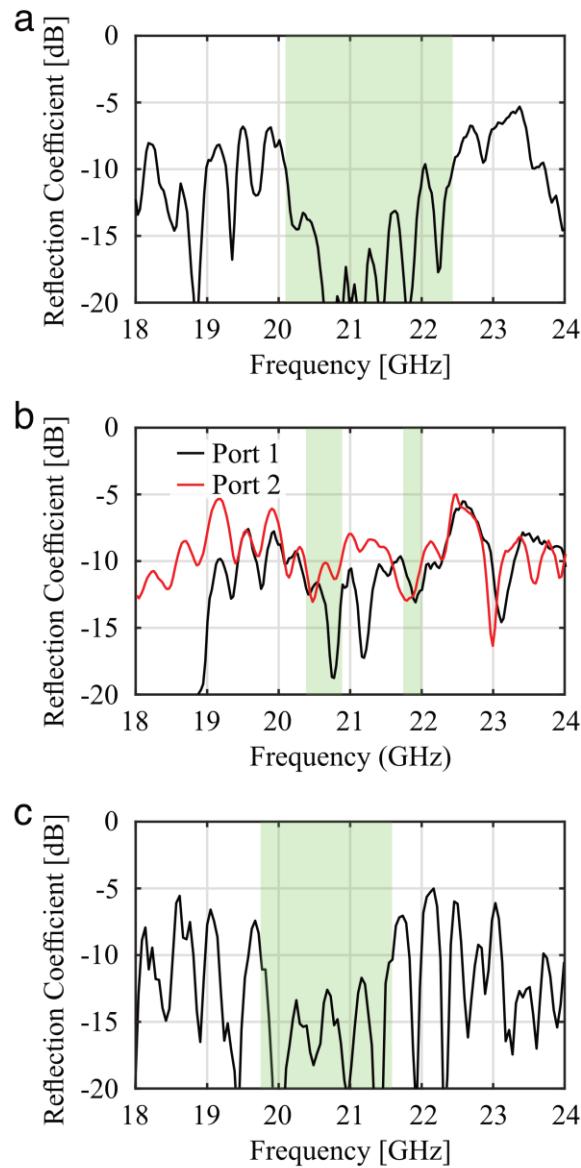
44. Minatti, G., Martini, E. & Maci, S. Efficiency of Metasurface Antennas. *IEEE Trans. Antennas Propag.* **65**, 1532–1541 (2017).

45. Sadrieva, Z., Frizyuk, K., Petrov, M., Kivshar, Y. & Bogdanov, A. Multipolar origin of bound states in the continuum. *Phys. Rev. B* **100**, 1–12 (2019).
46. Overvig, A. C., Malek, S. C. & Yu, N. Multifunctional Nonlocal Metasurfaces. *Phys. Rev. Lett.* **125**, 017402 (2020).

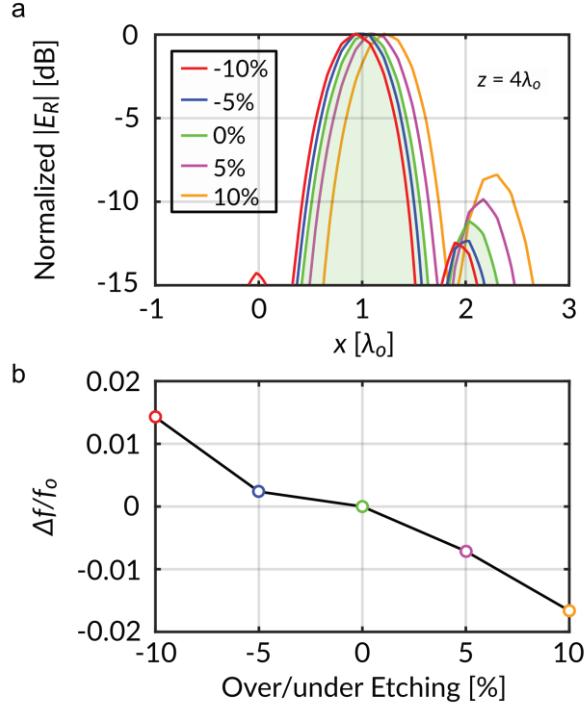
Supplementary Material



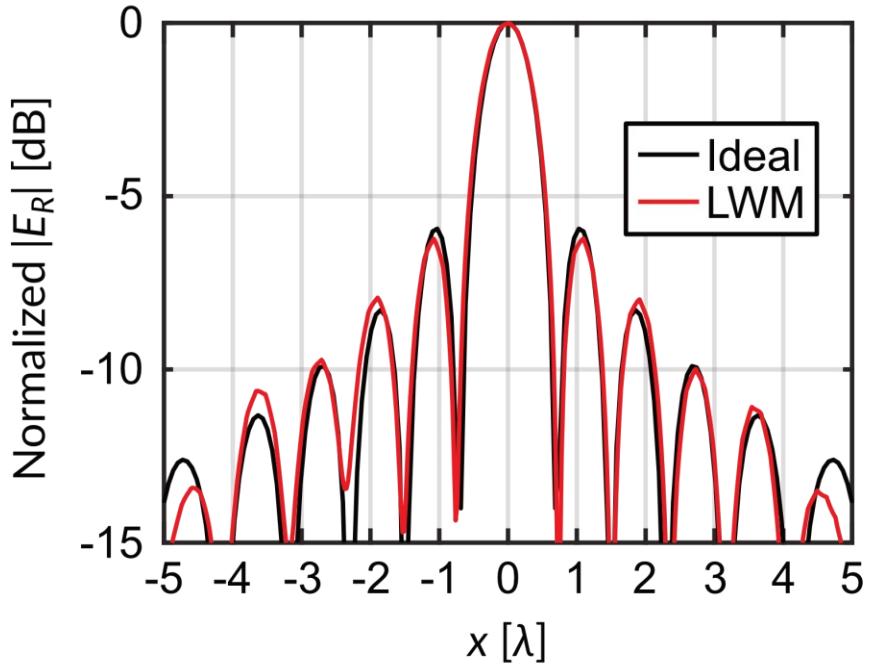
Supplementary Figure S1: Layout of the substrate integrated waveguide launcher employed in the LWM prototypes.
The vias have 0.5mm radii and 1.9mm maximum pitch, which is smaller than 1/4 of the wavelength inside the dielectric substrate (at a frequency of 20.5GHz). The locations of the matching vias and the source have been optimized to maximize the bandwidth of the launcher (in the absence of the LWM).



Supplementary Figure S2: Measured input reflection coefficients of the LWM prototypes. Results for (a) the SIMO LWM, (b) MIMO LWM, and the (c) multi-beam LWM antenna. The SIMO and multi-beam LWM exhibited around 10% -10dB fractional bandwidth (marked by the green shaded region). In comparison, the MIMO prototype had slightly reduced bandwidth due to the increased (but still acceptable) reflection at port 2.



Supplementary Figure S3: Study on the robustness of the LWM functionality to etching tolerances during fabrication. As an illustrative example, the SIMO LWM prototype examined in the main text is studied here. The normalized magnitude of the RCP component in the designated RCP focal plane $z = 4\lambda_o$ is plotted in panel (a) for various degree of over- and under-etching. The percentage value indicates the size deviation of the open slots from their intended dimensions. The focal spots drift slightly from the intended position as we increase the amount of etching error, which can be compensated by slightly detuning the operating frequency. In panel (b), we plot the frequency deviation required to maintain the focal spot at its intended location ($x = \lambda_o$), for various degree of over- and under-etching. It is evident that $\pm 10\%$ etching error will shift the optimal operating frequency only by approximately 1.5%, meaning the proposed LWM is highly robust against this type of manufacturing defect (which is the most common in practice).



Supplementary Figure S4: Comparison of the focusing resolution of a typical LWM design with theoretical expectations from a tapered aperture. The red curve depicts the electric field intensity in the focal plane ($NA = 0.78$, $f = 20.55$ GHz) predicted by theory (Fourier optics), assuming a continuous aperture field distribution given by equation (5b) in the main text. The black curve corresponds to full wave simulation result of an LWM prototype (untruncated in the lateral direction, obtained using COMSOL) designed to synthesize the same aperture. The two sets of results agree strongly, confirming the realizable focusing power of the q-BIC-based antenna.

Representative Work	Architecture	Capabilities and Key Advantages	Disadvantages
[11], [13]	Single-layered LWM with quasi-periodically modulated tensorial electric impedance	Arbitrary far-field beam-shaping with polarization and bandwidth control.	Requires multi-scale numerical optimization. Cannot precisely control the near field.
[20],[21]	Single-layered LWM consisting of leaky waveguides loaded with tunable meta-atoms	Reconfigurable far-field radiation patterns. Simple design framework facilitated by sparsely spaced meta-atoms.	No control over phase and polarization. Limited angular range and radiation efficiency. Cannot precisely control the near field.
[6], [10]	Multi-layered LWM with locally engineered electric and magnetic susceptibilities	Complete near-field and far-field control with high precision.	Requires multi-layered meta-atoms which are difficult to design and implement.
This work	Single-layered LWM supporting q-BIC	Complete and arbitrary near-field and far-field shaping of polarization, wavefront shape, with four degrees of freedom per unit cell, within a simple, rationally-designed analytical framework.	Possible limitations over the angular range and overall radiation efficiency.

Supplementary Table S1: Comparison of the proposed LWM with selected prior art.