

## Research paper

# A novel higher-order finite element framework for the process modeling of material extrusion additive manufacturing

Manish H. Nagaraj<sup>1</sup>, Marianna Maiaru<sup>\*,2</sup>

Department of Mechanical Engineering, University of Massachusetts Lowell, MA 01854, United States

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## ABSTRACT

Material extrusion additive manufacturing enables the rapid fabrication of complex structures for a wide range of applications, including within the aerospace and healthcare sectors. Optimizing the performance of additively manufactured polymer structures depends on the ability to predict residual stress induced by the sequential solidification of the extruded layers. Self-equilibrated residual stresses are influenced by the thermal history of the part during the manufacturing process. This work introduces a novel numerical framework for the process modeling of material extrusion additive manufacturing. The numerical modeling is based on higher-order finite elements derived from the Carrera Unified Formulation (CUF), which enables accurate prediction of the stress field while reducing the associated computational overheads. Element activation is adopted to model the evolving structure during material extrusion and deposition. Heat exchange mechanisms such as conduction (filament/filament, filament/build platform), convection, and radiation are included in the model. A transient thermal analysis is performed in this new framework to predict the temperature distribution within the part during its fabrication. Multiple numerical assessments are presented for the material extrusion additive manufacturing of parts ranging in size from 30 mm to over 1500 mm. The predicted thermal profiles are in excellent agreement with reference experimental observations, thereby validating the proposed numerical framework and demonstrating its capability to model the printing process accurately. Results from this work are a milestone toward optimizing additively manufactured polymer parts.

## 1. Introduction

Additive Manufacturing (AM) is an emerging processing technology that has gained significant prominence over the past two decades for its capability in fabricating complex parts whose geometries are beyond that of conventional manufacturing techniques [1]. Material extrusion additive manufacturing [2], commonly referred to as Fused Filament Fabrication (FFF), is one of the most popular forms of AM wherein a molten thermoplastic filament is extruded through a moving nozzle and deposited along a predefined path, thereby creating the required geometry. Because of its capabilities, the FFF processing technique has been adopted for a diverse range of applications within the automotive, aerospace, and medical device industries [3].

FFF involves high-temperature gradients within the printed component as it undergoes rapid heating due to the deposition of the semi-molten material and subsequently cools down via heat transfer with adjacent layers and the environment [4]. Localized regions in the vicinity of the deposition zone may also experience various levels of reheating due to the heat supplied by the deposition of the semi-molten

material. The temperature gradients resulting from repetitive heating and cooling can lead to the development of residual stresses within the manufactured component, which impacts both its dimensional accuracy as well as mechanical performance [5–8]. Processing conditions direct the evolution of material properties in polymer-based material systems [9–15], and can subsequently influence the mechanical response of the fabricated component [16–18]. In the case of FFF, the changes in temperature during the heating and cooling phases influences the crystalline morphology (microstructure) of the thermoplastic material, which significantly affects its mechanical properties [19,20]. Length and time scales involved in the material extrusion process can also significantly impact the final print quality. This is seen in large-scale additive manufacturing processes, such as Big Area Additive Manufacturing (BAAM), where the thermal mass of the printed structure is orders of magnitude larger than FFF processes [21]. The associated heat transfer and thermal gradients have an impact on the interlayer bond strength, and thermal stresses can often lead to delamination and warping [22,23]. BAAM structures are also prone to slumping,

\* Corresponding author.

E-mail addresses: [manish\\_nagaraj@uml.edu](mailto:manish_nagaraj@uml.edu) (M.H. Nagaraj), [marianna\\_maiaru@uml.edu](mailto:marianna_maiaru@uml.edu) (M. Maiaru).

<sup>1</sup> Postdoctoral Research Associate.

<sup>2</sup> Associate Professor.

i.e. collapsing under their self-weight, since they require long time periods to cool down and attain sufficient structural stiffness [24].

The temperature distribution within the printed part during its processing therefore drives its geometrical accuracy and mechanical performance. The thermal profile of a printed component is a function of process parameters, such as filament extrusion temperature and deposition path, print speed, and the ambient environmental state [25, 26]. These process parameters can be optimized to induce thermal profiles with minimal variations to limit residual stresses and, in turn, ensure optimal print quality and mechanical performance over the component's service life. Optimizing FFF process parameters through trial-error experimental approaches is inefficient in terms of cost and lead times due to the large number of involved parameters [27,28]. Therefore, virtual testing methodologies are becoming the preferred approach for process optimization [29,30].

Costa et al. investigated the heat transfer mechanisms relevant to FFF to develop guidelines for numerical modeling [4]. Some early 3D models based on the Finite Element Method (FEM) for process simulation were proposed by Zhang and Chou [31,32]. Considering the importance of accurately predicting the thermal profile during the printing process, several numerical approaches have been proposed in the literature to model heat transfer during FFF process modeling [21, 22,33–39]. In recent years, 3D-FE models have also been developed to investigate the influence of FFF thermal state on residual stress development and part distortion [5,6,40]. However, traditional physics-based numerical techniques to model the FFF process often incur high computational costs due to the need to model each deposition layer, limiting the capability to establish digital twins [35,41]. The significant limitations of traditional FE approaches become even more relevant for large-scale structures 3D-printed via Big Area Additive Manufacturing (BAAM), which requires the deposition of hundreds of layers [24,42, 43]. Recent investigations have proposed alternative numerical models for FFF simulation to reduce computational overheads. Owens et al. proposed a scalable 2D finite volume model to simulate thermal histories for FFF and BAAM processes rapidly [44]. Roy and Wodo recently developed a data-driven surrogate model for the thermal modeling of AM processes [45].

This work establishes a novel and computationally efficient numerical framework to model material extrusion-based additive manufacturing processes, which can be used to optimize process parameters for FFF. The computational model is based on higher-order finite elements and is developed using the Carrera Unified Formulation (CUF) [46]. CUF is a hierarchical mathematical framework capable of deriving structural theories of any polynomial order which, combined with 1D and 2D finite elements, leads to a 3D modeling approach whose accuracy is comparable to that of traditional 3D-FE models at significantly reduced computational cost [47]. CUF models have been successfully employed in various applications such as contact modeling [48], progressive damage and impact analysis of composite structures [49–51], and the micromechanical modeling and analysis of fiber-reinforced polymer composites [52,53]. CUF models have also been successfully combined with the global-local technique for computationally efficient nonlinear structural analysis [54–56]; however, its potential has never been explored for 3D printing process modeling. The present work proposes a CUF-based numerical framework where Lagrange polynomial expansions are implemented to model the FFF and BAAM processes and to predict the evolving thermal profile of the 3D-printed part.

The organization of this article is as follows: Section 2 describes the numerical modeling approach for the process modeling of material extrusion additive manufacturing. A series of numerical assessments are presented in Section 3 as validation cases compared to experimental data, and the main conclusions are summarized in Section 4.

## 2. Computational methods

This section provides an overview of the higher-order finite element approach used in the present work, and the modeling techniques adopted for AM simulation and thermal analysis.

### 2.1. Higher-order structural modeling

Structural modeling in the proposed numerical framework is based on higher-order structural theories derived using the Carrera Unified Formulation and implemented using the Finite Element Method [46]. In this approach, additional 2D interpolation terms – known as Expansion functions  $F_\tau$  – are employed to improve the kinematics of 1D finite elements (B2 and B3 beam elements with 2 and 3 nodes, respectively), respectively, as shown in Fig. 1, and are defined over the 1D element cross-section. This mathematical representation results in a 3D description of the displacement field, leading to numerical solutions comparable to 3D-FE models in accuracy but with significantly reduced computational effort [47]. A brief overview of 1D-CUF and its extension to model time-dependent property evolutions for 3D printing is presented hereinafter.

Considering the 1D-CUF model shown in Fig. 1, the displacement field  $\mathbf{u}$  is defined as

$$\mathbf{u} = F_\tau(x, z)\mathbf{u}_\tau(y), \quad \tau = 1, 2, \dots, M \quad (1)$$

where  $M$  is the number of terms within the expansion function  $F_\tau$  and  $\mathbf{u}_\tau$  represents the generalized displacements. Expansion functions based on Lagrange polynomials are used in the present work, and are implemented in the form of 2D quadrilateral elements as shown in Fig. 1 (L4 and L9 section elements with 4 and 9 nodes, respectively). This allows for the explicit modeling of the beam cross-section, and results in the Component-Wise modeling approach [57,58].

#### Finite element formulation

The stress and strain fields are defined as

$$\begin{aligned} \boldsymbol{\sigma} &= \{\sigma_{xx}, \sigma_{yy}, \sigma_{zz}, \sigma_{xy}, \sigma_{xz}, \sigma_{yz}\} \\ \boldsymbol{\epsilon} &= \{\epsilon_{xx}, \epsilon_{yy}, \epsilon_{zz}, \epsilon_{xy}, \epsilon_{xz}, \epsilon_{yz}\} \end{aligned} \quad (2)$$

The linear displacement-strain relationship is given by

$$\boldsymbol{\epsilon}(t) = \mathbf{D}\mathbf{u}(t) \quad (3)$$

where  $(t)$  indicates a dependency on time due to the printing process. The differentiation operator  $\mathbf{D}$  is defined as

$$\mathbf{D} = \begin{bmatrix} \frac{\partial}{\partial x} & 0 & 0 \\ 0 & \frac{\partial}{\partial y} & 0 \\ 0 & 0 & \frac{\partial}{\partial z} \\ \frac{\partial}{\partial y} & \frac{\partial}{\partial x} & 0 \\ \frac{\partial}{\partial z} & 0 & \frac{\partial}{\partial x} \\ 0 & \frac{\partial}{\partial z} & \frac{\partial}{\partial y} \end{bmatrix}$$

The constitutive relation is

$$\boldsymbol{\sigma}(t) = \mathbf{C}(t)\boldsymbol{\epsilon}(t) \quad (4)$$

where the material stiffness tensor is denoted by the  $6 \times 6$   $\mathbf{C}$  matrix, and evolves as a function of time due to changes in the material properties during the processing phase. Defining the displacement field in terms of the finite element shape functions  $N_i(y)$  and the cross-sectional expansion functions  $F_\tau(x, z)$  leads to the following 3D form

$$\mathbf{u}(x, y, z) = F_\tau(x, z)N_i(y)\mathbf{u}_{\tau i} \quad (5)$$

where  $i$  and  $\tau$  are nodal indices for the 1D finite element and 2D sectional element, respectively. According to the principle of virtual work

$$\delta L_{int} = \delta L_{ext} \quad (6)$$

where  $\delta L_{int}$  is the virtual variation of the internal strain energy and is defined as

$$\delta L_{int} = \int_V \delta \boldsymbol{\epsilon}^T : \boldsymbol{\sigma} \quad (7)$$

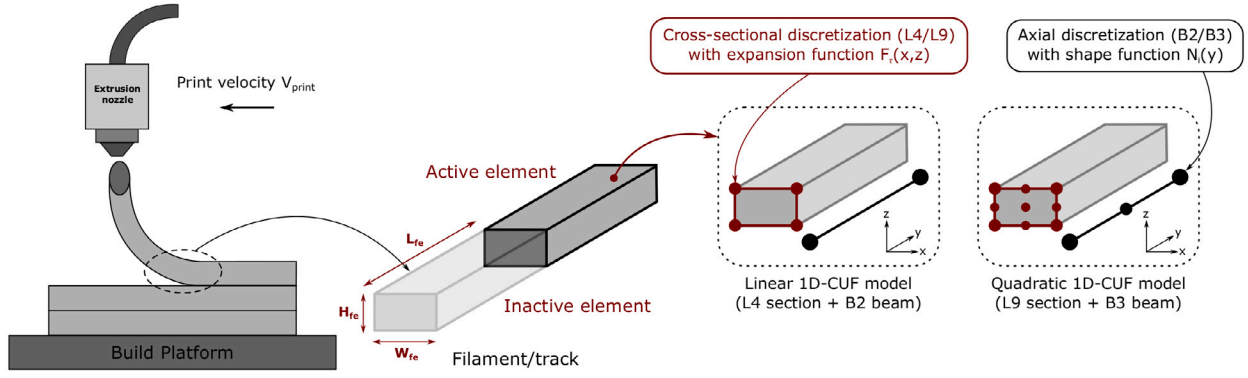


Fig. 1. 1D-CUF modeling of the deposited filament track for additive manufacturing simulation.

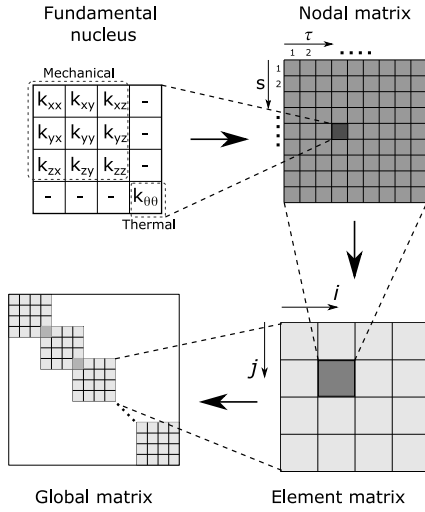


Fig. 2. Assembly of global matrices using fundamental nuclei in CUF.

Combining Eqs. (4), (5) and (7), Eq. (6) can be written as

$$\delta L_{int} = \delta \mathbf{u}_{sj}^T \mathbf{k}_{ij\tau s} \mathbf{u}_{\tau i} \quad (8)$$

where  $\mathbf{k}_{ij\tau s}$  is

$$\mathbf{k}_{ij\tau s} = \int_A \int_V \mathbf{D}^T(N_i(y)F_\tau(x,z))\mathbf{C}\mathbf{D}(N_j(y)F_s(x,z)) dA dl \quad (9)$$

Eq. (9) represents a  $3 \times 3$  matrix, termed the Fundamental Nucleus (FN), whose definition remains invariant with respect to the choice of finite element and expansion function used to derive the structural theory. Assembling the structural FN over the nodal indices  $\{i, j, \tau, s\}$  results in the element stiffness matrix, which can subsequently be assembled to develop the global stiffness matrix as seen schematically in Fig. 2.

## 2.2. Process simulation with element activation

The evolution of the printed domain that occurs due to continuous material deposition in FFF needs to be modeled to represent the additive manufacturing process accurately. A popular approach to model the evolving structural domain is via the element activation strategy, e.g., Ref. [5], which is adopted in this work. Element activation is combined with a voxelization technique, wherein the physical structure is modeled using cuboidal finite elements [59], as shown in Fig. 3 for the case of an 'L-shaped' structural domain. The filament cross-section is elliptical in reality, but is commonly simplified to a rectangular cross-section in computational models. This allows for a discretization

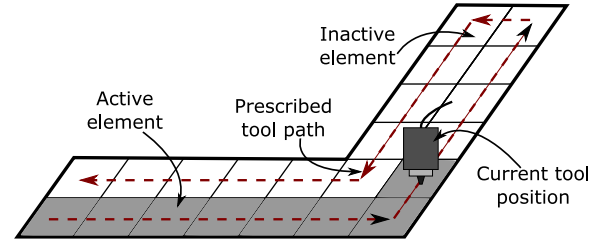


Fig. 3. Element activation strategy to simulate the FFF deposition process.

strategy based on the use of a single voxelized cuboid finite element to represent the filament cross-section, thereby avoiding the computational expense of modeling a true elliptical geometry [5,6,35]. A study on relevant heat transfer mechanisms for FFF by Costa et al. compares the influence of the considered cross-sectional geometry on the thermal profile during the printing process, and provides justification on the use of a simplified rectangular filament cross-section geometry [4]. In addition, perfect thermal contact is assumed at the filament–filament interface, and is based on the works of Lepoivre et al. which determined a weak influence of thermal contact resistance on the thermal behavior for a considered range of values [36].

In this approach, a finite element model of the entire structure is developed, and each element is initially set to be deactivated, i.e., the element does not transfer thermal or mechanical loads. During the time-based analysis, the tool's current position (extruder) is computed based on input parameters such as print velocity, current time, and the prescribed tool path. The relevant information is obtained from the G-code data associated with the specific printed geometry. Once the current tool position is evaluated, a check is performed to identify the elements through which the tool traverses with respect to its position at the previous time step, and the elements thus identified are activated, i.e., the tool-path is traced along the finite element model, and elements are activated according to the tool traversal between consecutive time-steps. The value of the time increment ( $dt$ ) is determined as the ratio of the length of the individual finite element (in the print direction) and the print velocity, i.e.,  $dt = \frac{L_{fe}}{V_{print}}$  (refer Fig. 1). This ensures that a single finite element is activated within a time increment.

## 2.3. Heat transfer mechanisms

The thermal profile of a component fabricated via FFF depends on the printed part's thermal interactions with the extrusion nozzle, build platform, and the surrounding environment [4]. A schematic view of the relevant heat transfer mechanisms is shown in Fig. 4.

Heating occurs due to the deposition of the molten filament at elevated temperatures, while cooling occurs due to heat loss from the

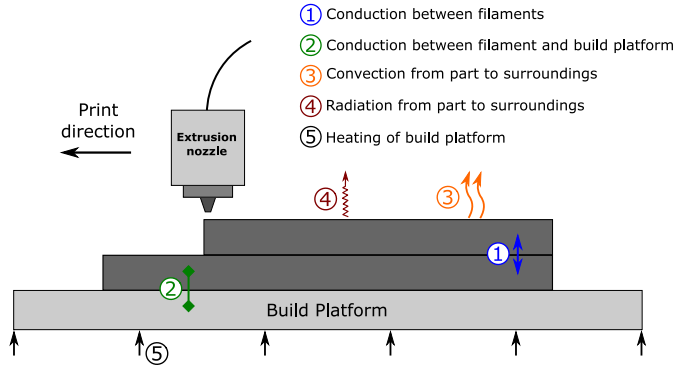


Fig. 4. Heat transfer mechanisms active during the FFF process and modeled within the proposed framework.

external surfaces of the structure to the surroundings via convection and radiation. Heat is transferred within a deposited filament and between consecutive layers via conduction. The part also interacts with the build platform through heat conduction, as shown in Fig. 4. These mechanisms and environmental factors, such as the presence of a heated print chamber or cooling fans, determine the temperature distribution within the printed domain. In the present work, all the aforementioned thermal mechanisms are accounted for during the FFF simulation by updating the numerical model's thermally available volume and surface area, which evolve according to the set of activated elements within a time step. A simple two-element model is schematically shown in Fig. 5 to illustrate the heat exchange mechanisms modeled.

In Fig. 5, a single element is initially active at time  $t_1$ . Therefore, cooling occurs via convection and radiation from the side and top faces, whereas conduction is responsible for interactions between the element and the build platform via the bottom face. The adjacent element is activated in a subsequent time step, time  $t_2$ . The shared face between the two elements, earlier an external surface area, is now interior to the structure and, therefore, no longer available for convection and radiation. Conduction through this shared face is responsible for the thermal interaction between the two elements in the current configuration. The remaining element faces exposed to the environment allow convective and radiative heat loss while the bottom faces conduct heat with the build platform, as shown in Fig. 5 at time  $t_2$ .

## 2.4. Transient thermal analysis

The temperature distribution within the printed domain evolves with time as molten filament is continuously deposited. An accurate evaluation of the temperature gradients and thermal state during printing requires the quantification of the relevant heat transfer mechanisms depicted in Fig. 4. A transient thermal analysis is performed to determine the thermal state within the printed domain [5,6]

$$\rho c_p \frac{\delta T}{\delta t} = \nabla \cdot (\kappa \nabla T) \quad (10)$$

where  $\rho$ ,  $c_p$  and  $\kappa$  represent the density, specific heat capacity, and thermal conductivity of the deposited filament, respectively, and  $T$  is the temperature. The temperature of newly deposited material at time  $t$  is specified as an initial condition

$$T(\mathbf{x}, t) = T_{\text{deposition}}, \quad \mathbf{x} \in \Omega_{\text{deposition}} \quad (11)$$

where  $T_{\text{deposition}}$  is the deposition temperature and  $\Omega_{\text{deposition}}$  is the domain of the deposited material. The build platform temperature is specified as a boundary condition

$$T(\mathbf{x}) = T_{\text{platform}}, \quad \mathbf{x} \in \Omega_{\text{platform}} \quad (12)$$

where  $T_{\text{platform}}$  is the temperature of the build platform  $\Omega_{\text{platform}}$ . The boundary conditions of the deposited domain are defined as

$$\kappa \frac{\delta T}{\delta \mathbf{n}} + q_c + q_r = 0, \quad \mathbf{x} \in S(t) \quad (13)$$

where  $S(t)$  is the evolving external surface of the deposited domain (see Fig. 5) with  $\mathbf{n}$  denoting its outward normal vector. The convective heat flux  $q_c$  and radiative heat flux  $q_r$  are evaluated as follows

$$q_c = h(T - T_{\text{ambient}}) \quad (14)$$

$$q_r = \sigma \epsilon (T^4 - T_{\text{ambient}}^4) \quad (15)$$

where  $h$  and  $\epsilon$  are the convective heat transfer coefficient and emissivity of the material, respectively.  $\sigma$  is the Stefan–Boltzmann constant, and  $T_{\text{ambient}}$  is the ambient temperature.

The numerical solution of the transient thermal problem requires the discrete form of the heat transfer equation as follows

$$\mathbf{M}\dot{\mathbf{T}} + \mathbf{K}\mathbf{T} = \mathbf{F} \quad (16)$$

where  $\mathbf{M}$  is the thermal capacitance matrix, and  $\mathbf{F}$  denotes the thermal loads.  $\mathbf{K}$  represents the thermal stiffness matrix and includes conductive, convective, and radiative contributions [60]. Applying the Backward Euler approach to Eq. (16)

$$\mathbf{M} \left( \frac{\mathbf{T}_{n+1} - \mathbf{T}_n}{\Delta t} \right) + \mathbf{K}\mathbf{T}_{n+1} = \mathbf{F}_{n+1} \quad (17)$$

Rearranging the above leads to

$$\left( \frac{\mathbf{M}}{\Delta t} + \mathbf{K} \right) \mathbf{T}_{n+1} = \left( \frac{\mathbf{M}}{\Delta t} \right) \mathbf{T}_n + \mathbf{F}_{n+1} \quad (18)$$

Eq. (18) is solved to obtain the evolving temperature field within the extant structure during the printing process. Within the CUF modeling approach (see Section 2.1), the fundamental nuclei, required for the assembly of  $\mathbf{M}$  and  $\mathbf{K}$  matrices, are respectively as follows [46,61]

$$\mathbf{m}_{ij\tau s} = \rho \int_I \int_A N_i(y) F_\tau(x, z) \cdot N_j(y) F_s(x, z) \, dA \, dI \quad (19)$$

$$\mathbf{k}_{ij\tau s} = \kappa \int_I \int_A \nabla^T (N_i(y) F_\tau(x, z)) \cdot \nabla (N_j(y) F_s(x, z)) \, dA \, dI \quad (20)$$

## 3. Results and discussion

This section presents a set of experimentally validated numerical studies to evaluate the performance of the proposed framework for AM simulation. Results are presented in terms of evolving temperature fields of the printed component under the influence of FFF and BAAM processing conditions. The simulations were performed (in serial) on an Intel(R) Core(TM) i7-10700 2.9 GHz Desktop Workstation with 32 GB RAM, and the analysis time spanned approximately 1–32 min depending on the geometry and model discretization. The computational performance of the proposed approach for AM process modeling, compared to existing numerical methods, is discussed at the end of Section 3.3.

### 3.1. Modeling of a single-filament wall

The numerical assessment considered herein is the FFF process modeling of a printed wall with a single-filament thickness, schematically shown in Fig. 6. The selected case is based on the work of Lepoivre et al. [36], which provides experimental reference data and numerical solutions. The present analysis aims to conduct an initial verification and validation of the proposed numerical framework for FFF process modeling. The thermoplastic filament is composed of Acrylonitrile butadiene styrene (ABS), with a filament thickness ( $dZ$ ) and width ( $dY$ ) of 0.8 mm and 1.25 mm, respectively. The voxelized numerical model, therefore, consists of finite elements of dimensions  $dX \times 1.25 \text{ mm} \times 0.8 \text{ mm}$ , where  $dX$  is the finite element length along the filament direction. The thermal properties of the ABS filament and the build



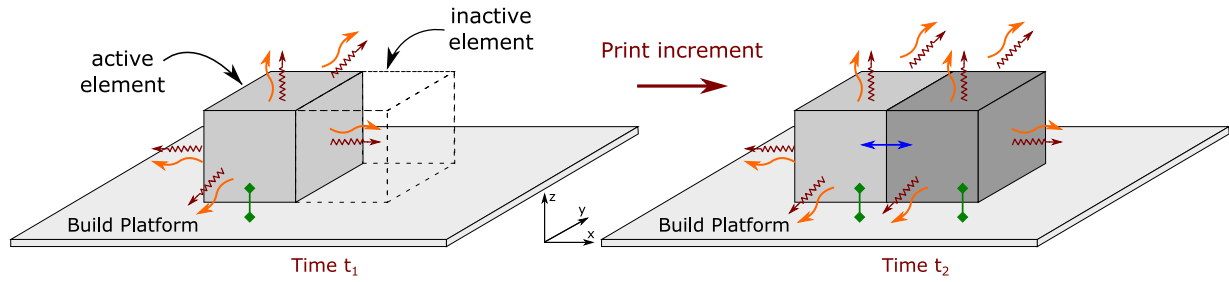


Fig. 5. Evolution of structural domain to implement the heat transfer mechanisms induced by FFF.

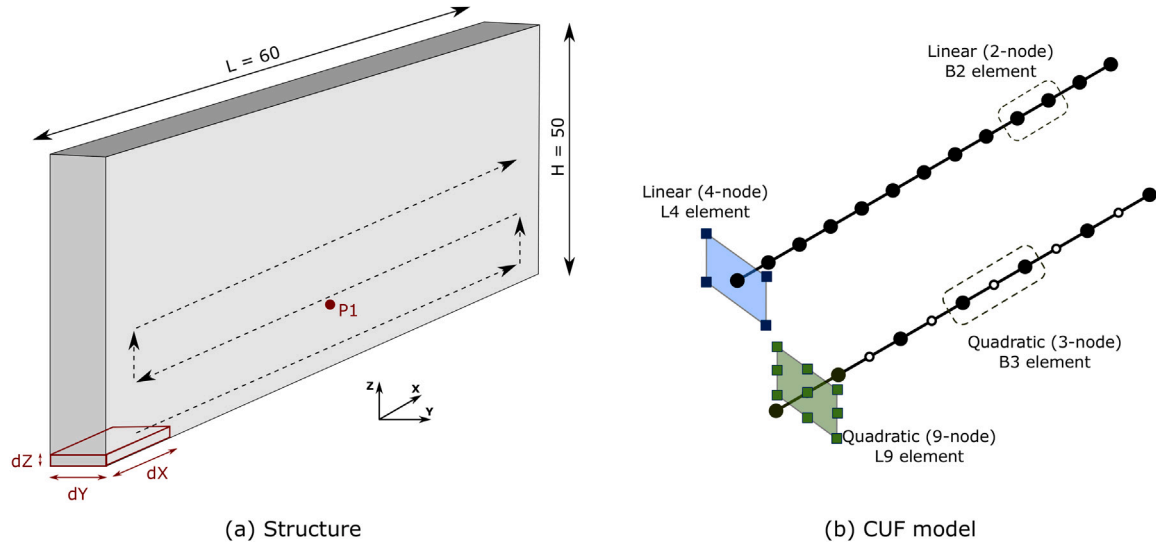


Fig. 6. Schematic representation of (a) the single-filament wall (dimensions in mm). The dashed lines indicate the tool travel path, and the highlighted  $dX \times dY \times dZ$  voxel domain represents an individual finite element, (b) an example of the linear and quadratic discretization used in the numerical analysis (summary of all models in Table 3).

Table 1

Thermal properties of the materials used in the numerical modeling of the single-wall [36].

Property	ABS	PEKK	build platform
Density [ $\text{kg/m}^3$ ]	1050.0	1140.0	2210.0
Thermal conductivity [ $\text{W/m K}$ ]	0.2	0.5	1.4
Specific heat capacity [ $\text{J/kg K}$ ]	2100.0	2200.0	730.0
Emissivity $\epsilon$	0.91	0.94	–
Filament width (dY) [mm]	1.25	2.20	–
Filament thickness (dZ) [mm]	0.80	0.80	–

Table 2

FFF process parameters used in the numerical modeling of the single-wall [36].

Parameter	ABS	PEKK
Extrusion temperature [ $^{\circ}\text{C}$ ]	255.0	356.0
Chamber temperature [ $^{\circ}\text{C}$ ]	95.0	139.0
build platform temperature [ $^{\circ}\text{C}$ ]	100.0	160.0
Convection coefficient [ $\text{W/m}^2 \text{K}$ ]	30.0	30.0
Print velocity [mm/s]	6.741	6.12

platform are listed in Table 1. The process parameters used in the analysis are summarized in Table 2.

A series of linear and quadratic CUF models have been developed by progressively refining the mesh along the filament direction, i.e., decreasing the 1D element length dX as shown in Fig. 6. A single sectional element (with dimensions  $dY \times dZ$ ) is used to represent the filament cross-section. The temperature profile at the midspan of Layer-6, i.e., the point P1 (30, 0, 4.4) (refer to Fig. 6), as predicted by the linear and quadratic CUF models, is plotted in Fig. 7(a) and (b), respectively. Reference experimental measurements and FE-based

Table 3

Summary of CUF models used in the single-wall thermal analysis.

Model	Discretization	Beam length (dX) [mm]	DOF
CUF - Linear 1	12 B2, 61 L4	5.0	1,612
CUF - Linear 2	20 B2, 61 L4	3.0	2,604
CUF - Linear 3	24 B2, 61 L4	2.5	3,100
CUF - Quadratic 1	6 B3, 61 L9	10.0	4,797
CUF - Quadratic 2	10 B3, 61 L9	6.0	7,749
CUF - Quadratic 3	12 B3, 61 L9	5.0	9,225

numerical predictions are also overlaid in the figure for comparison. A summary of the CUF models is provided in Table 3.

The temperature evolution within a single-wall structure printed using high melting-point thermoplastics such as PEKK ( $T_{\text{deposition}} = 356^{\circ}\text{C}$ ) was also experimentally investigated by Lepoivre et al. [36], and has been modeled in this work. This study aims to assess the model performance under high-temperature processing conditions. The PEKK material properties and process parameters are listed in Table 1 and Table 2, respectively. The CUF models used in the previous case (with ABS filament), as listed in Table 3, are retained for the FFF process modeling of the PEKK single-wall. The thermal profile predicted by the linear and quadratic CUF models at the midspan of Layer-6, P1 (30, 0, 4.4), with reference experimental and numerical data overlaid for comparison, is shown in Fig. 8. Numerical results based on the 'Linear-3' and 'Quadratic-3' models (see Table 3) have been omitted for the sake of brevity since they do not lead to a significant improvement in accuracy. The temperature distribution over the PEKK single-wall at various stages of the printing process, as predicted by the 'CUF - Linear 2' model, is shown in Fig. 9.

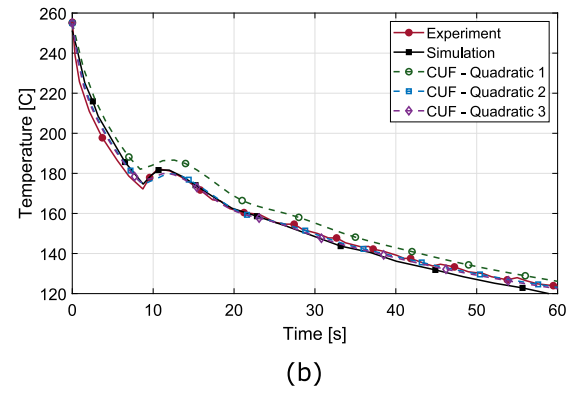
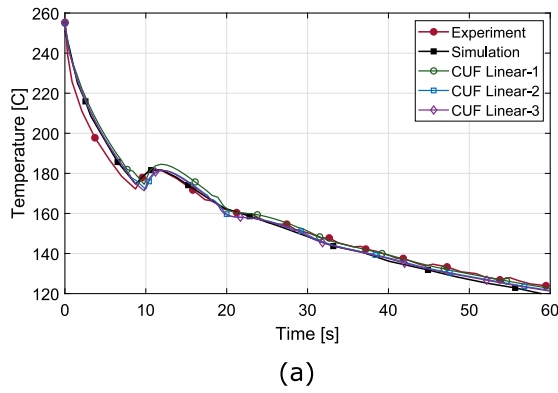


Fig. 7. Thermal profile of the ABS single-filament wall at Point P1 (see Fig. 6) as predicted by (a) the linear CUF models, and (b) the quadratic CUF models (see Table 3 for model details). Reference experimental and 2D-FE numerical data obtained from [36].

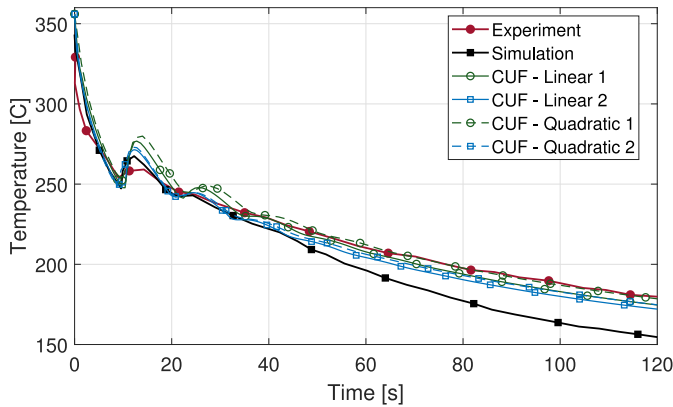


Fig. 8. Thermal profile of the PEKK single-filament wall at point P1 (see Fig. 6) as predicted by the CUF models (see Table 3 for model details). Reference experimental and 2D-FE numerical data obtained from [36].

It is seen from the predicted thermal profiles of the ABS single-wall, plotted in Fig. 7, that the CUF models are in excellent agreement with both experimental measurements and the reference numerical results. The mesh convergence analysis for both linear and quadratic CUF models indicates the coarsest discretization, i.e., the ‘CUF - Linear 1’ and the ‘CUF - Quadratic 1’ models slightly overestimate the temperature. In contrast, the more refined numerical models lead to an accurate evaluation of the temperature state. This case study provides an initial verification and validation of the proposed CUF-based numerical framework for FFF process modeling and transient thermal analysis.

Similarly, the CUF predictions for the case of the PEKK single-wall are also in excellent agreement with experimental data, as evidenced in Fig. 8. A discrepancy is observed before the 20-second time-mark, which corresponds to the secondary re-heating peak due to the deposition of adjacent layers. It is seen from the plot that this error reduces with further refinement of model discretization. The predicted thermal history is in contrast to the numerical results provided by the original study, which deviate from the experimental curve after approximately 40 s of the simulated time. The accuracy of the CUF predictions, relative to the 2D-FE reference simulation, likely stems from the fact that the current modeling approach is fully 3D in nature and can therefore model surface heat transfer mechanisms more accurately. This is supported by investigating the thermal profile along the filament deposition length for both ABS and PEKK cases. The temperature along the length of Layer-6 for both cases has been plotted in Fig. 10, and is a snapshot of the thermal profile at the end of Layer-6 deposition. It is seen from the plot that the PEKK case experiences an initial cooling rate of 3.12 °C/mm and a spatial temperature change of approximately

Table 4

PLA material properties used in the open-box analysis [6,39].

Property	PLA
Density [kg/m <sup>3</sup> ]	1250.0
Thermal conductivity [W/m K]	0.195
Specific heat capacity [J/kg K]	1950.0
Emissivity $\epsilon$	0.78
Filament width (dY) [mm]	1.0
Filament thickness (dZ) [mm]	0.6

Table 5

FFF process parameters used in the open-box analysis [39].

Parameter	PLA
Extrusion temperature [°C]	200.0
Chamber temperature [°C]	25.0
build platform temperature [°C]	25.0
Convection coefficient [W/m <sup>2</sup> K]	8.5
Print velocity [mm/s]	5.0

105 °C, which are significantly higher than the corresponding values for the ABS case. The temperature gradients along the filament length, which are more pronounced at the higher processing temperatures of the PEKK case, could explain the relative error between the ABS and PEKK predictions by the 2D reference numerical model. The results in Fig. 7 and Fig. 8 demonstrate the capability of CUF models in modeling FFF over a wide range of processing temperatures.

### 3.2. Modeling of an open-box

This numerical assessment models the FFF processing of an open box, i.e., a box without the top and bottom faces. The structure and test setup are based on the works of Zhang et al. [39,62], which provide reference experimental and numerical data. A schematic representation of the printed structure is shown in Fig. 11. The structure is printed using polylactic acid (PLA) filaments of width 1.0 mm and height 0.6 mm. The PLA material properties, obtained from Trofimov et al. [6], are used in the present analysis and are reported in Table 4. The FFF process parameters are summarized in Table 5.

As in the previous case, a series of linear and quadratic CUF models, with an incremental refinement of the voxelized filament length (dX), has been used in the analysis. A single Lagrange sectional element of dimensions  $dY \times dZ$  is used to model the filament cross-section. The CUF model predictions of the temperature profile at point P1 (15.0, 30.0, 0.9), i.e., the center of Layer-2 in the open-box side BC (refer Fig. 11), are plotted in Fig. 12. Experimental measurements and numerical predictions from Zhang et al. [39,62] have also been compared. The temperature distribution of the structure at various

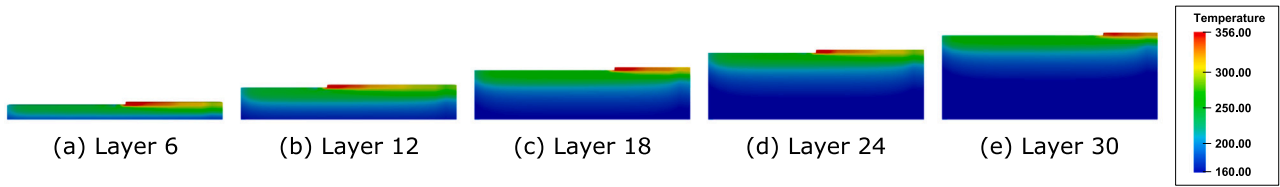


Fig. 9. Temperature distribution [°C] of the PEKK single-filament wall at various stages of print as predicted by the 'CUF - Linear 2' model (view from  $x-z$  plane, see Fig. 6).

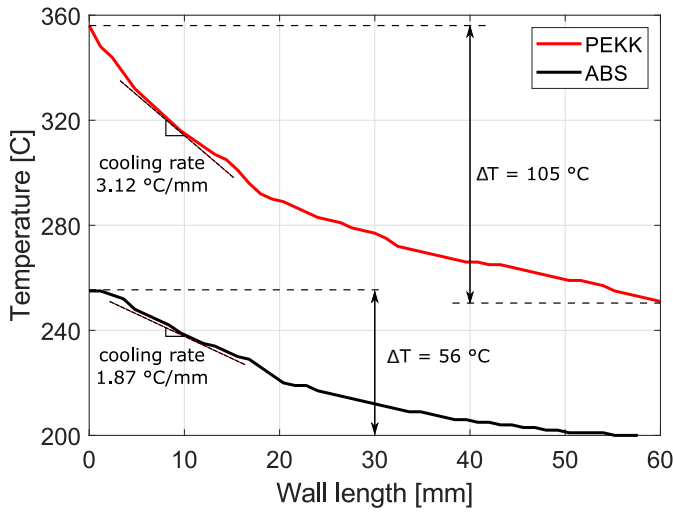


Fig. 10. CUF model prediction of the temperature along the length of Layer-6 of the single-wall, at the end of its deposition.

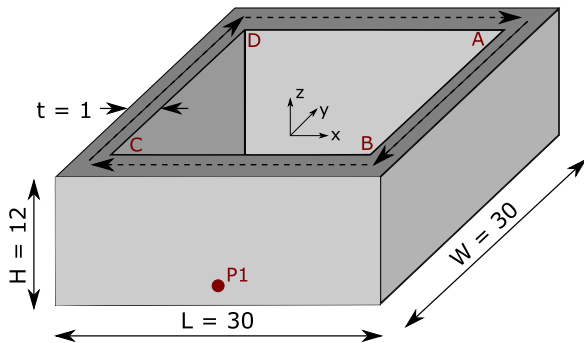


Fig. 11. Schematic representation of the open-box structure with dashed lines indicating the tool travel path (dimensions in mm).

Table 6  
Summary of CUF models used in the open-box thermal analysis.

Model	Discretization	Beam length (dX) [mm]	DOF
CUF - Linear 1	8 B2, 168 L4	4.67	1,870
CUF - Linear 2	12 B2, 252 L4	2.80	2,310
CUF - Linear 3	14 B2, 294 L4	2.33	2,530
CUF - Quadratic 1	6 B3, 126 L9	7.00	5,307
CUF - Quadratic 2	8 B3, 168 L9	4.67	7,587

stages of print is visualized in Fig. 13. A summary of the CUF models is presented in Table 6.

It is seen from Fig. 12 that all the CUF model predictions (apart from the coarsest 'CUF - Linear 1' model) are in good general agreement with the experimental reference data and perform better than the reference simulation results while capturing the secondary temperature peaks arising from subsequent layer deposition. The discrepancy between the numerical and experimental curves is attributed to the sensitivity of

Table 7

ABS/CF composite material properties used in the BAAM double-wall analysis [22].

Property	ABS/CF
Density [kg/m <sup>3</sup> ]	1140.0
Thermal conductivity [W/m K]	0.17
Specific heat capacity [J/kg K]	1640.0
Emissivity $\epsilon$	0.87
Track width (dY) [mm]	10.0
Track thickness (dZ) [mm]	4.064

Table 8

FFF process parameters used in the numerical modeling of the BAAM double-wall [22].

Parameter	ABS/CF
Extrusion temperature [°C]	200.0
Chamber temperature [°C]	18.0
build platform temperature [°C]	65.0
Convection coefficient [W/m <sup>2</sup> K]	8.5
Layer build time [s]	39.0

the temperature field to the thermal properties considered in the analysis [39]. Section 3.3 presents a further investigation of the sensitivity of the thermal analysis to variations in material properties.

### 3.3. Modeling of a composite double-wall

The last assessment investigates the capability of the proposed framework towards the modeling and thermal analysis of material extrusion AM of large-scale structures, i.e., those fabricated using BAAM processes. A wall-like structure is considered based on the works of Compton et al. [22], which also provides reference experimental data. The wall, as modeled, is two tracks wide and consists of 40 layers; the track width (dY) and height (dZ) are 10.0 mm and 4.064 mm, respectively. A schematic representation of the structure is shown in Fig. 14. The print material is ABS reinforced with 20% carbon fiber (ABS/CF), and its thermal properties, as suggested in [22], are listed in Table 7. The BAAM process parameters are summarized in Table 8.

The BAAM process simulation is performed using both linear and quadratic CUF models, as shown in Fig. 14(b) and (c), respectively. As reported in [22], no thermal gradients were experimentally observed along the length of the wall. This observation infers a the lack of sensitivity of the model results as a function of its numerical discretization along the track direction ( $dX$ ), which has been confirmed by a mesh convergence analysis not reported for the sake of brevity. As a result of the convergence study, results are presented for two types of discretization: linear (CUF - model 1, 12 elements), and quadratic (CUF - model 2, 6 elements). The thermal profile predicted by the two CUF models at the midspan of layer 1, point P1 (771.0, 20.0, 2.03); layer 15, P2 (771.0, 20.0, 58.92); and layer 30, P3 (771.0, 20.0, 119.88), have been plotted in Fig. 15. Reference experimental data from [22] and numerical simulation results based on a 2D finite volume approach [44] have also been overlaid for comparison. The temperature distribution within the double-wall cross-section, at its midspan, is visualized in Fig. 16 and demonstrates the thermal gradients which can exist across BAAM track cross-sections during the printing process of large-scale structures.

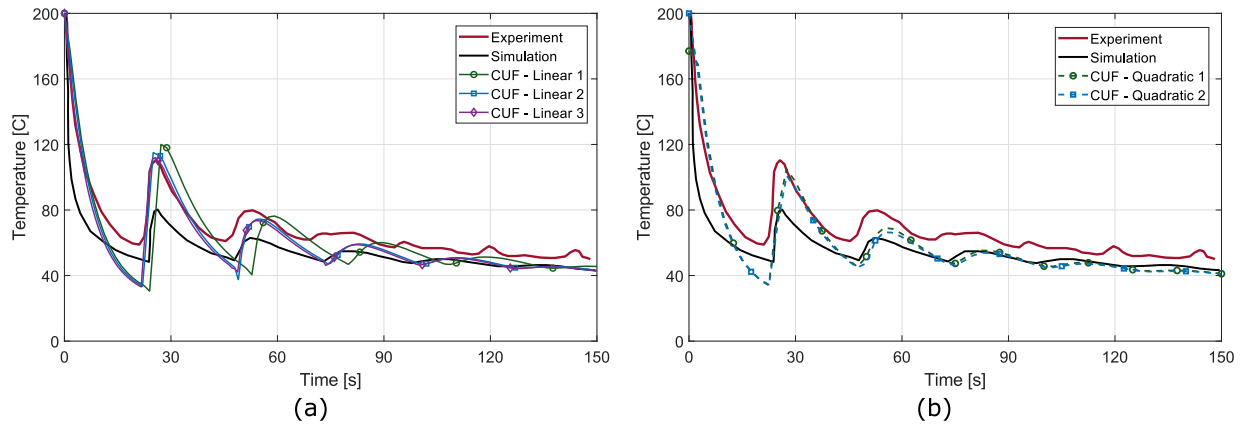


Fig. 12. Thermal profile of the PLA open-box at Point P1 (see Fig. 11) as predicted by (a) the linear CUF models, and (b) the quadratic CUF models (see Table 6 for model details). Reference experimental and numerical data based on the Finite Difference Method (FDM) obtained from Zhang et al. [39,62].

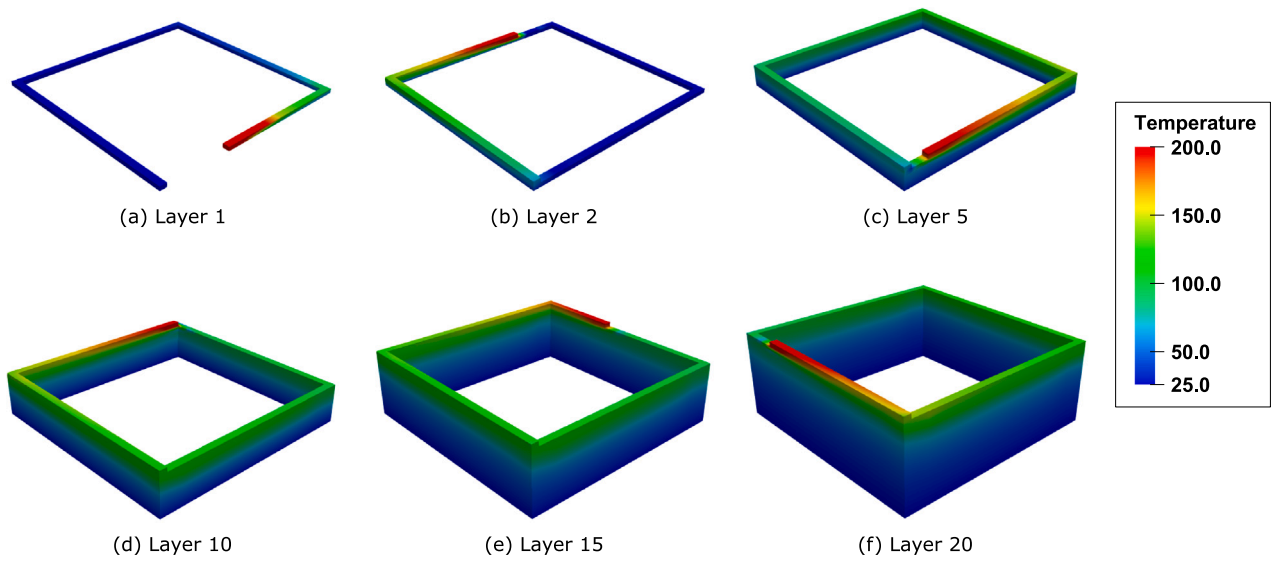


Fig. 13. Temperature distribution [°C] of the open-box at various stages of print as predicted by the 'CUF - Linear 3' model.

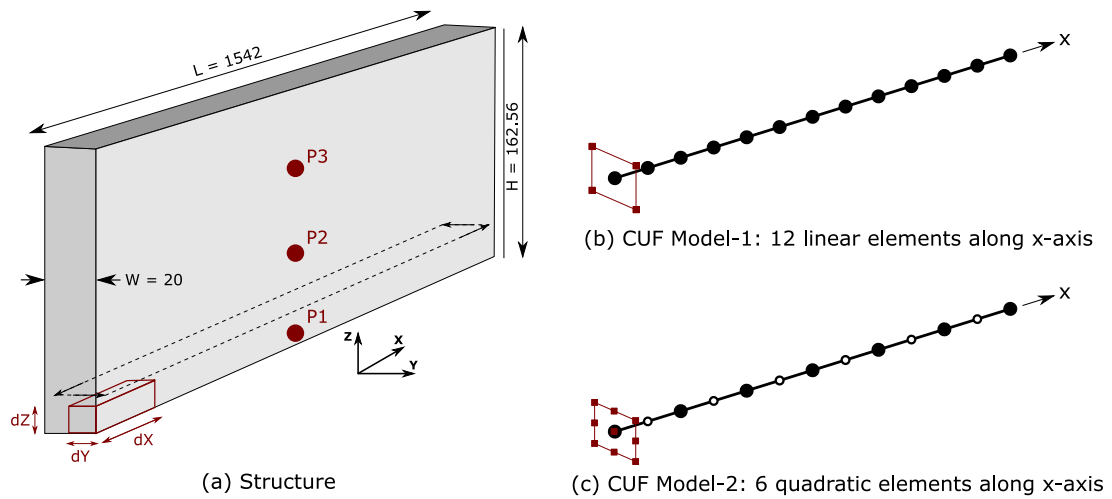


Fig. 14. Schematic representation of (a) the BAAM wall (dimensions in mm). The dashed lines indicate the tool travel path within a layer, and the highlighted  $dX \times dY \times dZ$  voxel domain represents an individual finite element, (b) the linear CUF model, and (c) the quadratic CUF model.



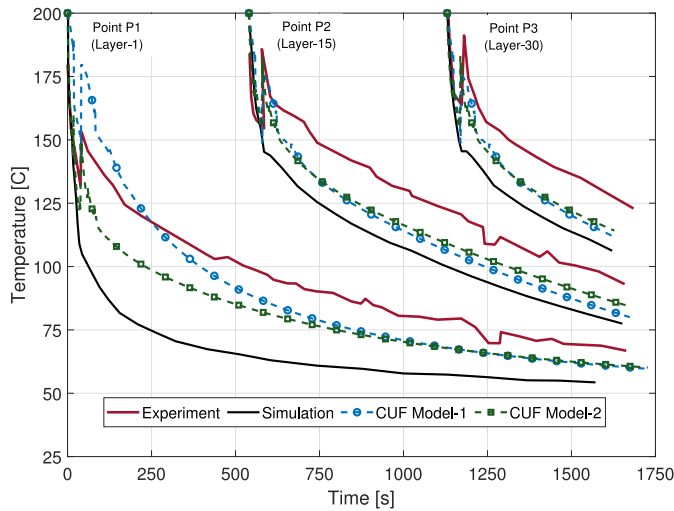


Fig. 15. Thermal profile of the ABS/CF composite double-width wall (layers 1, 15, and 30) as predicted by the CUF models. Reference experimental data obtained from Compton et al. [22], and numerical simulation results based on a 2D finite volume model from Owens et al. [44].

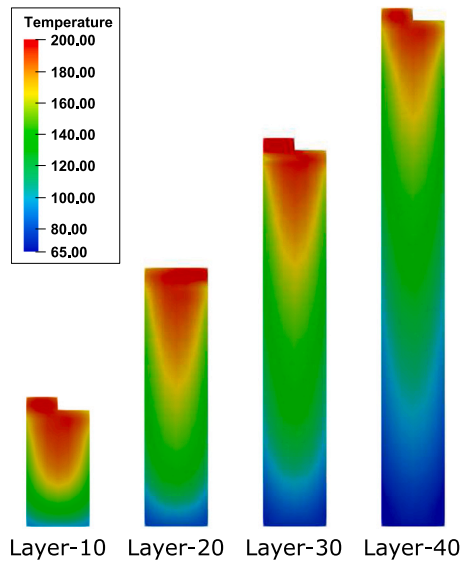


Fig. 16. Temperature distribution [°C] within the midspan cross-section of the BAAM wall at various stages of print as predicted by the (quadratic) CUF Model-2.

As seen in Fig. 15, the CUF model predictions are in qualitative agreement with the experimental curves and follow the same trend but do not correctly evaluate the temperature profile. Additionally, CUF results compare better to the experimental results than the numerical approach proposed in the original reference. The discrepancy between the experimental and numerical data likely stems from the choice of material thermal properties considered in the analysis (see Table 7, hereinafter referred to as ‘nominal’ values). Therefore, the influence of the specific heat capacity  $C_p$  and thermal conductivity  $\kappa$  – on the thermal profile of the BAAM process model has been investigated to determine the effect of the material properties on temperature prediction.

The nominal  $C_p$  value of the ABS/CF composite has been considered 1640 J/kg K in [22]. Such a value apparently neglects the presence of the reinforcement within the thermoplastic. It is seen from Table 1 that the  $C_p$  of neat ABS is about 2100 J/kg K, while that of commercially available carbon fiber is in the range 880–1100 J/kg K [63,64].

Table 9

Summary of CUF models used in the BAAM double-width wall analysis.

Model	Discretization	Beam length (dX) [mm]	DOF
CUF Model-1 (Linear)	12 B2, 82 L4	128.5	1,638
CUF Model-2 (Quadratic)	6 B3, 82 L9	257.0	5,395

Assuming a general  $C_p$  value of 900 J/kg K for CF, and applying the Rule of Mixtures, the effective  $C_p$  of 20% ABS/CF is estimated to be approximately 1860 J/kg K. The sensitivity of the thermal profile between the nominal and modified  $C_p$  values, as predicted by the CUF models at Layer-15, is plotted in Fig. 17(a). Similarly, the nominal thermal conductivity  $\kappa$  of the ABS/CF composite is 0.17 W/m K, while that of neat ABS at elevated temperatures is generally in the range 0.19–0.20 W/m K (see Table 1). Thermally conductive reinforcements such as CF generally have transverse conductivity values over 1.0 W/m K [65]. Their presence in ABS would result in a net increase in the effective thermal conductivity, even when assuming that fibers are aligned along the extruded material, and evaluating the effective composite conductivity in the transverse direction. The effective  $\kappa$  of the ABS/CF composite was therefore estimated to be approximately 0.27 W/m K following the works of Bard et al. [66]. The sensitivity of the thermal profile between the nominal and modified  $\kappa$  values, as predicted by the CUF models at Layer-15, is plotted in Fig. 17(b).

From Fig. 17(a, b), it is seen that individually modifying  $C_p$  and  $\kappa$  leads to a closer agreement between the CUF predictions and the experimental data when compared to the numerical results based on nominal composite thermal properties. However, a discrepancy in the temperature values is still observed and is likely due to the modification of only a single thermal property in each analysis. Considering the modified values of both  $C_p$  and  $\kappa$ , the CUF predictions of the thermal profile at Layer-15 are plotted in Fig. 17(c). In this case, the CUF predictions are in excellent agreement with the experimental curves and are significantly more accurate when compared to the predictions based on nominal thermal properties. It is noted that applying the modified material properties in the numerical approach of Ref. [44] would likely improve the discrepancy between their predictions and experimental data, but would not exceed the accuracy of the CUF models based on the trends seen in Fig. 15. In particular, it is observed from the figure that the quadratic CUF Model-2 is more accurate than the linear CUF Model-1. As seen in Fig. 16, the BAAM process involves extruded tracks whose cross-sectional dimensions are an order of magnitude larger than those used in FFF, and a non-negligible thermal gradient thus exists within the section. The second-order expansion function used in the quadratic CUF analysis to model the track cross-section can better capture these thermal gradients than the first-order functions used in the linear model and explains the relative performance of the two CUF models. The predicted thermal profiles at layers 1, 15, and 30, considering the modified values of  $C_p$  and  $\kappa$ , have been shown in Fig. 18. A summary of the linear and quadratic CUF models used in the BAAM analysis is presented in Table 9. The predicted results in Fig. 18 demonstrate the capability of the proposed higher-order models in accurately simulating the BAAM process and evaluating the evolving temperature field as a function of the process conditions.

A comparison of the computational cost in terms of analysis time is finally performed, to obtain an initial evaluation of the proposed framework’s performance. The reference numerical approach based on a 2D Finite Volume Method (FVM), proposed by Owen et al. [44], requires an analysis time of approximately 96 min (Supplementary Information, Table A2) to simulate the 40-layer BAAM model, on an Intel(R) Core(TM) i7-8850 laptop with 16 GB RAM. Performing the corresponding analysis with the same time-increment as the reference numerical case ( $dt = 0.1$  s), the CUF analysis requires approximately 16 min, i.e., a 6x improvement. Even though this is an indirect comparison (due to differing employed computational resources) from which limited conclusions can be drawn, the order-of-magnitude speed-up

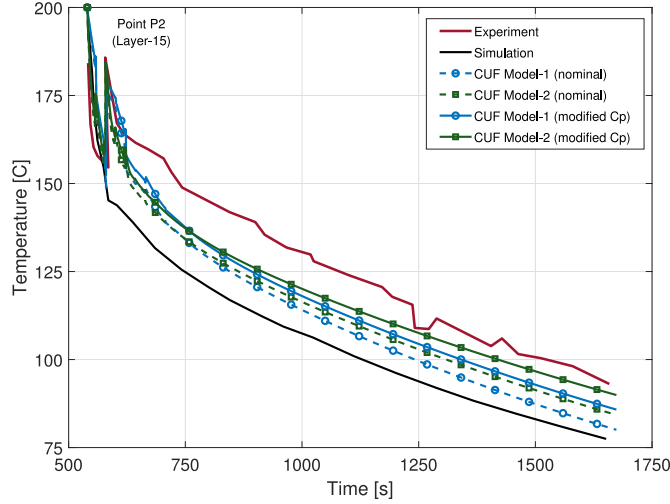
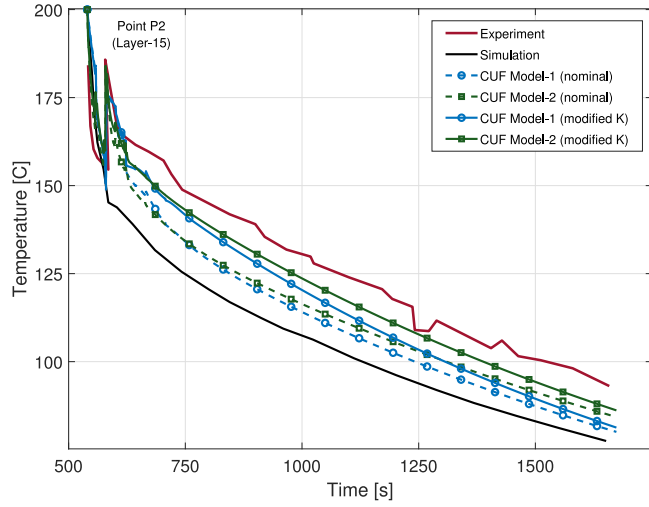
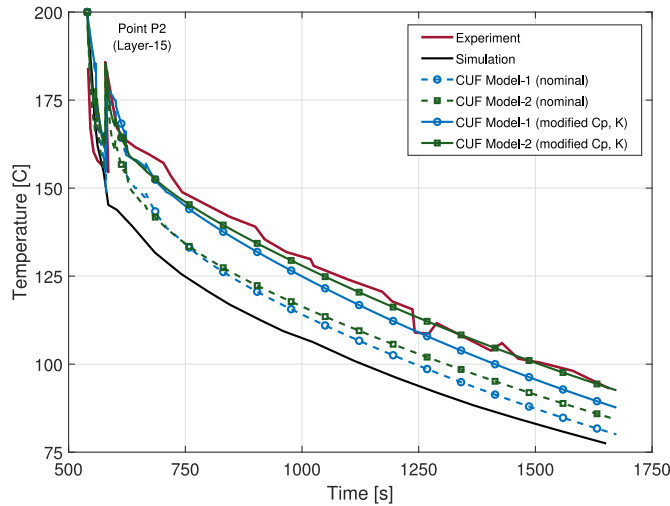
(a) Modified specific heat capacity  $C_p$ (b) Modified thermal conductivity  $\kappa$ (c) Modified  $C_p$  and  $\kappa$ 

Fig. 17. Sensitivity of numerically predicted thermal profiles to variation in thermal properties.

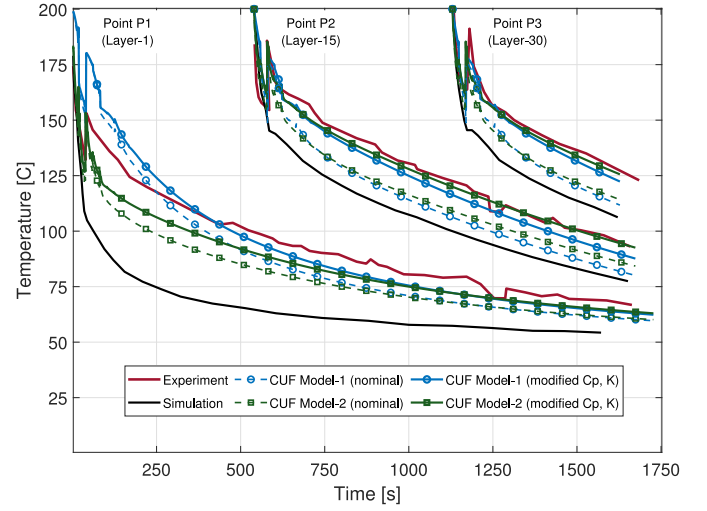


Fig. 18. Thermal profile of the ABS/CF composite double-width wall (layers 1, 15, and 30) as predicted by the CUF models considering nominal and modified thermal properties. Reference experimental data obtained from Compton et al. [22], and numerical simulation results based on a 2D finite volume model from Owens et al. [44].

exhibited by the CUF model is suggestive of its superior performance, and is consistent with previous works based on the CUF modeling approach, where a 10–20x reduction in computational size and analysis time was demonstrated when compared with traditional numerical approaches [47,49,52,67].

#### 4. Conclusion

A novel numerical framework for the process modeling of material extrusion additive manufacturing is introduced in this work. The numerical model is developed using higher-order structural theories derived from the Carrera Unified Formulation and implemented within the Finite Element Method. The element activation strategy is implemented within the higher-order FE numerical framework to model the evolution of the structure during the printing process, and a transient thermal analysis is performed to evaluate the temperature field. A series of numerical assessments was carried out to evaluate the capabilities and performance of the proposed numerical framework. Process modeling simulations of a single filament-width wall and an open-box were carried out for initial verification and validation. The obtained results were in excellent agreement with experimental data, thereby validating the framework for the process modeling of material extrusion additive manufacturing. The framework's capability in modeling Big Area Additive Manufacturing was also assessed by modeling a large-scale wall. The thermal profiles predicted by the higher-order models correlated very well with the experimental data, thus validating it for BAAM process modeling applications. A sensitivity study was also performed to investigate the influence of material thermal properties on the thermal profile of the BAAM wall. The obtained results demonstrate the capabilities of the numerical framework in accurately modeling the thermal profile evolution of material extrusion additive manufacturing processes at different structural scales using higher-order finite elements, proving the potential of the proposed approach as an optimization framework to estimate favorable process parameters. Future works include extending the framework to thermo-mechanical analysis to evaluate process-induced residual stress development and distortion in AM thermoplastic parts, as well as using multiscale techniques to investigate the relation between material microstructure and manufacturing conditions.

## CRediT authorship contribution statement

**Manish H. Nagaraj:** Writing – review & editing, Writing – original draft, Visualization, Software, Methodology, Investigation, Formal analysis, Data curation, Conceptualization. **Marianna Maiaru:** Writing – review & editing, Software, Methodology, Investigation, Project administration, Funding acquisition, Conceptualization.

## Declaration of competing interest

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: Marianna Maiaru reports financial support was provided by National Science Foundation.

## Data availability

Data will be made available on request.

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