

1                   **Enhancing Risk Assessment in Natural Gas Pipelines Using A Fuzzy-Aggregation Approach**  
2                   **Supported by Expert Elicitation**

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12                   **ABSTRACT:**

13                   Although the natural gas pipeline network is the most efficient and secure transportation mode  
14                   for natural gas, yet it is always susceptible to various external and internal risk factors. It is vital to address  
15                   the associated risk factors such as corrosion, third-party interference, natural disasters, and equipment  
16                   faults that may lead to pipeline leakage or failure. The conventional quantitative risk assessment  
17                   techniques require massive historical failure data that is sometimes unavailable or vague. Experts or  
18                   researchers in the same field can always provide insights into the latest failure assessment picture. In this  
19                   paper, fuzzy set theory is employed by getting the expert elicitation through linguistic variables to obtain  
20                   the failure probability of the Top Event (pipeline failure). By applying a combination of T- and S-Norms, the  
21                   fuzzy-aggregation approach can enable the most conservative risk failure assessment. The findings from  
22                   this study showed that internal factors, including material faults and operational errors, significantly  
23                   impact the pipeline failure integrity. Future directions should include sensitivity analyses to address the  
24                   uncertainty in data to ensure the reliability of assessment results.

25                   **Practical Applications**

26                   Natural gas pipelines are efficient and reliable transportation modes. The integrity of these valuable  
27                   assets is threatened by various risks such as corrosion, environmental factors, human errors, and

28 mechanical faults. For newly developed or less monitored pipeline networks, historical data is either  
29 unavailable or faulty. To overcome this shortcoming, experts from pipeline networks can provide  
30 invaluable insight by providing their expert opinion. This study uses the expert's elicitation by applying a  
31 fuzzy aggregation approach to predict the pipeline failure probability. The finding of this study confirmed  
32 that material faults and operational errors are the most critical risk factors leading to pipeline failure. The  
33 results of this study can be used to develop effective mitigation strategies for pipeline networks to  
34 minimize future failures.

35 **Keywords:** Failure factors, Fuzzy set theory, Cause and effect, Pipeline failure, External and internal failure  
36 factors, Corrosion

### 37 **Introduction**

38 Natural gas is one of the significant components of the energy sector that meets the requirements  
39 of power plants, industries, and residential areas (Liu & Bao, 2022). Natural gas accounts for 24 percent  
40 of world energy consumption, and pipelines are necessary for transporting and distributing it over long  
41 distances (Ding & Yu, 2005). In the United States, natural gas is transported through a highly integrated  
42 pipeline network, which serves three purposes, including collection from the source, transmission to  
43 target areas, and distribution to end users (Gharabagh et al., 2009). About 4.8 million km (3 million miles)  
44 of pipeline networks connect consumers with natural gas production and storage areas. Approximately  
45 77.7 million consumers received 781.6 billion cubic meter (27.6 trillion cubic feet) of natural gas during  
46 2021 through the natural gas transportation network (Han & Weng, 2011). Being the most secure and  
47 cost-effective means of transportation for natural gas, pipeline networks have expanded exponentially to  
48 transport enormous quantities of natural gas from production sites to end users. However, these  
49 networks also may pose a significant threat to the safety of users and the environment being exposed to  
50 several internal and external risk factors (Ding & Yu, 2005). The most well-known risk factors are leakages,

51 explosions, sabotage, environmental disasters, and health concerns (Gharabagh et al., 2009). Specifically,  
52 as the Pipeline and Hazardous Materials Safety Administration (PHMSA) reported, a pipeline rupture may  
53 result in catastrophic consequences, including injuries, deaths, revenue losses, and environmental  
54 damage. Since 2003, 660 pipeline incidents have been reported in the United States, resulting in 252  
55 fatalities and 1,081 injuries (Pahlevan et al., 2019). For public safety and environmental protection,  
56 preventing these incidents and minimizing their consequences are crucial.

57 PHMSA's pipeline incident data indicates five significant causes contributing to pipeline incidents,  
58 including corrosion, equipment failures, third-party damage, incorrect operations, and material  
59 failures(@USDOT, 2023; Tan et al., 2021). While addressing the associated risks, it is imperative to  
60 consider all possible variables that threaten the pipeline network's integrity. Mainly, risks in pipeline  
61 applications can be categorized into two main types including external factors encompassing elements  
62 like corrosion, third-party interference, and natural disasters (earthquakes, floods, lightning, and  
63 temperature variations) and internal factors that involve construction, material, design faults, and  
64 incorrect operations (Yeganeh et al., 2022).Therefore, natural gas pipeline networks need risk  
65 assessments to identify potential hazards, evaluate their impacts, and take preventative measures.

66 Term risk assessment describes how different variables, basic events (BEs), or *causes* threaten the  
67 integrity of pipelines, leading to failures commonly known as *effects*. Pipeline risk management involves  
68 evaluating the likelihood and consequences of incidents or failures in pipeline networks (Sheng et al.,  
69 2021). Many techniques for risk assessment of pipeline networks, including qualitative, quantitative, and  
70 index modeling have been explored (Han & Weng, 2011). Traditional pipeline risk assessment methods  
71 use quantitative data and deterministic models by estimating the potential consequences of an event and  
72 calculating the associated risks. Event Tree Analysis (ETA), Fault Tree Analysis (FTA) (Pahlevan et al., 2019),  
73 Hazard and Operability (HAZOP) studies (Jabbari et al., 2021), and Failure Modes and Effects Analysis  
74 (FMEA) are commonly used traditional methods . Although these methods yield valuable models and

75 provide an excellent tool for risk assessment, they have significant limitations since they cannot account  
76 for uncertainties, subjective judgments, and complex interactions between factors that impact risks (Hong  
77 et al., 2023).

78 Quantitative Risk Assessment (QRA) analyzes pipeline incidents using mathematical models and  
79 statistical data to determine their likelihood and potential consequences. QRA methods usually include  
80 Probabilistic Risk Assessment (PRA) and Monte Carlo simulation (Younesi Heravi et al., 2022). Although  
81 QRA has been widely used in pipeline safety assessments, it may not effectively account for emerging risks  
82 and uncertainties as it relies heavily on historical data. Index Modeling is yet another technique for risk  
83 assessment in which various risk factors are assigned numerical values, such as pipeline age, condition,  
84 proximity to population centers, and environmental sensitivity (Sheng et al., 2021). These factors are often  
85 combined into risk indices or scores to prioritize pipeline segments for further assessment or  
86 maintenance. Although Index Modeling can be quick and cost-effective, sometimes complex interactions  
87 may oversimplify risks (Tan et al., 2022). For instance, using soil pH and failure due to external coating as  
88 a risk indicator could underestimate risks.

89 Expert elicitation is a hybrid risk assessment technique involving gathering and integrating knowledge  
90 and expertise from subject matter experts (Zhang & Thai, 2016). This approach can be beneficial when  
91 dealing with complex systems, especially when no historical data is available, and uncertainties play a  
92 significant role in understanding and characterizing risks. It aims to assess and quantify risks associated  
93 with specific systems or processes (Salah & Moselhi, 2016). Risk assessment in pipelines often involves  
94 subjective judgments and uncertainties, such as the probability of rare events or human error. By eliciting  
95 expert opinion and insights, non-quantifiable knowledge, that cannot be quantified, is captured, and  
96 expert judgments can be represented and managed to handle inherent uncertainty (Sheng et al., 2021).  
97 Fuzzy Set Theory (FST) is a mathematical approach to evaluate and address risks based on uncertainty and  
98 imprecision. It is difficult to distinguish between low, medium, and high risks in many real-world

99 situations, and risks can have varying degrees of severity or likelihood (Younesi Heravi et al., 2022). With  
100 fuzzy logic, uncertainties can be dealt with more nuancedly. Risks are classified into multiple categories  
101 simultaneously instead of rigid categories like true or false (Moein Younesi Heravi, 2023).

102 Using the FST, risks can be represented and analyzed flexibly because the boundaries between risk  
103 levels are unclear and overlapping. Risks are multifaceted, and it is difficult to quantify or categorize them  
104 in a traditional binary fashion when associated with complex systems and decision-making processes  
105 (Salah & Moselhi, 2016). This approach facilitates a more holistic assessment of risks by considering the  
106 broader context and interdependencies of risk factors. Pipeline experts can provide detailed insights into  
107 challenges and vulnerabilities (Ren et al., 2009). Emerging risks and unique circumstances are particularly  
108 beneficial when using this approach, and input from domain experts and regular updates make expert  
109 elicitation adaptable to these changes. In addition, this can bridge the gap by combining qualitative and  
110 quantitative approaches as experts can provide qualitative insights while quantifying their judgments  
111 (Yeganeh et al., 2022).

112 Researchers have used FST for risk assessments to assess the risks associated with different variables.  
113 Using the Fuzzy Inference System, Raeihagh et al. developed a model to quantify the risks associated with  
114 sour gas pipelines, ensuring improved safety measures with applicability limited to sour gas pipelines  
115 (Raeihagh et al., 2020). Babaeian et al. proposed a semi-quantitative Risk-based inspection (RBI) by  
116 concluding that corrosion and erosion are the critical risk factors leading to the failure of gas pressure  
117 reduction station equipment for gas pipeline networks (Babaeian et al., 2023). Wen et al. proposed a  
118 hybrid machine learning model to assess the risks due to landslides by combining traditional assessment  
119 methods with machine learning. Although risks related to sour gas can be assessed using this method but  
120 risk assessment due to landslide comes in different domain and may not be applicable to most common  
121 natural gas pipeline risks (Wen et al., 2023). By combining the fuzzy technique for Order Preference by  
122 Similarities to Ideal Solution (TOPSIS) and cloud inference, Liang et al. proposed a methodology for

123 integrated risk assessment, and findings indicate polyethylene gas pipelines work effectively in urban  
124 settings. One possible limitation is that this methodology is primarily suitable for urban areas, potentially  
125 excluding consideration for pipelines made of other material types (Liang et al., 2022). Chen et al.  
126 introduced a method for classifying pipelines in high-risk regions based on failure scenarios and subjective  
127 data. They found that risk assessment in such areas is applicable when enough data is available (Chen et  
128 al., 2022). Using subtractive clustering fuzzy logic for risk assessment, Osman and Shehadeh investigated  
129 interstate pipelines. The study used hypothetical data to assess the risks associated with interstate  
130 pipelines, demonstrating its potential in pipeline risk assessment. However, it is important to note that  
131 since the modeling relied on hypothetical data, its accuracy may be limited in real life (Osman & Shehadeh,  
132 2022). Using fuzzy Analytical Hierarchy Processes (AHP), Jabbari et al. (2021) assessed the risks of fire,  
133 explosion, and toxic gas release. Through this model, safety managers received valuable data for decision-  
134 making (Jabbari et al., 2021). Based on fuzzy AHP, Ba et al. developed a corrosion risk assessment model  
135 by validating its effectiveness using a case study. The developed model used expert data only, which may  
136 introduce subjectivity (Ba et al., 2022). Zhang et al. introduced Fuzzy Bayesian networks (FBN) to assess  
137 the safety of heavy oil pipelines. The lack of data was addressed using FBN, which provided a valid model  
138 for risk assessment (Zhang et al., 2019). Pahlevan et al. analyzed the consequences of offshore pipeline  
139 failure using a fuzzy approach. Risk assessment of offshore pipelines was streamlined with a systematic  
140 approach (Pahlevan et al., 2019). Using Pythagorean fuzzy sets, Oz et al. assessed the risk of clearing and  
141 grading processes in natural gas pipeline projects by facilitating risk assessment in pipeline construction  
142 through a decision support system, but its relevance was mainly in pipeline construction (Oz et al., 2019).  
143 Yu et al. developed a fuzzy fault tree approach for assessing leakage risk in submarine pipelines but the  
144 applicability of the approach to pipelines in other setting is not known (Yu et al., 2019).

145 Due to several key benefits, FST can also be used to assess the risk of pipelines through expert  
146 elicitation. Subjective expertise can be incorporated, which is helpful when historical data is faulty or

147 unreliable, thus enhancing the accuracy of assessments (Hawari et al., 2018). Due to the complex and  
148 evolving nature of pipeline risk assessments, FST is ideally suited to coping with uncertainty and  
149 vagueness, allowing experts to define membership functions for input variables simplifies complexity and  
150 facilitates adaptability (Guo et al., 2021). Additionally, due to the interdisciplinary nature of this method,  
151 practical evaluation is ensured by bringing together experts from diverse backgrounds. Despite a lack of  
152 historical data, it provides transparent decision-making, facilitates risk communication, and can be applied  
153 even when no historical data is available. Expert elicitation with FST enables informed decision-making  
154 and proactive risk management during pipeline operations, making it a valuable tool for risk assessment  
155 (Ba et al., 2022).

156 As traditional risk assessment methods like QRA and FEMA heavily rely on quantitative data, historical  
157 records, and precise numerical values to evaluate the likelihood and consequences of different risk  
158 factors, there is a need for an alternative risk assessment methodology to bridge these gaps due to the  
159 dynamic risk factors, inherent uncertainties, and data limitations associated with natural gas pipeline  
160 networks. This paper introduces a fuzzy-aggregation-based expert elicitation approach to address this  
161 challenge by leveraging FST and expert opinions. The presented method provides a comprehensive risk  
162 assessment framework that thrives in data-scarce or data-uncertain environments. The methodology  
163 incorporates linguistic variables using membership functions and fuzzy-aggregation techniques to  
164 accommodate inherent uncertainties that quantitative data may not capture. Natural gas infrastructure  
165 will benefit from this innovative approach by improving safety, optimizing resource allocation, and guiding  
166 informed decisions. Specifically, this paper will meet the above-mentioned goal through creating a  
167 probabilistic questionnaire for expert elicitation, collecting expert opinions using the questionnaire, and  
168 applying a fuzzy-aggregation approach to quantify failure probabilities. This fuzzy-aggregation-based  
169 expert elicitation methodology is applied to assess the cause-and-effect relation leading to pipeline failure  
170 as a Top Event (TE).

171 This paper adopts the following structure. A fuzzy-aggregation approach is described in Step 2 to elicit  
172 expert opinions about the occurrence probabilities of BEs. After applying the proposed approach to  
173 Midwest region pipeline networks of the United States, next section reports the application methodology.  
174 Considering the findings, later proposed approach's applicability and results is discussed, while last section  
175 provides the conclusions.

176 **Fuzzy aggregation approach**

177 The proposed fuzzy aggregation procedure for expert elicitation is illustrated in Figure 1 to determine  
178 the likelihood of failure probabilities. It consists of three steps including the meticulous formulation of  
179 questionnaire, the systematic gathering of expert opinions, and the robust fuzzy aggregation process. The  
180 following subsections explain these steps, detailing the effectiveness of this proposed methodology.

181 **Meticulous Questionnaire Formulation**

182 **Determination of BEs**

183 The first step of a risk assessment methodology is to identify and characterize the fundamental  
184 components of risk or BEs. Based on the literature review and discussion with experts from the pipeline  
185 industry, sixteen BEs have been determined that potentially contribute to pipeline failure (Bertuccio &  
186 Moraleda, 2012; Hassan et al., 2022; Kabir et al., 2016). These BEs include transmitted material, soil pH,  
187 cathodic protection, external coating, earthquake, flood, thunder/lightning, temperature variation, third-  
188 party interference, material type, construction fault, material fault, design fault, and incorrect operation  
189 (Liu et al., 2020). Figure 2 represents the cause-and-effect relationship between the BEs and their relation  
190 to intermediate events (IEs), finally leading to pipeline failure, denoted as TE. Tier 2 and Tier 3 are the IEs  
191 getting influenced by BEs situated in Tier 3. The cumulative failure probabilities of IEs lead to pipeline  
192 failure (TE) in the risk assessment model.

193 **Development of the cause-and-effect relation**

194 After finalizing the determination of BEs, a cause-and-effect relationship needs to be established. For  
195 establishing the interactions and their influence on TE, BEs are examined, and causal relation is affirmed  
196 either directly or indirectly (Yu et al., 2023). For instance, as a direct representation of cause-and-effect  
197 relation, pipeline failure could occur due to external factors such as internal coatings, resulting in internal  
198 corrosion. It is crucial to distinguish stress corrosion cracking from typical external and internal corrosion  
199 processes. Unlike traditional forms of corrosion, stress corrosion cracking is a distinct phenomenon caused  
200 by a combination of tensile stress, susceptible material, and a corrosive environment. It often occurs in  
201 materials under mechanical stress, such as pipelines, and can lead to catastrophic failures without visible  
202 corrosion signs. Therefore, stress corrosion cracking is not categorized as external or internal corrosion.  
203 However, stress corrosion cracking can compromise the structural integrity of the pipeline, potentially  
204 creating pathways for external corrosion to occur over time due to exposure to environmental factors. So,  
205 while stress corrosion itself does not cause external corrosion, it can indirectly contribute to conditions  
206 conducive to external corrosion. To establish this indirect cause-and-effect relation, stress corrosion and  
207 cracking are not directly linked to external corrosion; rather, they are associated with external factors that  
208 ultimately result in pipeline failure.

209 Pressure reduction stations, an integral component of natural gas pipeline networks, are susceptible  
210 to failure when expansion valves, regulators, or relief devices malfunction. As part of failure analysis,  
211 equipment failure accounts for the malfunctioning of these components (Howard et al., 2011; Nasser et  
212 al., 2021; Xu et al., 2022). Corrosion and erosion are indirect factors contributing to the failure of  
213 equipment in pressure reduction stations (Babaeian et al., 2023). Degradation and failure of materials are  
214 accelerated by environmental factors such as extreme weather events, earthquakes, or soil erosion.  
215 Weather conditions such as heavy rainfall or flooding can cause pipeline components to corrode, making  
216 them more susceptible to failure. Additionally, seismic events can damage pressure reduction equipment,

217 compromising its integrity and reliability. Pressure reduction stations fail due to indirect causes such as  
218 environmental factors and equipment malfunctions (Xu et al., 2022). The indirect causal relationship  
219 between corrosion, mechanical faults, and environmental factors contributing to and leading to pressure  
220 reduction station equipment failure is shown in Figure 3.

221 **Questionnaire formulation**

222 In this step, expert opinions are gathered and a quantitative analysis is conducted on various risk  
223 factors. Unlike previous steps of risk assessment, this involves the use of a survey questionnaire designed  
224 to capture insights from domain experts in the pipeline industry. Within this questionnaire, experts employ  
225 linguistic variables, spanning from "Very Low" to "Very High," to provide nuanced responses (Jamshidi et  
226 al., 2013). For instance, external corrosion is an outcome of external failure coating due to surface  
227 exposure. In this particular question, experts are asked to provide their input based on their experience  
228 and knowledge. Another example is third-party interference, experts are asked to provide their opinion  
229 using their background knowledge to predict the pipeline failure due to external interference. To quantify  
230 fuzzy possibilities and probabilities through defuzzification, FST is applied. FST serves to systematically  
231 capture and process expert knowledge and opinions as expressed in the survey questionnaire. Ultimately,  
232 this step allows for the quantitative evaluation of the risk profile of the pipeline system.

233 **Systematic Experts' Opinions Gathering**

234 Experts' knowledge and experience are invaluable to assess the associated pipeline risks. Expert  
235 opinions are gathered and analyzed in this phase to develop a systematic analysis method. A  
236 comprehensive risk assessment of pipeline infrastructure can only be possible through analyzing these  
237 expert opinions, which are vital in quantitatively evaluating the BEs and their interconnectedness.

238 **Selection of experts**

239 The process of opinion-gathering hinges upon selecting experts who possess a deep understanding of  
240 pipeline failure, risk assessment methodologies, and related fields of natural gas pipeline operations. For

241 this study, individuals are chosen based on their practical experience and industry knowledge. A thorough  
242 selection process is employed to select a panel of experts based on their professional positions,  
243 experience, education, and age, as outlined in Table 1 (Leonardo Leoni, 2023). Although experience  
244 accounts for professional involvement with duration, age still is considered as one influencing factor as it  
245 may provide additional insight into how industry practices and technologies have changed over time and  
246 age may influence cognitive abilities, including adaptability, learning capacity, and decision-making, which  
247 affect expert judgment quality and reliability. Within the expert pool, these criteria ensure the inclusion  
248 of diverse perspectives and experiences so that accurate and credible experts influence the risk  
249 assessment decisions.

250 **Expert opinion elicitation**

251 Risk assessment techniques by obtaining expert opinions and judgments provide valuable insight,  
252 especially if historical data is limited or unavailable. Informed decisions are based on domain experts'  
253 knowledge, reducing risk by leveraging their expertise and experience. To extract valuable insights from  
254 the panel of experts, a thorough process of eliciting expert opinions was conducted. These experts were  
255 consulted and surveyed systematically, each tailored to specific aspects of the risk assessment process.  
256 Using linguistic variables such as "Very Low," "Low," "Fairly Low," "Medium," "Fairly High," "High," and  
257 "Very High," experts assess the likelihood and severity of each BE. Experts communicated risk assessments  
258 nuancedly by utilizing these linguistic variables to consider the inherent uncertainties and complexity  
259 associated with pipeline risk.

260 Iterative and collaborative approaches were used to elicit expert opinions. Using their extensive  
261 knowledge and experience, experts provided detailed explanations for their assessments. Experts differ  
262 in the depth of their knowledge, so weighing factors should be considered when determining their primary  
263 status. When evaluating an expert's status, professional characteristics, qualifications, and experience are

264 considered. This study assessed four types of weights: professional position, education, experience, and  
265 age to weigh the BEs (Shan et al., 2017). Weighing factors and scores assigned are shown in Table 1.

266 **Outlier treatment and weighing**

267 Expert opinions play a significant role in the credibility and quality of risk assessment methodologies.  
268 For accurate risk assessment, it is crucial to identify outliers before deciding whether to include or exclude  
269 them from the dataset (Nooghabi, 2019). An outlier is a data point that deviates significantly from the rest  
270 of the dataset. Outliers occur by measurement or data collection errors, unknown underlying patterns, or  
271 incorrect assumptions about data distribution (Tang et al., 2015). In risk assessment, outliers are always  
272 an issue that needs to be addressed before proceeding with data analysis. There are two main reasons for  
273 the occurrence of outliers. First, expert opinions differ significantly, especially when determining the  
274 likelihood of rare and severe events. It is imperative to recognize that one expert's assessment may be  
275 accurate while another may be completely different from the first. Secondly, being an outlier means that  
276 the questionnaire can be complex for some experts to comprehend, which can be considered an unknown  
277 factor affecting an expert's decision. Those errors can also appear as outliers if they are introduced  
278 inadvertently (Bhargavi & Sireesha, 2022). Analyzing data with outliers is always problematic because  
279 skewness always causes the data to be imbalanced resulting in unrealistic results (Zijlstra et al., 2011).

280 This study uses interquartile range (IQR) criteria to derive the most comprehensive aggregated  
281 probability by incorporating a range of viewpoints and excluding extreme values. IQR is calculated by  
282 subtracting the first quartiles from the third quartiles, and outliers are detected by adding 1.5 times the  
283 IQR to the third quartile and deducting 1.5 times the IQR from the first quartile. Any data point outside  
284 this range is considered an outlier (Jeong et al., 2017). Outliers are more likely to be excluded if using this  
285 method of outlier detection instead of only using absolute criteria, which leads to a more comprehensive  
286 and accurate analysis of the data. Aside from being more straightforward to implement, IQR criteria are  
287 also more reliable since they do not rely on a fixed threshold and consider the entire data set. Since IQR

288 criteria can be used to explain outliers and provide meaningful insights, they are also easier to interpret  
289 (Greco et al., 2023).

290 **Fuzzy aggregation approach**

291 **Fuzzy Set Theory (FST)**

292 Zadeh (1965) presented the FST as a tool for subjective judgment related to vagueness, ambiguity,  
293 and multi-criteria decision-making (MCDM) (Zadeh, 1965). The FST allows for a more nuanced and flexible  
294 representation of uncertainty in decision-making. The fuzzy numbers introduced in this approach are used  
295 to quantify and describe the uncertainty associated with imprecise values within the framework of  
296 traditional set theory. In this way, uncertain information can be represented more flexibly (Zhang et al.,  
297 2016). Fuzzy logic-based approaches handle uncertainty and imprecision in data and reasoning. This  
298 technique is helpful when there is uncertainty with traditional binary or Boolean logic, which describes  
299 only true or false states (Liang et al., 2022).

300 As part of the FST, imprecise data, subjective assessments, and linguistic terms are considered to  
301 represent and account for uncertainties and vague information. To capture uncertainties associated with  
302 pipeline risk factors, fuzzy sets can be used instead of crisp values to model membership degrees of belief.  
303 Pipeline risks can be assessed qualitatively or subjectively utilizing this method, such as corrosion rates,  
304 natural disasters and equipment faults (Yu et al., 2021). Using fuzzy sets, we can represent various levels  
305 of risk, including very low, low, medium, high, and very high. In a more advanced decision-making  
306 approach, it is possible to consider multiple pipeline risk factors (Kabir et al., 2016).

307 A fuzzy set consists of objects without well-defined boundaries that separate them. Among the  
308 members of a fuzzy set, there may be a degree of partial membership or uncertainty. A range of relevance  
309 or connection may exist between objects within a set (Kabir et al., 2016). A fuzzy number is used in the  
310 FST to represent inherent subjectivity and imprecision in expert judgment. A membership function  
311 establishes a relationship between an ambiguous quantity, such as the probability of an event or a root

312 node. Membership functions quantify a fuzzy set's relevance or membership to that set, ranging between  
313 0 and 1 with 0 being the very low and 1 very high. A fuzzy number, either regular, bound, or convex, can  
314 express the vagueness of natural language using linguistic variables. Linguistic variables are usually  
315 represented by trapezoidal fuzzy numbers (TFZs) or triangular fuzzy numbers (TpFNs) (Zarei et al., 2019).  
316 Since TpFNs and TFZs are characterized by linear membership functions, this study utilizes TpFNs since  
317 they are versatile and easy to operate, providing advantages over other membership functions.

318 **Conversion of linguistic terms to fuzzy numbers**

319 A failure probability estimate is based on expert elicitation and FST for basic root events (causes). The  
320 likelihood of the top event "pipeline failure" can be determined by analyzing the root events and  
321 determining their prior probabilities (Eleye-Datubo et al., 2008). Effective risk management strategies are  
322 expected to be developed and implemented based on this information to identify the most critical root  
323 events and their effects. Besides reducing the risk associated with the studied system, FST ensures accurate  
324 and reliable estimates. Table 2 explains the seven scale linguistic variables, their fuzzy membership values,  
325 and possible descriptions of each term.

326 As illustrated in Figure 4, TpFNs represent linguistic terms and their corresponding membership  
327 functions. These membership functions address the vagueness associated with linguistic terms by  
328 graphically representing the values associated with each set. This graphical transition between the value  
329 of zero and one helps determine a term's membership in a set by indicating whether it is a member.

330 **Fuzzy Possibilities (FPs) calculations**

331 Although there are many techniques to calculate FPs, fuzzy linear opinion pool is a simple yet effective  
332 method and is therefore used for this study. This method combines multiple experts' opinions to  
333 determine if the probability of an event or outcome can be determined by agreement or an aggregate  
334 estimate. Expert opinions are categorized using weights assigned to each source, which are aggregated to  
335 calculate the final results. It integrates opinions to arrive at an assessment and indicates the degree to

336 which an expert believes a particular outcome or event will occur (Thakur et al., 2022). Equation (1) can  
337 be used to calculate FPs:

$$338 \quad FPs = \sum_{i=1}^n W_j A_{ij}, \quad j = 1, 2, 3, \dots, m. \quad (1)$$

339 In Equation 1,  $A_{ij}$  is the linguistic value derived from expert  $j$  about event  $i$ , FPs is the fuzzy possibility  
340 representing the aggregated fuzzy value of event  $i$ , and  $W_j$  is the weighing score of expert  $j$  about event  $i$   
341 if there are  $n$  total events and  $m$  total experts. Table 1 describes the different criteria for experts and their  
342 relevant scores based on their position, education, experience, and age.

343 **Defuzzification**

344 Defuzzification is the process of transforming fuzzy sets into crisp values, creating a more efficient and  
345 effective decision-making process. This method involves converting fuzzy sets, which represent uncertain  
346 information, into crisp values that are more suitable for decision-making. Defuzzification methods include  
347 the maximum or mean-maximum method, the weighted average method, and the center of area (CoA). A  
348 standard defuzzification method is the CoA, which calculates the crisp value from a fuzzy set. Trapezoidal  
349 fuzzy numbers (TpFNs) or triangular fuzzy numbers (TFZs), Gaussian, and sigmoid membership functions  
350 can be used to represent linguistic terms (S, 2023; Zarei et al., 2019).

351 TpFZs are employed in this study to de-fuzzify and convert trapezoidal shapes into crisp values  
352 describing fuzzy set membership functions. Figure 5 illustrates the CoA method using TpZFs, which have  
353 four dimensions: the left shoulder, the rising edge, the falling edge, and the right shoulder, represented by  
354  $a_1, a_2, a_3$ , and  $a_4$ . The following equation represents the CoA defuzzification method (Sugeno & Kang,  
355 1986):

$$356 \quad X = \frac{\int \mu(x) x dx}{\int \mu(x)}. \quad (2)$$

357 In Equation 2,  $\mu(x)$  represents the aggregated membership function,  $x$  is the output variable, and  $X$   
358 represents the de-fuzzified output. For a given input variable  $x$ , the TpZFs ( $x$ ) can be defined as follows  
359 (Natarajan, 2011).

$$\begin{aligned}
 \mu(x) &= 0, & \text{For } x < a_1 \text{ or } x > a_4; \\
 \mu(x) &= \frac{(x - a_1)}{(a_2 - a_1)}, & \text{For } a_1 \leq x \leq a_2; \\
 \mu(x) &= 1, & \text{For } a_2 < x \leq a_3; \\
 \mu(x) &= \frac{(a_4 - x)}{(a_4 - a_3)}, & \text{For } a_3 < x \leq a_4.
 \end{aligned} \tag{3}$$

360 where the membership of fuzzy input variable  $x$  is represented by  $\mu(x)$  in the fuzzy set. Depending on how  
 361 strongly an input variable has been included in the fuzzy set, the degree of membership can range from 0  
 362 to 1. A value of 0 indicates impossibility, and 1 shows certainty.

363 **Calculating FPr**

364 An FPr is a way of representing probabilities that capture the uncertainty associated with the likelihood  
 365 of an event in the context of fuzzy sets or fuzzy logic. A fuzzy arithmetic operation and a fuzzy inference  
 366 technique can be used to calculate FPr (S, 2023). FPr distributions, or fuzzy numbers, are derived by  
 367 incorporating input uncertainty and propagating it to estimate the FPr distributions. In this study,  
 368 Onisawa's function was used to convert FPs into FPr (Onisawa, 1988):

$$\text{FPr} = \begin{cases} \frac{1}{10^K} \text{ if } \text{FPs} \neq 0 \\ 0 \text{ if } \text{FPs} = 0 \end{cases}, \tag{4}$$

$$\text{where, } K = \left[ \left( \frac{1 - \text{FPs}}{\text{FPs}} \right) \right]^{\frac{1}{3}} \times 2.301.$$

371 Equation (4) calculates  $K$  using the FPs value obtained from Equation (1). To introduce non-linearity,  
 372 which is desirable for certain applications, and show direct one-to-one mappings between possibility and  
 373 probability, Onisawa's function used the exponent of 1/3. Based on empirical rules for specific scaling or  
 374 normalization, a constant of 2.301 is used (ONISAWA, 1988).

375 **Fuzzy “AND” (T-Norm) and “OR” (S-Norm) operators**

376 Fuzzy “AND” (T-Norm) operators assess all conditions collectively to determine their degree of  
 377 fulfillment, calculated as the minimum of their fuzzy probabilities by considering all conditions together.

378 This approach quantifies the contribution of each condition or factor to risk assessment. For instance,  
379 applying the fuzzy “AND” operator, the minimum (MIN) of these fuzzy probabilities for BEs corrosion,  
380 maintenance quality, and environmental conditions is considered. The risk associated with this minimum  
381 operation reflects the contribution of all three BEs’ conditions. Conversely, the fuzzy “OR” (S-Norm)  
382 operators determine the extent to which at least one condition has been met by calculating the maximum  
383 of the BEs’ fuzzy probabilities. Unlike the fuzzy “AND” operator, the maximum of the fuzzy probabilities is  
384 taken as a result of each condition when applying the fuzzy “OR” operator. These two operators enable  
385 handling complex, uncertain, data and reasoning by accommodating degrees of truth and membership  
386 (Shi et al., 2014).

387 “AND” operators promote conservative decision-making by requiring both conditions to be true for  
388 the overall condition to be considered, and the result becomes more confident, decreasing the likelihood  
389 of making risky choices. However, when a more lenient approach is permitted, the “AND” operator may  
390 lead to excessively pessimistic decisions, reducing the possibility of positive outcomes or missing out on  
391 opportunities. The “OR” operator allows for inclusiveness and adaptability in decision-making by allowing  
392 either condition to be true and providing additional decision-making flexibility. It is suitable where strict  
393 criteria are not necessary, and adopting a more accommodating approach can be advantageous. Although  
394 the use of these operators is at the discretion of the decision-makers, however, using these operators  
395 requires a thorough understanding of the problem because “AND” is more conservative and cautious,  
396 while “OR” is more flexible and tolerant (Gupta & Qi, 1991).

397 **Application of Fuzzy-aggregation approach using PHMSA data and domain expert elicitation in  
398 the Midwest USA**

399 To validate the developed fuzzy-aggregation approach for assessing the risk involved in pipeline  
400 networks, this study analyzed the natural gas pipeline risk in Midwest USA using PHMSA historical  
401 database from 2010 to 2022. The historical data was employed to calculate CPr. While, to calculate the

402 FPr, domain experts from the Midwest region were also elicited in the data analysis process to supplement  
403 the factors for which historical data is scarce (Database, 2023). A sole focus of this study is the elicitation  
404 of expert data to evaluate the proposed model and description of CPr is to compare the effectiveness of  
405 the approach.

406 **Calculation of expert's weighing score**

407 Each variable received in linguistic terms was added to the total weight using Equation (2), and  
408 weighing values were calculated using Equation (3). Expert elicitation received from experts showing their  
409 professional position, experience, education, age, and weighing score and value are shown in Table 3.

410 **Calculation of CPr and FPr**

411 A CPr reflects the likelihood of an event or outcome based on historical data. Each risk factor is  
412 considered individually and its corresponding CPr is calculated. Dataset from PHMSA contains information  
413 about pipeline incidents, failure modes, and contributing factors (Database, 2023). The dataset was  
414 carefully reviewed and preprocessed before analysis to ensure data quality and integrity. In this process,  
415 the data was cleaned, missing values were addressed, and the consistency of variables was verified. Table  
416 4 shows the CPr calculated from the historical data for the Midwest region and based on the pre-  
417 processed dataset, CPr is calculated for pipeline network risk factors and failure modes.

418 To calculate the FPr through expert elicitation, a survey questionnaire was formulated using Qualtrics  
419 based on variables explained in Section 2.3.1. and submitted for formal approval by the Institutional  
420 Review Board (IRB). After the IRB approval, the survey questionnaire was sent to fifty experts in the field  
421 and academia with expertise and experience in pipeline networks. The experts were selected based on  
422 their cutting edge research reports submitted to the PHMSA for the last five years, 2018-2023 (Database,  
423 2023).

424 A few reminders later, fifteen responses were received, but after reviewing, it was realized that they  
425 needed to be sorted according to their completeness. Outliers were identified using the IQR technique to

426 make the responses fit for analysis. Five responses were declared outliers due to inconsistent points  
427 outside the  $\sigma \pm 1$ . Therefore, only ten complete responses from the Midwest region have been considered  
428 for conducting for calculation of FPr. As these responses come from experts from industry and academia  
429 with different backgrounds and areas of specialization, they cover various aspects of the problem.

430 A significant difference exists between crisp failure probabilities derived from PHMSA data and  
431 corresponding FPr derived from expert elicitation, as shown in Table 5. Uncertainty introduces  
432 considerable ambiguity in risk analysis, and lack of failure probability data, inherent ambiguity, and  
433 imprecise information lead to underestimating or overestimating risks. (Zarei et al., 2019). Secondly,  
434 enhanced safety measures at gas facilities play a crucial role, and due to technological advances,  
435 preventive measures, and other factors, recent years have seen substantial improvement in safety levels.  
436 (Ramzali et al., 2015). As a result, databases such as PHMSA often present failure data that remains static  
437 over time and fails to adequately represent recent advancements in component reliability. Consequently,  
438 fuzzy failure probabilities are anticipated to yield results more reflective of the nuanced and evolving  
439 safety environment, in contrast to the reliance on rigidly crisp probabilities. Figure 6 explains the  
440 comparison of FPr calculated through expert elicitation for sixteen BEs.

441 **Employment of Fuzzy-logic Operators**

442 Before employing T-Norms (fuzzy “AND” operators) or S-Norms (fuzzy “OR” operators), logical  
443 relationships are considered to decide the use of sixteen BEs. The T-Norm is used in strict conjunction  
444 when all conditions must be met simultaneously for an event to occur. For instance, failure due to  
445 transmitted material will cause failure of internal coating and eventually lead to internal corrosion. On the  
446 contrary, S-Norm is used as a permissive conjunction when at least one associated condition is satisfied  
447 e.g., soil pH, failure due to cathodic protection, and failure of external coating, if any of the conditions is  
448 met, it will lead to external corrosion. (Singh et al., 2022). Based on the same rules, Table 6 shows the

449 application of both operators for the fuzzy-aggregation approach. When the T-Norm is used, it will ensure  
450 the conservative approach by taking the minimum value out of two failure probabilities.

451 Figure 7 describes the graphical representation of the fuzzy logic operator for risk assessment  
452 probability for TE. For BE1 and 2, T-Norm is used by assuming that transmitted material and failure of  
453 internal coating are expected to happen simultaneously or that transmitted material is the root cause for  
454 the occurrence of internal corrosion. External corrosion may occur due to poor soil conditions or external  
455 coating failure, suggesting employing S-Norm. For natural disasters, T-Norm is used because typically  
456 inclement weather, lightning/ thunder, and flood happen simultaneously, leading to natural disasters.  
457 Different faults are independent, suggesting using S-Norm leading to IE faults. To ensure risk is  
458 represented conservatively and realistically, the T-Norm is used for external factors probability  
459 determination. For IEs, internal corrosion, external corrosion, soil pH, stress corrosion cracking, natural  
460 disasters, and third-party interference, all critical conditions must be met simultaneously for the event to  
461 be deemed probable. S-Norm allows for a more realistic representation of "Internal Factors" probabilities  
462 by aligning with the logic that any critical condition can independently lead to the top event. Finally, as  
463 part of the risk assessment process, T-Norm calculates the probability of pipeline failure since it captures  
464 the logic that for the TE to occur, a combination of external and internal factors must occur simultaneously.

465 **Results and discussion**

466 In this study, the pipeline risk assessment model, a fuzzy-aggregation approach, is employed to  
467 calculate the risk probability of pipeline failure as TE. The model integrates sixteen BEs into four IEs, i.e.,  
468 internal corrosion, external corrosion, natural disaster, and faults in the first step. BE 1 and 2 yielded a  
469 failure probability of 0.005 for internal corrosion using T-Norm. BE 3,4 and 5 resulted in a failure score of  
470 0.0132 for external corrosion using S-Norm. The output for IE 3 (Natural disaster), using BE 6,7,8 and 9, is  
471 0.0011 using T-Norm. For IE 4, we used S-Norm for BE 12, 13, and 14, which yielded a failure probability  
472 of 0.0098. IEs calculation depicts the membership values for "External Factors" and "Internal Factors,"

473 which encompass events related to external risks such as corrosion, third-party interference, and natural  
474 disasters. The calculated membership value for "External Factors" is 0.0011, indicating a low but non-  
475 negligible likelihood of external factors collectively leading to pipeline failure. Internal factors represent  
476 internal risks like material faults and operational errors. The calculated membership value for "Internal  
477 Factors" is 0.0098, signifying a higher likelihood of internal risk factors contributing to pipeline failure.  
478 Higher probability explains that risks contributing to human error or design faults are more significant than  
479 external factors and require deliberate attention to reduce the risk of TE occurrence. Table 7 describes the  
480 calculation for TE occurrence. TE results explain the final risk probability for Pipeline Failure. Applying the  
481 AND operator to the membership values of "External Factors" and "Internal Factors," a failure probability  
482 value of 0.0011 is calculated. This value represents the likelihood of external and internal risk factors  
483 coinciding with a pipeline failure event.

484 Interpreting these results is crucial in understanding the overall risk assessment and its implications.  
485 The nearly identical membership values for "External Factors" and "Internal Factors" (0.0011 and 0.0098,  
486 respectively) indicate that both external and internal factors play a crucial role in pipeline failure. This  
487 balanced contribution suggests that risk mitigation efforts should consider internal and external factors.  
488 T-Norm or "AND" tends to be more conservative because it takes the minimum value, assuming  
489 the smallest possibility or the most pessimistic estimate. It focuses on the lower bounds of  
490 confidence and is associated with a safer, more cautious approach. On the contrary, S-Norm or  
491 "OR" tends to be less conservative because it takes the maximum value, assuming the largest  
492 possibility or the most optimistic estimate. It's risk-acceptant and may be perceived as less  
493 cautious or safe. The higher membership value for "Internal Factors" implies that internal risks, such as  
494 material faults and operational errors, may significantly impact pipeline failure. This sensitivity  
495 underscores the importance of rigorous quality control, maintenance, and operating procedures. The  
496 lower membership value for "External Factors" suggests that while external risks like corrosion and natural

497 disasters are significant, the pipeline may have some resilience against them. Protective measures such  
498 as coatings and monitoring systems effectively reduce the likelihood of external factors leading to failure.  
499 Based on these results, risk mitigation strategies should focus on maintaining the integrity of internal  
500 factors, reducing the impact of external factors, and ensuring a comprehensive risk management plan that  
501 addresses both types of risks.

502 A fuzzy-aggregation approach using fuzzy logic operators offers several advantages over traditional  
503 binary methods for assessing natural gas pipeline risk. Fuzzy logic captures the interaction between risk  
504 factors and models their dependencies, which is ideal for assessing pipeline failure risks. This approach  
505 avoids the potential pitfalls of overestimation and underestimation that binary methods can face due to  
506 their balanced consideration of internal and external risk factors. The conservative estimation approach  
507 ensures a realistic and cautious risk assessment by combining T-Norms (AND operators) with S-Norms (OR  
508 operators). Consequently, the method avoids risk exaggeration while accommodating subtle shifts in risk  
509 conditions, thereby offering a balanced assessment that is both reliable and accurate.

510 This balanced assessment informs practical maintenance and design decisions for pipeline networks.  
511 The calculated probabilities derived from this approach offer valuable insights into maintenance  
512 prioritization and design enhancements. Prioritizing maintenance activities based on calculated  
513 probabilities allows for optimal resource allocation, reducing the likelihood of unplanned downtime or  
514 incidents. Moreover, insights from these probabilities inform the design and construction of new pipeline  
515 infrastructure or the retrofitting of existing systems. Design enhancements may include redundant safety  
516 features, optimized material selection, or advanced monitoring systems, all aimed at mitigating identified  
517 risks. By leveraging the calculated probabilities from the fuzzy-aggregation approach, pipeline operators  
518 can proactively manage risks, allocate resources efficiently, and enhance the overall safety and reliability  
519 of pipeline networks.

520 The results of this fuzzy-aggregation approach analysis provided valuable insight into data refinement  
521 efforts and can be used to identify the key factors contributing to uncertainty. Acknowledging the  
522 variability of calculated probabilities over time and as the pipeline degrades, it is recognized that these  
523 probabilities are not fixed values and can dynamically change based on evolving pipeline conditions.  
524 Pressure reduction stations are a crucial part of the natural gas pipeline system and are  
525 vulnerable to failure due to faulty expansion valves, regulators, and relief devices. The analysis  
526 incorporates equipment failure and environmental factors to assess malfunction risk.  
527 Environmental factors can exacerbate equipment degradation, increasing its susceptibility to  
528 failure. Corrosion of pipeline components, particularly in severe weather conditions, further  
529 heightens the risk. Additionally, seismic events threaten pressure reduction equipment's  
530 integrity and reliability. The failure probability of 0.6% arising from third-party interference endorsed  
531 the implementation of ASME B31.8 by designing a higher-class location which will reduce the risk of  
532 leakage or rupture by minimizing the corrosion or overpressure to a considerable limit. Observation of  
533 ASME B31.8 helps to reduce the risk of leaks, ruptures, and other failures by enhancing public safety and  
534 environmental protection. Adherence to these standards is also crucial for the safe and reliable operation  
535 of natural gas pipeline networks by promoting industry best practices and regulatory compliance.

536 Cost-benefit analysis is crucial for pipeline risk assessment models as it helps quantify the economic  
537 implications of safety measures versus potential risks. This also helps decision-makers identify optimal  
538 strategies to mitigate risks while maximizing cost-effectiveness and ensuring resource allocation aligns  
539 with safety priorities. There is a notable absence of a cost-and-benefit analysis within the research which  
540 is attributed to the lack of data from the PHMSA database, which hindered the authors' ability to conduct  
541 such an analysis.

542 **Conclusions and Future Work**

543 In this paper, a practical approach to modeling pipeline risk assessment complexity and uncertainty  
544 has been developed by combining fuzzy aggregation with expert elicitation. Using qualitative methods,  
545 such as probability factors, pipeline risks are assessed more nuancedly than binary methods, which only  
546 determine success or failure. Further contributions from this study are summarized as follows:

547 • The results indicate that both internal and external risk factors influence pipeline failures. Internal  
548 factors, such as material faults and operational errors, cause more pipeline failures due to human  
549 errors and manufacturing faults.

550 • By analyzing internal factors, it is evident that material faults and operational errors are the most  
551 critical factors leading to pipeline failures. The findings of this study show that it is imperative to  
552 address the risks associated with external risk factors such as corrosion, third-party interference, and  
553 natural disasters.

554 • This study shows that qualitative methods provide a better understanding of pipeline risks and  
555 facilitate decision-making. With crucial insights into natural gas pipeline risk profiles, the  
556 investigation will significantly improve pipeline safety and reliability.

557 • In addition to promoting the development and maintenance of natural gas pipelines, the model can  
558 provide a base for research on mitigating pipeline risks and informing policymakers about potential  
559 risks.

560 • The proposed framework can assess potential risks associated with soil characteristics,  
561 environmental factors, and material faults. Further, it can evaluate the effectiveness of various  
562 mitigation measures, such as leak detection and corrosion control, by highlighting the corrosion risks  
563 by pipeline operators in the form of expert elicitation.

564 There is potential for improvements in several areas in this field, such as conducting sensitivity  
565 analyses to address the concerns about uncertainty in data to ensure the reliability of assessment results,

566 and including more diverse expert views considering gender and ethnic diversity, etc. Efforts can be made  
567 to minimize the inaccuracies in the input data by enhancing the data collection and monitoring process.  
568 Developing novel methods to account for dependencies is possible, providing a more precise  
569 representation of complex systems. Further validation with empirical data is necessary to ensure the  
570 model's practical applicability. Furthermore, refinement techniques can make the quantification process  
571 more robust and consistent. Conducting targeted studies and risk assessments by including pressure  
572 reduction stations can help fill the knowledge gaps and inform decision-making processes aimed at  
573 enhancing safety and reliability. To ensure public safety and promote environmental sustainability and  
574 efficiency in natural gas transportation, future studies should incorporate the guidelines and requirements  
575 outlined in ASME B31.8. Future works may also include the cost-benefit analysis for these invaluable assets  
576 to facilitate the decision-makers for the best implementation of these risk assessment models.

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582 **Data Availability Statement**

583 The data, models, or code that support the findings of this study are available from the corresponding  
584 author upon reasonable request.

585 The following symbols are used in this paper:  $\Sigma$ : summation;  $\int$ : Integral;  $<$ : Less than;  $>$ : greater than.

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773

774 **Tables**

775 **Table 1.** Weighing scores are given to experts based on their characteristics.

Criterion	Description	Score	Criterion	Description	Score
Professional Position	Sr./Jr. academic	5	Experience	<5	2
	Engineer	4		5-9	2
	Technician	3		10-19	3
	Operator	3		20-30	4
	Other	2		>30	5
Education	Ph.D.	5	Age	<30	2
	Masters	4		30-39	3
	Bachelor	3		40-50	4
	Social degree	3		>50	5
	High school	2			
	Other	2			

776

777 **Table 2.** Explanation of linguistic variables and membership function with possible description (Guo et  
 778 al., 2021).

Linguistic variables	Fuzzy membership function					Description
Very Low (VL)	0	0	0.1	0.2		Indicates an extremely low level of risk that the likelihood of an adverse event or the severity of its consequences is extremely unlikely or negligible.
Low (L)	0.1	0.2	0.2	0.3		Signifies a relatively low level of risk that the likelihood of an adverse event or the severity of its consequences is low but not as negligible as in the case of "very low."
Fairly Low (FL)	0.2	0.3	0.4	0.5		A moderately low level of risk means that the likelihood of an adverse event or the severity of its consequences is somewhat higher than "low" but remains at a reasonably manageable level.
Medium (M)	0.4	0.5	0.5	0.6		A moderate level of risk means that the likelihood of an adverse event or the severity of its consequences is neither too high nor too low, falling within an average range.
Fairly High (FH)	0.5	0.6	0.7	0.8		A moderately high level of risk means that the likelihood of an adverse event or the severity of its consequences is somewhat higher than "medium" but still manageable.
High (H)	0.7	0.8	0.8	0.9		A significant level of risk means that the likelihood of an adverse event or the severity of its consequences is considerably higher, demanding increased attention and comprehensive risk management strategies.
Very High (VH)	0.8	0.9	1	1		An extremely high level of risk means that the likelihood of an adverse event or the severity of its consequences is significantly elevated, requiring immediate action and extensive risk mitigation efforts.

**Table 3.** Expert's details and corresponding weight for the Midwest region.

Expert	Professional Position	Education Level	Experience	Age (Years)	Weighing Score	Weighing value
E1	5	5	2	3	15	0.0904
E2	5	5	2	5	17	0.1024
E3	4	5	4	4	17	0.1024
E4	4	5	5	5	19	0.1145
E5	5	5	3	3	16	0.0964
E6	5	5	2	3	15	0.0904
E7	5	5	3	4	17	0.1024
E8	5	5	3	4	17	0.1024
E9	5	5	3	3	16	0.0964
E10	4	3	5	5	17	0.1024

**Table 4.** CPr based on PHMSA historical data for the Midwest region.

Attribute	Basic Event	Frequency	CPr (%)
Internal corrosion	Failure due to transmitted material (BE 1)		
	Failure of internal coating (BE 2)	1	0.3
	Soil pH (BE 3)		
External corrosion	Failure of cathodic protection (BE 4)		
	Failure of external coating (BE 5)	17	4.8
	Failure due to earthquake (BE 6)		No data
Natural Disaster	Flood (BE 7)	10	2.8
	Thunder/ lightning (BE 8)	14	4
	Temperature variation (BE 9)	9	2.6
Third-party interference	third-party interference (BE 10)	117	33.3
Stress corrosion cracking	Stress corrosion cracking (BE 11)		No data
	Construction fault (BE 12)	21	6
	Material fault (BE 13)	20	5.7
Faults	Design fault (BE 14)		No data
	Incorrect operation (BE 15)		No data
	Material type (BE 16)		No data

**Table 5.** Calculations of FPs and FPr for BEs.

BEs	Fuzzy aggregation number				K- Value	FPs	FPr (%)
BE1	0.37	0.46	0.565	0.68	2.24	0.5188	0.57
BE2	0.28	0.42	0.585	0.71	2.30	0.4988	0.5
BE3	0.36	0.505	0.685	0.82	2.03	0.5925	0.93
BE4	0.44	0.545	0.66	0.77	2.00	0.6038	1
BE5	0.42	0.57	0.74	0.86	1.88	0.6475	1.32
BE6	0.12	0.2	0.31	0.44	3.22	0.2675	0.14
BE7	0.22	0.33	0.45	0.56	2.67	0.3900	0.14
BE8	0.12	0.18	0.28	0.42	3.32	0.2500	0.11
BE9	0.28	0.4	0.535	0.65	2.41	0.4663	0.24
BE10	0.44	0.565	0.69	0.79	1.95	0.6213	0.6
BE11	0.28	0.4	0.555	0.69	2.36	0.4813	0.53
BE12	0.37	0.54	0.725	0.84	1.96	0.6188	0.32
BE13	0.31	0.43	0.55	0.65	2.35	0.4850	0.28
BE14	0.33	0.515	0.705	0.81	2.04	0.5900	0.65
BE15	0.42	0.57	0.735	0.85	1.89	0.6438	0.98
BE16	0.19	0.355	0.53	0.64	2.53	0.4288	0.45

786 **Table 6.** Application of fuzzy-logic operators.

Level	T-Norms (fuzzy "AND" operator)	S-Norms (fuzzy "OR" operator)
	<ul style="list-style-type: none"> <li>• Failure due to transmitted material</li> <li>• Failure of internal coating</li> </ul>	<ul style="list-style-type: none"> <li>• Soil pH</li> <li>• Failure of cathodic protection</li> <li>• Failure of external coating</li> </ul>
Third tier (BEs)	<ul style="list-style-type: none"> <li>• Failure due to earthquake</li> <li>• Flood</li> <li>• Thunder/ lightning</li> <li>• Temperature variation</li> </ul>	<ul style="list-style-type: none"> <li>• Construction fault</li> <li>• Material fault</li> <li>• Design fault</li> </ul>
Second tier (IEs)	<ul style="list-style-type: none"> <li>• Internal corrosion</li> <li>• External corrosion</li> <li>• Soil pH</li> <li>• Stress corrosion cracking</li> <li>• Natural disaster</li> <li>• Third-party interference</li> </ul>	<ul style="list-style-type: none"> <li>• Material type</li> <li>• Faults</li> <li>• Incorrect operation</li> </ul>
Top Event (Pipeline failure)	<ul style="list-style-type: none"> <li>• External factors</li> <li>• Internal factors</li> </ul>	

788 **Table 7.** Calculation of failure probability for TE.

BEs	IEs	IEs	TE
BE1	IE 1=		
	BE1 $\cap$ BE2 = MIN [ $\mu$ (0.0057), $\mu$ (0.0050)] =		
BE2	0.0050		
BE3	IE 2=		
BE4	BE3 $\cup$ BE4 $\cup$ BE5 = MAX [ $\mu$ (0.0093), $\mu$	IE 5=	
BE5	(0.0100), $\mu$ (0.0132)] = 0.0132	IE1 $\cap$ IE2 $\cap$ BE10 $\cap$ IE 3	
BE6	BE6	$\cap$ BE11 = MIN [ $\mu$	
BE7		(0.0050), $\mu$ (0.0060), $\mu$	
BE8	IE 3=	(0.0132), $\mu$ (0.0053), $\mu$	TE=
BE9	BE6 $\cap$ BE7 $\cap$ BE8 $\cap$ BE9 = MIN [ $\mu$ (0.0014), $\mu$	(0.0011)] = 0.0011	IE5 $\cap$ IE6 = MIN
BE10	(0.0014), $\mu$ (0.0011), $\mu$ (0.0024)] = 0.0011		(0.0098, 0.0011) =
BE11	BE11		0.0011
BE12	BE12		
BE13	IE 4=	IE 6=	
BE14	BE12 $\cup$ BE13 $\cup$ BE14 = MAX [ $\mu$ (0.0032), $\mu$	BE15 $\cup$ IE4 $\cup$ BE16 = MAX	
BE15	(0.0028), $\mu$ (0.0065)] = 0.0065	[ $\mu$ (0.0098), $\mu$ (0.0065),	
BE16	BE16	$\mu$ (0.0045)] = 0.0098	

790 **List of figure captions**

791 **Figure 1.** Fuzzy aggregation technique to determine the probability of failure incidents.

792 **Figure 2.** Cause-and-effect variables leading to natural gas pipeline failure are represented in three tiers.

793 **Figure 3.** Indirect causal relation of risk factor responsible for pressure reduction station failure.

794 **Figure 4.** Linguistic terms with corresponding fuzzy membership functions.

795 **Figure 5.** Trapezoidal fuzzy number  $A^{\sim}$ .

796 **Figure 6.** Comparison of FPr using expert elicitation.

797 **Figure 7.** Graphical representation of fuzzy logic operator.